

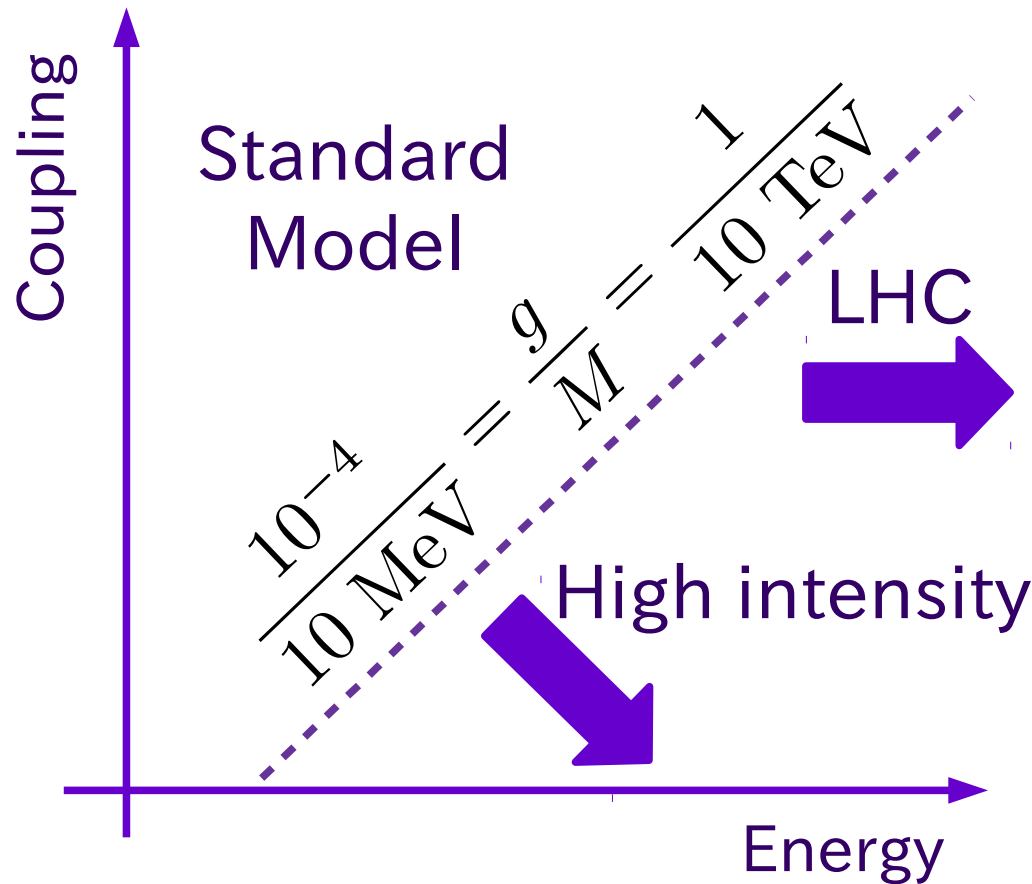
# Probing new intra-atomic force with isotope shifts

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Based on 1710.11443  
with K. Mikami & M. Tanaka (Osaka U)

# Physics of light new boson



## Real production



Stellar cooling, dark matter, thermal history, Higgs decay, flavor physics, etc.

◆ The light bosons may appear in many observations.

◆ Atomic spectroscopy with an extreme precision.

😊 Error of the atomic clocks  $O(10^{-15}-10^{-18})$ .

$^{87}\text{Sr}$  : 429 228 004 229 873.4 Hz

(From Wikipedia:atomic clock)

c.f.) the electron  $g-2$  is  $O(10^{-10})$ .

$$\frac{g_e - 2}{2} = \begin{cases} -0.001\,159\,652\,180\,73(28)_{\text{EX}} \\ -0.001\,159\,652\,181\,64(76)_{\text{TH}} \end{cases}$$

😞 The calculation of the spectrum is too difficult.

▶ How to reduce the uncertainty.

▶ The new constraints on **the light new boson**.

