

# Recent results on $\tau$ -lepton decays with the *BABAR* detector

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on behalf of the *BABAR* collaboration

INFN Pisa and SNS Pisa

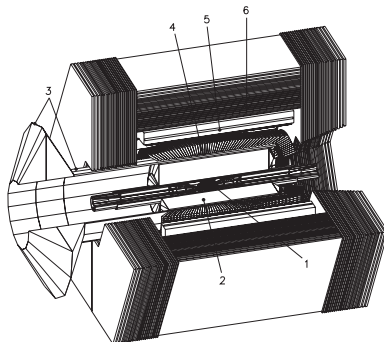
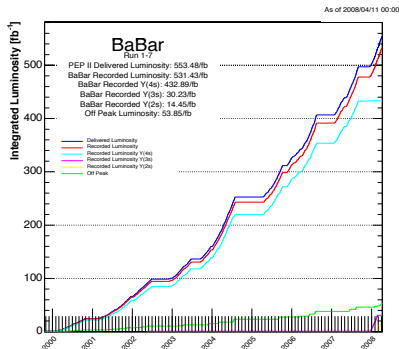
7th July 2018,  
at ICHEP 2018 in Seoul



# Outline

- Introduction and dataset
- Spectral function  $\tau^- \rightarrow K^- K_S \nu_\tau$ 
  - Introduction
  - Event selection
  - Results
- Branching fractions  $\tau^- \rightarrow h^- n \pi^0 \nu_\tau$ 
  - Introduction
  - Event selection
  - Results
- Summary

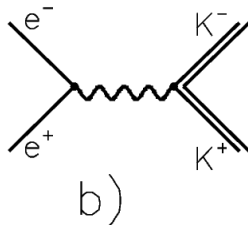
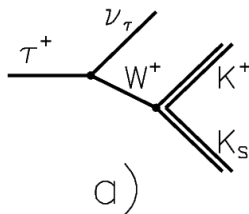
- *BABAR* detector: multi purpose experiment operated at PEP-II asymmetric  $B$  - Factory (1999 - 2008)
- dataset: around  $430 \times 10^6$  of  $e^+e^- \rightarrow \tau^+\tau^-$  events (at  $\sqrt{s} = 10.58$  GeV)



(1) silicon vertex tracker; (2) drift chamber; (3) Cherenkov detector; (4) electromagnetic calorimeter; (5) superconducting solenoid; (6) flux return and muon detector

## Motivation: spectral function $\tau^- \rightarrow K^- K_S \nu_\tau$

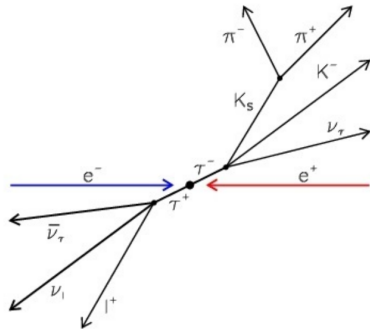
- $\tau$  lepton heavy enough to decay into light mesons
- can be used measure the spectral function:
  - $$V(q) = \frac{m_\tau^8}{12\pi C(q)|V_{ud}|^2} \frac{\mathcal{B}(\tau^- \rightarrow K^- K_S \nu_\tau)}{\mathcal{B}(\tau^- \rightarrow e^- \nu_\tau \bar{\nu}_e)} \frac{1}{N} \frac{dN}{dq}$$
- spectral function is related to the cross section for  $e^+e^- \rightarrow K\bar{K}$ :
  - $$\sigma_{e^+e^- \rightarrow K\bar{K}}^{I=1}(q) = \frac{4\pi^2\alpha^2}{q^2} V(q)$$
- input for the vacuum polarization corrections for g-2



