

*SUSY 2018 Barcelona July 23-28*

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# Precision top & electroweak measurements.

Joe Boudreau  
University of Pittsburgh  
Results from ATLAS & CMS

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# Top quark precision measurements

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- ❖ Two processes:  $t\bar{t}$  and t-channel single top production
- ❖ Two interactions: strong (**g<sub>tt</sub> vertex**) and weak (**Wtb vertex**)
- ❖ Only one significant decay channel: W boson + b quark.
- ❖ Measurements constrain both the strength of these couplings and their structure.
- ❖ Two languages: EFT and anomalous couplings
$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} O_i + \mathcal{O}(\Lambda^{-4})$$
- ❖ Precision measurements are based on production cross sections and angular analyses of decay products.

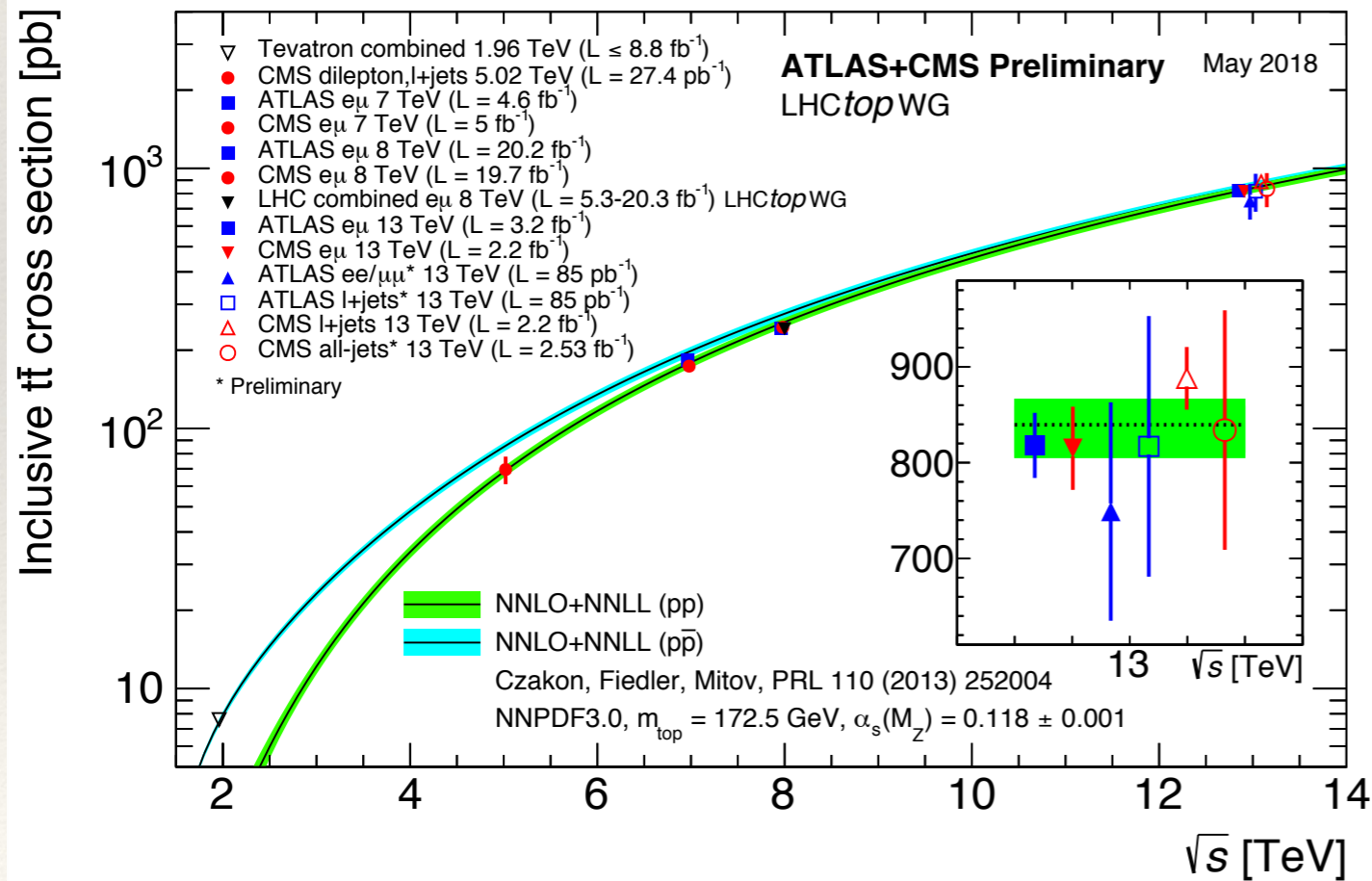
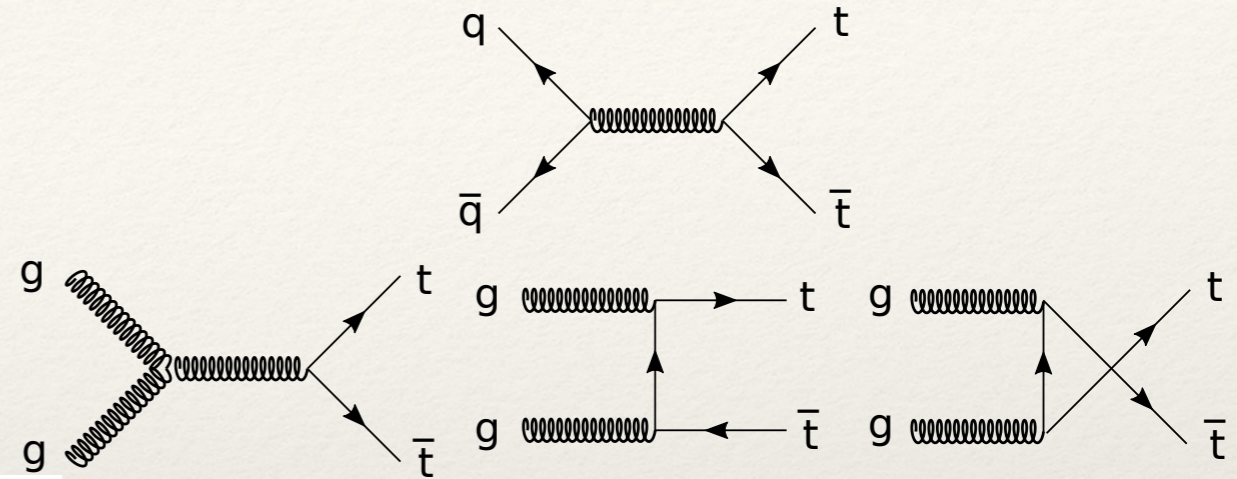


# $t\bar{t}$ cross section

Standard model production mechanisms  
for  $q\bar{q} \rightarrow t\bar{t}$  and  $gg \rightarrow t\bar{t}$ .

s-channel  $q\bar{q} \rightarrow t\bar{t}$

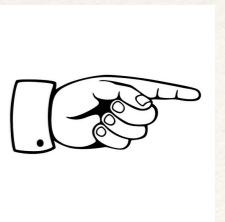
s, t, u-channel  $gg \rightarrow t\bar{t}$ .



Cyan:  $p\bar{p} \rightarrow t\bar{t}$  (Tevatron, 1.9 TeV)  
Green:  $pp \rightarrow t\bar{t}$  (LHC, 5, 7, 8, and 13 TeV)

All measurements in good agreement with SM predictions.

They can be interpreted in the framework of effective field theory





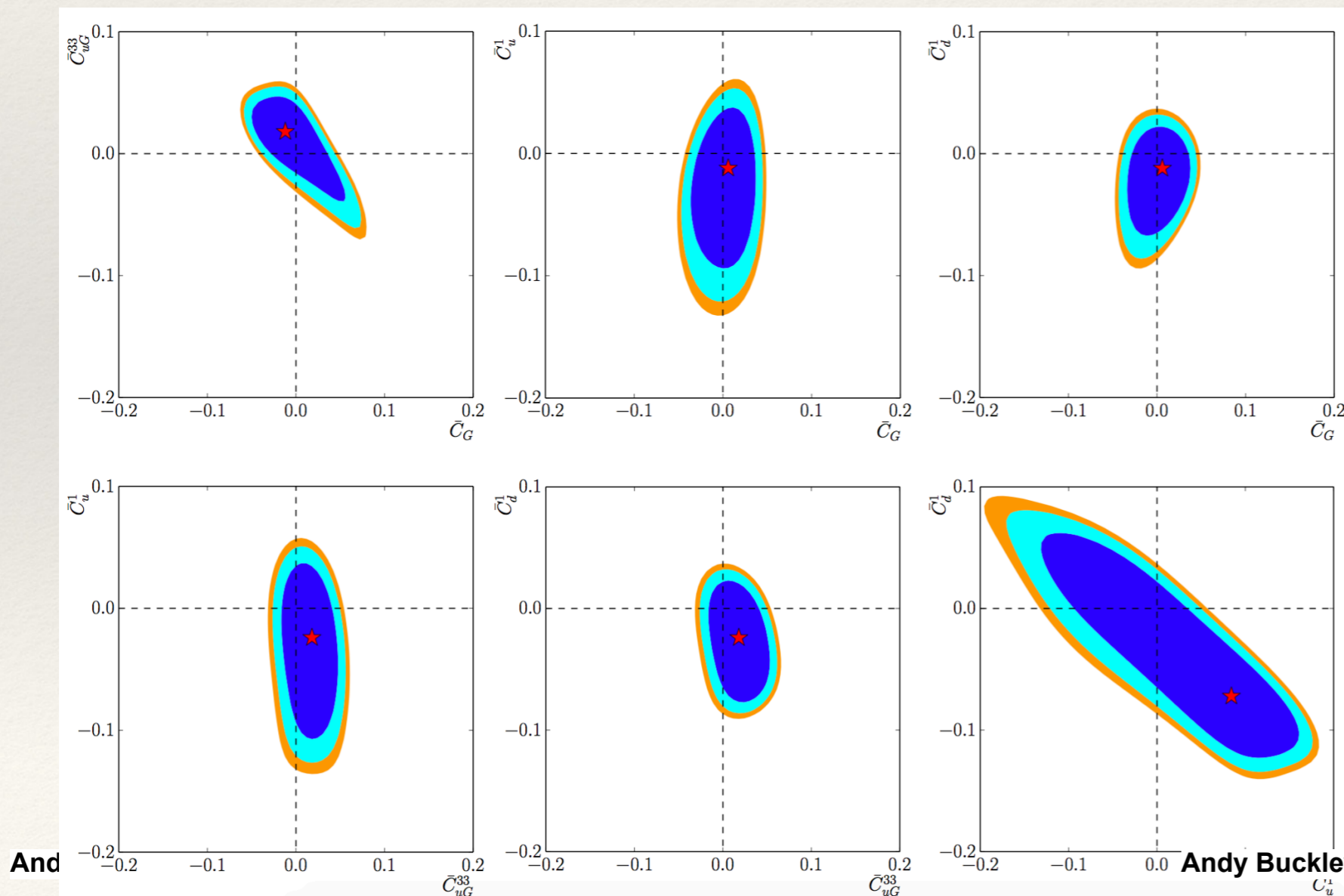
# $t\bar{t}$ cross section and effective field theory