# Plan

- ◆ Introduction
- ◆ The linearity and its violation
- ◆ The field shift and its higher order
- ◆ The particle shift
- ◆ The constraint of a light new boson
- ◆ Conclusion

# Isotope shift and the linearity

3

- ◆ Isotope shifts follow a linearity.

$$\delta H_{A'A} = \delta K_{A'A} + \delta V_{A'A}$$

$$\delta \nu = G \delta \mu + F \delta \langle r^2 \rangle$$

▼ Isotope dependence.

↙ ↘ Wave function dependence.

- ▶ Linearity for isotope pairs. 1963: W. H. King

$$\frac{\delta \nu_2}{\delta \mu} = \frac{F_2}{F_1} \frac{\delta \nu_1}{\delta \mu} + \left( G_2 - \frac{F_2}{F_1} G_1 \right)$$

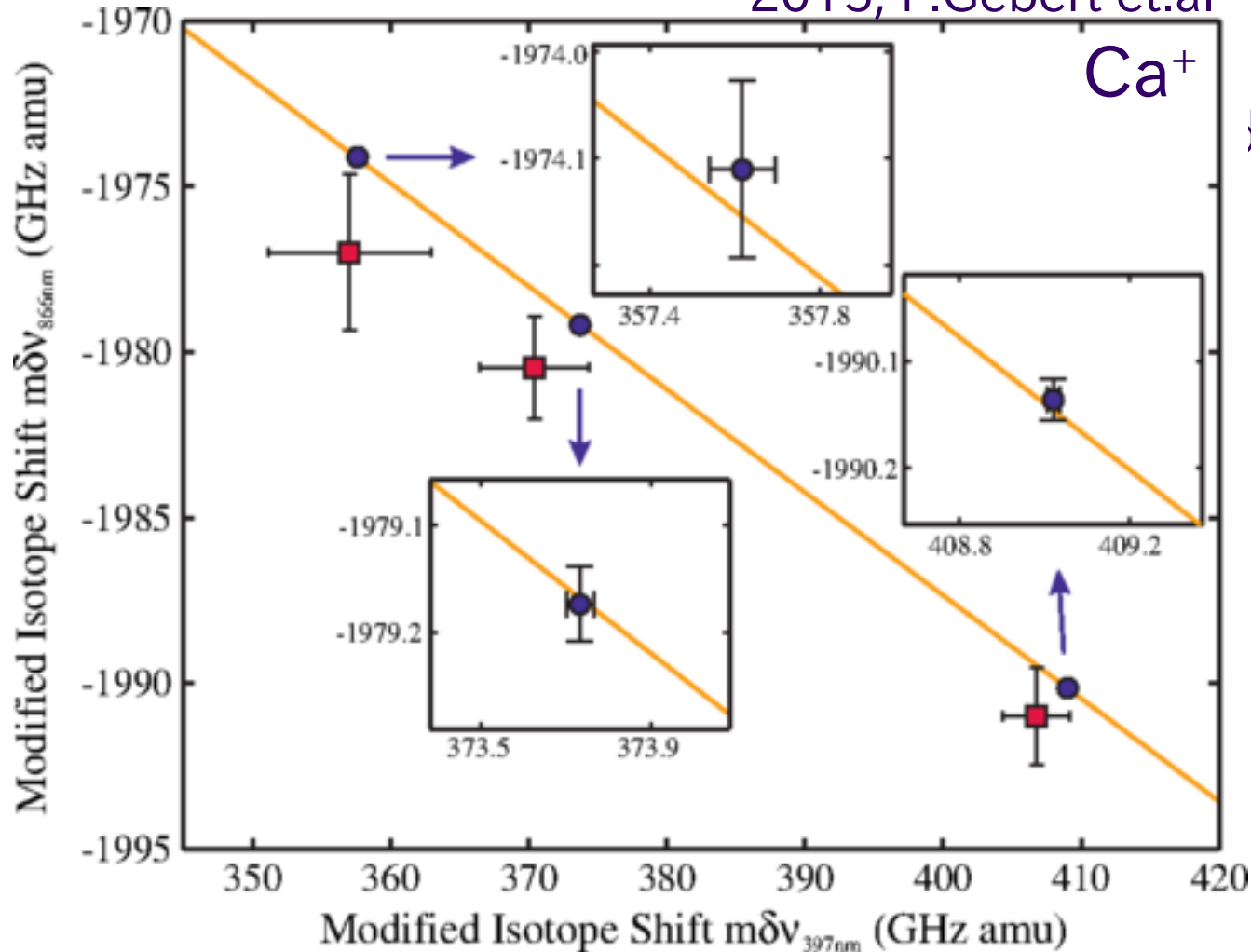
Constant for isotope pairs.

