# Search for a heavy dark photon at future $e^+e^-$ colliders

# Gang Li

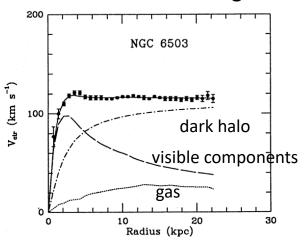
**National Taiwan University** 

In collaboration with Min He, Xiao-Gang He and Cheng-Kai Huang

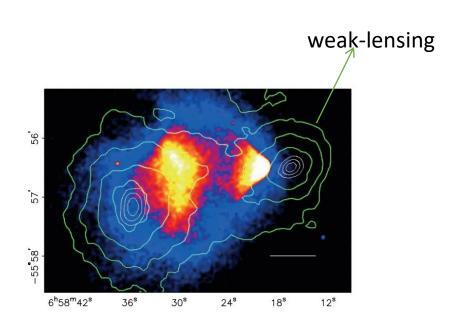
JHEP 1803 (2018) 139 (arXiv:1712.09095)

### Why we need dark photon?

- Evidences of dark matter:
  - spiral galaxy rotation curves
  - merging clusters and galaxies
  - cosmic microwave background



K.G. Begeman, A.H. Broeils, R.H. Sanders, MNRAS 249(1991) 523

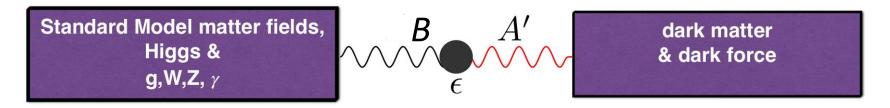


D. Clowe, et al, Astrophys. J. 648 (2006) L109

- But there is no dark matter candidate in the SM
- Dark matter may not interact with the SM directly, but through some mediator

### Why we need dark photon?

Dark photon provides such connection between the SM and the dark sector



through a kinetic mixing between  $U(1)_{A'}$  field with  $U(1)_Y$  field

W. Xue, 2016

Simplest case: one heavy particle ψ with both EM charge & dark charge

B. Holdom, Phys. Lett. 166B, 196 (1986)

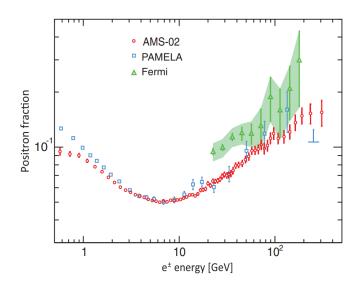
generates 
$$\epsilon \sim \frac{e g_D}{16\pi^2} \log \frac{m_{\psi}}{M_*} \sim 10^{-2} - 10^{-4}$$

N. Toro, Dark Sectors 2016

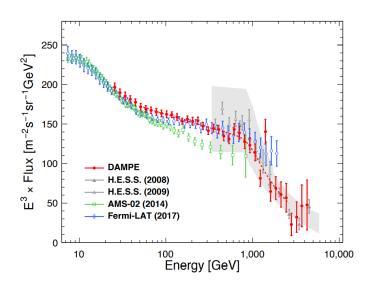
### Why we need dark photon?

- Dark photon provides such connection between the SM and the dark sector through a kinetic mixing between  $U(1)_{A'}$  field with  $U(1)_Y$  field
  - excess in positron fraction
  - peak-like spectrum of cosmic-ray electrons and positrons

