

Controlled Flavour Changing Neutral Couplings in Two Higgs Doublet Models

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Multi-Higgs Doublet Models

Definition

- Fermionic content: SM;
 - Gauge symmetry: $G_{SM} = SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$;
 - Scalar content: N scalars $\phi_a = (1, 2, \frac{1}{2})$.
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- Why MHDMs?
 - Strong CP Problem;
 - Baryogenesis;
 - Dark Matter;
 - Hierarchy Problem*.

- Scalar Potential

- $V(\phi) = \mu_{ab}(\phi_a^\dagger \phi_b) + \lambda_{ab,cd}(\phi_a^\dagger \phi_b)(\phi_c^\dagger \phi_d)$;
- $\frac{1}{2}N^2(N^2 + 3) - 2$ new parameters.

- Yukawa sector

- $-\mathcal{L}_{yuk} = (R_a + i\epsilon_q J_a) (\bar{q}_L N_{qa} q_R) / v + h.c.$;
- $N_{qa} = \frac{1}{\sqrt{2}} v O_{ab} e^{i\epsilon_q \alpha_b} \left(U_{qL}^\dagger Y_b^q U_{qR} \right)$;
- $36(N - 1)$ new parameters.

Multi-Higgs Doublet Models

Problems

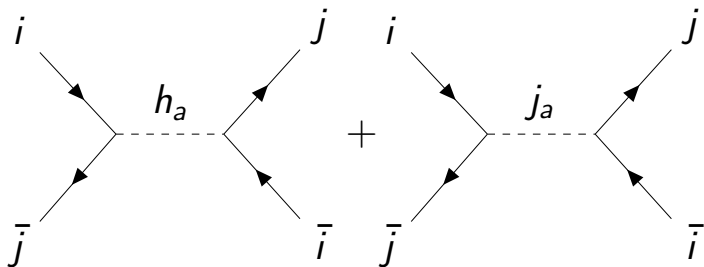


Figure: Tree-level diagrams contributing to meson-antimeson mixing in a MHDM

$$\left| f_1 \left(\frac{m_P^2}{m_j^2} \right) \sum_a \frac{1 - R_{a1}^2}{m_{h_a}^2} (\tau_a^+)^2 - f_2 \left(\frac{m_P^2}{m_j^2} \right) \sum_a \frac{1}{m_{j_a}^2} (\tau_a^+)^2 + (\dots) \right| \leq \frac{24v^2 \Delta m_P}{m_P f_P^2}$$

Multi-Higgs Doublet Models

Problems

- Take decoupling limit, $m_h \ll m_{h_a}, m_{j_a}$

$$c_{\beta\alpha}^2 \left\{ g_1 \sum_b \left[|(N_{qb})_{ij}|^2 + |(N_{qb})_{ji}|^2 \right] - g_2 \sum_b \text{Re} [(N_{qb})_{ij}(N_{qb})_{ji}] \right\} \leq \frac{24v^2 m_h^2 \Delta m_P}{m_P f_P^2}$$

- Assume Yukawa couplings of order one
 - Up sector restricted by $D - \bar{D}$;
 - Down sector restricted by $K - \bar{K}$.

$$c_{\beta\alpha}^2 (1.1c_1^u - c_2^u) < 3 \times 10^{-9}, \quad c_{\beta\alpha}^2 (1.2c_1^d - c_2^d) < 8 \times 10^{-10}.$$

- 2HDM invariant under the Abelian Flavour Symmetry*

[Branco, Grimus and Lavoura, arXiv:9601383]

$$q_{L3} \rightarrow \Upsilon q_{L3}, \quad u_{R3} \rightarrow \Upsilon^2 u_{R3}, \quad \phi_2 \rightarrow \Upsilon \phi_2, \quad \Upsilon^2 \neq 1.$$

- Yukawa textures of BGL models*

$$\Gamma_1 = \begin{bmatrix} x & x & x \\ x & x & x \\ 0 & 0 & 0 \end{bmatrix}, \quad \Gamma_2 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ x & x & x \end{bmatrix}, \quad \Delta_1 = \begin{bmatrix} x & x & 0 \\ x & x & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad \Delta_2 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & x \end{bmatrix}.$$

- WBI definition of BGL models*

$$\Gamma_1^\dagger \Gamma_2 = \Delta_1^\dagger \Delta_2 = \Gamma_1^\dagger \Delta_2 = \Gamma_2^\dagger \Delta_1 = \Delta_1 \Delta_2^\dagger = 0, \quad \Gamma_1 \neq 0, \quad \Gamma_2 \neq 0.$$