$$\begin{aligned} \mathcal{L}_{D6} \supset & \frac{C_{uG}}{\Lambda^2} (\bar{q}\sigma^{\mu\nu}T^A u) \tilde{\varphi}G_{\mu\nu}^A + \frac{C_G}{\Lambda^2} f_{ABC}G_{\mu}^{A\nu}G_{\nu}^{B\lambda}G_{\lambda}^{C\mu} + \frac{C_{\varphi G}}{\Lambda^2} (\varphi^\dagger\varphi)G_{\mu\nu}^AG^{A\mu\nu} \\ & + \frac{C_{qq}^{(1)}}{\Lambda^2} (\bar{q}\gamma_{\mu}q)(\bar{q}\gamma^{\mu}q) + \frac{C_{qq}^{(3)}}{\Lambda^2} (\bar{q}\gamma_{\mu}\tau^I q)(\bar{q}\gamma^{\mu}\tau^I q) + \frac{C_{uu}}{\Lambda^2} (\bar{u}\gamma_{\mu}u)(\bar{u}\gamma^{\mu}u) \\ & + \frac{C_{qu}^{(8)}}{\Lambda^2} (\bar{q}\gamma_{\mu}T^A q)(\bar{u}\gamma^{\mu}T^A u) + \frac{C_{qd}^{(8)}}{\Lambda^2} (\bar{q}\gamma_{\mu}T^A q)(\bar{d}\gamma^{\mu}T^A d) + \frac{C_{ud}^{(8)}}{\Lambda^2} (\bar{u}\gamma_{\mu}T^A u)(\bar{d}\gamma^{\mu}T^A d) \end{aligned}$$

Dimension 6 operators leading to a modification of the production cross section.

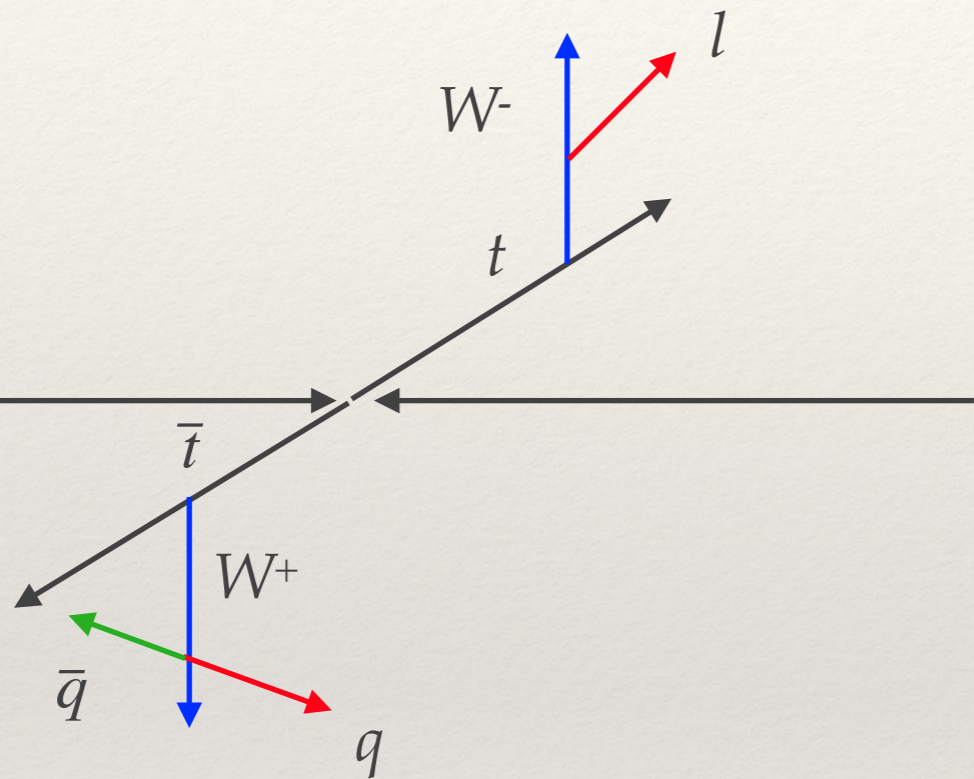
The plots show constraints on their Wilson coefficients (or linear combinations).

All other coefficients constrained to zero in these plots.





# Kinematics of $t\bar{t}$ production+decay



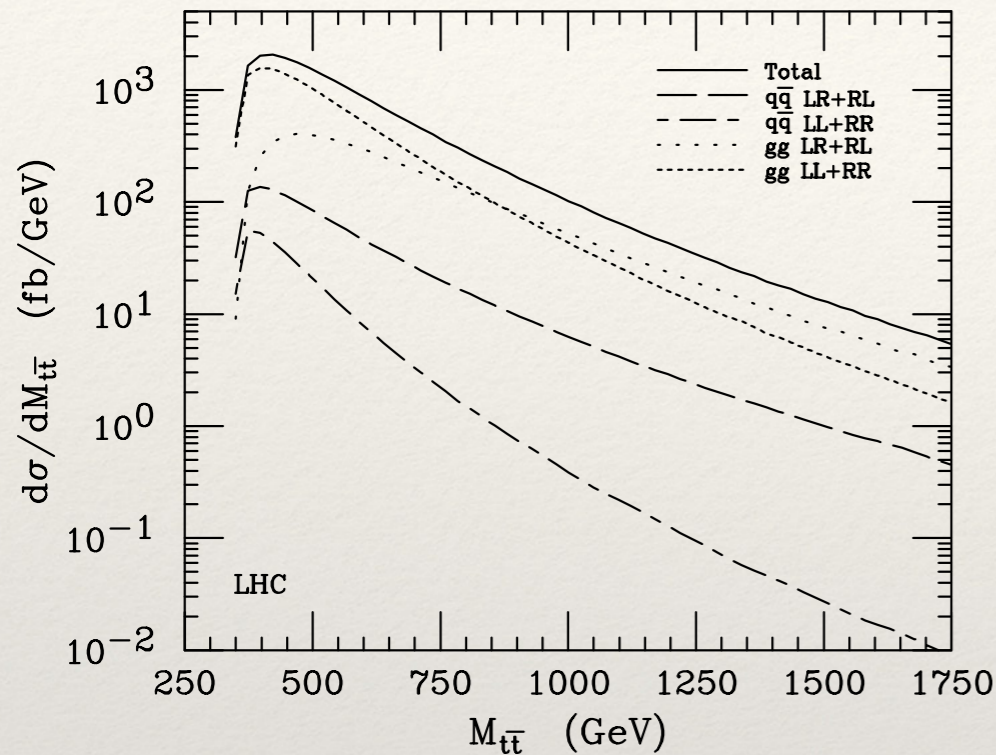
- Rapidity of  $t\bar{t}$  system
- Production angle in  $t\bar{t}$  rest frame
- Polar and azimuthal angle of  $W^+$  boson
- Polar and azimuthal angle of  $W^-$  boson
- Polar and azimuthal angle of the fermion from  $W^-$  decay
- Polar and azimuthal angle of the antifermion from the  $W^+$  decay.

Decays are classified as dilepton (10.5%), lepton + jets (43.8%), and fully hadronic (45.7%, not used for precision measurement).

Measurements are based upon distributions of observables — projections of the joint PDF for the production+decay process. Sensitive to the structure of the **g $t\bar{t}$  vertex** (production) and the  **$Wtb$  vertex** (decay)



# Spin correlations



LL+RR partons produce  $t\bar{t}$  pairs w/ opposite spins  
 LR+RL partons produce  $t\bar{t}$  pairs w/ aligned spins  
 New physics can alter the spin correlation:

- Via exotic production mechanisms ( $Z'$ , heavy Higgs, SUSY)
- Via virtual effects (anomalous couplings) at the  $ggt$  vertex.

Stephen J. Parke, arXiv:1202.2345

Decay time of the top quark ( $10^{-25}$  s) shorter than the hadronization time ( $10^{-24}$  s)

*==> spin information is transferred to the decay products of the top quark.*

The weak decay of the top quark  $t \rightarrow Wb$  is a spin analyzer.

$$\frac{1}{\Gamma_T} \frac{d\Gamma}{d \cos \chi_i} = (1 + \alpha_i \cos \chi_i) / 2$$

$$\alpha_i = \begin{cases} +0.998 & l^+ \leftarrow \\ +0.966 & \bar{d} \\ -0.314 & \bar{\nu} \\ -0.317 & \bar{u} \\ -0.393 & b \end{cases} \quad (\text{NLO})$$



Angle between decay product and spin axis, top rest frame.



# Old news: spin correlations established in 2012

Simplest observable is  $\Delta\phi$ , the difference in azimuth of two leptons in the laboratory frame:

- Does not require the reconstruction of full event kinematics
- Can easily be applied to top dilepton events, the cleanest sample of  $t\bar{t}$  events

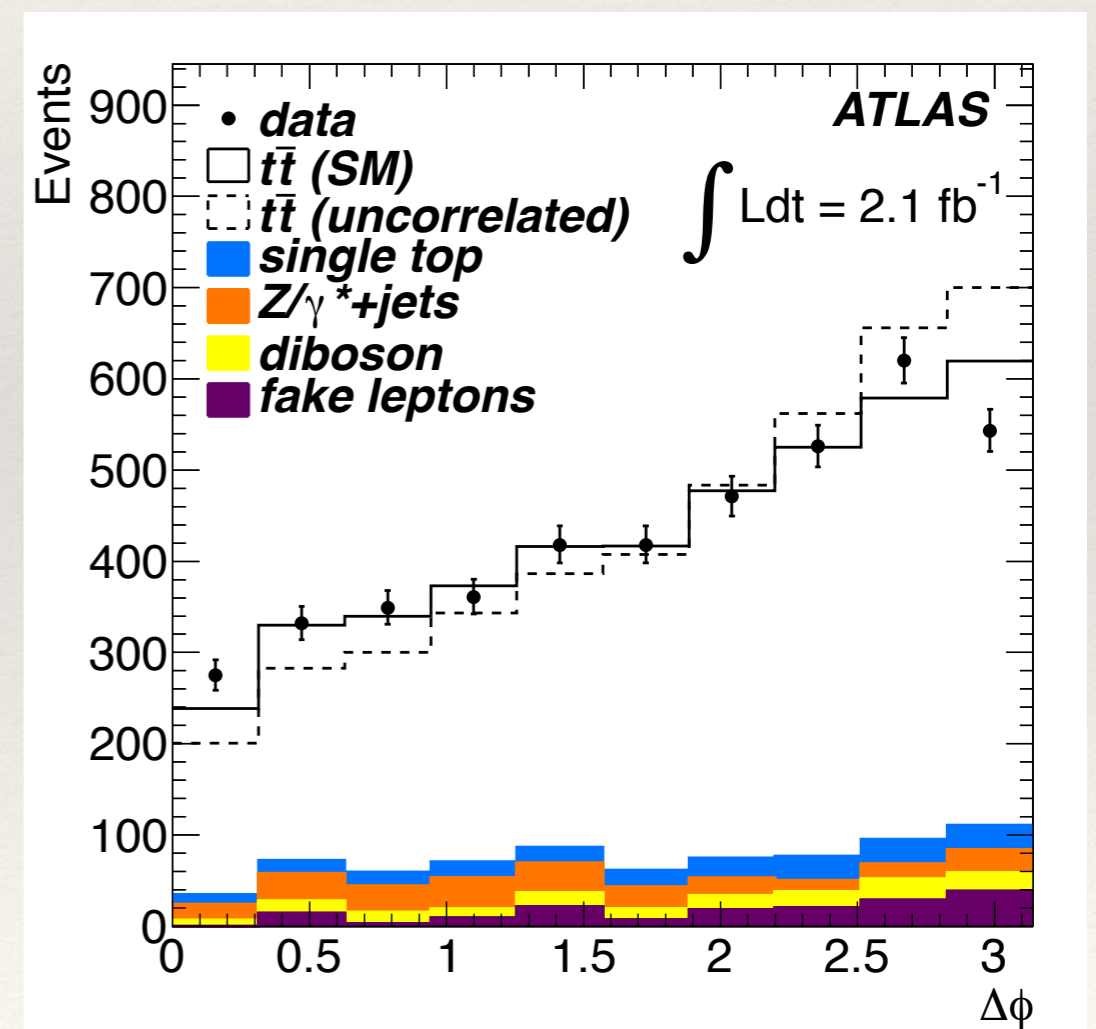
These correlations are established experimentally in 2012 using the distribution of  $\Delta\phi \implies$