# Isotope shift and the linearity

3

- ◆ Isotope shifts follow a linearity.

2015, F.Gebert et.al



ence.

H. King

# Isotope shift and the linearity

3

does not

non

- ◆ Isotope shifts follow a linearity.

$$\delta H_{A'A} = \delta K_{A'A} + \delta V_{A'A}$$

$$\delta\nu = G \delta\mu + F \delta\langle r^2 \rangle + \underline{X}$$

Isotope dependence.

NLO corrections  
Yukawa potential

Wave function dependence.

▶ Linearity for isotope pairs.

2016, C. Delaunay et. al

Non

$$\frac{\delta\nu_2}{\delta\mu} = \frac{F_2}{F_1} \frac{\delta\nu_1}{\delta\mu} + \left( G_2 - \frac{F_2}{F_1} G_1 \right) + \underline{\left( X_2 - \frac{F_2}{F_1} X_1 \right) / \delta\mu}$$

Constant for isotope pairs.

# Field shift

4

Def:  $\int d\vec{r} (|\psi_j(\vec{r})|^2 - |\psi_i(\vec{r})|^2) \delta V(\vec{r})$

$-Z\alpha \int d\vec{r}' \frac{\delta\rho(\vec{r}')}{|\vec{r} - \vec{r}'|}$

Expand

$$\propto \int_0^\infty dr' \int_0^{r'} dr r^2 \sum_k \xi_k r^k \left( r' - \frac{r'^2}{r} \right) \delta\rho(r')$$

$$\delta\langle r^k \rangle = \int d\vec{r} r^k \delta\rho(r)$$

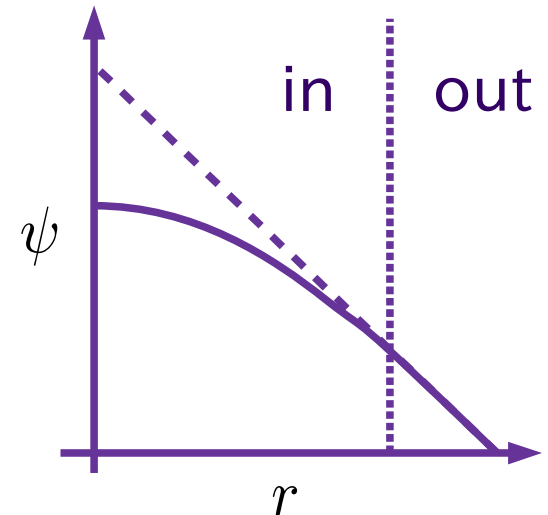
$$= Z\alpha \sum_k \frac{\xi_k}{(k+3)(k+2)} \delta\langle r^{k+2} \rangle$$

1969, E. C. Seltzer

## ► NLO field shift

$$\delta\nu = G\delta\mu + F\delta\langle r^2 \rangle + \tilde{F}\delta\langle r^4 \rangle + \dots$$

$$\psi \sim \chi_0 + \chi_2 r^2 + \dots$$





# Field shift

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$= Z\alpha \sum_k \frac{\xi_k}{(k+3)(k+2)} \delta\langle r^{k+2} \rangle$

