

CKM and CP Constraints from B-Decays

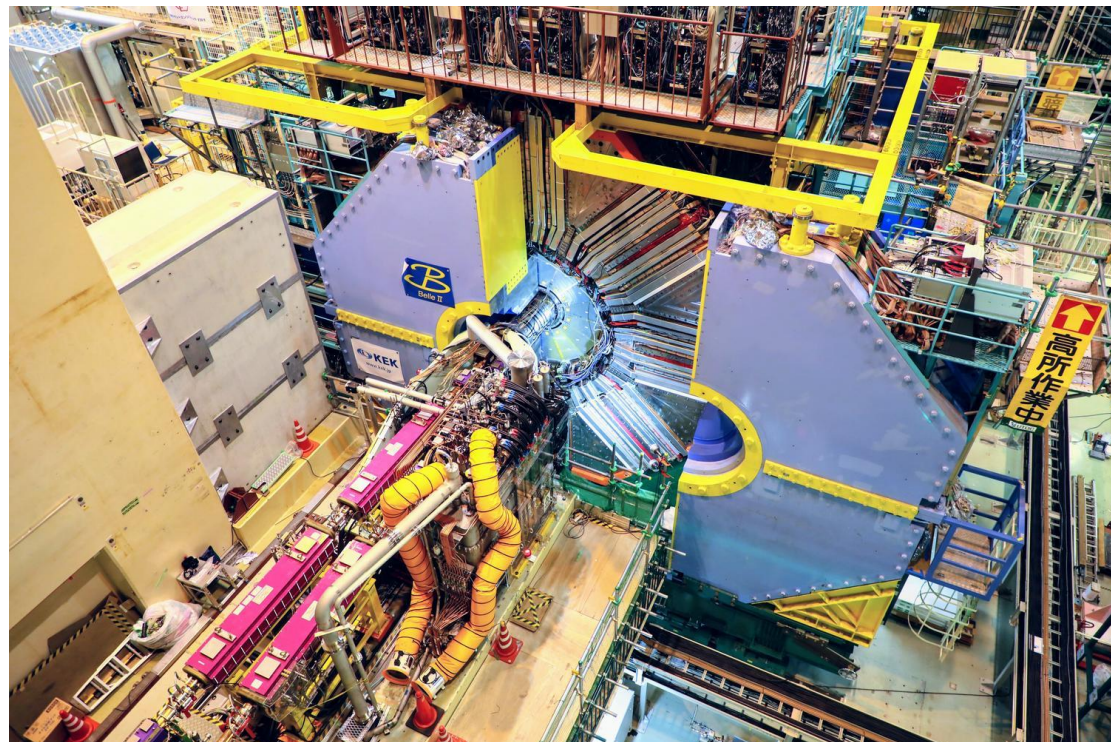
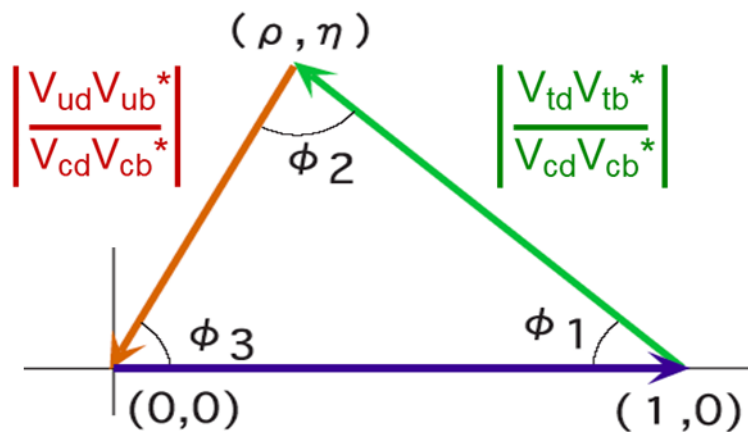
Shohei Nishida

KEK

Lepton Photon 2019

Aug. 9, 2019

- ϕ_1 / β
- ϕ_s
- ϕ_3 / γ
- $|V_{cb}|$
- CP Asymmetry in
 $B^+ \rightarrow \pi^+ K^+ K^-$, $\pi^+ \pi^- \pi^+$



Kobayashi-Maskawa theory

Complex phase in the quark mixing matrix
→ CP violation in the Standard Model (SM)

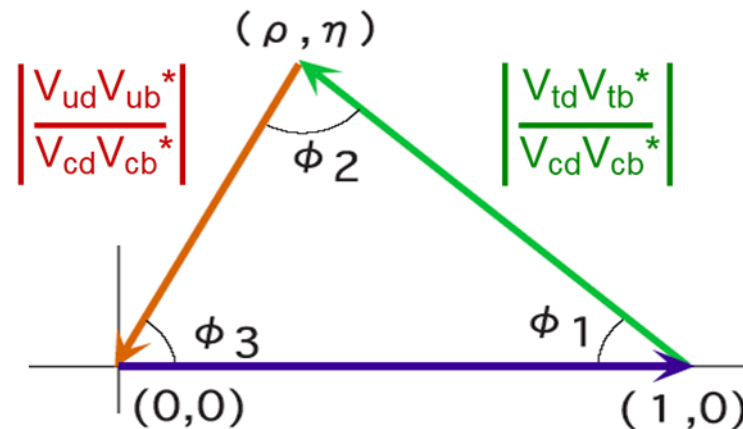


CKM (Cabibbo-Kobayashi-Maskawa) Matrix

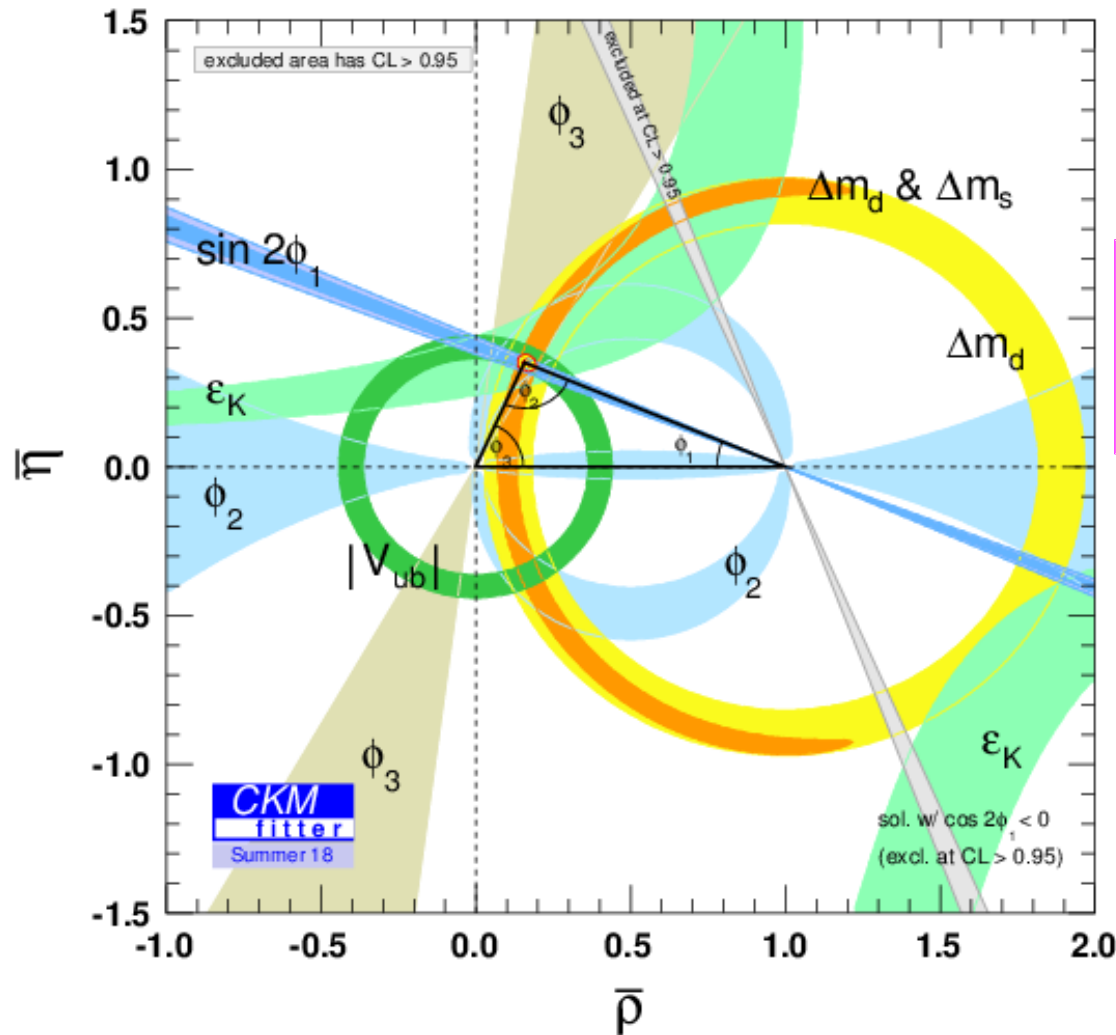
$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

From the unitarity of the matrix:

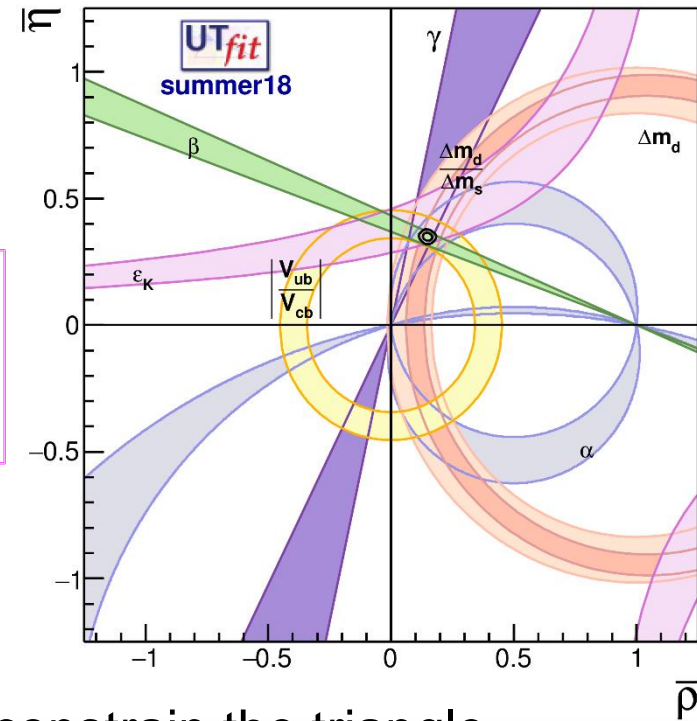
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



$$\begin{aligned} \phi_1 &= \beta \\ \phi_2 &= \alpha \\ \phi_3 &= \gamma \end{aligned}$$



$$\begin{aligned}\phi_1 &= \beta \\ \phi_2 &= \alpha \\ \phi_3 &= \gamma\end{aligned}$$



- Overconstrain the triangle
→ test of the SM
- Measurements generally consistent.
- Still room for O(10%) New Physics effect.

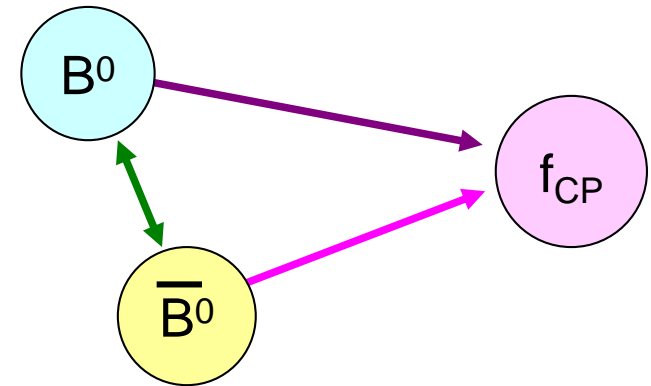
Mixing-induced CP asymmetry

- B^0 and \bar{B}^0 decay to a common CP eigenstate f_{CP} .
- CP violation appears as a decay time difference.

$$A_{CP}(\Delta t) = \frac{\Gamma(\bar{B}^0(\Delta t) \rightarrow f_{CP}) - \Gamma(B^0(\Delta t) \rightarrow f_{CP})}{\Gamma(\bar{B}^0(\Delta t) \rightarrow f_{CP}) + \Gamma(B^0(\Delta t) \rightarrow f_{CP})}$$

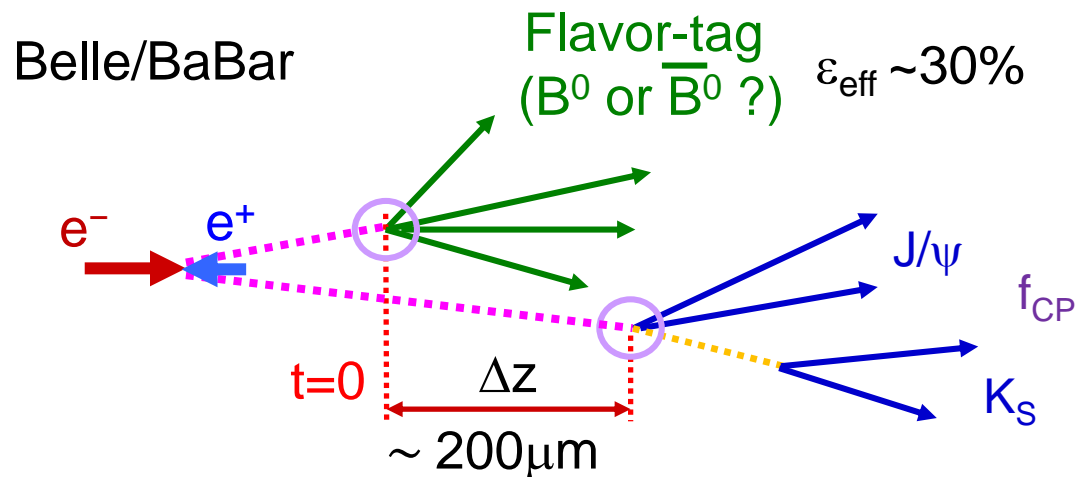
$$= S \sin(\Delta m \Delta t) + A \cos(\Delta m \Delta t)$$

$$S = -\xi \sin(2\phi_1) \text{ for } B \rightarrow J/\psi K_{S/L}$$

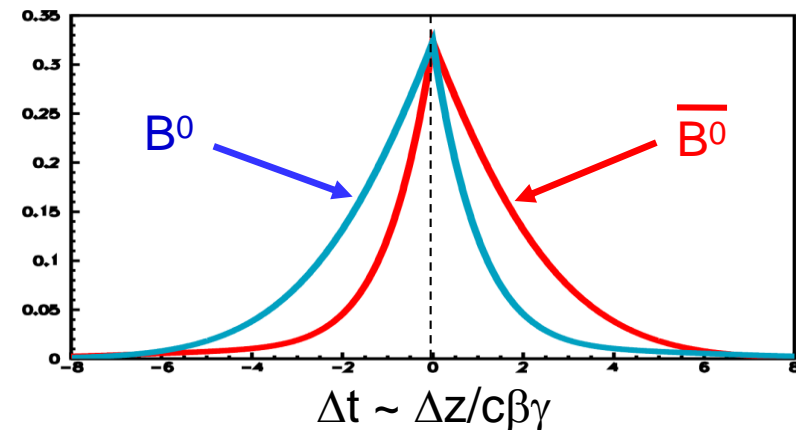


S : mixing induced CPV

A : direct CPV ($= -C$)



measure position instead of time



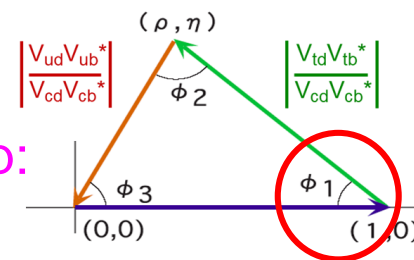
- $\sin(2\phi_1)$ has been measured precisely with $b \rightarrow c\bar{c}s$ tree process

$$\sin(2\phi_1) = 0.699 \pm 0.017 \quad (\text{HFLAV})$$

- Measurement of $\sin(2\phi_1)$ using other processes with penguin loop:

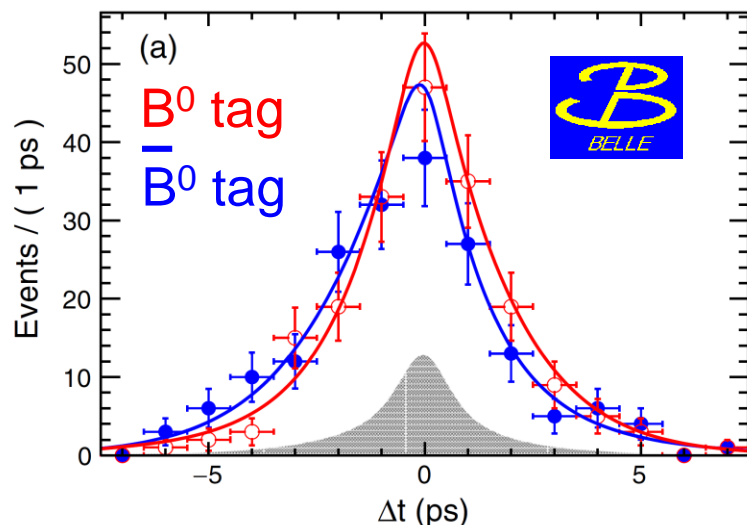
✓ To probe non-SM contribution in the penguin loop.