P.-H. Gu, X.-G. He, Phys.Lett. B778 (2018) 292



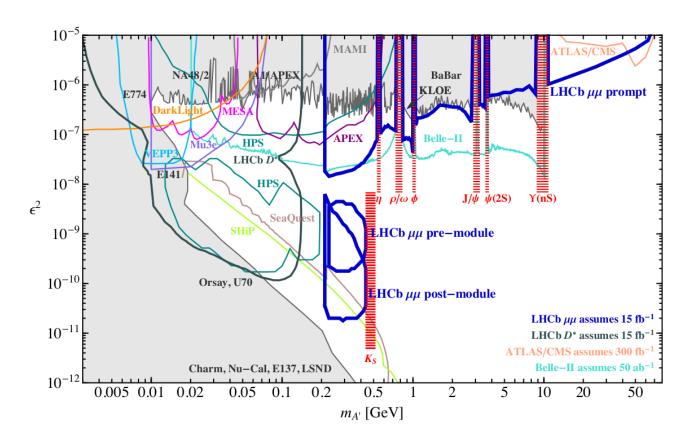
AMS, Phys.Rev.Lett. 110 (2013) 141102

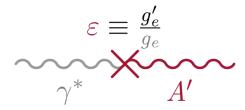


DAMPE, Nature 552 (2017) 63-66 ~1.4 TeV

### Light dark photon searches

- Many efforts have been made to constrain the mixing parameter for a dark photon mass below  $m_Z$
- Beam damp experiments, fixed target experiments, low energy  $e^+e^-$  colliders, rare meson decays...

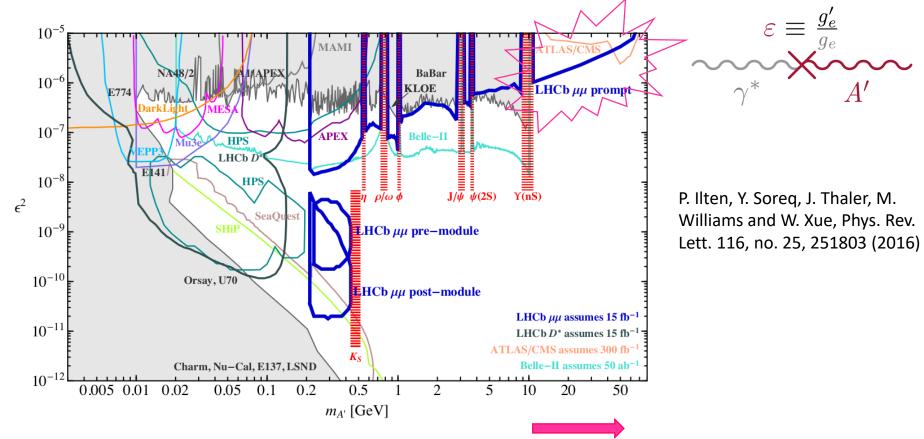




P. Ilten, Y. Soreq, J. Thaler, M. Williams and W. Xue, Phys. Rev. Lett. 116, no. 25, 251803 (2016)

### Light dark photon searches

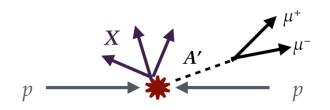
- Many efforts have been made to constrain the mixing parameter for a dark photon mass below  $m_{Z}$
- Beam damp experiments, fixed target experiments, low energy  $e^+e^-$  colliders, rare meson decays...

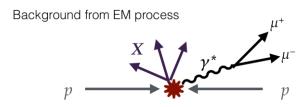


### Light dark photon searches

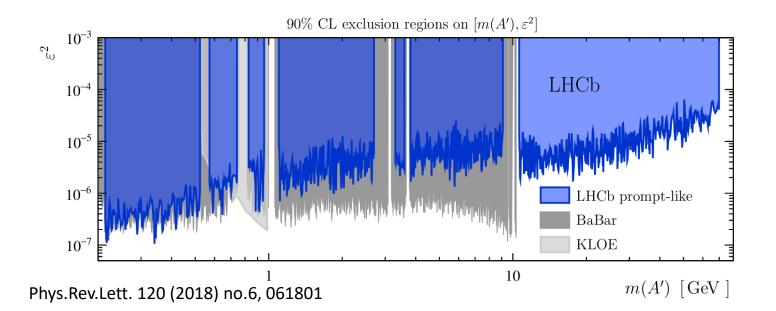
### Prompt $\mu^+\mu^-$ @ LHCb

W. Xue, 2016





Scales as : 
$$\frac{\mathrm{d}\sigma_{pp\to XA'\to X\mu^+\mu^-}}{\mathrm{d}\sigma_{pp\to X\gamma^*\to X\mu^+\mu^-}} = \epsilon^4 \frac{m_{\mu\mu}^4}{(m_{\mu\mu}^2-m_{A'}^2)^2 + \Gamma_{A'}^2 m_{A'}^2}$$

