

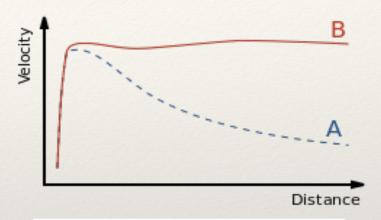
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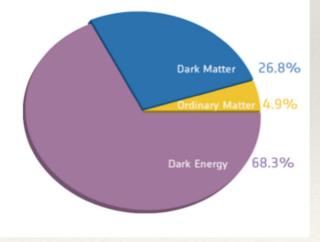
A frequentist analysis of protonphilic spin-dependent inelastic Dark Matter (pSIDM) as an explanation of the DAMA effect

Jong-Hyun Yoon @ Sogang U. In collaboration with Prof. Stefano Scopel Dr. Gaurav Tomar Mr. Sunghyun Kang

Introduction

- Dark Matter and the Standard Model
- Numerous evidences
- A variety of candidates
- WIMP (Weakly Interacting Massive Particle)
- Worldwide efforts to search for DM

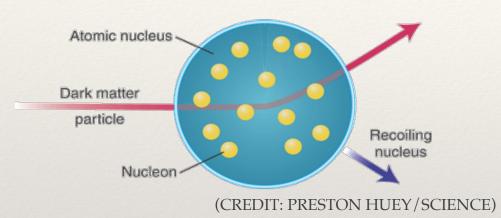




(Credit: ESA and the Planck Collaboration.)

Introduction

Dark Matter Direct Detection





(COSINE-100 Dark Matter Experiment)

* WIMP rates

$$R_{[E'_1, E'_2]} = MT \int_{E'_1}^{E'_2} \frac{dR}{dE'} dE'$$

$$\frac{dR}{dE'} = \sum_{T} \int_{0}^{\infty} \frac{dR_{\chi T}}{dE_{ee}} \mathcal{G}_T(E', E_{ee}) \epsilon(E') dE_{ee}$$

$$E_{ee} = q(E_R) E_R,$$

Germanium experiments carry only a very small amount of ⁷³Ge, the only isotope with spin, carried by an unpaired neutron

Isotope	Spin	Z (# of protons)	A-Z (# of neutrons)	Abundance
⁷³ Ge	9/2	32	41	7.7 %

Xenon experiment contain two isotopes with spin, both carried mostly by an unpaired neutron

Isotope	Spin	Z (# of protons)	A-Z (# of neutrons)	Abundance
¹²⁹ Xe	1/2	54	75	26%
¹³¹ Xe	3/2	54	77	21%

If the WIMP particle couples only to protons (cⁿ/c^p<<1) in a spin-dependent way the rate for Germanium and Xenon detectors is strongly suppressed and their bounds can be evaded

 Low v_min can explain the DAMA excess and the null signal from other experiments

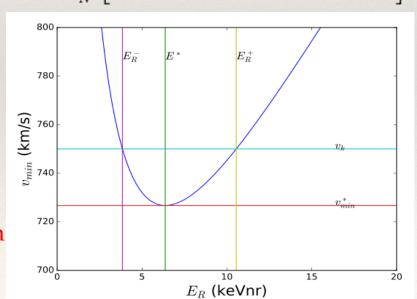
$$rac{dR_{\chi T}}{dE_R} = N_T \int_{v_{min}}^{v_{esc}} rac{
ho_\chi}{m_\chi} v rac{d\sigma_{\chi T}}{dE_R} \, f(v) dv,$$

$$\int_0^\infty dE_R \int_{v_{min}}^\infty dv \to \int_{v_{min}^*}^\infty dv \int_{E_R^-(v)}^{E_R^+(v)} dE_R, \quad E_R^\pm(v_{min}, m_\chi, \delta) = \frac{\mu_{\chi N}^2}{m_N} \left[v_{min}^2 - \frac{(v_{min}^*)^2}{2} \pm \sqrt{v_{min}^2 - (v_{min}^*)^2} \right],$$

$$v_{min}^* = \sqrt{\frac{2\delta}{\mu_{\chi N}}}, \ v_{min} = \frac{1}{\sqrt{2m_N E_R}} \left| \frac{m_N E_R}{\mu_{\chi N}} + \delta \right|,$$

$$v_{min}^{*Na} < v_{cut}^{lab} < v_{min}^{*F},$$

For appropriate choice of parameters WIMPfluorine scatterings can be kinematically forbidden while WIMP-sodium scatterings can explain the DAMA effect



