

# **Electroweak Symmetry Breaking by a Neutral Sector : Dynamical Relaxation of the Little Hierarchy Problem**

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- The **naturalness** problem of **EW scale** and **Higgs boson mass** has been the most important issue for last four decades.
- The **MSSM** has been the most promising BSM candidate.
- **No evidence** of **BSM** has been observed yet at LHC.
  - **Theoretical puzzles** raised in the SM still remain **UNsolved**.
- **A barometer** of **the solution** to the naturalness problem is the **stop mass** .
  - The **stop mass** bound has been already **> 1 TeV**.
  - (The **gluino mass** bound has exceeded **> 2 TeV**.)
  - They start threatening the traditional status of SUSY as a solution to the naturalness problem of the EW phase transition.

- ATLAS and CMS have discovered the **SM(-like) Higgs with 125 GeV mass**, which is too heavy as a SUSY Higgs.
- According to the recent analyses, **10-20 TeV stop mass** is necessary **for the 125 GeV Higgs mass** (without a large stop mixing).

$$\Delta m_{h_u}^2|_{1\text{-loop}} \approx \frac{3|y_t|^2}{8\pi^2} \tilde{m}_t^2 \log\left(\frac{\tilde{m}_t^2}{\Lambda^2}\right) \left[1 + \frac{1}{2} \frac{A_t^2}{\tilde{m}_t^2}\right],$$

$$\Delta m_H^2|_{1\text{-loop}} \approx \frac{3m_t^4}{4\pi^2 v_h^2} \left[ \log\left(\frac{\tilde{m}_t^2}{m_t^2}\right) + \frac{A_t^2}{\tilde{m}_t^2} \left(1 - \frac{1}{12} \frac{A_t^2}{\tilde{m}_t^2}\right) \right],$$

$$\frac{1}{2} m_Z^2 = \frac{m_{h_d}^2 - m_{h_u}^2 \tan^2 \beta}{\tan^2 \beta - 1} - |\mu|^2.$$

- ATLAS and CMS have discovered the **SM(-like) Higgs with 125 GeV mass**, which is too heavy as a SUSY Higgs.
- According to the recent analyses, **10-20 TeV stop mass** is necessary **for the 125 GeV Higgs mass** (without a large stop mixing).

A **fine-tuning of  $10^{-3} - 10^{-4}$**   
seems to be **unavoidable !! ??**

- Recently some new ideas (without SUSY) have been suggested to relax the gauge hierarchy problem.
- For UV completion, however, embedding them in SUSY also have been discussed.

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We will attempt to address  
the (little) hierarchy problem  
in the **SUSY** framework.

# Little Hierarchy Problem

$$|\mu|^2 + \frac{1}{2}M_Z^2 = \frac{m_{h_d}^2 - m_{h_u}^2 \tan^2 \beta}{\tan^2 \beta - 1}$$

Why is  $M_Z^2$  [=  $(g_2^2 + g_Y^2)(v_u^2 + v_d^2)/2$ ] **so small** compared to **the soft masses** ?

$$[v_u^2 + v_d^2 \equiv \langle |H|^2 \rangle = (174 \text{ GeV})^2]$$

# Problems in SUSY models

## Gravity Mediated SUSY Breaking mech.

$\mu$  and  $B\mu$  terms are O.K.

But Flavor and CP problems would arise.

## Gauge Mediated SUSY Breaking mech.

Flavor and CP problems are absent.

But  $\mu$  and  $B\mu$  problems would be serious.



# A funny model

$$V = M^2 |H|^2 + m^2 |\phi|^2 + \lambda^2 |H|^2 |\phi|^2 + \delta V$$

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$$\begin{aligned}(\lambda^2 |H|^2 + m^2) \phi + \partial \delta V / \partial \phi^* &= 0, \\(\lambda^2 |\phi|^2 + M^2) H + \partial \delta V / \partial H^* &= 0.\end{aligned}$$

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▪ An interesting extrm. Point: If  $\partial \delta V / \partial \phi^*$  is negligible,

$$|H|^2 = -m^2 / \lambda^2, \quad |\phi|^2 = -M^2 / \lambda^2 - g^2 m^2 / \lambda^4$$

# A funny model

$\phi$  becomes massless, and so  
it can get a large VEV.