$$n_i = f_{\text{SM}} n_{\text{spin}} + (1 - f_{\text{SM}}) n_{\text{nospin}}$$

$f_{\text{SM}}$  factor has SM expectation of 1.0

$$f_{\text{SM}} = 1.30 \pm 0.14^{+0.27}_{-0.22} \quad \text{Phys. Rev. Lett. 108 (2012) 212001}$$

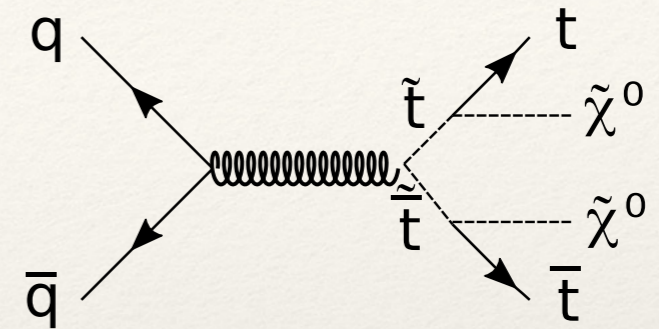
5.1  $\sigma$  observation of spin correlations (ATLAS),



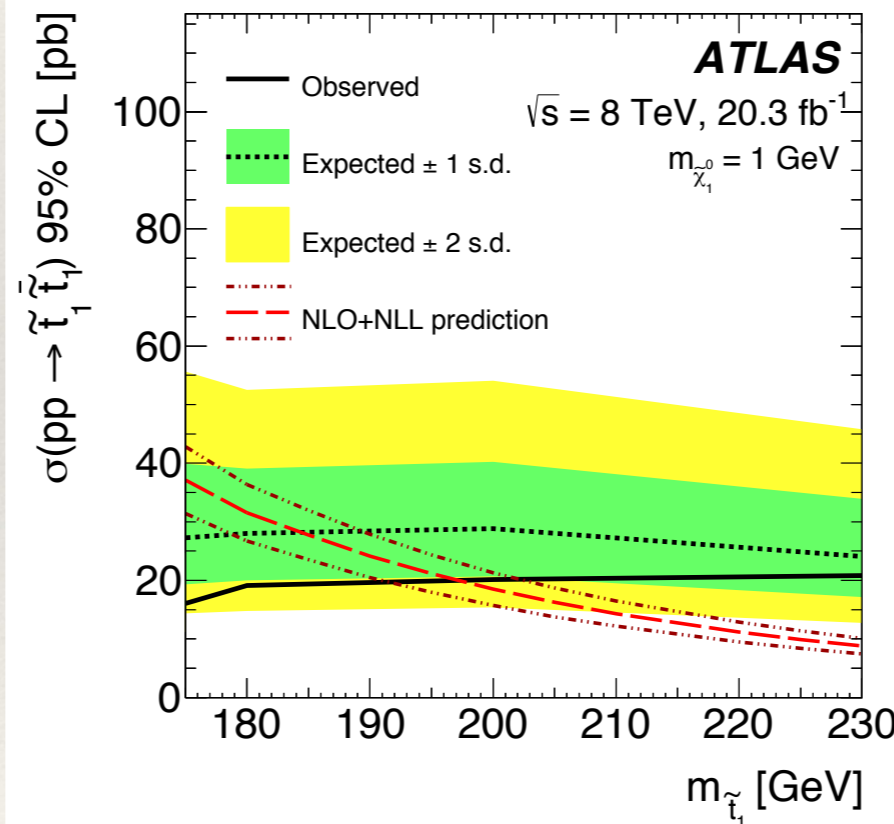
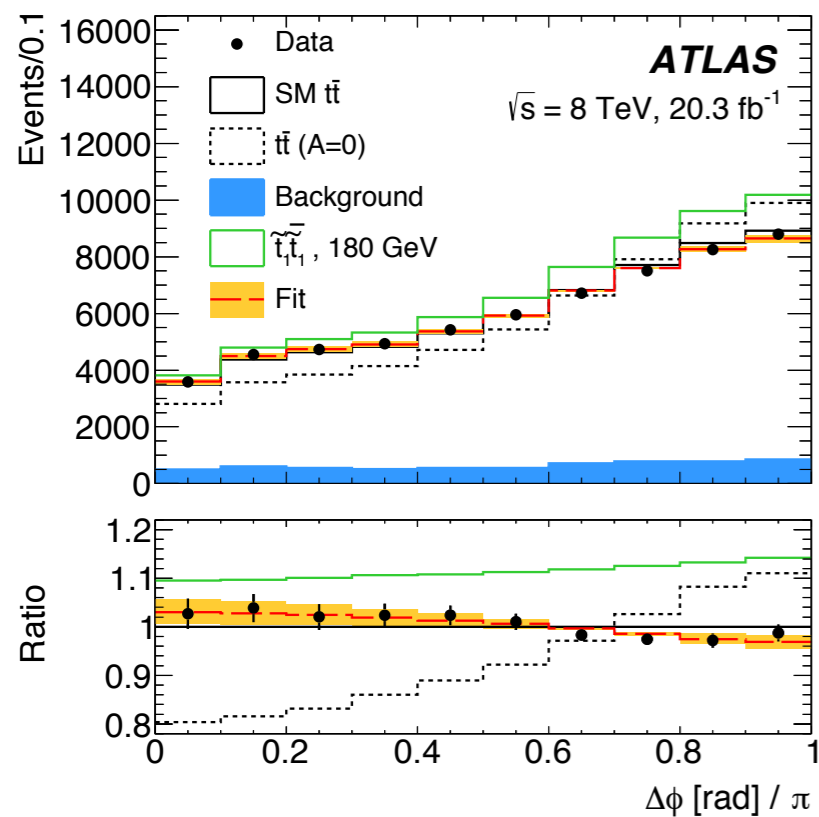


# Spin Correlations in 8 TeV data and limits on the $m_{\tilde{t}_1}$

- dilepton events used
- Spin correlation strength  $A_{\text{helicity}} = (N_{\text{like}} - N_{\text{unlike}}) / (N_{\text{like}} + N_{\text{unlike}})$  extracted
- Bounds on the mass of the lightest stop inferred.
- The search looks for right-handed tops from the lightest stop.



Phys. Rev. Lett. 114 (2015) 142001



From cross section only, limits are weaker:

$$m_t < m_{\tilde{t}_1} < 177 \text{ GeV}$$

see

Eur. Phys. J. C 74  
3109 (2014)

$$A_{\text{helicity}} = 0.38 \pm 0.04$$

compare with

$$A_{\text{helicity}}^{\text{SM}} = 0.318 \pm 0.006$$

[Nucl. Phys. B 725 115 (2013)]

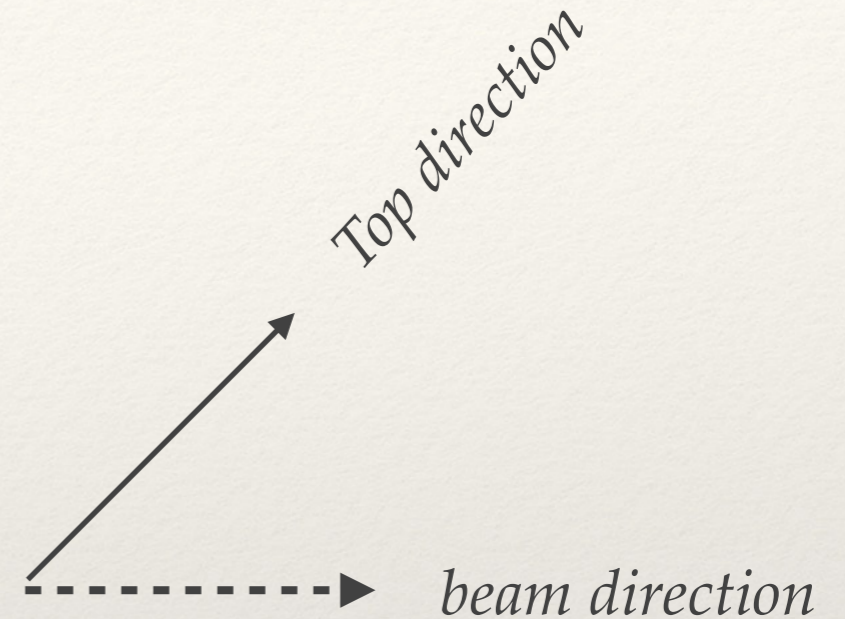
$$m_t < m_{\tilde{t}_1} < 191 \text{ GeV} \quad (95\%)$$