Non-relativistic effective models

$$\mathcal{H} = \sum_{ au=0,1} \sum_{k=1}^{15} c_k^ au \mathcal{O}_k \, t^ au, \quad t^0 = 1, \, t^1 = au_3$$

$$rac{d\sigma_{\chi T}}{dE_R} = rac{1}{10^6} rac{2m_T}{4\pi} rac{c^2}{v^2} \left[rac{1}{2j_\chi + 1} rac{1}{2j_T + 1} \sum_{spin} |\mathcal{M_T}|^2
ight]$$

$$\frac{1}{2j_{\chi}+1}\frac{1}{2j_{T}+1}\sum_{spin}|\mathcal{M}_{\mathcal{T}}|^{2} = \frac{4\pi}{2j_{T}+1}\sum_{\tau\tau'}\sum_{l}R_{l}^{\tau\tau'}W_{T,l}^{\tau\tau'}, \quad l=M,\Sigma'',\Sigma',\Phi'',\Phi''M,\;\check{\Phi}',\Delta,\;\Delta\Sigma'$$

$$R_l^{\tau \tau'} = R_{0,l}^{\tau \tau'} + R_{1,l}^{\tau \tau'} (v^2 - v_{min}^2).$$

 $\mathcal{L}_{int} \ni c^p \vec{S}_{\chi} \cdot \vec{S}_p + c^n \vec{S}_{\chi} \cdot \vec{S}_n$, A.L.Fitzpatrick, W.Haxton, E.Katz, N.Lubbers and Y.Xu, JCAP1302, 004 (2013),1203.3542;

N.Anand, A.L.Fitzpatrick and W.C.Haxton, Phys.Rev.C89, 065501 (2014) 1308 6288

Reassemble the integration

$$R_{[E_1',E_2']}=rac{
ho_\chi}{m_\chi}\sigma_p\int_{v_{min}^*}^\infty dv \hat{\mathcal{H}}(v)f(v), \quad \sigma_p=(c_4^p)^2rac{\mu_{\chi N}^2}{\pi},$$

$$\begin{split} \hat{\mathcal{H}}(v) &= \sum_{T} N_{T} M T \frac{c^{2}}{v} \frac{m_{T}}{\mu_{\chi T}^{2}} \frac{2\pi}{10^{6}} \int_{E_{R}^{-}(v)}^{E_{R}^{+}(v)} dE_{R} \int_{E_{1}^{\prime}}^{E_{2}^{\prime}} dE^{\prime} \epsilon(E^{\prime}) \mathcal{G}_{T}[E^{\prime}, q(E_{R})E_{R}] \times \\ &\frac{1}{2j_{T}+1} \sum_{\tau \tau^{\prime}} \sum_{l} \left[\hat{R}_{0,l}^{\tau \tau^{\prime}} + \hat{R}_{1,l}^{\tau \tau^{\prime}}(v^{2} - v_{min}^{2}) \right] W_{l}^{\tau \tau^{\prime}} = \\ &\frac{c^{2}}{v} \int_{E_{R}^{-}(v)}^{E_{R}^{+}(v)} dE_{R} \left\{ \hat{\mathcal{R}}_{0}(E_{R}) + \hat{\mathcal{R}}_{1}(E_{R})(v^{2} - v_{min}(E_{R})^{2}) \right\}, \end{split}$$

$$\begin{split} \hat{\mathcal{R}}_{\{0,1\}} &= \sum_{T} N_{T} M T \frac{m_{T}}{\mu_{\chi T}^{2}} \frac{2\pi}{10^{6}} \int_{E_{1}'}^{E_{2}'} dE' \epsilon(E') \mathcal{G}_{T}[E', q(E_{R}) E_{R}] \frac{1}{2j_{T}+1} \sum_{\tau \tau'} \sum_{l} \hat{R}_{\{0,1\}, l}^{\tau \tau'} W_{l}^{\tau \tau'} \\ &= \sum_{T} \left[\hat{\mathcal{R}}_{\{0,1\}} \right]_{T}, \quad \hat{R}_{0, l}^{\tau \tau'} \equiv R_{0, l}^{\tau \tau'} / (c_{4}^{p})^{2} \end{split}$$

Halo-independent analysis

$$\begin{split} f(v) &\equiv -v \frac{d}{dv} \eta(v), \quad R_{[E'_1, E'_2]} = \frac{\rho_{\chi}}{m_{\chi}} \sigma_p \int_0^{\infty} dv \hat{\mathcal{R}}(v) \eta(v) = \int_0^{\infty} dv \mathcal{R}(v) \tilde{\eta}(v), \\ \tilde{\eta}(v, t) &= \frac{\rho_{\chi}}{m_{\chi}} \sigma \eta(v, t), \quad \eta(v, t) = \int_v^{\infty} \frac{f(v, t)}{v} \, dv, \qquad \hat{\mathcal{R}}(v) = \frac{d}{dv} \left[v \hat{\mathcal{H}}(v) \right] \\ \tilde{\eta}_{0, 1}(v) &= \sum_{k=1}^{N} \tilde{\eta}_{0, 1}^{k} \theta(v - v_{k-1}) \theta(v_k - v), \qquad \tilde{\eta}_{0, 1}^{k}(v_{min}) = \sum_{i=k}^{N} \delta \tilde{\eta}_{0, 1}^{i}, \\ R_{[E'_1, E'_2]} &= N_T M T \frac{\rho_{\chi}}{m_{\chi}} \sigma \int_{v_{min}}^{\infty} dv \frac{d}{dv} \left\{ v \frac{c^2}{v} \int_{E_R^-(v)}^{E_R^+(v)} dE_R \left\{ \hat{\mathcal{R}}_0(E_R) + \hat{\mathcal{R}}_1(E_R)[v^2 - v_{min}(E_R)^2] \right\} \right\} \\ &\times \sum_{k=1}^{N} \delta \tilde{\eta}^k \theta(v_k - v) = N_T M T \frac{\rho_{\chi}}{m_{\chi}} \sigma c^2 \sum_{k=1}^{N} \delta \tilde{\eta}^k \times \\ &\int_{E_R^-(v)}^{E_R^{max}(v_k)} dE_R \left\{ \hat{\mathcal{R}}_0(E_R) + \hat{\mathcal{R}}_1(E_R)[v_k^2 - v_{min}(E_R)^2] \right\}. \end{split}$$