***$\phi$  compensates the large  $M^2$ .***

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***$\phi$  compensates the large  $M^2$ .***

$$(\lambda^2 |H|^2 + m^2) + \partial \mathcal{V} / \partial \phi^* = 0,$$

If  $m^2 \ll M^2$ ,

***a small  $m^2$  is responsible for  
the small Higgs VEV.***

If  $\phi \gg v$

$$|H|^2 = -m^2/\lambda, \quad |\phi|^2 = m^2/\lambda^2 - g^2 m^2/\lambda^4$$

# A funny model

$\phi$  becomes massless, and so  
it can get a large VEV.

*$\phi$  compensates the large  $M^2$ .*

**BUT such a point is a saddle point of  $V$ !!**

The mixing btw  $H$  and  $\phi$  is almost maximal.  
One of the mass E.state is tachyonic.

If

$\lambda^4$

# A funny model

1. Why is  $\partial\delta V/\partial\phi^*$  negligible?

$$V = M^2 |H|^2 + m^2 |\phi|^2 + \lambda^2 |H|^2 |\phi|^2 + \delta V$$

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How can a relatively small  $m^2$  be generated?

How can the smallness of  $m^2$  be maintained?

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3. How can the *mixing btw H and  $\phi$*  be suppressed?

# A funny model

1. Why is  $\partial\delta V/\partial\phi^*$  negligible?

Introduce **SUSY**.

$\Phi$  can be a **flat direction** in the SUSY limit.

How can a relatively small  $m^2$  be generated?

How can the smallness of  $m^2$  be maintained?

$$(\lambda^2|\phi|^2 + M^2)\pi + \partial\delta V/\partial H^* = 0.$$

3. How can the **mixing btw  $H$  and  $\phi$**   
**be suppressed?**

# A funny model

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How can a relatively small  $m^2$  be generated?

How can the smallness of  $m^2$  be maintained?

Introduce both **gravity-** and **gauge-mediated SUSY breaking mech.,**

assuming **gauge mediated effects dominate.**

The **messenger scale** of gauge med. needs to be **low** enough.

# A funny model

1. Why is  $\partial\delta V/\partial\phi^*$  negligible?

$\lambda^2$  needs **small** enough.

$$V = M^2 |\phi|^2 + \delta V$$

2. Why  $m^2 \ll M^2$ ?

How can a relatively small  $m^2$  be generated?

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$$(\lambda^2 |\phi|^2 + M^2) H + \partial\delta V/\partial H^* = 0.$$

3. How can the *mixing btw H and  $\phi$*  be suppressed?

By more singlets

# Model

$$W = (\lambda_1 X + \lambda_2 \phi + \mu) \text{ h u h d} + M XY + (\kappa/2) Y\phi^2$$

# Model

$$W = (\lambda_1 X + \lambda_2 \phi + \mu) h_u h_d + M XY + (\kappa/2) Y \phi^2$$

$$W_{UV} \supset \Psi (y_1 X_1 + y_2 X_2) Z + y_3 \Psi^c Z \phi \\ + (y_4 X_1 + y_5 X_2) h_u h_d + \frac{(\Psi^c)^2}{M_P} (y_6 X_1 + y_7 X_2) Y + \frac{\kappa}{2} Y \phi^2,$$

Superfields	$X_{1,2}$	$Y$	$Z$	$\phi$	$\Psi$	$\Psi^c$
$U(1)_{PQ}$	-1	4/3	5/6	-2/3	1/6	-1/6

# Model

$$W = (\lambda_1 X + \lambda_2 \phi + \mu) h_u h_d + M XY + (\kappa/2) Y \phi^2$$

$$V \supset |H|^2 |\lambda_1 X + \lambda_2 \phi + \mu|^2 + |\lambda_1 h_u h_d + M Y|^2 + \left| \frac{\kappa}{2} \phi^2 + M X \right|^2 \\ + |\lambda_2 h_u h_d + \kappa Y \phi|^2 + m_X^2 |X|^2 + m_Y^2 |Y|^2 + m_\phi^2 |\phi|^2 \\ + \left\{ (\lambda_1 a_1 X + \lambda_2 a_2 \phi) h_u h_d + M b X Y + \frac{\kappa}{2} a Y \phi^2 + \text{h.c.} \right\},$$

