

Precision Electroweak Measurements in ATLAS and CMS

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on behalf of ATLAS and CMS collaborations

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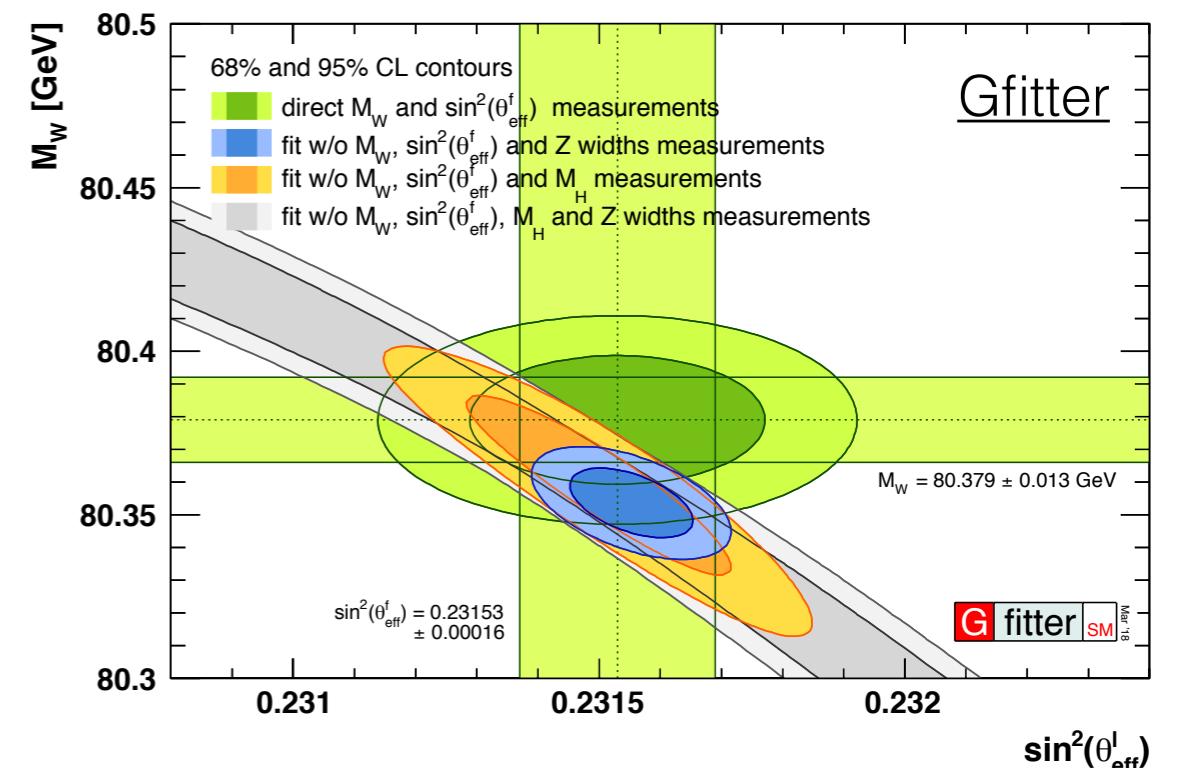


Outline



$$\sin^2 \theta_W = 1 - M_W^2 / M_Z^2$$

- ▶ W mass measurement
- ▶ $\sin^2 \theta_W$ measurement
- ▶ Recent W,Z cross section measurements:
 - Z $d\sigma/dm$ at 13TeV
 - Z $d\sigma/p_T$, $d\sigma/d\phi^*$, $d\sigma/dy$ at 13TeV
 - W production and charge asymmetry at 8TeV
 - W,Z at 5.02 TeV
- ▶ Related talks:
 - Electroweak precision measurements with ATLAS ([Elena Yatsenko](#)) and CMS ([Dylan George Hsu](#))





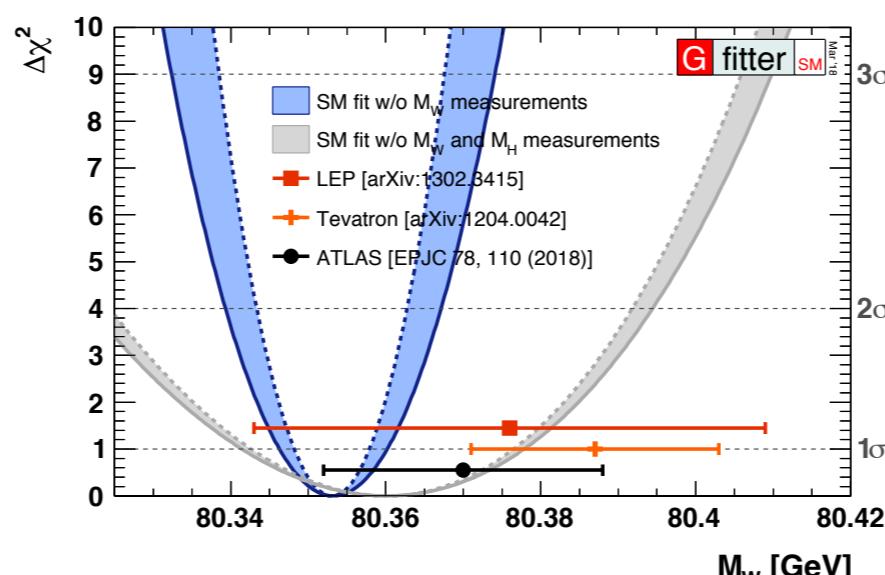
Introduction



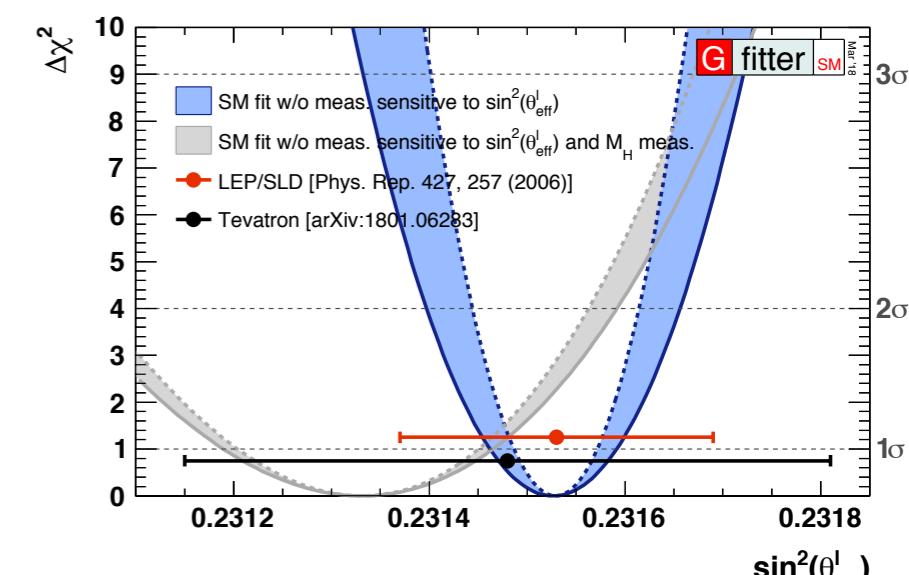
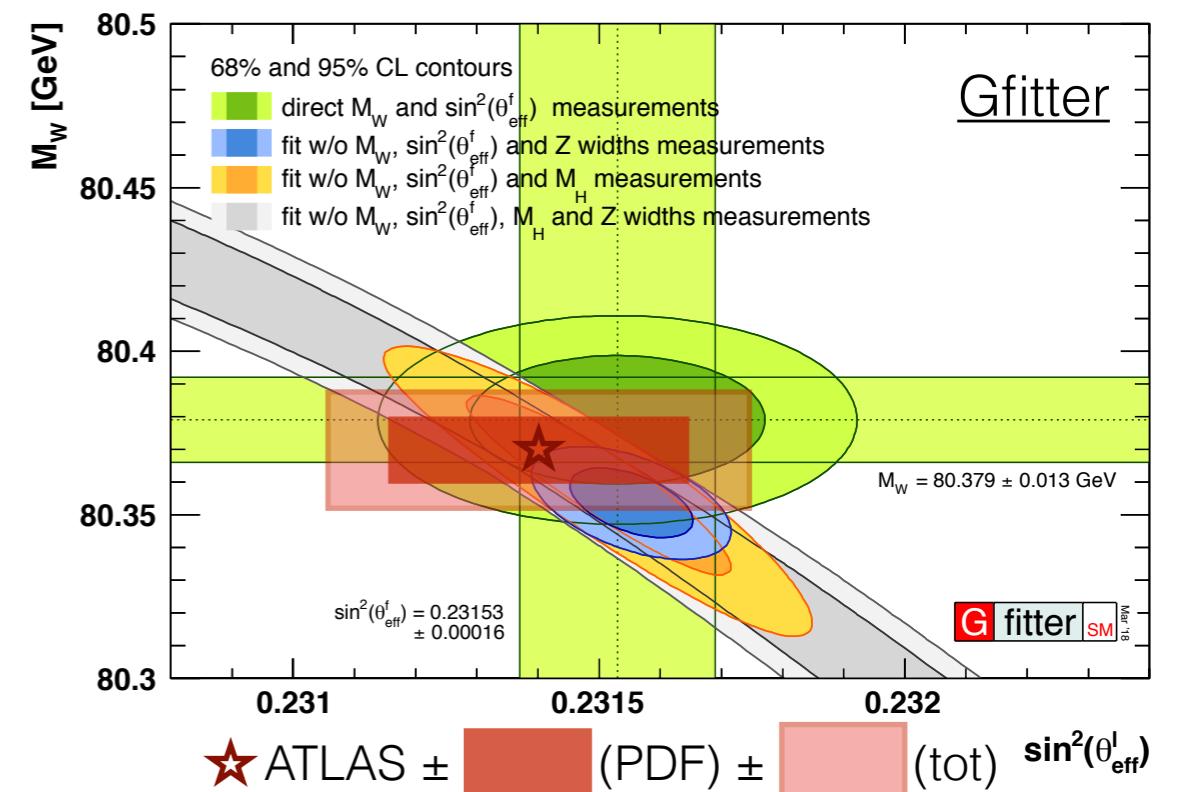
- $\sin^2\theta_W$ and m_W are key parameters of the SM
 - can be calculated from m_Z , a_{EM} , $G\mu$ (with corrections from m_{top} and m_H)
- To test SM, our goal is to reach the precision of global EW fit with direct measurements:
 - m_W at $\pm 10\text{MeV}$
 - $\sin^2\theta_W$ at $\lesssim \pm 10^{-4}$
- LHC individual experiments approaching sensitivity of LEP/SLD and Tevatron combined
 - But PDF uncertainties are becoming the bottleneck

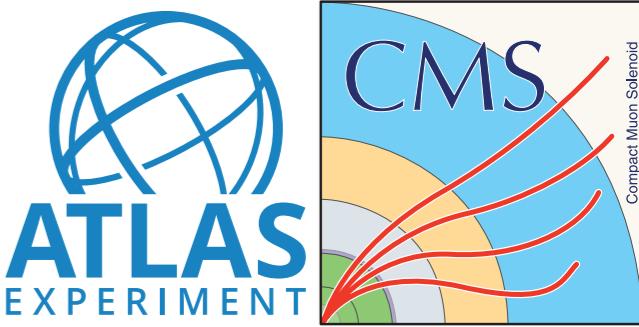
| EW Fit World Avg | |
|--------------------|-----------------------|
| $\sin^2\theta_W$ | 0.23153 ± 0.00006 |
| $m_W [\text{GeV}]$ | 80.354 ± 0.007 |

gFitter



$$\sin^2\theta_W = 1 - M_W^2/M_Z^2$$





W Mass

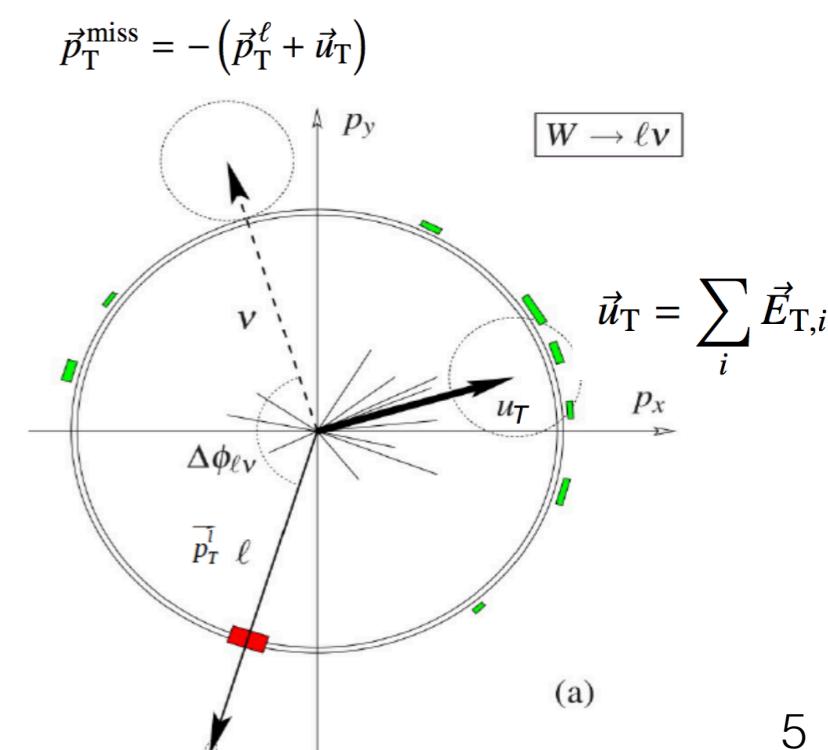
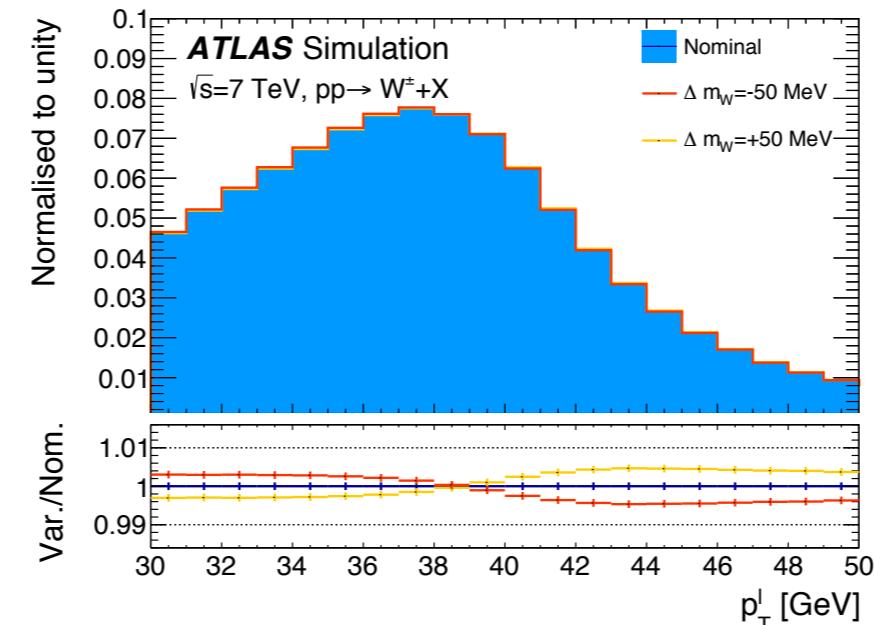
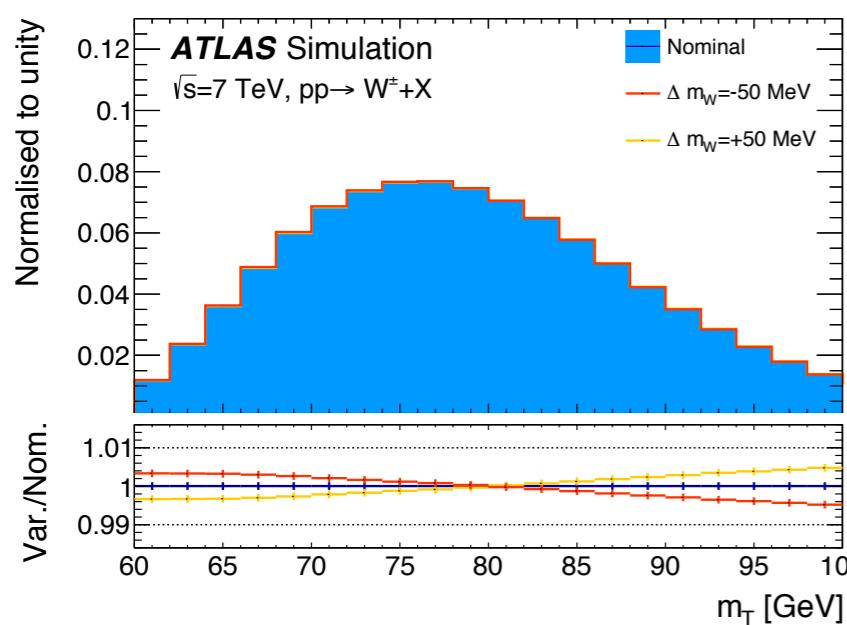
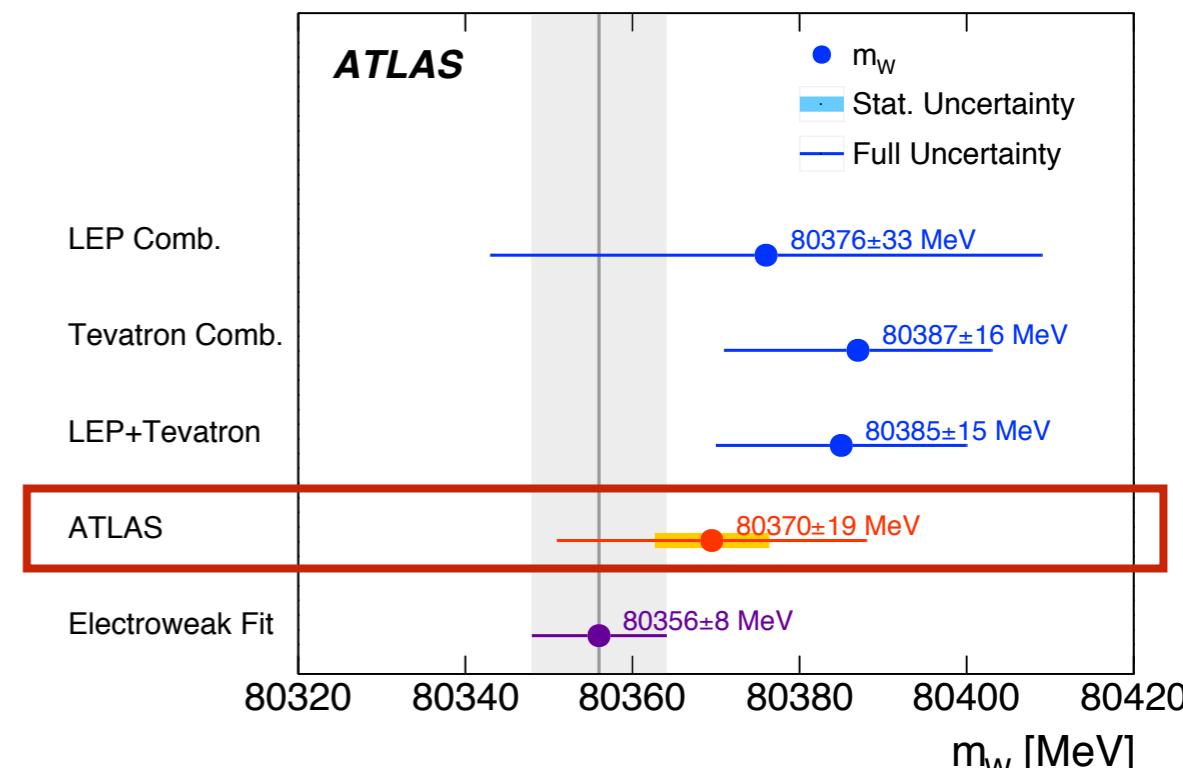


W Mass



[EPJC78\(2018\)110](#)

- Measured with 4.6 fb^{-1} at 7 TeV by ATLAS
 - both $W \rightarrow e\nu$ and $W \rightarrow \mu\nu$ channels analysed
- Template fit to p_T^l and m_T
 - p_T^l sensitive to p_T^W modelling
 - m_T sensitive to hadronic recoil u_T
- Templates built with Powheg+Pythia8 and reweighted to best theoretical modelling
 - $d\sigma/d\eta$ and W polarisation with DYNNLO
 - $d\sigma/dp_T$ with Pythia8 and AZ tune

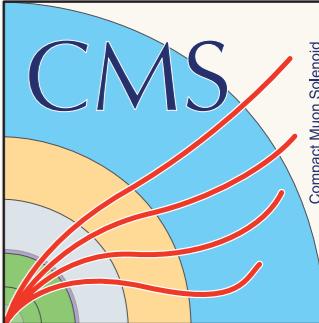




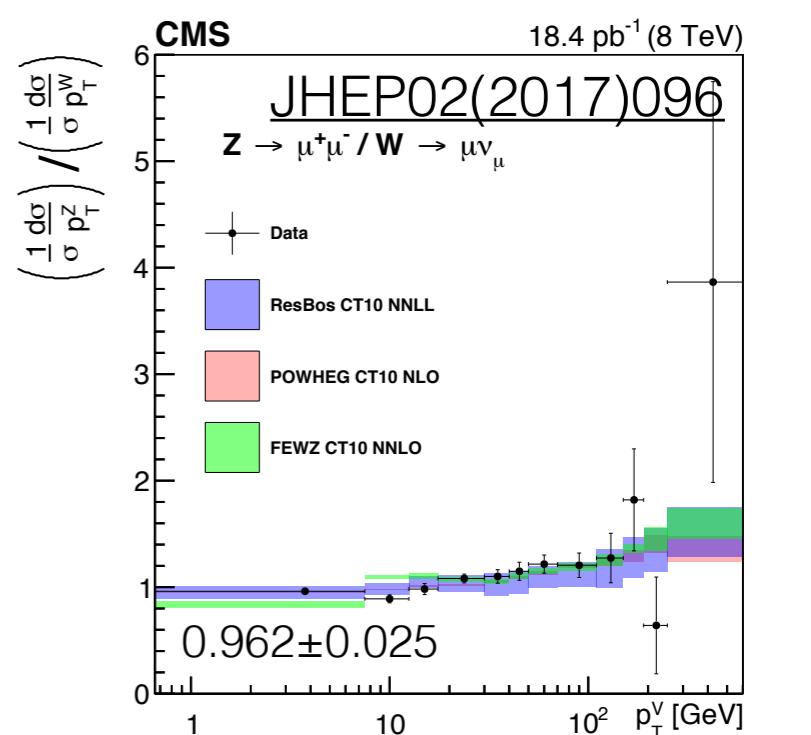
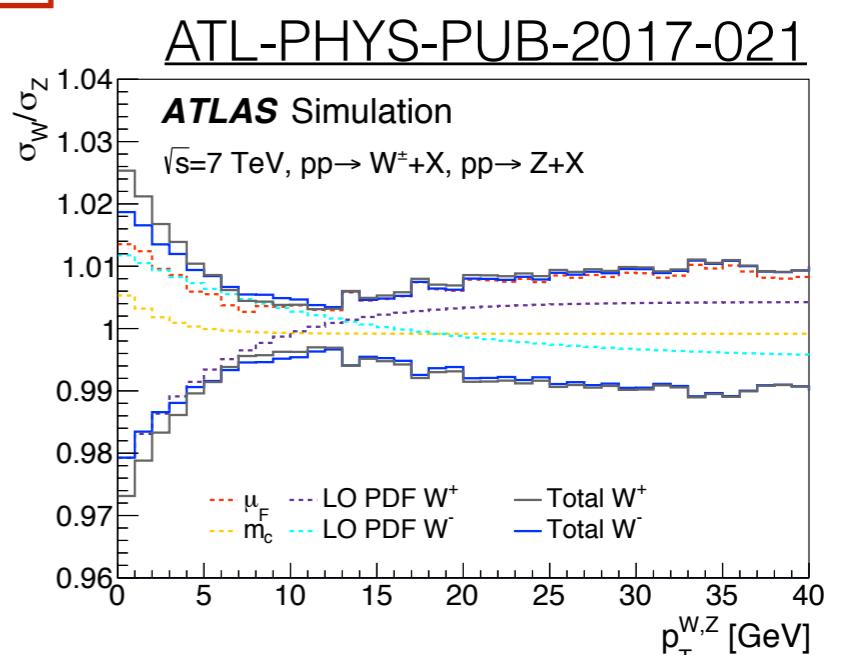
m_W Uncertainties

ATL-PHYS-PUB-2017-021

| Combined categories | Value [MeV] | Stat. Unc. | Muon Unc. | Elec. Unc. | Recoil Unc. | Bckg. Unc. | QCD Unc. | EW Unc. | PDF Unc. | Total Unc. | χ^2/dof of Comb. |
|--------------------------------|-------------|------------|-----------|------------|-------------|------------|----------|---------|----------|------------|------------------------------|
| $m_T - p_T^\ell, W^\pm, e-\mu$ | 80369.5 | 6.8 | 6.6 | 6.4 | 2.9 | 4.5 | 8.3 | 5.5 | 9.2 | 18.5 | 29/27 |



- ▶ PDF uncertainties
 - lepton distributions affected by W polarisation (sensitive to PDF)
 - p_T^W spectrum dependent on the flavour of the incoming quarks
 - needs for future results:
 - improved precision with more W, Z measurements (and N3LL+NNLO predictions? [ATL-PHYS-PUB-2018-004](#))
 - estimate of correlations among PDF sets for combinations with other m_W and $\sin^2\theta_W$ measurements
- ▶ QCD systematics mainly due to uncertainties on p_T^W
 - at 7TeV with $\langle \mu \rangle \sim 9$, p_T^W precision limited by $\sigma(u_T) \sim 13\text{GeV}$ resolution on hadronic recoil
 - p_T^W modelled from Z p_T data via Pythia8 AZ tune $\rightarrow 2.5\%$ uncertainty at low p_T from extrapolation syst
 - same 2.5% precision also in W/Z ratio in 8TeV data (CMS)

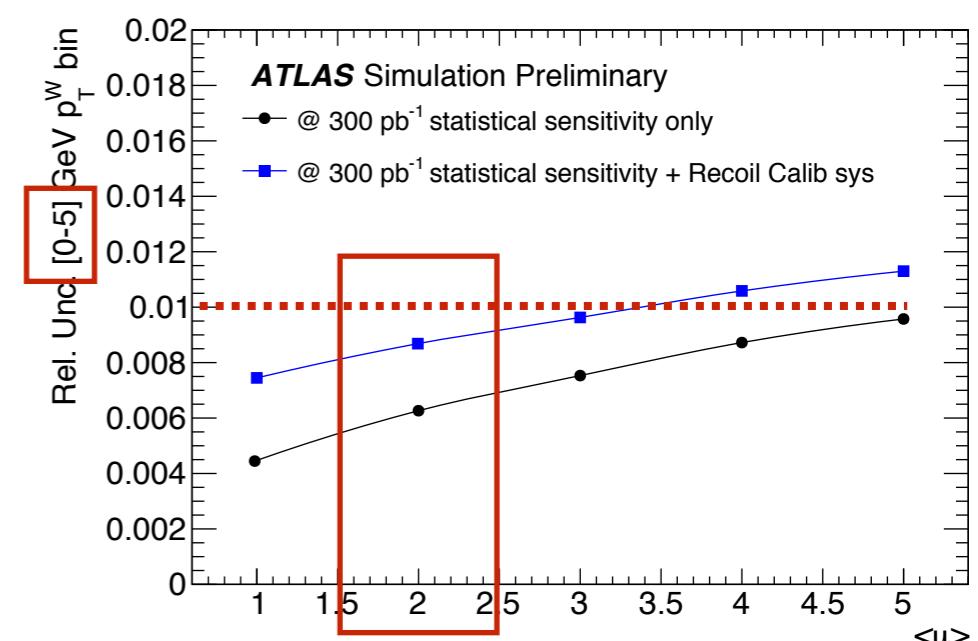




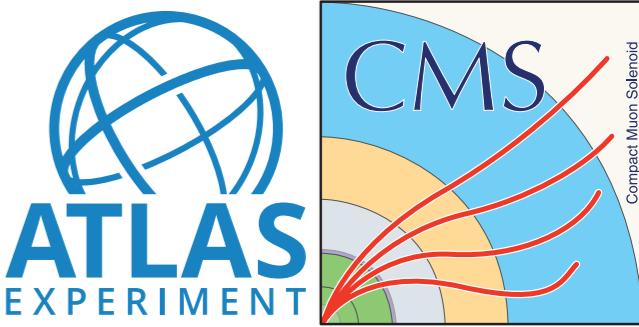
p_T^W Prospects



- ▶ Plan to directly measure p_T^W in data in W events at low μ and with good u_T resolution
 - target 1% precision in 5GeV-bins of p_T^W at low $p_T \rightarrow x0.5$ QCD modelling syst for W mass
 - requires $\sigma(u_T) \lesssim 5\text{GeV}$ to control bin-by-bin migration syst
 - expected to be achieved with low μ data, lower calorimeter thresholds and new improved particle-flow algorithm for hadronic recoil ([EPJC77\(2017\)466](#))
- ▶ Low- μ datasets, $\langle\mu\rangle \sim 2$:
 - ATLAS/CMS: 380/200pb $^{-1}$ at 13TeV, 260/300pb $^{-1}$ at 5TeV (preliminary luminosity calibrations)
 - for equal luminosity, 5TeV and 13TeV data expected to have same sensitivity (better u_T resolution at 5TeV, ie lower UE, and higher cross section at 13TeV)



[ATL-PHYS-PUB-2017-021](#)



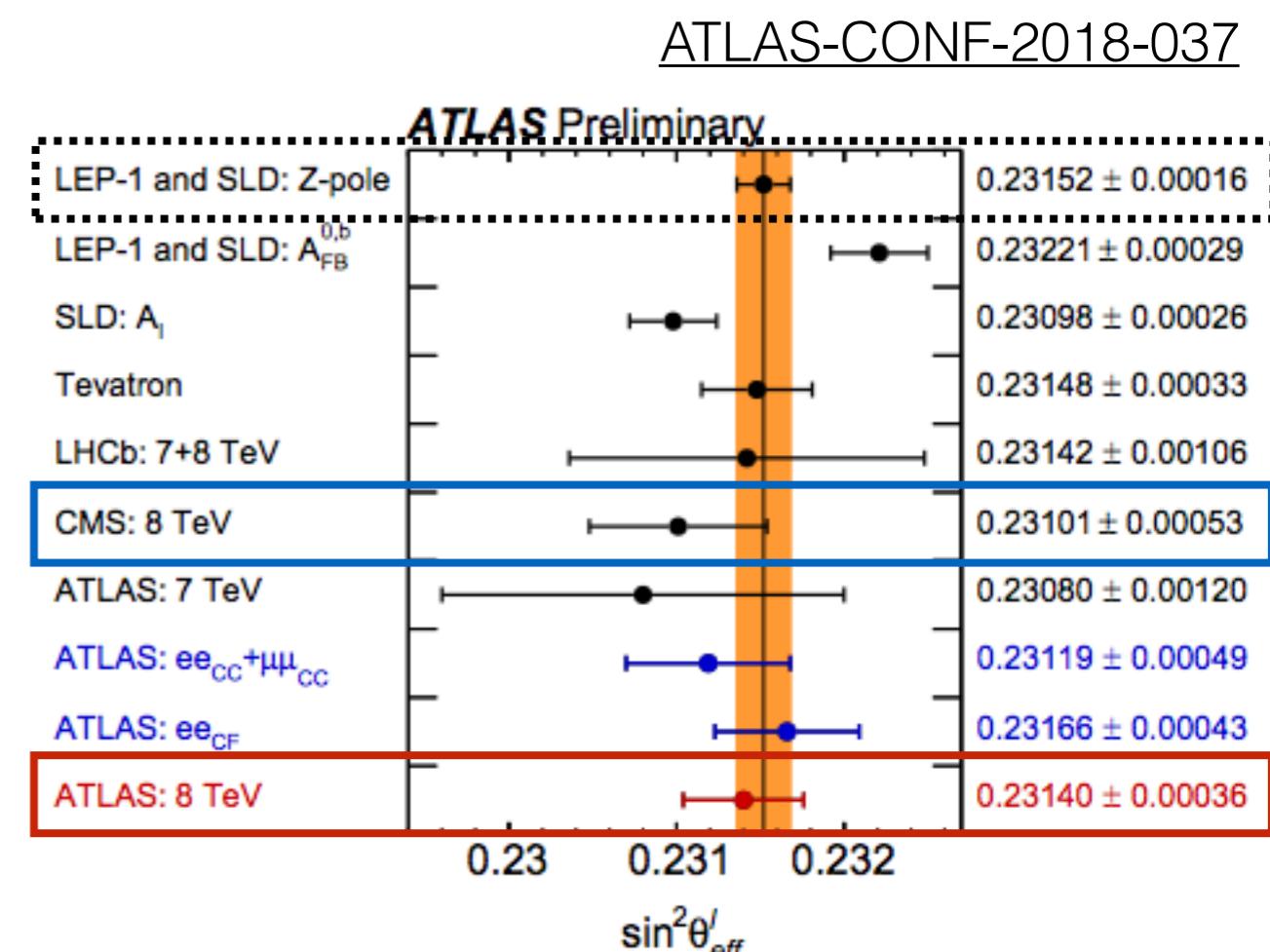
$\sin^2\theta_W$



$\sin^2\theta_W$



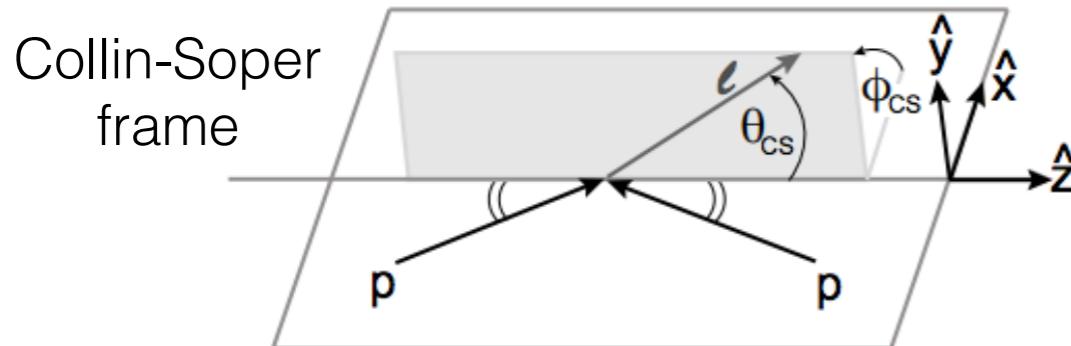
- Measured via asymmetry in lepton angular distributions in Z decays induced by the Z coupling structure
- Most-precise measurement from LEP+SLD combination (16×10^{-5}), but with a difference between the two most sensitive individual results at 3.2σ
- At LHC, two related methodologies:
 - A_4 angular coefficients in full decay lepton phase space ([ATLAS-CONF-2018-037](#))
 - triple differential ($\cos\theta_{\text{CS}}$, m_{\parallel} , y_{\parallel}) cross section and A_{FB} in fiducial phase space ([JHEP12\(2017\)059](#), [EPJC78\(2018\)701](#))