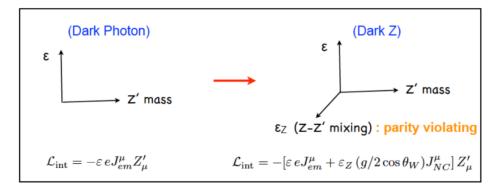


### Dark photon searches: from light to heavy

- There is no special reason why dark photon mass should be small
- Introducing a singlet S with a non-trival  $U(1)_{A^{\prime}}$  quantun number  $s_{A^{\prime}}$

$$(D_{\mu}S)^{\dagger}(D^{\mu}S)$$
  $\longrightarrow$   $m_{A'} = g_{A'}s_{A'}v_s/\sqrt{2}$ 

- Mixing of  $U(1)_{A'}$  and  $U(1)_{Y}$  can induce mixing between
  - photon and dark photon
  - Z boson and dark photon



H.-S. Lee, 1410.8435

Figure 2. Dark Photon vs. Dark Z. The dark Z is a dark photon with more general couplings.

### Formalism

$$L_{\text{kinetic}} = -\frac{1}{4}B_0^{\mu\nu}B_{0,\mu\nu} - \frac{1}{2}\sigma F'_{0,\mu\nu}B_0^{\mu\nu} - \frac{1}{4}F'_{0,\mu\nu}F'^{\mu\nu}_0$$

In the canonical form  $A_0'=\frac{1}{\sqrt{1-\sigma^2}}\tilde{A}', \quad B_0=\tilde{B}-\frac{\sigma}{\sqrt{1-\sigma^2}}\tilde{A}'$  renormalizable

$$\begin{pmatrix} A_0 \\ Z_0 \\ A'_0 \end{pmatrix} = S \begin{pmatrix} \tilde{A} \\ \tilde{Z} \\ \tilde{A}' \end{pmatrix} , \quad S = \begin{pmatrix} 1 & 0 & -\frac{c_W \sigma}{\sqrt{1 - \sigma^2}} \\ 0 & 1 & \frac{s_W \sigma}{\sqrt{1 - \sigma^2}} \\ 0 & 0 & \frac{1}{\sqrt{1 - \sigma^2}} \end{pmatrix}$$

Interactions with the SM currents

$$J_{em}^{\mu}(\tilde{A}_{\mu} - \frac{c_{W}\sigma}{\sqrt{1 - \sigma^{2}}}\tilde{A}'_{\mu}) + J_{Z}^{\mu}(\tilde{Z}_{\mu} + \frac{s_{W}\sigma}{\sqrt{1 - \sigma^{2}}}\tilde{A}'_{\mu}) + \frac{1}{\sqrt{1 - \sigma^{2}}}J_{D}^{\mu}\tilde{A}'_{\mu}$$

In the  $ilde{Z}$  and  $ilde{A}'$  basis, the mass matrix

$$\begin{pmatrix} m_Z^2 & \frac{\sigma s_W}{\sqrt{1-\sigma^2}} m_Z^2 \\ \frac{\sigma s_W}{\sqrt{1-\sigma^2}} m_Z^2 & \frac{1}{1-\sigma^2} m_{A'}^2 + \frac{s_W^2 \sigma^2}{1-\sigma^2} m_Z^2 \end{pmatrix}$$