- Recent results from Belle: $B \rightarrow J/\psi \pi^0, \pi^0 \pi^0 K_S$ with 711 fb^{-1}



$B \rightarrow J/\psi \pi^0$ (tree + penguin) [PRD98 (2018) 112008]

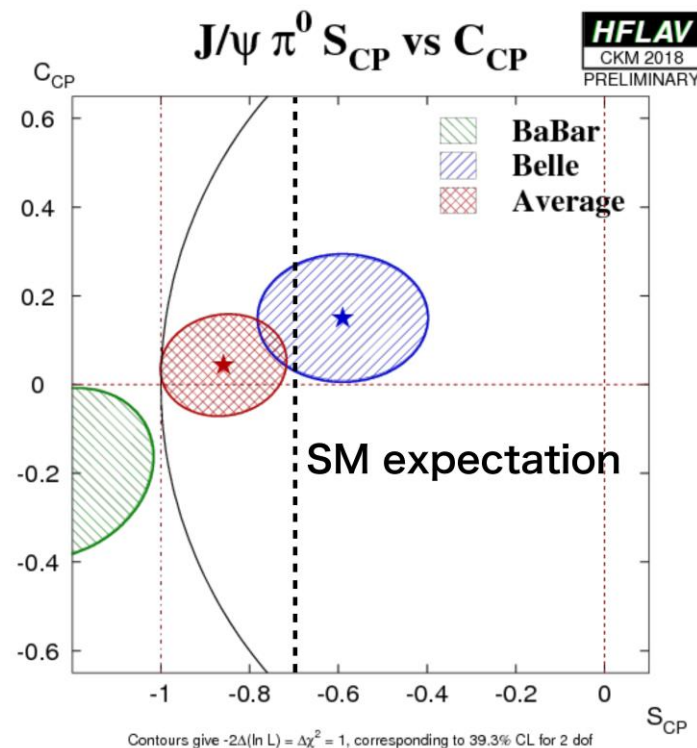
Understanding of penguin contribution could improve the uncertainty of $\sin(2\phi_1)$



$S = -\sin(2\phi_1)$ in SM

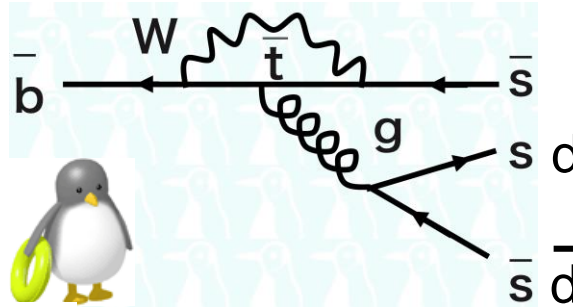
$$S = -0.59 \pm 0.19 \pm 0.03$$

$$A = -C = 0.15 \pm 0.14^{+0.04}_{-0.03}$$



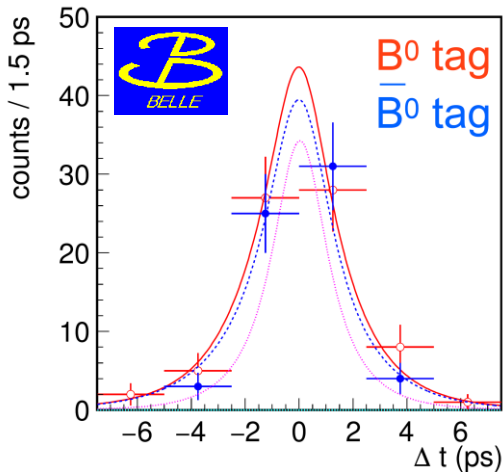
$B \rightarrow \pi^0 \pi^0 K_S$

[PRD99 (2019)
011102]



$b \rightarrow \bar{s} q q$ $\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$

HFLAV
Summer 2018
PRELIMINARY



New result
from Belle is
coming soon

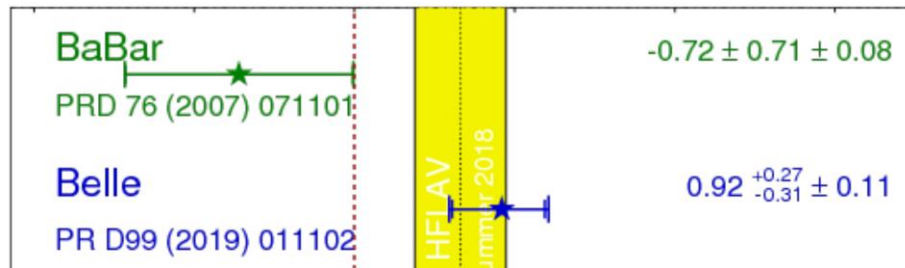
$S = -\sin(2\phi_1)$ in SM

$S = -0.92^{+0.27}_{-0.31} {}^{+0.10}_{-0.11}$

$A = 0.28 \pm 0.21 \pm 0.04$

$b \rightarrow ccs$	World Average		0.70 ± 0.02
ϕK^0	Average		$0.74^{+0.11}_{-0.13}$
$\eta' K^0$	Average		0.63 ± 0.06
$K_S K_S K_S$	Average		0.72 ± 0.19
$\pi^0 K^0$	Average		0.57 ± 0.17
$\rho^0 K_S$	Average		$0.54^{+0.18}_{-0.21}$
ωK_S	Average		0.71 ± 0.21
$f_0 K_S$	Average		$0.69^{+0.10}_{-0.12}$
$f_2 K_S$	Average		0.48 ± 0.53
$f_X K_S$	Average		0.20 ± 0.53
$\pi^0 \pi^0 K_S$	Average		0.66 ± 0.28
$\phi \pi^0 K_S$	Average		$0.97^{+0.03}_{-0.52}$
$\pi^+ \pi^- K_S$	Average		0.01 ± 0.33
$K^+ K^- K^0$	Average		$0.68^{+0.09}_{-0.10}$

Study items at Belle II



Another combination of the unitarity of the CKM matrix makes a squashed triangle.

$$V_{us}V_{ub}^* + V_{cs}V_{cb}^* + V_{ts}V_{tb}^* = 0$$

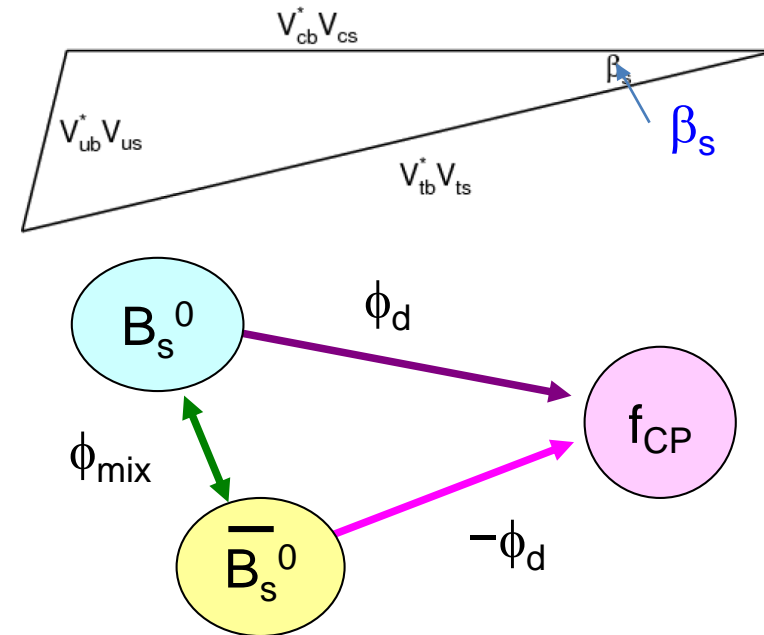
- β_s can be measured in mixing-induced CP violation in B_s decays like $B_s \rightarrow J/\psi \phi$.

$$\phi_s = \phi_{\text{mix}} - 2\phi_d = -2\beta_s \quad (\text{in SM})$$

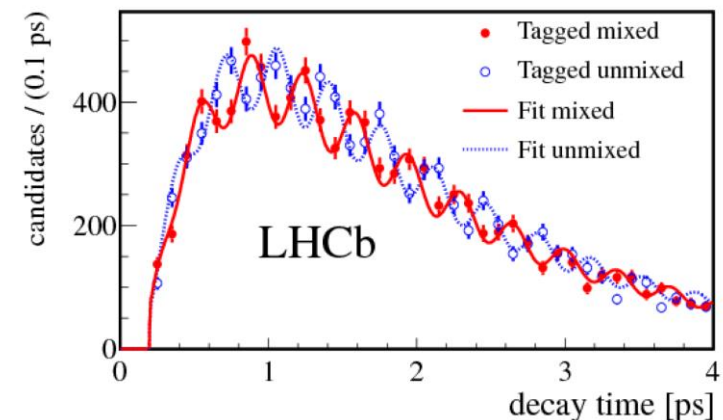
$$\phi_s = -36.8^{+1.0}_{-0.7} \text{ mrad (SM)}$$

Experimental technique

- ✓ excellent time resolution (<100fs) necessary because of fast B_s oscillation,
 - Cannot be studied at B-factories due to small boost factor.
- ✓ flavor tagging
- ✓ angular distribution to extract CP eigenstate.

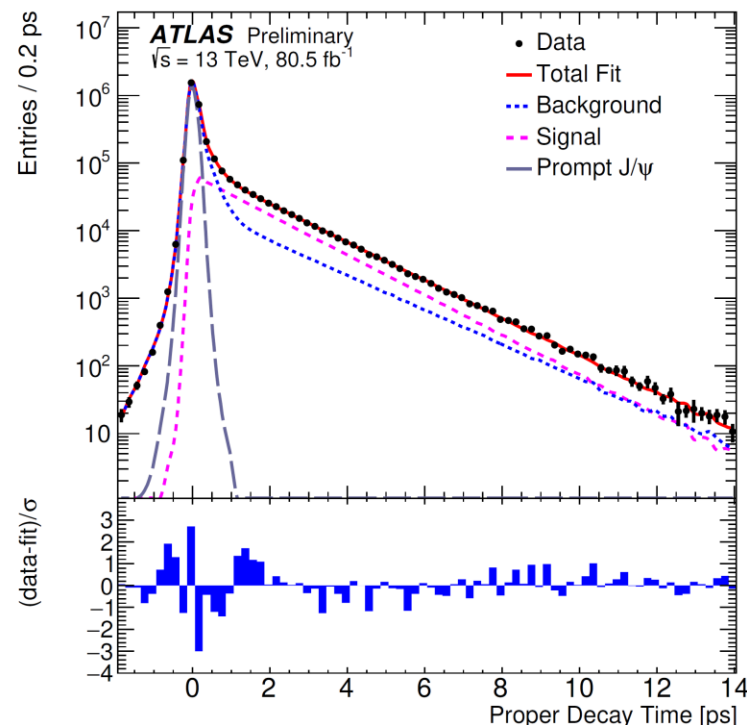
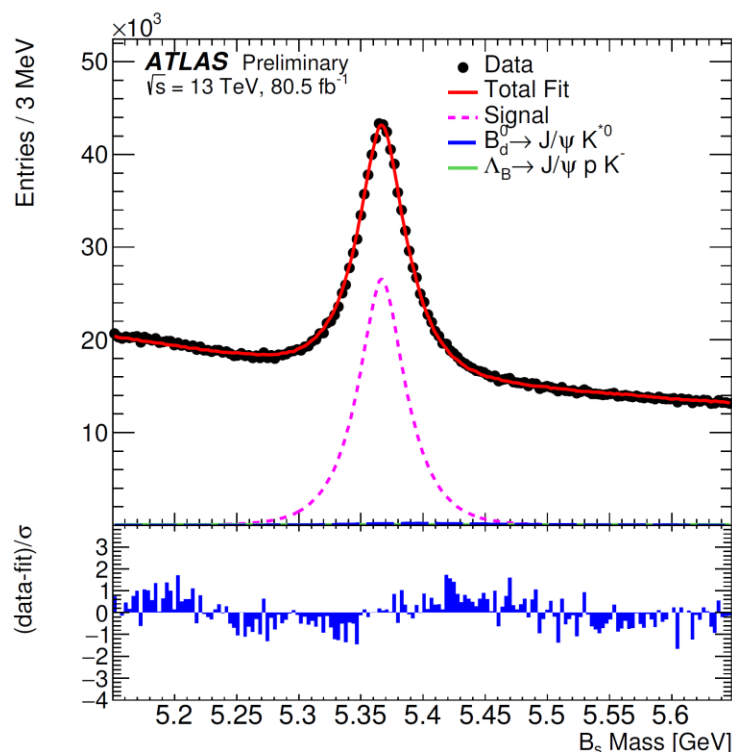


[New J. Phys. 15 (2013) 053021]



[ATL-CONF-2019-009]

- $B_s \rightarrow J/\psi \phi$
- Previous result from ATLAS was based on 19.2 fb^{-1} at 7-8 TeV (Run1).
- **New measurement with 80.5 fb^{-1} at 13 TeV (Run2).**
- Flavor tagging (of the other side b-hadron) using weighted sum of the charge in a cone around a lepton or in a jet. **Calibrated with $B^+ \rightarrow J/\psi K^+$.**



Physical values obtained from 80.5 fb⁻¹

Parameter	Value	Statistical uncertainty	Systematic uncertainty
ϕ_s [rad]	-0.068	0.038	0.018
$\Delta\Gamma_s$ [ps ⁻¹]	0.067	0.005	0.002
Γ_s [ps ⁻¹]	0.669	0.001	0.001
$ A_{ }(0) ^2$	0.219	0.002	0.002
$ A_0(0) ^2$	0.517	0.001	0.004
$ A_S(0) ^2$	0.046	0.003	0.004
δ_{\perp} [rad]	2.946	0.101	0.097
$\delta_{ }$ [rad]	3.267	0.082	0.201
$\delta_{\perp} - \delta_S$ [rad]	-0.220	0.037	0.010