where  $|H|^2 \equiv |h_u|^2 + |h_d|^2$



# Model

$$W = (\lambda_1 X + \lambda_2 \phi + \mu) h_u h_d + M XY + (\kappa/2) Y \phi^2$$

$$V \supset |H|^2 |\lambda_1 X + \lambda_2 \phi + \mu|^2 + |\lambda_1 h_u h_d + MY|^2 + \underbrace{\left| \frac{\kappa}{2} \phi^2 + MX \right|^2}_{\text{red underline}} \\ + |\lambda_2 h_u h_d + \kappa Y \phi|^2 + m_X^2 |X|^2 + m_Y^2 |Y|^2 + m_\phi^2 |\phi|^2 \\ + \left\{ (\lambda_1 a_1 X + \lambda_2 a_2 \phi) h_u h_d + MbXY + \frac{\kappa}{2} a Y \phi^2 + \text{h.c.} \right\},$$

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# Model

$$W = (\lambda_1 X + \lambda_2 \phi + \mu) h_u h_d + M XY + (\kappa/2) Y \phi^2$$

$$V \supset |H|^2 |\lambda_1 X + \lambda_2 \phi + \mu|^2 + |\lambda_1 h_u h_d + MY|^2 + \underbrace{\left| \frac{\kappa}{2} \phi^2 + MX \right|^2}_{=0} + |\lambda_2 h_u h_d|^2$$

$$(\kappa/2)\phi^2 + MX = 0$$

***FLAT direction (= modulus-like)***

***in SUSY limit, with  $h_u = h_d = Y = 0$***

where  $|H|^2 = \frac{1}{2} \mu^2$

# Model

$$W = (\lambda_1 X + \lambda_2 \phi + \mu) h_u h_d + M XY + (\kappa/2) Y \phi^2$$

$$V \supset |H|^2 |\lambda_1 X + \lambda_2 \phi + \mu|^2 + |\lambda_1 h_u h_d + MY|^2 + \left| \frac{\kappa}{2} \phi^2 + MX \right|^2$$

Suppose

$$m_X^2, m_Y^2, m_\phi^2, a, b, \text{ etc.}$$

$$\sim O(m^2) \ll \text{MSSM soft para.}$$

where  $|H|^2 \equiv |h_u|^2 + |h_d|^2$

# Effective $\mu$ and $B\mu$

$$\mu_{\text{eff}} = \lambda_1 \langle X \rangle + \lambda_2 \langle \phi \rangle + \mu,$$

$$B\mu_{\text{eff}} = (\lambda_1 M^* + \lambda_2 \kappa^* \langle \phi^* \rangle) \langle Y^* \rangle + \lambda_1 a_1 \langle X \rangle + \lambda_2 a_2 \langle \phi \rangle + B\mu,$$

# Extreme Conditions

extreme conditions for  $X$ ,  $Y$ , and  $\phi$

$$\left\{ \begin{array}{l} \mathcal{M}_X^2 X + M^* b^* Y^* = -\frac{\kappa}{2} M^* \phi^2 - (\lambda_2 \phi + \mu) \lambda_1^* |H|^2 \\ \quad - \lambda_1^* a_1^* h_u^* h_d^*, \\ \mathcal{M}_Y^2 Y^* + MbX = -\frac{\kappa}{2} a \phi^2 - (\lambda_1^* M + \lambda_2^* \kappa \phi) h_u^* h_d^*, \\ (|\kappa Y|^2 + |\lambda_2 H|^2 + m_\phi^2) \phi + \left(\frac{\kappa}{2} \phi^2 + MX\right) \kappa^* \phi^* \\ \quad + (\lambda_1 X + \mu) \lambda_2^* |H|^2 + \lambda_2^* a_2^* h_u^* h_d^* \\ \quad + (\lambda_2 h_u h_d + a^* \phi^*) \kappa^* Y^* = 0. \end{array} \right.$$