#### Formalism

#### Diagonalizing it by an unitary transformation U

$$\begin{pmatrix} \tilde{A} \\ \tilde{Z} \\ \tilde{A}' \end{pmatrix} = U \begin{pmatrix} A \\ Z \\ A' \end{pmatrix}, \quad \begin{pmatrix} A_0 \\ Z_0 \\ A'_0 \end{pmatrix} = SU \begin{pmatrix} A \\ Z \\ A' \end{pmatrix}, \quad V \equiv SU$$
or  $m_{A'} < m_Z(m_{A'} > m_Z)$  are given by
$$\mathbf{M} = \sqrt{(\lambda_1 - m_Z^2)^2 + \frac{\sigma^2 s_W^2}{1 - \sigma^2} m_Z^4}$$

 $V = V_{-}(V_{+})$  for  $m_{A'} < m_{Z}(m_{A'} > m_{Z})$  are given by

$$V_{-} = \begin{pmatrix} 1 & \frac{-c_W \sigma(\lambda_1 - m_Z^2)}{\mathbf{M}\sqrt{1 - \sigma^2}} & \frac{-\sigma^2 s_W c_W m_Z^2}{\mathbf{M}(1 - \sigma^2)} \\ 0 & \frac{s_W \sigma \lambda_1}{\mathbf{M}\sqrt{1 - \sigma^2}} & \frac{1}{\mathbf{M}} \left( m_Z^2 - \lambda_1 + \frac{\sigma^2 s_W^2 m_Z^2}{1 - \sigma^2} \right) \\ 0 & \frac{\lambda_1 - m_Z^2}{\mathbf{M}\sqrt{1 - \sigma^2}} & \frac{\sigma s_W m_Z^2}{\mathbf{M}(1 - \sigma^2)} \end{pmatrix} , \quad V_{+} = V_{-} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{pmatrix}$$

$$\lambda_{1,2} = \frac{1}{2} \left( m_Z^2 + \frac{1}{1 - \sigma^2} m_{A'}^2 + \frac{\sigma^2 s_W^2}{1 - \sigma^2} m_Z^2 \pm \Delta \right), \quad \lambda_1 \ge \lambda_2,$$

$$\Delta \equiv \sqrt{\left( m_Z^2 - \frac{1}{1 - \sigma^2} m_{A'}^2 - \frac{\sigma^2 s_W^2}{1 - \sigma^2} m_Z^2 \right)^2 + \frac{4\sigma^2 s_W^2}{1 - \sigma^2} m_Z^4}.$$

$$m_{A'}^{\text{phys.}} = \begin{cases} \lambda_2, & \text{for } m_{A'} < m_Z, \\ \lambda_1, & \text{for } m_{A'} > m_Z. \end{cases}$$

$$m_{A'}^{\text{phys.}} = \begin{cases} \lambda_2, & \text{for } m_{A'} < m_Z, \\ \lambda_1, & \text{for } m_{A'} > m_Z. \end{cases}$$

#### Formalism

$$J_{em}^{\mu}(V_{11}A_{\mu} + V_{12}Z_{\mu} + \epsilon A_{\mu}') + J_{Z}^{\mu}(V_{22}Z_{\mu} + \tau A_{\mu}')$$

if  $|m_Z - m_{A'}| \gg s_W m_Z \sigma$ ,

$$\Delta = |m_Z^2 - m_{A'}^2| + \frac{(m_{A'}^4 + s_W^2 m_Z^4 - c_W^2 m_Z^2 m_{A'}^2)\sigma^2}{|m_Z^2 - m_{A'}^2|} + \mathcal{O}(\sigma^3)$$

$$V_{+} = V_{-} = \begin{pmatrix} 1 & 0 & -c_{W}\sigma \\ 0 & 1 & \frac{s_{W}\sigma m_{A'}^{2}}{m_{A'}^{2} - m_{Z}^{2}} \\ 0 & -\frac{s_{W}\sigma m_{Z}^{2}}{m_{A'}^{2} - m_{Z}^{2}} & 1 \end{pmatrix} + \mathcal{O}(\sigma^{2})$$