$\sin^2\theta_{\text{eff}} = \sin^2\theta_W K^f(s,t)$, with K^f fermion-flavour dependent form factors that absorbs EW corrections



Ai Methodology



$$\frac{d\sigma}{dp_T^{\ell\ell} dy^{\ell\ell} dm^{\ell\ell} d\cos\theta d\phi} = \frac{3}{16\pi} \frac{d\sigma^{U+L}}{dp_T^{\ell\ell} dy^{\ell\ell} dm^{\ell\ell}}$$

$$\left\{ (1 + \cos^2\theta) + \frac{1}{2} A_0(1 - 3\cos^2\theta) + A_1 \sin 2\theta \cos\phi \right.$$

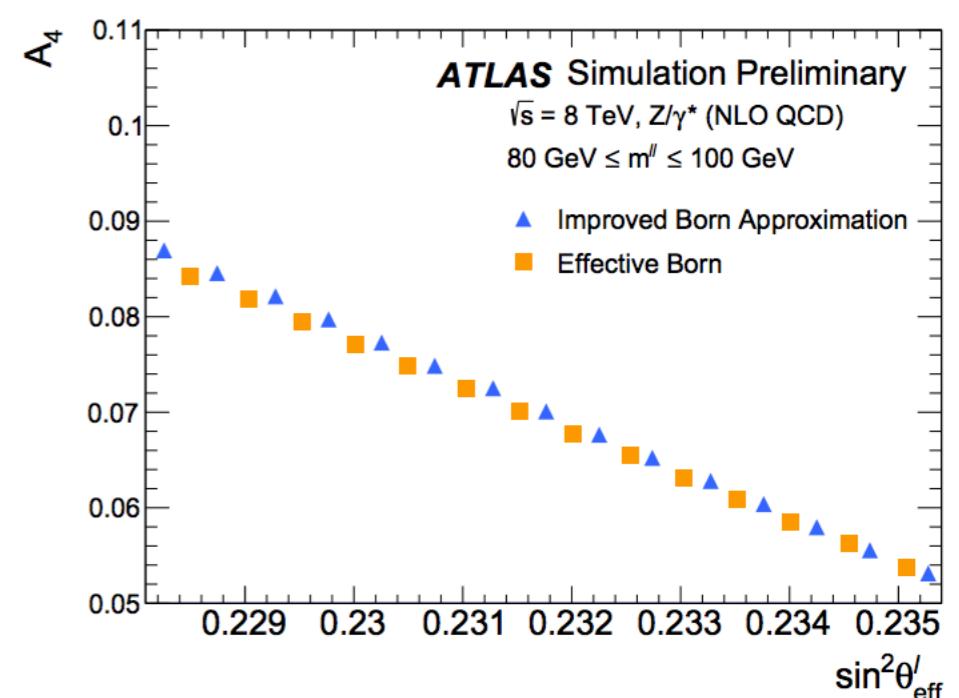
$$+ \frac{1}{2} A_2 \sin^2\theta \cos 2\phi + A_3 \sin\theta \cos\phi + \boxed{A_4 \cos\theta}$$

$$\left. + A_5 \sin^2\theta \sin 2\phi + A_6 \sin 2\theta \sin\phi + A_7 \sin\theta \sin\phi \right\}$$

- pp $\rightarrow Z \rightarrow ll$ cross section in full lepton phase space determined by 5 variables that separate Z production from decay kinematics

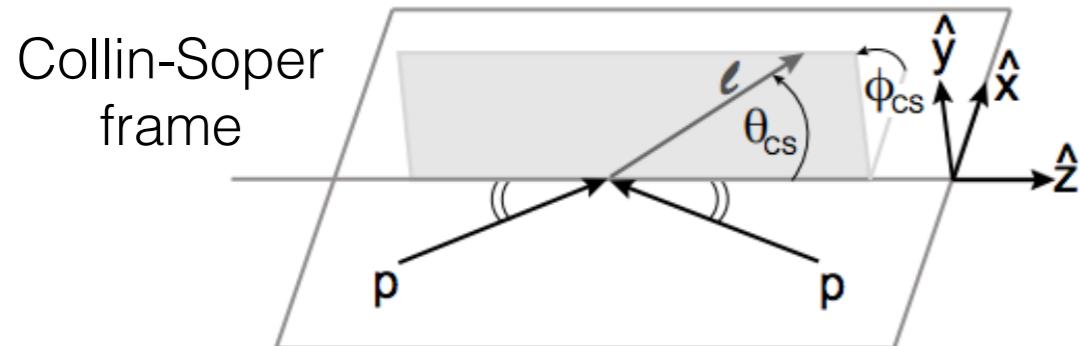
- 9 harmonic polynomials $P_i(\cos\theta_{CS}, \phi_{CS})$ describe the lepton angular distributions in Z rest frame
- 8 $A_i(m^ll, p_T^ll, y^ll)$ coefficients and total unpolarised cross section $\sigma^{U+L}(m^ll, p_T^ll, y^ll)$ describe the Z kinematics

- Parity-violating A_4 term sensitive to $\sin^2\theta_{eff}^f$
- A_4 proportional to $\sin^2\theta_{eff}^f$ based on effective linear relation (including EW corrections)
- 10^{-4} in $A_4 \rightarrow 2 \cdot 10^{-5}$ in $\sin^2\theta_{eff}^f$
- in decay lepton full phase space $A_{FB} = 3/8 A_4$



ATLAS-CONF-2018-037

Ai Methodology



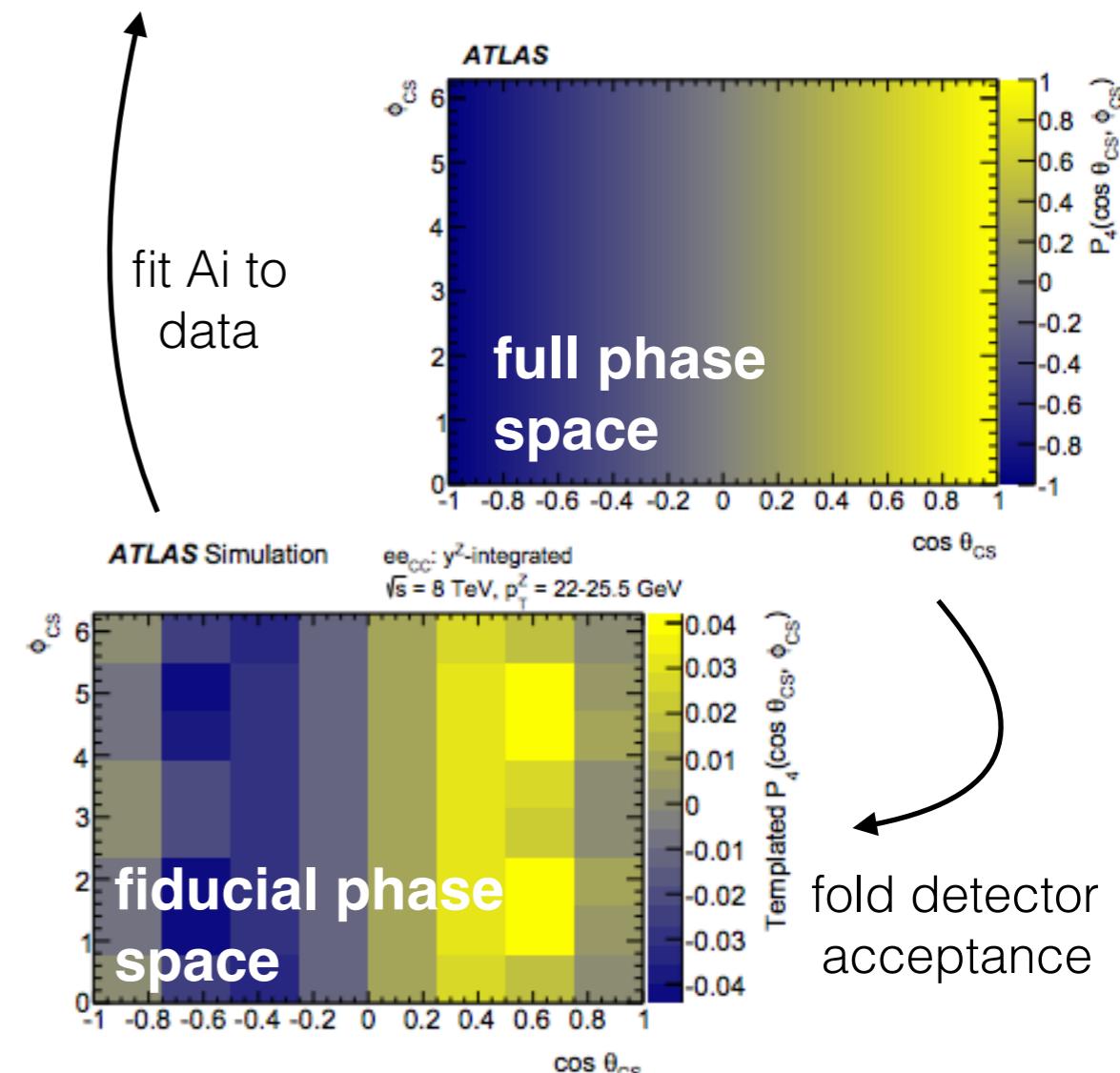
$$\frac{d\sigma}{dp_T^{\ell\ell} dy^{\ell\ell} dm^{\ell\ell} d\cos\theta d\phi} = \frac{3}{16\pi} \frac{d\sigma^{U+L}}{dp_T^{\ell\ell} dy^{\ell\ell} dm^{\ell\ell}}$$

$$\left\{ (1 + \cos^2\theta) + \frac{1}{2} A_0(1 - 3\cos^2\theta) + A_1 \sin 2\theta \cos \phi \right.$$

$$+ \frac{1}{2} A_2 \sin^2\theta \cos 2\phi + A_3 \sin\theta \cos\phi + \boxed{A_4 \cos\theta}$$

$$\left. + A_5 \sin^2\theta \sin 2\phi + A_6 \sin 2\theta \sin\phi + A_7 \sin\theta \sin\phi \right\}$$

- ▶ Fold $P_i(\cos\theta_{CS}, \phi_{CS})$ to detector level
- ▶ Fit reconstructed $\cos\theta_{CS}, \phi_{CS}, m_{||}, y_{||}$ distributions in born-level $m_{||}, y_{||}$ bins
- ▶ Extract A_4 in full decay lepton phase space and use predictions of A_4 to infer $\sin^2\theta_{eff}^f$
- ▶ A_4 measurement dominated by statistical uncertainties
- ▶ QCD and PDF uncertainties dominate $\sin^2\theta_{eff}^f$ interpretation of A_4

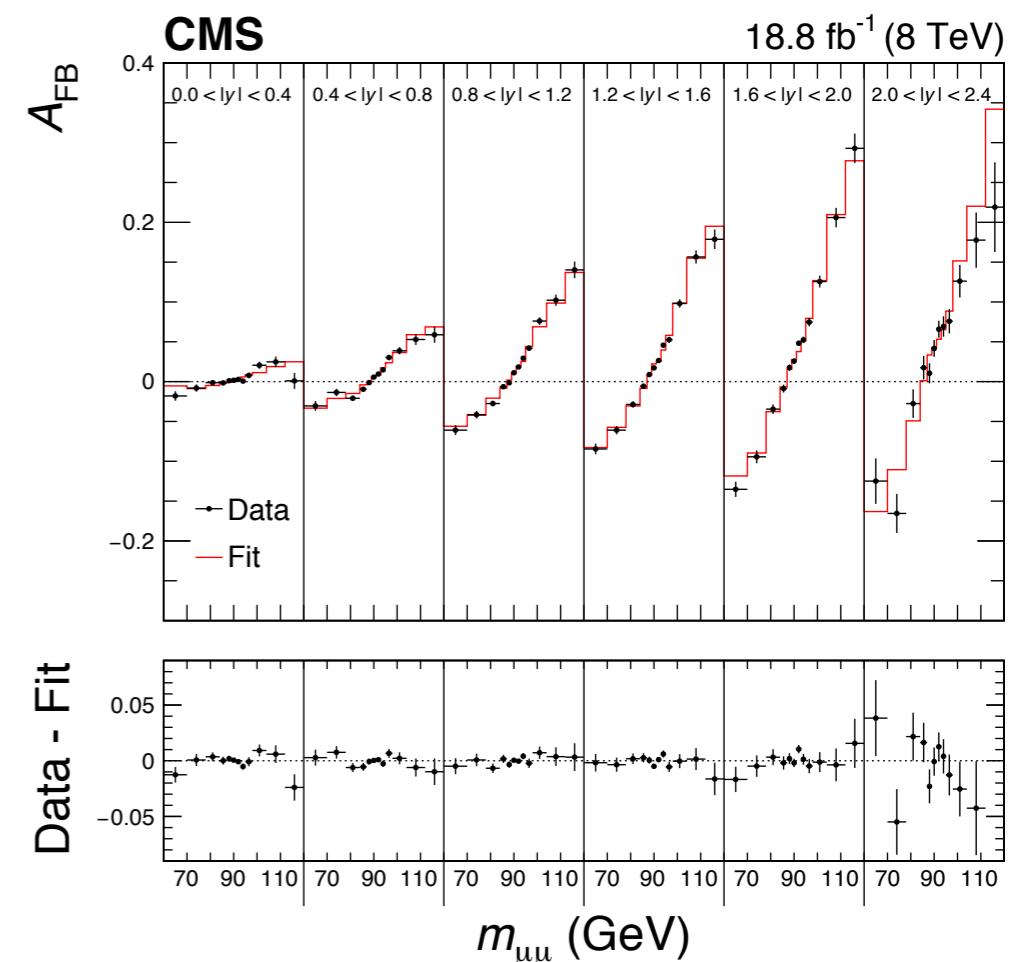
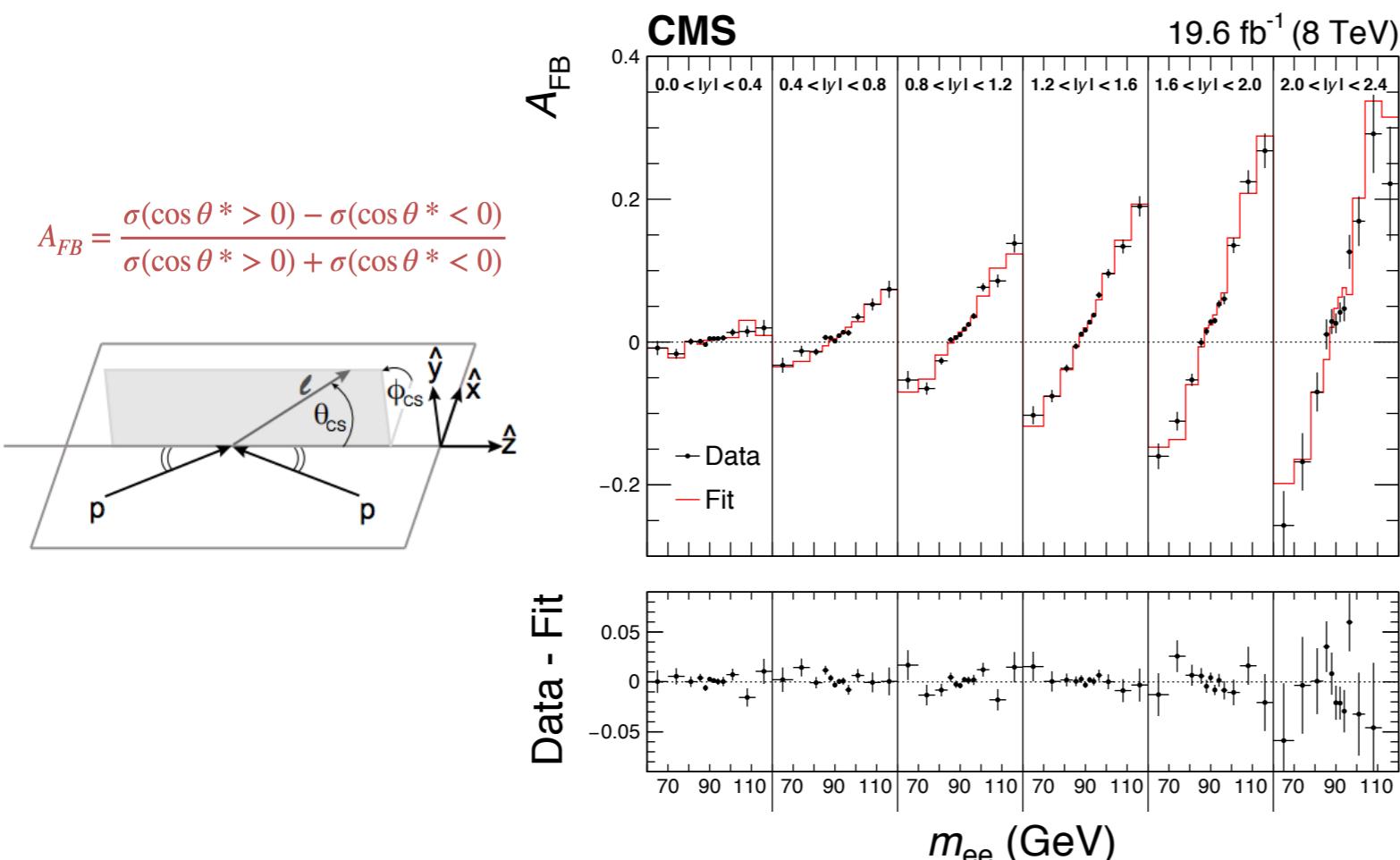




A_{FB} Methodology



- Measure of A_{FB} asymmetry in Collin-Soper frame in reconstructed m_{ll}, y_{ll} bins
 - angular event-weighted A_{FB} to improve statistical uncertainty and reduce impact of efficiency and acceptance uncertainties
- sin²θ_{eff} extracted from template fit to A_{FB} in data using predictions (Powheg v2+NNPDF3.0)

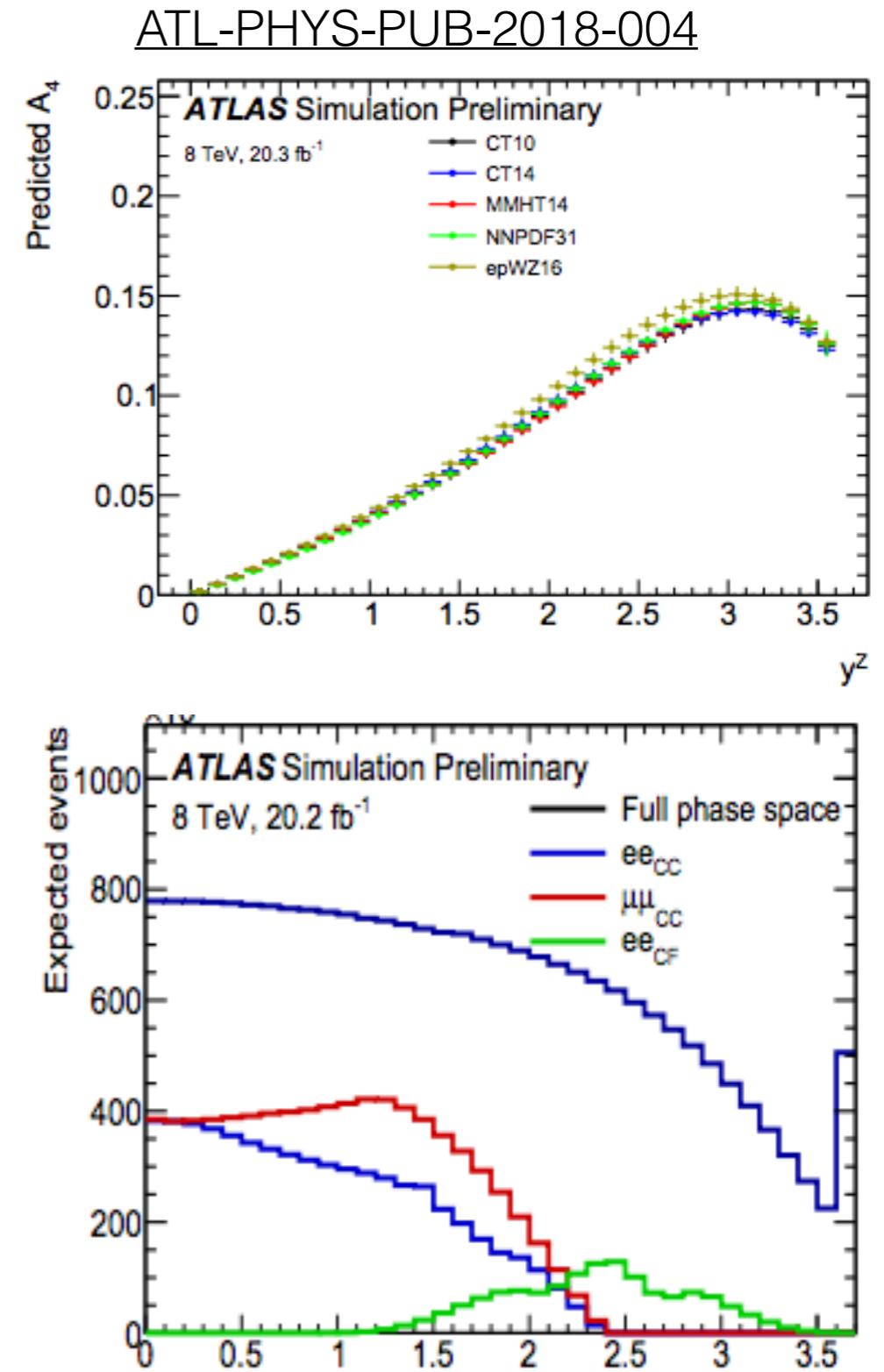




A_{FB}, A₄ at LHC



- ▶ A_{FB}, A₄ strongly depend on PDF
 - quark assigned based on Z rapidity
 - largest at high y^Z where valence quark PDFs dominate at large x
 - also depend on quark flavour, so on relative contributions of u and d PDFs
- ▶ $\mu\mu CC$ and $eeCC$ channels with central leptons $|\mu| < 2.4$ ($|\mu_e| < 2.5$ in CMS)
 - high statistics, good to constrain PDFs
 - similar sensitivity in ATLAS and CMS
- ▶ $eeCF$ channel with a forward electron $2.5 < |\mu| < 4.9$
 - low statistics, high sensitivity to $\sin^2\theta_{\text{eff}}^f$
 - experimentally challenging, unique to ATLAS





$\sin^2\theta_f^{\text{eff}}$



| Channel | $eeCC$ | $\mu\mu CC$ | $eeCF$ | $eeCC + \mu\mu CC$ | $eeCC + \mu\mu CC + eeCF$ | ATLAS | CMS |
|-----------------------------------|---------|-------------|---------|--------------------|---------------------------|-------------|--------|
| Central value | 0.23148 | 0.23123 | 0.23166 | 0.23119 | 0.23140 | eeCC | $eeCC$ |
| Uncertainties | | | | | | | |
| Total | 68 | 59 | 43 | 49 | 36 | $\mu\mu CC$ | 53 |
| Stat. | 48 | 40 | 29 | 31 | 21 | Comb | 36 |
| Syst. | 48 | 44 | 32 | 38 | 29 | | |
| Uncertainties in measurements | | | | | | | |
| PDF (meas.) | 8 | 9 | 7 | 6 | 4 | | |
| p_T^Z modelling | 0 | 0 | 7 | 0 | 5 | | |
| Lepton scale | 4 | 4 | 4 | 4 | 3 | | |
| Lepton resolution | 6 | 1 | 2 | 2 | 1 | | |
| Lepton efficiency | 11 | 3 | 3 | 2 | 4 | | |
| Electron charge misidentification | 2 | 0 | 1 | 1 | < 1 | | |
| Muon sagitta bias | 0 | 5 | 0 | 1 | 2 | | |
| Background | 1 | 2 | 1 | 1 | 2 | | |
| MC. stat. | 25 | 22 | 18 | 16 | 12 | | |
| Uncertainties in predictions | | | | | | | |
| PDF (predictions) | 37 | 35 | 22 | 33 | 24 | | |
| QCD scales | 6 | 8 | 9 | 5 | 6 | | |
| EW corrections | 3 | 3 | 3 | 3 | 3 | | |

ATLAS-CONF-2018-037

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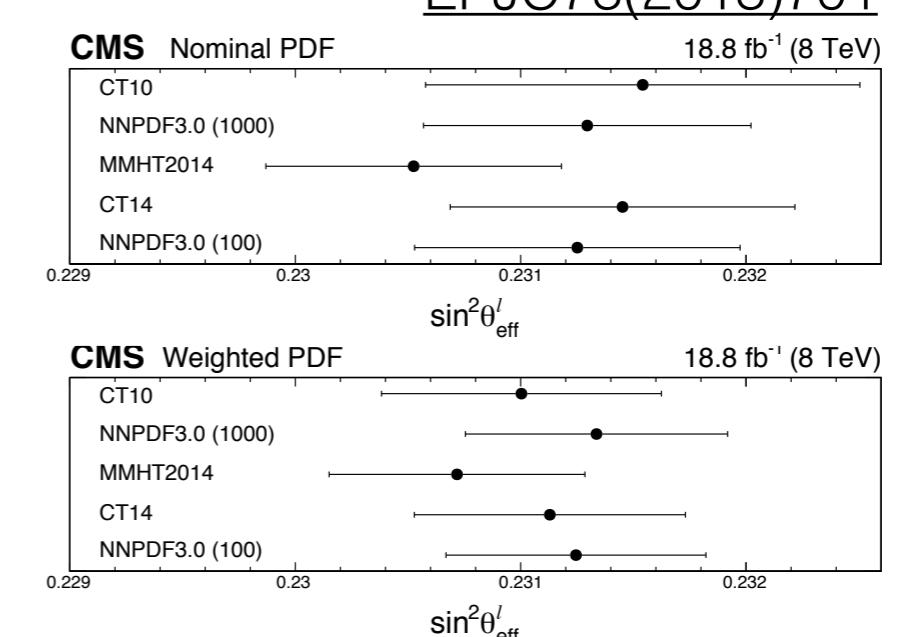
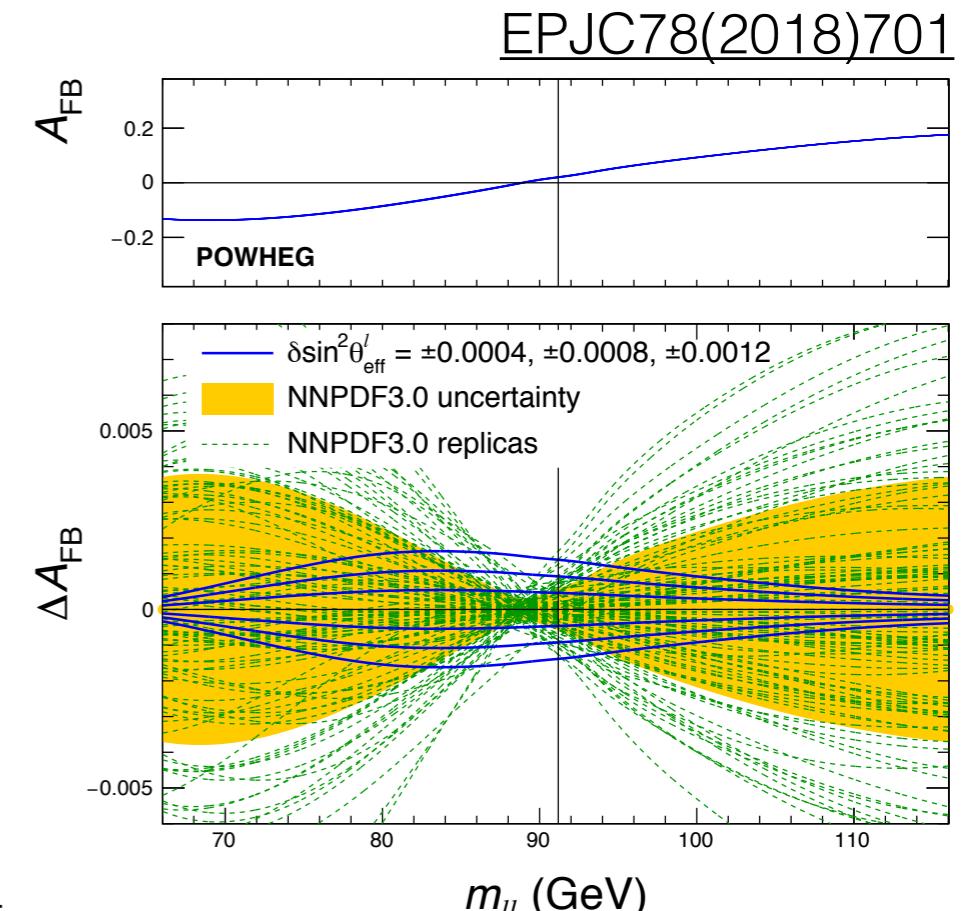


$\sin^2\theta_{\text{eff}}^f$ and PDFs



- PDF uncertainties constrained in $A_{\text{FB}}, A_4 \rightarrow \sin^2\theta_{\text{eff}}^f$ interpretation exploiting correlations in m^{\parallel} and y^{\parallel}
 - PDF uncertainties profiled in ATLAS
 - Bayesian χ^2 reweighting in CMS
- Yet PDF is source of large systematic uncertainty
 - CMS: PDF syst ± 31 , spread among PDF sets $\sim 65 [10^{-5}]$
 - ATLAS: PDF syst ± 24 , spread among PDF sets $\sim 28 [10^{-5}]$
 - compatibility cannot be estimated without correlations
- Improved understanding of PDF differences and correlations is key
 - new PDF sets with more LHC W,Z data will reduce impact of in-situ PDF constraints and ease combinations

| | CT10 | CT14 | MMHT14 | NNPDF31 |
|-------------------------------|---------|---------|---------|---------|
| $\sin^2\theta_{\text{eff}}^f$ | 0.23118 | 0.23141 | 0.23140 | 0.23146 |
| Uncertainties in measurements | | | | |
| Total | 39 | 37 | 36 | 38 |
| Stat. | 21 | 21 | 21 | 21 |
| Syst. | 32 | 31 | 29 | 31 |