# Solutions of Extrim. Condi.

$$X \approx \frac{-\kappa\phi^2}{2\mathcal{M}_X^2} M^* \left[ 1 - \frac{(a-b)b^*}{\mathcal{M}_Y^2} + \frac{2(\lambda_2\phi + \mu)\lambda_1^*|H|^2}{\kappa\phi^2 M^*} \right],$$
$$Y^* \approx \frac{-\kappa\phi^2}{2\mathcal{M}_Y^2} (a-b) - \frac{(\lambda_1^* M + \lambda_2^* \kappa\phi) h_u^* h_d^*}{\mathcal{M}_Y^2}.$$

where  $\mathcal{M}_X^2 \equiv |\lambda_1 H|^2 + m_X^2 + |M|^2 \quad (\approx |M|^2)$

$$\mathcal{M}_Y^2 \equiv |\kappa\phi|^2 + m_Y^2 + |M|^2$$

# Extrm. Condi. for $\Phi$

The extremum condition for  $T_\zeta$  ( $\equiv \kappa\phi/M$ )

$$\begin{aligned} \frac{1}{2}|T_\zeta|^2 (|\lambda_1 H|^2 + \underline{m_X^2}) - T_\zeta^* \left( \lambda_2 + \frac{\mu}{\phi} \right) \lambda_1^* |H|^2 - \frac{1}{2} T_\zeta \lambda_2^* \lambda_1 |H|^2 \\ + \frac{\mu}{\phi} \lambda_2^* |H|^2 + (|\lambda_2 H|^2 + \underline{m_\phi^2}) \approx \frac{|T_\zeta|^2 (|T_\zeta|^2 + 2)}{4(|T_\zeta|^2 + 1)^2} \underline{|a - b|^2}, \end{aligned}$$

# Extrm. Condi. for $\Phi$

The extremum condition for  $T_\zeta$  ( $\equiv \kappa\phi/M$ )

$$\frac{1}{2}|T_\zeta|^2 (|\lambda_1 H|^2 + \underline{m_X^2}) - T_\zeta^* \left( \lambda_2 + \frac{\mu}{\phi} \right) \lambda_1^* |H|^2 - \frac{1}{2} T_\zeta \lambda_2^* \lambda_1 |H|^2$$

$$\text{or } |H|^2 \approx \frac{-m_\phi^2 - \frac{1}{2} (m_X^2 - |a - b|^2) |T_\zeta|^2}{\left( \lambda_2 - \frac{1}{2} T_\zeta \lambda_1 + \frac{\mu}{\phi} \right) (\lambda_2^* - T_\zeta^* \lambda_1^*)},$$



# Extrm. Condi. for $\Phi$

The extremum occurs at  $T_\zeta (\equiv \kappa\phi/M)$

$$|H|^2 \sim -m_{\phi, X}^2 / |\lambda_{2,1}|^2$$

$$\text{or } |H|^2 \approx \frac{-m_\phi^2 - \frac{1}{2} (m_X^2 - |a-b|^2) |T_\zeta|^2}{\left(\lambda_2 - \frac{1}{2} T_\zeta \lambda_1 + \frac{\mu}{\phi}\right) (\lambda_2^* - T_\zeta^* \lambda_1^*)},$$

# Dynamical Relaxation

$$\mu_{\text{eff}} = \lambda_1 \langle X \rangle + \lambda_2 \langle \phi \rangle + \mu,$$

$$\approx \frac{MT_\zeta}{\kappa} \left( \lambda_2 - \frac{1}{2} \lambda_1 T_\zeta \right) + \mu,$$

$$|\mu|^2 + \frac{1}{2} M_Z^2 = \frac{m_{h_d}^2 - m_{h_u}^2 \tan^2 \beta}{\tan^2 \beta - 1} \quad (\approx -m_{h_u}^2)$$

$\mu_{\text{eff}}$

satisfying the conditions for EW symmetry breaking,

$$2B\mu < (m_{h_u}^2 + |\mu|^2) + (m_{h_d}^2 + |\mu|^2)$$

$$(B\mu)^2 > (m_{h_u}^2 + |\mu|^2)(m_{h_d}^2 + |\mu|^2)$$

$B\mu_{\text{eff}}$

# Dynamical Relaxation

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$\mu_{\text{eff}}$

$B\mu_{\text{eff}}$

**For  $|\lambda_2 M / \kappa|^2 \gg -m_{h_u}^2$**

**$|T_\zeta(1 - T_\zeta \lambda_1 / 2\lambda_2)| \ll 1$**

# Little Hierarchy Problem

$$|\mu|^2 + \frac{1}{2}M_Z^2 = \frac{m_{h_d}^2 - m_{h_u}^2 \tan^2 \beta}{\tan^2 \beta - 1}$$