$$\epsilon = -c_W \sigma, \quad \tau = \frac{s_W \sigma m_{A'}^2}{m_{A'}^2 - m_Z^2}$$

$$\tau = -\frac{s_W m_{A'}^2 \epsilon}{c_W (m_{A'}^2 - m_Z^2)}$$

 $\tau$  is very small if  $m_{A'} \ll m_Z$ 

Z boson and dark photon physical mass

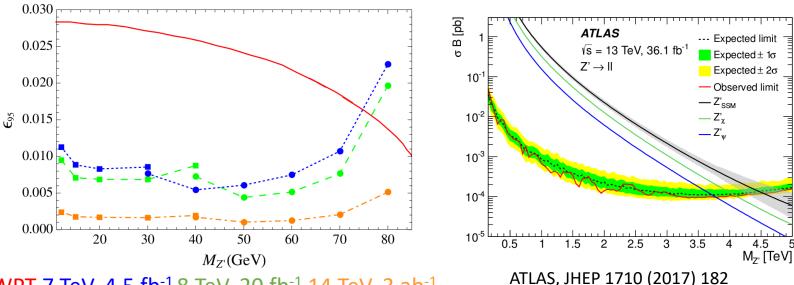
$$(m_Z^{\text{phys.}})^2 = m_Z^2 + \frac{m_Z^4 s_W^2 \sigma^2}{m_Z^2 - m_{A'}^2} + \mathcal{O}(\sigma^3),$$

$$(m_{A'}^{\text{phys.}})^2 = m_{A'}^2 + \frac{(c_W^2 m_Z^2 - m_{A'}^2) m_{A'}^2 \sigma^2}{m_Z^2 - m_{A'}^2} + \mathcal{O}(\sigma^3)$$

### Dark photon searches @ ATLAS & CMS

$$J_{em}^{\mu}(V_{11}A_{\mu} + V_{12}Z_{\mu} + \epsilon A_{\mu}') + J_{Z}^{\mu}(V_{22}Z_{\mu} + \tau A_{\mu}')$$

### Direct searches via Drell-Yan process @ ATLAS and CMS (Z' searches)

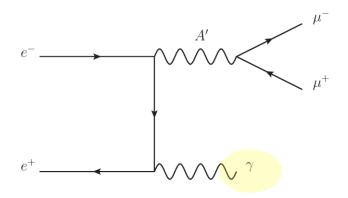


EWPT 7 TeV, 4.5 fb<sup>-1</sup> 8 TeV, 20 fb<sup>-1</sup> 14 TeV, 3 ab<sup>-1</sup>

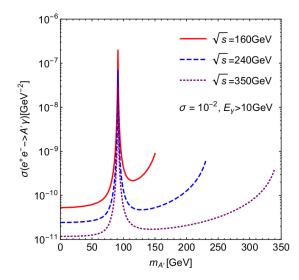
$$\epsilon_{95} \sim 10^{-3}$$
 
$$\epsilon_{95\%\text{C.L.}} = \left(\frac{[\sigma(A')\text{Br}(\mu^+\mu^-)]^{95\%\text{C.L.}}}{K_{\text{NLO}}\sigma_{\text{LO}}(A')\text{Br}(\mu^+\mu^-)/(10^{-4}c_W^2)}\sqrt{\frac{36.1 \text{ fb}^{-1}}{\mathcal{L}}}\right)^{1/2}$$

I. Hoenig, G. Samach and D. Tucker-Smith, Phys. Rev. D 90, no. 7, 075016 (2014)

We studied a dark photon with mass as large as kinematically allowed through  $e^+e^- \to A'X$ ,  $A' \to \mu^+\mu^-$ 



$$J_{em}^{\mu}(V_{11}A_{\mu} + V_{12}Z_{\mu} + \epsilon A_{\mu}') + J_{Z}^{\mu}(V_{22}Z_{\mu} + \tau A_{\mu}')$$