Expand

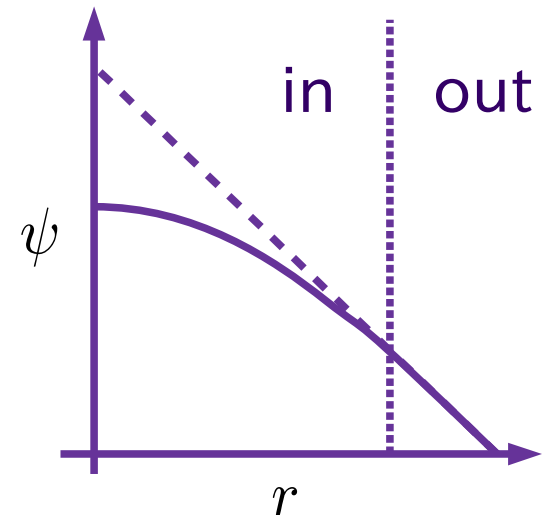
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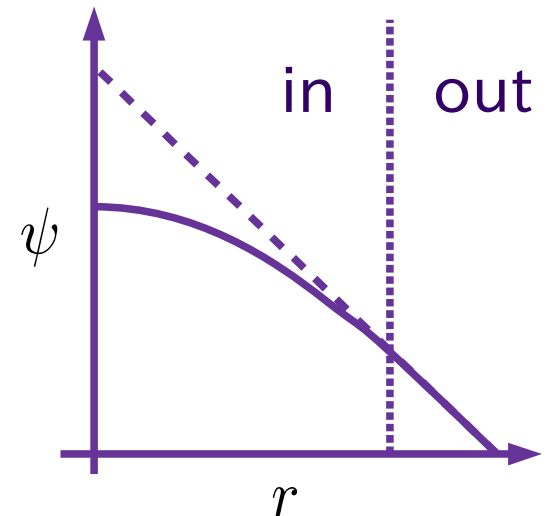
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# Particle shift

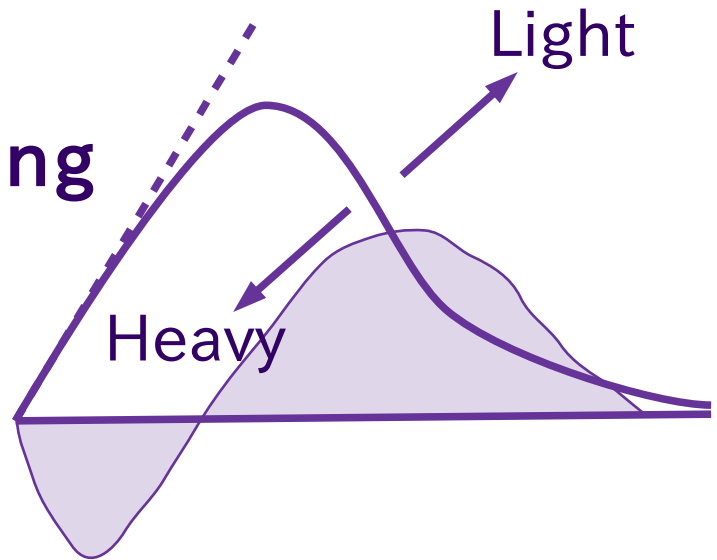
Def: 
$$\int d\vec{r} (|\psi_j(\vec{r})|^2 - |\psi_i(\vec{r})|^2) (A' - A) \frac{g_n g_e}{4\pi} \frac{e^{-mr}}{r}$$