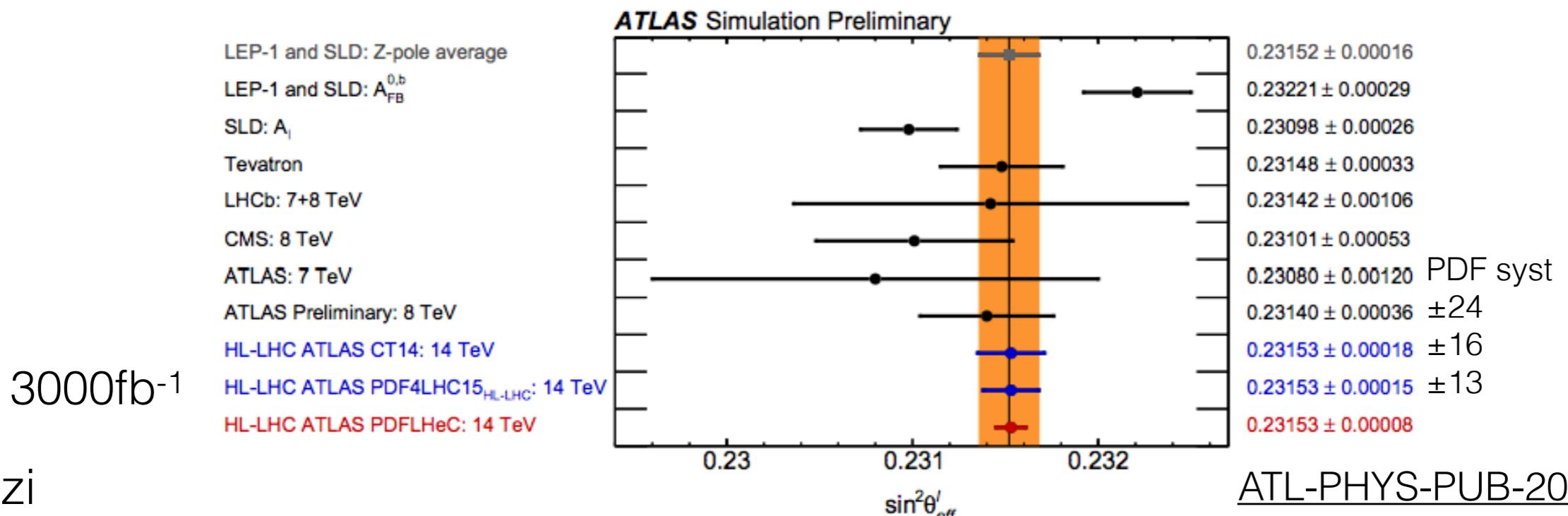


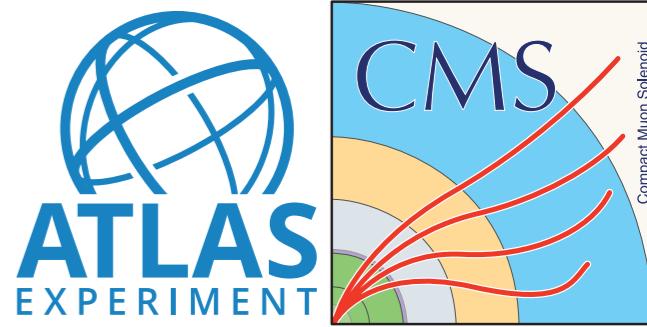


$\sin^2\theta_{\text{eff}}^f$ Prospects



- LHC Run1 measurements dominated by statistical and PDF uncertainties
- Future measurements at 13/14TeV:
 - higher statistics can more strongly constrain PDFs
 - higher dilution balanced by higher statistics
- Work ongoing in LHC EW precision group (April meeting in Durham) and PDF4LHC forum to investigate
 - EW/QED corrections, EW schemes, benchmark NNLO and resummed calculations and uncertainties
 - PDF differences and correlations





Recent W,Z Cross Section Measurements

More details in talks by Elena Yatsenko
(ATLAS) and Dylan George Hsu (CMS)



W,Z Overview

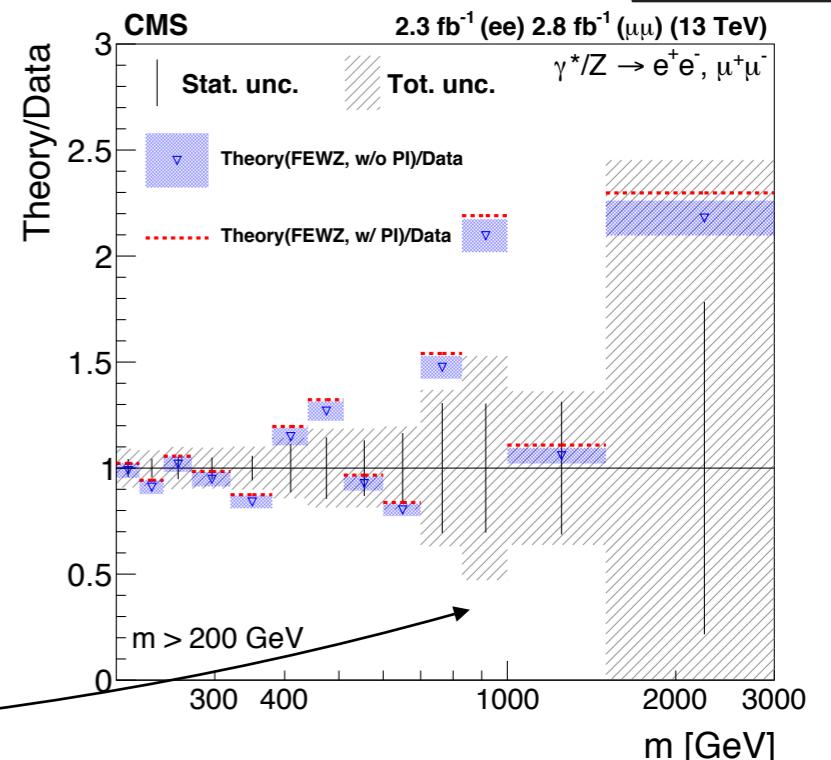
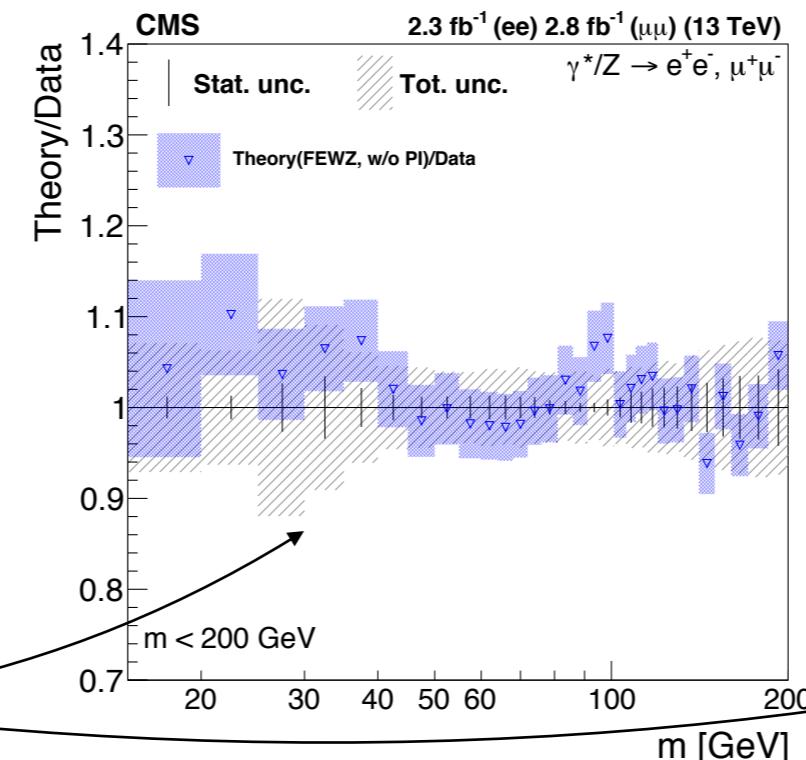
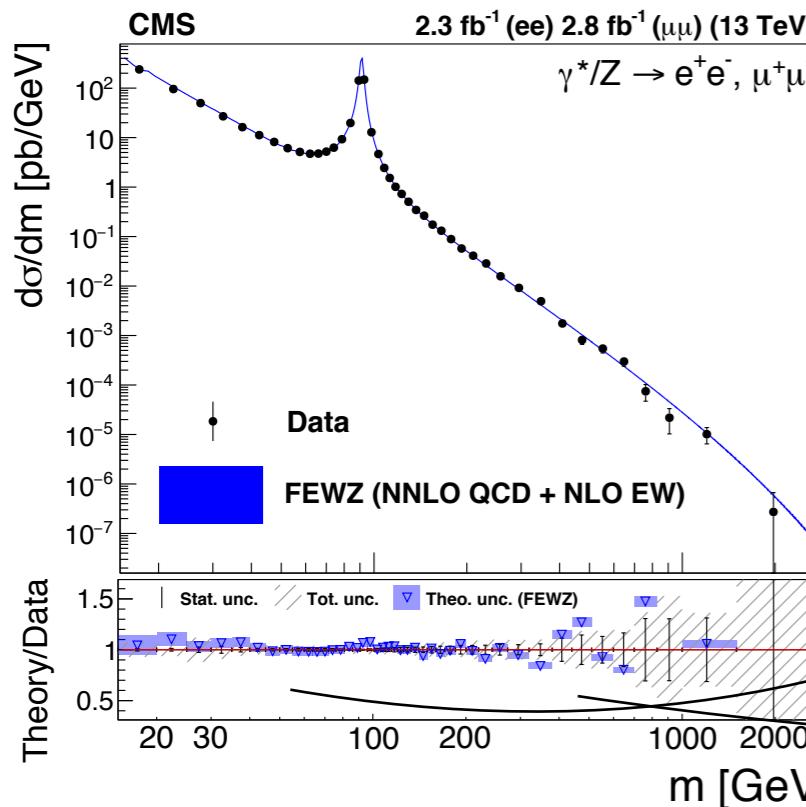
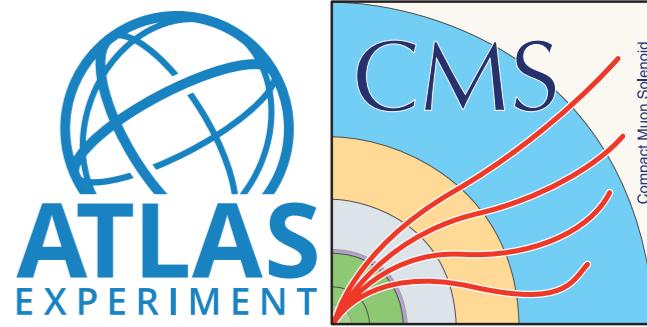


| ATLAS/CMS | | 2.76 TeV | 5 TeV | 7 TeV | 8 TeV | 13 TeV |
|-----------|----------------------------------|------------------|--------------------------------------|--|---|--|
| W | inclusive | STDM-2018-06 (*) | | | | PLB759(2016)6 |
| | $d\sigma/dpt$ | | | PRD85(2012)012005 | JHEP02(2017)096 | |
| | $d\sigma/d\eta$ | | EPJC79(2019) 128 | EPJC77(2017)367 | arXiv:1904.05631 (sub. to EPJC) EPJC76(2016)469 | |
| | asym | | EPJC79(2019) 128 | EPJC77(2017)367 PRL109(2012)111806 PRD90(2014)032004 | arXiv:1904.05631 (sub. to EPJC) EPJC76(2016)469 | |
| Z | mass | | | EPJC78(2018)110 | | |
| | inclusive | STDM-2018-06 (*) | | | | PLB759(2016)6 |
| | $d\sigma/dm$ | | | PLB725(2013)223 (high-mass), JHEP06(2014)112 (low-mass), EPJC77(2017)367, | JHEP12(2017)059, JHEP08(2016)009 (high mass) EPJC75(2015)147 | arXiv: 1812.10529 (sub. to JHEP) |
| | $d\sigma/dpt$ | | | JHEP09(2014)145 PRD85(2012)032002 | EPJC76(2016)291 JHEP02(2017)096 PLB749(2015)187 | CMS-PAS-SMP-17-010 |
| | $d\sigma/d\eta$ | | EPJC79(2019) 128 | EPJC77(2017)367 PRD85(2012)032002 JHEP12(2013)030 | JHEP12(2017)059 EPJC75(2015)147 PLB749(2015)187 | CMS-PAS-SMP-17-010 |
| | $d\sigma/d\phi^*$ | | | | EPJC76(2016)291 JHEP03(2018)172 | CMS-PAS-SMP-17-010 |
| | A _i /A _F B | | | | JHEP08(2016)159 EPJC78(2018)701 PLB750(2015)154 | |
| | $\sin 2\theta_W$ | | | | ATLAS-CONF-2018-037 EPJC78(2018)701 | |

(*) in Elena Yatsenko's talk



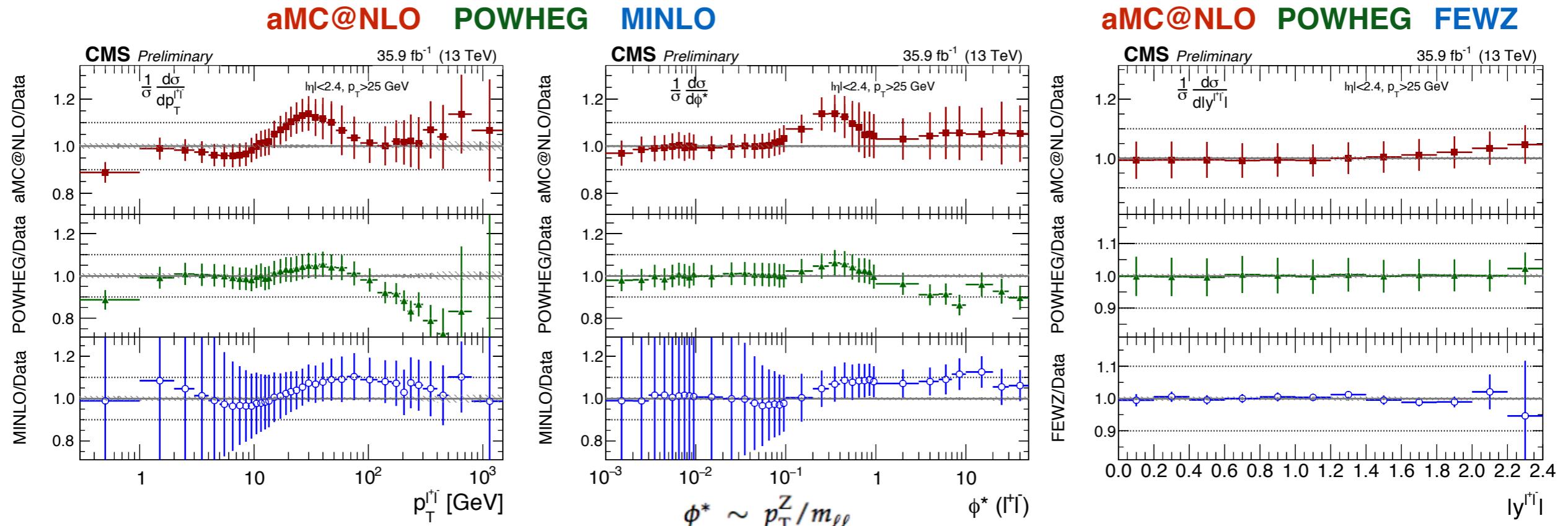
Z at 13 TeV



- ▶ $d\sigma/dm$ of Z cross section with $2.3\text{-}2.8 \text{ fb}^{-1}$ at 13 TeV (2015)
 - fiducial selection (leptons after FSR) for $Z \rightarrow \mu\mu(\text{ee})$: $p_T^l > 22(30), 10 \text{ GeV}$, $|\eta| < 2.4(2.5)$
 - cross sections in full lepton phase space corrected for FSR effects (dressed leptons)
- ▶ Full phase space cross sections in good agreement with FEWZ(NNLO QCD + NLO EW) with NNPDF3.0
 - predictions with photon-induced contributions also tested at high m_{\parallel} with FEWZ+LUXqed

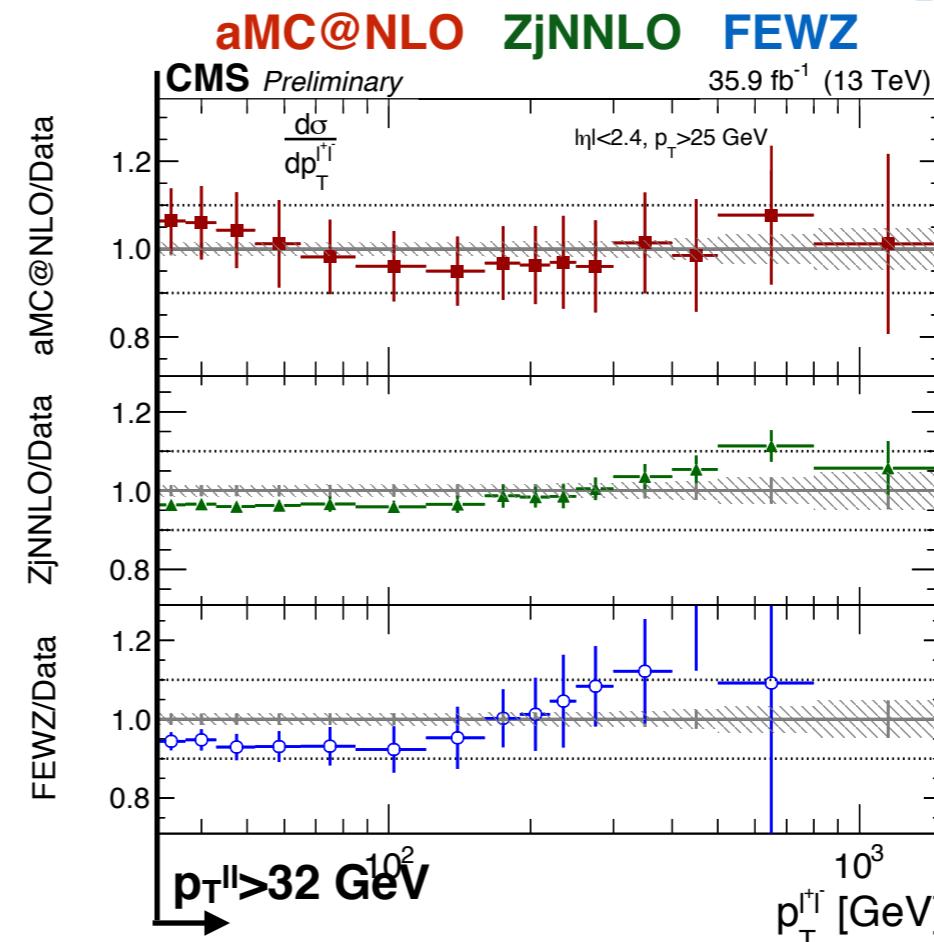
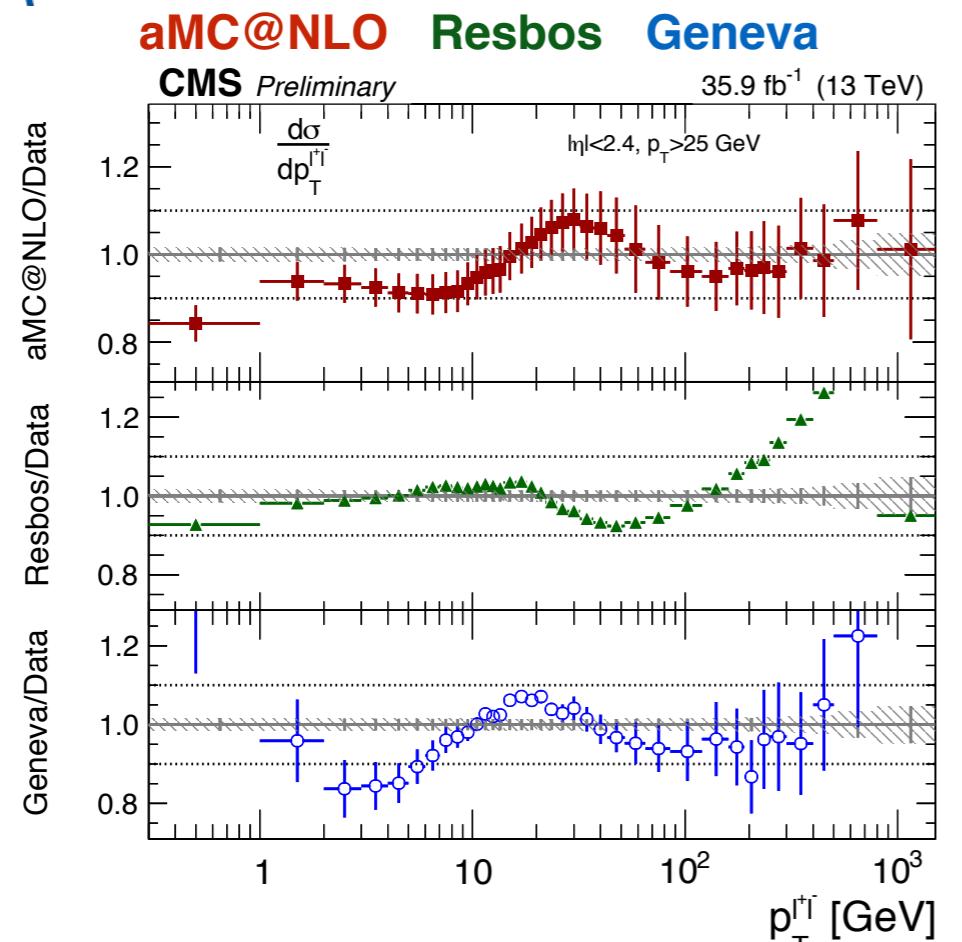


Z at 13 TeV



- p_T^{\parallel} , ϕ^* , y^{\parallel} differential Z cross section in $ee, \mu\mu$ events at 13 TeV with 35.9 fb^{-1} (also 2D p_T^{\parallel} - y^{\parallel} differential cross section)
 - fiducial selection: fiducial selection (leptons after FSR): $p_T^{\parallel} > 25 \text{ GeV}$, $|\eta| < 2.4$, $|m_{\parallel} - 91.2| < 15 \text{ GeV}$
- Normalised cross section uncertainties smaller than 0.5% for $p_T^{\parallel} < 50 \text{ GeV}$
- Measurements compared fixed-order, resummed and parton shower predictions
 - FO: Z at NNLO QCD (FEWZ) and Z+j at NNLO QCD (ZjNNLO). LO EW
 - Resummed (NNLL): Geneva, Resbos
 - PS: MadGraph5_aMC@NLO (0,1,2j at NLO, FxFx), Powheg (NLO), Powheg+MiNLO (0,1j at NLO)

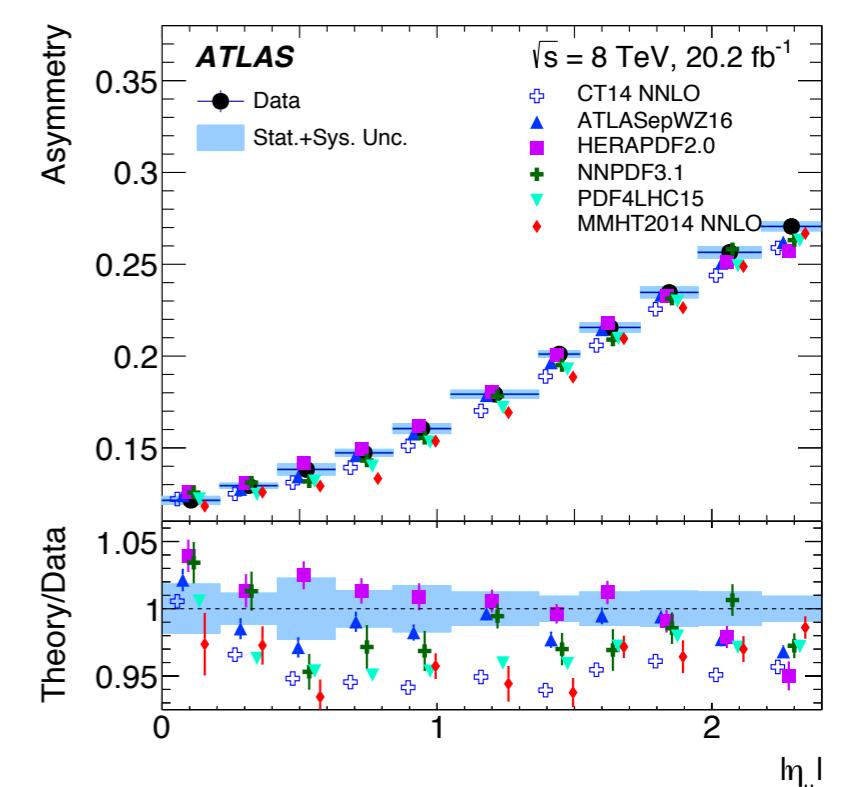
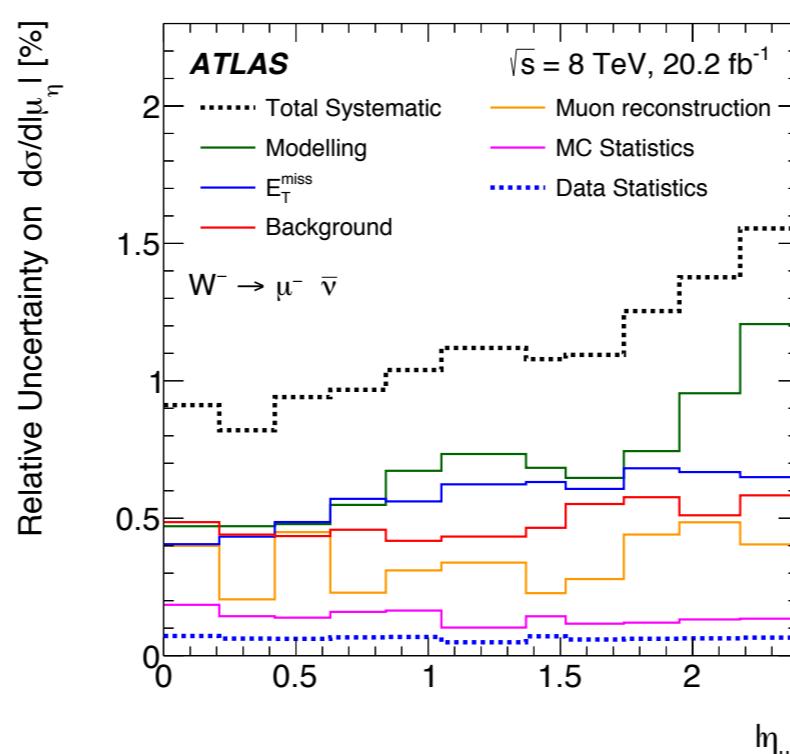
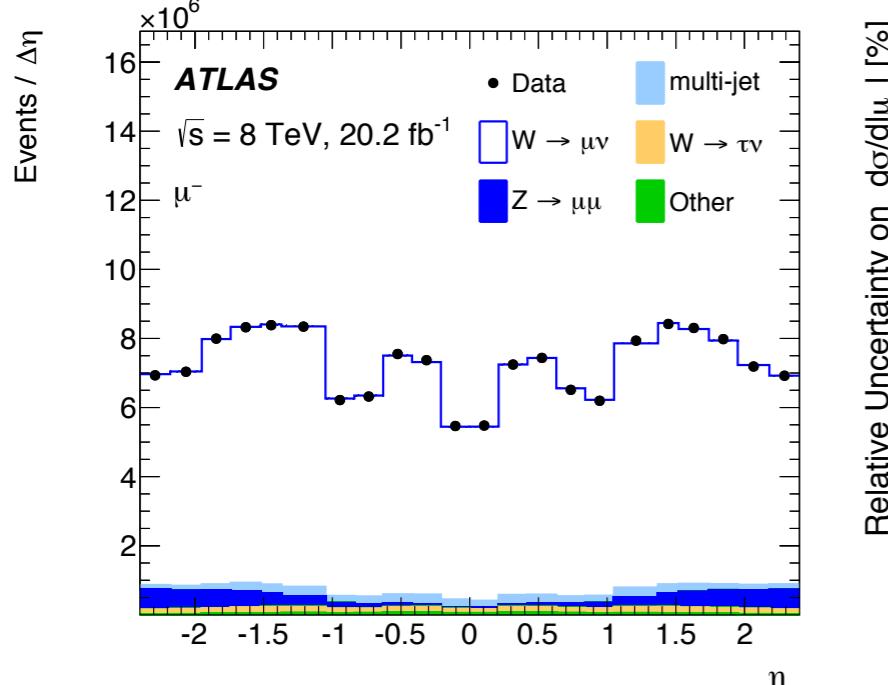
Z at 13 TeV



- ▶ $p_T^{\parallel}, \phi^*, y^{\parallel}$ differential Z cross section in $ee, \mu\mu$ events at 13 TeV with 35.9 fb^{-1} (also 2D p_T^{\parallel} - y^{\parallel} differential cross section)
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 - Resummed (NNLL): Geneva, Resbos
 - PS: MadGraph5_aMC@NLO (0,1,2j at NLO, FxFx), Powheg (NLO), Powheg+MiNLO (0,1j at NLO)



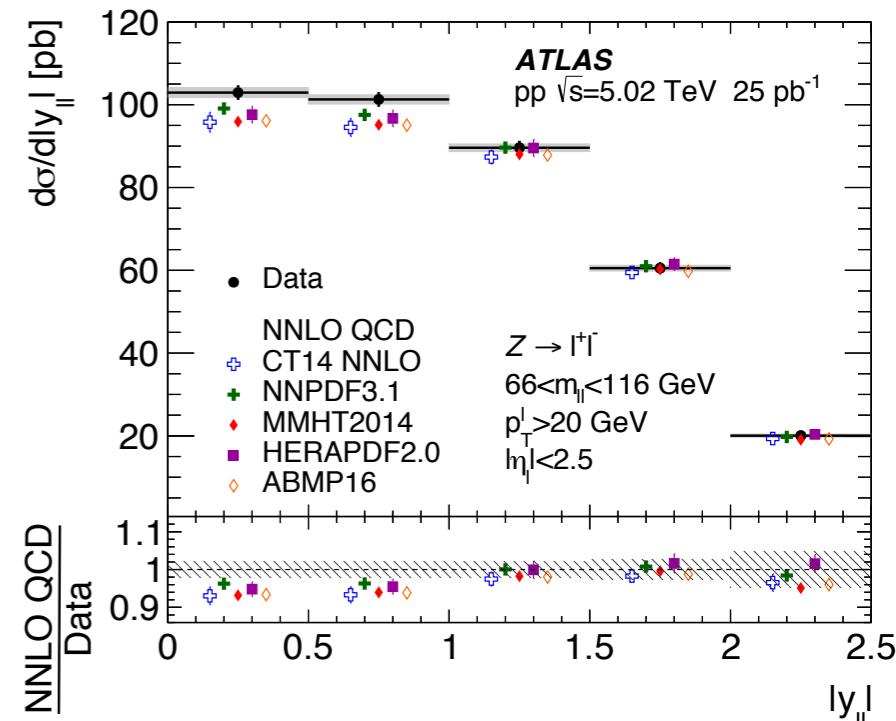
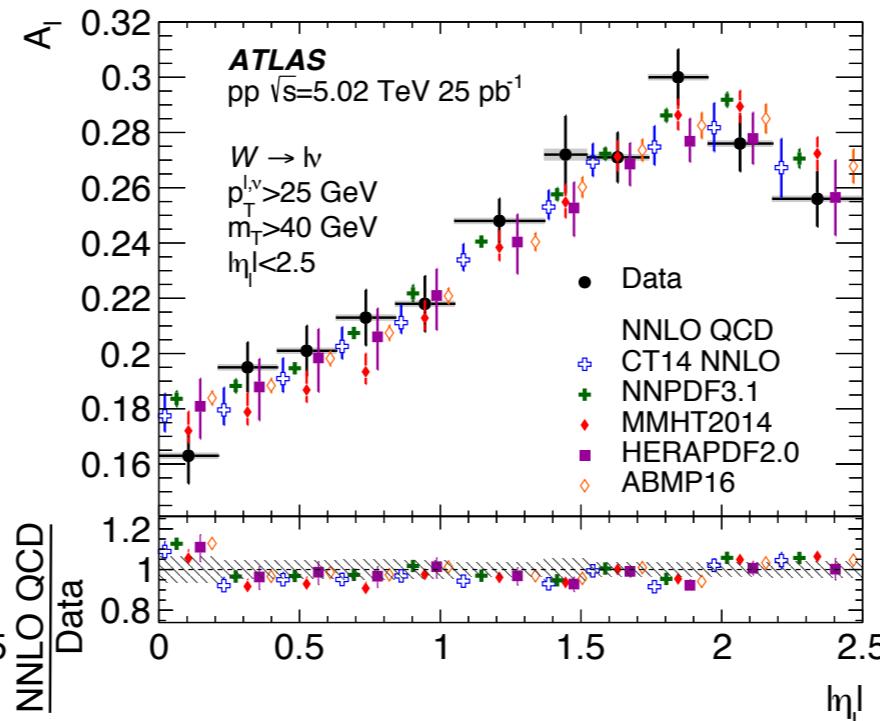
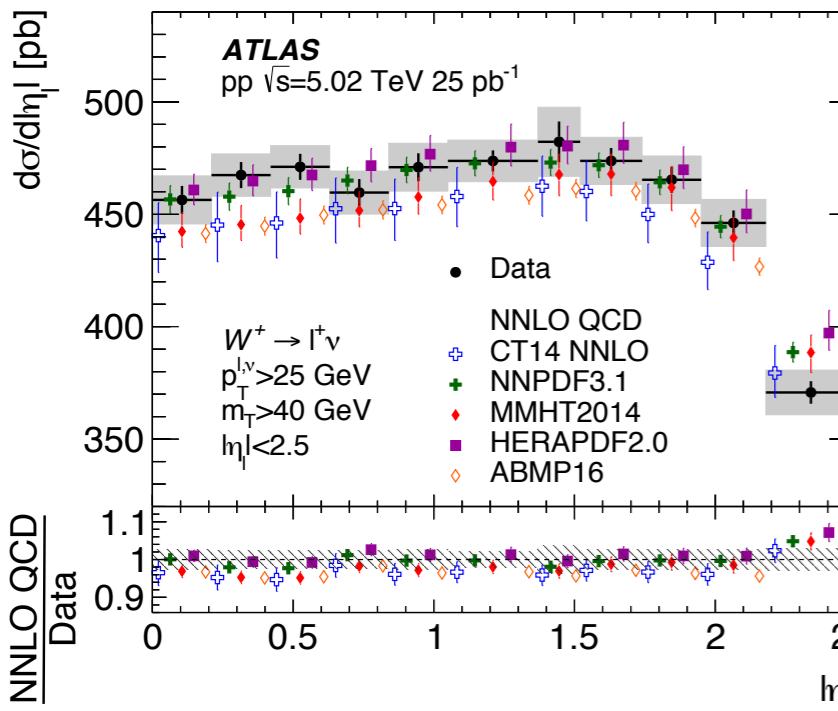
$W \rightarrow \mu\nu$ at 8 TeV