# Event selection

## Selection requirements

- tag side:  $\tau^+ \rightarrow \ell^+ \bar{\nu}_\tau \nu_\ell$
- signal side:  $\tau^- \rightarrow K^- K_S \nu_\tau$
- 4 tracks from IP (total charge zero)
- quality cuts on tracks: good Particle IDentification (PID); and reject  $e^+e^- \rightarrow e^-e^+$  and  $e^+e^- \rightarrow \mu^-\mu^+$
- select events with event shapes compatible with  $\tau$  decays
- Particle IDentification (PID) for lepton ( $e^\pm$  or  $\mu^\pm$ ) and kaon (opposite charge)
- remaining 2 tracks:  $K_S \rightarrow \pi^-\pi^+$
- avg. selection efficiency  $\approx 13\%$



# Background subtraction

## Main background contributions:

- $\tau^- \rightarrow K^- K_S \pi^0 \nu_\tau$  (79%);
- $\tau^- \rightarrow \pi^- K_S \nu_\tau$  (10%);
- $\tau^- \rightarrow \pi^- K_S \pi^0 \nu_\tau$  (3%)
- mis-identified lepton (7%) from  $\tau^- \rightarrow \pi^- \nu_\tau$  and  $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$

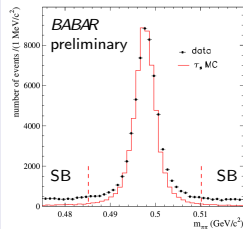
## Data driven background estimation

- background subtraction bin by bin in  $m_{K-K_S}$
- use data to subtract background decays containing  $\pi^0$  or have a mis-reconstructed  $K_S$
- subtract without simulation and assumption on invariant  $K^- K_S$  - mass
- only the remaining backgrounds are subtracted from MC

# Background subtraction

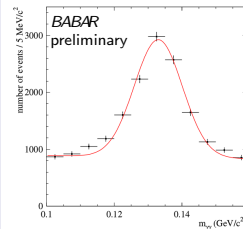
## Background from mis-reconstructed $K_S$

- subtract non- $K_S$  background using sidebands (SB) in  $m_{\pi^+\pi^-}$
- fraction of non-  $K_S$  bkg:  $\approx 10\%$  for  $m_{K-K_S} < 1.3 \text{ GeV}/c^2$  increases to up to 50% for  $m_{K-K_S} > 1.6 \text{ GeV}/c^2$  (mean  $m_{K-K_S} \approx 1.3 \text{ GeV}/c^2$ )



## Subtraction of background containing $\pi^0$

- reconstruct  $\pi^0 \rightarrow \gamma\gamma$  and sub-divide sample into events with at least one  $\pi^0$  and events without  $\pi^0$
- $\pi^0$  reconstruction efficiency estimated on MC  $\Rightarrow$  solve for number of signal events



# Systematic uncertainties

- several sources of systematic uncertainties
- estimated by varying inputs to this analysis

Sources	uncertainty (%)
Luminosity	0.5
Tracking efficiency	1.0
PID	0.5
non- $K_S$ background subtraction	0.4
$\tau^+ \tau^-$ background without $\pi^0$	0.3
$\tau^+ \tau^-$ background with $\pi^0$	2.3
$q\bar{q}$ background	0.5
total	2.7

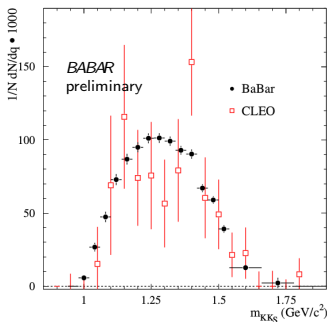


# Results

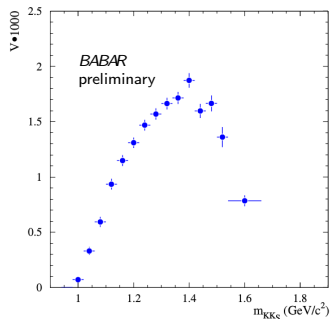
## Branching fraction estimation

- $N_{exp} = 223741 \pm 3461$  (stat uncert. only, efficiency corrected)
- $\mathcal{B}(\tau^- \rightarrow K^- K_S \nu_\tau) = \frac{N_{exp}}{2\mathcal{L}\mathcal{B}_{lep}\sigma_{\tau\tau}} = (0.739 \pm 0.011 \pm 0.020) \times 10^{-3}$