Syst. for ϕ_s is mainly from tagging

Combined with 19.2 fb⁻¹ data @ 7,8 TeV

$$\phi_s = -0.076 \pm 0.034 \pm 0.019 \text{ mrad}$$

$$\Delta\Gamma_s = 0.068 \pm 0.004 \pm 0.003 \text{ ps}^{-1}$$

$\Gamma_s, \Delta\Gamma_s$

decay with and decay width difference

$\phi_s (\approx 2\beta_s)$

CP violating phase

$|A_0|^2, |A_{||}|^2$

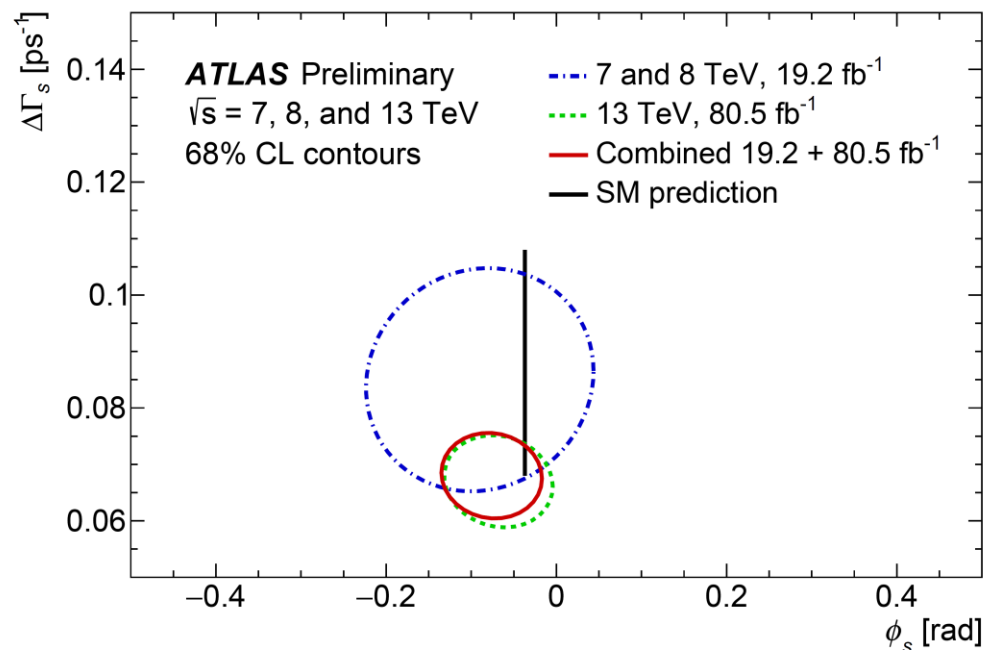
CP state amplitudes

$\delta_{||}, \delta_{\perp}$

Strong phases

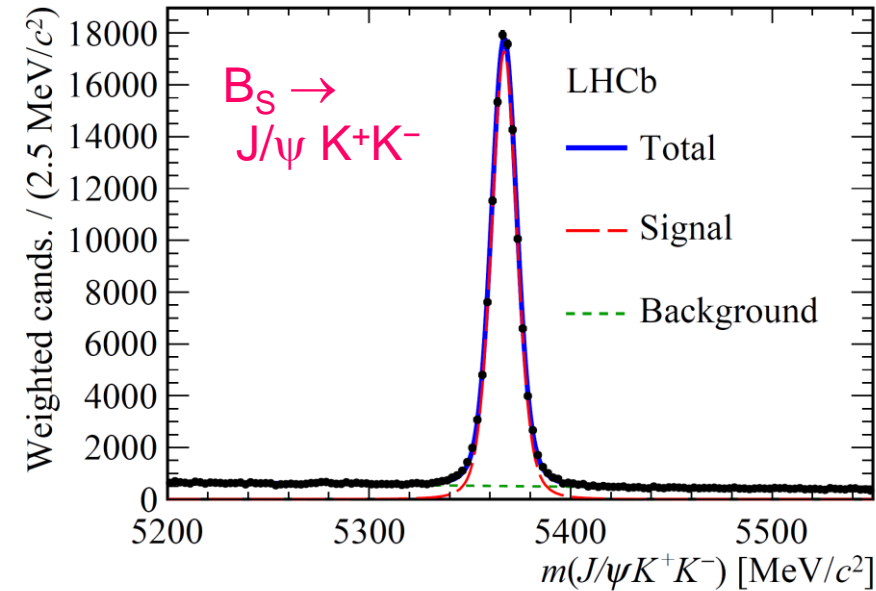
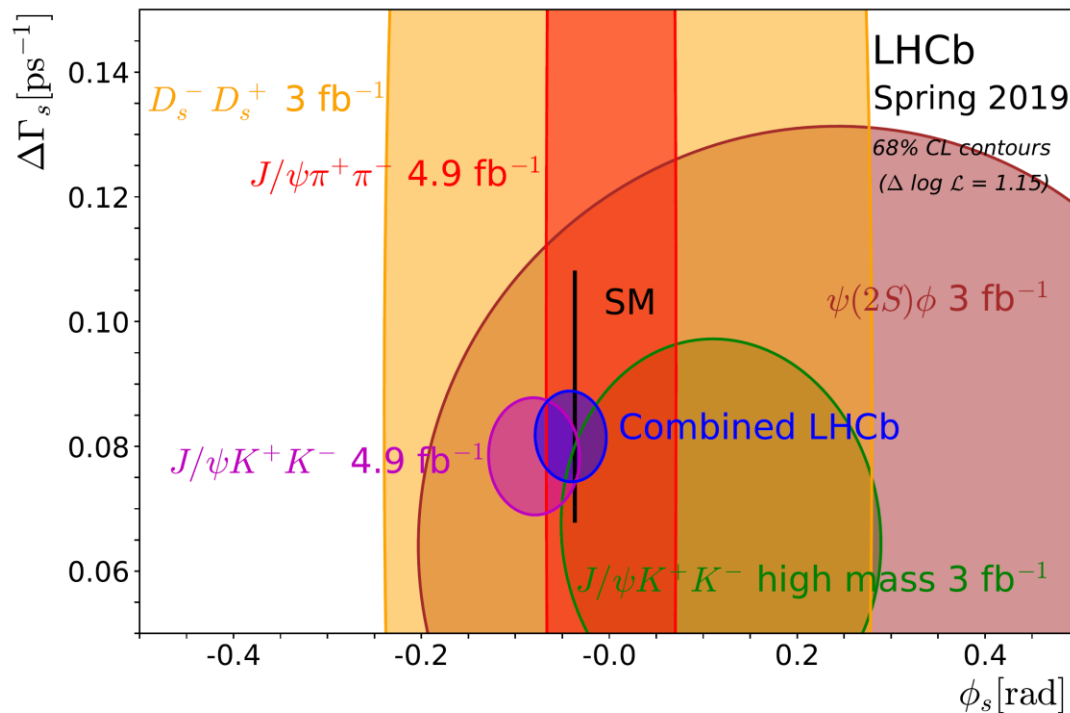
$|A_S|^2, \delta_S$

S-wave parameters



- $B_s \rightarrow J/\psi K^+ K^-$ and $B_s \rightarrow J/\psi \pi^+ \pi^-$.
- 1.9 fb^{-1} from LHC Run2.
- $B_s \rightarrow J/\psi K^+ K^-$ around ϕ region.

[arXiv:1906.08356, arXiv:1903.05530]



$B_s \rightarrow J/\psi K^+ K^-$

$$\phi_s = -84 \pm 41 \pm 6 \text{ mrad}$$

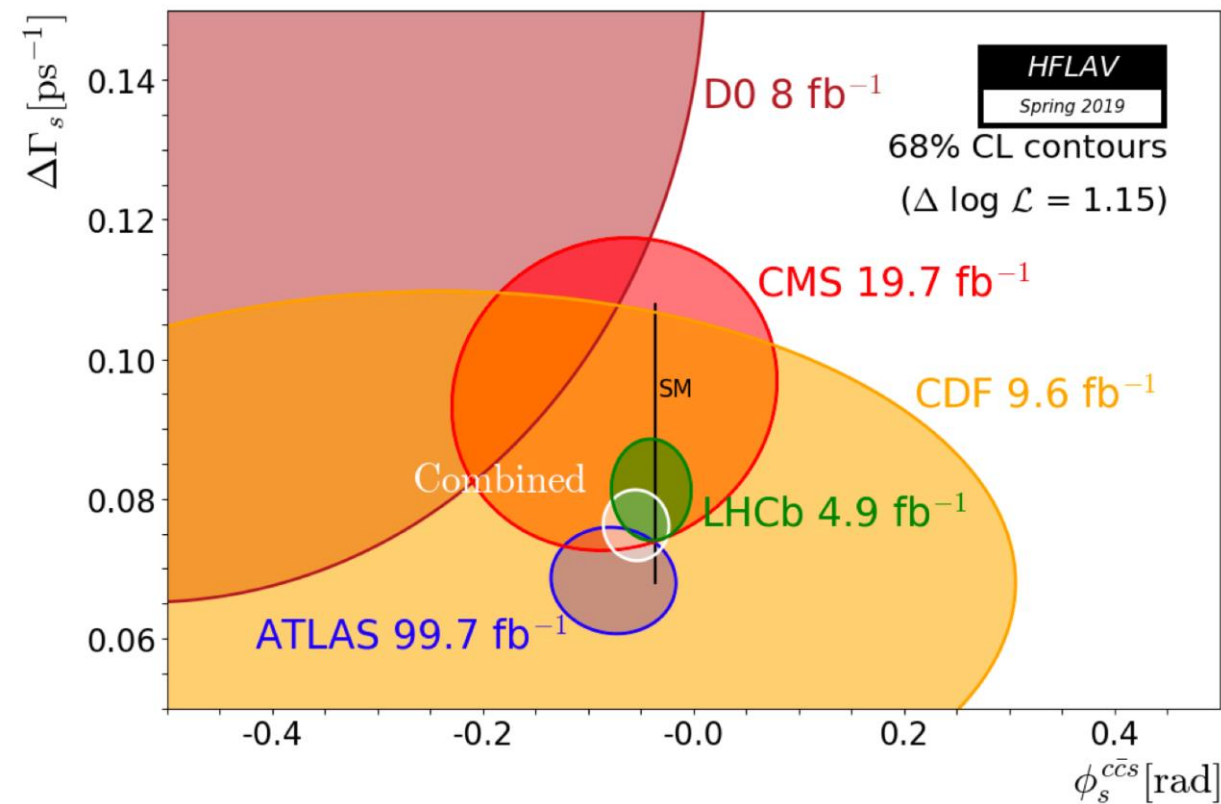
$B_s \rightarrow J/\psi \pi^+ \pi^-$

$$\phi_s = -57 \pm 60 \pm 11 \text{ mrad}$$

LHCb combined

$$\phi_s = -41 \pm 25 \text{ mrad}$$

[Parallel Talk by C.Santamarina on Thursday]



- Improved measurements from ATLAS and LHCb.
- Exp. error still one order larger than the SM.
- Measurements are limited by statistics. Further improvement is expected at HL-LHC.

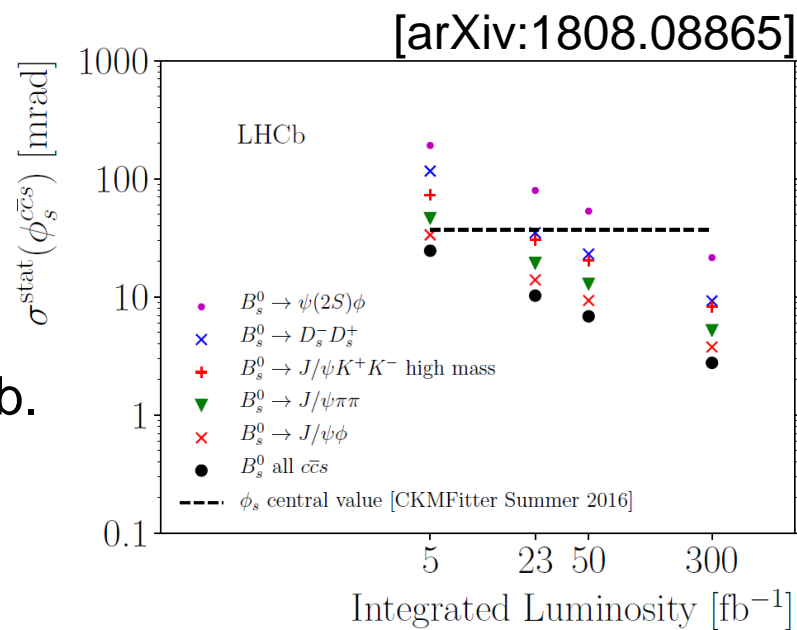
SM prediction

$$\phi_s = -36.8^{+1.0}_{-0.7} \text{ mrad}$$

(CKMFitter)

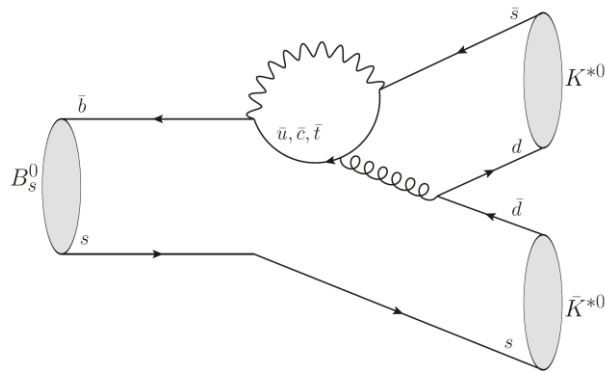
HFLAV (exp. average)

$$\phi_s = -55 \pm 21 \text{ mrad}$$



- Measure ϕ_s in other processes through loop diagram.
- Good probes for New Physics: heavy NP particles in the loop.

$$B_S \rightarrow (K^+\pi^-)(K^-\pi^+)$$



3.0 fb⁻¹ at 7, 8 TeV

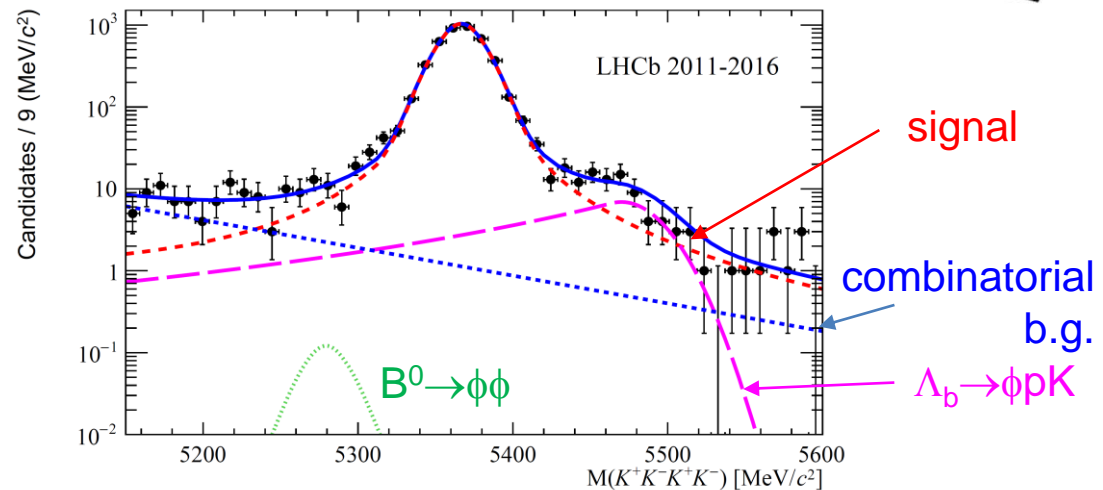
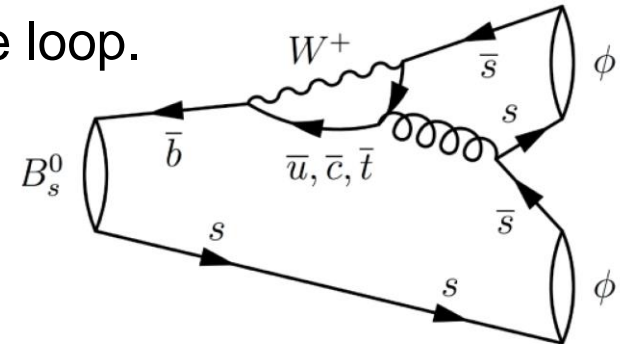
$$\phi_s (dd) = -0.10 \pm 0.13 \pm 0.14 \text{ rad}$$

[JHEP03 (2018) 140]

$$\phi_s = -55 \pm 21 \text{ mrad (HFLAV) for } b \rightarrow ccs$$

[Parallel Talk by C.Santamarina on Thursday]

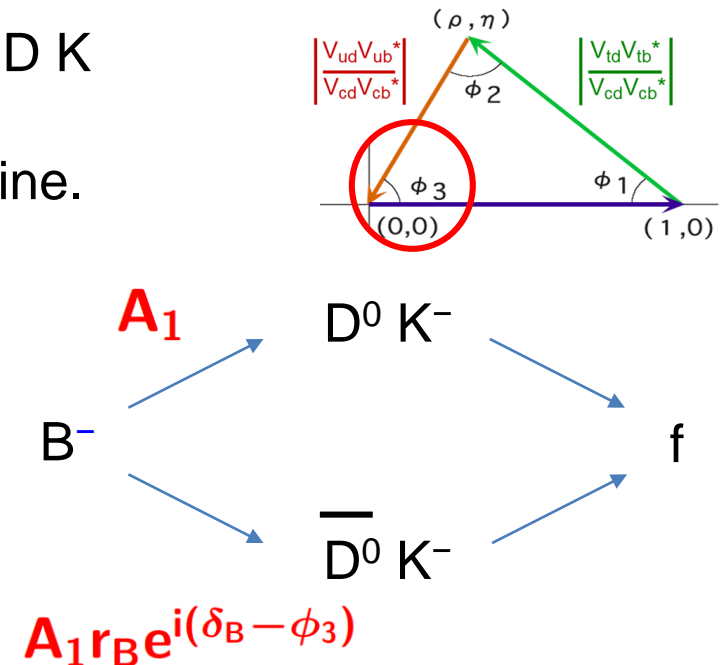
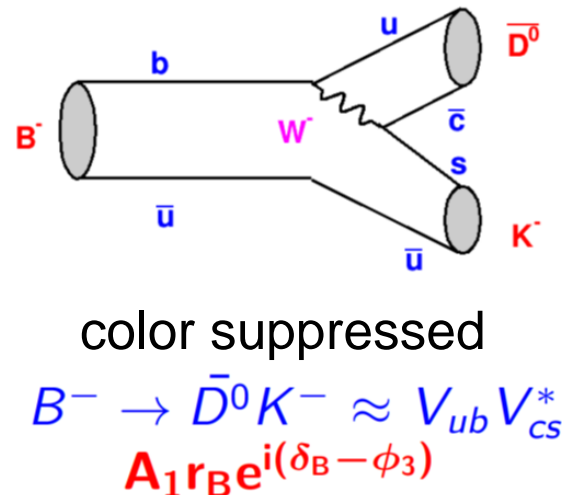
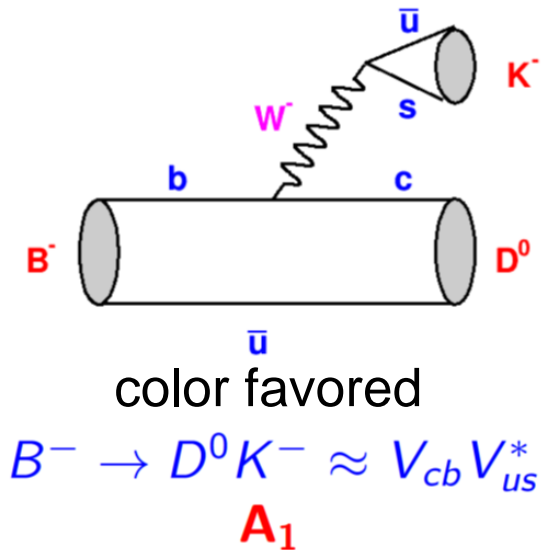
$$B_S \rightarrow \phi\phi$$



$$\phi_s (sss) = -73 \pm 115 \pm 27 \text{ mrad}$$

[arXiv:1907.10003]

- ϕ_3 / γ can be measured using the interference $B \rightarrow D K$ and $B \rightarrow \bar{D} K$.
 - ✓ Not necessarily $B \rightarrow D K$. $B \rightarrow D K^*$ etc. are fine.



- Only tree contributions: theoretically clean.
- Several decay modes (final states) possible to extract ϕ_3 / γ .
- Amplitude ratio r_B and strong phase δ_B are mode-dependent.
 - ✓ sensitivity depends on modes.

- GLW (Gronau-London-Wyler) [PLB 253 (1991) 483, PLB 265 (1991) 172]
 - ✓ $B^\pm \rightarrow D_{CP}^0 K^\pm$
 - ✓ Use CP eigenstate of D meson.
- ADS (Atwood-Dunietz-Soni) [PRL 78, 3357 (1997), PRD 63. 036005 (2001)]
 - ✓ Enhancement of CP violation by using doubly Cabibbo suppressed decays.
- GGSZ (Giri-Grossmann-Soffer-Zupan) [PRD 68. 054018 (2003)]
 - ✓ 3 (or multi-) body final state.
 - ✓ Different amplitude and strong phase in different region of Dalitz plot.
- GLS (Grossmann-Ligeti-Soffer) [PRD 67. 071301 (R) (2003)]
 - ✓ Singly Cabibbo suppressed D decay ($K_S K \pi$)

- Binned Dalitz plot analysis using $B^- \rightarrow D^0 K^-$, $D^0 \pi^-$ with $D^0 \rightarrow K_S \pi^+ \pi^- \pi^0$.
 - ✓ Model-independent formalism
 - ✓ $D^0 \rightarrow K_S \pi^+ \pi^-$ is the primary mode for such studies, but $D^0 \rightarrow K_S \pi^+ \pi^- \pi^0$ has twice larger branching fraction (5.2%).
 - ✓ $r_B(DK) \sim 0.1$ and $r_B(D\pi) \sim 0.005$ while $B(B^- \rightarrow D^0 \pi^-) \sim 10 \times B(B^- \rightarrow D^0 K^-)$.
 $B^- \rightarrow D^0 \pi^-$ is not sensitive to ϕ_3 , but serves as a control mode.