- ▶ $|\eta_\mu|$ -differential fiducial W cross section and charge asymmetry
 - $W \rightarrow \mu\nu$ events with 20 fb^{-1} of pp collisions at 8 TeV
 - results consistent with $W \rightarrow e\nu$ at 8TeV ([JHEP05\(2018\)077](#))
 - fiducial selection (born lepton): $p_T^\mu > 25 \text{ GeV}$, $p_T^\nu > 25 \text{ GeV}$, $|\eta_\mu| < 2.4$, $m_T > 40 \text{ GeV}$
- ▶ Dominant uncertainty from luminosity (1.9%), other uncertainties at ~0.5%
- ▶ Measurements compared to DYNNLO predictions with different PDF sets
 - data at 1% precision can discriminate among PDF sets



W,Z at 5 TeV



- ▶ Differential fiducial W^\pm, Z cross sections and W charge asymmetry at 5.02 TeV
 - 25 pb $^{-1}$ of pp collisions (reference for $PbPb$ run)
 - fiducial selection (born leptons):
 - W : $p_T^l > 25$ GeV, $p_T^\nu > 25$ GeV, $|\eta| < 2.5$, $m_T > 40$ GeV
 - Z : $p_T^l > 20$ GeV, $|\eta| < 2.5$, $66 < m_{ll} < 116$ GeV
- ▶ Dominant uncertainties from luminosity (1.9%) and lepton selection efficiencies
- ▶ Measurements ($\sim 2\%$ precision) compared to DYNNLO predictions with different PDF sets
 - $1-2\sigma$ deviations, in particular in central y_{ll} (consistent with 7 TeV result [EPJC77\(2017\)367](#))

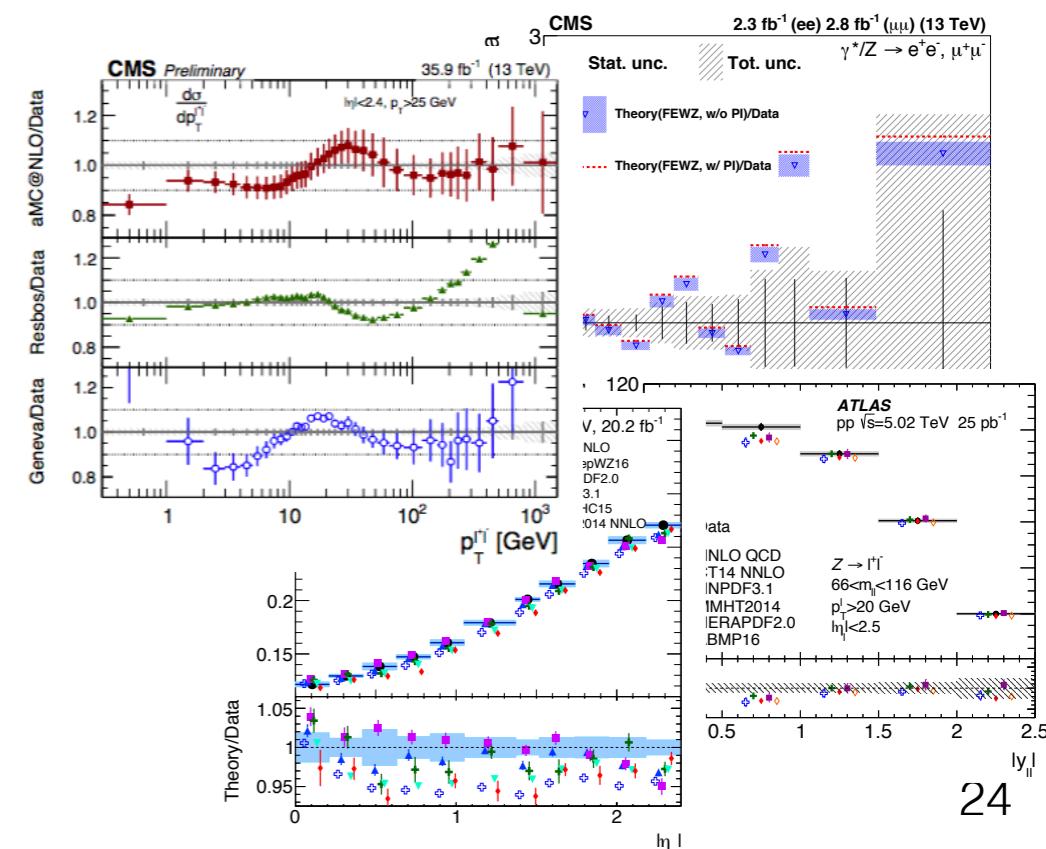
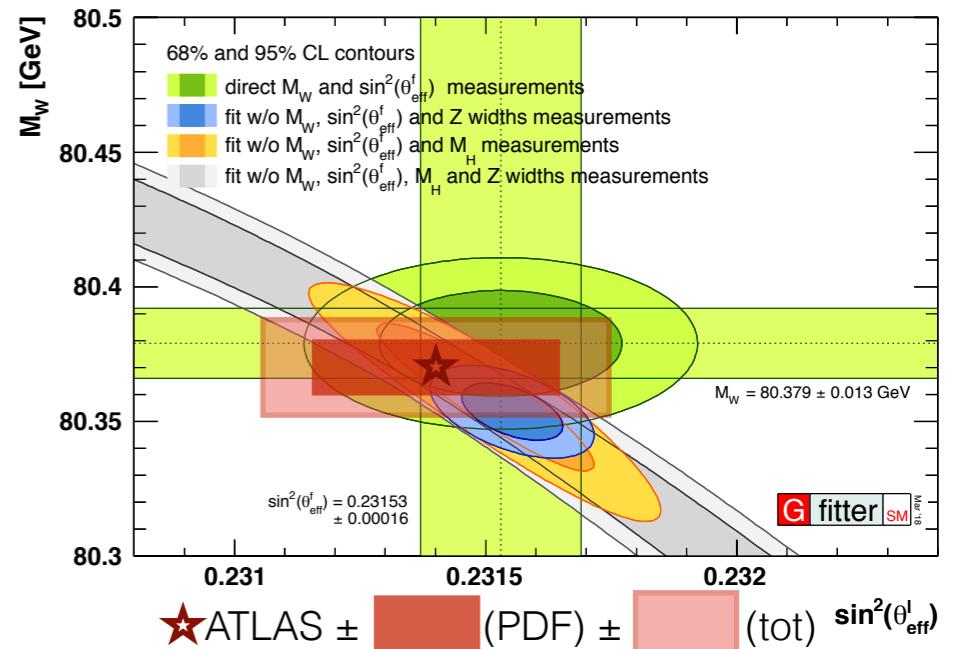


Summary

- ▶ LHC experiments reaching unprecedented precisions
 - accurate knowledge of detector at different energies and pileup conditions
 - individual LHC experiments at similar precision of combined LEP, SLD and Tevatron EW measurements
 - (multi-)differential W,Z cross sections at sub-percent precision
- ▶ Prediction uncertainties (PDFs) limiting factor in exploiting full LHC potential for EW measurements
- ▶ Experimental and theory communities working towards future measurements and combinations
 - studies of differences/correlations among PDF sets
 - studies of O(1%) corrections from EW, QED, HO and NP QCD effects and their correlations
 - better assessment of theory uncertainties
 - use of high-precision LHC data to improve knowledge of (non-)perturbative QCD and of proton structure



$$\sin^2 \theta_W = 1 - M_W^2/M_Z^2$$





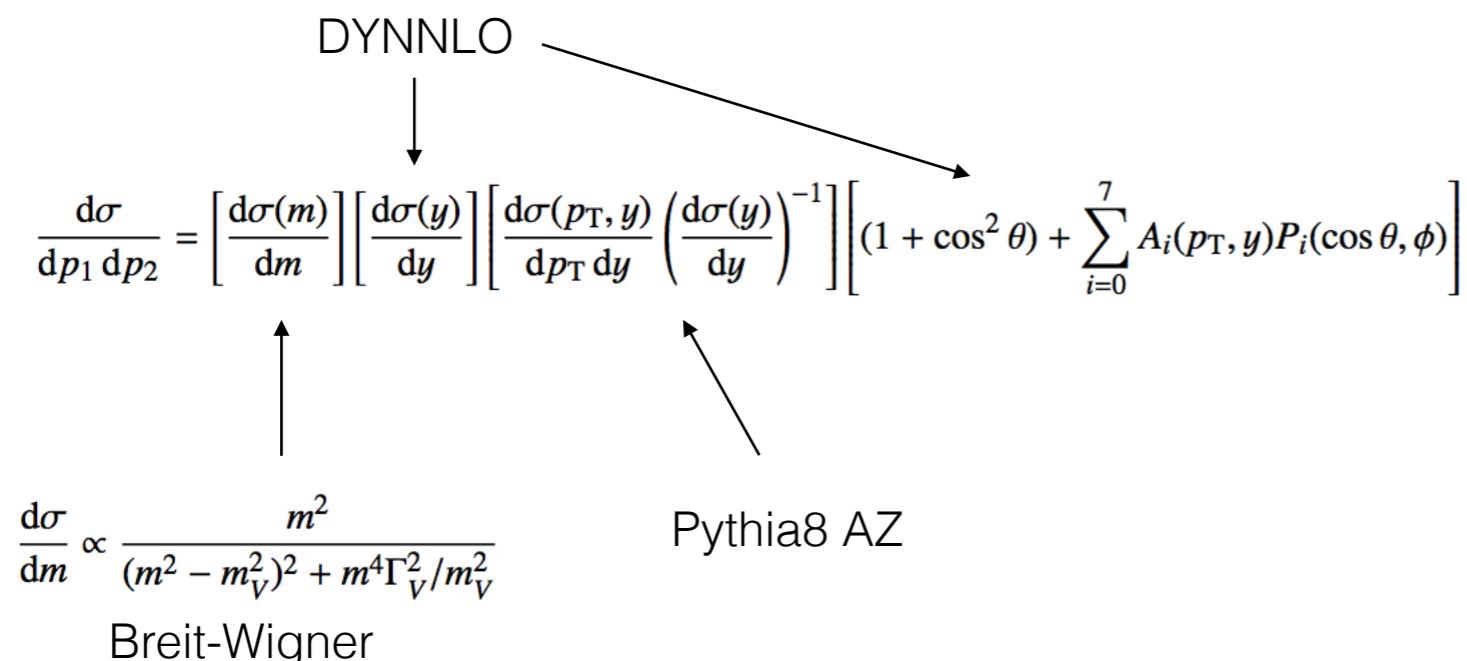
Additional Material



W mass and W pT

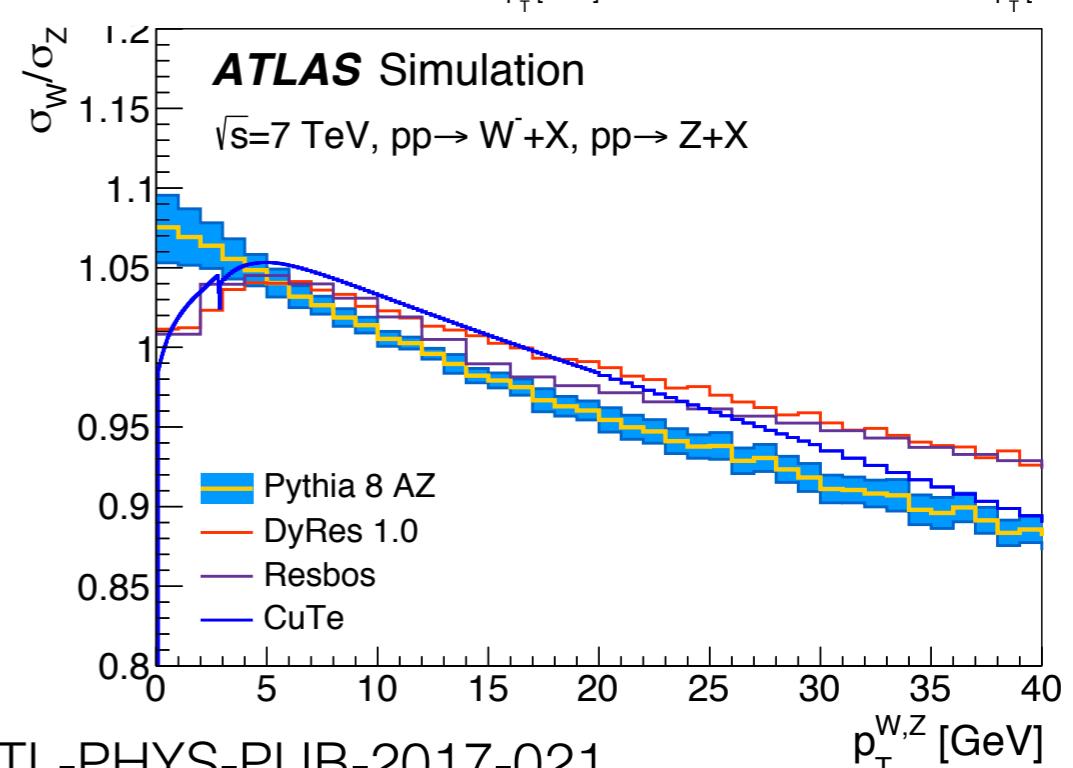
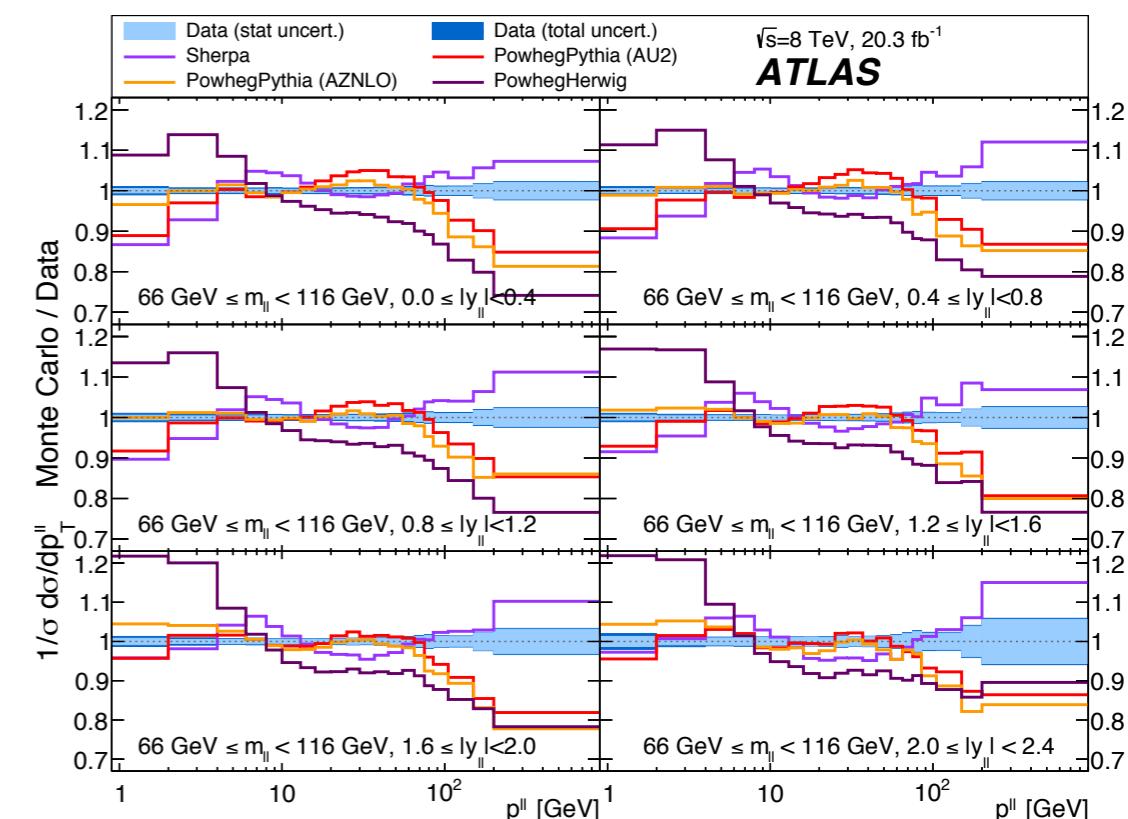


EPJC76(2016)291



| W-boson charge Kinematic distribution | W^+ | | W^- | | Combined | |
|--|------------|-------|------------|-------|------------|-------|
| | p_T^ℓ | m_T | p_T^ℓ | m_T | p_T^ℓ | m_T |
| δm_W [MeV] | | | | | | |
| Fixed-order PDF uncertainty | 13.1 | 14.9 | 12.0 | 14.2 | 8.0 | 8.7 |
| AZ tune | 3.0 | 3.4 | 3.0 | 3.4 | 3.0 | 3.4 |
| Charm-quark mass | 1.2 | 1.5 | 1.2 | 1.5 | 1.2 | 1.5 |
| Parton shower μ_F with heavy-flavour decorrelation | 5.0 | 6.9 | 5.0 | 6.9 | 5.0 | 6.9 |
| Parton shower PDF uncertainty | 3.6 | 4.0 | 2.6 | 2.4 | 1.0 | 1.6 |
| Angular coefficients | 5.8 | 5.3 | 5.8 | 5.3 | 5.8 | 5.3 |
| Total | 15.9 | 18.1 | 14.8 | 17.2 | 11.6 | 12.9 |

= PDF syst, the rest are QCD syst

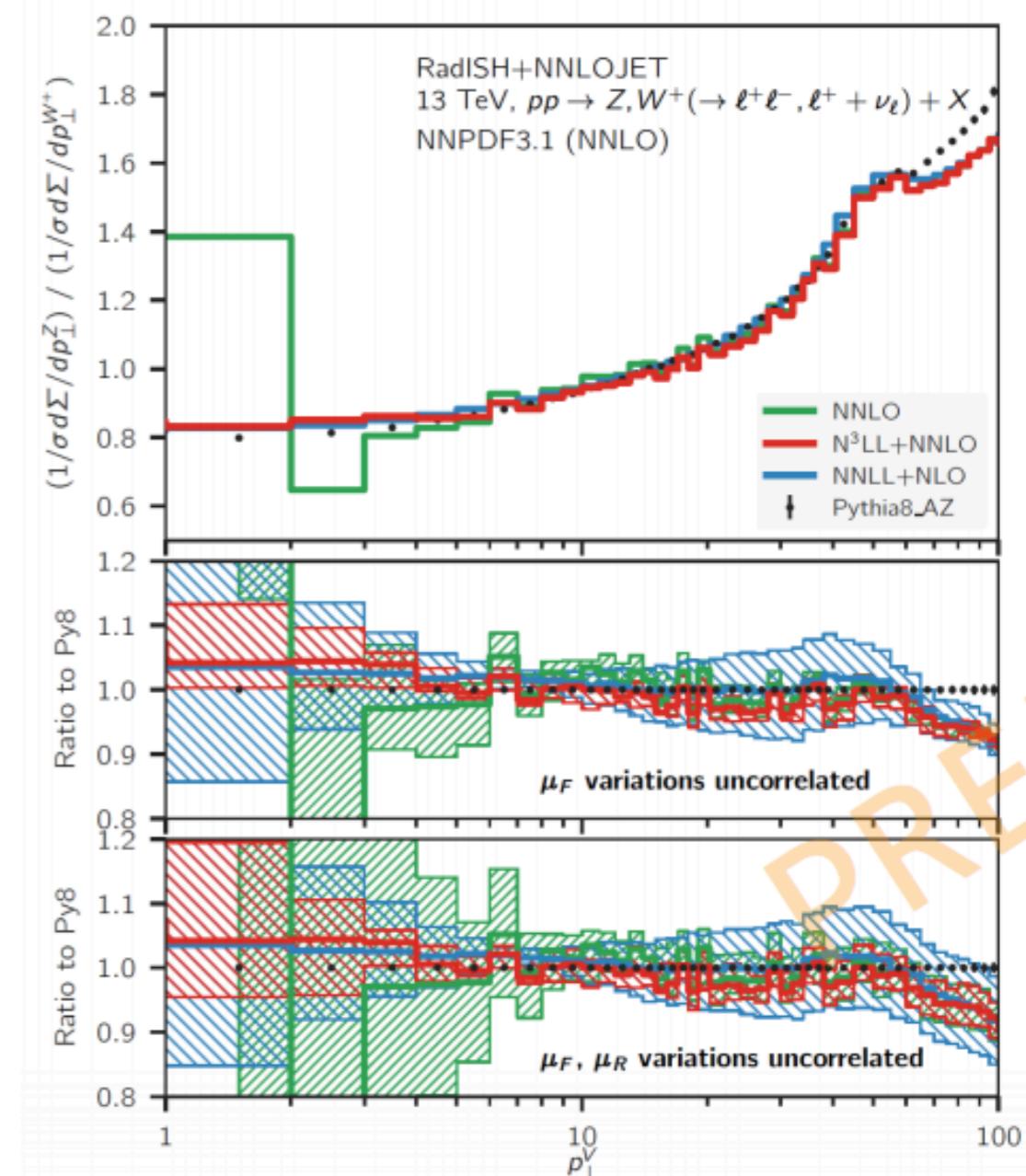




p_T^W Prospects



- ▶ Improved N3LL+NNLO predictions?
 - preferable to MC tunes which cannot model all corners of phase space and are not expected to scale properly with energy
 - MC tunes at <1% precision to be handled with care to avoid unphysical correlations
- ▶ Promising results, but 1% uncertainty won't be reached soon
 - currently good agreement with data in different eta/mass bins at 5% precision
 - uncertainty on W/Z ratio depends a lot on correlation scheme (not yet established)
- ▶ LHC W,Z measurements, at low and high μ , will help improving predictions (p_T^W , UE, PDF) and
 - study mechanisms responsible for differences in Z and W pTs (eg HF initial state partons)
 - energy dependence in p_T modelling
- ▶ Efforts ongoing in benchmarking resummed calculations within LHC EW precision group



PF Monni, SM@LHC'19



sin $2\theta_W$



- ▶ Z boson couplings differ between L- and R-handed leptons and this leads to an asymmetry in the angular distributions of charged leptons from Z decays
- ▶ This asymmetry depends on the weak mixing angle $\sin 2\theta_W$ that is the relative coupling strengths between photon and Z boson
- ▶ Differential LO cross section $Z/\gamma^* \rightarrow l l$ decay (θ is angle between lepton and quark, s is q/q CoME)
- ▶ Asymmetric term B generated by χ_1 interference between Z and γ^* (proportional to couplings not dependent on $\sin 2\theta_W$) and χ_2 Z Breit-Wigner (with vector couplings proportional to $\sin 2\theta_W$)
- ▶ Experimental asymmetry AFB (θ^* is angle between negative lepton and quark in Collin-Soper frame) depends directly on axial and vector couplings, and on $\sin 2\theta_W$ that relates the two
 - in decay lepton full phase space $A_{FB} = 3/8A4$

$$\sin^2 \theta_{OS} = 1 - \frac{m_W^2}{m_Z^2} \quad \text{on shell definition, valid at all orders}$$

$$\sin^2 \theta_{eff}^l = \left(1 - \frac{m_W^2}{m_Z^2}\right) K_Z^l$$

$$\frac{d\sigma}{d(\cos \theta)} = \frac{\alpha^2}{4s} \left[\frac{3}{8} A(1 + \cos^2 \theta) + B \cos \theta \right]$$

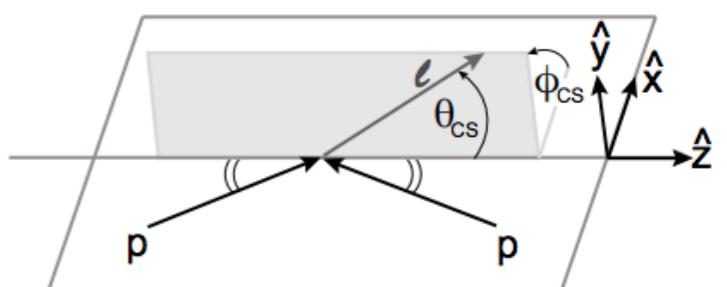
$$A = Q_l^2 Q_q^2 - 2Q_l g_V^q g_V^l \chi_1 + (g_A^{q2} + g_V^{q2})(g_A^{l2} + g_V^{l2}) \chi_2,$$

$$B = -4Q_l g_A^q g_A^l \chi_1 + 8g_A^q g_V^q g_A^l g_V^l \chi_2,$$

$$g_A^f = t_3^f$$

$$g_V^f = t_3^f - (2Q_f \times \sin^2 \theta_W)$$

$$A_{FB} = \frac{N(\cos \theta^* > 0) - N(\cos \theta^* < 0)}{N(\cos \theta^* > 0) + N(\cos \theta^* < 0)} = \frac{3B}{8A}$$

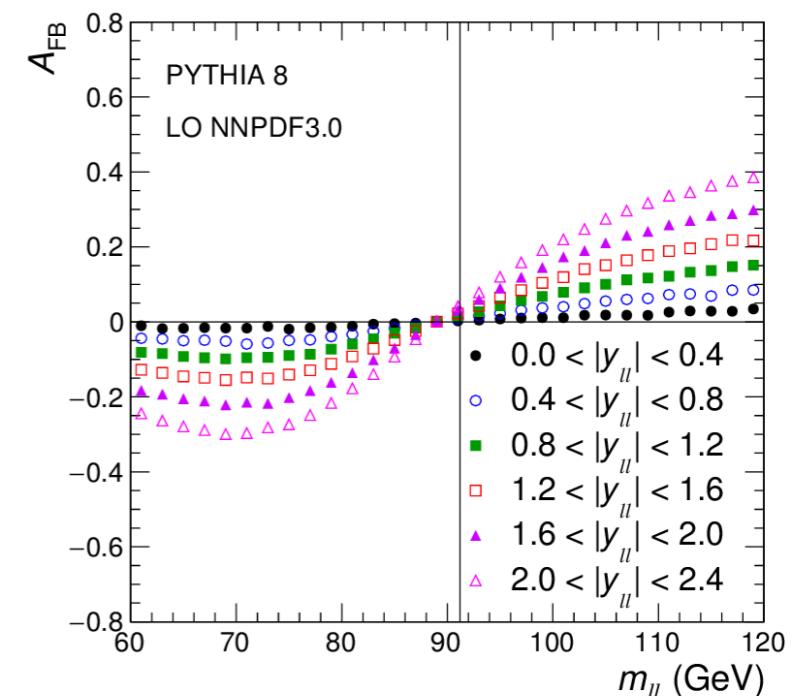
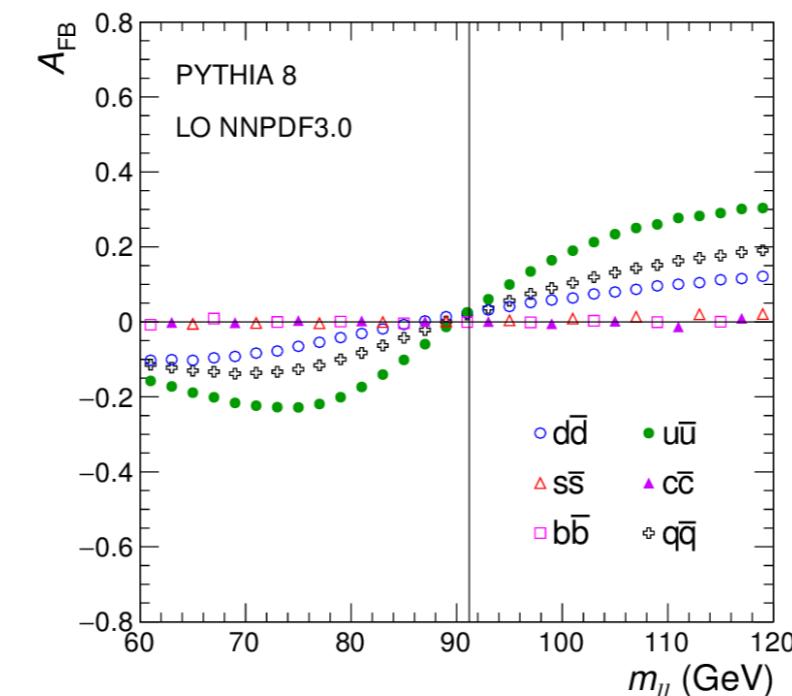
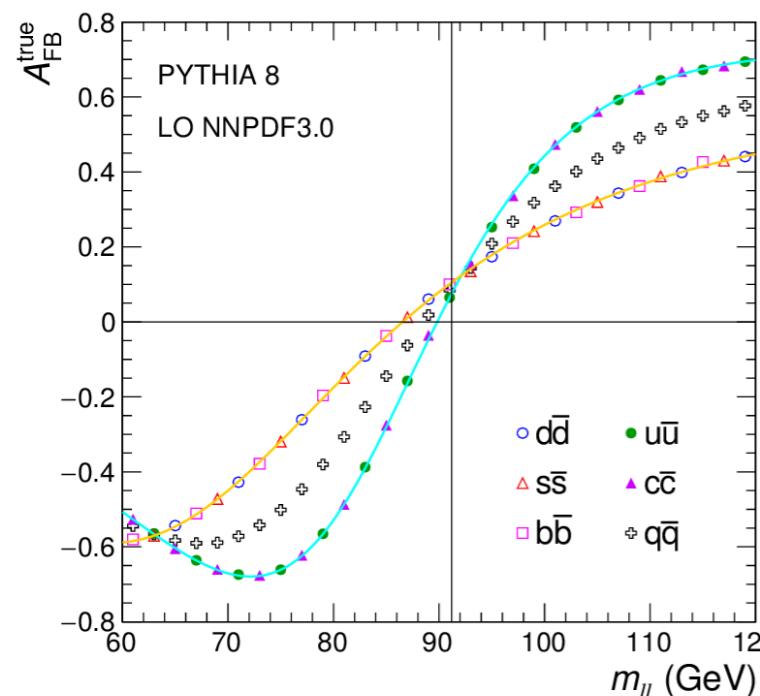
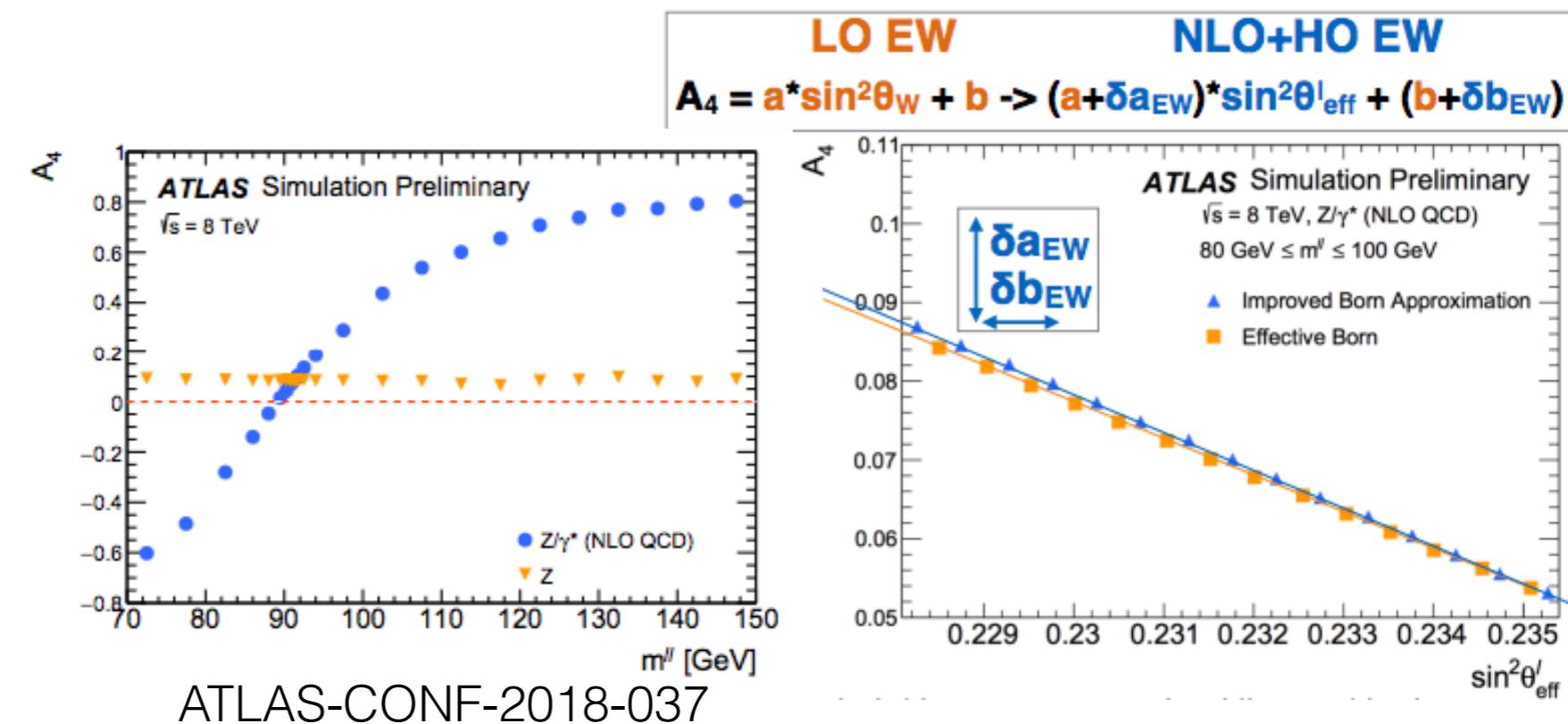




sin $2\theta_W$

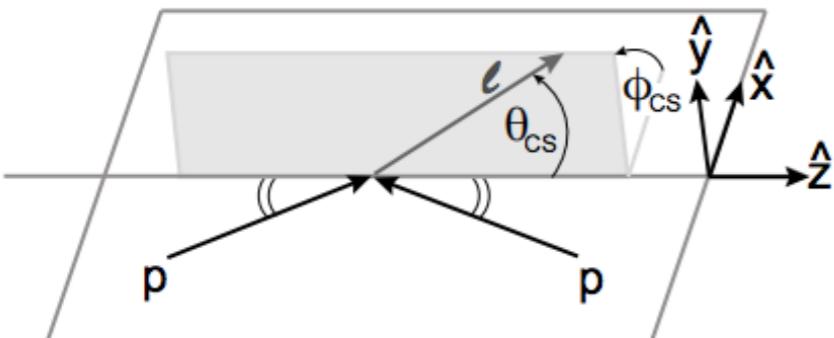


- ▶ A_{FB}, A_4 arise from
 - Z/γ^* interference (strongly m^{ll} dependent)
 - Z coupling (sensitive to $\sin^2\theta_{eff}^f$ and constant in m^{ll} , no need for fine binning in m^{ll})
- ▶ Asymmetries dependent on quark flavours and dilution effect



