Introduction to Recombination Physics and Why it is Important for Cosmology and Early-Universe Physics



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The University of Manchester



Cosmic Microwave Background Anisotropies



Planck all sky map

CMB has a blackbody spectrum in every direction
tiny variations of the CMB temperature Δ*T*/*T* ~ 10⁻⁵

CMB anisotropies (with SN, LSS, etc...) clearly taught us a lot about the Universe we live in!

- Standard 6 parameter concordance cosmology with parameters known to percent level precision
- Gaussian-distributed adiabatic fluctuations with nearly scaleinvariant power spectrum over a wide range of scales
- cold dark matter ("CDM")
- accelerated expansion today ("Λ")
- Standard BBN scenario $\rightarrow N_{\text{eff}}$ and Y_{p}
- Standard ionization history $\rightarrow N_{\rm e}(z)$



Parameter	TT+lowP 68 % limits	TT+lowP+lensing 68 % limits	TT+lowP+lensing+ext 68 % limits	TT,TE,EE+lowP 68 % limits	TT,TE,EE+lowP+lensing 68 % limits	TT,TE,EE+lowP+lensing+ext 68 % limits
$\Omega_{ m b}h^2$	0.02222 ± 0.00023	0.02226 ± 0.00023	0.02227 ± 0.00020	0.02225 ± 0.00016	0.02226 ± 0.00016	0.02230 ± 0.00014
$\Omega_{\rm c} h^2$	0.1197 ± 0.0022	0.1186 ± 0.0020	0.1184 ± 0.0012	0.1198 ± 0.0015	0.1193 ± 0.0014	0.1188 ± 0.0010
$100\theta_{\rm MC}$	1.04085 ± 0.00047	1.04103 ± 0.00046	1.04106 ± 0.00041	1.04077 ± 0.00032	1.04087 ± 0.00032	1.04093 ± 0.00030
τ	0.078 ± 0.019	0.066 ± 0.016	0.067 ± 0.013	0.079 ± 0.017	0.063 ± 0.014	0.066 ± 0.012
$\ln(10^{10}A_{\rm s})$	3.089 ± 0.036	3.062 ± 0.029	3.064 ± 0.024	3.094 ± 0.034	3.059 ± 0.025	3.064 ± 0.023
$n_{\rm s}$	0.9655 ± 0.0062	0.9677 ± 0.0060	0.9681 ± 0.0044	0.9645 ± 0.0049	0.9653 ± 0.0048	0.9667 ± 0.0040

Planck Collaboration, 2015, paper XIII



Sketch of the Cosmic Ionization History



CMB Sky \rightarrow Cosmology



small-scale CMB, Supernovae, large-scale structure/ BAO, Lyman- α forest, lensing, ...

Cosmological Time in Years



Redshift z

How does cosmological recombination work?

What is the recombination problem about?



- coupled system describing the interaction of *matter* with the ambient CMB *photon* field
- atoms can be in different excitation states
 - \implies lots of levels to worry about
- recombination process changes Wien tail of CMB and this affects the recombination dynamics
 - \implies radiative transfer problem

Have to follow evolution of: $N_{\rm e}, T_{\rm e}, N_{\rm p}, N_i \text{ and } \Delta I_{\nu}$

electron temperature

Only problem in time!

number densities

non-thermal photons

Physical Conditions during Recombination

- Anisotropies negligible for recombination problem
- Temperature $T_{\gamma} \sim 2.725 (1+z) \text{ K} \sim 3000 \text{ K}$
- Baryon number density $N_{\rm b} \sim 2.5 \times 10^{-7} {\rm cm}^{-3} (1+z)^3 \sim 330 {\rm cm}^{-3}$
- Photon number density $N_{\gamma} \sim 410 \text{ cm}^{-3} (1+z)^3 \sim 2 \times 10^9 N_b$ \Rightarrow photons in very distant Wien tail of blackbody spectrum can keep
 - hydrogen ionized until $hv_{\alpha} \sim 40 kT_{\gamma} \Leftrightarrow T_{\gamma} \sim 0.26 \text{ eV}$ (Ly-c 13.6 eV!)
- Collisional processes negligible (completely different in stars!!!)
- Rates dominated by radiative processes (e.g. stimulated emission & stimulated recombination)
- Compton interaction couples electrons very tightly to photons until $z \sim 200 \Rightarrow T_{\gamma} \sim T_e \sim T_m$





3-level Hydrogen Atom and Continuum



Routes to the ground state ?

 direct recombination to 1s Emission of photon is followed by immediate re-absorption 	} No
• recombination to 2p followed by Lyman- α emission	
 medium optically thick to Ly-α phot. many resonant scatterings escape very hard (<i>p</i> ~10⁻⁹ @ <i>z</i> ~1100) 	
 recombination to 2s followed by 2s two-photon decay 	
 2s → 1s ~10⁸ times slower than Ly-α 2s two-photon decay profile → maximum at v ~ 1/2 v_α 	~ 57%
- immediate escape	

Zeldovich, Kurt & Sunyaev, 1968, ZhETF, 55, 278 Peebles, 1968, ApJ, 153, 1

 $\Delta N_{\rm e}$ / $N_{\rm e}$ ~ 10% - 20%

These first computations were completed in 1968!