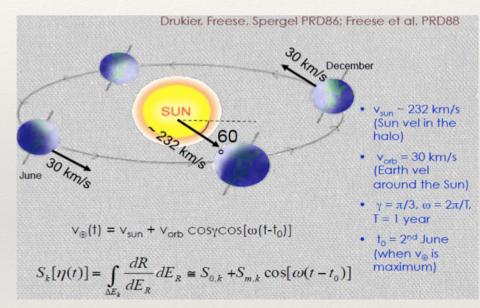
DAMA experiment and Annual modulation

Average rate

$$egin{align} S_0 &\equiv rac{1}{T} \int_0^T S(t) dt = \int_0^\infty \mathcal{R}(v) ilde{\eta}_0(v) \, dv, \ & ilde{\eta}_0(v) \equiv rac{1}{T} \int_0^T ilde{\eta}(v,t) dt, \ \end{matrix}$$

Annual modulation

$$S_1 \equiv rac{2}{T} \int_0^T \cos\left[rac{2\pi}{T}(t-t_0)
ight] S(t) dt = \int_0^\infty \mathcal{R}(v) ilde{\eta}_1(v) \, dv, \ ilde{\eta}_1(v) \equiv rac{2}{T} \int_0^T \cos\left[rac{2\pi}{T}(t-t_0)
ight] ilde{\eta}(v,t) dt,$$



Likelihood analysis

$$-2 \ln \mathcal{L}(\mathbf{d}|\Theta) = \sum_{n=1}^{N_{DAMA}} \left(\frac{S_{1,n}(\Theta) - S_{1,n}^{exp}}{2\sigma_n^{exp}} \right)^2 - 2 \sum_{i=1}^{N_{exp}} \sum_{j=1}^{N_{bin}} \mathcal{L}_j^i(\Theta) \qquad \theta \equiv (m_\chi, \delta, r)$$

$$\Theta = (\theta, \eta) \quad -2\mathcal{L}_j^i(\Theta) = 2 \left[S_{0,j}^i(\Theta) + B_j^i - N_j^i - N_j^i \ln \frac{S(\Theta)_{0,j}^i + B_j^i}{N_j^i} \right]$$

 $S_{1,n}$ is the prediction of the DAMA modulation amplitude in the n-th bin

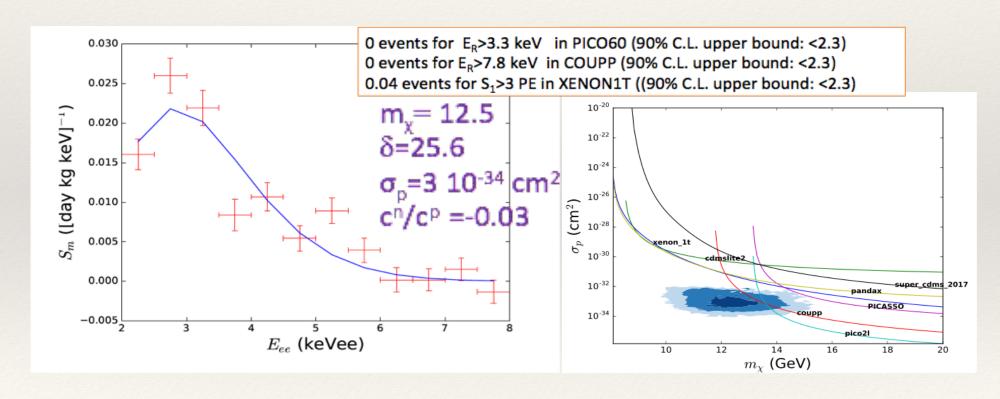
 $S_{1,n}^{exp}$ the corresponding measurement with error σ_n^{exp}