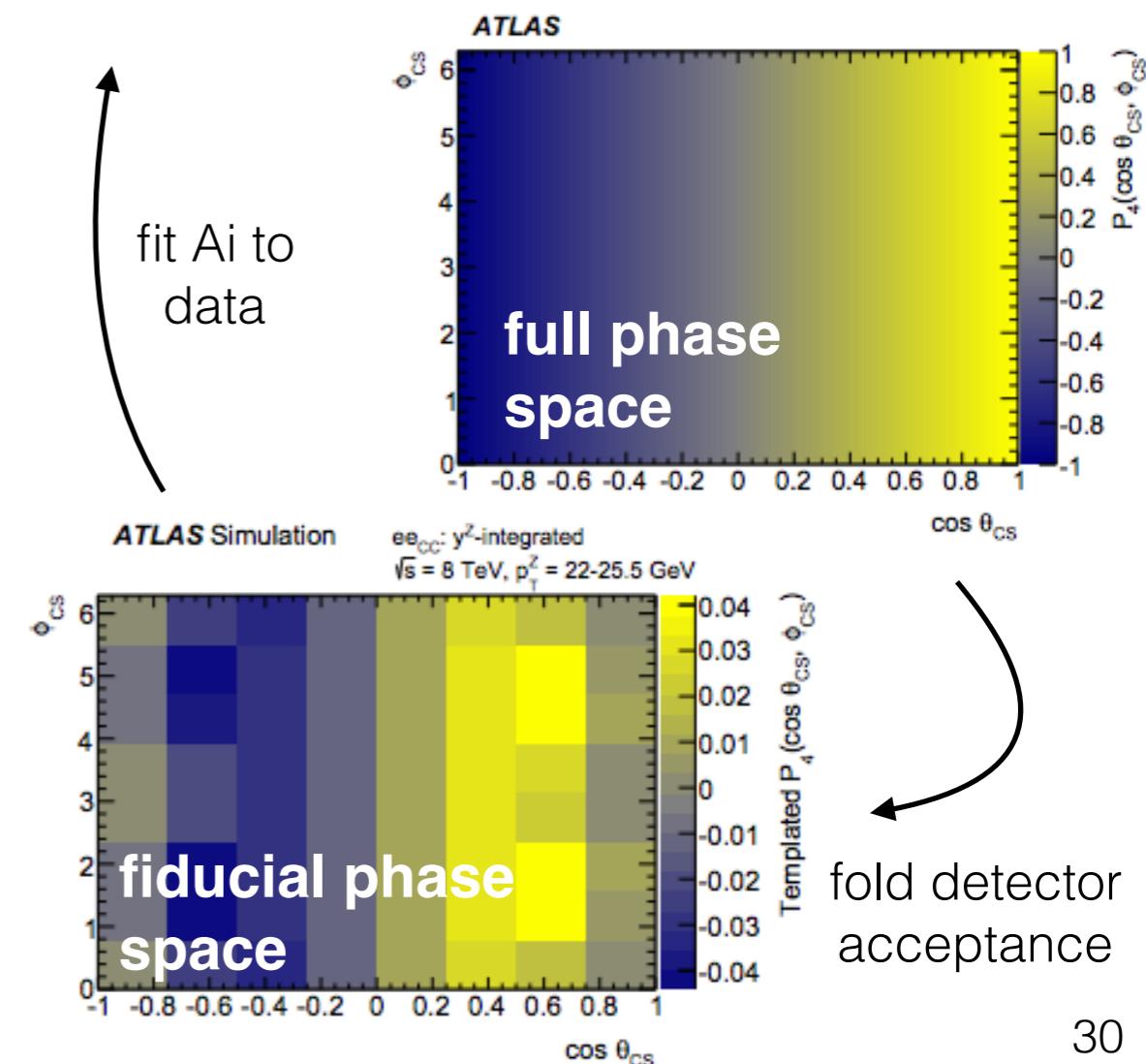


Ai vs Z3D



$$\frac{d\sigma}{dp_T^{\ell\ell} dy^{\ell\ell} dm^{\ell\ell} d\cos\theta d\phi} = \frac{3}{16\pi} \frac{d\sigma^{U+L}}{dp_T^{\ell\ell} dy^{\ell\ell} dm^{\ell\ell}} \left\{ (1 + \cos^2\theta) + \frac{1}{2} A_0(1 - 3\cos^2\theta) + A_1 \sin 2\theta \cos\phi \right. \\ \left. + \frac{1}{2} A_2 \sin^2\theta \cos 2\phi + A_3 \sin\theta \cos\phi + A_4 \cos\theta \right. \\ \left. + A_5 \sin^2\theta \sin 2\phi + A_6 \sin 2\theta \sin\phi + A_7 \sin\theta \sin\phi \right\}.$$

- Advantages of harmonic decomposition compared to fiducial cross section measurement
 - can constraint experimental systematics
 - extrapolation to full phase space reduces theory systematics and allows for channel-to-channel comparison without extrapolation
- Cons: more sensitive to NLO EW corrections (including boxes) that can break decomposition
- More details in <https://indico.cern.ch/event/749003/contributions/3329387/attachments/1826179/2988810/armbruster.pdf>





EW Corrections

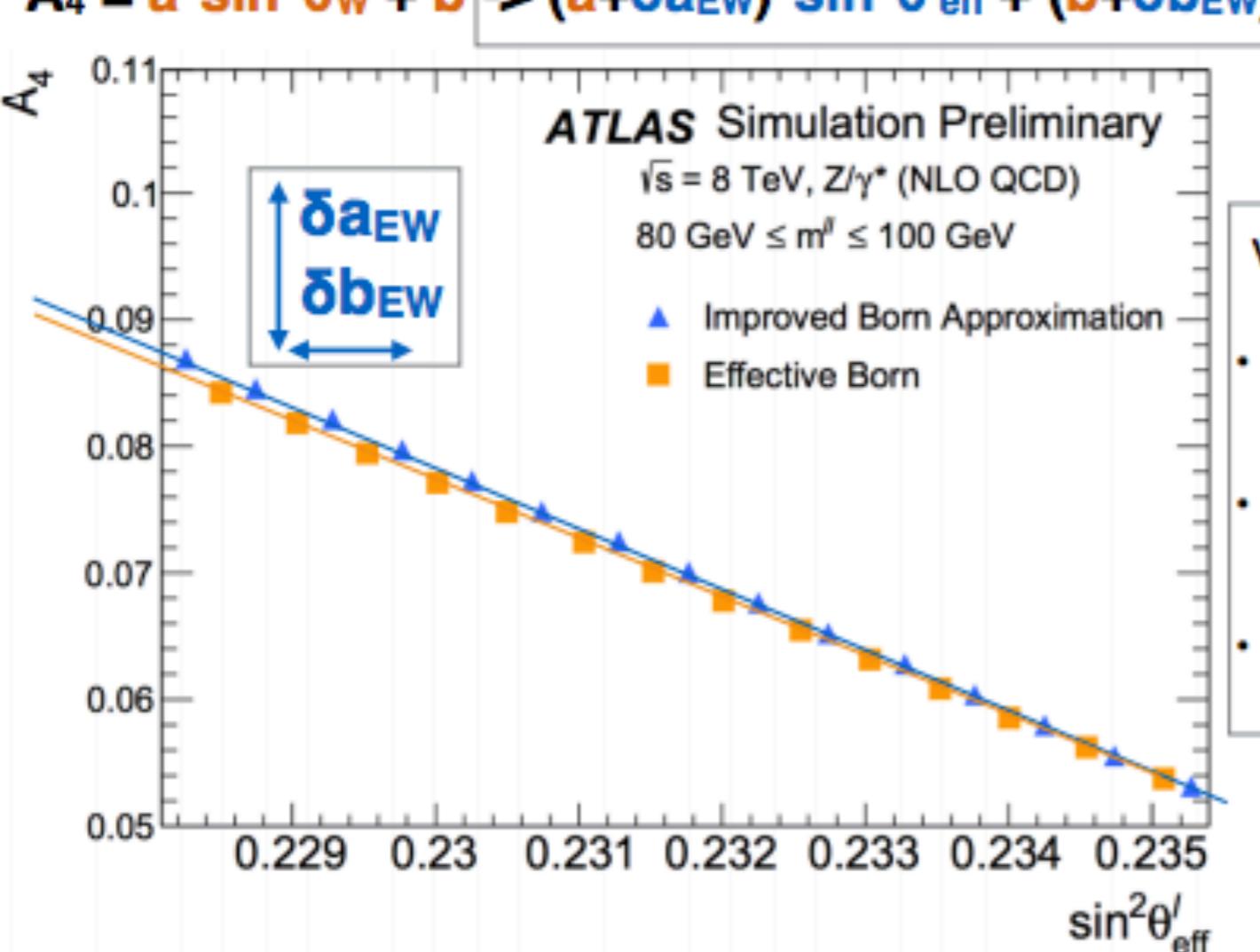


~Linear relation between A_4 and $\sin^2\theta_{\text{eff}}^l$

LO EW

$$A_4 = a * \sin^2\theta_W + b \rightarrow (a + \delta a_{\text{EW}}) * \sin^2\theta_{\text{eff}}^l + (b + \delta b_{\text{EW}})$$

NLO+HO EW



$$v_f = (2 * T_{f3} - 4 * q_f * \sin^2\theta_W * K^f(s, t)) / \Delta$$

- Compute form factors $K^f(s, t)$ using DIZET libraries
- Define *effective leptonic* WMA at $s=m^Z$
 - $\sin^2\theta_{\text{lept}}^l = \sin^2\theta_W * K^{\text{lep}}(m^Z)$

$$v_f = (2 * T_{f3} - 4 * q_f * (\sin^2\theta_W * K^f(s, t) + \delta v)) / \Delta$$

- Scan $\sin^2\theta_{\text{lept}}^l$ in predictions by scanning equivalent shift in coupling term
- Compute correction $\delta a_n^{\text{EW}}, \delta b_n^{\text{EW}}$ and add to LO EW predictions to obtain scan vs $\sin^2\theta_{\text{lept}}^l$
- Results in $\sim 25 * 10^{-5}$ shift in measurement

- ▶ A. Armbruster at DIS2019 ([link](#))



Ai Results



eeCC

| 70 < m_{ll} < 80 GeV | | | | |
|------------------------|---------|--------|-----------|----------------|
| $ y_{ll} $ | Data | Top+EW | Multijets | Non-fiducial Z |
| 0-0.8 | 106 718 | 0.023 | 0.015 | 0.010 |
| 0.8-1.6 | 95 814 | 0.015 | 0.020 | 0.010 |
| 1.6-2.5 | 47 078 | 0.012 | 0.041 | 0.009 |

| 80 < m_{ll} < 100 GeV | | | | |
|-------------------------|-----------|--------|-----------|----------------|
| $ y_{ll} $ | Data | Top+EW | Multijets | Non-fiducial Z |
| 0-0.8 | 2 697 316 | 0.003 | 0.001 | < 0.001 |
| 0.8-1.6 | 2 084 856 | 0.002 | 0.001 | < 0.001 |
| 1.6-2.5 | 839 424 | 0.002 | 0.002 | < 0.001 |

| 100 < m_{ll} < 125 GeV | | | | |
|--------------------------|---------|--------|-----------|----------------|
| $ y_{ll} $ | Data | Top+EW | Multijets | Non-fiducial Z |
| 0-0.8 | 106 855 | 0.034 | 0.016 | 0.023 |
| 0.8-1.6 | 80 403 | 0.025 | 0.019 | 0.027 |
| 1.6-2.5 | 28 805 | 0.015 | 0.025 | 0.029 |

mmCC

| 70 < m_{ll} < 80 GeV | | | | |
|------------------------|---------|--------|-----------|----------------|
| $ y_{ll} $ | Data | Top+EW | Multijets | Non-fiducial Z |
| 0-0.8 | 124 050 | 0.019 | 0.017 | 0.009 |
| 0.8-1.6 | 137 984 | 0.015 | 0.014 | 0.014 |
| 1.6-2.5 | 74 976 | 0.010 | 0.011 | 0.019 |

| 80 < m_{ll} < 100 GeV | | | | |
|-------------------------|-----------|--------|-----------|----------------|
| $ y_{ll} $ | Data | Top+EW | Multijets | Non-fiducial Z |
| 0-0.8 | 2 866 016 | 0.002 | 0.001 | < 0.001 |
| 0.8-1.6 | 2 948 371 | 0.002 | 0.001 | < 0.001 |
| 1.6-2.5 | 1 314 890 | 0.002 | 0.001 | < 0.001 |

| 100 < m_{ll} < 125 GeV | | | | |
|--------------------------|---------|--------|-----------|----------------|
| $ y_{ll} $ | Data | Top+EW | Multijets | Non-fiducial Z |
| 0-0.8 | 119 650 | 0.030 | 0.023 | 0.023 |
| 0.8-1.6 | 122 775 | 0.020 | 0.015 | 0.023 |
| 1.6-2.5 | 55 886 | 0.010 | 0.005 | 0.022 |

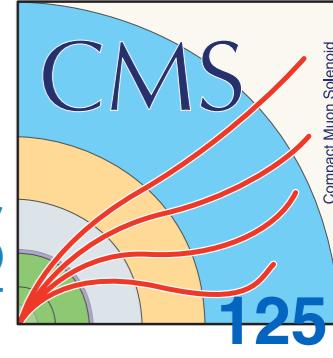
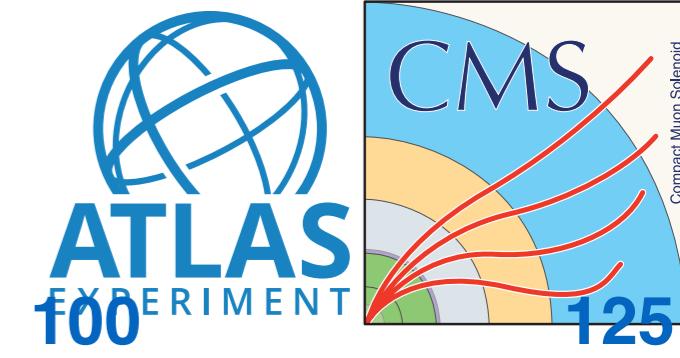
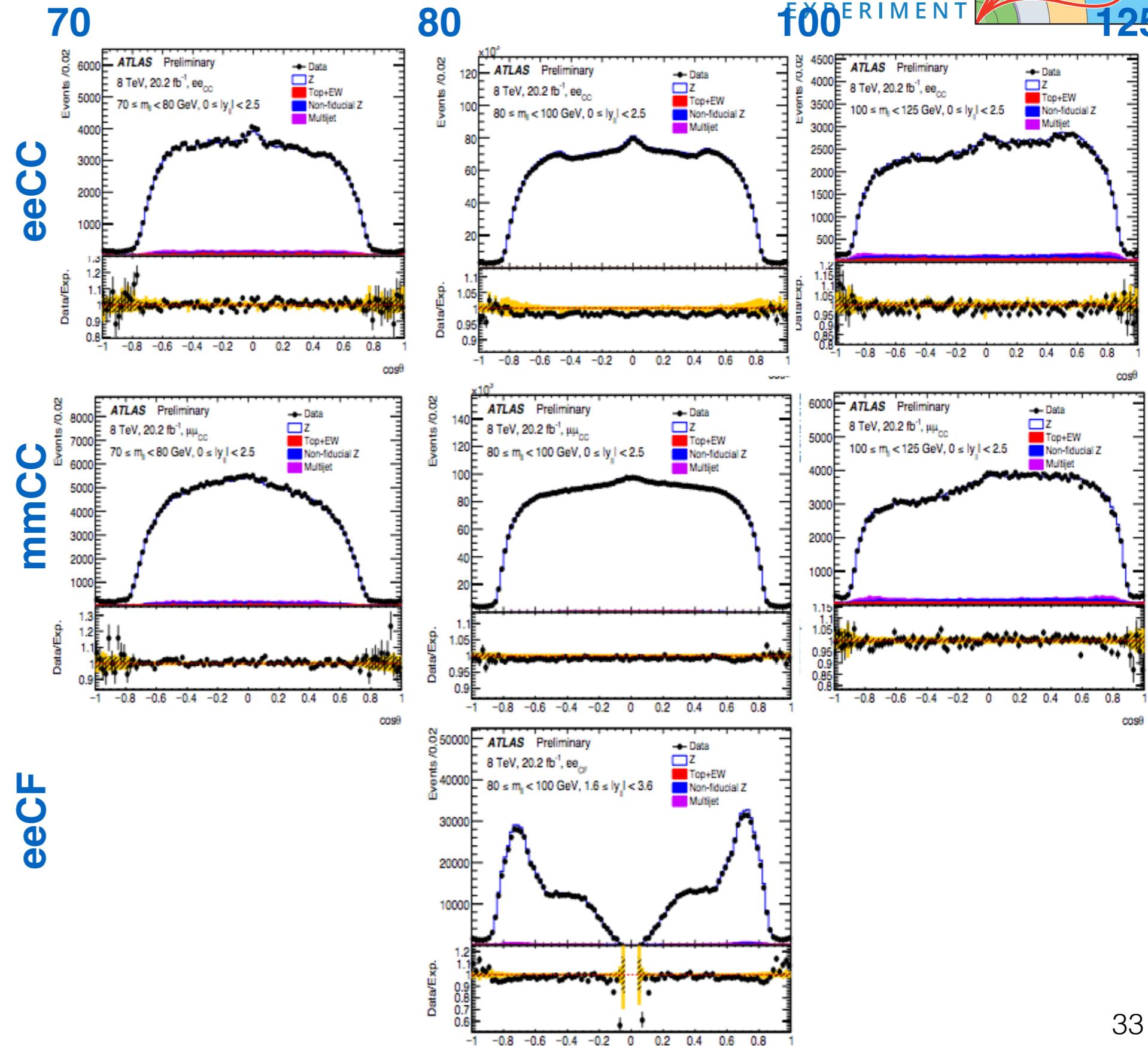
eeCF

| 80 < m_{ll} < 100 GeV | | | | |
|-------------------------|---------|--------|-----------|----------------|
| $ y_{ll} $ | Data | Top+EW | Multijets | Non-fiducial Z |
| 1.6-2.5 | 702 142 | 0.001 | 0.010 | 0.017 |
| 2.5-3.6 | 441 104 | 0.001 | 0.011 | 0.013 |



Ai Control Plots

- Good modelling of angular distributions between data and MC “prefit”
- Angular coefficients measured in-situ → theory modelling corrected within fit
- Very high and very low $|\cos\theta|$ regions in eeCF related to pTZ modelling
 - little impact on measured $\sin 2\theta_W$, covered by systematics
- Large lever-arm in eeCF channel: contributes to superiority of channel





CMS sin $2\theta_W$



$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta^*} = \frac{3}{8} \left[1 + \cos^2 \theta^* + \frac{A_0}{2} (1 - 3 \cos^2 \theta^*) + A_4 \cos \theta^* \right]$$

The A_{FB} value in each $(m_{\ell\ell}, y_{\ell\ell})$ bin is calculated using the “angular event weighting” method, described in Ref. [40], in which each event with a $\cos \theta^*$ value (denoted as “ c ”), is reflected in the denominator (D) and numerator (N) weights through:

$$w_D = \frac{1}{2} \frac{c^2}{(1 + c^2 + h)^3}, \quad (8)$$

$$w_N = \frac{1}{2} \frac{|c|}{(1 + c^2 + h)^2}, \quad (9)$$

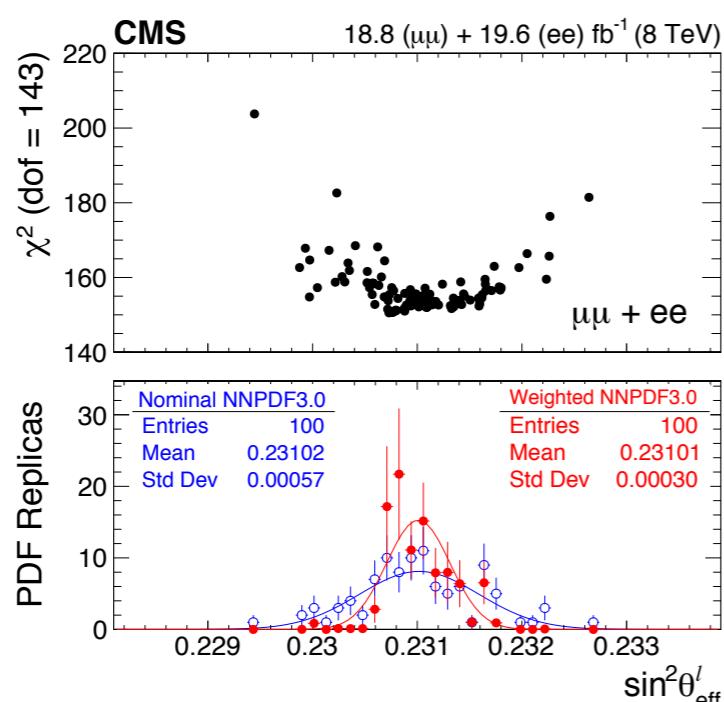
where $h = 0.5A_0(1 - 3c^2)$. Here, as a baseline we use the $p_{T,\ell\ell}$ -averaged A_0 value of about 0.1 in each measurement $(m_{\ell\ell}, y_{\ell\ell})$ bin, as predicted by the signal MC simulation. Using the weighted sums N and D for forward ($\cos \theta^* > 0$) and backward ($\cos \theta^* < 0$) events, we obtain

$$D_F = \sum_{c>0} w_D, \quad D_B = \sum_{c<0} w_D, \quad (10)$$

$$N_F = \sum_{c>0} w_N, \quad N_B = \sum_{c<0} w_N, \quad (11)$$

from which the weighted A_{FB} of Eq. (2) can be written as:

$$A_{FB} = \frac{3}{8} \frac{N_F - N_B}{D_F + D_B}. \quad (12)$$



| Source | Muons | Electrons |
|-----------------------------|---------|-----------|
| Size of MC event sample | 0.00015 | 0.00033 |
| Lepton selection efficiency | 0.00005 | 0.00004 |
| Lepton momentum calibration | 0.00008 | 0.00019 |
| Background subtraction | 0.00003 | 0.00005 |
| Modeling of pileup | 0.00003 | 0.00002 |
| Total | 0.00018 | 0.00039 |

| Modeling parameter | Muons | Electrons |
|--|---------|-----------|
| Dilepton p_T reweighting | 0.00003 | 0.00003 |
| μ_R and μ_F scales | 0.00011 | 0.00013 |
| POWHEG MINLO Z+j vs. Z at NLO | 0.00009 | 0.00009 |
| FSR model (PHOTOS vs. PYTHIA 8) | 0.00003 | 0.00005 |
| Underlying event | 0.00003 | 0.00004 |
| Electroweak $\sin^2 \theta_{\text{eff}}^l$ vs. $\sin^2 \theta_{\text{eff}}^{\text{u,d}}$ | 0.00001 | 0.00001 |
| Total | 0.00015 | 0.00017 |

| Channel | Statistical uncertainty |
|-----------|-------------------------|
| Muons | 0.00044 |
| Electrons | 0.00060 |
| Combined | 0.00036 |

| Channel | Not constraining PDFs | Constraining PDFs |
|-----------|-----------------------|-----------------------|
| Muons | 0.23125 ± 0.00054 | 0.23125 ± 0.00032 |
| Electrons | 0.23054 ± 0.00064 | 0.23056 ± 0.00045 |
| Combined | 0.23102 ± 0.00057 | 0.23101 ± 0.00030 |



$\sin^2\theta_W$ PDF uncertainty



- As measurement performed in m_Z and yZ bins, PDF correlation patterns are important in final impact of PDF syst on measurement
 - PDF and $\sin^2\theta_W$ correlations very different in m_{ll}
- Correlations exploited to reduce PDF syst by constraints to data

[EPJC78\(2018\)701](#)