- ▶ Similar to the field shift.
- ▶ Sensitive to the **e-n coupling**

◆ For heavier particle

$$= (A' - A) \frac{g_n g_e}{4\pi} \sum_k \frac{k!}{m^{k+2}} \xi_k$$

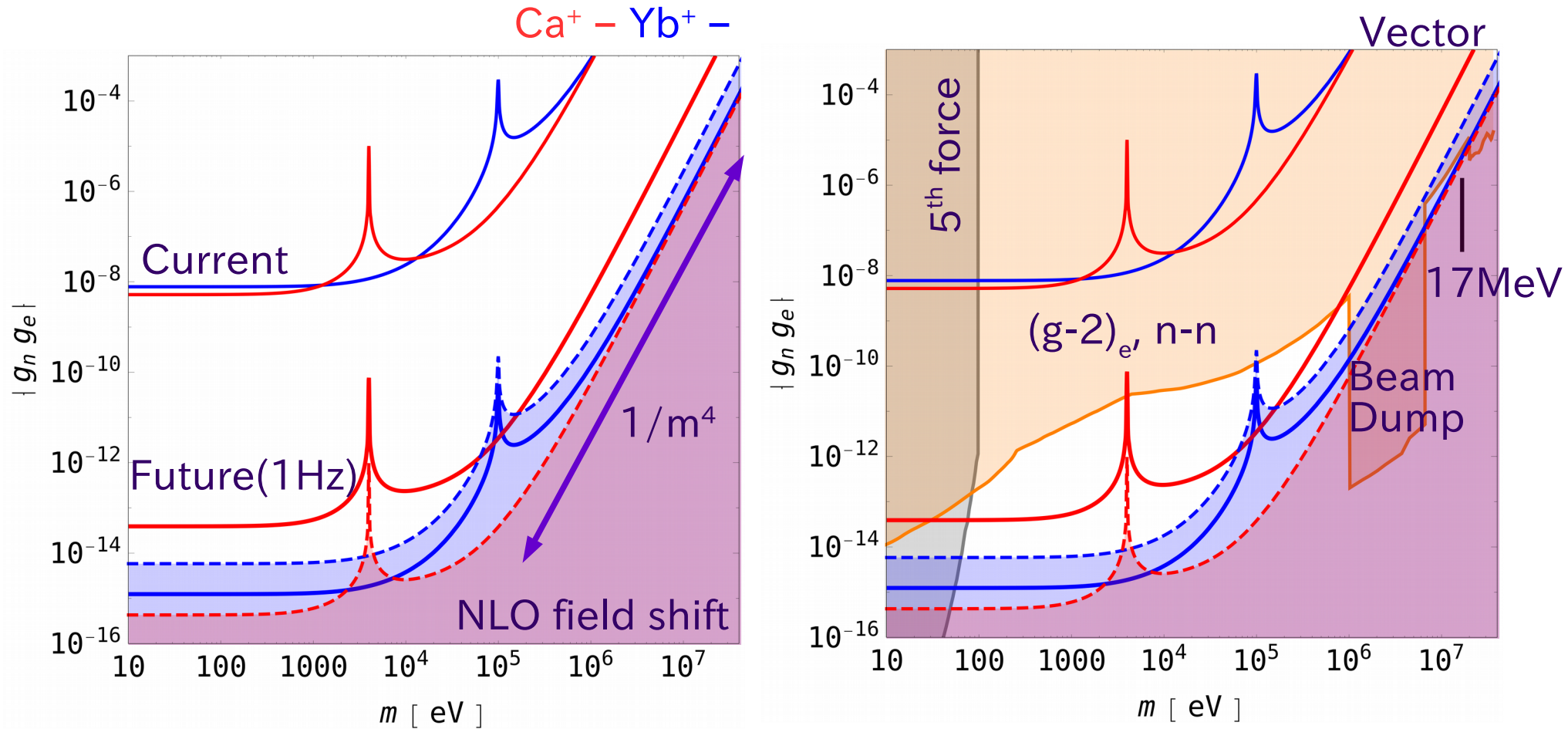
- ▶ 
$$\delta\nu = G\delta\mu + F (\delta\langle r^2 \rangle + c_0/m^2)$$
- $$+ \tilde{F} (\delta\langle r^4 \rangle + c_2/m^4) + \dots$$



Keep the linearity

Non-linearity

# Sensitivity and constraints



- ◆ NLO field shift limits the future sensitivity.
- ◆ 100 eV – 1 MeV is the main target.