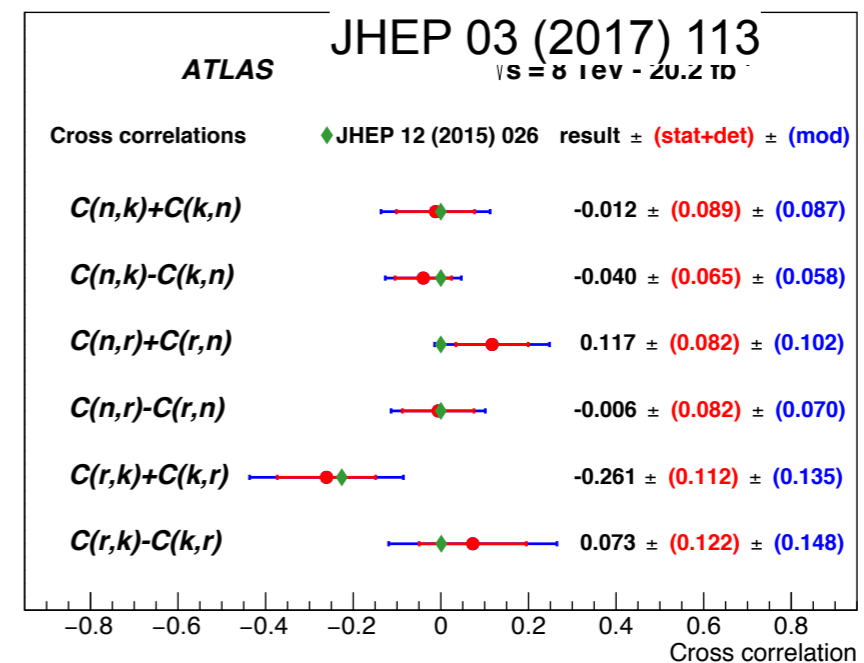
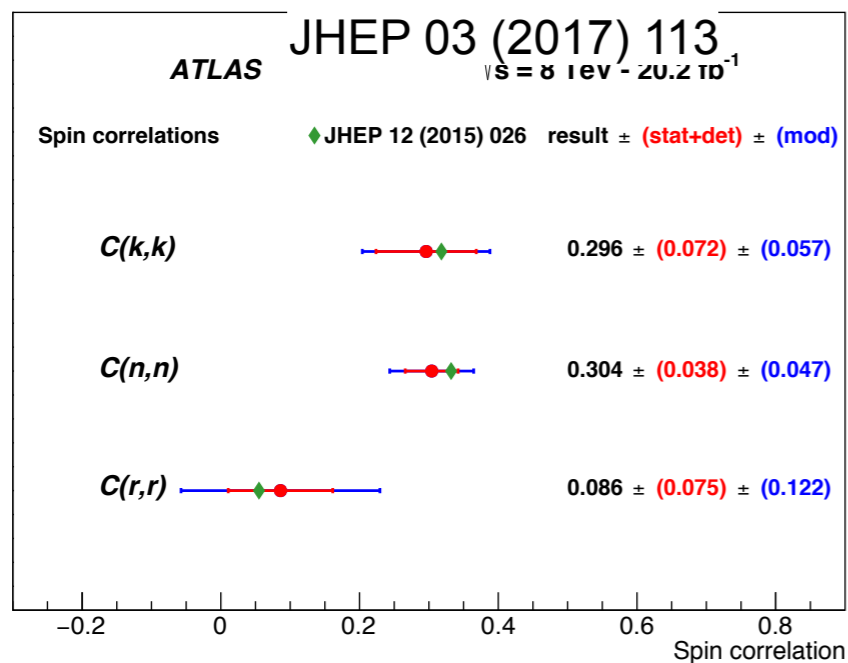
# Spin correlations in all three directions

In the Zero Momentum Frame (ZMF), we identify three angles:

- Helicity angle  $\theta$
- Transverse angle,  $\perp$  production plane
- “R-axis angle”, third orthogonal direction
- All components of the  $t\bar{t}$  pair spin-density matrix measured in the analysis from ATLAS.



$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_1 d \cos \theta_2} = \frac{1}{4} (1 - C \cos \theta_1 \cos \theta_2) \text{ Simplest form.}$$





# CMS 8 TeV (dilepton analysis)

CMS collaboration, PRD D 93 052007 (2016). The main reference and roadmap for this work is Bernreuther and Si PLB 725 (2013) 115, examining the effect of anomalous top **chromo-magnetic and chromo-electric dipole moments**.

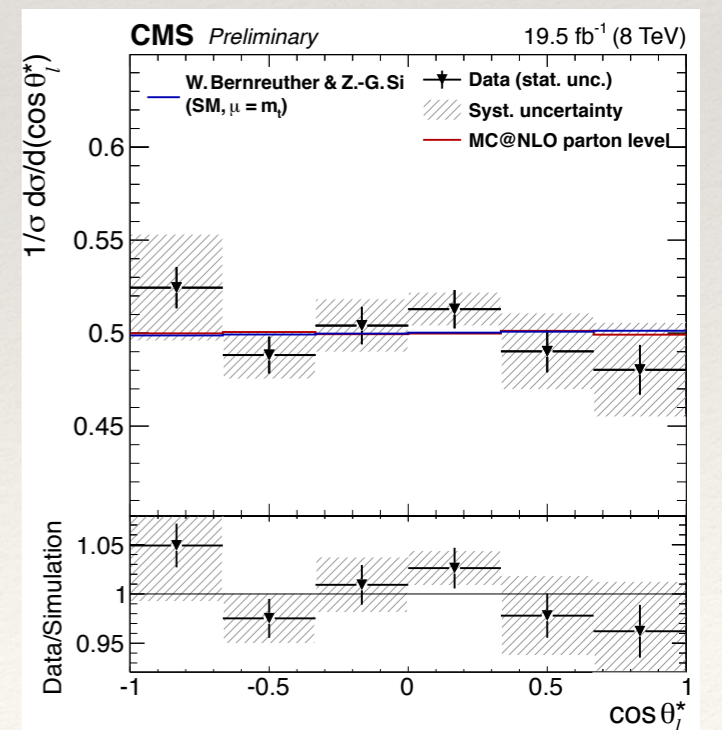
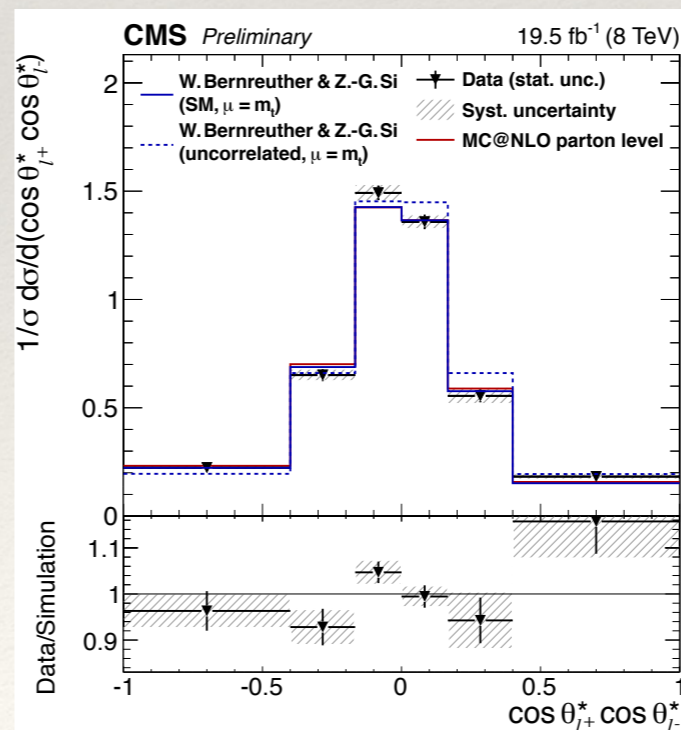
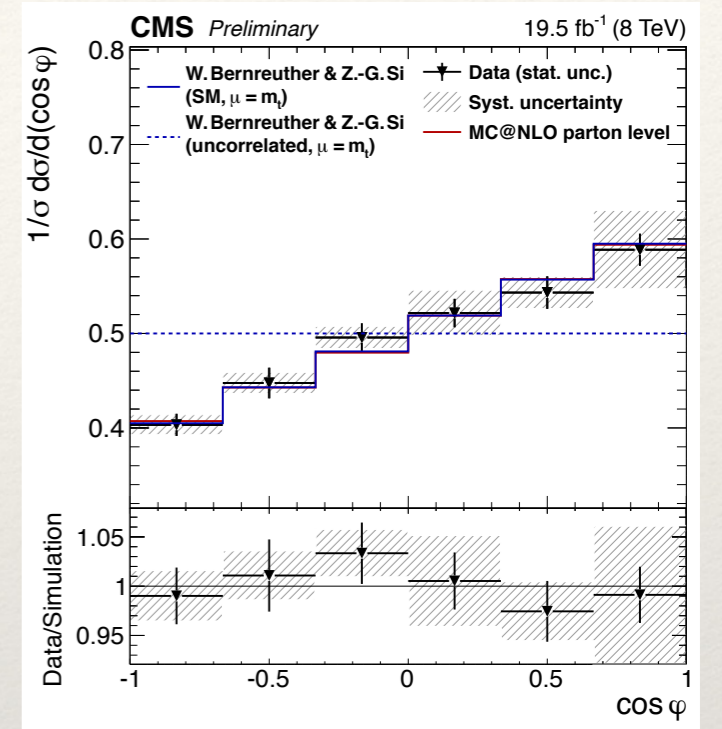
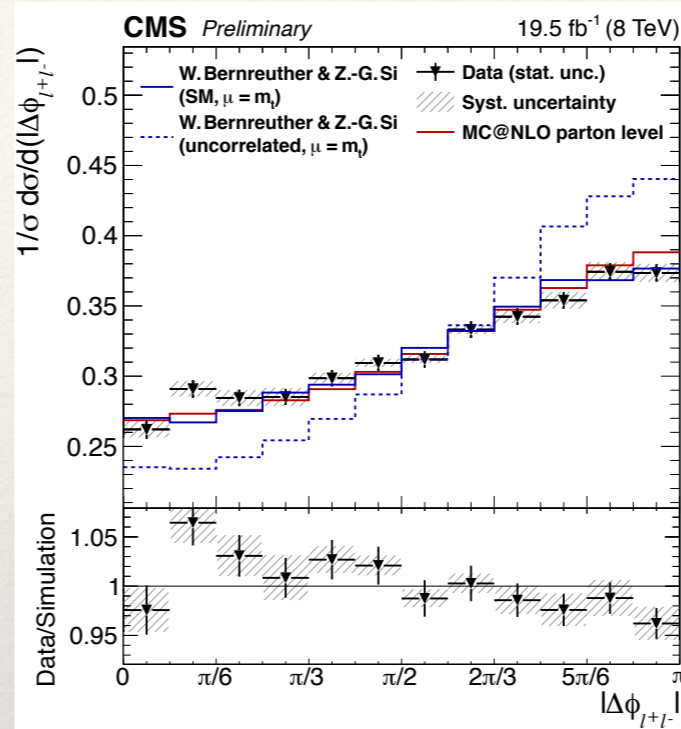
$$A_{\Delta\phi} = \frac{N(|\Delta\phi_{\ell^+\ell^-}| > \pi/2) - N(|\Delta\phi_{\ell^+\ell^-}| < \pi/2)}{N(|\Delta\phi_{\ell^+\ell^-}| > \pi/2) + N(|\Delta\phi_{\ell^+\ell^-}| < \pi/2)}$$

$$A_{c_1c_2} = \frac{N(c_1c_2 > 0) - N(c_1c_2 < 0)}{N(c_1c_2 > 0) + N(c_1c_2 < 0)}$$

$$A_{\cos\varphi} = \frac{N(\cos\varphi > 0) - N(\cos\varphi < 0)}{N(\cos\varphi > 0) + N(\cos\varphi < 0)}$$

$$A_{P^\pm} = \frac{N(\cos\theta_{\ell^\pm}^* > 0) - N(\cos\theta_{\ell^\pm}^* < 0)}{N(\cos\theta_{\ell^\pm}^* > 0) + N(\cos\theta_{\ell^\pm}^* < 0)}$$