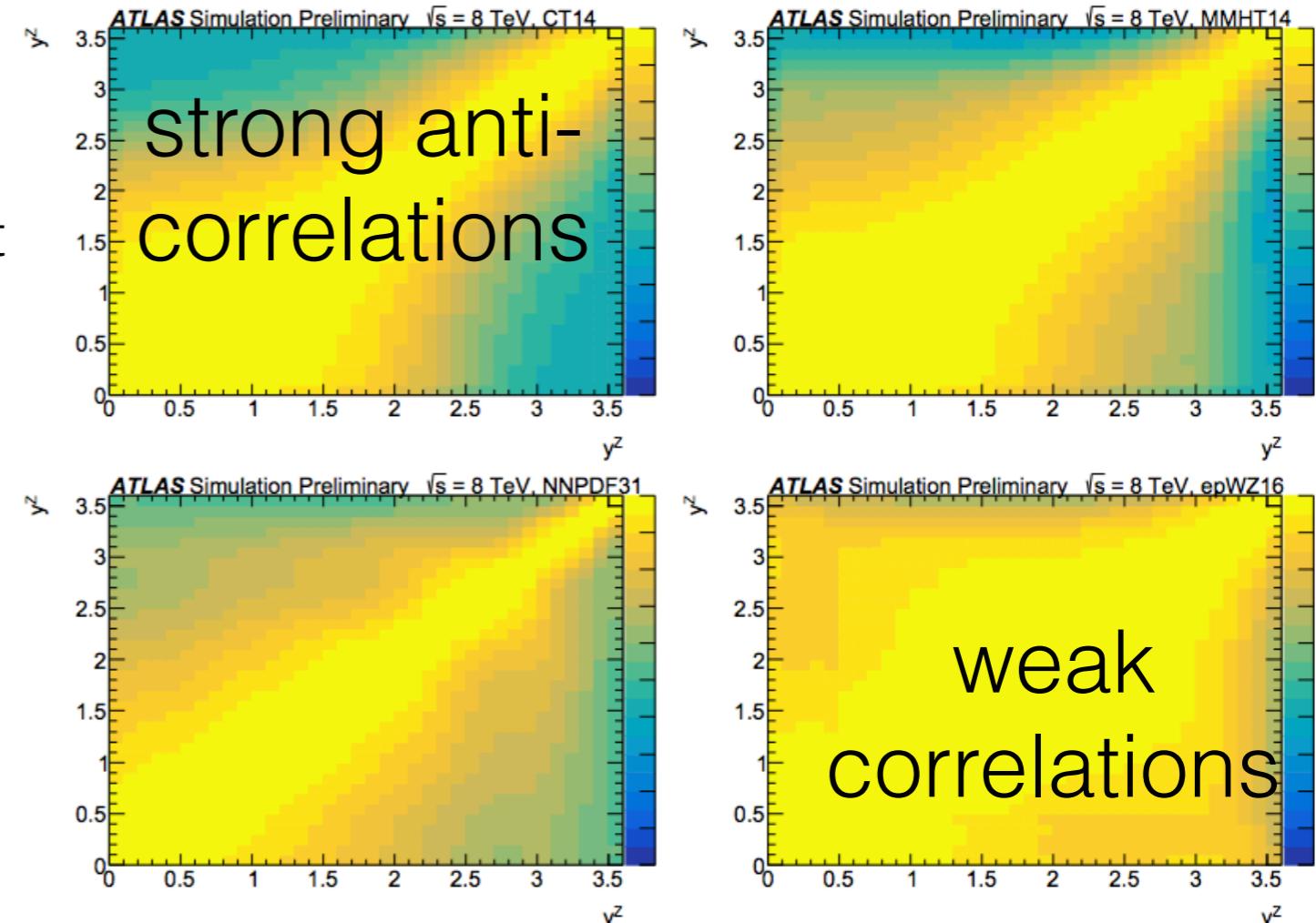
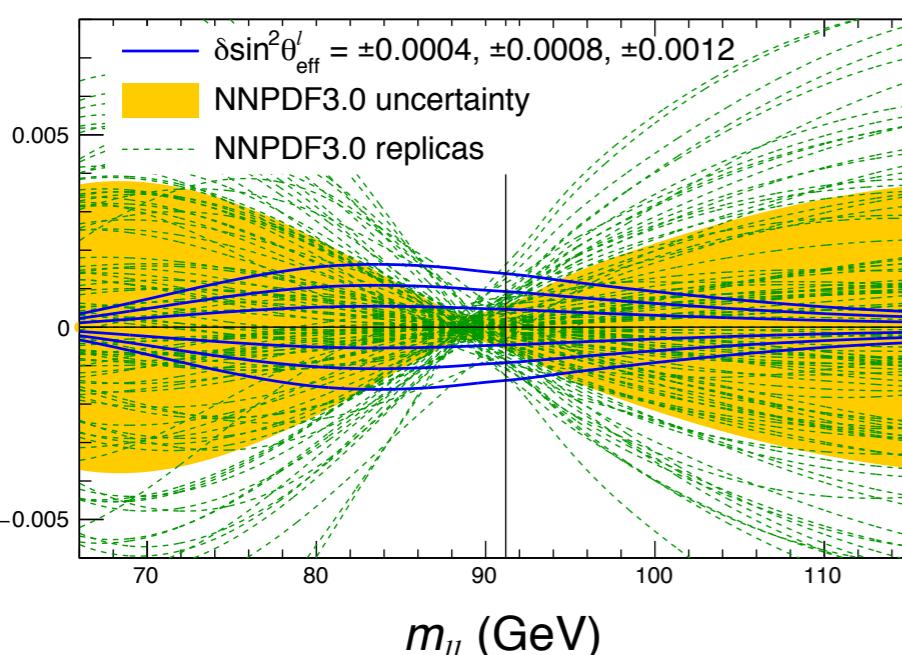
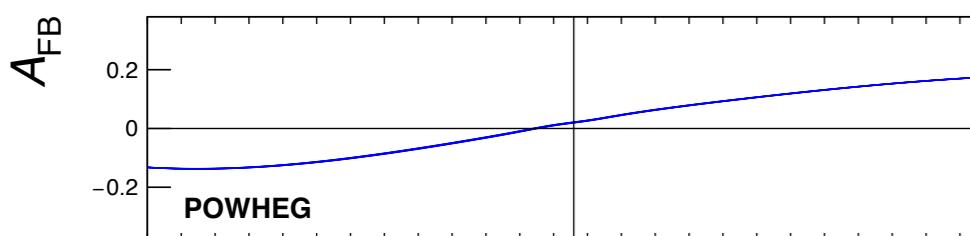
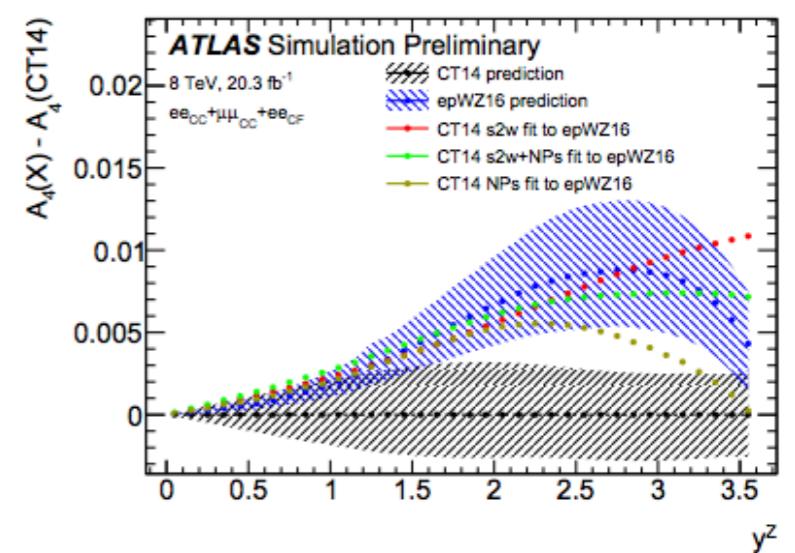
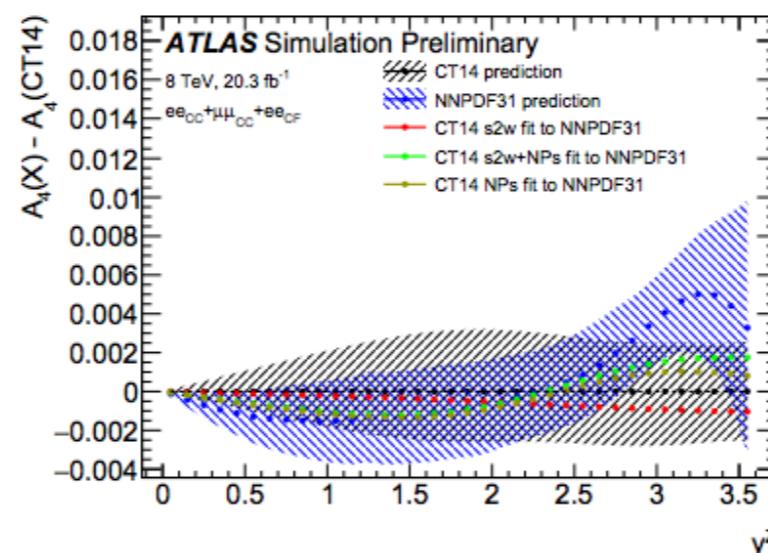
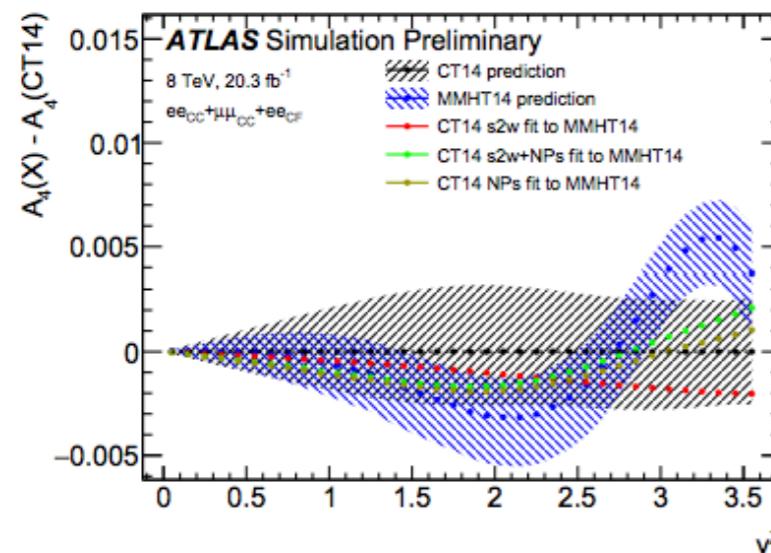
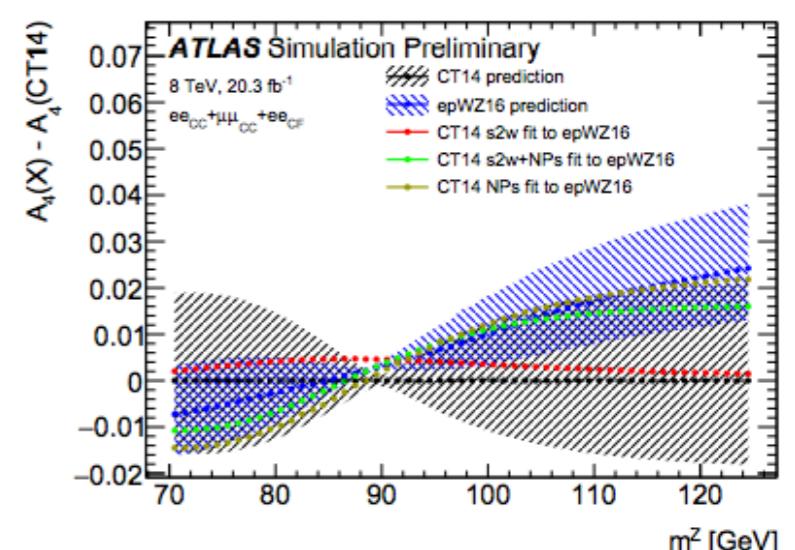
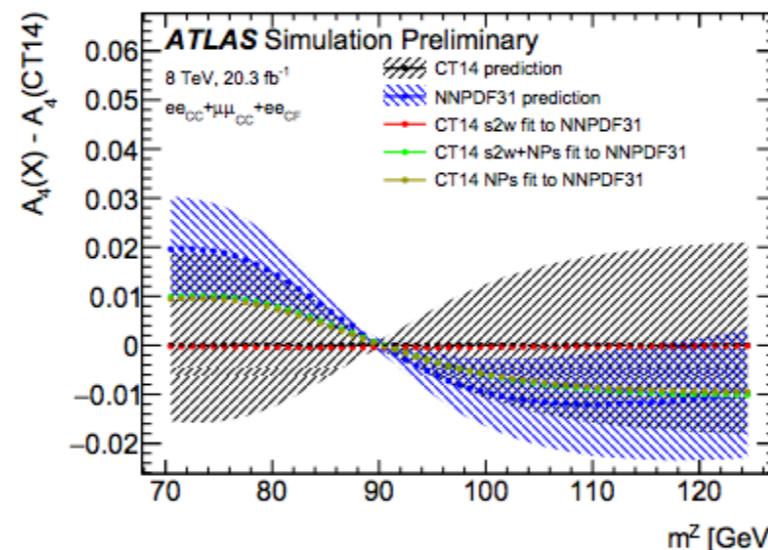
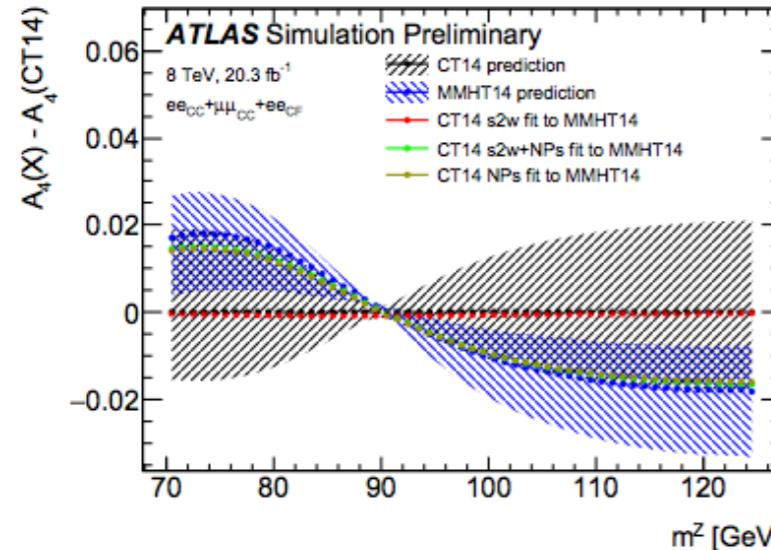


Figure 4: Correlations between the predicted angular coefficient A_4 as a function of y^Z , shown for the CT14 (top left), MMHT14 (top right), NNPDF31 (bottom left), and ATLAS epWZ16 (bottom right) PDF sets. The colour scale runs over the whole range from +1 (yellow) to -1 (blue).

[ATL-PHYS-PUB-2018-004](#)



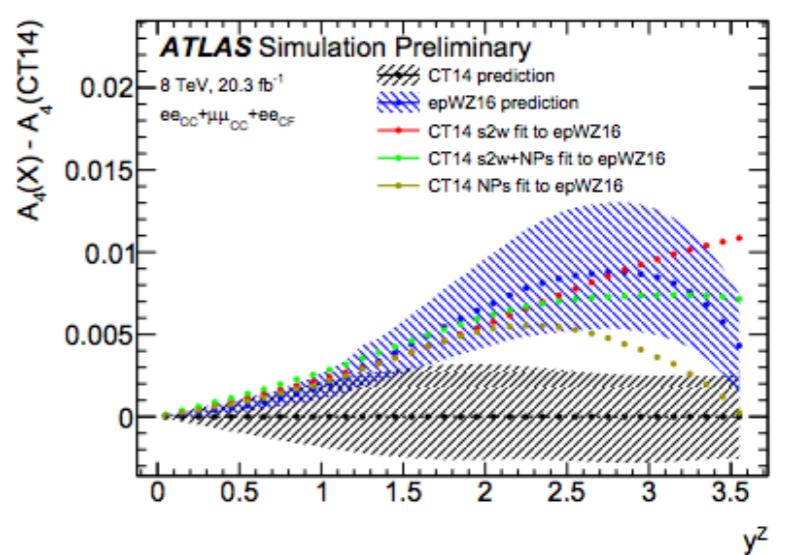
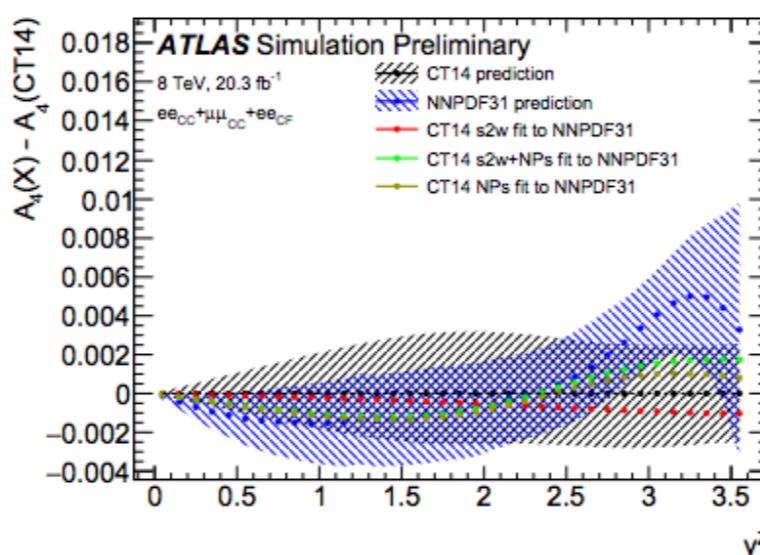
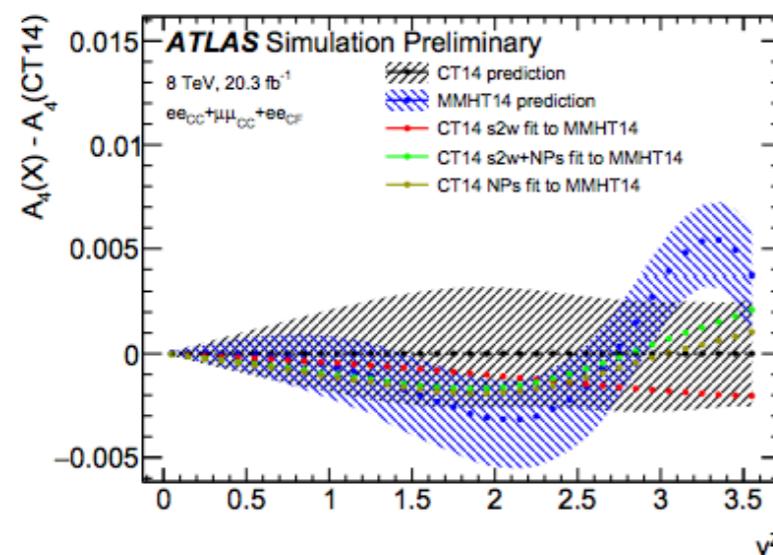
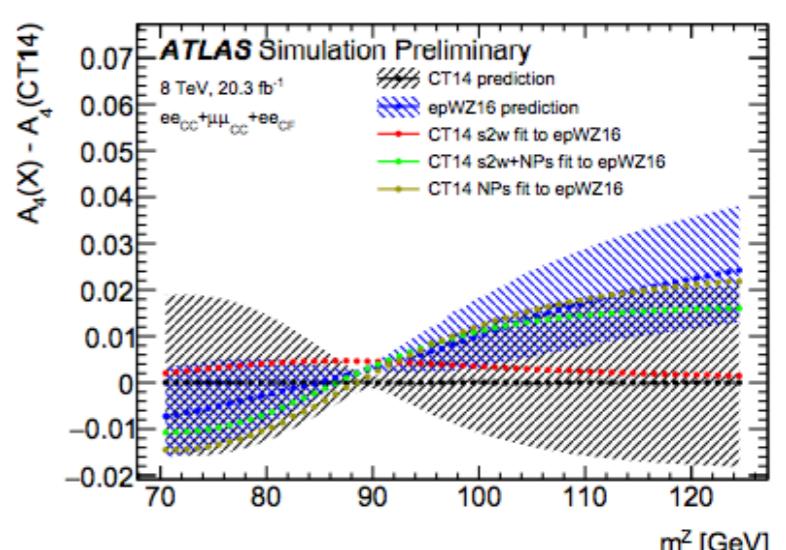
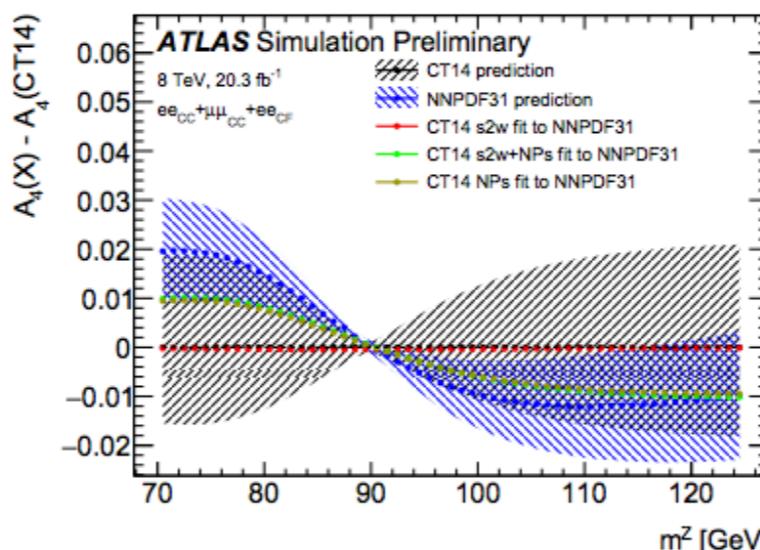
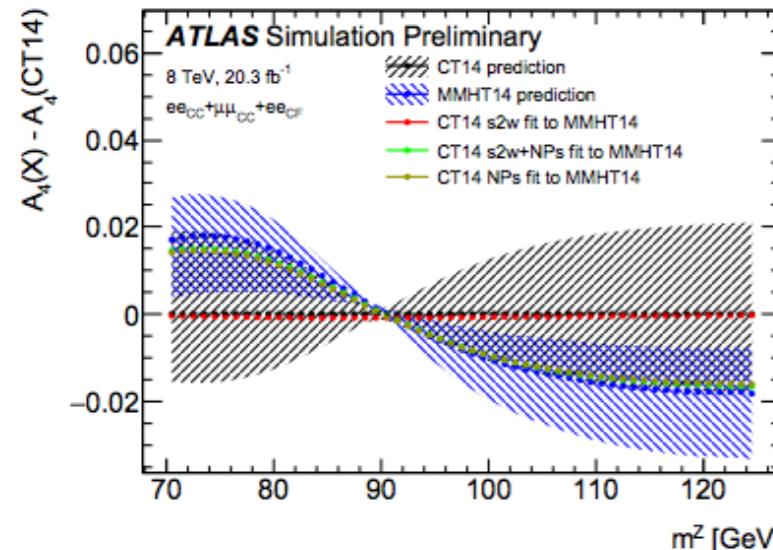
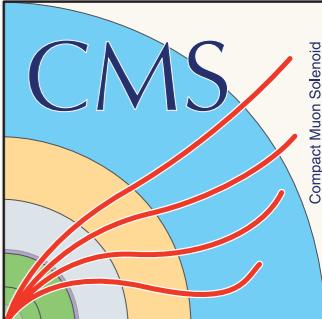
$\sin^2\theta_W$ PDF Closure



- Fit closes well in mll since variations in A_4 from $\sin^2\theta_W$ and PDF are different
- Although with uncertainties, fit not closing in yll, possibly because of course analysis yll-bins and low stat at high yll



$\sin^2\theta_W$ PDF Closure

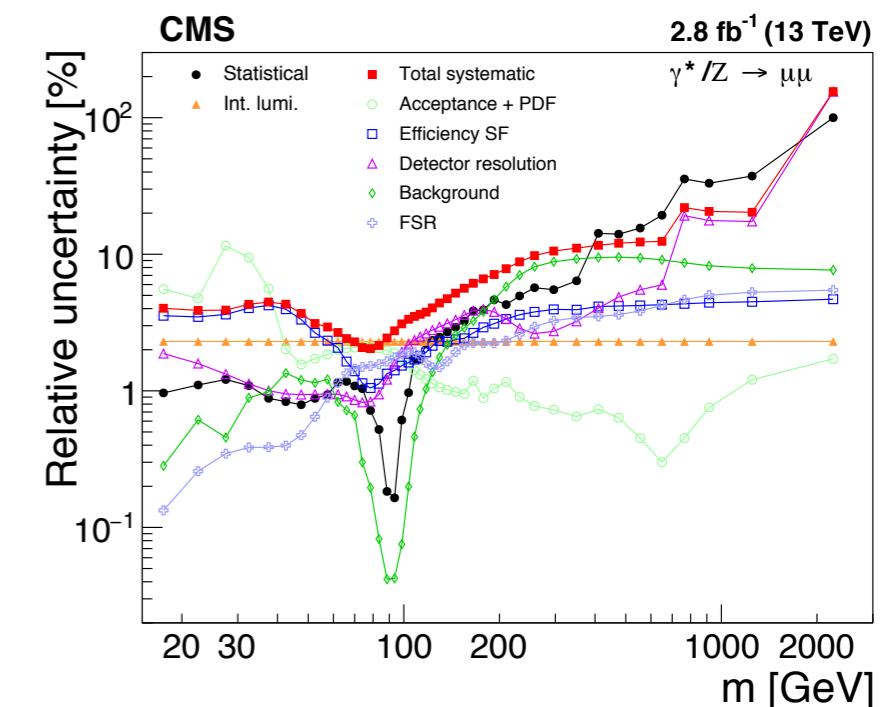
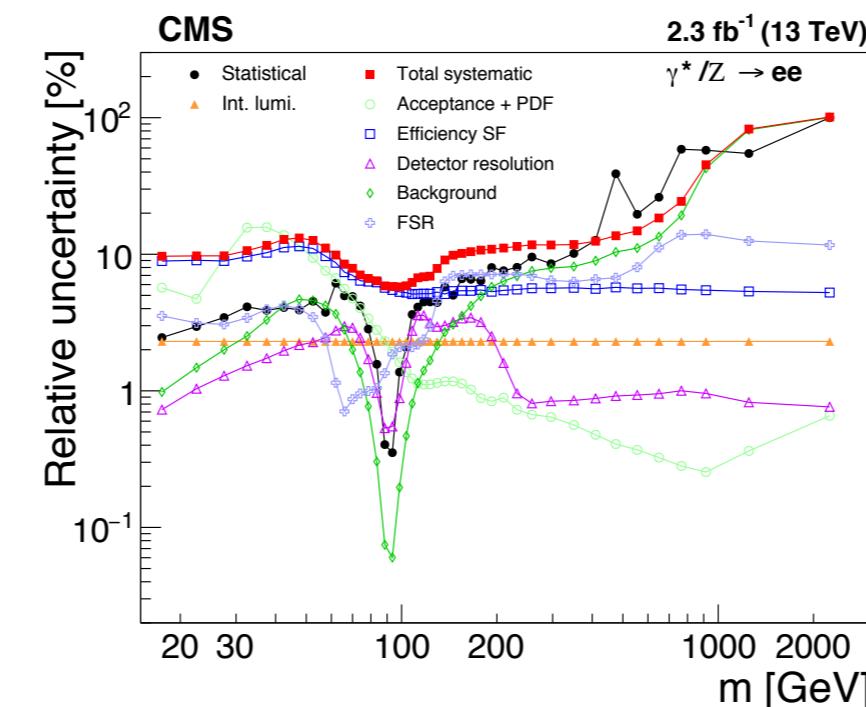
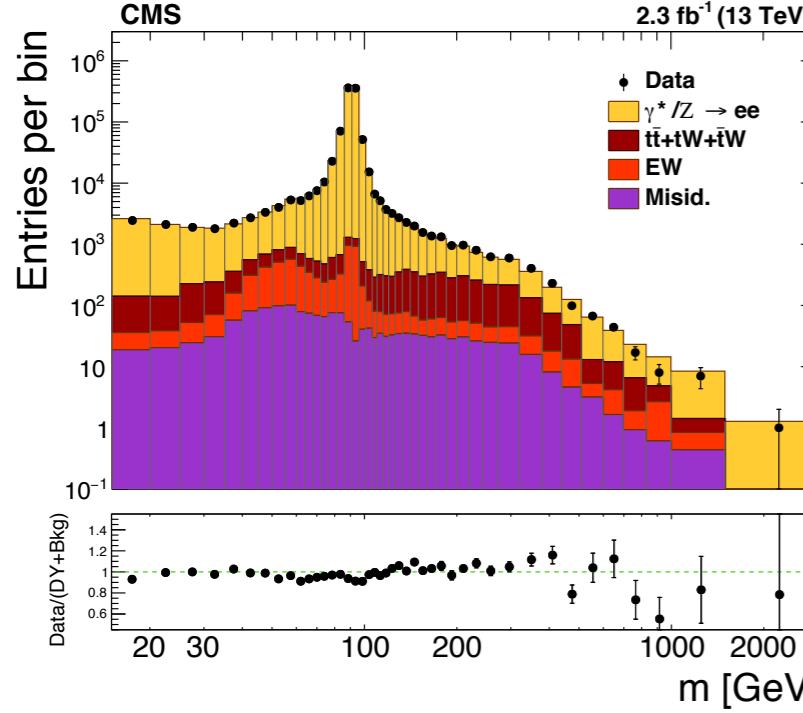
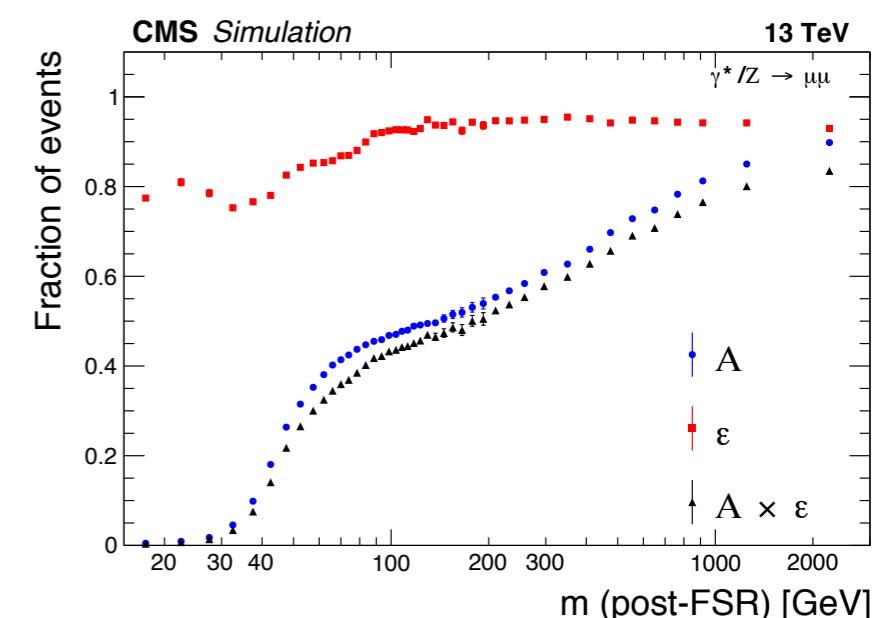
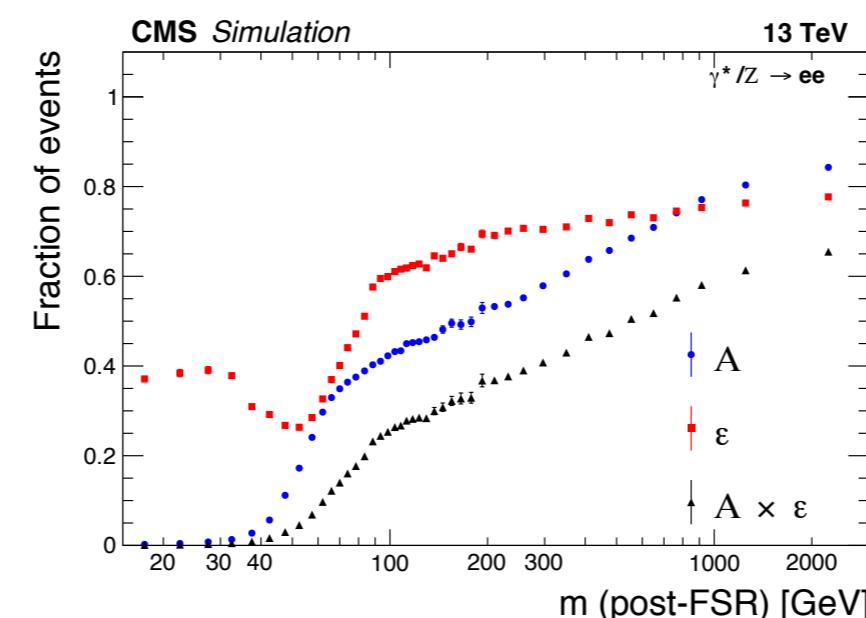
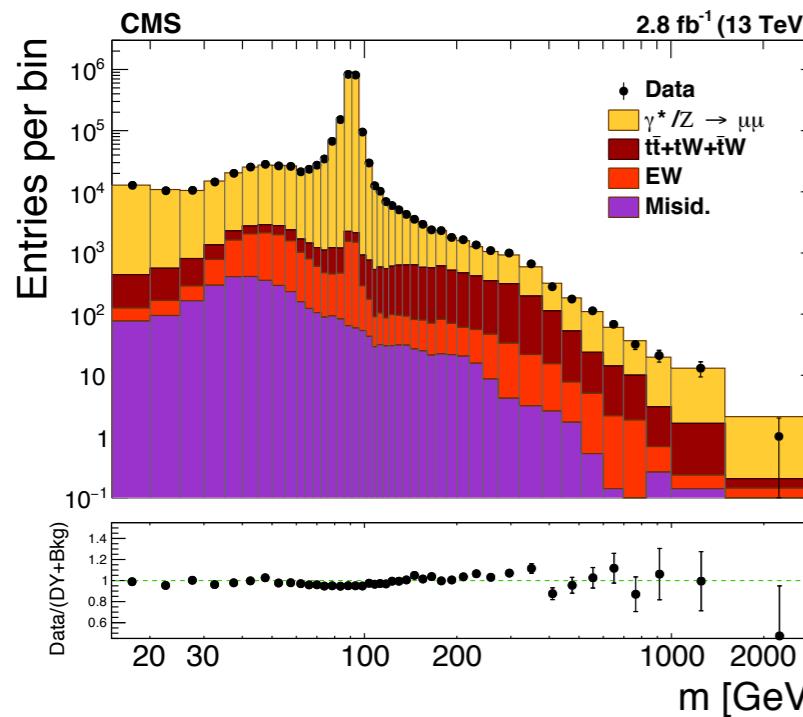
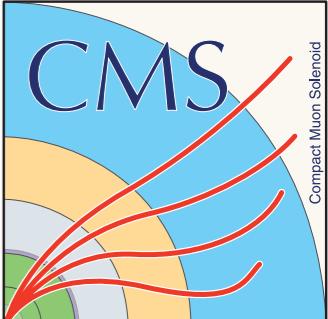


| Generated pseudodata | PDFs used for interpretation of A_4 versus $\sin^2\theta_W$ | | | | | | | | | |
|----------------------|---|------|--------|---------|--------|----------------------|------|--------|---------|--------|
| | Before PDF constraint | | | | | After PDF constraint | | | | |
| | CT10 | CT14 | MMHT14 | NNPDF31 | epWZ16 | CT10 | CT14 | MMHT14 | NNPDF31 | epWZ16 |
| CT10 | - | 20 | 2 | 11 | 109 | - | 3 | 19 | 19 | 52 |
| CT14 | -20 | - | -18 | -9 | 91 | 8 | - | 21 | 21 | 56 |
| MMHT14 | -1 | 18 | - | 9 | 108 | -25 | -11 | - | 1 | 31 |
| NNPDF31 | -10 | 9 | -9 | - | 99 | -14 | -9 | 4 | - | 43 |
| epWZ16 | -116 | -95 | -114 | -105 | - | -44 | -66 | -42 | -42 | - |

- differences mostly within 1σ PDF uncertainties (except for epWz16)
- expected statistical uncertainty of $\sim 20 \times 10^{-5}$