Moscow





Vladimir Kurt (UV astronomer)



Rashid Sunyaev



losif Shklovskii

Princeton



Jim Peebles

Let's do the simple 3-level atom derivation?

Multi-level Atom ⇔ Recfast-Code



Seager, Sasselov & Scott, 1999, ApJL, 523, L1 Seager, Sasselov & Scott, 2000, ApJS, 128, 407

RECFAST reproduces the result of detailed recombination calculation using fudge-functions

Output of $N_{\rm e}/N_{\rm H}$

Hydrogen:

- up to 300 levels (shells)
- $n \ge 2 \Rightarrow$ full SE for *l*-sub-states

Helium:

- Hel 200-levels (z ~ 1400-1500)
- Hell 100-levels (*z* ~ 6000-6500)
- Helll 1 equation

Low Redshifts:

- H chemistry (only at low z)
- cooling of matter (Bremsstrahlung, collisional cooling, line cooling)



Getting the job done for Planck

44 GHz

Hydrogen recombination

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- Feedback of the Lyman- α distortion on the 1s-2s two-photon absorption rate (Kholupenko & Ivanchik, 2006, Astr. Lett.; Fendt et al. 2008; Hirata 2008)
- Non-equilibrium effects in the angular momentum sub-states (Rubiño-Martín, JC & Sunyaev, 2006, MNRAS; JC, Rubiño-Martín & Sunyaev, 2007, MNRAS; Grin & Hirata, 2009; JC, Vasil & Dursi, 2010)
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- Collisions and Quadrupole lines (JC, Rubiño-Martín & Sunyaev, 2007; Grin & Hirata, 2009; JC, Vasil & Dursi, 2010; JC, Fung & Switzer, 2011)
- Raman scattering (Hirata 2008; JC & Thomas , 2010; Haimoud & Hirata, 2010)

Helium recombination

- Similar list of processes as for hydrogen (Switzer & Hirata, 2007a&b; Hirata & Switzer, 2007)
- Spin forbidden 2p-1s triplet-singlet transitions (Dubrovich & Grachev, 2005, Astr. Lett.; Wong & Scott, 2007; Switzer & Hirata, 2007; Kholupenko, Ivanchik&Varshalovich, 2007)
- Hydrogen continuum opacity during He I recombination (Switzer & Hirata, 2007; Kholupenko, Ivanchik & Varshalovich, 2007; Rubiño-Martín, JC & Sunyaev, 2007; JC, Fung & Switzer, 2011)
- Detailed feedback of helium photons (Switzer & Hirata, 2007a; JC & Sunyaev, 2009, MNRAS; JC, Fung & Switzer, 2011)







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Solving the problem for the *Planck* Collaboration was a common effort!



Atomic Physics Challenges

Hydrogen Atom & Hydrogenic Helium

- Rather simple and basically analytic (e.g., Karzas & Latter, 1961)
- Even 2γ rates can be computed precisely (e.g., Goeppert-Mayer, 1931)
- Collisional rates less robust, but effect small (new rates became available!)
- Biggest computational challenge is the number of levels (~ n²)

Neutral Helium

- Lower levels non-hydrogenic (perturbative approach needed)
- Spectrum complicated and data (was) rather sparse (e.g., Drake & Morton, 2007)





Grotrian diagram for neutral helium



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Neutral Helium

- Lower levels non-hydrogenic (perturbative approach needed)
- Spectrum complicated and data (was) rather sparse (e.g., Drake & Morton, 2007)
- Collisional rate estimates pretty rough (important for distortions...)
- Computational challenge because of levels not as demanding if you only want to get the free electron fraction right

(not true for spectrum...)





Stimulated HI 2s \rightarrow 1s decay



2s-1s emission profile

Transition rate in vacuum $\rightarrow A_{2s1s} \sim 8.22 \text{ sec}^{-1}$ CMB ambient photons field $\rightarrow A_{2s1s}$ increased by ~1%-2% \rightarrow HI - recombination faster by $\Delta N_e/N_e \sim 1.3\%$



Feedback of Ly- α on the HI 1s \rightarrow 2s transition



- Some Ly-α photon are reabsorbed in the 1s-2s channel
- delays recombination
- net effect on 2s-1s channel $\Delta N_e/N_e \sim 0.6\%$ around z~1100
- 2s-1s self-feedback $\Delta N_e/N_e \sim -0.08\%$ around z~1100 (JC & Thomas, 2010)

Kholupenko et al. 2006 Fendt, JC, Rubino-Martin & Wandelt, 2009

Two-photon emission process from upper levels



Seaton cascade (1+1 photon)

No collisions \rightarrow two photons (mainly H- α and Ly- α) are emitted!