## Efficiency corrected yield



## Resulting spectral function

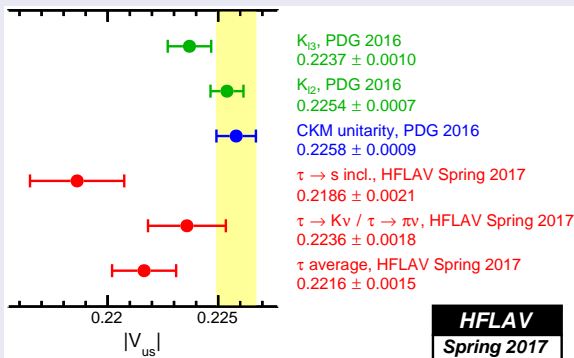


# Branching fractions $\tau^- \rightarrow h^- n \pi^0 \nu_\tau$ ( $h = K; \pi; n = 0..4$ )

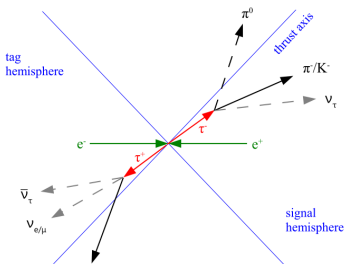
## Motivation

- $\tau$  decays with neutrals in final state poorly measured
- input to  $|V_{us}|_{incl}$  estimated from  $\tau \rightarrow s$  inclusive

$|V_{us}|_{incl}$  current tension with other  $|V_{us}|$  estimates:



# Event selection $\tau^- \rightarrow h^- n \pi^0 \nu_\tau$



## Selection requirements

- two oppositely charged tracks from IP:  $\ell^\pm$  (tag),  $K^\pm$  or  $\pi^\pm$  (sig.)
- quality cuts on track and photon
- reconstruct up to 4  $\pi^0 \rightarrow \gamma\gamma$
- reject events with additional photons
- event topology consistent with  $\tau$  decay
- cuts on missing mass of event and signal  $\tau$ -decay to reject bkg.  
 $(e^+e^- \rightarrow \ell^+\ell^-, \tau \rightarrow \eta X \nu)$
- reject two-photon events:

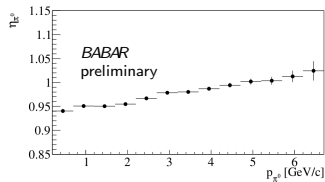
$$\frac{p_T}{E_{miss}} = \frac{(\vec{p}_1^{CM} + \vec{p}_2^{CM})_T}{\sqrt{s} - p_1^{CM} - p_2^{CM}} > 0.2$$

## $\pi^0$ efficiency correction

- compare control channels  
 $\tau^- \rightarrow t^- \nu_\tau$  with  $\tau^- \rightarrow t^- \pi^0 \nu_\tau$   
 (track  $t$  no PID except  $e^\pm$ -veto)
- correction factor:  $\eta =$   

$$\frac{N(\tau^- \rightarrow t^- \pi^0 \nu_\tau)_{data}}{N(\tau^- \rightarrow t^- \pi^0 \nu_\tau)_{MC}} \frac{N(\tau^- \rightarrow t^- \nu_\tau)_{MC}}{N(\tau^- \rightarrow t^- \nu_\tau)_{data}}$$
- applied to each reconstructed  $\pi^0$   
 in MC as function of  $p_{\pi^0}$