Why is  $M_Z^2$  [=  $(g_2^2 + g_Y^2)(v_u^2 + v_d^2)/2$ ] **so small** compared to **the soft masses** ?

$$[v_u^2 + v_d^2 \equiv \langle |H|^2 \rangle = (174 \text{ GeV})^2]$$

# Little Hierarchy Problem

*It is because  $m_\phi$ ,  $m_\chi$  are so small compared to the **MSSM soft masses.***

Why is  $M_Z^2$  [ $= (g_2^2 + g_Y^2)(v_u^2 + v_d^2)/2$ ] so small compared to **the soft masses** ?

$$[v_u^2 + v_d^2 \equiv \langle |H|^2 \rangle = (174 \text{ GeV})^2]$$

**For small enough  $m_{\phi, X^2}$**

**Introduce Gauge Med. SUSY Breaking  
as well as Gravity Med. SUSY breaking**

**Gauge Med.** → Heavy MSSM soft masses  
avoiding Exp. Bounds and SUSY flavor and CP problems

**Gravity Med.** → Small MSSM **singlet** masses and  $B\mu$  term

For small enough  $m_{\phi, X^2}$

Introduce Gauge Med. SUSY Breaking  
as well as Gravity Med. SUSY breaking

- *Messenger Scale of the Gauge Med.*  
*needs to be LOW enough.*
- $\lambda_2$  *needs to be SMALL enough.*

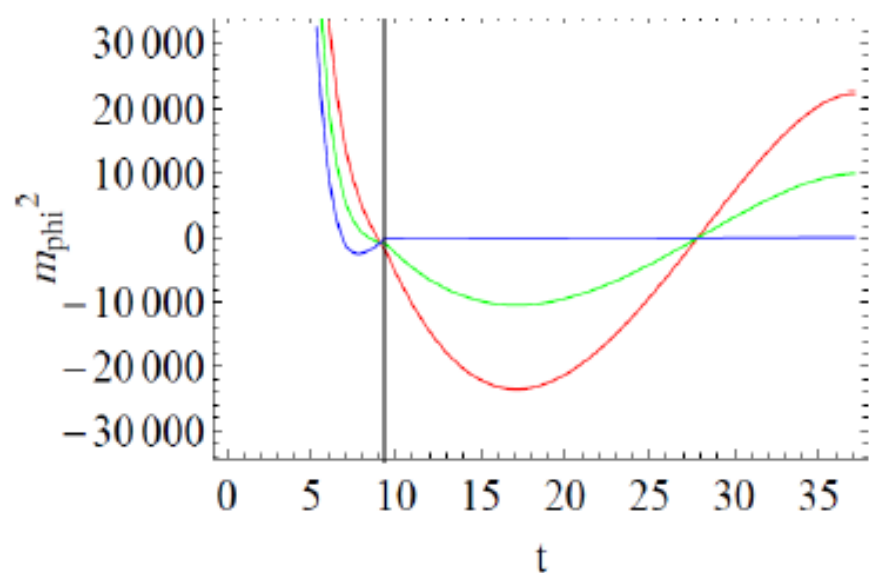
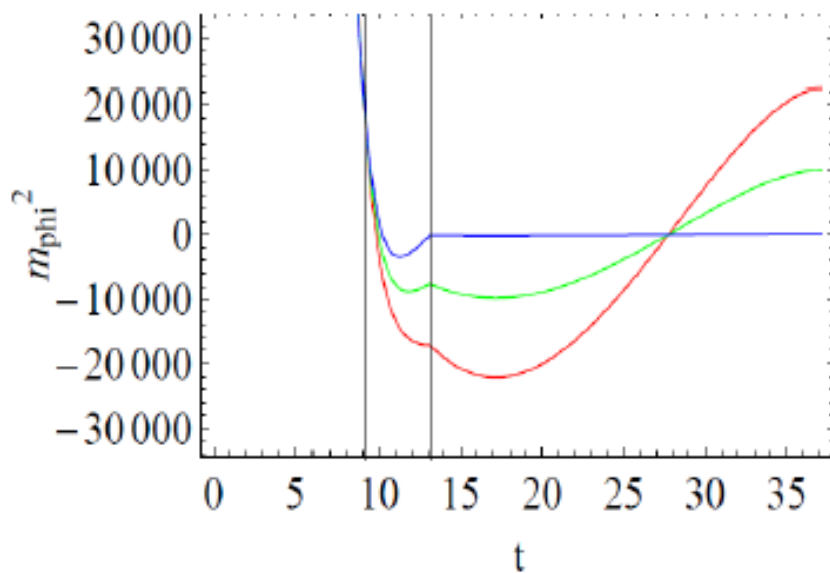
Gravity

term

Items

# Focus Point

(  $\lambda_1=0.7 \gg \lambda_2=0.02$  )