- Non-diagonal couplings of BGL models*

$$(N_d)_{ij} = \left[t_\beta \delta_{ij} - (t_\beta + t_\beta^{-1}) V_{ti}^* V_{tj} \right] (m_d)_{jj},$$

$$N_u = \text{diag} \left\{ t_\beta m_u, t_\beta m_c, -t_\beta^{-1} m_t \right\}.$$

- Experimental Constraints*

$$|c_{\beta\alpha}(t_\beta + t_\beta^{-1})| < 3.$$

- Baryon Asymmetry of the Universe*

$$\frac{BAU_{BGL}}{BAU_{SM}} = (t_\beta + t_\beta^{-1}) \frac{E^4}{m_t^4} \sim 1.$$

- MHDM invariant under abelian symmetry

[Alves, Botella, Branco, Cornet-Gomez, Nebot and Silva, arXiv:1803.11199]

$$N_d^0 = L_d^0 D_d^0, \quad N_u^0 = L_u^0 D_u^0.$$

- For 2HDM, $(L_d^0)_{ij}$ are determined by

$$(\Gamma_1)_{ij} \neq 0 \Rightarrow (L_d^0)_{ij} = t_\beta,$$

$$(\Gamma_2)_{ij} \neq 0 \Rightarrow (L_d^0)_{ij} = -t_\beta^{-1}.$$

- Each line of a mass matrix of a quark of a given charge can only receive contributions from one scalar;
- There are only five classes of left models in 2HDM.

- 2HDM invariant under the Abelian Flavour Symmetry

[Alves, Botella, Branco, Cornet-Gomez and Nebot, arXiv:1703.03796]

$$q_{L3} \rightarrow -q_{L3}, \quad \phi_2 \rightarrow -\phi_2.$$

- Yukawa textures of gBGL models

$$\Gamma_1 \sim \Delta_1 \sim \begin{bmatrix} x & x & x \\ x & x & x \\ 0 & 0 & 0 \end{bmatrix}, \quad \Gamma_2 \sim \Delta_2 \sim \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ x & x & x \end{bmatrix}.$$

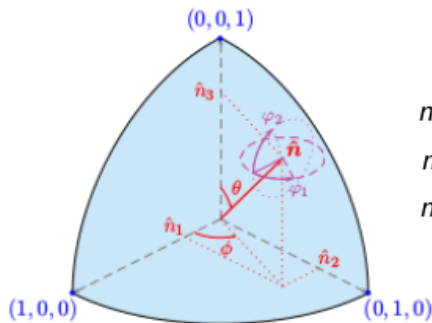
- WBI definition of gBGL models

$$\Gamma_1^\dagger \Gamma_2 = \Delta_1^\dagger \Delta_2 = \Gamma_1^\dagger \Delta_2 = \Gamma_2^\dagger \Delta_1 = 0, \quad \Gamma_1 \neq 0, \quad \Gamma_2 \neq 0.$$

- Non-diagonal couplings of gBGL models

$$(N_d)_{ij} = \left[t_\beta \delta_{ij} - (t_\beta + t_\beta^{-1}) V_{mi}^* V_{nj} n_m^* n_n \right] (m_d)_{jj},$$

$$(N_u)_{ij} = \left[t_\beta \delta_{ij} - (t_\beta + t_\beta^{-1}) n_i^* n_j \right] (m_u)_{jj}.$$



$$n_d = (V_{ud}^*, V_{cd}^*, V_{td}^*), \quad n_u = (1, 0, 0)$$

$$n_s = (V_{us}^*, V_{cs}^*, V_{ts}^*), \quad n_c = (0, 1, 0)$$

$$n_b = (V_{ub}^*, V_{cb}^*, V_{tb}^*), \quad n_t = (0, 0, 1)$$

- Experimental Constraints

$$|c_{\beta\alpha}(t_\beta + t_\beta^{-1})| < 0.02,$$

$$|c_{\beta\alpha}(t_\beta + t_\beta^{-1})| < 3 [\sim tBGL].$$

- Baryon Asymmetry of the Universe

$$\frac{BAU_{gBGL}}{BAU_{SM}} \sim 10^{16} (t_\beta + t_\beta^{-1}) |n_2^* n_3| \sin [\arg (n_3^* n_2 V_{tb}^* V_{cb})],$$

$$\frac{BAU_{\sim tBGL}}{BAU_{SM}} \sim 10^{16} (t_\beta + t_\beta^{-1}) |V_{ts}| \text{Im} [\delta_b + \delta_s^*] \sim 10^{12}.$$