## distribution of the $\pi^0$ efficiency correction factor



## Correction of PID efficiency

- standard *BABAR* PID: correct for data MC difference
- custom correction:  $\pi^\pm$  as  $\pi^\pm$ ,  $K^\pm$  as  $K^\pm$  PID;  $\pi^\pm$  as  $K^\pm$  mis-ID
  - use control samples of 3-1-topology  $\tau\tau$  - events:
    - $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$
    - $\tau^- \rightarrow \pi^- K^+ K^- \nu_\tau$
  - identify 2 of the three tracks  $\Rightarrow$  ID third track

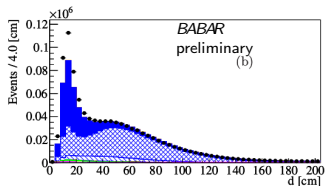
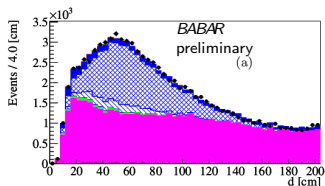
## Split-off correction

- *Split-offs*: separated neutrons from hadronic showers in the EMC can travel and cause a shower which is then identified as photon
- not well modeled in MC  $\Rightarrow$  apply correction obtained on data
- use the  $\tau^- \rightarrow \pi^- \nu_\tau$  control channel
- correction factor  

$$\eta = \frac{N^{data}(d < 40 \text{ cm}) - N^{MC}(d < 40 \text{ cm})}{N^{data}}$$
- applied to each simulated event with hadron

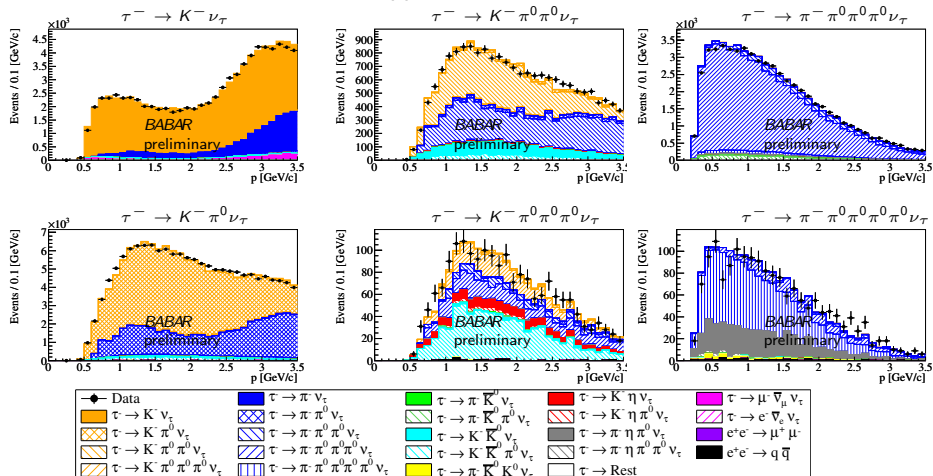
### Distance to closest neutral cluster

- a)  $\tau^- \rightarrow \mu^- \nu_\tau \bar{\nu}_\mu$
- b)  $\tau^- \rightarrow \pi^- \nu_\tau$