 $S_{0,j}^i$ the expected rate in the *i*-the energy bin of the *j*-th experiment

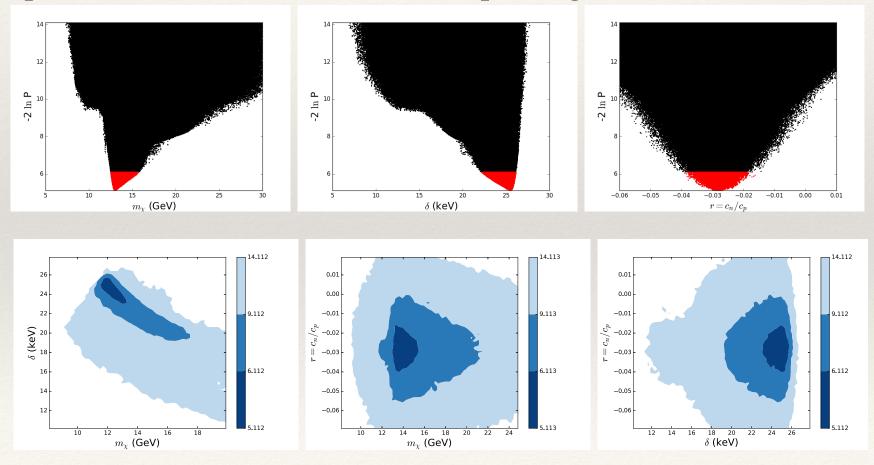
 N_j^i the corresponding measured count rate

 B_j^i the expected background

- * DAMA run 1
- * Best fit: χ 2 = 8.5 with 12-4 d.o.f. (p-value: 0.38)



DAMA/LIBRA <u>phase-1</u> (frequentist interval for three parameters: WIMP mass, mass splitting and cⁿ/c^p)



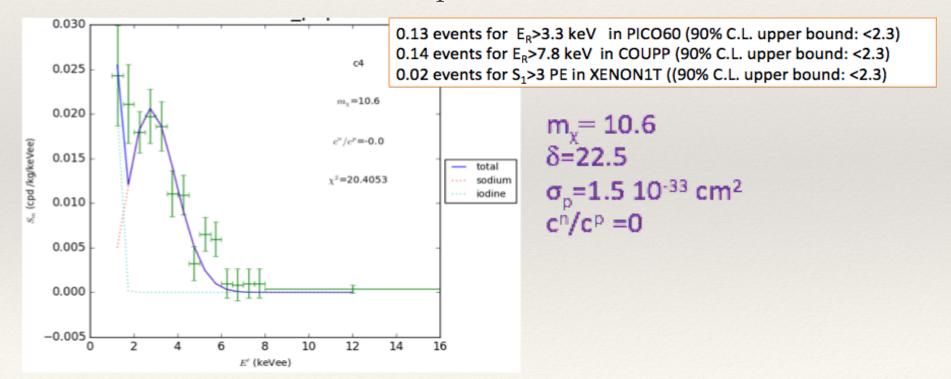
DAMA/LIBRA <u>phase-1</u> (frequentist interval for three parameters: WIMP mass, mass splitting and cⁿ/c^p)

12.5 GeV
$$\leq m_{\chi} \leq 15.7$$
 GeV
22.1 keV $\leq \delta \leq 26.1$ keV
 $-0.039 \leq r \leq -0.016$.

For this choice of parameters, pSIDM explains DAMA/LIBRA phase-1 in compliance with ALL other constraints!

DAMA/LIBRA phase-2 changed it all: lower threshold brings in WIMP-iodine scatterings

- pSIDM update with DAMA run2
- * Harder to fit iodine in the first two bin
- * Best fit: $\chi 2 = 20.4$ with 11 d.o.f. (p-value: 0.04)



Work in progress

- We are working on it
- In the meantime today I will discuss DAMA phase2 in non-relativistic effective models



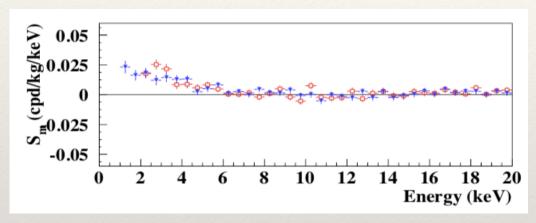


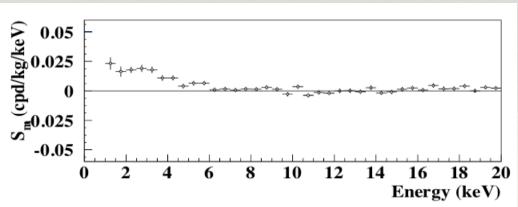
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DAMA/LIBRA-phase2 in WIMP effective models

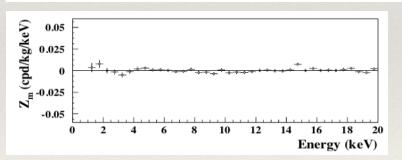
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DAMA released the first model independent results