- 2HDM invariant under the Abelian Flavour Symmetry

$$\phi_2 \rightarrow \Upsilon \phi_2, \quad q_{L3}^0 \rightarrow \Upsilon^{-1} q_{L3}^0, \quad d_R^0 \rightarrow \Upsilon^{-1} d_R^0$$

- Yukawa textures of gBGL models

$$\Delta_1 \sim \Gamma_2 \sim \begin{bmatrix} x & x & x \\ x & x & x \\ 0 & 0 & 0 \end{bmatrix}, \quad \Delta_2 \sim \Gamma_1 \sim \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ x & x & x \end{bmatrix}.$$

- WBI definition of jBGL models

$$\Gamma_1^\dagger \Gamma_2 = \Delta_1^\dagger \Delta_2 = \Gamma_1^\dagger \Delta_1 = \Gamma_2^\dagger \Delta_2 = 0, \quad \Gamma_1 \neq 0, \quad \Gamma_2 \neq 0.$$

- Non-diagonal couplings of jBGL models

$$(N_d)_{ij} = \left[-t_\beta^{-1} \delta_{ij} + (t_\beta + t_\beta^{-1}) V_{mi}^* V_{nj} n_m^* n_n \right] (m_d)_{jj},$$

$$(N_u)_{ij} = \left[t_\beta \delta_{ij} - (t_\beta + t_\beta^{-1}) n_i^* n_j \right] (m_u)_{jj}.$$

- Experimental Constraints

$$|c_{\beta\alpha}(t_\beta + t_\beta^{-1})| < 0.02$$

- Baryon Asymmetry of the Universe

$$\frac{BAU_{jBGL}}{BAU_{SM}} \sim 10^{16} (t_\beta + t_\beta^{-1}) |n_2^* n_3| \sin [\arg (n_3^* n_2 V_{tb}^* V_{cb})],$$

- MHDM invariant under abelian symmetry

[Alves, Botella, Branco, Cornet-Gomez, Nebot and Silva, arXiv:1803.11199]

$$N_d^0 = D_d^0 R_d^0, \quad N_u^0 = D_u^0 R_u^0$$

- For 2HDM, $(R_d^0)_{ij}$ are determined by

$$(\Gamma_1)_{ij} \neq 0 \Rightarrow (R_d^0)_{ij} = t_\beta$$

$$(\Gamma_2)_{ij} \neq 0 \Rightarrow (R_d^0)_{ij} = -t_\beta^{-1}$$

- Each column of a mass matrix of a quark of a given charge can only receive contributions from one scalar;
- There are only eight classes of right models in 2HDM.

- Type A(B)

$$\Gamma_1 \sim \begin{bmatrix} x & x & x \\ x & x & x \\ x & x & x \end{bmatrix}, \quad \Gamma_2 = 0, \quad \Delta_1 \sim \begin{bmatrix} x & x & 0 \\ x & x & 0 \\ x & x & 0 \end{bmatrix}, \quad \Delta_2 \sim \begin{bmatrix} 0 & 0 & x \\ 0 & 0 & x \\ 0 & 0 & x \end{bmatrix}.$$

- Type E(F)

$$\Gamma_1 \sim \Delta_1 \sim \begin{bmatrix} x & x & 0 \\ x & x & 0 \\ x & x & 0 \end{bmatrix}, \quad \Gamma_2 \sim \Delta_2 \sim \begin{bmatrix} 0 & 0 & x \\ 0 & 0 & x \\ 0 & 0 & x \end{bmatrix}.$$

- Experimental constraints

$$|c_{\beta\alpha}(t_\beta + t_\beta^{-1})| < 0.02$$

- Type C (D)

$$\Gamma_1 \sim \begin{bmatrix} x & x & 0 \\ x & x & 0 \\ x & x & 0 \end{bmatrix}, \quad \Gamma_2 \sim \begin{bmatrix} 0 & 0 & x \\ 0 & 0 & x \\ 0 & 0 & x \end{bmatrix}, \quad \Delta_1 \sim \begin{bmatrix} x & x & x \\ x & x & x \\ x & x & x \end{bmatrix}, \quad \Delta_2 = 0.$$

- Experimental constraints

$$|c_{\beta\alpha}(t_\beta + t_\beta^{-1})| < 0.03$$

	(3, 0)	(0, 3)	(2, 1)	(1, 2)
(3, 0)	Type I	Type II	Type A	Type B
(0, 3)	Type II	Type I	Type B	Type A
(2, 1)	Type C	Type D	Type E	Type F
(1, 2)	Type D	Type C	Type F	Type E

Table: WBI identification of Right Models.