For the B^- decay,

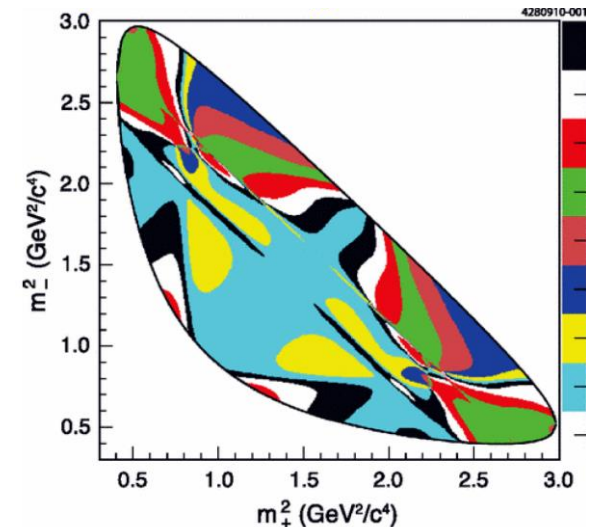
$$\Gamma_i^- = K_i + r_B^2 \bar{K}_i + 2\sqrt{K_i \bar{K}_i} (c_i x_- + s_i y_-)$$

$$\mathbf{x}_{\pm} = r_B \cos(\delta_B \pm \phi_3); \mathbf{y}_{\pm} = r_B \sin(\delta_B \pm \phi_3)$$

c_i, s_i - cosine and sine of the strong phase difference between D^0 and \bar{D}^0

Input from CLEO-c or BESIII

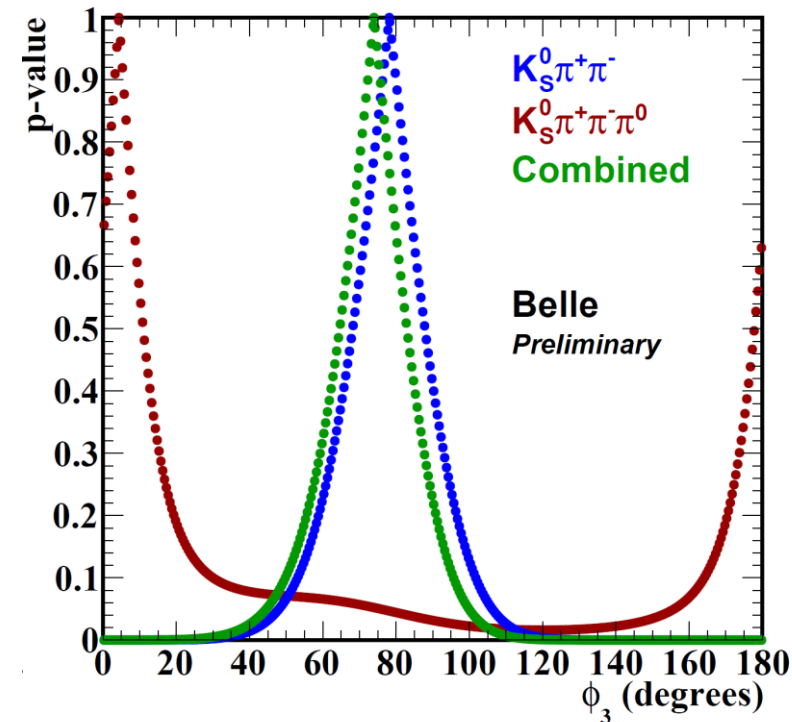
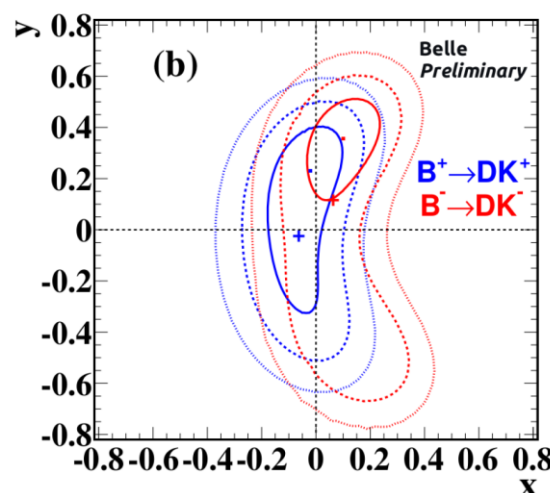
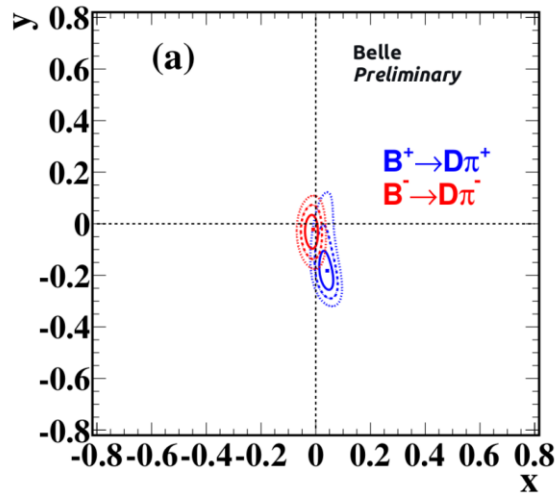
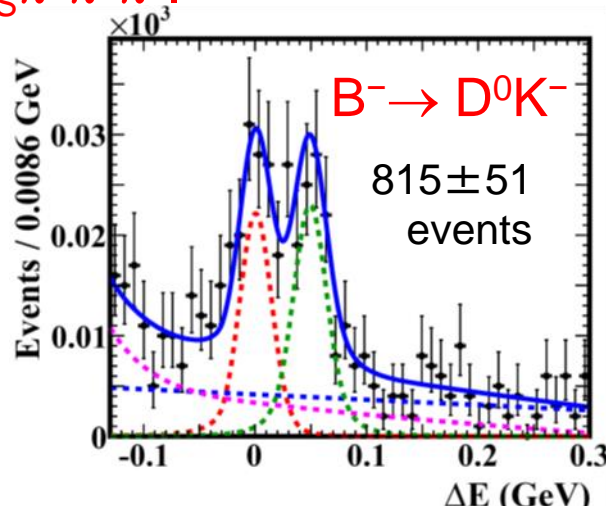
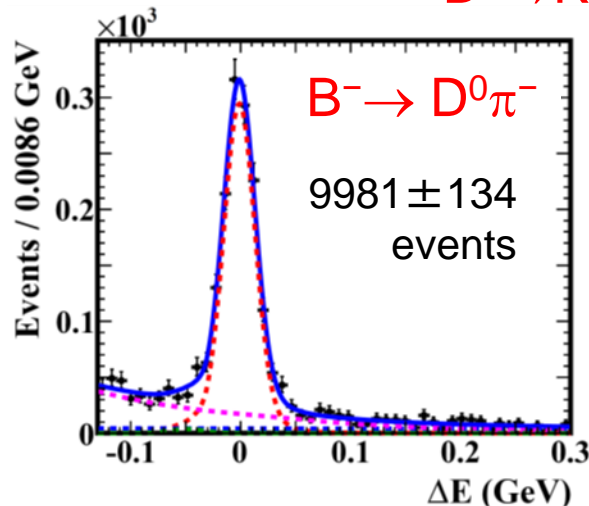
K_i and \bar{K}_i - fraction of flavour-tagged D events



Dalitz plot binning for $K_S^0 \pi^+ \pi^-$.

PRD82, 112006(2010)

$D^0 \rightarrow K_S \pi^+ \pi^- \pi^0$



ϕ_3 from Belle

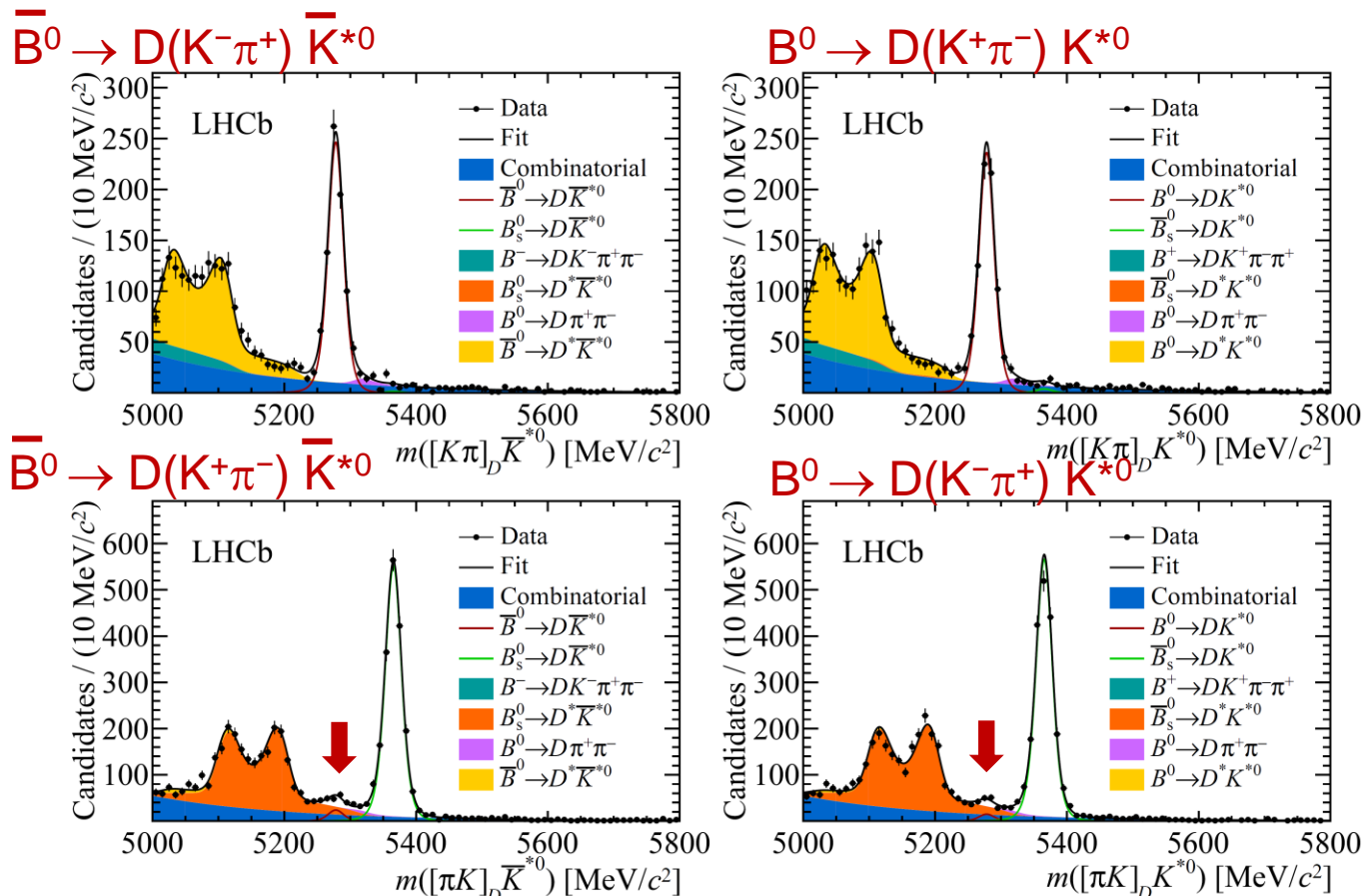
$$(78^{+14}_{-15})^\circ \Rightarrow (74^{+13}_{-14})^\circ$$

with this measurement

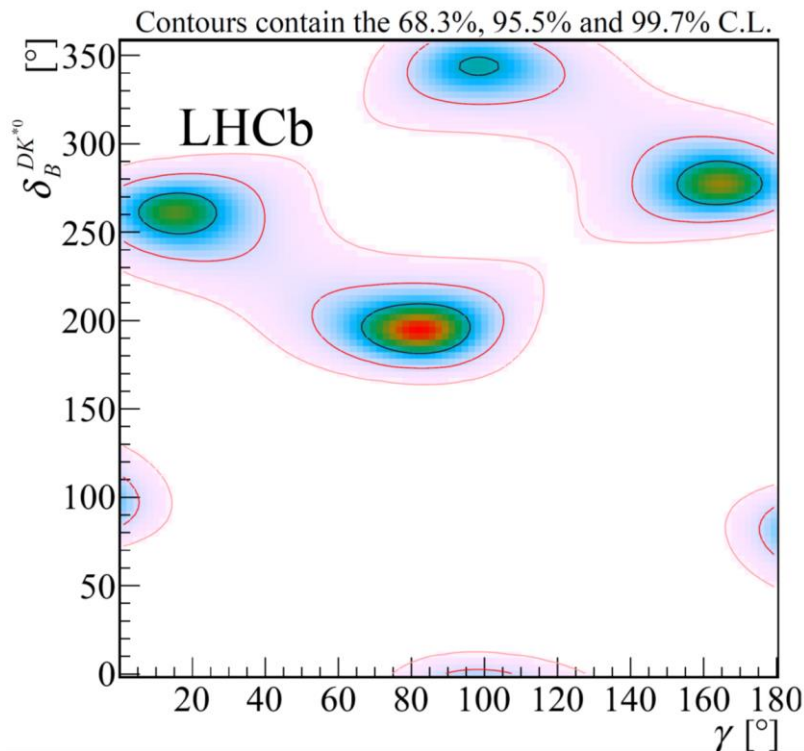
Promising at Belle II (estimation: 4.4° at 50 ab^{-1})

- Updated γ ($=\phi_3$) measurement by LHCb with ADS/GLW method.
- $B^0 \rightarrow DK^{*0}$ with $D \rightarrow K^+\pi^-, K^+K^-, \pi^+\pi^-, K^+\pi^-\pi^+\pi^-, \pi^+\pi^-\pi^+\pi^-$ (+c.c.).
- 4.8 fb^{-1} at 7, 8, 13 TeV (Run1+2)

[arXiv:1905.08297]

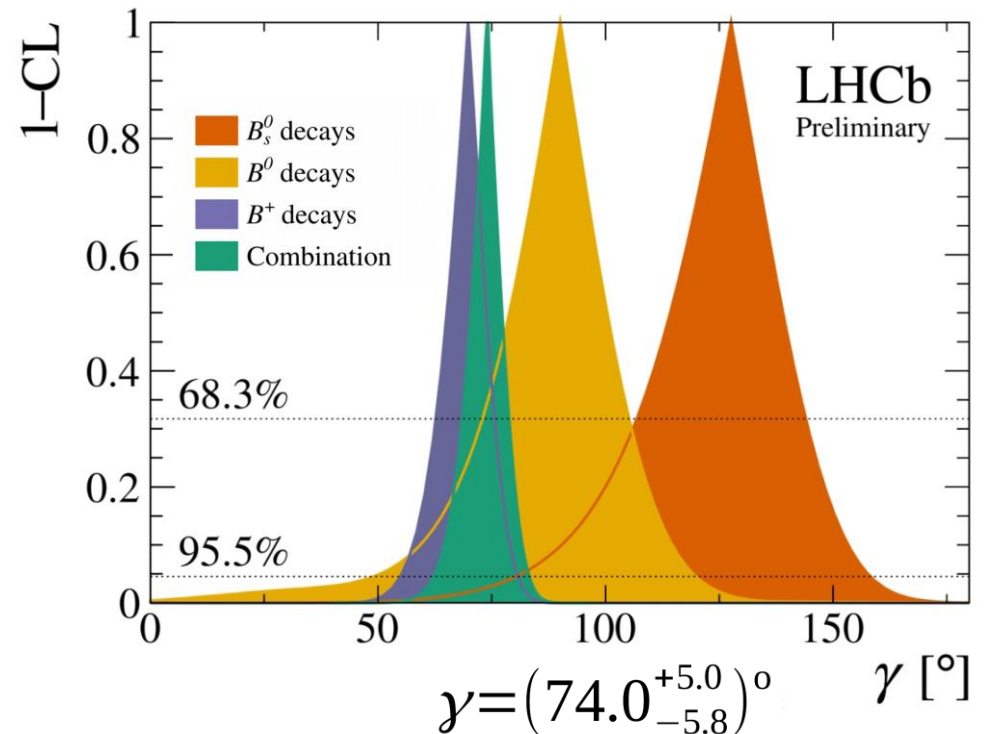


Contour from this result



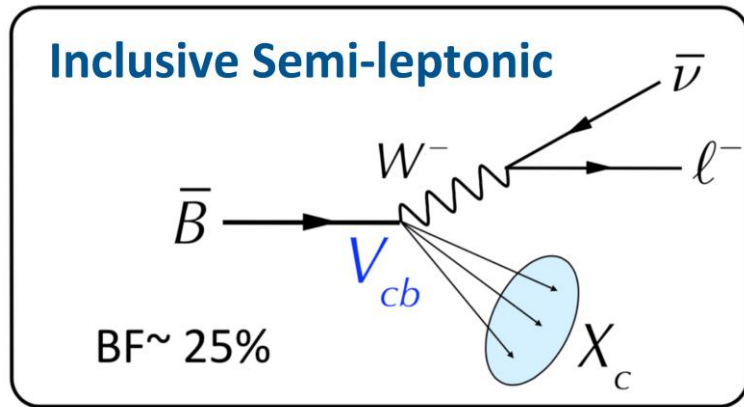
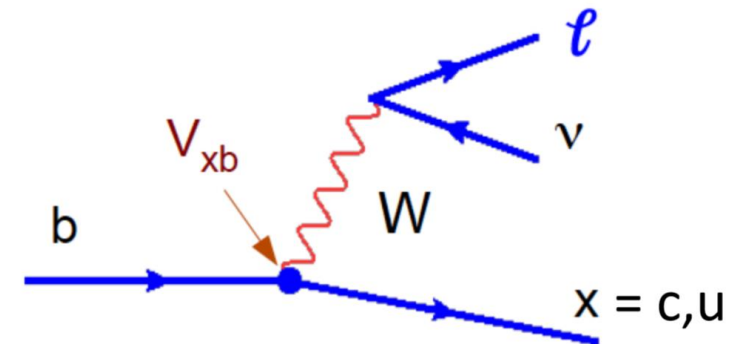
Expect to improve the error slightly.