Energy	$S_m (\text{cpd/kg/keV})$	Energy	$S_m \text{ (cpd/kg/keV)}$
(1.0-1.5) keV	(0.0232 ± 0.0052)	(6.5-7.0) keV	(0.0016±0.0018)
(1.5-2.0) keV	(0.0164 ± 0.0043)	(7.0-7.5) keV	(0.0007 ± 0.0018)
(2.0-2.5) keV	(0.0178 ± 0.0028)	(7.5-8.0) keV	(0.0016 ± 0.0018)
(2.5-3.0) keV	(0.0190 ± 0.0029)	(8.0-8.5) keV	(0.0014 ± 0.0018)
(3.0-3.5) keV	(0.0178 ± 0.0028)	(8.5-9.0) keV	(0.0029 ± 0.0018)
(3.5-4.0) keV	(0.0109 ± 0.0025)	(9.0-9.5) keV	(0.0014 ± 0.0018)
(4.0-4.5) keV	(0.0110 ± 0.0022)	(9.5-10.0) keV	$-(0.0029\pm0.0019)$
(4.5-5.0) keV	(0.0040 ± 0.0020)	(10.0-10.5) keV	(0.0035 ± 0.0019)
(5.0-5.5) keV	(0.0065 ± 0.0020)	(10.5-11.0) keV	$-(0.0038\pm0.0019)$
(5.5-6.0) keV	(0.0066 ± 0.0019)	(11.0-11.5) keV	-(0.0013±0.0019)
(6.0-6.5) keV	(0.0009 ± 0.0018)	(11.5-12.0) keV	$-(0.0019\pm0.0019)$



$$\begin{split} S_{\scriptscriptstyle i}(E) &= S_{\scriptscriptstyle 0}(E) + S_{\scriptscriptstyle m}(E) \; cos \; \omega(t_{\scriptscriptstyle i} - t_{\scriptscriptstyle 0}) + Z_{\scriptscriptstyle m}(E) \; sin \; \omega(t_{\scriptscriptstyle i} - t_{\scriptscriptstyle 0}) \\ &= S_{\scriptscriptstyle 0}(E) + Y_{\scriptscriptstyle m}(E) \; cos \; \omega(t_{\scriptscriptstyle i} - t^{\scriptscriptstyle *}). \end{split}$$

Bernabei et al. (DAMA Collaboration), 1805.10486

Elastic effective models with the standard Maxwellian

$$\mathcal{H}(\mathbf{r}) = \sum_{\tau=0,1} \sum_{j=1}^{15} c_{j}^{\tau} \mathcal{O}_{j}(\mathbf{r}) t^{\tau}, \qquad \mathcal{O}_{1} = 1_{\chi} 1_{N}; \quad \mathcal{O}_{2} = (v^{\perp})^{2}; \quad \mathcal{O}_{3} = i \vec{S}_{N} \cdot (\frac{\vec{q}}{m_{N}} \times \vec{v}^{\perp})$$

$$\mathcal{O}_{4} = \vec{S}_{\chi} \cdot \vec{S}_{N}; \quad \mathcal{O}_{5} = i \vec{S}_{\chi} \cdot (\frac{\vec{q}}{m_{N}} \times \vec{v}^{\perp}); \quad \mathcal{O}_{6} = (\vec{S}_{\chi} \cdot \frac{\vec{q}}{m_{N}})(\vec{S}_{N} \cdot \frac{\vec{q}}{m_{N}})$$

$$t^{0} = 1, t^{1} = \tau_{3}$$

$$\mathcal{O}_{7} = \vec{S}_{N} \cdot \vec{v}^{\perp}; \quad \mathcal{O}_{8} = \vec{S}_{\chi} \cdot \vec{v}^{\perp}; \quad \mathcal{O}_{9} = i \vec{S}_{\chi} \cdot (\vec{S}_{N} \times \frac{\vec{q}}{m_{N}})$$

$$\mathcal{O}_{10} = i \vec{S}_{N} \cdot \frac{\vec{q}}{m_{N}}; \quad \mathcal{O}_{11} = i \vec{S}_{\chi} \cdot \frac{\vec{q}}{m_{N}}; \quad \mathcal{O}_{12} = \vec{S}_{\chi} \cdot (\vec{S}_{N} \times \vec{v}^{\perp})$$

$$\mathcal{O}_{13} = i (\vec{S}_{\chi} \cdot \vec{v}^{\perp})(\vec{S}_{N} \cdot \frac{\vec{q}}{m_{N}}); \quad \mathcal{O}_{14} = i (\vec{S}_{\chi} \cdot \frac{\vec{q}}{m_{N}})(\vec{S}_{N} \cdot \vec{v}^{\perp})$$