# Reconstructed signal hadron momentum

- data - MC comparison after event selection
- all corrections to MC applied



## Signal extraction

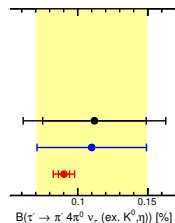
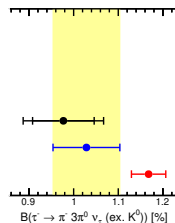
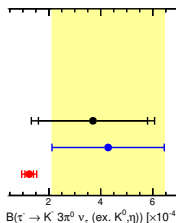
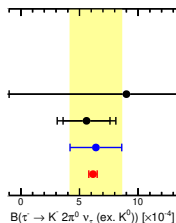
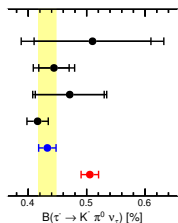
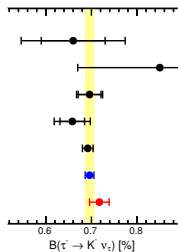
- signal events reconstructed in the wrong signal channel are taken into account
- use *migration matrix*  $\mathbf{M} = M_{ki}$ :
  - element  $M_{ki}$ : probability of reconstructing true signal  $k$  in reconstruction channel  $i$  estimated on MC
- inverting  $\mathbf{M}$  and solve linear equation:
  - $\vec{N}^{prod} = \mathbf{M}^{-1} \left( \vec{N}^{sel} - \sum_l \vec{N}_{rest(l)}^{sel} \right)$ 
    - $\vec{N}^{prod}$ : true produced signal events
    - $\vec{N}^{sel}$ : measured number of selected data events
    - $\vec{N}_{rest(l)}^{sel}$ : number of selected non-signal bkg. events taken from MC prediction
- branching fractions are then calculated as:  $\mathcal{B} = 1 - \sqrt{1 - \frac{N^{prod}}{\mathcal{L}\sigma}}$   
 (takes into account that both  $\tau$  in the event can decay to signal final state)

- several sources systematic uncertainties evaluated using toys:
  - vary inputs according to their uncertainty
  - assign RMS of results as uncertainty
- additional syst. uncertainties currently investigated: MC modeling

$\tau^-$ - Decay mode	$K^- \nu_\tau$ ( $\times 10^{-3}$ )	$K^- \pi^0 \nu_\tau$ ( $\times 10^{-3}$ )	$K^- 2\pi^0 \nu_\tau$ ( $\times 10^{-4}$ )	$K^- 3\pi^0 \nu_\tau$ ( $\times 10^{-4}$ )	$\pi^- 3\pi^0 \nu_\tau$ ( $\times 10^{-2}$ )	$\pi^- 4\pi^0 \nu_\tau$ ( $\times 10^{-4}$ )
Branching fraction	7.174	5.054	6.151	1.246	1.168	9.020
Stat. uncertainty	0.033	0.021	0.117	0.164	0.006	0.400
Syst. uncertainty	0.213	0.148	0.338	0.238	0.038	0.652
Total uncertainty	0.216	0.149	0.357	0.289	0.038	0.765
Stat. uncertainty [%]	0.46	0.41	1.91	13.13	0.52	4.44
Syst. uncertainty [%]	2.97	2.93	5.49	19.12	3.23	7.23
Total uncertainty [%]	3.00	2.95	5.81	23.19	3.27	8.48
$\epsilon_{signal}$ [%]	0.27	0.27	0.87	3.99	0.27	1.50
$\epsilon_{bkg}$ [%]	0.15	0.15	0.87	6.32	0.11	1.67
Background $\mathcal{B}$ 's [%]	0.18	0.30	1.44	11.52	0.21	3.49
BABAR PID [%]	0.15	0.11	0.18	0.71	0.08	0.20
Custom PID [%]	1.83	1.55	1.78	2.56	0.20	0.26
Muon mis-id [%]	1.48	0.01	0.00	0.00	0.00	0.00
# $\tau^+ \tau^-$ pairs [%]	0.79	0.93	1.40	2.61	0.71	0.98
Track efficiency [%]	0.43	0.50	0.76	1.42	0.38	0.53
Split-off correction [%]	1.52	1.84	2.77	5.17	1.40	1.94
$\pi^0$ correction [%]	0.03	1.20	3.63	10.56	2.76	5.36
$\pi 5\pi^0 \rightarrow \pi 4\pi^0$ migr. [%]	0.00	0.00	0.00	0.02	0.04	1.08
$K 4\pi^0 \rightarrow K 3\pi^0$ migr. [%]	0.00	0.00	0.13	4.78	0.00	0.00



- comparison results **this analysis**, **HFLAV average**, and selection of measurements
- NOTE: HFLAV averages contain more inputs than shown here