LHCb 2018

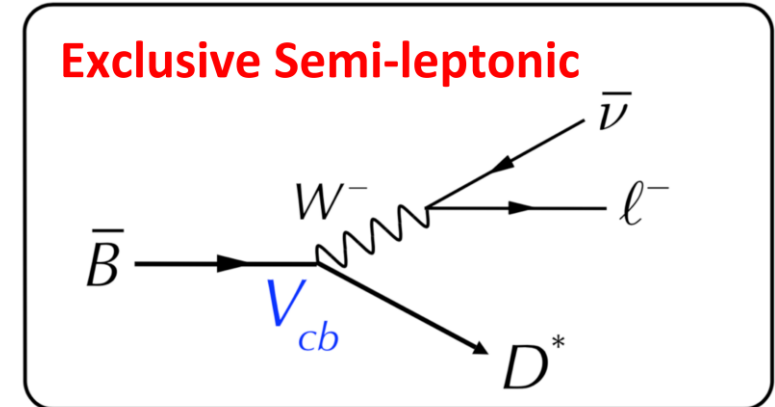


HFLAV	$(71.1^{+4.6}_{-5.3})^\circ$
CKM fit	$(65.8^{+1.0}_{-1.7})^\circ$

- $|V_{ub}|$ and $|V_{cb}|$ can be measured using semi-leptonic decays $b \rightarrow u\ell\nu$, $c\ell\nu$.
- Two approaches: **inclusive** and **exclusive**



do not specify hadron state

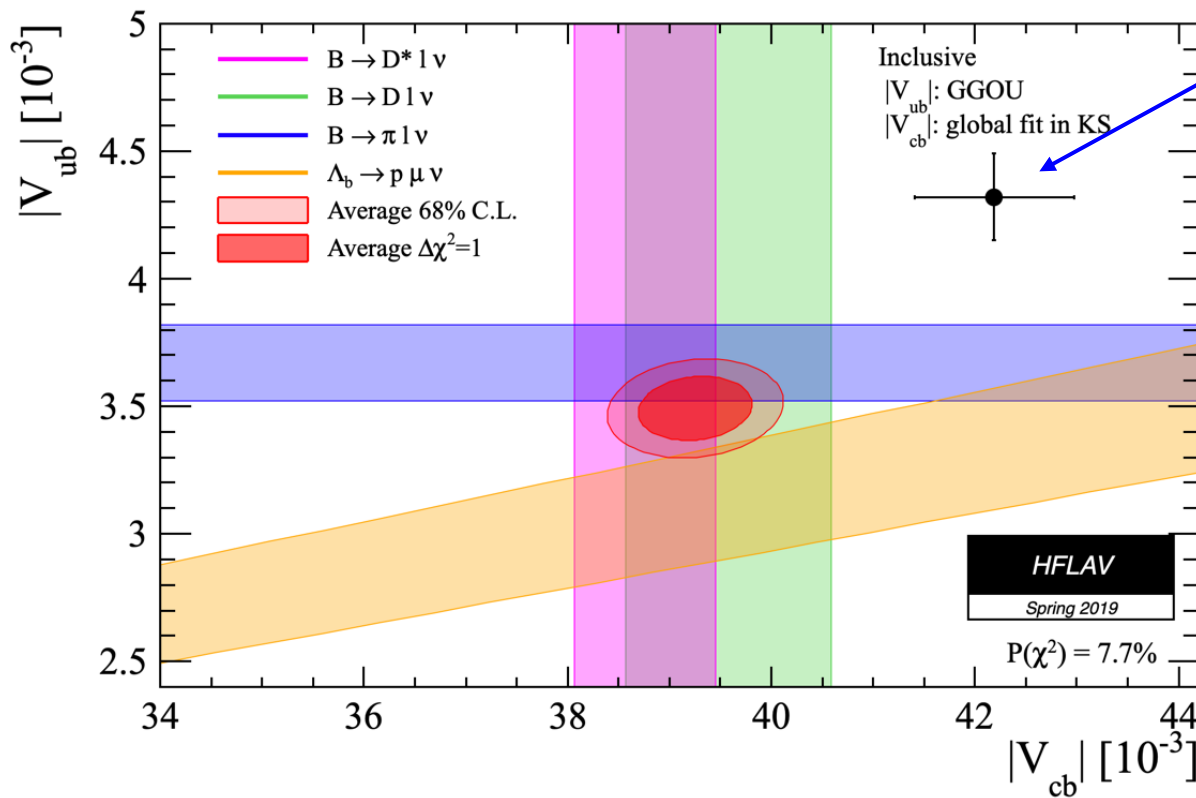


specify hadrons (experimentally clean)

- QCD corrections to parton level decay rate
- Operator Product Expansion (OPE) in α_s and Λ/m_b
- QCD contributions parametrized in form factors
- Lattice QCD (high q^2) or LCSR (low q^2)

Tension between inclusive and exclusive

exclusive measurements (2019 spring)



average for inclusive

$$|V_{cb}| = (42.19 \pm 0.78) \times 10^{-3} \quad (\text{inclusive})$$

$$|V_{cb}| = (39.25 \pm 0.56) \times 10^{-3} \quad (\text{exclusive})$$

$$|V_{ub}| = (4.32 \pm 0.17) \times 10^{-3} \quad (\text{inclusive})$$

$$|V_{ub}| = (3.49 \pm 0.13) \times 10^{-3} \quad (\text{exclusive})$$

- New result of untagged analysis of $B \rightarrow D^* \ell \nu$ by Belle.
- Simultaneous fit to $\cos\theta_\ell$, $\cos\theta_\nu$, χ , w (hadronic recoil) to extract form factors and $F(1) |V_{cb}|$.
- Two form factor parametrization, CLN [NPB530, 153 (1998)] and BGL [PRL74, 463 (1995)] are used.
 - ✓ CLN was mainly used in previous measurements.

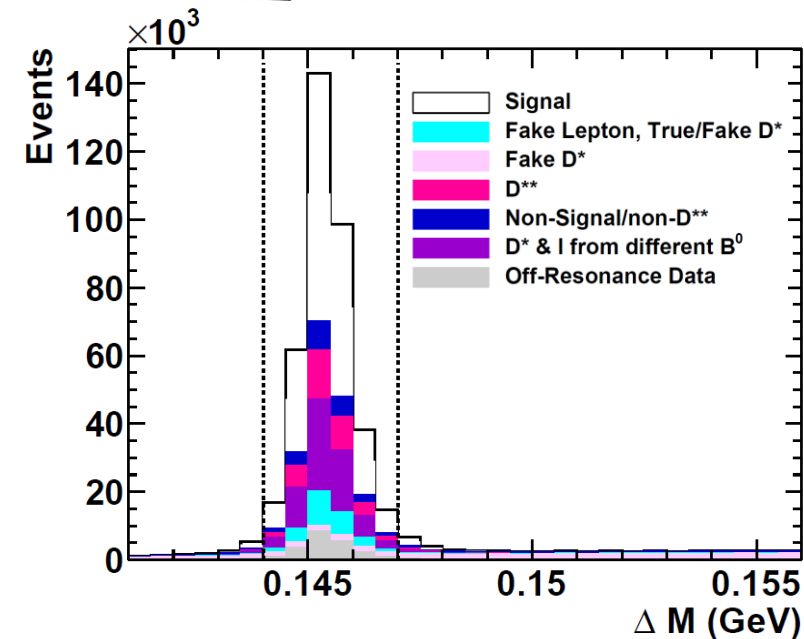
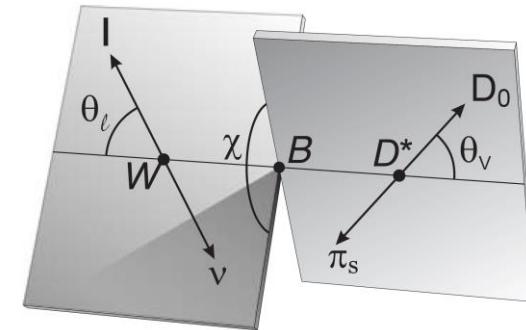
$$N(B \rightarrow D^* e \nu) = 90738$$

$$N(B \rightarrow D^* \mu \nu) = 89082$$

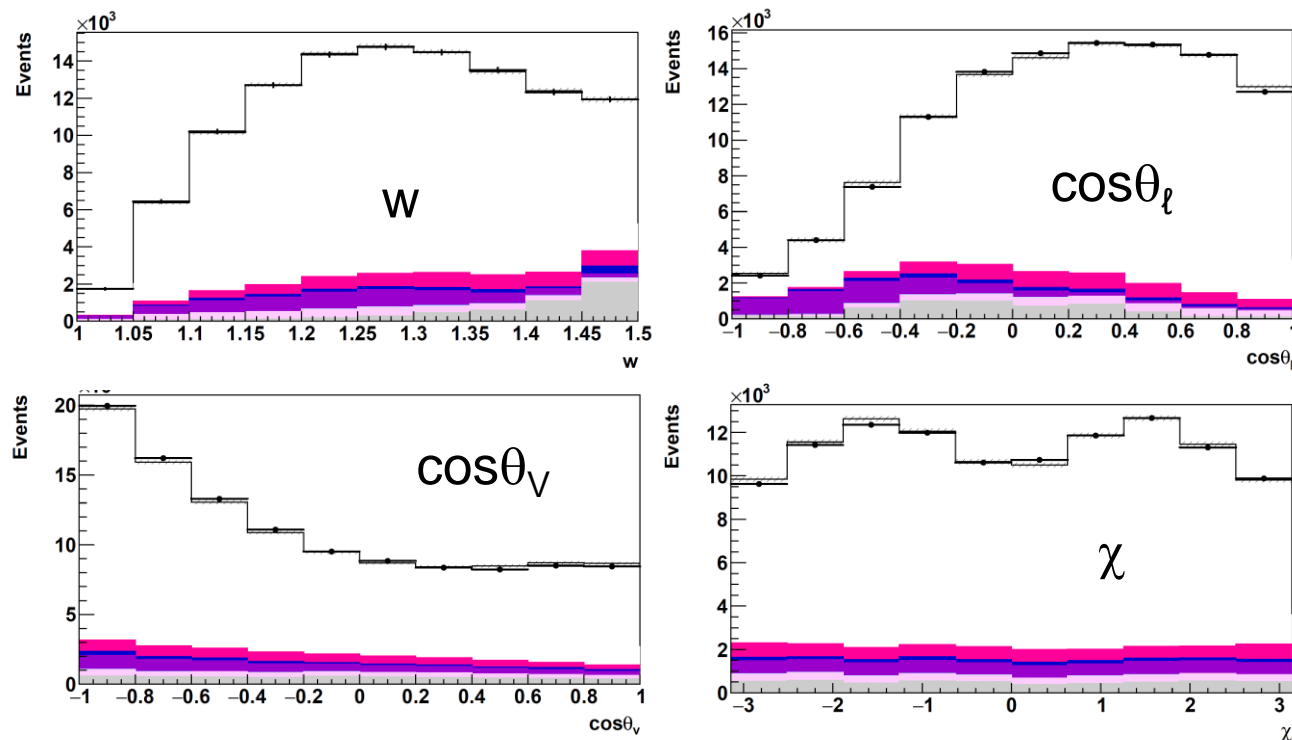
Bonus: Lepton Flavor Universality test

$$\frac{\mathcal{B}(B^0 \rightarrow D^{*-} e^+ \nu)}{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu)} = 1.01 \pm 0.01 \pm 0.03$$

[arXiv:1809.03290
to appear in PRD]



Fit for BGL parametrizations for $B \rightarrow D^* \mu \nu$



world average

$$|V_{cb}| = (42.19 \pm 0.78) \times 10^{-3} \quad (\text{inclusive})$$

$$|V_{cb}| = (39.25 \pm 0.56) \times 10^{-3} \quad (\text{exclusive})$$

(including this result)

In the preliminary result, the tension seemed to be solved by BGL parametrization, but actually not.

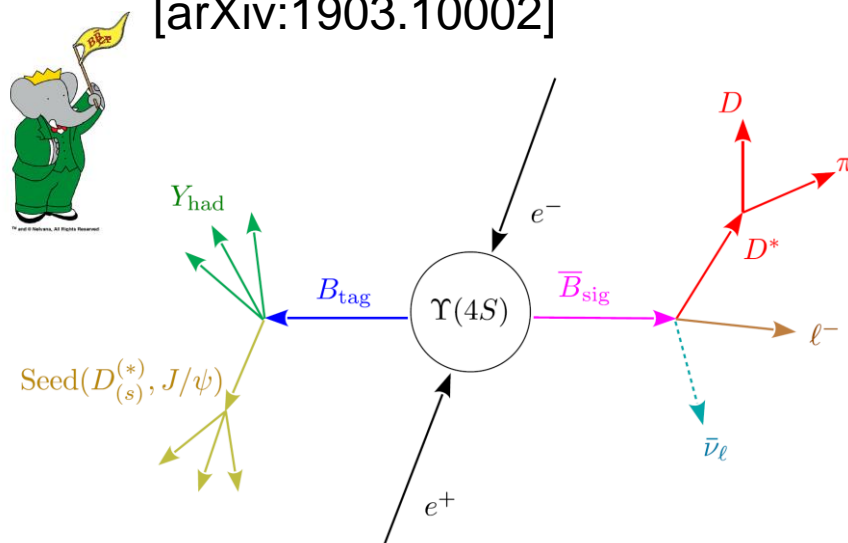
Tension still persists.

$$\text{CLN: } |V_{cb}| = (38.4 \pm 0.2 \pm 0.6 \pm 0.6) \times 10^{-3}$$

$$\text{BGL: } |V_{cb}| = (38.3 \pm 0.3 \pm 0.7 \pm 0.6) \times 10^{-3}$$

- BaBar performed **full 4-d analysis** using 426 fb⁻¹ data set.
- Hadronic B_{tag} reconstruction with 2968 modes (more modes than before for higher efficiency).

[arXiv:1903.10002]



	$ V_{cb} \times 10^3$
BGL	38.36 ± 0.90
CLN	38.40 ± 0.84

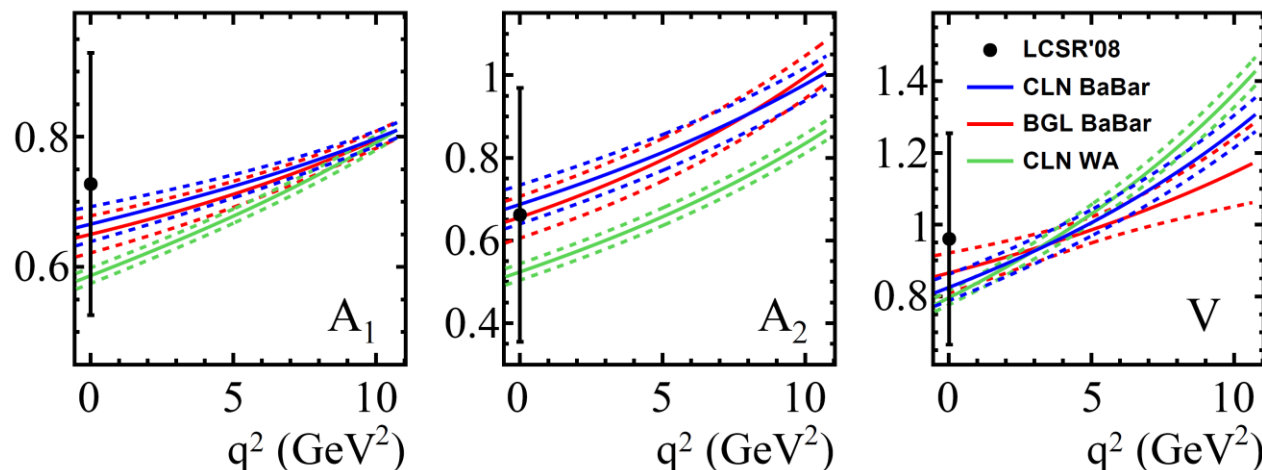
Tension still persists.

world average

$$|V_{cb}| = (42.19 \pm 0.78) \times 10^{-3} \quad (\text{inclusive})$$

$$|V_{cb}| = (39.25 \pm 0.56) \times 10^{-3} \quad (\text{exclusive})$$

Form Factor



- Large local CP asymmetry in the phase space was found by LHCb and Belle in the decay $B^+ \rightarrow \pi^+ K^+ K^-$.