**CPV:**  $A_{CPV} = A_{P^+} - A_{P^-}$





# Chromo-moments at the gtt vertex

Variable	$f_{\text{SM}} \pm (\text{stat}) \pm (\text{syst}) \pm (\text{theor})$	Total uncertainty
$A_{\Delta\phi}$	$1.14 \pm 0.06 \pm 0.13 \begin{smallmatrix} +0.08 \\ -0.11 \end{smallmatrix}$	$\begin{smallmatrix} +0.16 \\ -0.18 \end{smallmatrix}$
$A_{\cos\varphi}$	$0.90 \pm 0.09 \pm 0.10 \pm 0.05$	$\pm 0.15$
$A_{c_1c_2}$	$0.87 \pm 0.17 \pm 0.21 \pm 0.04$	$\pm 0.27$
$A_{\Delta\phi} (\text{vs. } M_{t\bar{t}})$	$1.12 \pm 0.06 \pm 0.08 \begin{smallmatrix} +0.08 \\ -0.11 \end{smallmatrix}$	$\begin{smallmatrix} +0.12 \\ -0.15 \end{smallmatrix}$

CMS PRD 93 052007 (2016)

$$\mathcal{L}_{\text{eff}} = -\frac{\tilde{\mu}_t}{2} \bar{t} \sigma^{\mu\nu} T^a t G_{\mu\nu}^a - \frac{\tilde{d}_t}{2} \bar{t} i \sigma^{\mu\nu} \gamma_5 T^a t G_{\mu\nu}^a$$

$$\hat{\mu}_t \equiv \frac{m_t}{g_s} \tilde{\mu}_t \quad \hat{d}_t \equiv \frac{m_t}{g_s} \tilde{d}_t$$



The CMS analysis is sensitive to  $\text{Re}(\hat{\mu}_t)$  and  $\text{Im}(\hat{d}_t)$

Dimensionless anomalous chromo-magnetic & electric dipole moment parameters.

$$\delta\hat{\mu}_t = \frac{\sqrt{2}}{g_s} \text{Re} C_{uG\phi}^{33} \frac{vm_t}{\Lambda^2} \quad \delta\hat{d}_t = \frac{\sqrt{2}}{g_s} \text{Re} C_{uG\phi}^{33} \frac{vm_t}{\Lambda^2}$$

**Relation to Wilson coefficients**

J.A. Aguilar-Saveedra, Nucl.Phys.B812:181-204,2009



# Re( $\hat{\mu}$ ) & Im( $\hat{d}$ ) from spin correlations (CMS)

$$\frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^-}|} = \left( \frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^-}|} \right)_{\text{SM}} + \text{Re}(\hat{\mu}_t) \left( \frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^-}|} \right)_{\text{NP}}$$

Fit to Re( $\hat{\mu}_t$ ) assuming all other parameters have SM values

==>

$$-0.053 < \text{Re}(\hat{\mu}_t) < 0.042 \text{ (95\%)}$$

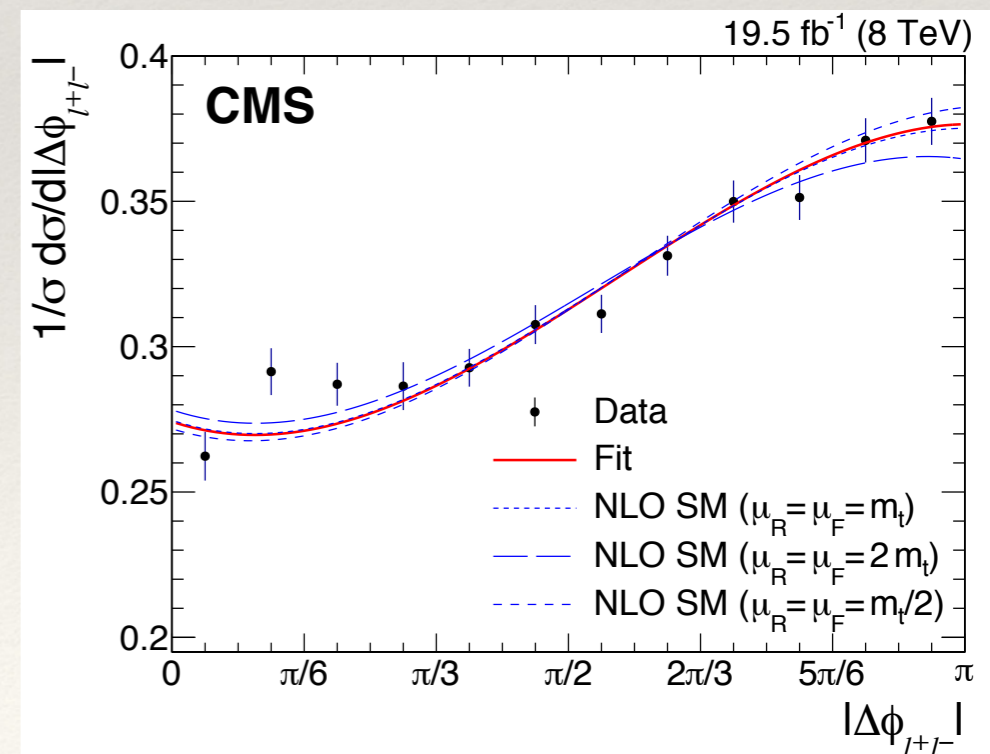
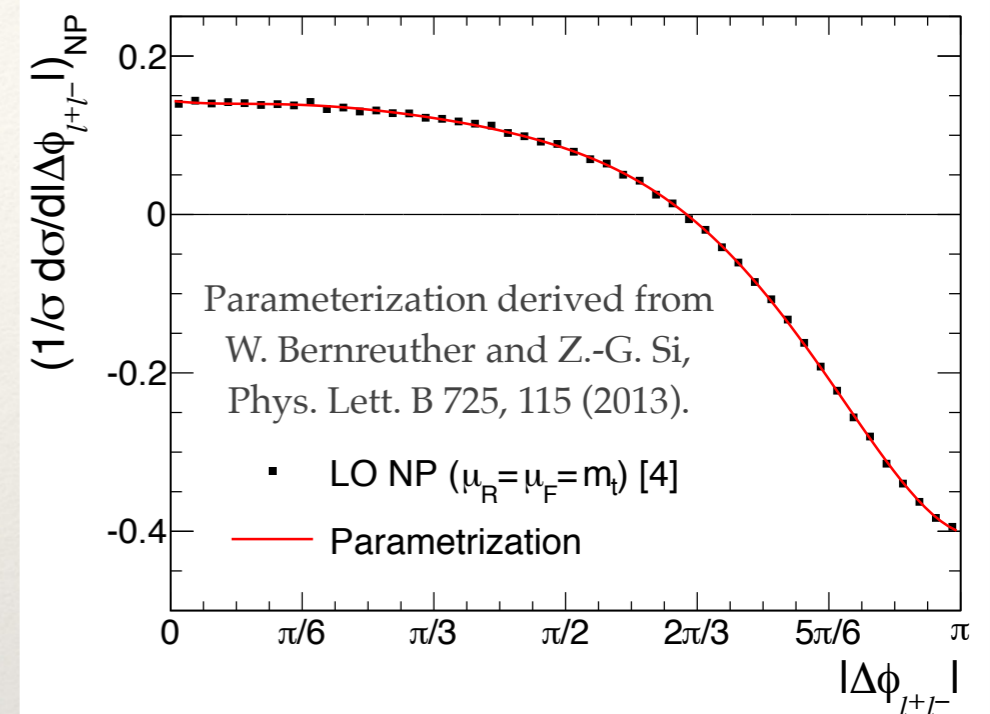
Using the asymmetry in  $\cos\phi$  ==>

$$-0.053 < \text{Re}(\hat{\mu}_t) < 0.026 \text{ (95\%)}$$

CP violation in  $t\bar{t}$  production? From  $A_{\text{CPV}} = A_{\text{P}^+} - A_{\text{P}^-}$

$$-0.068 < \text{Im}(\hat{d}_t) < 0.067 \text{ (95\%)}$$

(Chromomagnetic moment is also constrained by differential cross section in CMS; see talk by Xin Chen in parallel session.)