## Summary spectral function $\tau^- \rightarrow K^- K_S \nu$

- most precise determination of spectral function for  $\tau^- \rightarrow K^- K_S \nu$
- preprint server: arXiv:1806.10280 (SLAC-PUB-17286)
- is submitted to PRD

## Summary branching fraction measurements $\tau^- \rightarrow h^- n \pi^0 \nu$

- reconstructed signal channels:
  - $\tau^- \rightarrow K^- n \pi^0 \nu$ ,  $n=0\dots3$
  - $\tau^- \rightarrow \pi^- n \pi^0 \nu$ ,  $n=3,4$
- for most channels most precise result up to now
- analysis in final stage of approval by collaboration
- publication in preparation
- results for  $|V_{us}|$  added soon

# Backup

# Numerical results $\tau^- \rightarrow h^- n \pi^0 \nu_\tau$

$$\begin{aligned}
 \mathcal{B}(\tau^- \rightarrow K^- \nu_\tau) &= (7.174 \pm 0.033 \pm 0.213) \times 10^{-3}, \\
 \mathcal{B}(\tau^- \rightarrow K^- \pi^0 \nu_\tau) &= (5.054 \pm 0.021 \pm 0.148) \times 10^{-3}, \\
 \mathcal{B}(\tau^- \rightarrow K^- 2\pi^0 \nu_\tau) &= (6.151 \pm 0.117 \pm 0.338) \times 10^{-4}, \\
 \mathcal{B}(\tau^- \rightarrow K^- 3\pi^0 \nu_\tau) &= (1.246 \pm 0.164 \pm 0.238) \times 10^{-4}, \\
 \mathcal{B}(\tau^- \rightarrow \pi^- 3\pi^0 \nu_\tau) &= (1.168 \pm 0.006 \pm 0.038) \times 10^{-2}, \\
 \mathcal{B}(\tau^- \rightarrow \pi^- 4\pi^0 \nu_\tau) &= (9.020 \pm 0.400 \pm 0.652) \times 10^{-4},
 \end{aligned}$$

# Number of selected events $\tau^- \rightarrow h^- n \pi^0 \nu_\tau$

Selected mode	data	bkg from MC	$\epsilon$ from MC [%]
$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$	1075810	62364.0	0.74
$\tau^- \rightarrow \pi^- \nu_\tau$	1473594	340960.0	1.278
$\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$	6742483	368918.5	3.28
$\tau^- \rightarrow \pi^- 2\pi^0 \nu_\tau$	1268108	75058.7	1.55
$\tau^- \rightarrow \pi^- 3\pi^0 \nu_\tau$	58598	9698.1	0.49
$\tau^- \rightarrow \pi^- 4\pi^0 \nu_\tau$	1706	729.5	0.12
$\tau^- \rightarrow K^- \nu_\tau$	80715	18669.3	0.99
$\tau^- \rightarrow K^- \pi^0 \nu_\tau$	146948	51983.2	2.16
$\tau^- \rightarrow K^- 2\pi^0 \nu_\tau$	17930	11128.8	1.34
$\tau^- \rightarrow K^- 3\pi^0 \nu_\tau$	1863	1467.7	0.13