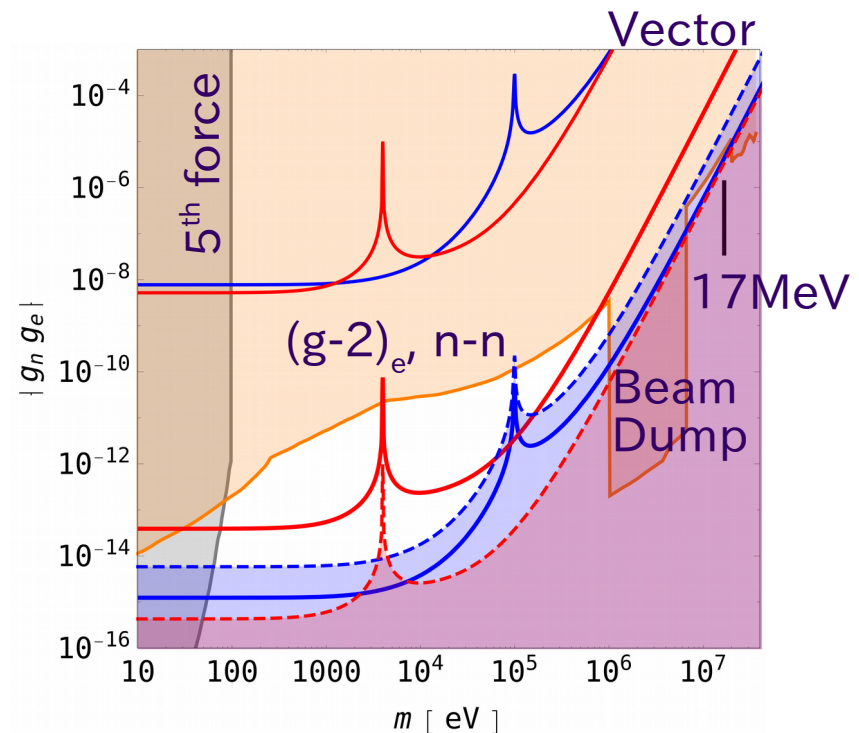
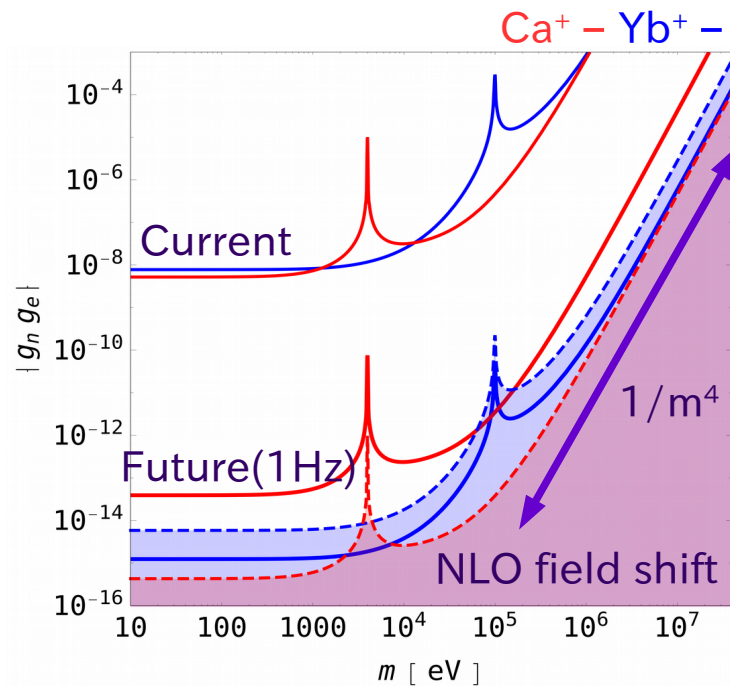
# Conclusion

Precision spectroscopy + Linearity of isotopes



New physics as the non-linearity

- ◆ SM background of NLO field shift.
- ◆ The scaling law at the heavy region.