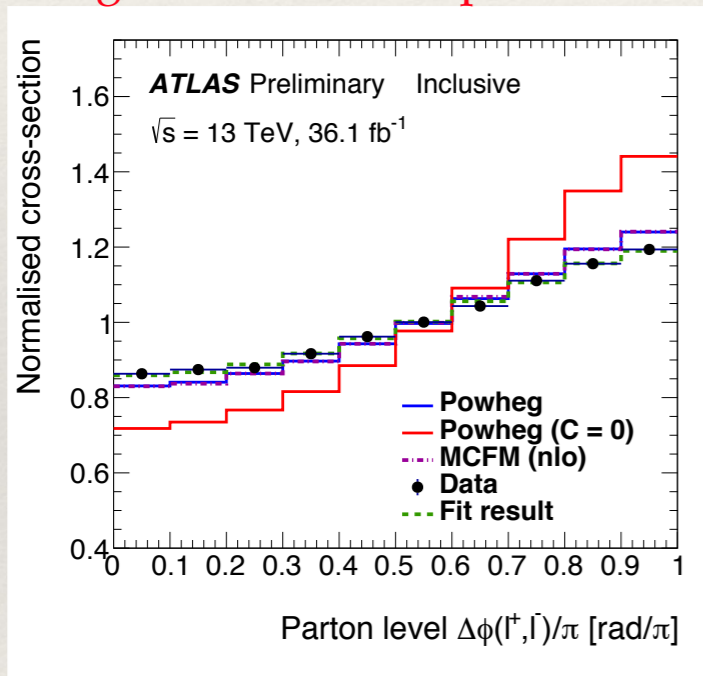




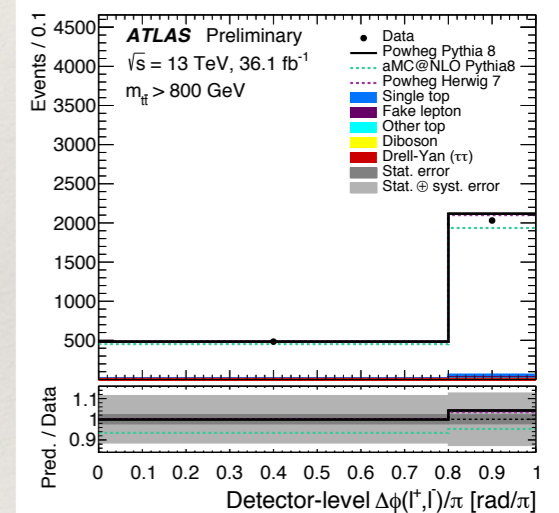
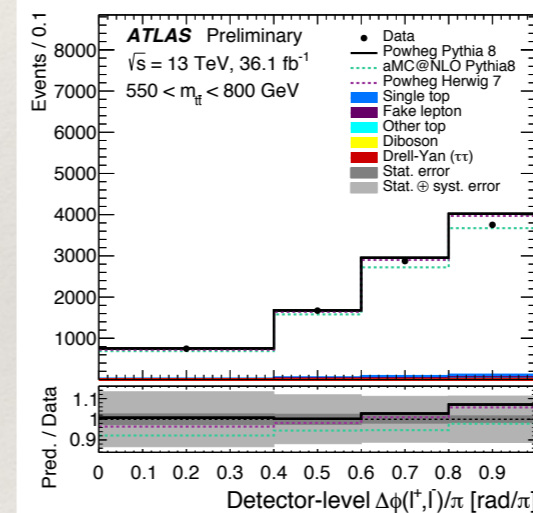
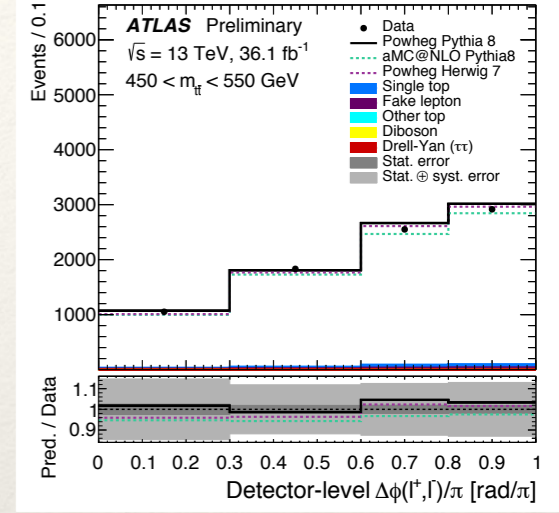
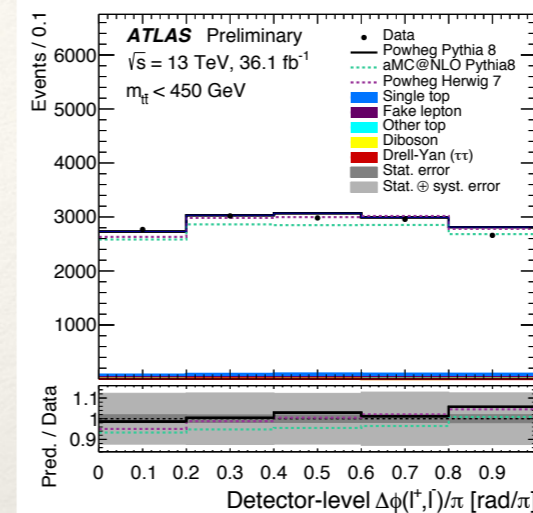
# Latest word on spin correlations (ATLAS, 13 TeV)

[ATLAS-CONF-2018-027]

- Spin correlation in  $e\mu$  channel.
- $\Delta\phi$  distribution unfolded to parton level
- Absolute and normalized cross sections measured.
- $f_{SM}$  from normalized cross section
- Signal modeling uncertainties dominant
- **Significant excess spin correlation observed:**



Excess spin correlation increases  $m(t\bar{t})$  but significance is limited by the sample size when divided into bins  $\rightarrow$



Region	$f_{SM}$	Significance (incl. theory uncertainties)
$m_{t\bar{t}} < 450$ GeV	$1.11 \pm 0.04 \pm 0.13$	0.85 (0.84)
$450 < m_{t\bar{t}} < 550$ GeV	$1.17 \pm 0.09 \pm 0.14$	1.00 (0.91)
$550 < m_{t\bar{t}} < 800$ GeV	$1.60 \pm 0.24 \pm 0.35$	1.43 (1.37)
$m_{t\bar{t}} > 800$ GeV	$2.2 \pm 1.8 \pm 2.3$	0.41 (0.40)
inclusive	$1.250 \pm 0.026 \pm 0.063$	3.70 (3.20)

The only hint so far of an anomaly in  $t\bar{t}$  production...

*SUSY interpretation in progress*

$\leftarrow$  The trend was present in past measurements 13



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# The Wtb vertex

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The previous results are probes of the gtt vertex, assuming a SM Wtb vertex.

Experiment also can probe the Wtb vertex, as we will show in the next slides.

$$\mathcal{L}_{Wtb} = -\frac{g}{\sqrt{2}}\bar{b}\gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- - \frac{g}{\sqrt{2}}\bar{b}\frac{i\sigma^{\mu\nu}q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^- + H.c.$$

Language of anomalous couplings

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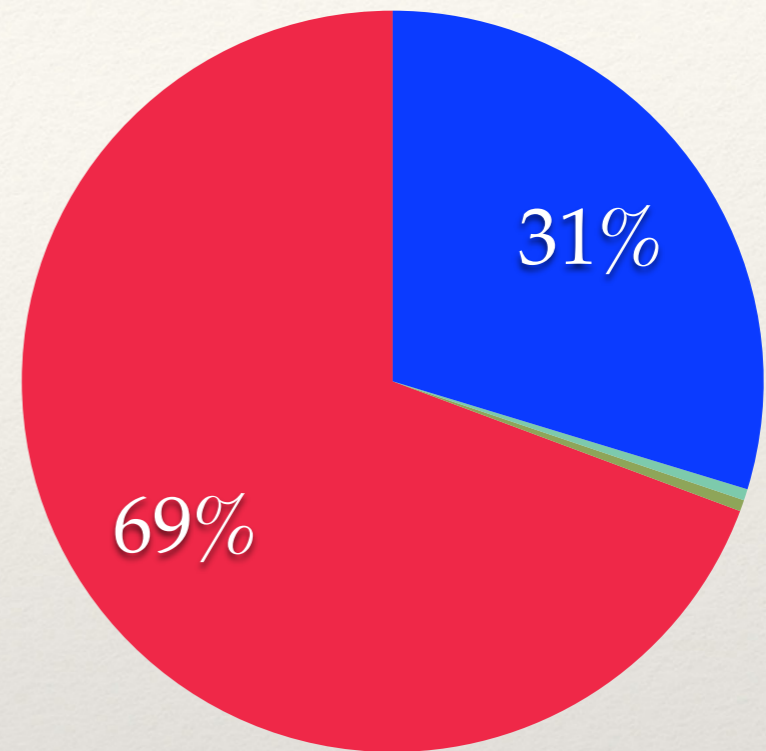
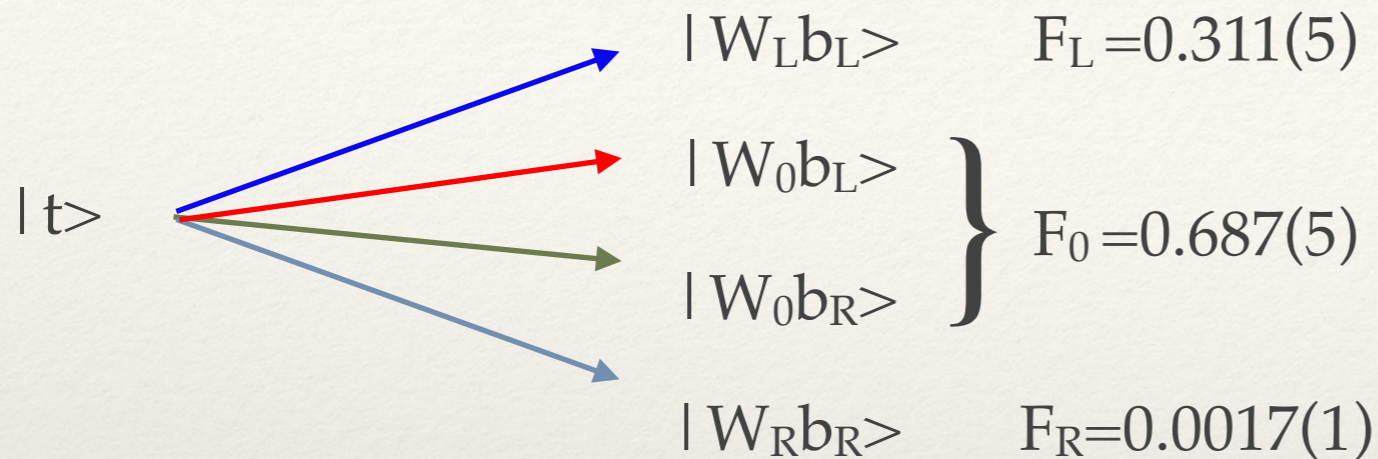
$$\delta V_L = C_{\phi q}^{(3,33)*} \frac{v^2}{\Lambda^2} \quad \delta g_L = \sqrt{2} C_{dW}^{33*} \frac{v^2}{\Lambda^2}$$

$$\delta V_R = \frac{1}{2} C_{\phi\phi}^{33} \frac{v^2}{\Lambda^2} \quad \delta g_R = \sqrt{2} C_{uW}^{33} \frac{v^2}{\Lambda^2}$$