# Numerical results for the spectral function of $\tau \rightarrow K^- K_S \nu_\tau$

$m_{K^- K_S} (\text{GeV}/c^2)$	$N_s/N_{tot} \times 10^3$	$V \times 10^3$
0.98 – 1.02	$5.6 \pm 1.4$	$0.071 \pm 0.018 \pm 0.006$
1.02 – 1.06	$26.0 \pm 2.7$	$0.331 \pm 0.034 \pm 0.026$
1.06 – 1.10	$46.0 \pm 3.2$	$0.593 \pm 0.042 \pm 0.042$
1.10 – 1.14	$70.8 \pm 3.5$	$0.934 \pm 0.046 \pm 0.056$
1.14 – 1.18	$84.4 \pm 3.4$	$1.148 \pm 0.047 \pm 0.057$
1.18 – 1.22	$92.3 \pm 3.3$	$1.309 \pm 0.046 \pm 0.052$
1.22 – 1.26	$98.2 \pm 3.2$	$1.468 \pm 0.048 \pm 0.044$
1.26 – 1.30	$98.4 \pm 3.2$	$1.569 \pm 0.050 \pm 0.042$
1.30 – 1.34	$96.3 \pm 3.0$	$1.663 \pm 0.052 \pm 0.042$
1.34 – 1.38	$90.2 \pm 2.9$	$1.715 \pm 0.052 \pm 0.039$
1.38 – 1.42	$87.8 \pm 3.1$	$1.873 \pm 0.066 \pm 0.039$
1.42 – 1.46	$65.1 \pm 2.6$	$1.597 \pm 0.064 \pm 0.032$
1.46 – 1.50	$57.3 \pm 2.5$	$1.666 \pm 0.073 \pm 0.032$
1.50 – 1.54	$38.1 \pm 2.5$	$1.361 \pm 0.090 \pm 0.023$
1.54 – 1.66	$36.9 \pm 2.4$	$0.785 \pm 0.049 \pm 0.013$
1.66 – 1.78	$6.6 \pm 10.2$	$0.986 \pm 1.520 \pm 0.014$

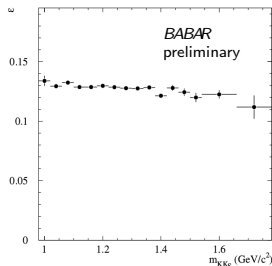
- reference: arXiv:1806.10280
- Shown uncertainties are statistical and systematic, respectively.

# Event selection

## Selection requirements

- 4 tracks from IP (total charge zero)
- Particle IDentification (PID) for lepton ( $e^\pm$  or  $\mu^\pm$ ) and kaon (opposite charge)
- quality cuts on track momentum and angle: good PID; and reject  $e^+e^- \rightarrow e^-e^+$  and  $e^+e^- \rightarrow \mu^-\mu^+$
- remaining tracks:  $K_S \rightarrow \pi^-\pi^+$  with  $m_{\pi\pi}$  within 25 MeV of  $m(K_S)$
- flight length of  $K_S > 1\text{cm}$
- $\sum E_{\text{neutral}} < 2\text{GeV}$
- $\text{Thrust} > 0.875$  (charged tracks)
- angle  $KK_S$  - lepton  $> 110^\circ$

## Selection efficiency as function of $m_{KK_S}$



- average selection efficiency  $\approx 13\%$

## Signal extraction by migration matrix method

- number of selected signal events for reconstructed channel  $i$  can be written as:

$$N_{sig}^{sel(i)} = N^{sel(i)} - \sum_{j \neq i} N_j^{sel(i)} - \sum_l N_{rest(l)}^{sel(i)}$$

- this can be rewritten as matrix equation relating the number of produced event  $N^{prod}$  with the selected events:

$$\sum_j M_{ij} N^{prod(j)} = N^{sel(i)} - \sum_l N_{rest(l)}^{sel(i)}$$

where  $M_{ij}$  is the probability to reconstruct the signal decay  $j$  in reconstructed channel  $i$ , estimated on MC

- by inverting the matrix  $\mathbf{M} = M_{ij}$  one obtains a relation between the number of produced events  $\vec{N}^{prod}$ , the number selected data events  $\vec{N}^{sel}$ , and the number of non-signal bkg events  $\vec{N}_{rest}^{sel}$ :

$$\vec{N}^{prod} = \mathbf{M}^{-1} \left( \vec{N}^{sel} - \sum_l \vec{N}_{rest(l)}^{sel} \right)$$