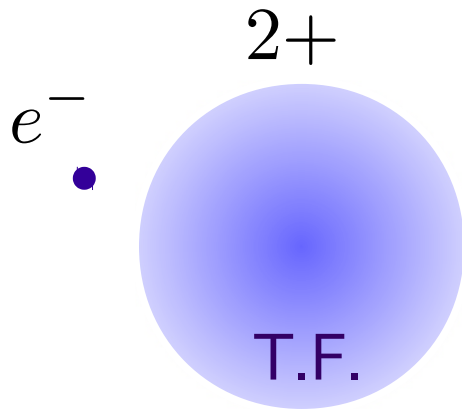
# Other issues

- ◆ **Relativistic effects** on wave function and potential.
  - ▶ The inner behavior can be modified.
  - ▶ Possibly important for light elements.
- ◆ **Isotope shift corrections** to wave functions.
  - ▶ Can be large for heavy elements.
- ◆ **Details of nuclear density** distributions.
  - ▶ Angular distributions.

And others...

- ▶ **Suggest appropriate atoms to experiments.**

# Wave functions of ions



Single electron  
+  
The **Thomas-Fermi** potential  
(Semi-classical free electron gas.)

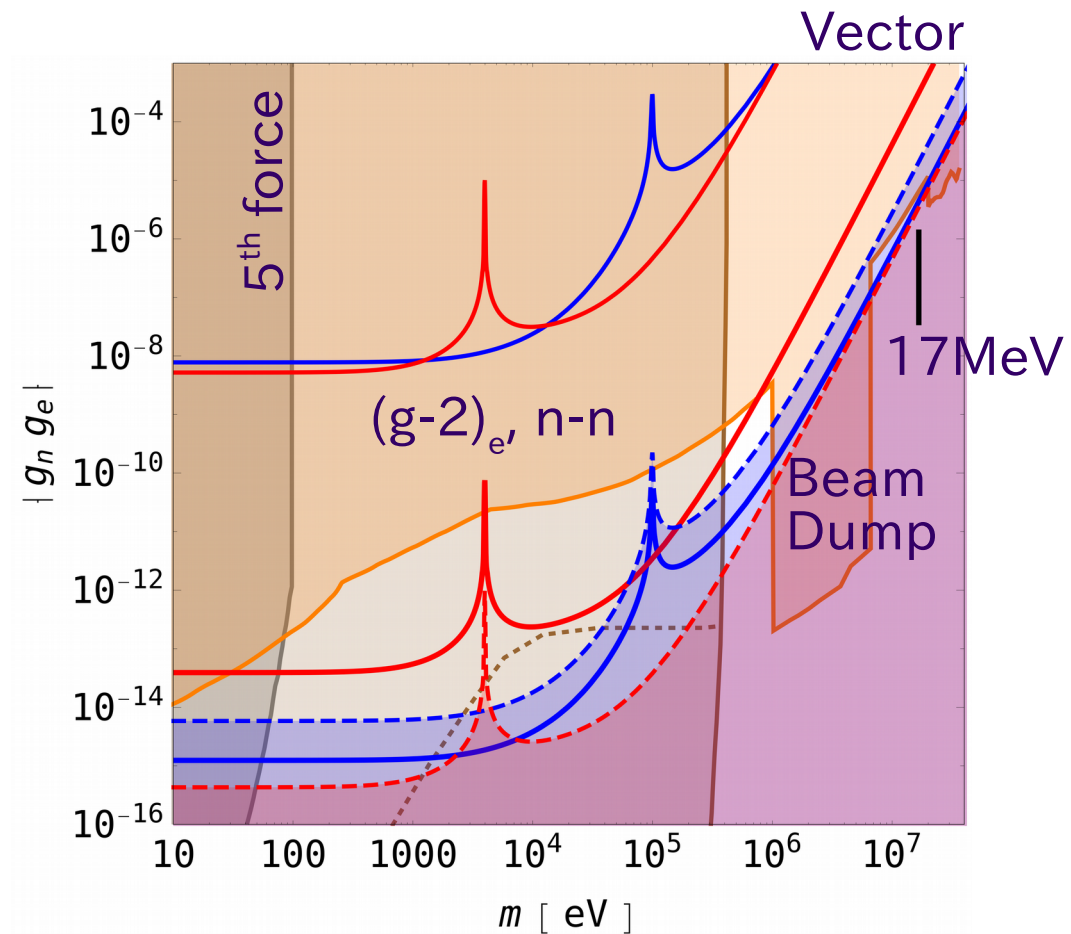