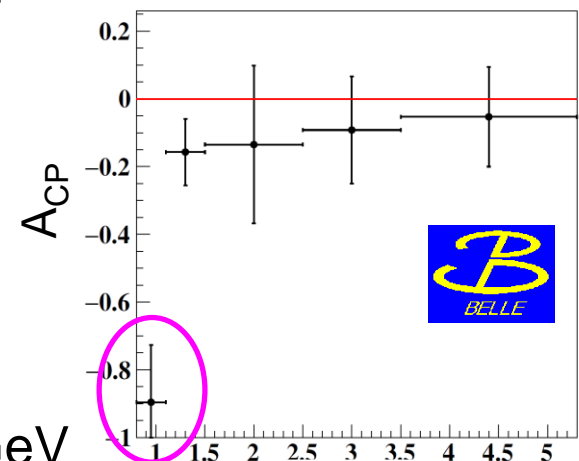
✓ $A_{CP} = -0.123 \pm 0.017 \pm 0.012 \pm 0.007$ (LHCb)

[PRD90, 112004 (2014)]

- Amplitude analysis of $B^+ \rightarrow \pi^+ K^+ K^-$ and $B^+ \rightarrow \pi^+ \pi^- \pi^+$ by LHCb.

[Parallel Talk by C.Santamarina on Thursday]

[PRD96, 031101(R) (2017)]



Mass distributions for B^- and B^+ at $1.0 < M(KK/\pi\pi) < 1.5$ GeV

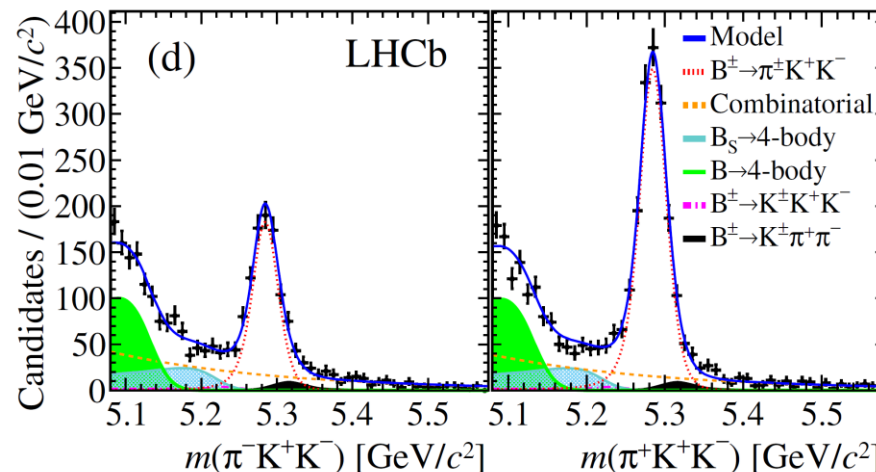
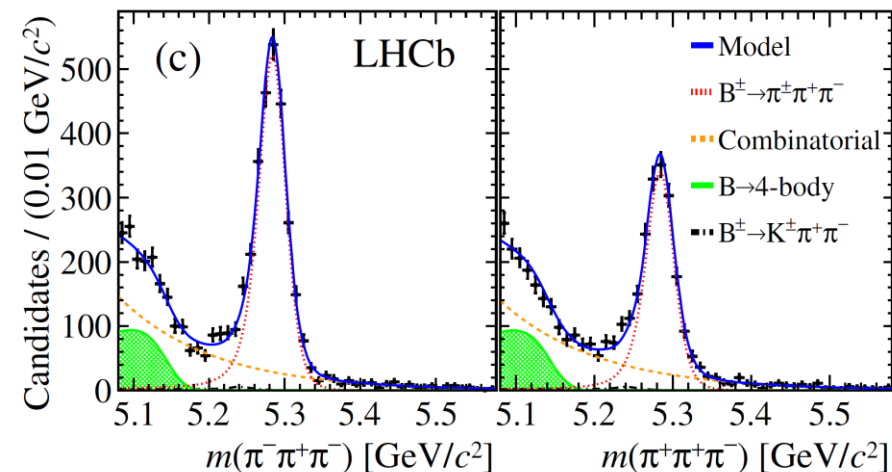
$B^- \rightarrow \pi^- \pi^- \pi^+$

$B^+ \rightarrow \pi^+ \pi^- \pi^+$

$B^- \rightarrow \pi^- K^+ K^-$

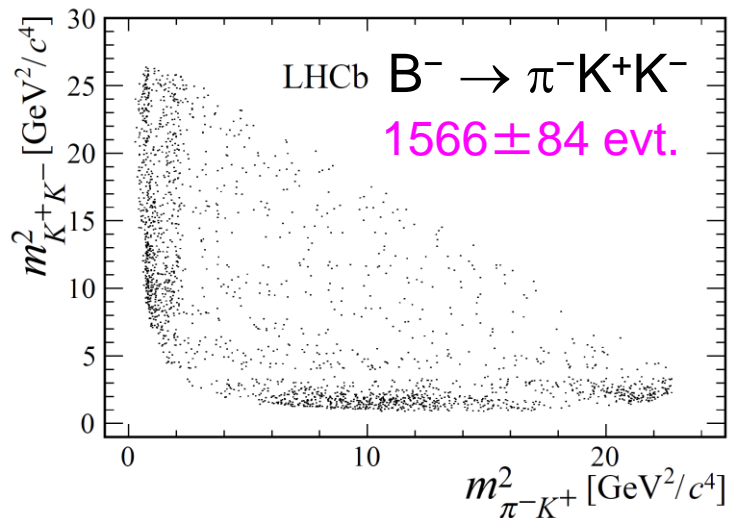
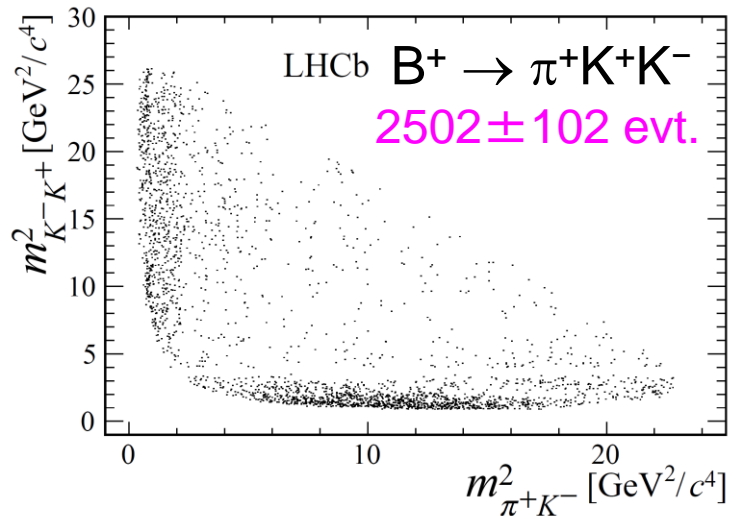
$B^+ \rightarrow \pi^+ K^+ K^-$

$M(KK)$



3.0 fb⁻¹ at Run 1

[arXiv:1905.09244]



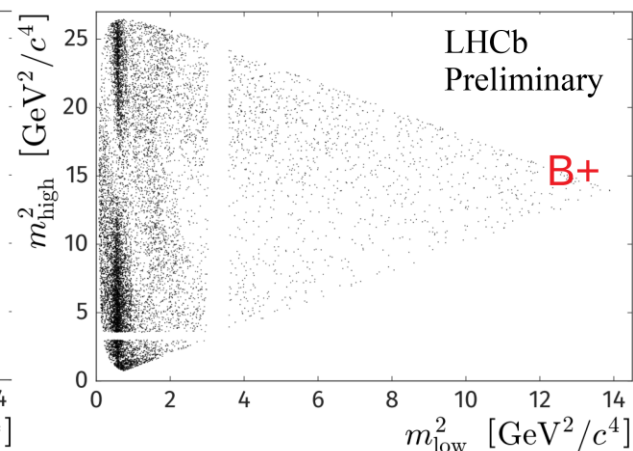
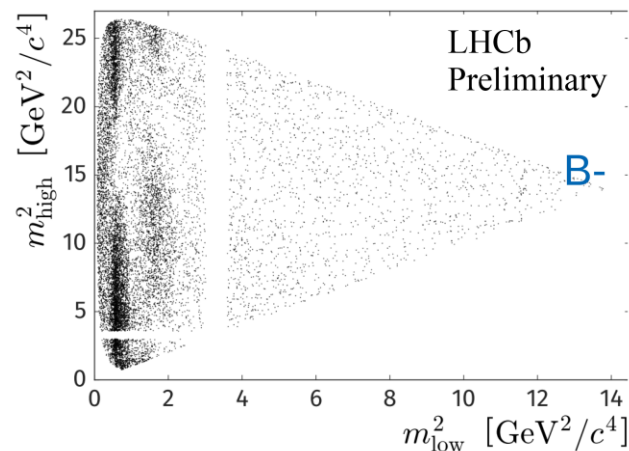
Contribution	Fit Fraction(%)	$A_{CP}(\%)$		
$K^*(892)^0$	$7.5 \pm 0.6 \pm 0.5$	$+12.3 \pm 8.7 \pm 4.5$		
$K_0^*(1430)^0$	$4.5 \pm 0.7 \pm 1.2$	$+10.4 \pm 14.9 \pm 8.8$		
Single pole	$32.3 \pm 1.5 \pm 4.1$	$-10.7 \pm 5.3 \pm 3.5$		
$\rho(1450)^0$	$30.7 \pm 1.2 \pm 0.9$	$-10.9 \pm 4.4 \pm 2.4$		
$f_2(1270)$	$7.5 \pm 0.8 \pm 0.7$	$+26.7 \pm 10.2 \pm 4.8$		
Rescattering	$16.4 \pm 0.8 \pm 1.0$	$-66.4 \pm 3.8 \pm 1.9$		
$\phi(1020)$	$0.3 \pm 0.1 \pm 0.1$	$+9.8 \pm 43.6 \pm 26.6$		

- Fit to 5 resonances + non-resonant + $\pi\pi \leftrightarrow KK$ rescattering.
- Large CP asymmetry comes from the rescattering component.
 - ✓ Can explain the previous result.

[Parallel Talk by C.Santamarina on Thursday]

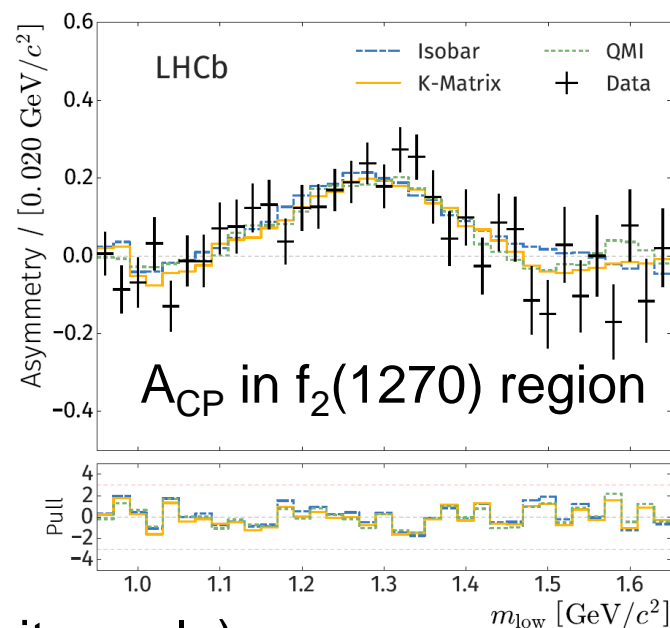
3.0 fb⁻¹ at 7-8 TeV (Run1)

[LHCb-PAPER-2019-017, LHCb-PAPER-2019-018]



- Large CP asymmetries found in

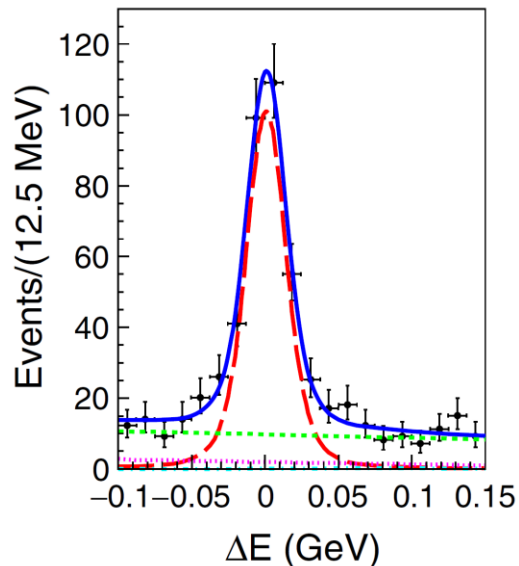
- ✓ $f_2(1270)$ component.
- ✓ $\rho(770)$ -scalar interference (in projection to helicity angle).
- ✓ S-wave components (with three approaches).



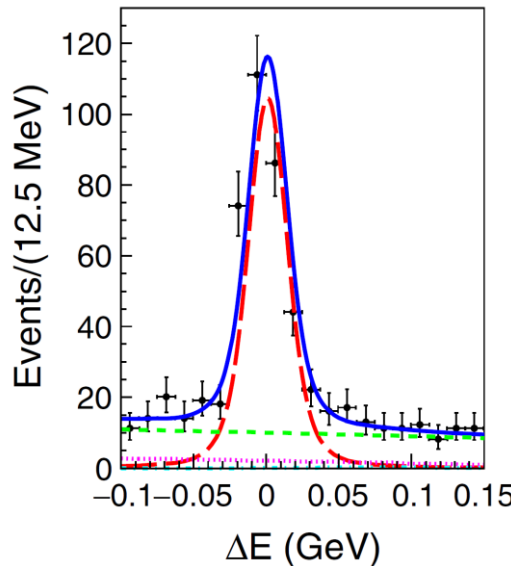
[Parallel Talk by C.Santamarina on Thursday]

More study can be done with LHCb Run2 data.

$B^+ \rightarrow K_S K_S K^+$



$B^- \rightarrow K_S K_S K^-$



[PRD99 (2019) 031102]



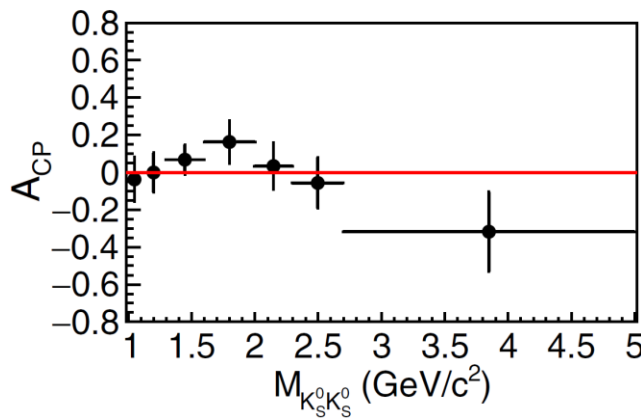
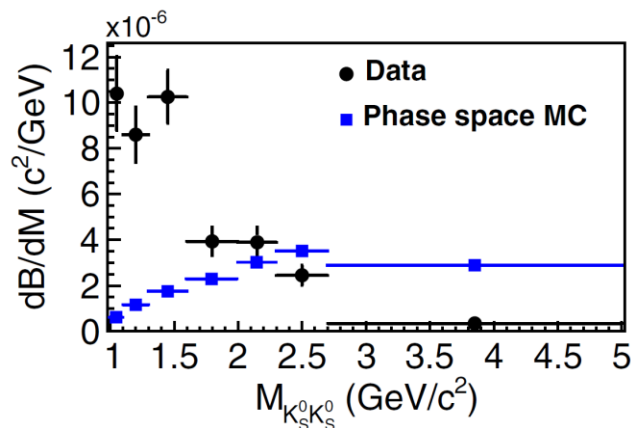
Belle 711 fb⁻¹

Not an amplitude analysis

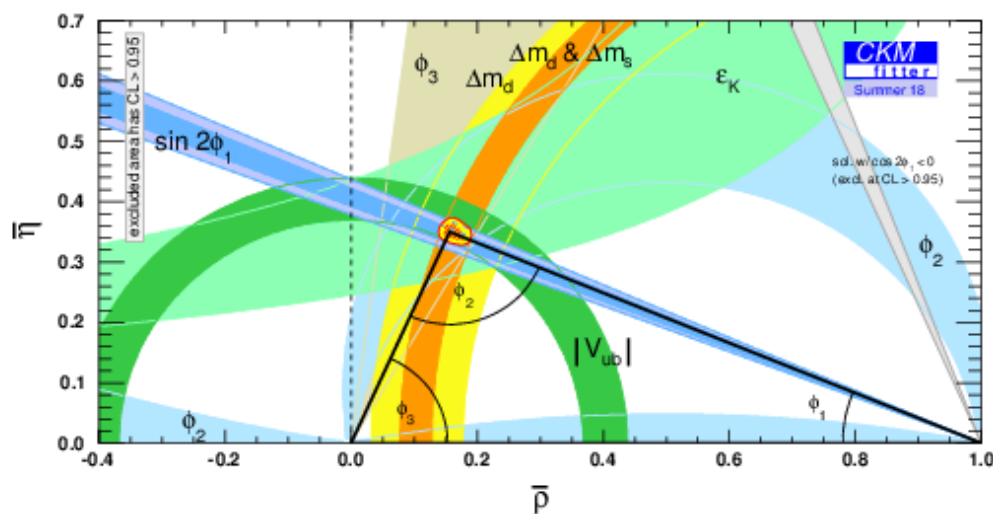
$$B(B^+ \rightarrow K_S K_S K^+) = (6.5 \pm 2.6 \pm 0.4) \times 10^{-7}$$

$$A_{CP}(B^+ \rightarrow K_S K_S K^+) = (+1.6 \pm 3.9 \pm 0.9)\%$$

$$B(B^+ \rightarrow K_S K_S \pi^+) < 8.7 \times 10^{-7}$$

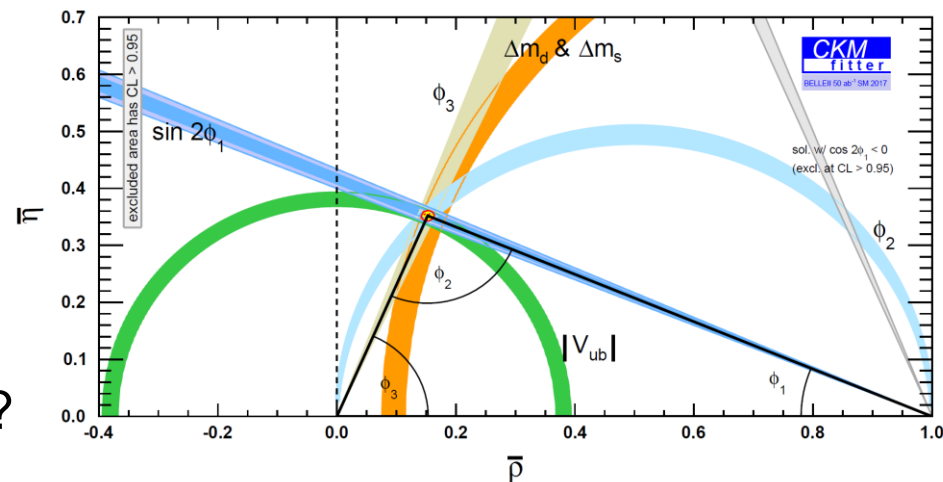


- Updates on ϕ_3 / γ , $|V_{cb}|$, ϕ_s .
- CP Asymmetry in $B^+ \rightarrow \pi^+ K^+ K^-$, $\pi^+ \pi^- \pi^+$.