Z at 13TeV



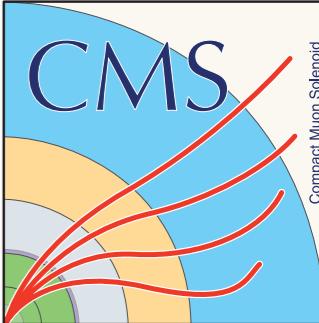
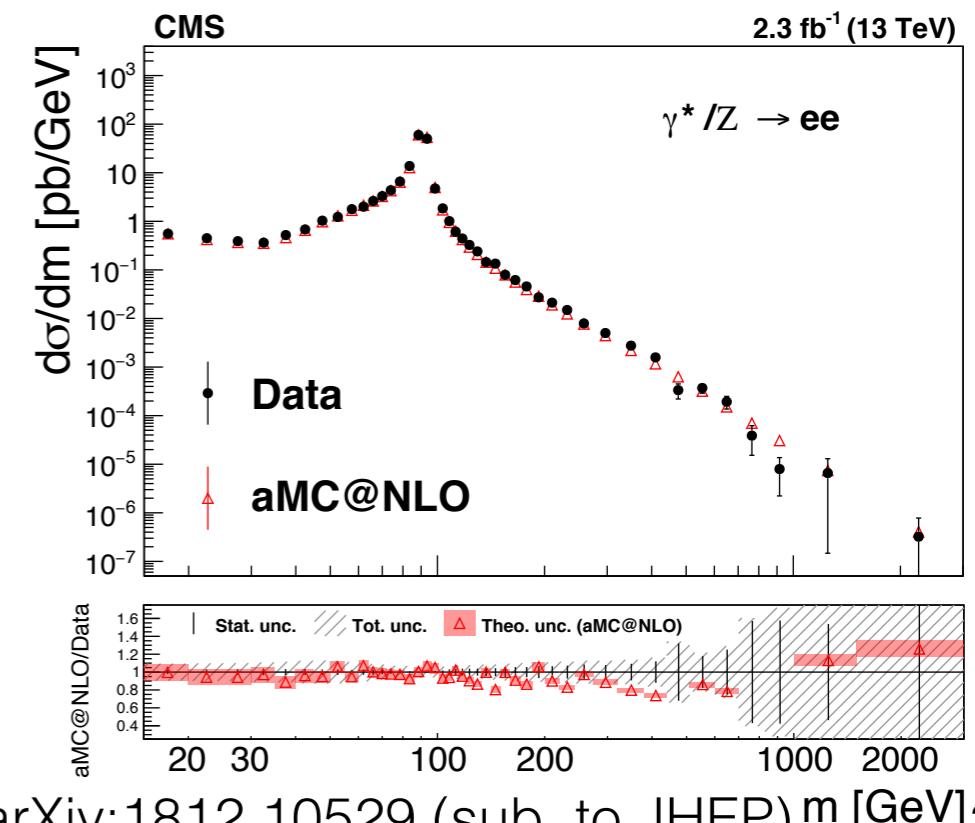
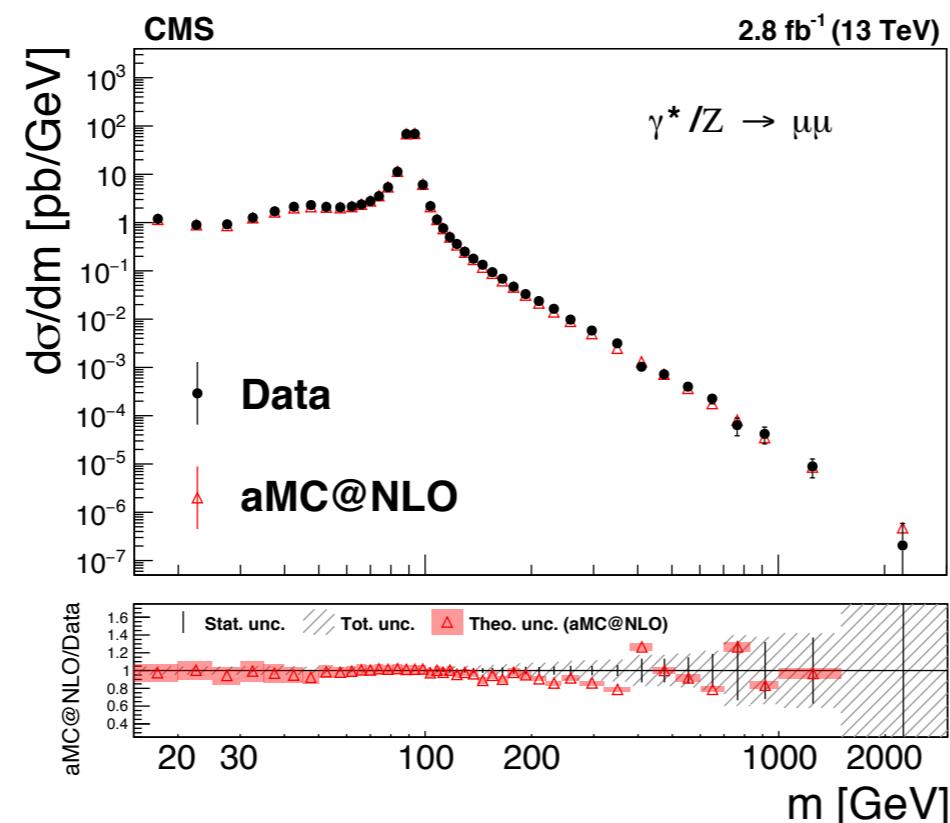
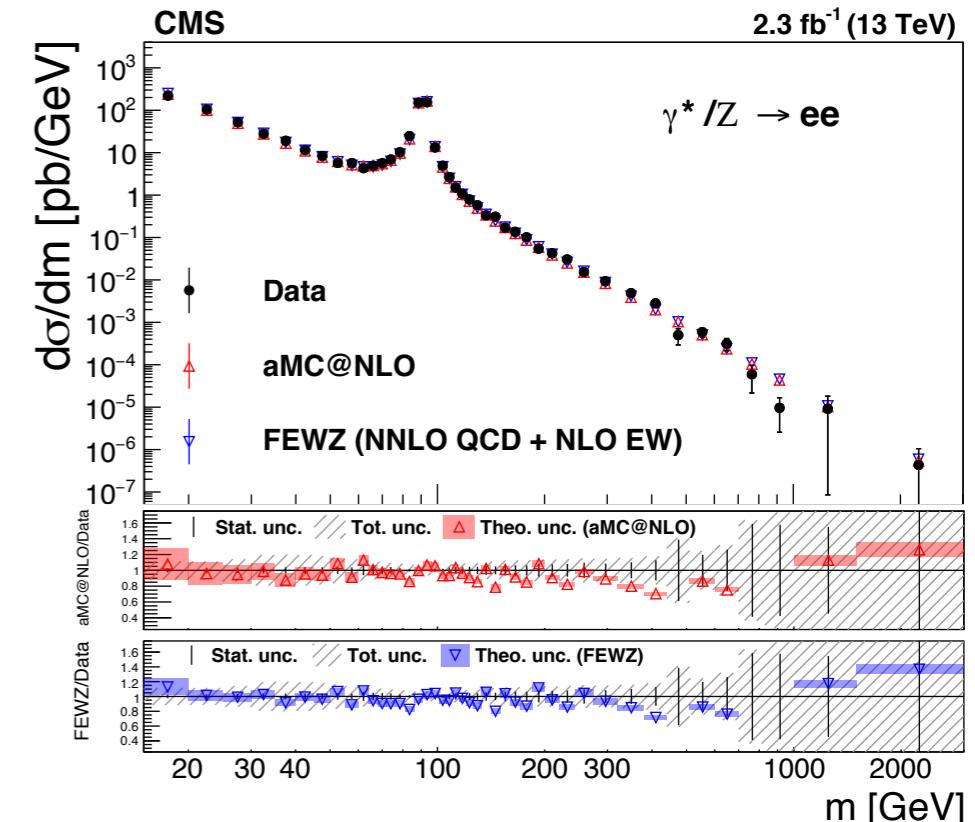
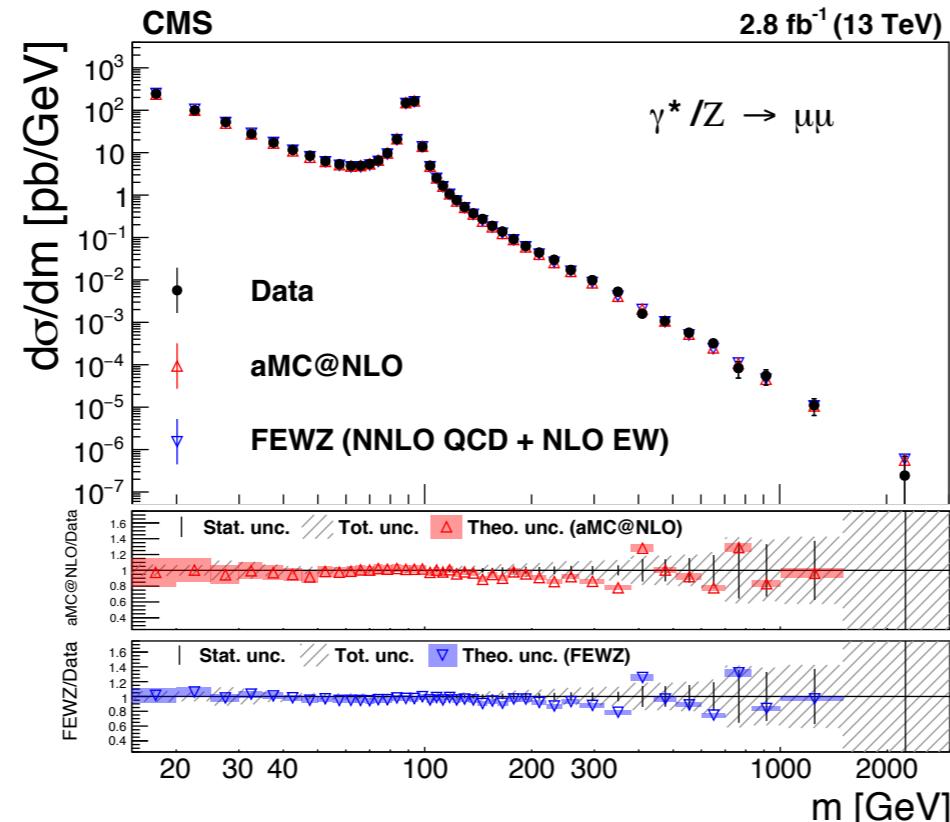


Z at 13 TeV

Full phase space with dressed leptons

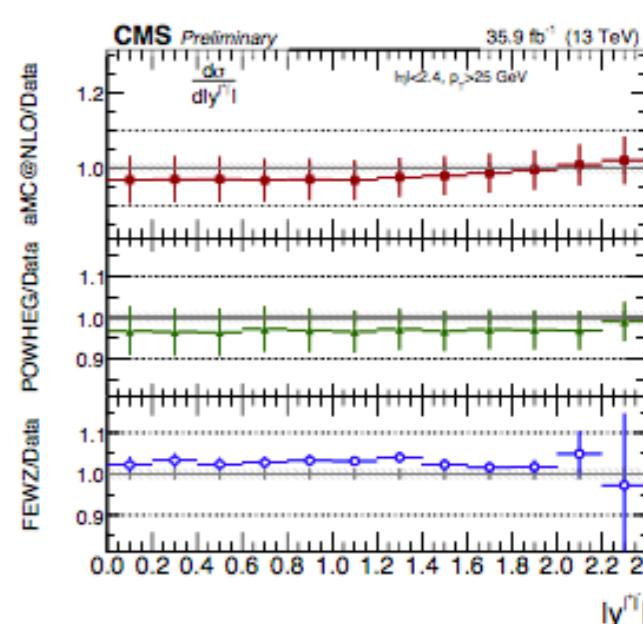
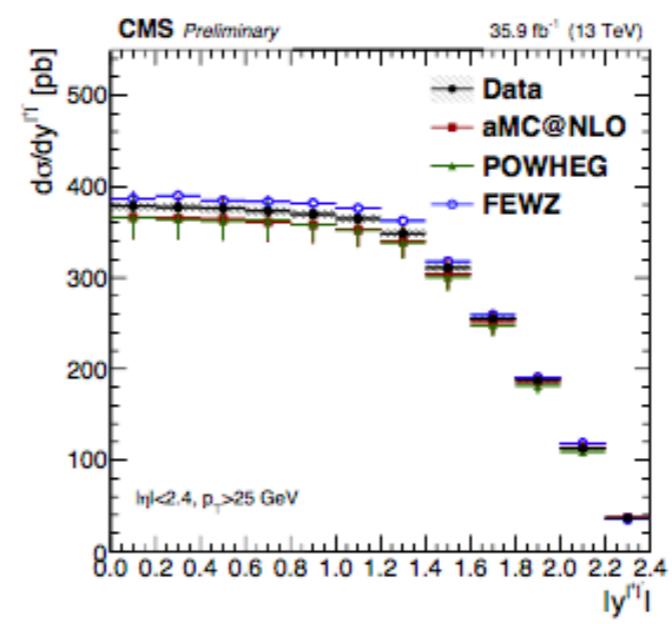
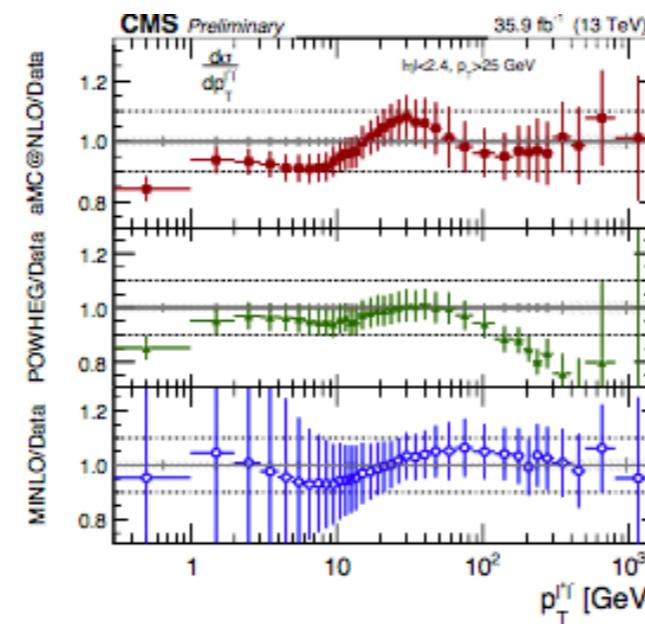
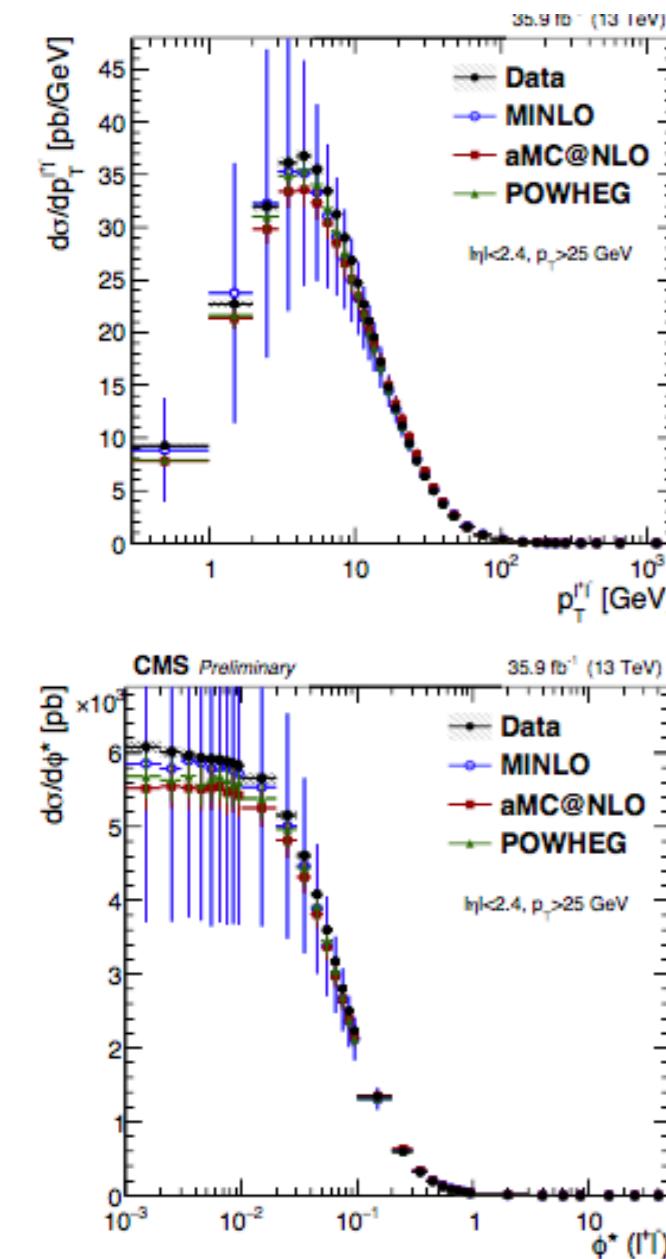
dressed: four-momenta of all simulated photons originating from the leptons are summed within a cone of $\Delta R < 0.1$ around the candidate lepton

Fiducial cross section with leptons after FSR





Z at 13 TeV



► absolute cross sections

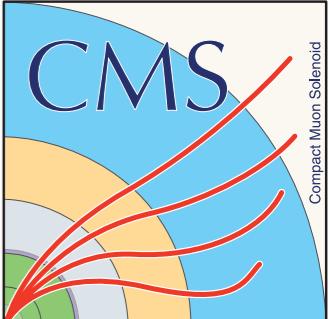
$$\phi^* = \tan\left(\frac{\pi - \Delta\phi}{2}\right) \sin(\theta_\eta^*)$$

$$\cos(\theta_\eta^*) = \tanh\left(\frac{\eta^- - \eta^+}{2}\right),$$

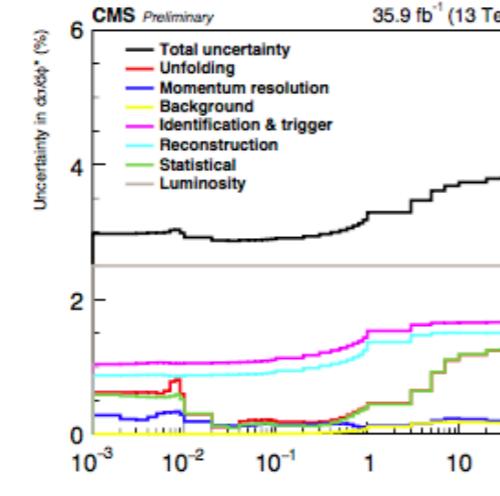
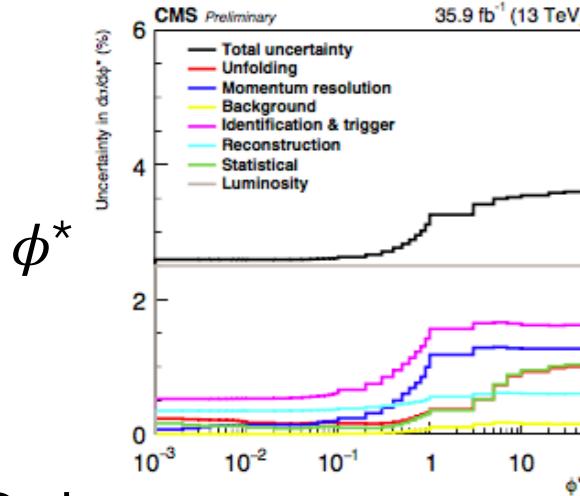
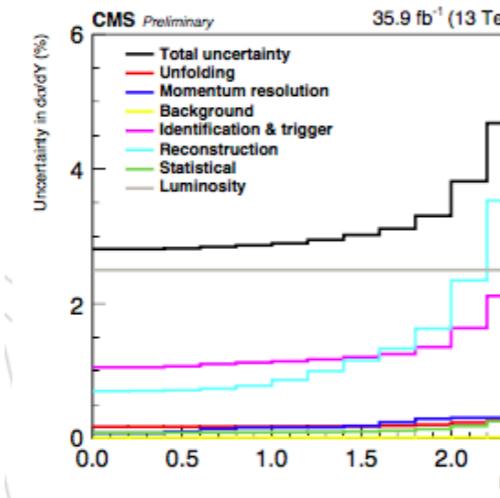
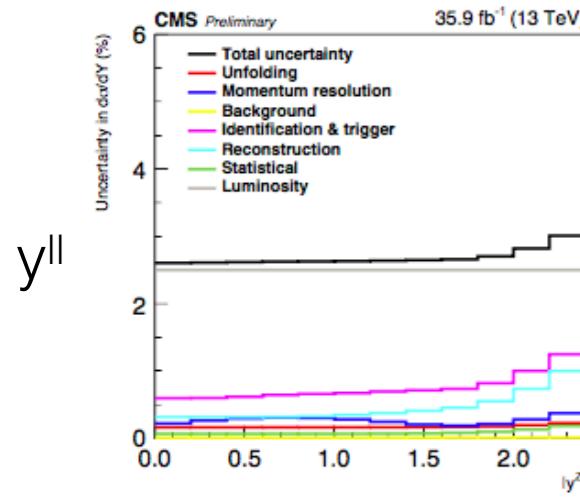
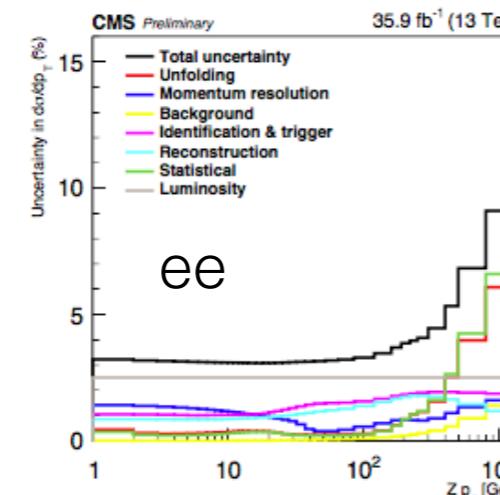
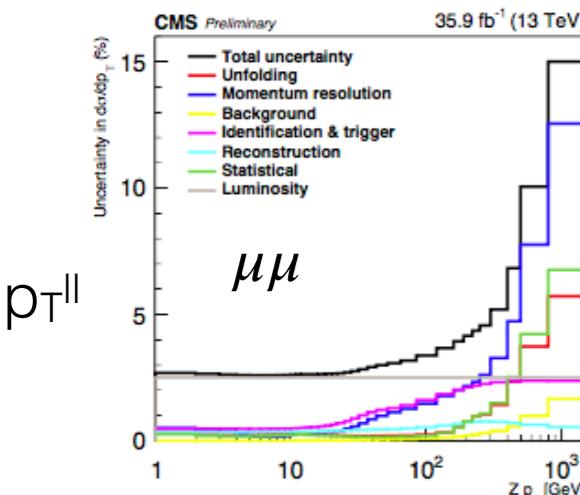
$$\phi^* \sim p_T^Z / m_{\ell\ell}$$



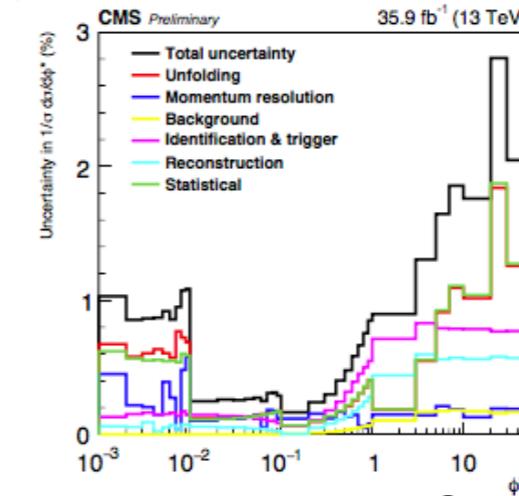
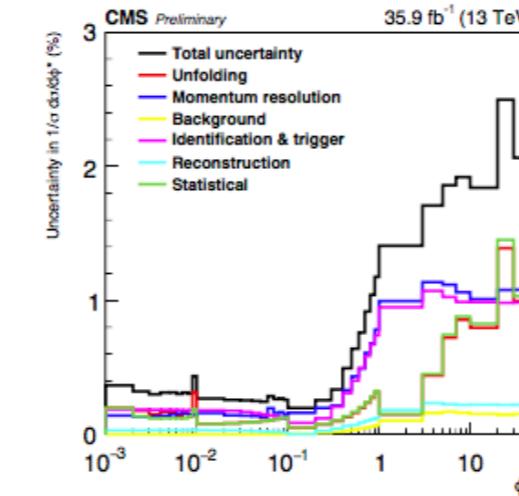
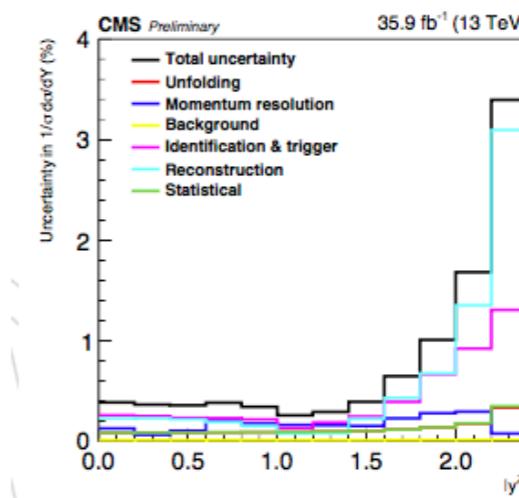
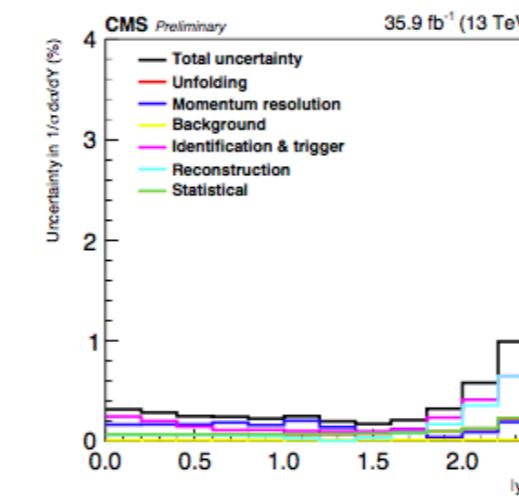
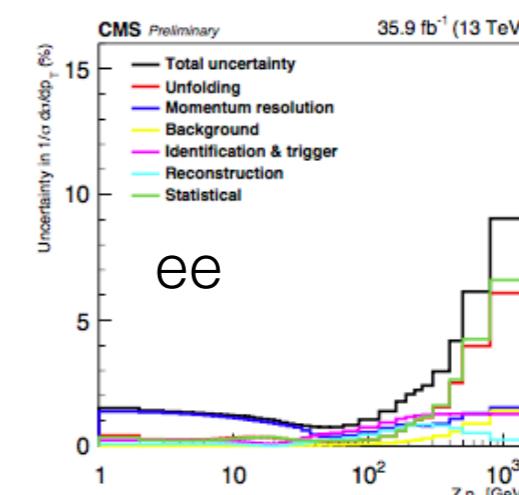
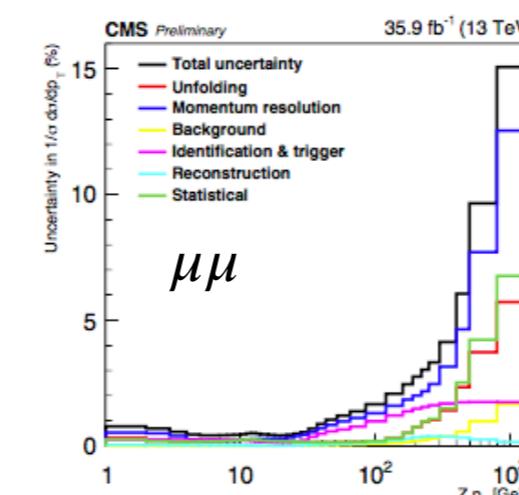
Z at 13 TeV



Absolute cross sections



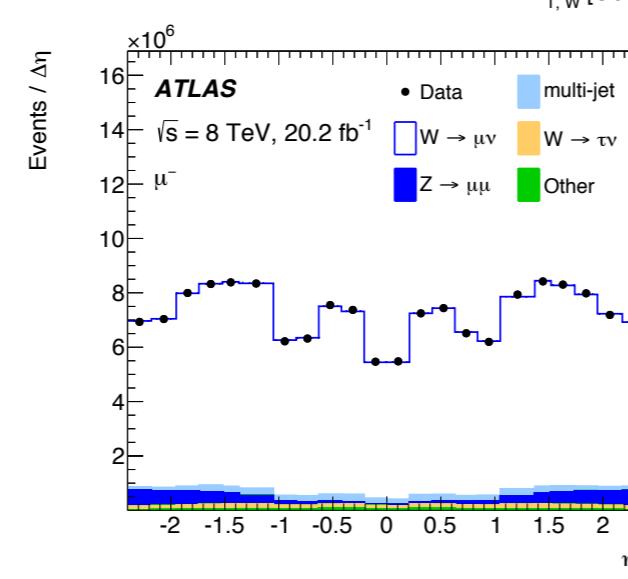
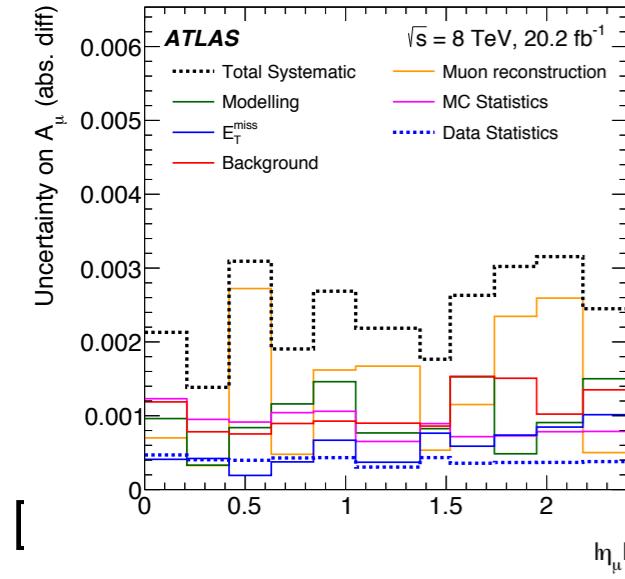
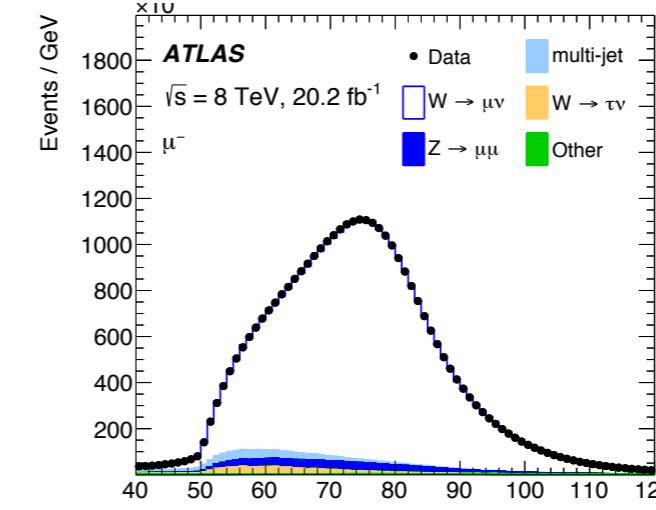
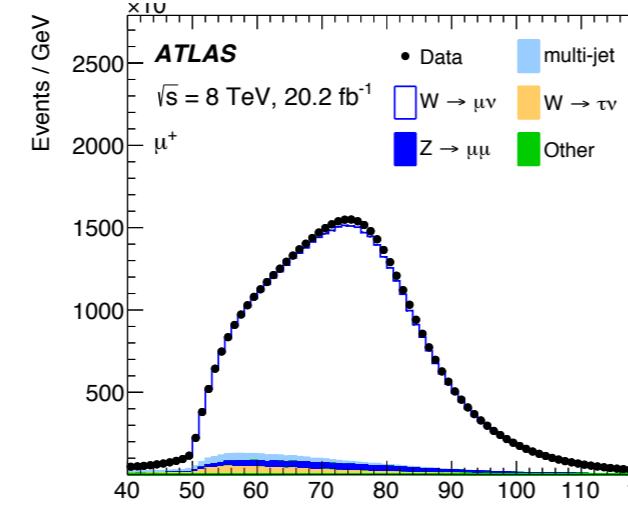
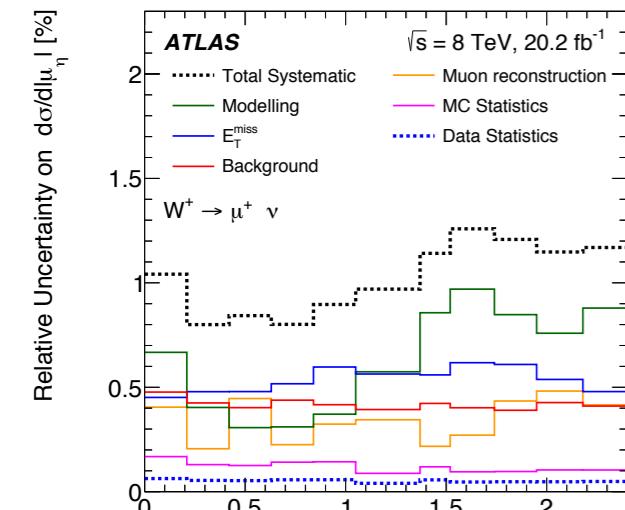
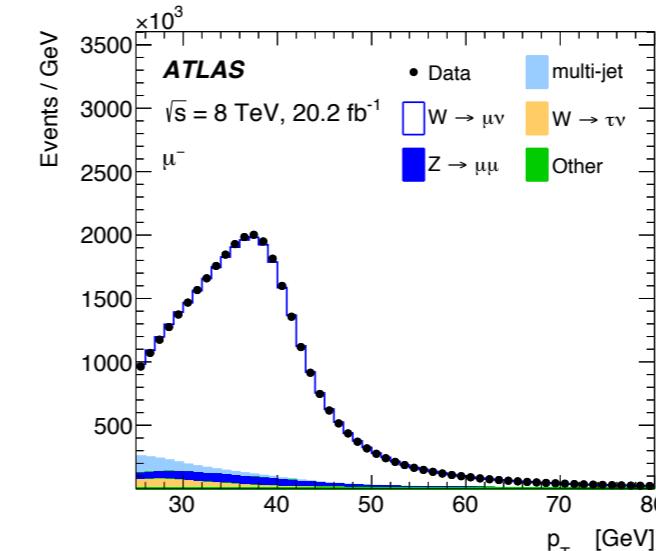
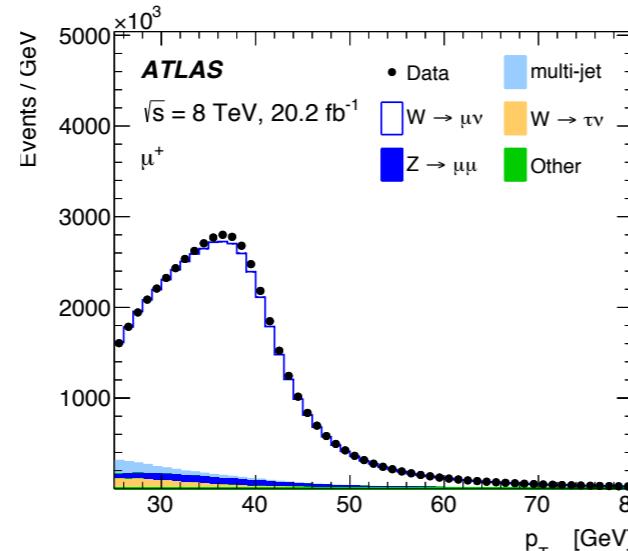
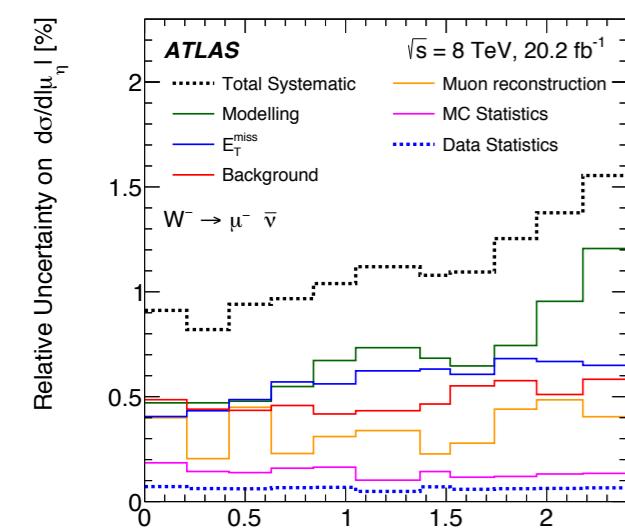
Normalised cross sections