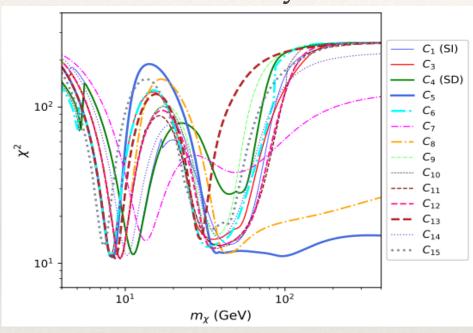
$$\mathcal{O}_{15} = -(\vec{S}_{\chi} \cdot \frac{\vec{q}}{m_{N}})((\vec{S}_{N} \times \vec{v}^{\perp}) \cdot \frac{\vec{q}}{m_{N}}),$$

$$\chi^{2}(m_{\chi},\sigma_{p},r) = \sum_{k=1}^{14} \frac{\left[S_{m,k} - S_{m,k}^{exp}(m_{\chi},\sigma_{p},r)\right]^{2}}{\sigma_{k}^{2}} \\ v_{min}^{2} = \frac{q^{2}}{4\mu_{T}^{2}} = \frac{m_{T}E_{R}}{2\mu_{T}^{2}}, \\ \text{A.L.Fitzpatrick, W.Haxton, E.Katz, N.Lubbers and Y.Xu, JCAP1302, 004}$$

(2013),1203.3542;

N.Anand, A.L.Fitzpatrick and W.C.Haxton, Phys.Rev.C89, 065501 (2014) 1308 6288

Likelihood analysis



$$\chi^2(m_\chi,\sigma_p,r) = \sum_{k=1}^{14} rac{\left[S_{m,k} - S_{m,k}^{exp}(m_\chi,\sigma_p,r)
ight]^2}{\sigma_k^2}$$

 $\overline{k=1}$ δ_k Sunghyun Kang, S.S., G. Tomar, J.H. Yoon,

$\mathbf{c}_{\mathbf{j}}$	$m_{\chi, min}$ (GeV)	$\mathbf{r}_{\chi, ext{min}}$	$\sigma \ (\mathrm{cm^2})$	χ^2_{\min}
c_1	11.17	-0.76	2.67e-38	11.38
	45.19	-0.66	1.60e-39	13.22
c_3	8.10	-3.14	2.27e-31	11.1
	35.68	-1.10	9.27e-35	14.23
	11.22	1.71	2.95e-36	11.38
c_4	44.71	-8.34	5.96e-36	27.7
	8.34	-0.61	1.62e-29	10.83
c_5	96.13	-5.74	3.63e-34	11.11
	8.09	-7.20	5.05e-28	11.11
c_6	32.9	-6.48	5.18e-31	12.74
	13.41	-4.32	4.75e-30	13.94
C7	49.24	-0.65	1.35e-30	38.09
	9.27	-0.84	8.67e-33	10.82
c ₈	42.33	-0.96	1.30e-34	11.6
0-	9.3	4.36	8.29e-33	10.69
<i>c</i> ₉	37.51	-0.94	1.07e-33	15.23
	9.29	3.25	4.74e-33	10.69
c_{10}	36.81	0.09	2.25e-34	12.40
	9.27	-0.67	1.15e-34	10.69
c_{11}	38.51	-0.66	9.17e-37	13.02
	9.26	-2.85	3.92e-34	10.69
c_{12}	35.22	-1.93	2.40e-35	12.47
0	8.65	-0.26	1.21e-26	10.76
c ₁₃	29.42	0.10	5.88e-29	14.28
0	10.28	-0.59	2.61e-26	11.21
c_{14}	38.88	-1.93	2.19e-27	14.48
0	7.32	-3.58	2.04e-27	12.91
c_{15}	33.28	4.25	2.05e-33	16.26

Nuclear response functions

coupling	$R_{0k}^{ au au'}$	$R_{1k}^{ au au'}$	coupling	$R_{0k}^{ au au'}$	$R_{1k}^{ au au'}$
1	$M(q^0)$	-	3	$\Phi''(q^4)$	$\Sigma'(q^2)$
4	$\Sigma''(q^0), \Sigma'(q^0)$	-	5	$\Delta(q^4)$	$M(q^2)$
6	$\Sigma''(q^4)$	-	7	-	$\Sigma'(q^0)$
8	$\Delta(q^2)$	$M(q^0)$	9	$\Sigma'(q^2)$	-
10	$\Sigma''(q^2)$	-	11	$M(q^2)$	-
12	$\Phi''(q^2), \tilde{\Phi}'(q^2)$	$\Sigma''(q^0), \Sigma'(q^0)$	13	$\tilde{\Phi}'(q^4)$	$\Sigma''(q^2)$
14	-	$\Sigma'(q^2)$	15	$\Phi''(q^6)$	$\Sigma'(q^4)$

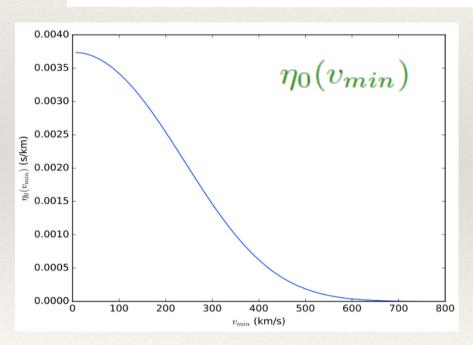
$$R_k^{\tau\tau'} = R_{0k}^{\tau\tau'} + R_{1k}^{\tau\tau'} \frac{(v_T^{\perp})^2}{c^2} = R_{0k}^{\tau\tau'} + R_{1k}^{\tau\tau'} \frac{v_T^2 - v_{\min}^2}{c^2}$$