$$\sigma_{A'\gamma} = -\frac{e^2(m_{A'}^4 + s^2)(1 - \ln\frac{s}{m_e^2})}{4\pi s^2(s - m_{A'}^2)} \left\{ e^2 \epsilon^2 + \frac{g^2 \tau^2 \left[ (g_V^e)^2 + (g_A^e)^2 \right]}{4c_W^2} - \frac{egg_V^e \epsilon \tau}{c_W} \right\}$$

$$J_{em}^{\mu}(V_{11}A_{\mu} + V_{12}Z_{\mu} + \epsilon A_{\mu}') + J_{Z}^{\mu}(V_{22}Z_{\mu} + \tau A_{\mu}')$$

$$\Gamma(A' \to f\bar{f}) = \frac{g^{2}m_{A'}}{12\pi c_{W}^{2}} N_{c}^{f} \left\{ \epsilon^{2}Q_{f}^{2}c_{W}^{2}s_{W}^{2} + \epsilon\tau Q_{f}c_{W}s_{W}g_{V}^{f} + \frac{1}{4}\tau^{2}[(g_{V}^{f})^{2} + (g_{A}^{f})^{2}] \right\},$$

$$\Gamma(A' \to Zh) = \frac{g^{2}\tau^{2}m_{A'}}{192\pi c_{W}^{2}} \lambda^{1/2}(1, x_{Z}, x_{h}) \left\{ \lambda(1, x_{Z}, x_{h}) + 12x_{Z} \right\},$$

$$\Gamma(A' \to W^{+}W^{-}) = \frac{g^{2}s_{W}^{2}(\epsilon + \tau \cot\theta_{W})^{2}m_{A'}}{192\pi} x_{W}^{-2}(1 - 4x_{W})^{3/2}(1 + 20x_{W} + 12x_{W}^{2}),$$

$$x_{W,Z,h} = (m_{W,Z,h}/m_{A'})^{2}$$

$$x_{W,Z,h} = (m_{W,Z,h}/m_{A'})^{2}$$

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signal: 
$$e^+e^- \to \gamma A' \to \gamma \mu^+\mu^-$$
 main background:  $e^+e^- \to \gamma \mu^+\mu^-$ 

- Interference and off-shell A' contributions are negligible for a narrow A' resonance
- At CEPC: delphes\_card\_CEPC.tcl

$$-\frac{\Delta p_T}{p_T} = 0.1\% \oplus \frac{p_T}{10^5 \text{ GeV}} \text{ for } |\eta| < 1.0 \text{ and } 10 \text{ times larger for } 1.0 < |\eta| < 3.0;$$

$$-\frac{\Delta E}{E} = \frac{0.20}{\sqrt{E/\text{GeV}}} \oplus 0.5\%. \text{ for } |\eta| < 3.0.$$

• At FCC-ee: delphes\_card\_ILD.tcl

- 
$$\frac{\Delta p_T}{p_T} = 0.1\% \oplus \frac{p_T}{10^5 \text{ GeV}}$$
 for  $|\eta| < 1.0$  and 10 times larger for  $1.0 < |\eta| < 2.4$ ;

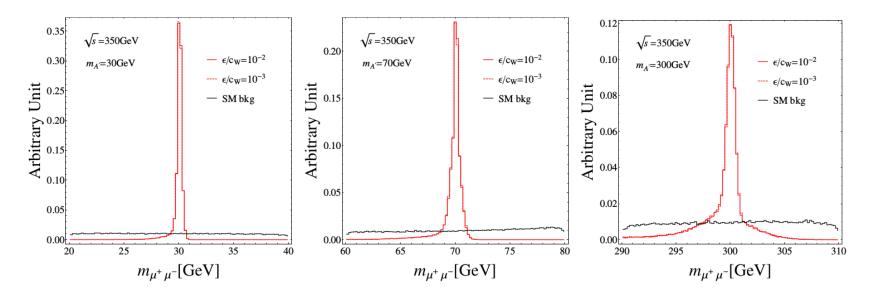
$$-\frac{\Delta E}{E} = \frac{0.15}{\sqrt{E/\text{GeV}}} \oplus 1\%. \text{ for } |\eta| < 3.0.$$