- $\vec{N}_{rest(l)}^{sel}$  is taken from MC prediction

- branching fractions are then calculated as:  $B = 1 - \sqrt{1 - \frac{N^{prod}}{\mathcal{L}\sigma}}$



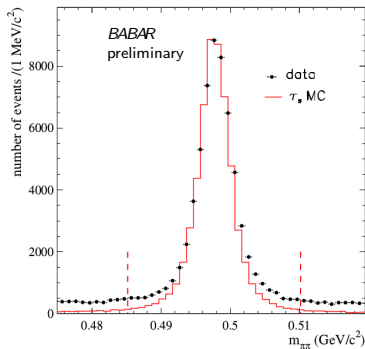
# Subtraction of non- $K_S$ background

- subtract non- $K_S$  background by using sidebands and assuming a flat distribution
  - reconstructed events composed of background and true  $K_S$   

$$N = N_{K_S} + N_b$$
  - number of events in the side-band:  

$$N_{sb} = \alpha N_b + \beta N_{K_S}$$
  - solve for the number of true  $K_S$ :  $N_{K_S} = \frac{\alpha N - N_{sb}}{\alpha - \beta}$
- subtract bin by bin in  $m_{KK_S}$
- fraction of non-  $K_S$  bkg:  
 $\approx 10\%$  for  $m_{KK_S} < 1.3\text{GeV}$   
 increases to up to 50% for  $m_{KK_S} > 1.6\text{GeV}$

## Reconstructed invariant mass of $K_S$ candidates

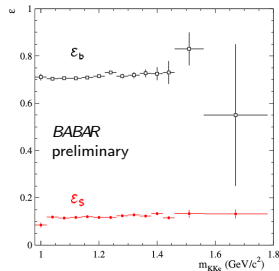
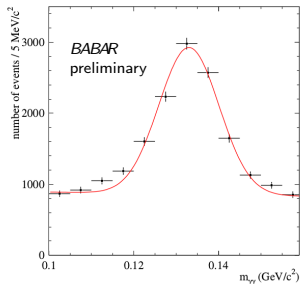


# Subtraction of background including $\pi^0$

- main bkg contributions:
  - $\tau^- \rightarrow K^- K_S^0 \nu_\tau$  (79%);
  - $\tau^- \rightarrow \pi^- K_S^0 \nu_\tau$  (10%);
  - $\tau^- \rightarrow \pi^- K_S^0 \nu_\tau$  (3%)
  - mis-identified lepton (7%) from  
 $\tau^- \rightarrow \pi^- \nu_\tau$  and  $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$
- reconstruct  $\pi^0$  and sub-divide sample:
  - at least one  $\pi^0$ :  

$$N_{1\pi^0} = \epsilon_s N_s + \epsilon_b N_b$$
  - zero  $\pi^0$ :  

$$N_{0\pi^0} = (1 - \epsilon_s) N_s + (1 - \epsilon_b) N_b$$
- solve for number of signal events  $N_s$
- remaining bkg. subtracted using MC



# Event Selection

## Event selection $\tau^- \rightarrow h^- n \pi^0 \nu_\tau$

- two oppositely charged tracks from IP: PID  $\ell^\pm$  (tag),  $K^\pm$  or  $\pi^\pm$  (sig.)
- reconstruct up to 4  $\pi^0 \rightarrow \gamma\gamma$
- reject events with additional photons
- several track and photon quality cuts: ensure good PID; reject bkg
- $0.88 < \text{thrust of event } T < 0.99$
- angle between lepton and signal hadron  $> 2.95 \text{ rad}$
- cuts on missing mass of event and signal  $\tau$ -decay to reject bkg.  
 ( $e^+e^- \rightarrow \ell^+\ell^-$ )
- reject two-photon events:  $\frac{p_T}{E_{\text{miss}}} = \frac{(\vec{p}_1^{CM} + \vec{p}_2^{CM})_T}{\sqrt{s} - p_1^{CM} - p_2^{CM}} > 0.2$