RG evolutions of  $m_{\phi}^2$  under various trial  $m_0^2$ s.

the messenger scale = 500 TeV (L) and 12 TeV (R).

In both cases, the stop mass scales = 10 TeV.



# Focus Point

Case I	$\tan \beta = 10$	Case II	$\tan \beta = 40$
$\lambda_2^2 = 5 \cdot 10^{-4}$	$\tilde{m}_t^2 = (10 \text{ TeV})^2$	$\lambda_2^2 = 8 \cdot 10^{-3}$	$\tilde{m}_t^2 = (20 \text{ TeV})^2$
$\lambda_1^2 = 0.5$	$\Lambda_M = 15 \text{ TeV}$	$\lambda_1^2 = 0.5$	$\Lambda_M = 25 \text{ TeV}$
$\Delta_{m_0^2}$	19.1	$\Delta_{m_0^2}$	79.6
$\Delta_{M_{1/2}}$	83.2	$\Delta_{M_{1/2}}$	28.6
$\Delta_{\lambda_2^2}$	59.7	$\Delta_{\lambda_2^2}$	56.5
$\Delta_{GM}$	37.1	$\Delta_{GM}$	153.5
$\Delta_{\Lambda_M}$	6.0	$\Delta_{\Lambda_M}$	21.3

# Focus Point

Case I	$\tan \beta = 10$	Case II	$\tan \beta = 40$
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$\lambda_1^2 = 0.5$	$\Lambda_M = 15 \text{ TeV}$	$\lambda_1^2 = 0.5$	$\Lambda_M = 25 \text{ TeV}$

$$\mathbf{F_{gauge} / (16\pi^2 \Lambda_M) \equiv GM \approx 5.1 \text{ TeV (I) and } 10.5 \text{ TeV (II) ,}$$

$$\mathbf{F_{gauge} \ll F_{gravity} ,}$$

$$\mathbf{m_{3/2} \approx F_{gravity} / (\sqrt{3} M_{Pl}) \approx m_0 = 30.4 \text{ GeV (I) and } 124.7 \text{ GeV (II) ,}$$

We set  $\mathbf{M_{1/2} = 125 m_0}$  (I) and  $\mathbf{54 m_0}$  (II) at the GUT scale.

# Focus Point

Case I	$\tan \beta = 10$	Case II	$\tan \beta = 40$
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$\lambda_1^2 = 0.5$	$\Lambda_M = 15 \text{ TeV}$	$\lambda_1^2 = 0.5$	$\Lambda_M = 25 \text{ TeV}$

**$(M_G, M_W, M_B) \approx (12, 5, 3) \text{ TeV (I) and } (22, 9, 5) \text{ TeV (II)}$**

**$\mu_{\text{eff}} \approx 2.5 \text{ TeV (I) and } 2.3 \text{ TeV (II)}$**

**The SUSY particles' masses of the 1<sup>st</sup> and 2<sup>nd</sup> generations are much heavier.**

# Mass Matrix (fermion)

$$\begin{pmatrix} \kappa Y & \kappa \phi & 0 & \lambda_2 h_u & \lambda_2 h_d \\ \kappa \phi & 0 & M & 0 & 0 \\ 0 & M & 0 & \lambda_1 h_u & \lambda_1 h_d \\ \lambda_2 h_u & 0 & \lambda_1 h_u & 0 & \mu_{\text{eff}} \\ \lambda_2 h_d & 0 & \lambda_1 h_d & \mu_{\text{eff}} & 0 \end{pmatrix}$$