Maria-Göppert-Mayer (1931): description of two-photon emission as single process in Quantum Mechanics

→ Deviations of the two-photon line profile from the Lorentzian in the damping wings

→ Changes in the optically thin
 (below ~500-5000 Doppler width)
 parts of the line spectra

3s and 3d two-photon decay spectrum



Direct Escape in optically thin regions:

- → HI -recombination is a bit *slower* due to 2γ-transitions from s-states
- → HI -recombination is a bit *faster* due to 2γ-transitions from d-states

2s-1s Raman scattering



- Computation similar to two-photon decay profiles
- collisions weak \implies process needs to be modeled as single quantum act



Hirata 2008 JC & Thomas, 2010

Deviations from Statistical Equilibrium in the upper levels

Basis for Recfast computation (Seager et al. 2000)

- *l*-dependence of populations neglected
- Levels in a given shell assumed to be in Statistical Equilibrium (SE)
- Complexity of problem scales like ~ n_{max}

$$N_{nl} = \frac{2l+1}{n^2} N_{\text{tot},n}$$

Processes for the upper levels



recombination & photoionization

- *n* small \rightarrow *l*-dependence not drastic
- high shells \rightarrow more likely to *l*<<*n*
- large $n \rightarrow induced$ recombination
- many radiative dipole transitions
 - Lyman-series optically thick
 - $\Delta l = \pm 1$ restriction (electron cascade)
 - large *n* & small $\Delta n \rightarrow$ *induced* emission
- *l*-changing collisions
 - help to establish full SE within the shell
 - only effective for n > 25-30
- *n*-changing collisions
- Collisional photoionization
- Three-body-recombination

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Refined computation

(JC, Rubino-Martin & Sunyaev, 2007)

- need to treat angular momentum sub-levels separately!
- include collision to understand how close things are to SE
- Complexity of problem scales like ~ n²max
- But problem very sparse
 (Grin & Hirata, 2010; JC, Vasil & Dursi, 2010)



JC, Vasil & Dursi, MNRAS, 2010

Sparsity of the problem and effect of ordering

20 shell Hydrogen + 5 shell Helium model



Shell-by-Shell ordering

 $1s, 2s, 2p, 3s, 3p, 3d, \ldots$

Angular momentum ordering

 $1s, 2s, 3s, \dots, ns, 2s, 3p, \dots, np, 3d, 4d, \dots$

Grin & Hirata, 2010 JC, Vasil & Dursi, MNRAS, 2010

The Lyman- α radiative transfer problem

Sobolev approximation

(developed in late 50's to model moving envelopes of stars)





To solve the coupled system of rate-equations

→ need to know mean intensity across the Ly- α (& Ly-n) resonance at different times

- \rightarrow approximate solution using *escape probability*
- \rightarrow Escape == photons stop interacting with Ly- α resonance
 - == photons stop supporting the 2p-level
 - == photons reach the very distant red wing

Main assumptions of Sobolev approximation

- populations of level + radiation field quasi-stationary
- every 'scattering' leads to complete redistribution
- emission & absorption profiles have the same shape

Doppler width

$$\frac{\Delta\nu_{\rm D}}{\nu} = \sqrt{\frac{2kT}{m_{\rm H}c^2}} \simeq {\rm few} \times 10^{-5}$$

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- emission & absorption profiles have the same shape
- Sobolev escape probability & optical depth

$$P_{\rm S} = \frac{1 - e^{-\tau_{\rm S}}}{\tau_{\rm S}} \simeq 10^{-8}$$

$$\tau_{\rm S} = \frac{c \,\sigma_{\rm r} N_{\rm 1s}}{H} \,\frac{\Delta \nu_{\rm D}}{\nu} = \frac{g_{\rm 2p}}{g_{\rm 1s}} \,\frac{A_{\rm 21} \lambda_{\rm 21}^3}{8\pi H} \,N_{\rm 1s}$$

Problems with Sobolev approximation:

Complete redistribution ⇔ partial redistribution



Sobolev-approximation:

- Important variation of the photon distribution at ~1.5 times the ionization energy!
- For 1% accuracy one has to integrate up to ~10⁷ Doppler width!
- Complete redistribution bad approximation and very unlikely (p~10⁻⁴-10⁻³)