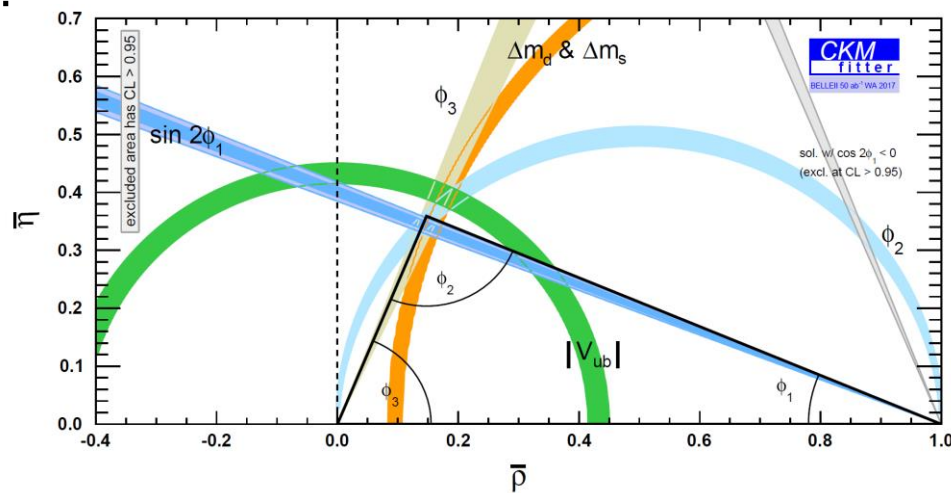


- More results from LHCb are expected.
- Belle II started, will join the game.

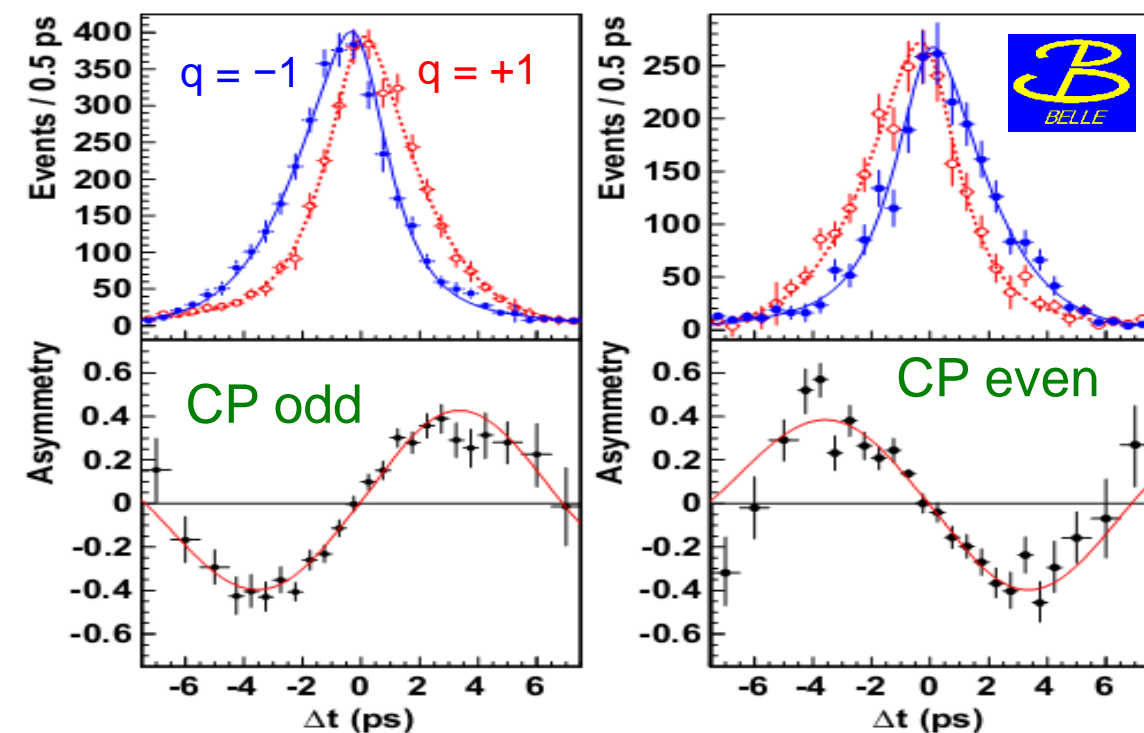
[Talk by T.Browder on Monday]



Belle II 50 ab^{-1} [arXiv:1808.10567]

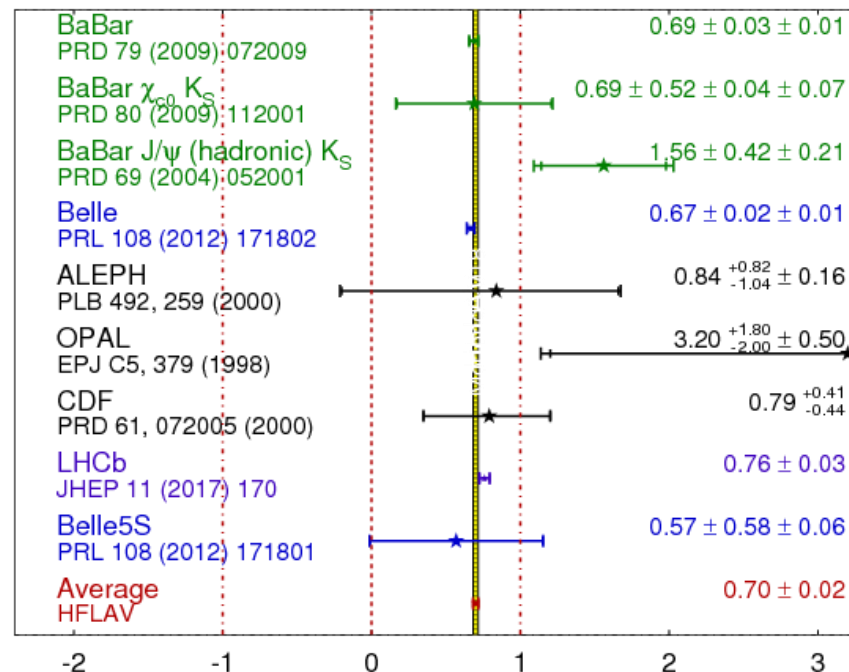


Backup



$$\sin(2\beta) \equiv \sin(2\phi_1)$$

HFLAV
Moriond 2018
PRELIMINARY



$$\sin(2\phi_1) = 0.667 \pm 0.023 \pm 0.012$$

$$A = 0.006 \pm 0.016 \pm 0.012$$

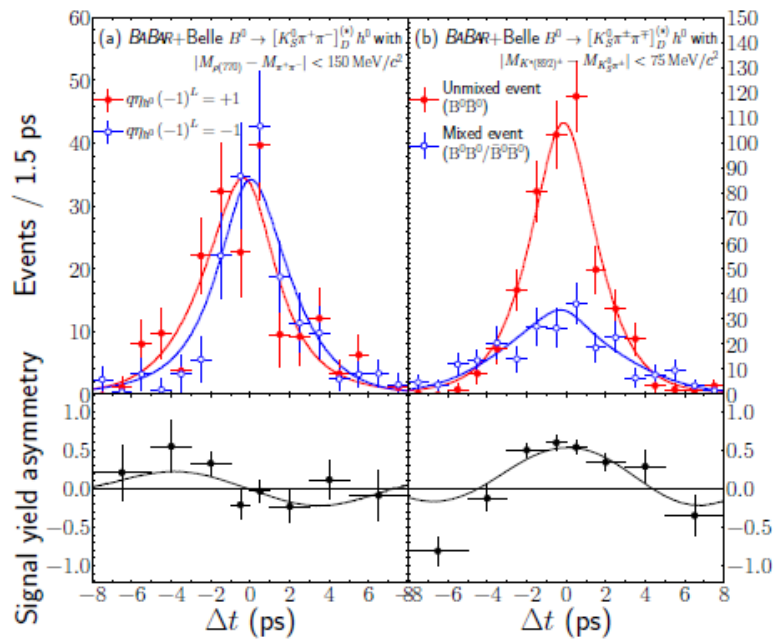
[PRL 108, 171802 (2012)]



- sin2β is precisely measured, but trigonometric ambiguity exists for β.
- Time-dependent Dalitz analysis of B → D(*)h⁰, D → K_Sπ⁺π⁻ (h = π⁰, η, ω) can resolve it.
- Joint Babar + Belle analysis. ✓ 471 + 772 M BB

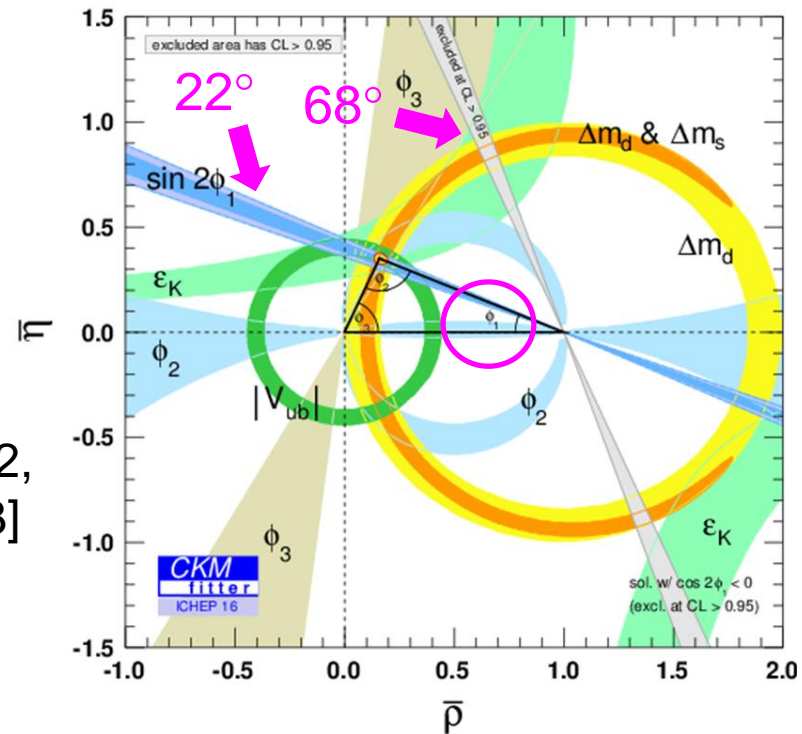


BABAR



(two different region in Dalitz plane)

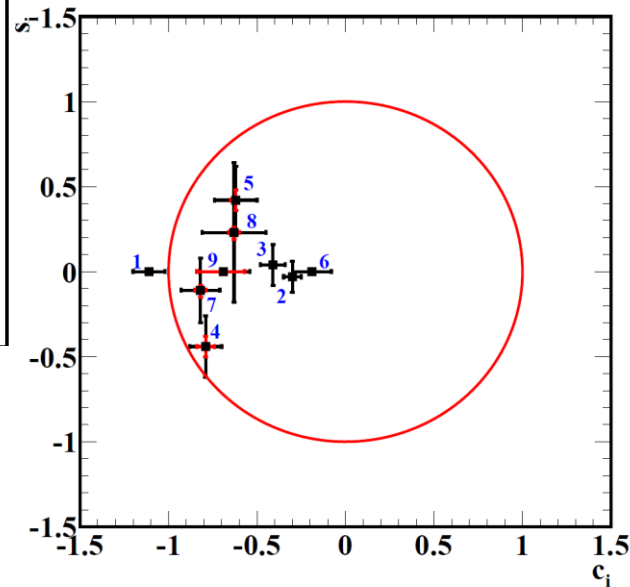
[arXiv:1804.06152,
arXiv:1804.06153]



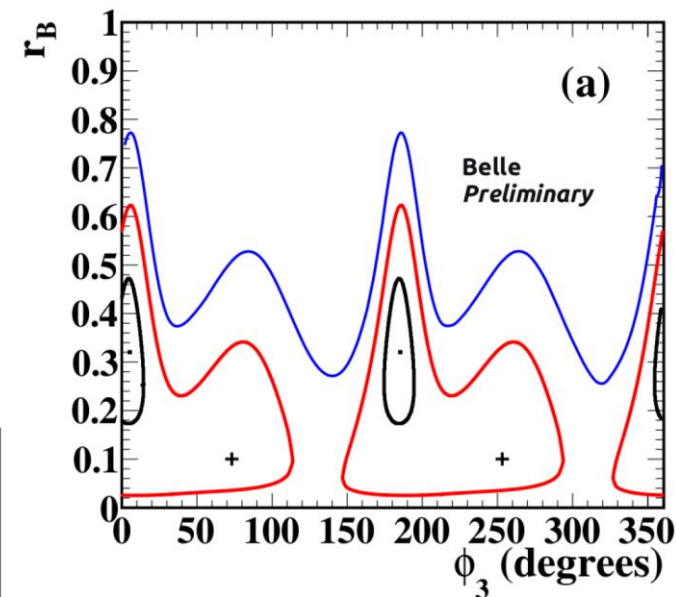
$$\begin{aligned}\sin(2\beta) &= 0.80 \pm 0.14 \text{ (stat.)} \pm 0.06 \text{ (syst.)} \pm 0.03 \text{ (model)} \\ \cos(2\beta) &= 0.91 \pm 0.22 \text{ (stat.)} \pm 0.09 \text{ (syst.)} \pm 0.07 \text{ (model)} \\ \beta &= (22.5 \pm 4.4 \text{ (stat.)} \pm 1.2 \text{ (syst.)} \pm 0.6 \text{ (model)})^\circ\end{aligned}$$

- First evidence of cos2β > 0.

Bin	Bin region
1	$m(\pi^+ \pi^- \pi^0) \approx m(\omega)$
2	$m(K_S^0 \pi^-) \approx m(K^{*-})$ & $m(\pi^+ \pi^0) \approx m(\rho^+)$
3	$m(K_S^0 \pi^+) \approx m(K^{*+})$ & $m(\pi^- \pi^0) \approx m(\rho^-)$
4	$m(K_S^0 \pi^-) \approx m(K^{*-})$
5	$m(K_S^0 \pi^+) \approx m(K^{*+})$
6	$m(K_S^0 \pi^0) \approx m(K^{*0})$
7	$m(\pi^+ \pi^0) \approx m(\rho^+)$
8	$m(\pi^- \pi^0) \approx m(\rho^-)$
9	Remainder



c_i and s_i results in 9 bins using CLEO-c data



Systematic Uncertainties

	ϕ_s [rad]	$\Delta\Gamma_s$ [ps ⁻¹]	Γ_s [ps ⁻¹]	$ A_{ }(0) ^2$	$ A_0(0) ^2$	$ A_S(0) ^2$	δ_{\perp} [rad]	$\delta_{ }$ [rad]	$\delta_{\perp} - \delta_S$ [rad]
Tagging	1.7×10^{-2}	0.4×10^{-3}	0.3×10^{-3}	0.2×10^{-3}	0.2×10^{-3}	2.3×10^{-3}	1.9×10^{-2}	2.2×10^{-2}	2.2×10^{-3}
Acceptance	0.7×10^{-3}	$< 10^{-4}$	$< 10^{-4}$	0.8×10^{-3}	0.7×10^{-3}	2.4×10^{-3}	3.3×10^{-2}	1.4×10^{-2}	2.6×10^{-3}
ID alignment	0.7×10^{-3}	0.1×10^{-3}	0.5×10^{-3}	$< 10^{-4}$	$< 10^{-4}$	$< 10^{-4}$	1.0×10^{-2}	7.2×10^{-3}	$< 10^{-4}$
S-wave phase	0.2×10^{-3}	$< 10^{-4}$	$< 10^{-4}$	0.3×10^{-3}	$< 10^{-4}$	0.3×10^{-3}	1.1×10^{-2}	2.1×10^{-2}	8.3×10^{-3}
Background angles model:									
Choice of fit function	1.8×10^{-3}	0.8×10^{-3}	$< 10^{-4}$	1.4×10^{-3}	0.7×10^{-3}	0.2×10^{-3}	8.5×10^{-2}	1.9×10^{-1}	1.8×10^{-3}
Choice of p_T bins	1.3×10^{-3}	0.5×10^{-3}	$< 10^{-4}$	0.4×10^{-3}	0.5×10^{-3}	1.2×10^{-3}	1.5×10^{-3}	7.2×10^{-3}	1.0×10^{-3}
Choice of mass interval	0.4×10^{-3}	0.1×10^{-3}	0.1×10^{-3}	0.3×10^{-3}	0.3×10^{-3}	1.3×10^{-3}	4.4×10^{-3}	7.4×10^{-3}	2.3×10^{-3}
Dedicated backgrounds:									
B_d^0	2.3×10^{-3}	1.1×10^{-3}	$< 10^{-4}$	0.2×10^{-3}	3.1×10^{-3}	1.4×10^{-3}	1.0×10^{-2}	2.3×10^{-2}	2.1×10^{-3}
Λ_b	1.6×10^{-3}	0.4×10^{-3}	0.2×10^{-3}	0.5×10^{-3}	1.2×10^{-3}	1.8×10^{-3}	1.4×10^{-2}	2.9×10^{-2}	0.8×10^{-3}
Fit model:									
Time res. sig frac	1.4×10^{-3}	1.1×10^{-3}	$< 10^{-4}$	0.5×10^{-3}	0.6×10^{-3}	0.6×10^{-3}	1.2×10^{-2}	3.0×10^{-2}	0.4×10^{-3}
Time res. p_T bins	3.3×10^{-3}	1.4×10^{-3}	0.1×10^{-2}	$< 10^{-4}$	$< 10^{-4}$	0.5×10^{-3}	6.2×10^{-3}	5.2×10^{-3}	1.1×10^{-3}
Total	1.8×10^{-2}	0.2×10^{-2}	0.1×10^{-2}	0.2×10^{-2}	0.4×10^{-2}	0.4×10^{-2}	9.7×10^{-2}	2.0×10^{-1}	0.1×10^{-1}