Language of effective field theory

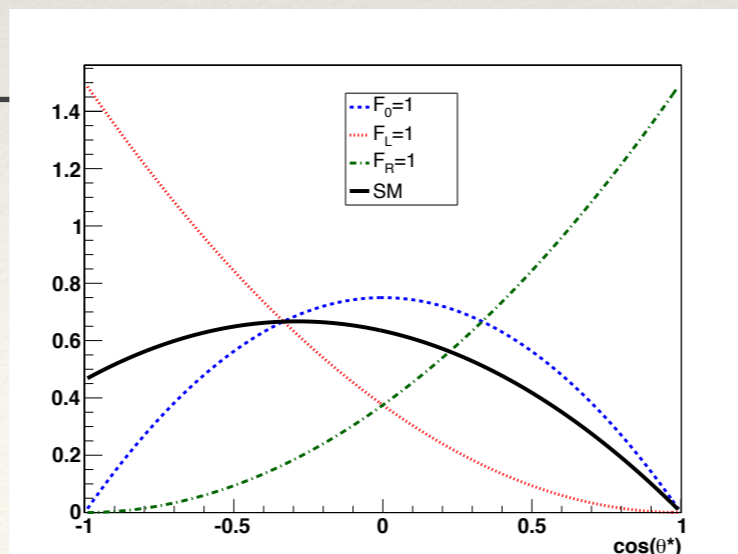
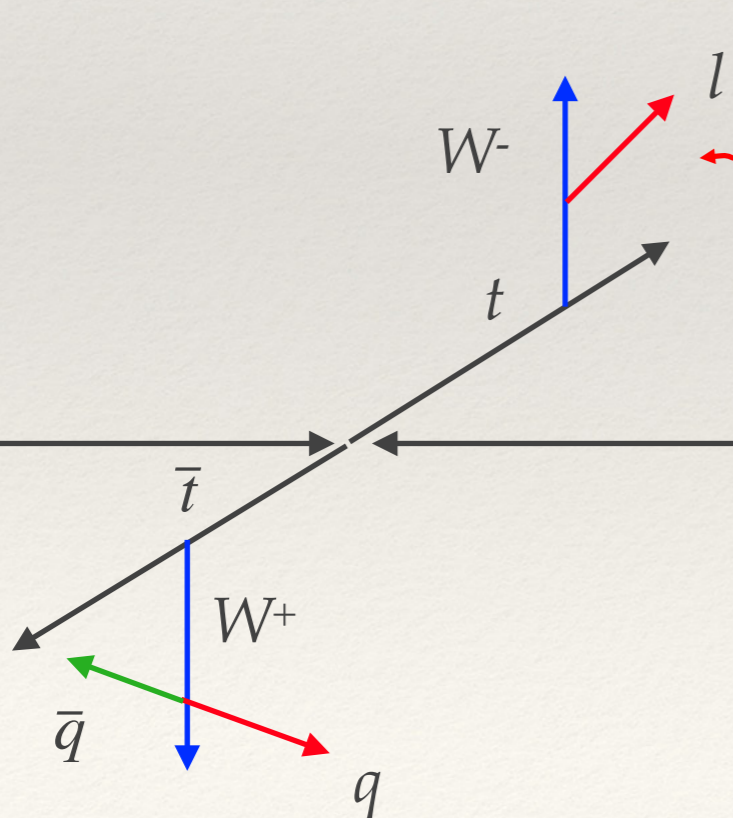


# W Boson Helicity Fractions



(NNLO QCD) Phys. Rev. D **81**, 111503 (2010)

Helicity fractions are determined from an analysis of the angle  $\theta^*$ : angle between the W boson in the top quark frame and the charged lepton in the W frame.



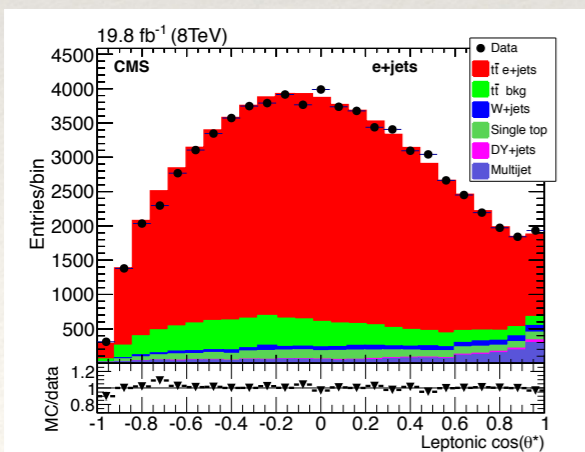
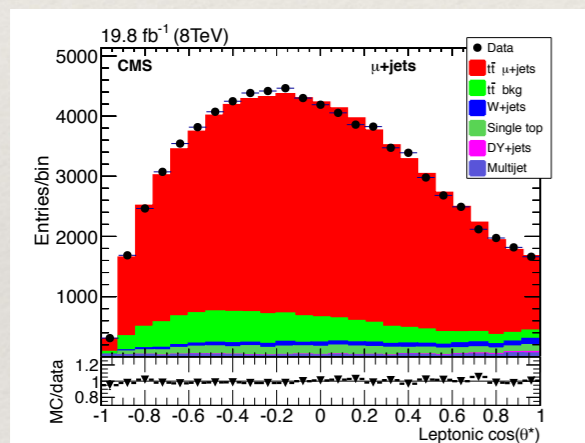
$$\begin{aligned}
 \frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta^*} &= \frac{3}{8} (1 - \cos \theta^*)^2 F_L \\
 &+ \frac{3}{4} (\sin \theta^*)^2 F_0 \\
 &+ \frac{3}{8} (1 + \cos \theta^*)^2 F_R
 \end{aligned}$$



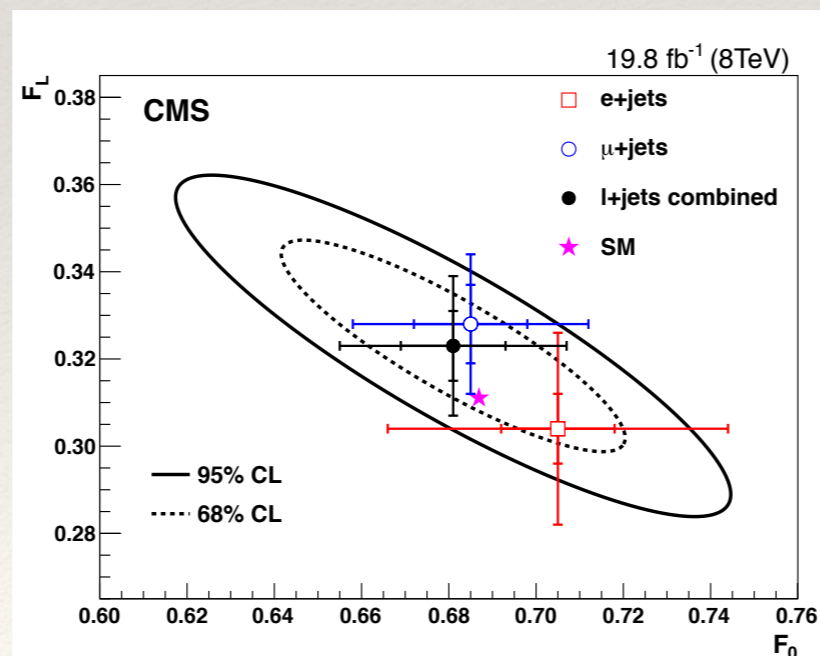
# Helicity fractions from $t\bar{t}$ events (CMS)

- Lepton+jet events
- Require 1 lepton (e or  $\mu$ ) + 4 jets events, two of which are b-tagged.
- Reconstruct neutrino momentum,  $t\bar{t}$  system, angles  $\theta^*$  on hadronic and leptonic side
- Binned likelihood fit to  $\theta^*$  on leptonic side extracts helicity fractions.

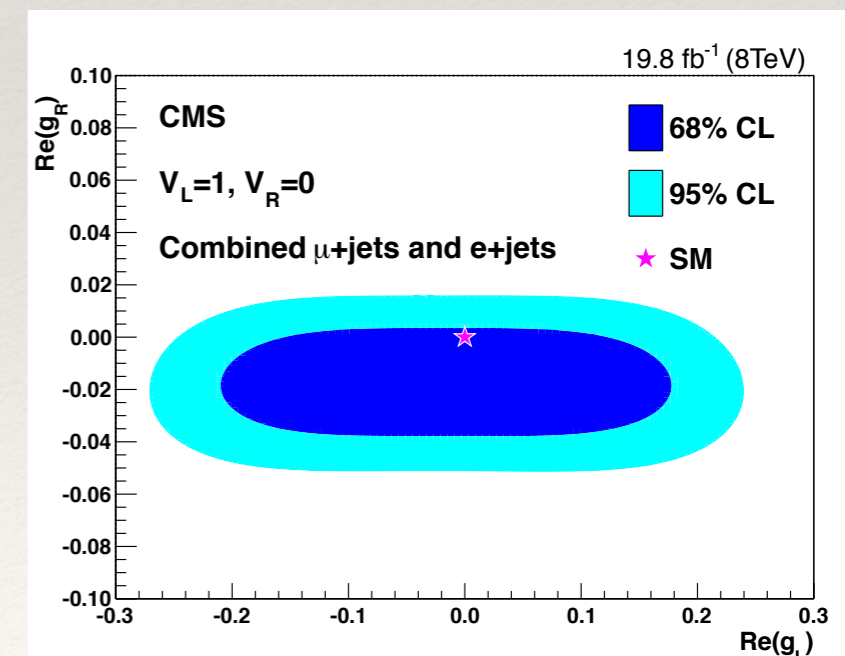
Channel	$F_0 \pm (\text{stat}) \pm (\text{syst})$	$F_L \pm (\text{stat}) \pm (\text{syst})$	$F_R \pm (\text{stat}) \pm (\text{syst})$	$\rho_{0,L}$
e+jets	$0.705 \pm 0.013 \pm 0.037$	$0.304 \pm 0.009 \pm 0.020$	$-0.009 \pm 0.005 \pm 0.021$	-0.950
$\mu$ +jets	$0.685 \pm 0.013 \pm 0.024$	$0.328 \pm 0.009 \pm 0.014$	$-0.013 \pm 0.005 \pm 0.017$	-0.957
$\ell$ +jets	$0.681 \pm 0.012 \pm 0.023$	$0.323 \pm 0.008 \pm 0.014$	$-0.004 \pm 0.005 \pm 0.014$	-0.959



## Helicity fractions



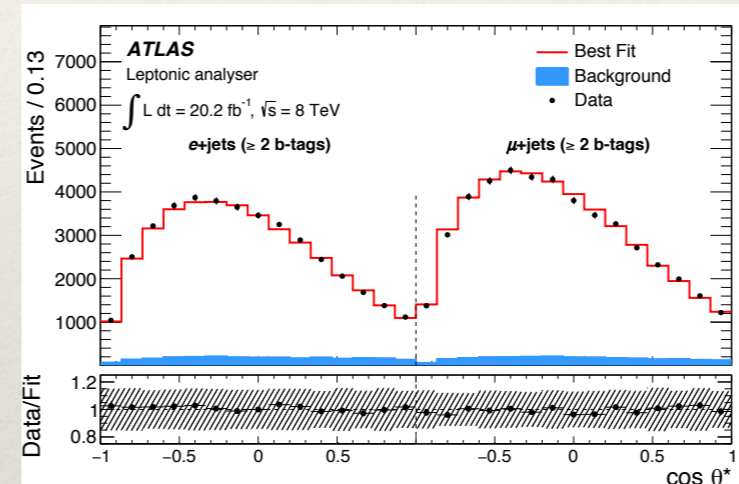
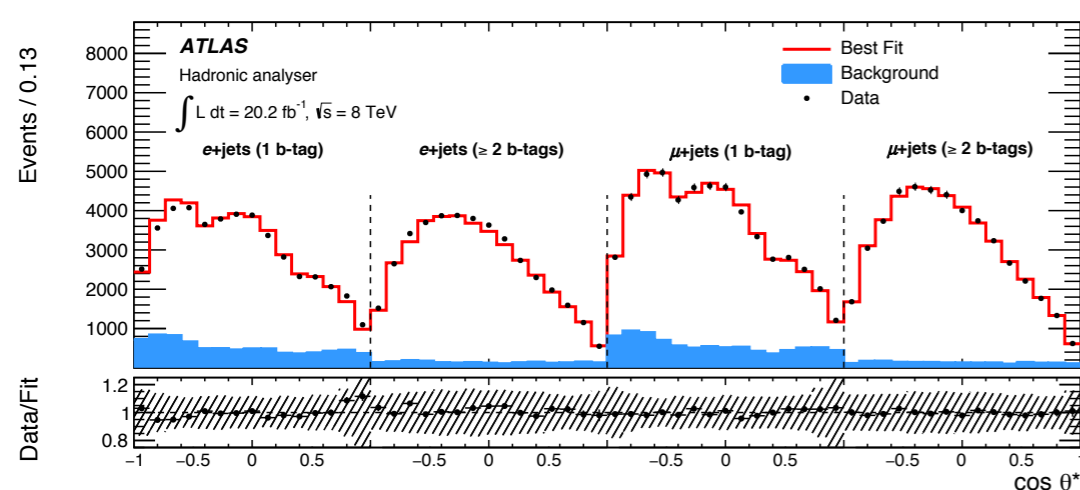
## Anomalous couplings