Total uncertainty
Unfolding
Momentum resolution
Background
Identification & trigger
Reconstruction
Statistical
Luminosity



$W \rightarrow \mu\nu$ at 8 TeV



$$m_T = \sqrt{2 p_T^\mu p_T^\nu (1 - \cos(\phi^\mu - \phi^\nu))}$$

$$A_\mu = \frac{d\sigma_{W_\mu^+}/d\eta_\mu - d\sigma_{W_\mu^-}/d\eta_\mu}{d\sigma_{W_\mu^+}/d\eta_\mu + d\sigma_{W_\mu^-}/d\eta_\mu}$$



$W^+ \rightarrow \mu^+\nu$ $W^- \rightarrow \mu^-\bar{\nu}$

Number of events

| Data | 50 390 184 | 34 877 365 |
|------|------------|------------|
|------|------------|------------|

Percentage of data

| | | |
|-------------------------|-----------------|-----------------|
| Multijet | 2.4 ± 0.3 | 3.1 ± 0.3 |
| $W \rightarrow \tau\nu$ | 1.9 ± 0.1 | 2.0 ± 0.1 |
| $Z \rightarrow \mu\mu$ | 3.1 ± 0.2 | 4.0 ± 0.2 |
| Others | 0.62 ± 0.02 | 0.82 ± 0.03 |

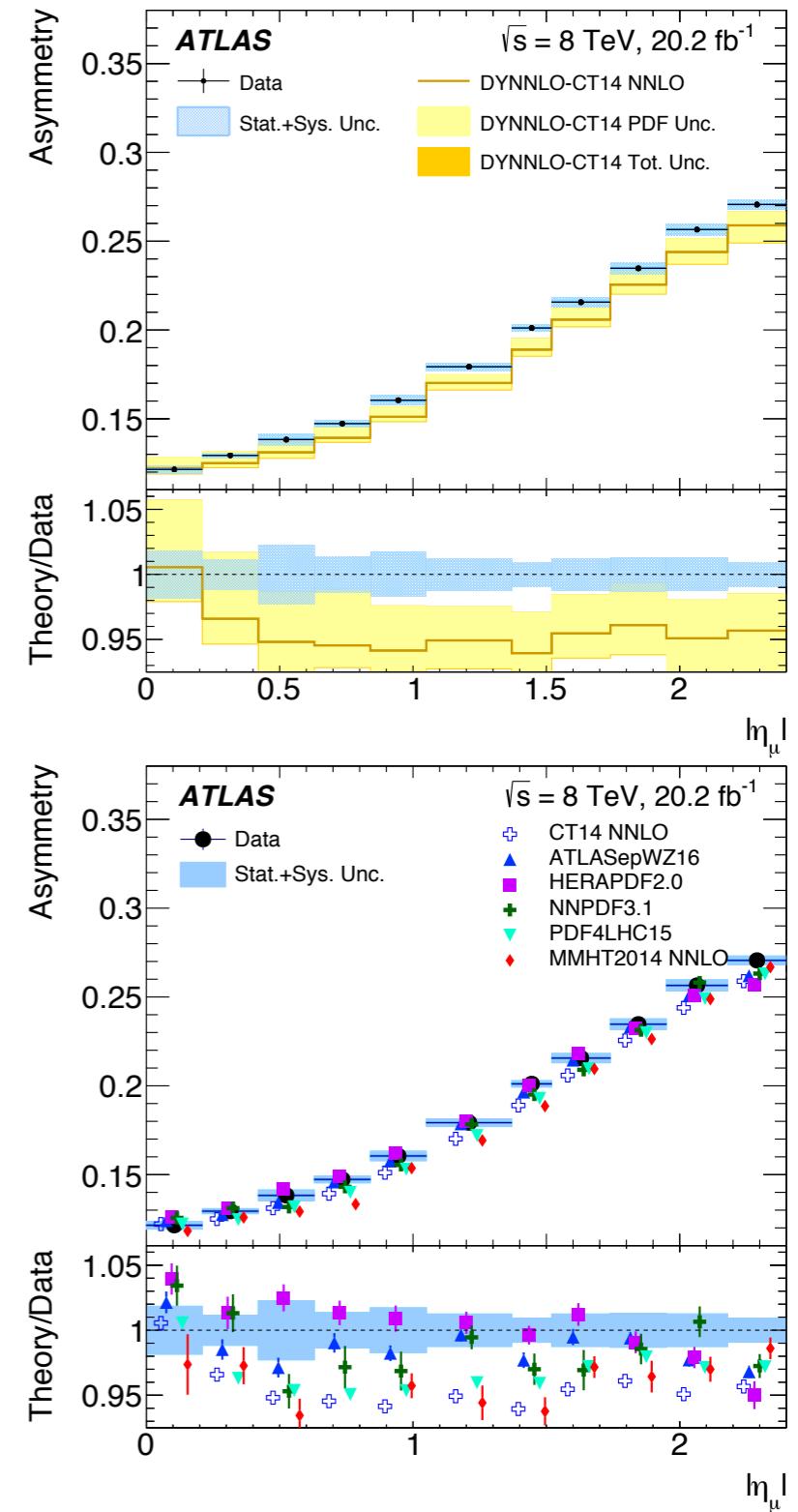
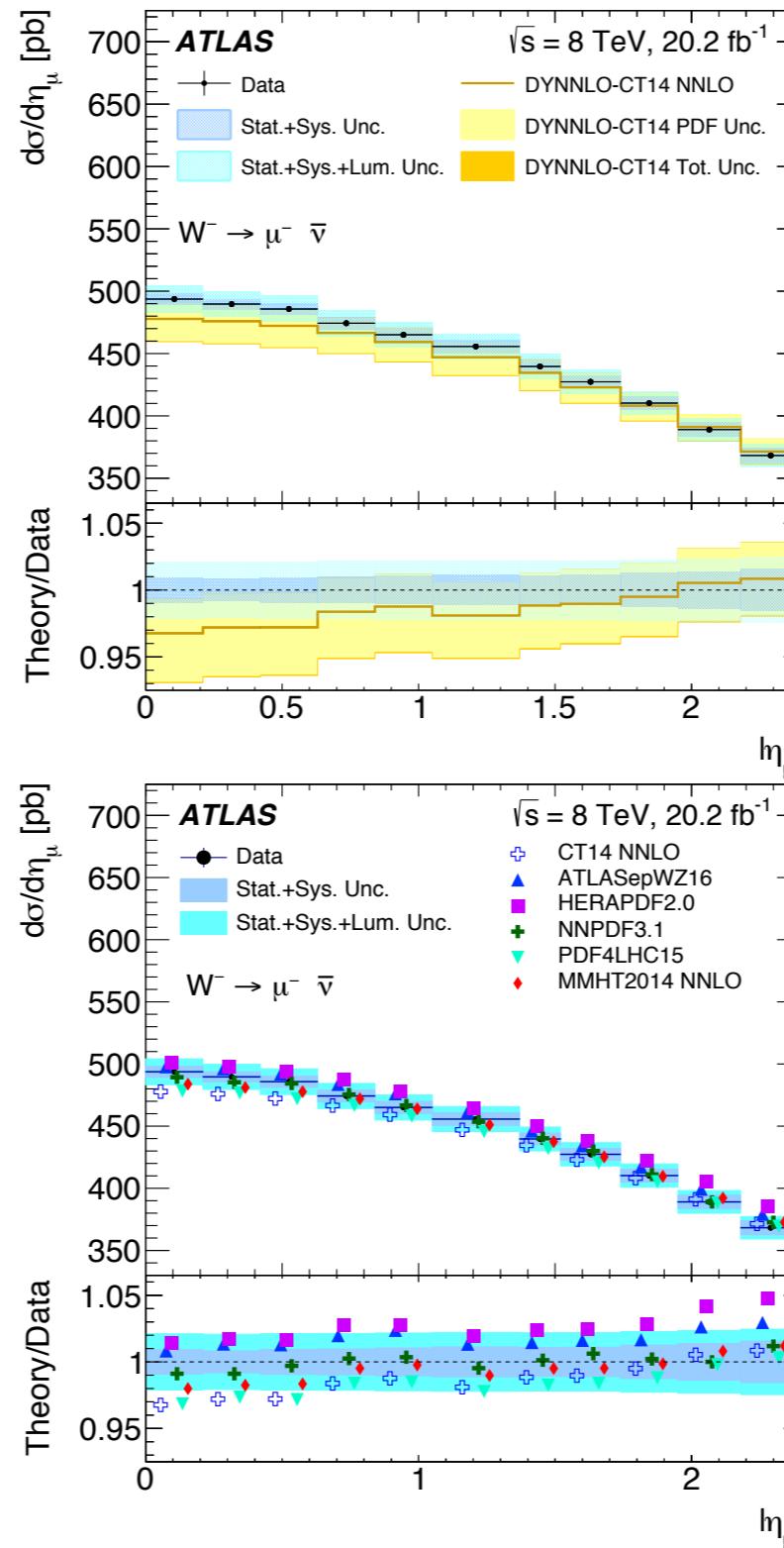
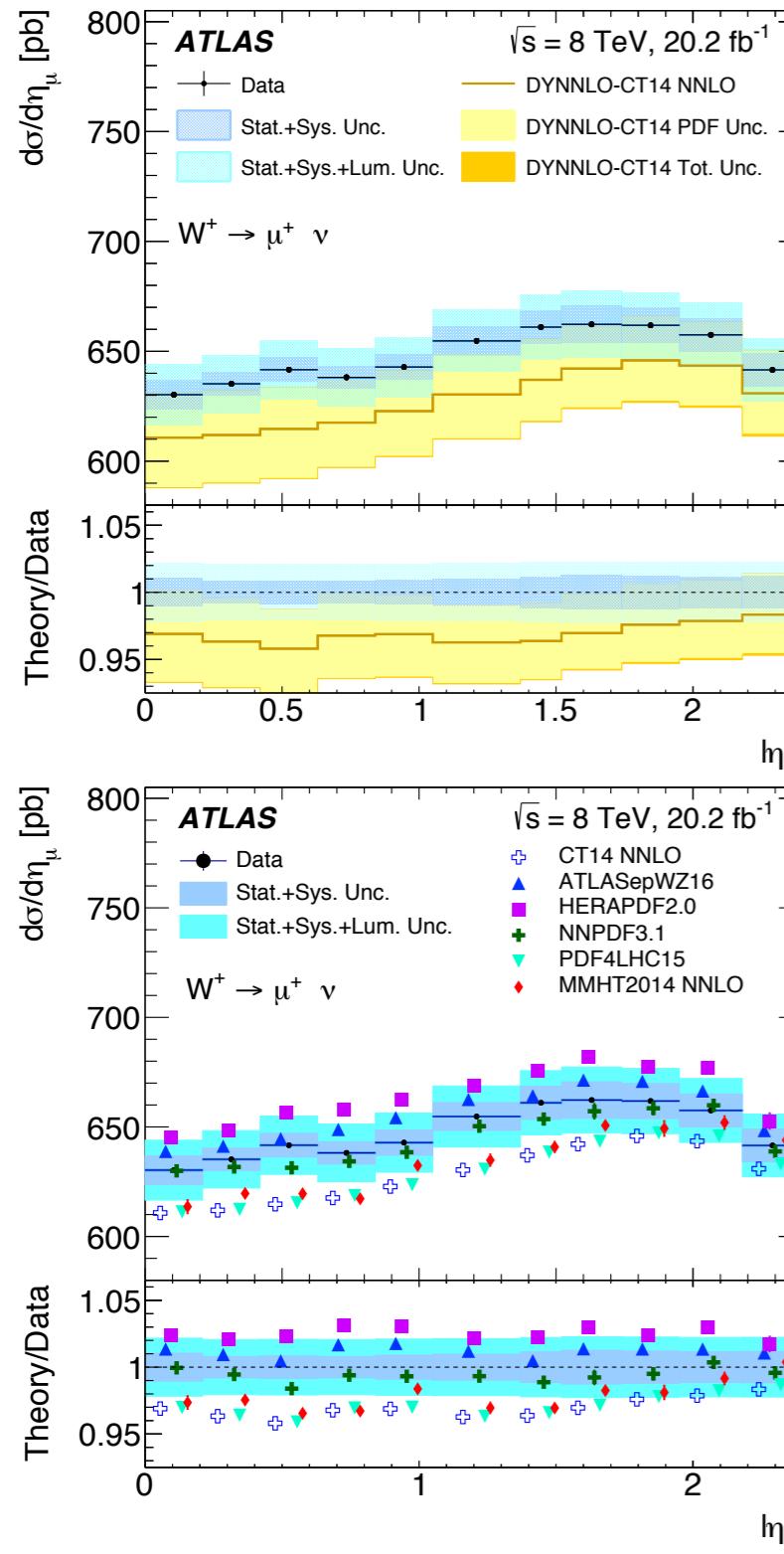
| $ \eta_\mu $ | $W^+ \rightarrow \mu^+\nu$ | $W^- \rightarrow \mu^-\bar{\nu}$ |
|--------------|----------------------------|----------------------------------|
| 0.00–0.21 | 0.508 ± 0.004 | 0.505 ± 0.004 |
| 0.21–0.42 | 0.684 ± 0.004 | 0.679 ± 0.004 |
| 0.42–0.63 | 0.702 ± 0.005 | 0.702 ± 0.005 |
| 0.63–0.84 | 0.611 ± 0.004 | 0.613 ± 0.005 |
| 0.84–1.05 | 0.603 ± 0.004 | 0.601 ± 0.005 |
| 1.05–1.37 | 0.795 ± 0.006 | 0.796 ± 0.007 |
| 1.37–1.52 | 0.848 ± 0.008 | 0.845 ± 0.007 |
| 1.52–1.74 | 0.861 ± 0.009 | 0.856 ± 0.007 |
| 1.74–1.95 | 0.856 ± 0.009 | 0.855 ± 0.008 |
| 1.95–2.18 | 0.792 ± 0.008 | 0.794 ± 0.009 |
| 2.18–2.40 | 0.802 ± 0.008 | 0.812 ± 0.011 |
| Integrated | 0.736 ± 0.003 | 0.727 ± 0.003 |

| Data | |
|---|---|
| $\sigma(W^+ \rightarrow \mu^+\nu)$ [pb] | 3110 ± 0.5 (stat.) ± 29 (syst.) ± 59 (lumi.) |
| $\sigma(W^- \rightarrow \mu^-\bar{\nu})$ [pb] | 2137 ± 0.4 (stat.) ± 22 (syst.) ± 41 (lumi.) |
| Sum [pb] | 5247 ± 0.6 (stat.) ± 50 (syst.) ± 100 (lumi.) |
| Ratio | 1.4558 ± 0.0004 (stat.) ± 0.0040 (syst.) |

| DYNNLO (CT14 NNLO PDF set) | |
|---|--|
| $\sigma(W^+ \rightarrow \mu^+\nu)$ [pb] | 3015 ± 92 (PDF) ± 15 (scale) |
| $\sigma(W^- \rightarrow \mu^-\bar{\nu})$ [pb] | 2105 ± 53 (PDF) ± 10 (scale) |
| Sum [pb] | 5120 ± 140 (PDF) ± 23 (scale) |
| Ratio | 1.4320 ± 0.0100 (PDF) ± 0.0007 (scale) |

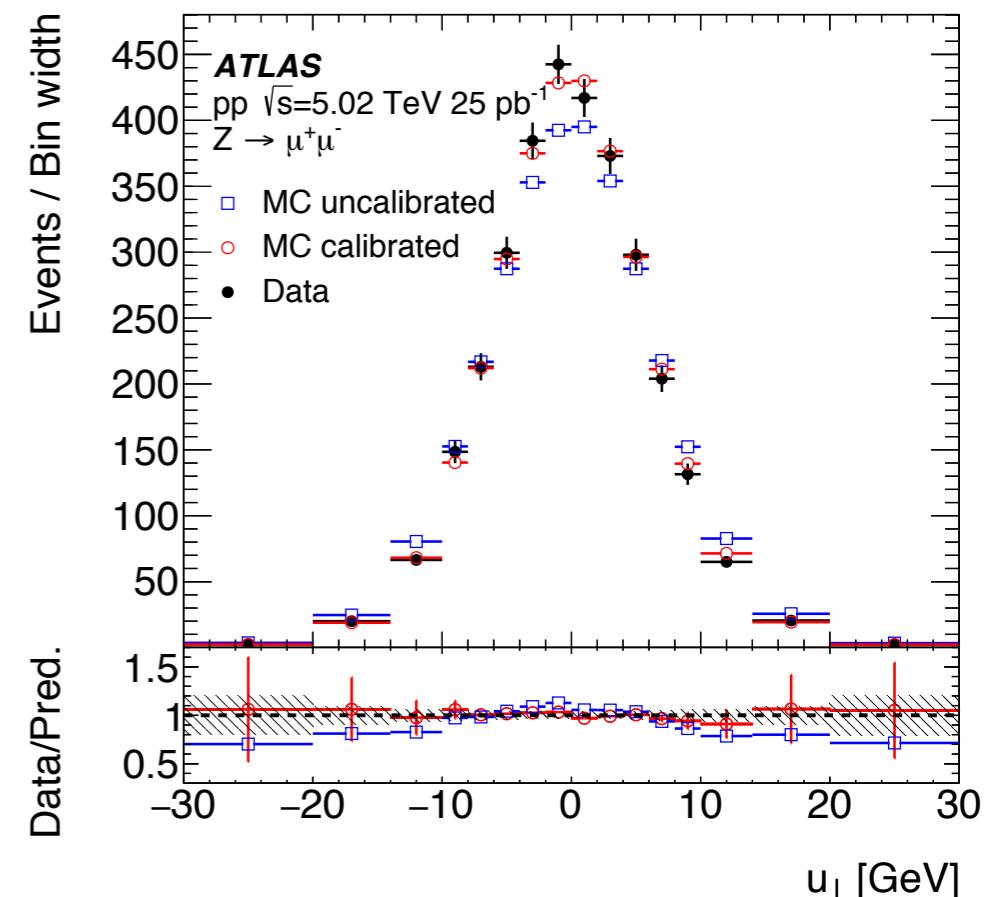
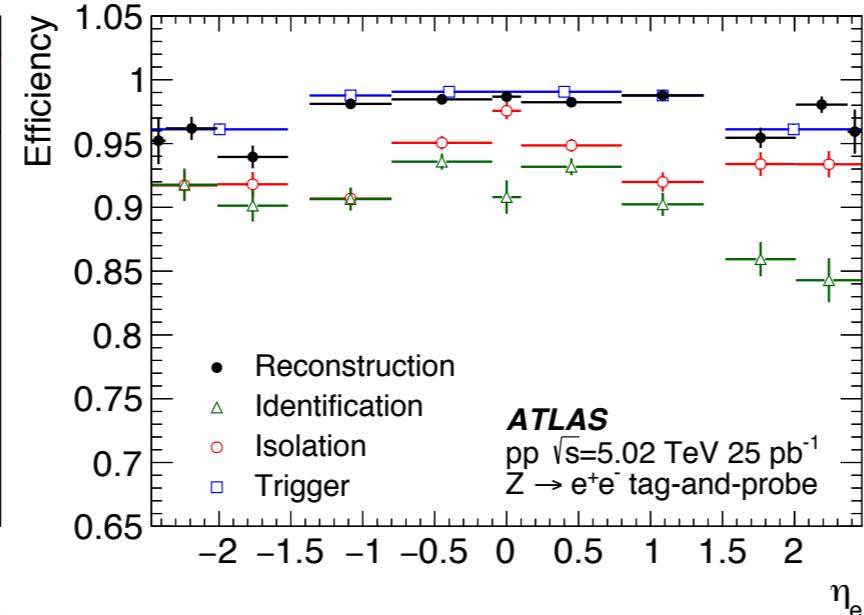
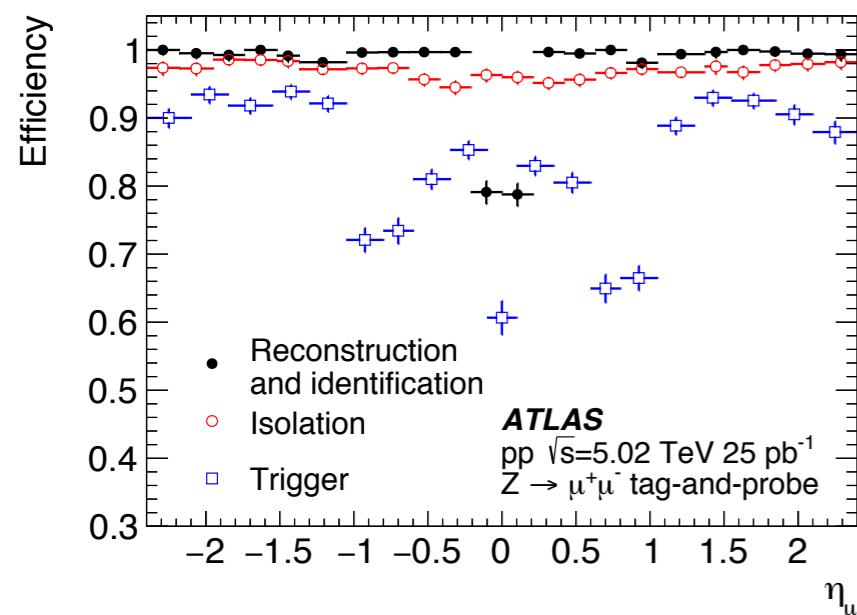


$W \rightarrow \mu\nu$ at 8 TeV

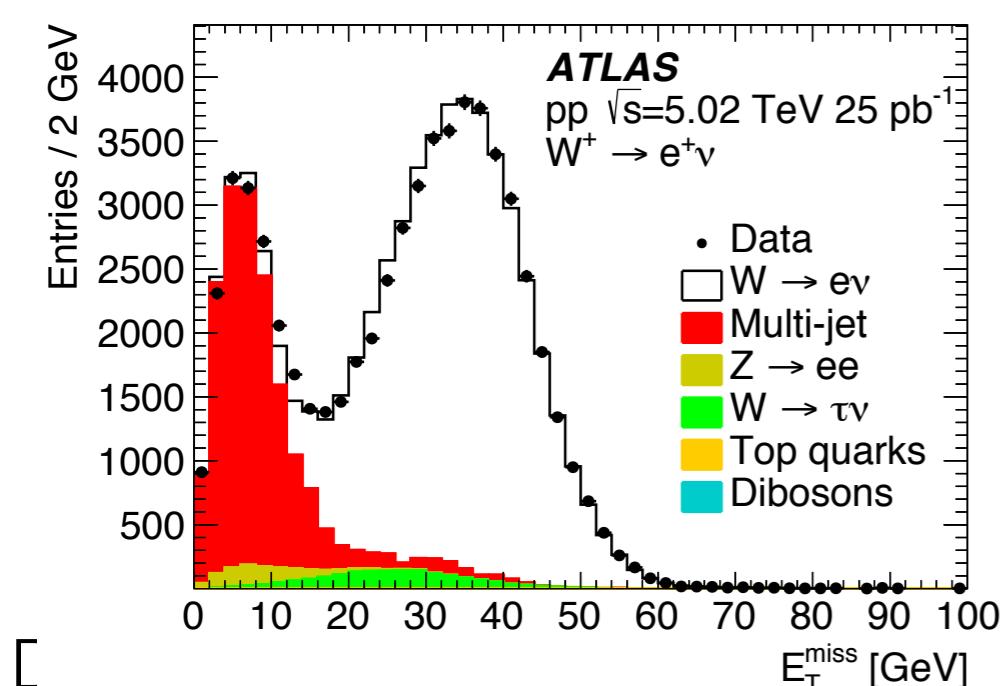




W,Z at 5.02TeV



- Precision in lepton efficiency limited by number of $Z \rightarrow l\bar{l}$ candidates
- Hadronic recoil with particle flow objects
- Calibration of hadronic recoil based on $Z \rightarrow l\bar{l}$ candidates

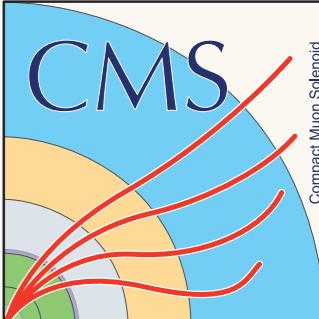


| Background | $W^+ \rightarrow e^+\nu$ ($W^+ \rightarrow \mu^+\nu$) [%] | $W^- \rightarrow e^-\nu$ ($W^- \rightarrow \mu^-\nu$) [%] | $Z \rightarrow e^+e^-$ ($Z \rightarrow \mu^+\mu^-$) [%] |
|--|---|---|---|
| $Z \rightarrow \ell^+\ell^-$, $\ell = e, \mu$ | 0.1 (2.8) | 0.2 (3.8) | — |
| $W^\pm \rightarrow \ell^\pm \nu$, $\ell = e, \mu$ | — | — | <0.01 (<0.01) |
| $W^\pm \rightarrow \tau^\pm \nu$ | 1.8 (1.8) | 1.8 (1.8) | <0.01 (<0.01) |
| $Z \rightarrow \tau^+\tau^-$ | 0.1 (0.1) | 0.1 (0.1) | 0.07 (0.07) |
| Multi-jet | 0.9 (0.1) | 1.4 (0.2) | <0.01 (<0.01) |
| Top quark | 0.1–0.2 (0.1–0.2) | 0.1–0.2 (0.1–0.2) | 0.06 (0.08) |
| Diboson | 0.1 (0.1) | 0.1 (0.1) | 0.14 (0.08) |



W,Z at 5.02TeV

$$\sigma_{W^\pm \rightarrow \ell^\pm \nu [Z \rightarrow \ell^+ \ell^-]}^{\text{fid}} = \frac{N_{W[Z]} - B_{W[Z]}}{C_{W[Z]} \cdot L_{\text{int}}}$$



| | | $W^- \rightarrow \ell^- \nu$ | | | | $W^+ \rightarrow \ell^+ \nu$ | | | | | |
|----------------------------|----------------------------|------------------------------------|--|--|--|------------------------------|----------------------------|------------------------------------|--|--|--|
| $ \eta_\ell ^{\text{min}}$ | $ \eta_\ell ^{\text{max}}$ | $d\sigma/d \eta_\ell [\text{pb}]$ | $\delta\sigma_{\text{stat}} [\text{pb}]$ | $\delta\sigma_{\text{syst}} [\text{pb}]$ | $\delta\sigma_{\text{lumi}} [\text{pb}]$ | $ \eta_\ell ^{\text{min}}$ | $ \eta_\ell ^{\text{max}}$ | $d\sigma/d \eta_\ell [\text{pb}]$ | $\delta\sigma_{\text{stat}} [\text{pb}]$ | $\delta\sigma_{\text{syst}} [\text{pb}]$ | $\delta\sigma_{\text{lumi}} [\text{pb}]$ |
| 0.00 | 0.21 | 329 | 5 | 8 | 6 | 0.00 | 0.21 | 456 | 6 | 11 | 9 |
| 0.21 | 0.42 | 315 | 5 | 6 | 6 | 0.21 | 0.42 | 467 | 6 | 9 | 9 |
| 0.42 | 0.63 | 315 | 5 | 6 | 6 | 0.42 | 0.63 | 471 | 6 | 9 | 9 |
| 0.63 | 0.84 | 298 | 5 | 6 | 6 | 0.63 | 0.84 | 460 | 6 | 10 | 9 |
| 0.84 | 1.05 | 303 | 5 | 7 | 6 | 0.84 | 1.05 | 471 | 6 | 11 | 9 |
| 1.05 | 1.37 | 286 | 4 | 5 | 6 | 1.05 | 1.37 | 474 | 5 | 9 | 9 |
| 1.37 | 1.52 | 276 | 7 | 7 | 5 | 1.37 | 1.52 | 482 | 9 | 15 | 9 |
| 1.52 | 1.74 | 272 | 4 | 6 | 5 | 1.52 | 1.74 | 474 | 6 | 11 | 9 |
| 1.74 | 1.95 | 249 | 4 | 5 | 5 | 1.74 | 1.95 | 465 | 6 | 11 | 9 |
| 1.95 | 2.18 | 253 | 4 | 6 | 5 | 1.95 | 2.18 | 446 | 6 | 10 | 9 |
| 2.18 | 2.50 | 219 | 4 | 6 | 4 | 2.18 | 2.50 | 371 | 5 | 10 | 7 |
| 0.00 | 2.50 | 1401 | 7 | 18 | 27 | 0.00 | 2.50 | 2266 | 9 | 29 | 43 |

| | | $Z \rightarrow \ell^+ \ell^-$ | | | |
|-------------------------------|-------------------------------|---------------------------------------|--|--|--|
| $ y_{\ell\ell} ^{\text{min}}$ | $ y_{\ell\ell} ^{\text{max}}$ | $d\sigma/d y_{\ell\ell} [\text{pb}]$ | $\delta\sigma_{\text{stat}} [\text{pb}]$ | $\delta\sigma_{\text{syst}} [\text{pb}]$ | $\delta\sigma_{\text{lumi}} [\text{pb}]$ |
| 0.0 | 0.5 | 103.0 | 1.7 | 1.2 | 1.9 |
| 0.5 | 1.0 | 101.3 | 1.8 | 1.1 | 1.9 |
| 1.0 | 1.5 | 89.6 | 1.7 | 0.9 | 1.7 |
| 1.5 | 2.0 | 60.5 | 1.4 | 0.7 | 1.1 |
| 2.0 | 2.5 | 20.0 | 0.9 | 0.4 | 0.4 |
| 0.0 | 2.5 | 374.5 | 3.4 | 3.6 | 7.0 |

| | |
|----------------------------|---|
| R_{W^+/W^-}^{fid} | $1.617 \pm 0.012 \text{ (stat)} \pm 0.003 \text{ (syst)}$ |
| $R_{W/Z}^{\text{fid}}$ | $9.81 \pm 0.13 \text{ (stat)} \pm 0.01 \text{ (syst)}$ |
| $R_{W^+/Z}^{\text{fid}}$ | $6.06 \pm 0.08 \text{ (stat)} \pm 0.01 \text{ (syst)}$ |
| $R_{W^-/Z}^{\text{fid}}$ | $3.75 \pm 0.05 \text{ (stat)} \pm 0.01 \text{ (syst)}$ |

| $ \eta_\ell ^{\text{min}}$ | $ \eta_\ell ^{\text{max}}$ | A_ℓ | δA_{stat} | δA_{syst} |
|----------------------------|----------------------------|----------|--------------------------|--------------------------|
| 0.00 | 0.21 | 0.163 | 0.010 | 0.001 |
| 0.21 | 0.42 | 0.195 | 0.009 | 0.001 |
| 0.42 | 0.63 | 0.201 | 0.009 | 0.001 |
| 0.63 | 0.84 | 0.213 | 0.010 | 0.001 |
| 0.84 | 1.05 | 0.218 | 0.010 | 0.001 |
| 1.05 | 1.37 | 0.248 | 0.008 | 0.001 |
| 1.37 | 1.52 | 0.272 | 0.014 | 0.002 |
| 1.52 | 1.74 | 0.271 | 0.009 | 0.001 |
| 1.74 | 1.95 | 0.300 | 0.010 | 0.001 |
| 1.95 | 2.18 | 0.276 | 0.010 | 0.001 |
| 2.18 | 2.50 | 0.256 | 0.010 | 0.001 |



Z3D