No redistribution case:

- Much closer to the correct solution (*partial redistribution*)
- Avoids some of the unphysical aspect

Other Problems with Sobolev approximation

Time-dependence of the emission process

- Quasi-stationarity ok close to line center
- Non-stationarity important in the distant wings
- Wings even at ~ 10⁴ Doppler width ($\Delta \nu / \nu \sim 10\%$) required for <0.1% precision

Asymmetry of emission / absorption profiles

- Standard textbook equations always assume $v \sim v_0$
- Basically wrong in distant damping wings
- Detailed balance off → blackbody not conserved!
- Formulation that includes profile asymmetries required



Evolution of the HI Lyman-series distortion



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Main corrections during Hel Recombination



- Delayed neutral helium recombination was indeed one of the *Recfast* results
- Effect of HI absorption already mentioned in Hu et al. 1995 (priv. comm Peebles)
- Spin-forbidden Hel transition estimated in 1977 (Lin et al.)
- But neutral helium recombination not as crucial for Cl's...

Kholupenko et al, 2007 Switzer & Hirata, 2007

Evolution of the Hel high frequency distortion

CosmoRec v2.0 only!



HeI Lyman-series spectral distortion at z = 2996



So why is all this so important?

Cosmological Time in Years



Cumulative Changes to the Ionization History





JC & Thomas, MNRAS, 2010; Shaw & JC, MNRAS, 2011

Cumulative Change in the CMB Power Spectra





Importance of recombination for Planck



CITA Guidantian Shaw & JC, 2011, and references therein

Biases as they would have been for Planck



- Biases a little less significant with real *Planck* data
- absolute biases very similar
- In particular n_s would be biased significantly

Planck Collaboration, XIII 2015

Importance of recombination for inflation constraints



Planck Collaboration, 2015, paper XX

Analysis uses refined recombination model (CosmoRec/HyRec)

CMB constraints on N_{eff} and Y_p



Consistent with SBBN and standard value for N_{eff}

• Future CMB constraints (Stage-IV CMB) on Yp will reach 1% level

Importance of recombination for measuring helium



Cosmological Recombination Radiation

Simple estimates for hydrogen recombination

Hydrogen recombination:

 per recombined hydrogen atom an energy of ~ 13.6 eV in form of photons is released

- at $z \sim 1100 \rightarrow \Delta \epsilon/\epsilon \sim 13.6 \text{ eV } N_b / (N_\gamma 2.7 \text{k} T_r) \sim 10^{-9} \text{--} 10^{-8}$
- \rightarrow recombination occurs at redshifts $z < 10^4$
- At that time the *thermalization* process doesn't work anymore!
- There should be some small spectral distortion due to additional Ly-α and 2s-1s photons! (Zeldovich, Kurt & Sunyaev, 1968, ZhETF, 55, 278; Peebles, 1968, ApJ, 153, 1)
- → In 1975 *Viktor Dubrovich* emphasized the possibility to observe the recombinational lines from n > 3 and $\Delta n << n!$



Rubino-Martin et al. 2006, 2008; Sunyaev & JC, 2009

Cosmological Time in Years



New detailed and fast computation!



CosmoSpec: fast and accurate computation of the CRR



- Like in old days of CMB anisotropies!
- detailed forecasts and feasibility studies
- non-standard physics (variation of α, energy injection etc.)

CosmoSpec will be available here:

What would we actually learn by doing such hard job?

Cosmological Recombination Spectrum opens a way to measure:

- \rightarrow the specific *entropy* of our universe (related to $\Omega_{b}h^{2}$)
- \rightarrow the CMB *monopole* temperature T_0
- \rightarrow the pre-stellar abundance of helium Y_p

→ If recombination occurs as we think it does, then the lines can be predicted with very high accuracy!

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→ In principle allows us to directly check our understanding of the standard recombination physics

Dark matter annihilations / decays



- Additional photons at all frequencies
- Broadening of spectral features
- Shifts in the positions

JC, 2009, arXiv:0910.3663



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If something unexpected or non-standard happened:

- → non-standard thermal histories should leave some measurable traces
- \rightarrow direct way to measure/reconstruct the recombination history!
- \rightarrow possibility to distinguish pre- and post-recombination y-type distortions
- \rightarrow sensitive to energy release during recombination
- → variation of fundamental constants

Summary

The standard recombination problem has been solved to a level that is sufficient for the analysis of current and future CMB data (<0.1% precision!)</p>

- Many people helped with this problem!
- Without the improvements over the original version of Recfast cosmological parameters derived from Planck would be *biased* significantly
- In particular the discussion of *inflatio* models would have been affected
- Cosmological recombination radiation allows us to directly constrain the recombination history