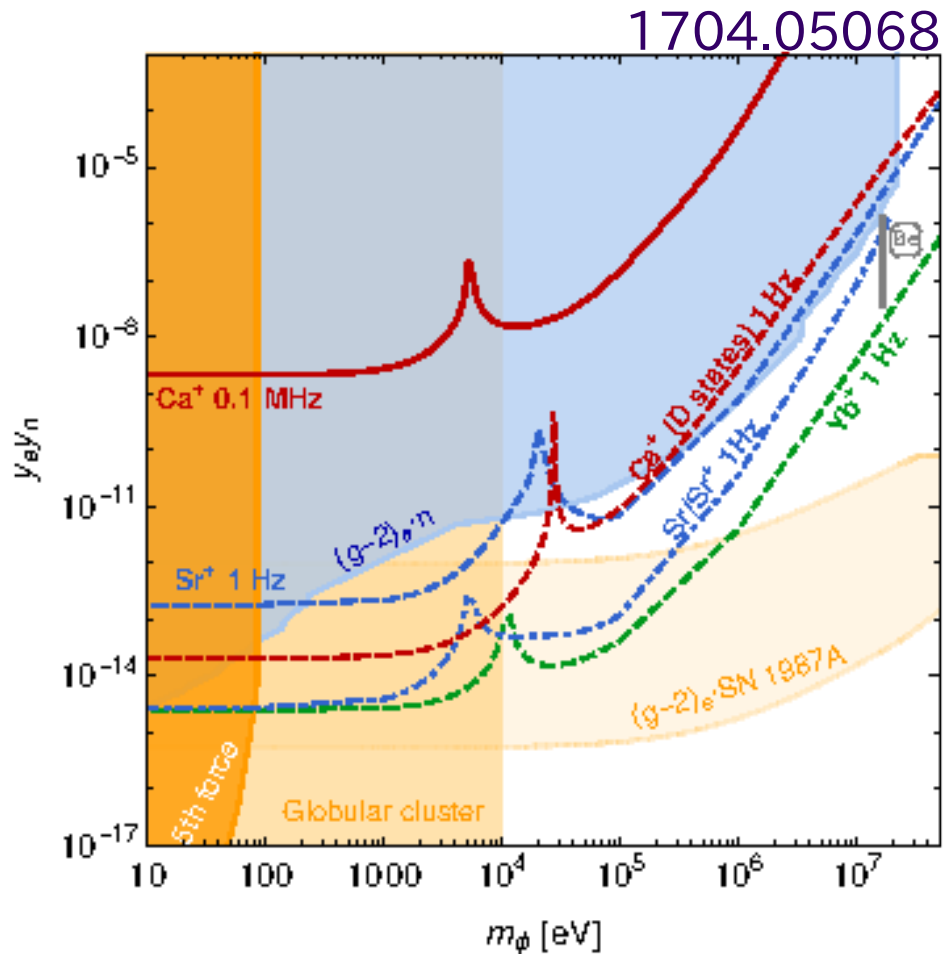
Ca <sup>+</sup>	${}^2S_{1/2} \rightarrow {}^2P_{1/2}$ (323meV)	${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ (704meV)
	$4s \rightarrow 4p$ (386meV)	$3d \rightarrow 4p$ (-1309meV)
Yb <sup>+</sup>	${}^2S_{1/2} \rightarrow {}^2P_{1/2}$ (301meV)	${}^2D_{3/2} \rightarrow {}^2D[3/2]_{1/2}$ (760meV)
	$6s \rightarrow 6p$ (309meV)	$4f \rightarrow 6s$ (39.5meV)

▶ s- & p-states are 😊, d- & f-states are ☹️.

▶ Numerically, good agreement with other results.



# Some comments



- ◆ The stellar cooling has large uncertainty.
- ◆ Our result is smooth because of the analytic study.