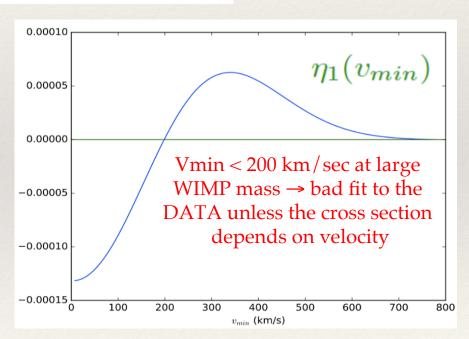
- •M= vector-charge (scalar, usual spin-independent part, non-vanishing for all nuclei)
- Φ "=vector-longitudinal, related to spin-orpit coupling σ ·l (also spin-independent, non-vanishing for all nuclei)
- • Σ ' and Σ '' = associated to longitudinal and transverse components of nuclear spin, <u>their sum is</u> the usual spin-dependent interaction, require nuclear spin <u>j>0</u>
- •∆=associated to the orbital angular momentum operator I, also requires j>0
- • $\mathring{\Phi}$ '= related to a vector-longitudinal operator that transforms as a tensor under rotations, requires j>1/2

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WIMP velocity distribution

$$\eta(v_{min}, t) = \int_{v_{min}}^{\infty} \frac{f(v)}{v} dv = \eta_0(v_{min}) + \eta_1(v_{min}) \cos \omega(t - t_0)$$

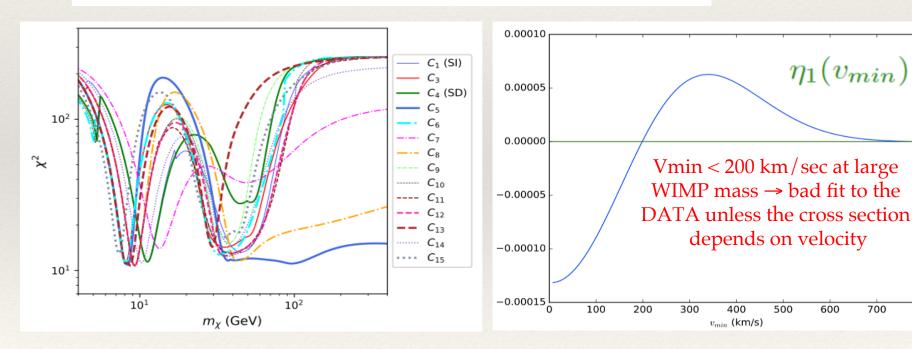




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* WIMP velocity distribution

$$\eta(v_{min}, t) = \int_{v_{min}}^{\infty} \frac{f(v)}{v} dv = \eta_0(v_{min}) + \eta_1(v_{min}) \cos \omega(t - t_0)$$



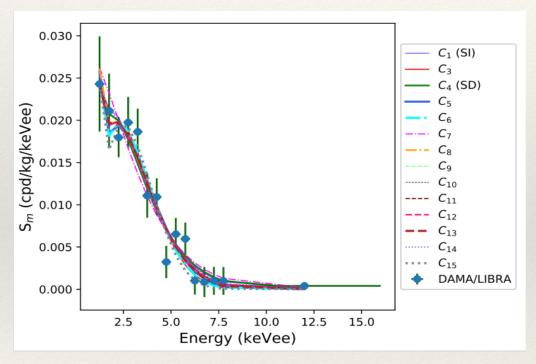
700

800

Sunghyun Kang, S.S., G. Tomar, J.H. Yoon,

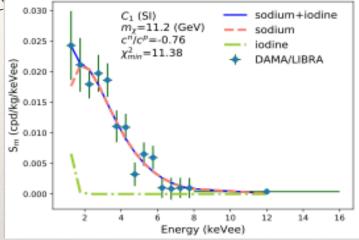
DAMA modulation amplitudes as a function of the measured ionization

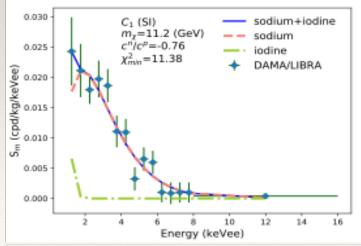
energy Eee for the absolute minima of each effec



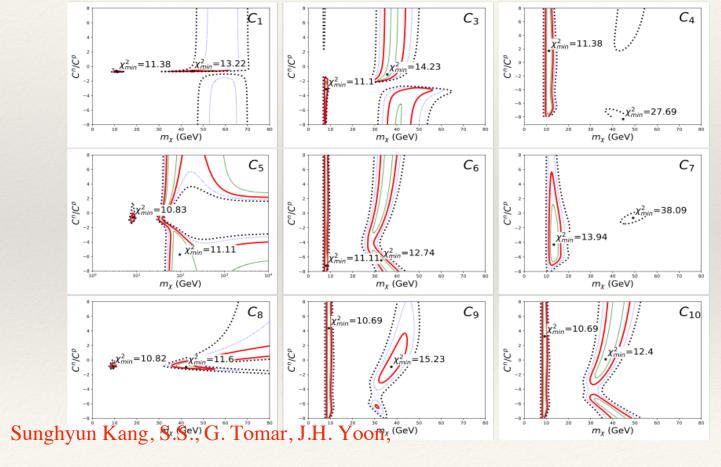
$$\sigma_{\chi N} \propto [c^p Z + (A - Z)c^n]^2$$