signal: 
$$e^+e^- \rightarrow \gamma A' \rightarrow \gamma \mu^+\mu^-$$

signal:  $e^+e^- \to \gamma A' \to \gamma \mu^+\mu^-$  main background:  $e^+e^- \to \gamma \mu^+\mu^-$ 

normalized  $m_{\mu^+\mu^-}$  distributions

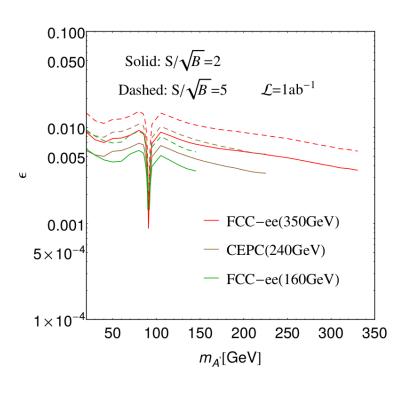
- Total width
- Momentum resolution



$$\Delta m_{\mu^+\mu^-} < 0.5 \sim 1.5 \text{ GeV}, \quad E_T^{\text{miss}} < 5 \text{ GeV}$$

### signal significance:

$$\frac{S}{\sqrt{B}} = (\frac{S}{\sqrt{B}})_0 \frac{\epsilon^2}{10^{-4}} \sqrt{\frac{\mathcal{L}}{1 \text{ ab}^{-1}}},$$



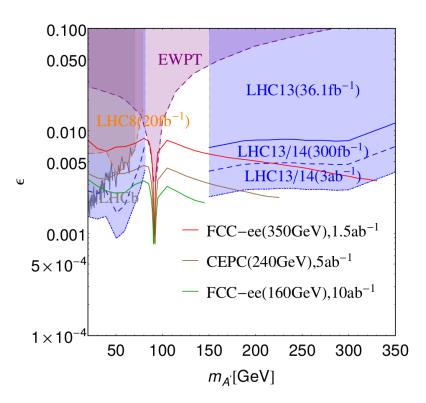


TABLE IV: The values of  $\epsilon$  corresponding to  $S/\sqrt{B}=2$  for  $m_{A'}=30$  GeV, 115 GeV, 230 GeV and 320 GeV in different channels at the 350 GeV FCC-ee with the integrated luminosity of 1.5 ab<sup>-1</sup>. The notation of "aE-b" stands for  $a \times 10^{-b}$ .

FCC-ee (350 GeV)	$30 \; \mathrm{GeV}$	$115  \mathrm{GeV}$	230 GeV	$320  \mathrm{GeV}$
$\mu^+\mu^-\gamma$	7.62E-3	8.47E-3	5.26E-3	3.81E-3
$e^+e^-\gamma$	1.06E-2	1.62E-2	3.28E-2	7.74E-3
$ au^+ au^-\gamma$	3.40E-2	3.55E-2	1.22E-2	7.27E-3
$qar{q}\gamma$	9.40E-3	8.18E-3	3.92E-3	2.48E-3
$Zh\gamma$	_	_	3.90E-2	2.10E-2
$W^+W^-\gamma$	_	_	4.05E-2	2.21E-2

### Also promising in jet final state

### Summary

- A coupling of dark photon to the SM can be generated through kinetic mixing
- A non-zero mixing parameter  $\epsilon$  induces a mixing between A' and Z if dark photon mass is not zero, which can be large when  $m_{A'}$  close to  $m_Z$  even if  $\epsilon$  is small
- Many efforts have been made to constrain the mixing parameter for a dark photon mass below  $m_{Z}$
- We studied the search for dark photon in  $e^+e^- \to \gamma A' \to \gamma \mu^+\mu^-$  for a dark photon mass as large as kinematically allowed at future  $e^+e^-$  colliders