Uncertainty in the calibration of the B_s -tag probability; MC statistical uncertainty included in fit stat. error

Alternative detector acceptance fit-functions and binning determined from MC

Radial expansion uncertainties determined from their effect on tracks d_0 in the data

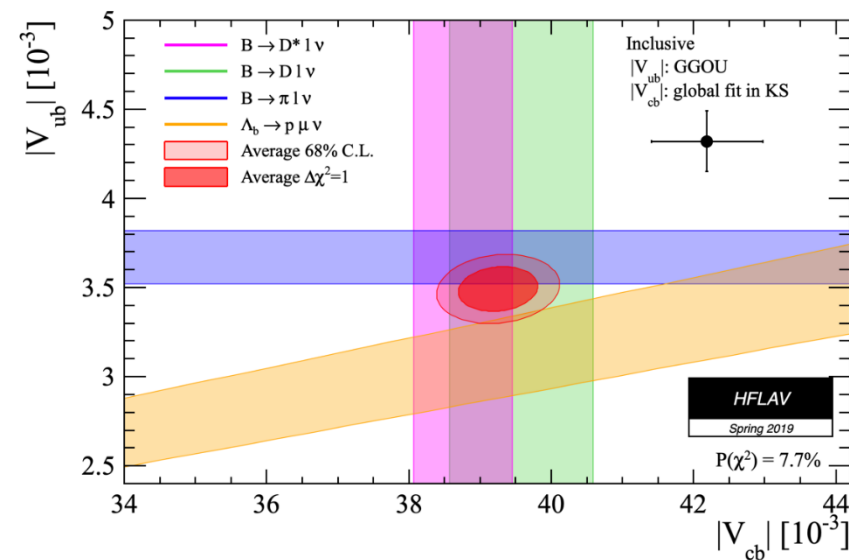
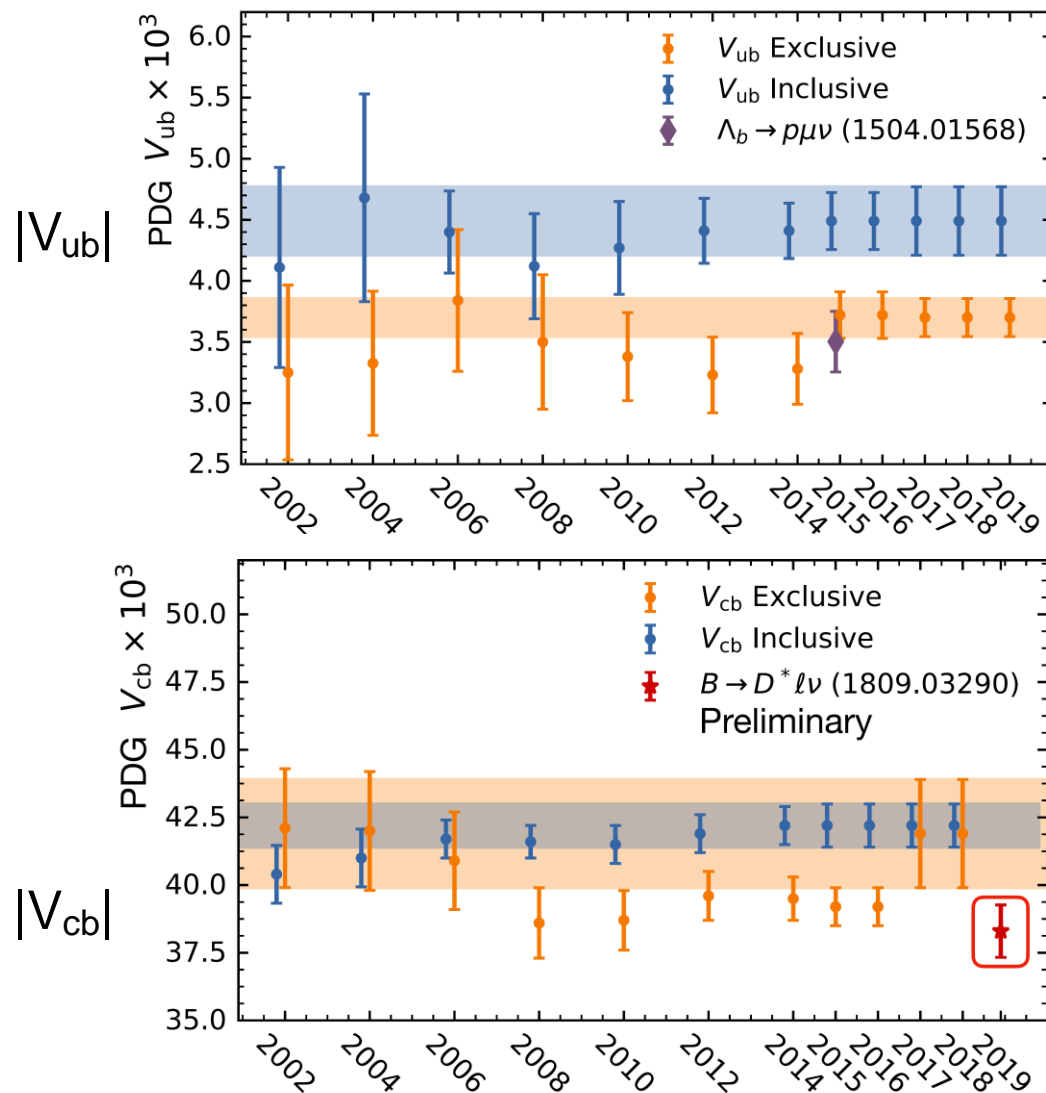
Background angles model (fixed in UML fit) extracted from data with varying sidebands size and binning

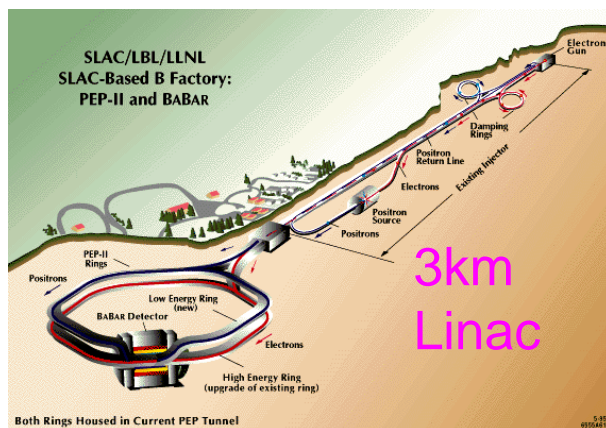
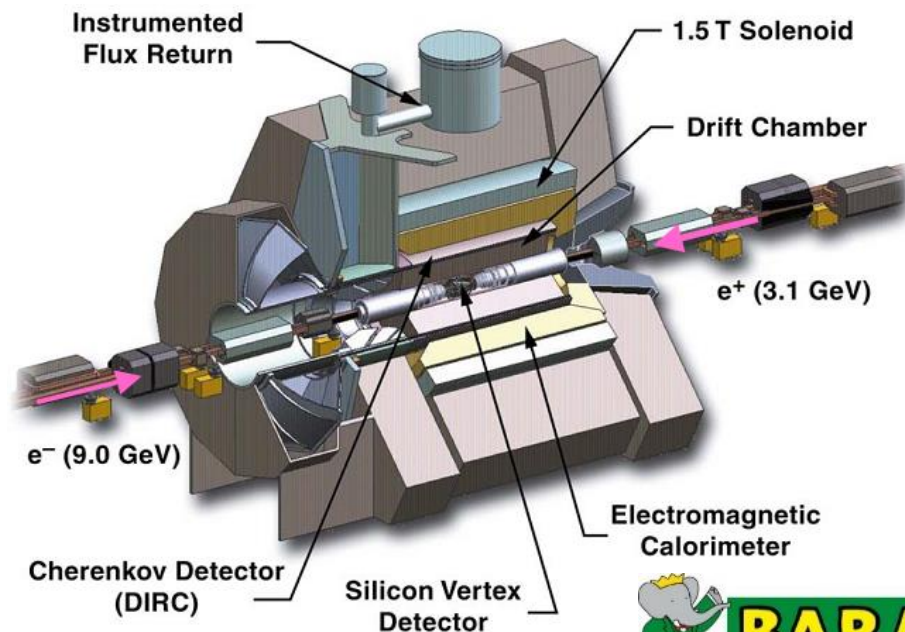
Uncertainties of relative fraction; fit-model and P-wave contribution

Uncertainties of relative fraction; fit-model and contributions from $\Lambda_b \rightarrow J/\psi \Lambda^*$ decays

Toy-MC studies; pulls of the default fit model, default fit on toy-data generated with modified PDFs

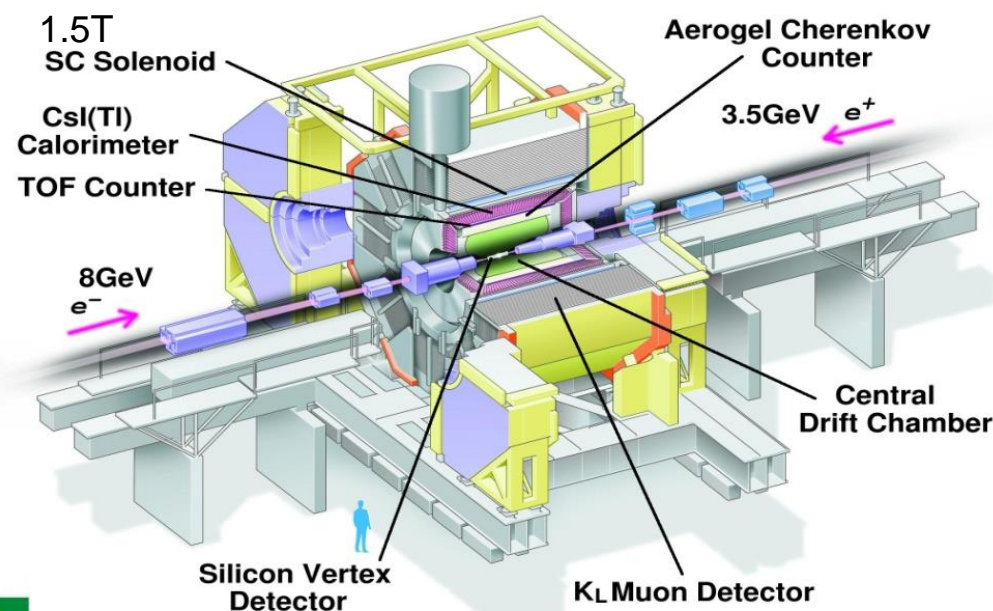
slides from A.B.





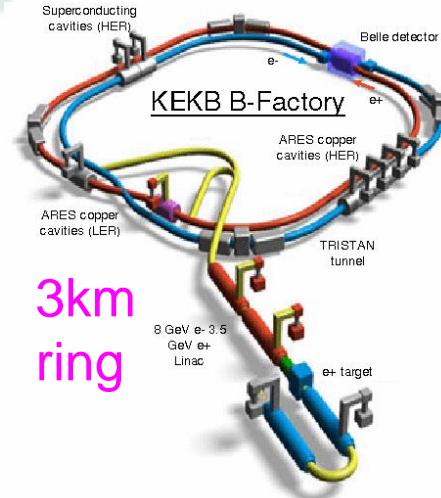
BaBar @ PEP-II

$9 \text{ GeV } e^- + 3.1 \text{ GeV } e^+$



Belle @ KEKB

$8 \text{ GeV } e^- + 3.5 \text{ GeV } e^+$



$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B} \quad (\sigma=1.1\text{nb})$$

$$1 \text{ fb}^{-1} \sim 10^6 B\bar{B} @ \Upsilon(4S)$$

$$\text{Total} \sim 1040 \text{ fb}^{-1}$$

$$\text{Peak} 2.11 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

On resonance:

$$\Upsilon(5S): 121 \text{ fb}^{-1}$$

$$\Upsilon(4S): 711 \text{ fb}^{-1}$$

$$\Upsilon(3S): 3 \text{ fb}^{-1}$$

$$\Upsilon(2S): 24 \text{ fb}^{-1}$$

$$\Upsilon(1S): 6 \text{ fb}^{-1}$$

B_s

Off resonance, scan:

$$\sim 100 \text{ fb}^{-1}$$

$$\text{Total} 550 \text{ fb}^{-1}$$

$$\text{Peak} 1.21 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

On resonance:

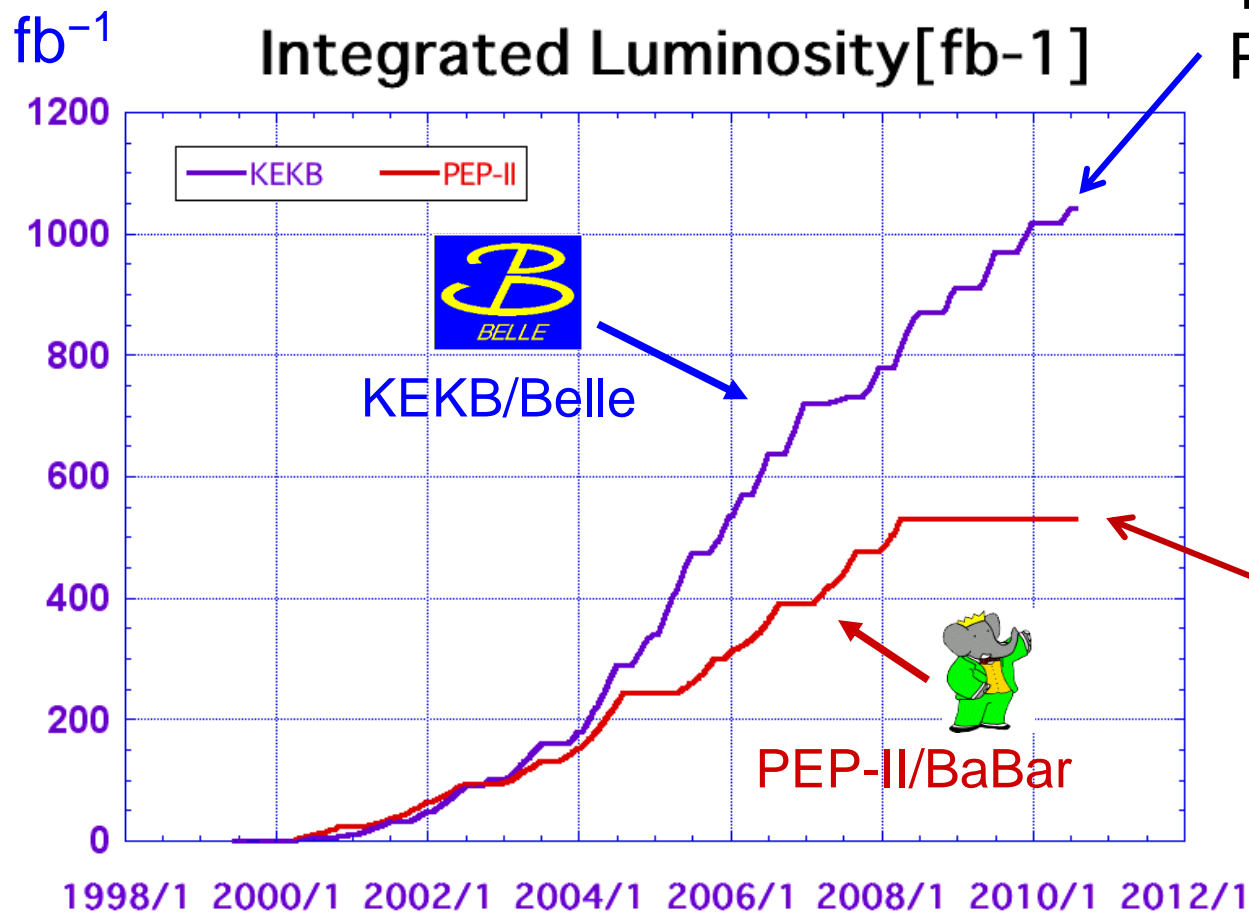
$$\Upsilon(4S): 433 \text{ fb}^{-1}$$

$$\Upsilon(3S): 30 \text{ fb}^{-1}$$

$$\Upsilon(2S): 14 \text{ fb}^{-1}$$

Off resonance:

$$\sim 54 \text{ fb}^{-1}$$



These data are taken till 2010.