 $r_{Iodine} \simeq -53/(127-53) \simeq -0.7 \ (\simeq -0.9)$ for sodium Sunghyun Kang, S.S., G. Tomar, J.H. Yoon,

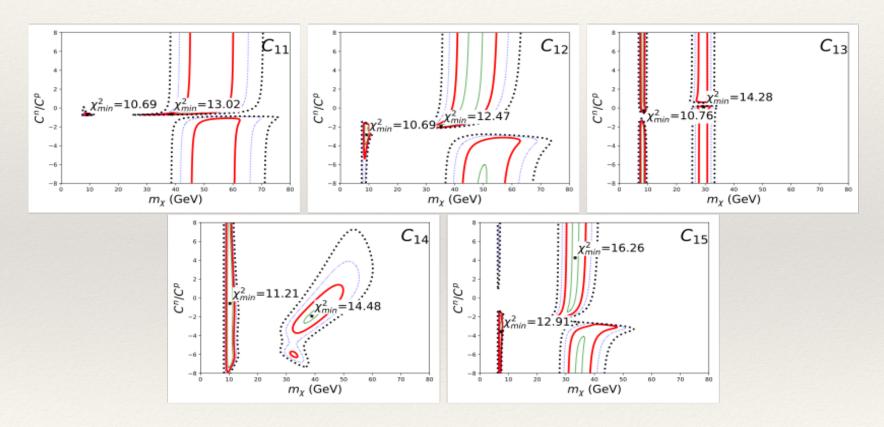




* Contour plots of χ 2 on the WIMP mass v.s. r plane

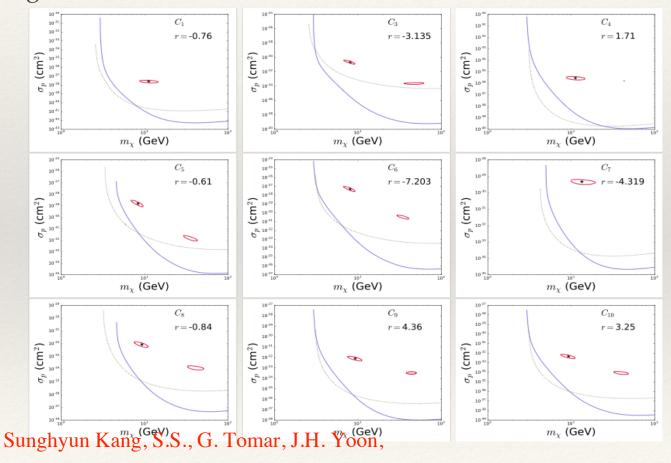


* Contour plots of χ^2 on the WIMP mass v.s. r plane

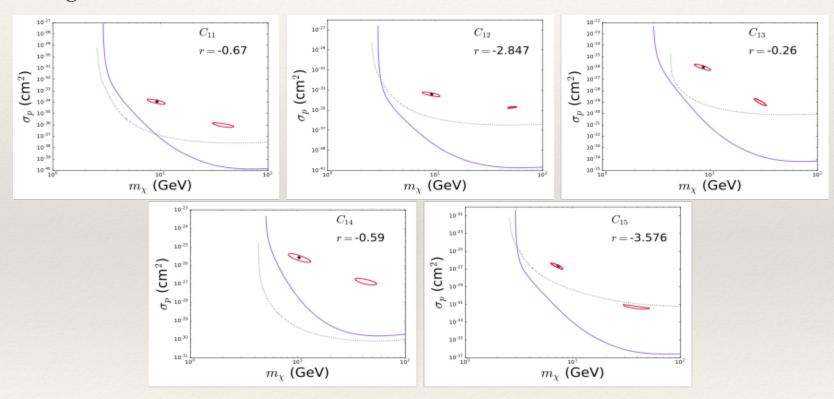


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 5-sigma best fit DAMA regions with XENON1T(solid purple line) and PICO60(green dots)



 5-sigma best fit DAMA regions with XENON1T(solid purple line) and PICO60(green dots)



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Conclusions

- No fit of the DAMA result is available in the literature in terms of non-relativistic EFT models
- * In addition to increasing the exposure, the phase2 result also includes a lower energy threshold, and the new spectrum of modulation amplitudes no longer shows a maximum, but is rather monotonically decreasing with energy
- We extended an assessment of the goodness of fit of the new DAMA result to NREFT scenarios
- * All models yield an acceptable $\chi 2$
- All best-fit minima are inconsistent with the bounds from XENON1T and PICO60

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