in the basis of  $\{\phi, Y, X, h_d, h_u\}$

# Mass Matrix (fermion)

$$\left( \begin{array}{ccc|cc} \kappa Y & \kappa \phi & 0 & \lambda_2 h_u & \lambda_2 h_d \\ \kappa \phi & 0 & M & 0 & 0 \\ 0 & M & 0 & \lambda_1 h_u & \lambda_1 h_d \\ \hline \lambda_2 h_u & 0 & \lambda_1 h_u & 0 & \mu_{\text{eff}} \\ \lambda_2 h_d & 0 & \lambda_1 h_d & \mu_{\text{eff}} & 0 \end{array} \right)$$

in the basis of  $\{\phi, Y, X, h_d, h_u\}$

# Mass Matrix (fermion)

$$\begin{pmatrix} \kappa Y & \kappa \phi & 0 & \lambda_2 h_u & \lambda_2 h_d \\ \kappa \phi & 0 & M & 0 & 0 \\ 0 & M & 0 & \lambda_1 h_u & \lambda_1 h_d \\ \hline \lambda_2 h_u & 0 & \lambda_1 h_u & 0 & \mu \\ \lambda_2 h_d & 0 & \lambda_1 h_d & 0 & \mu \end{pmatrix}$$

$$\frac{\kappa \langle Y \rangle}{1 + T_\zeta^2} \approx \frac{1}{2} T_\zeta^2 (b^* - a^*)$$

The smallest mass E. value

**$\approx$  sub GeV or lighter,**

*The lightest E. state plays the role of DM.*

# Mass Matrix (scalar)

$$\begin{pmatrix} m_H^2 & \lambda_2 H \mu_{\text{eff}}^* & \lambda_1 H \mu_{\text{eff}}^* \\ \lambda_2^* H^* \mu_{\text{eff}} & m_\phi^2 + |\lambda_2 H|^2 + |\kappa \phi|^2 & \lambda_2^* \lambda_1 |H|^2 + \kappa^* \phi^* M \\ \lambda_1^* H^* \mu_{\text{eff}} & \lambda_1^* \lambda_2 |H|^2 + \kappa \phi M^* & m_X^2 + |\lambda_1 H|^2 + |M|^2 \end{pmatrix}$$

in the basis of  $\{H, \phi, X\}$

# Mass Matrix (scalar)

- In the limit of  $\lambda_2/\lambda_1 = \kappa\phi/M$  ( $=T_\zeta$ ),  
The **mixing angle** btw the **Higgs** and **singlets**  
are **suppressed**.

We assume  $(\lambda_2/\lambda_1 - \kappa\phi/M)/(\lambda_2/\lambda_1) \sim 0.1$ .

- We can consider one more flat direction  
to easily get ALL positive E. values:

$$W \supset m XY' + (\kappa/2)Y'\phi'^2,$$

which leaves almost intact the above results,  
except adding a small SUSY mass to X.



# Mass Matrix (scalar)

We can fulfill the constraints e.g. with

- $\lambda_1 \approx 0.7$ ,  $|\lambda_2/\lambda_1| = 0.03$  (0.12),  $T_\zeta < 0.027$  (0.11),
  - $M_3 \sim 1 - 10$  GeV,  $M_2 \sim 5$  TeV,
  - $\varepsilon \sim 10^{-1} - 10^{-2}$ ,  $|\tan\theta| > 10^{+1}$ .

The mixing btw H and the singlets can be suppressed enough.

The mixing btw  $\phi$  and X is almost the maximal.

# Conclusion

- The **MSSM  $\mu$  term** is dynamically adjusted by singlets such that the min. cond. of the Higgs is fulfilled.  
A **FLAT DIRECTION** compensates  $m_{hu}^2$ , while the **SM Higgs** does  $m_\phi^2$ .
- A relatively **small soft mass of a singlet** ( $m_\phi^2$  or  $m_\chi^2$ ) is responsible for the **small  $\langle H \rangle$**  (or small  $M_Z$ ). Possible by **Small Gravity Medi. Effects!**
- The **MSSM SUSY ptl.s** are **heavy** enough to avoid Exp. Bounds and FCNC. Possible by **Large Gauge Medi. Effects!**
- A **sub-GeV fermionic DM** is predicted, while the Higgsino is quite heavy.
- The **Mixings btw the Higgs and singlets** can be **suppressed** enough by introducing **several singlets**.

**Thank You !!**