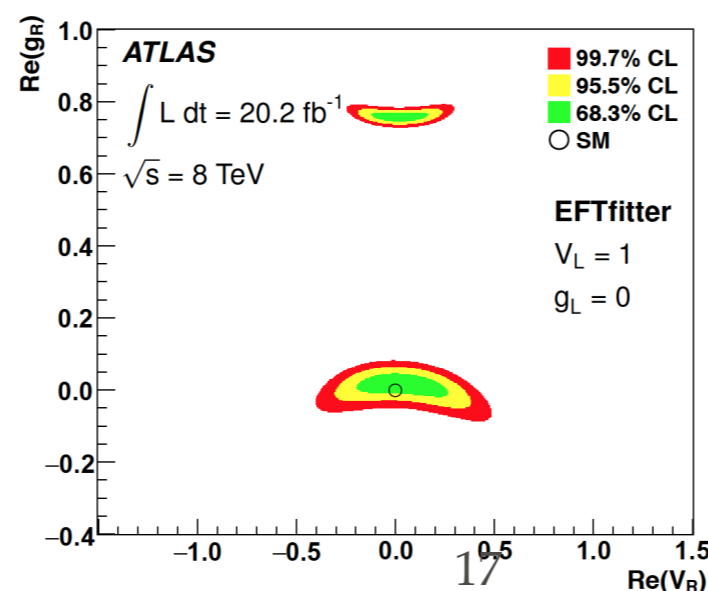
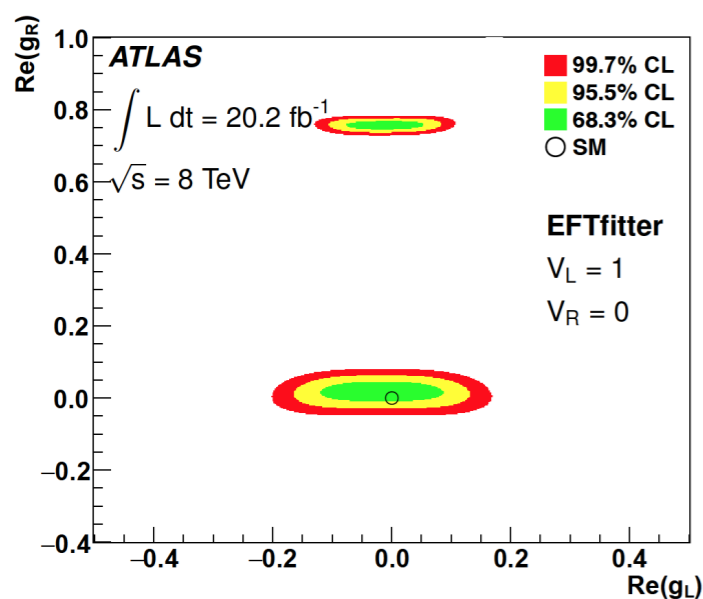


# Helicity fractions from $t\bar{t}$ events (ATLAS)

- Lepton+jet events
- Require 1 lepton (e or  $\mu$ ) + 4 jets events, at least one of which are b-tagged.
- Kinematic fit (KLFitter, NIM A 748 18 2014) to reconstruct  $t\bar{t}$  system
- Binned likelihood fit to  $\theta^*$  from both leptonic & hadronic side used
  - How is that possible?  $\implies$  b-tagging on the hadronic side to identify (anti)fermion from W decay!



EPJ 77 (2017) 264

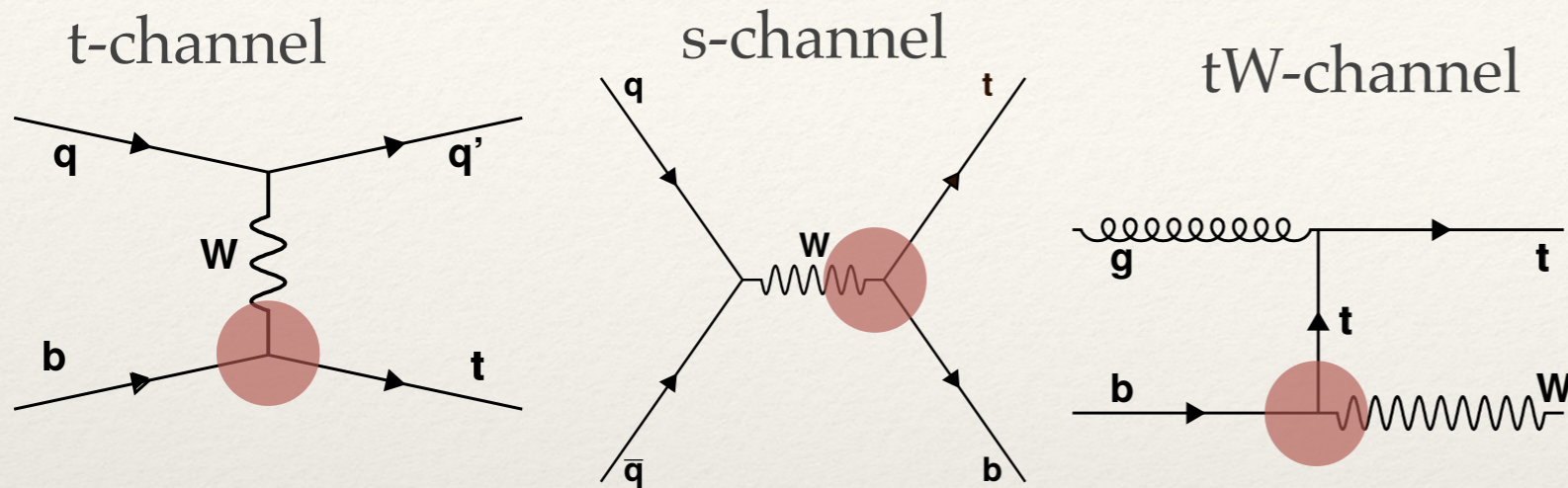


$F_0 = 0.709 \pm 0.012$  (stat+bkg.norm)  $\pm 0.015$  (syst)  
 $F_L = 0.299 \pm 0.008$  (stat+bkg.norm)  $\pm 0.013$  (syst)  
 $F_R = -0.008 \pm 0.006$  (stat+bkg.norm)  $\pm 0.012$  (syst)

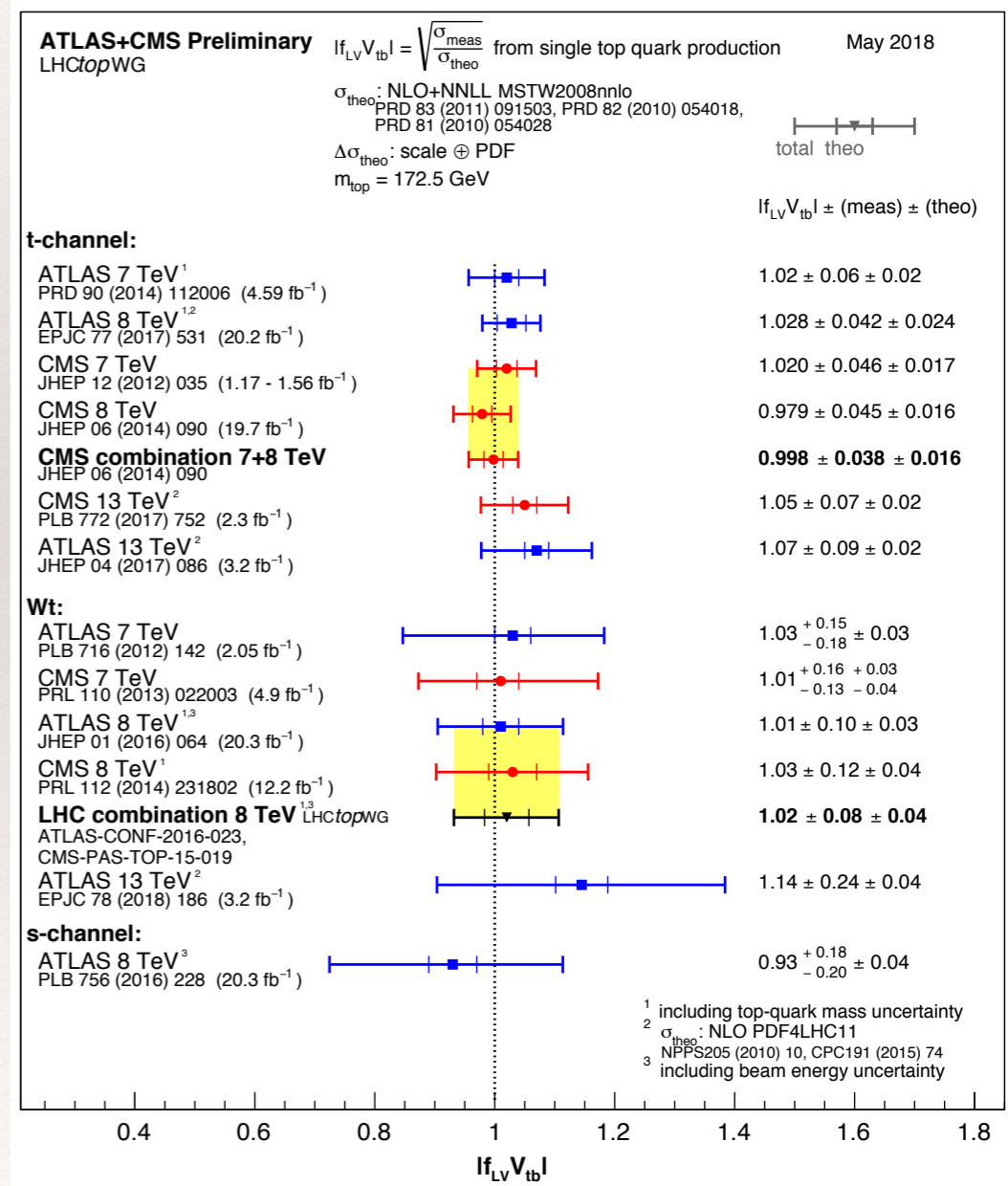
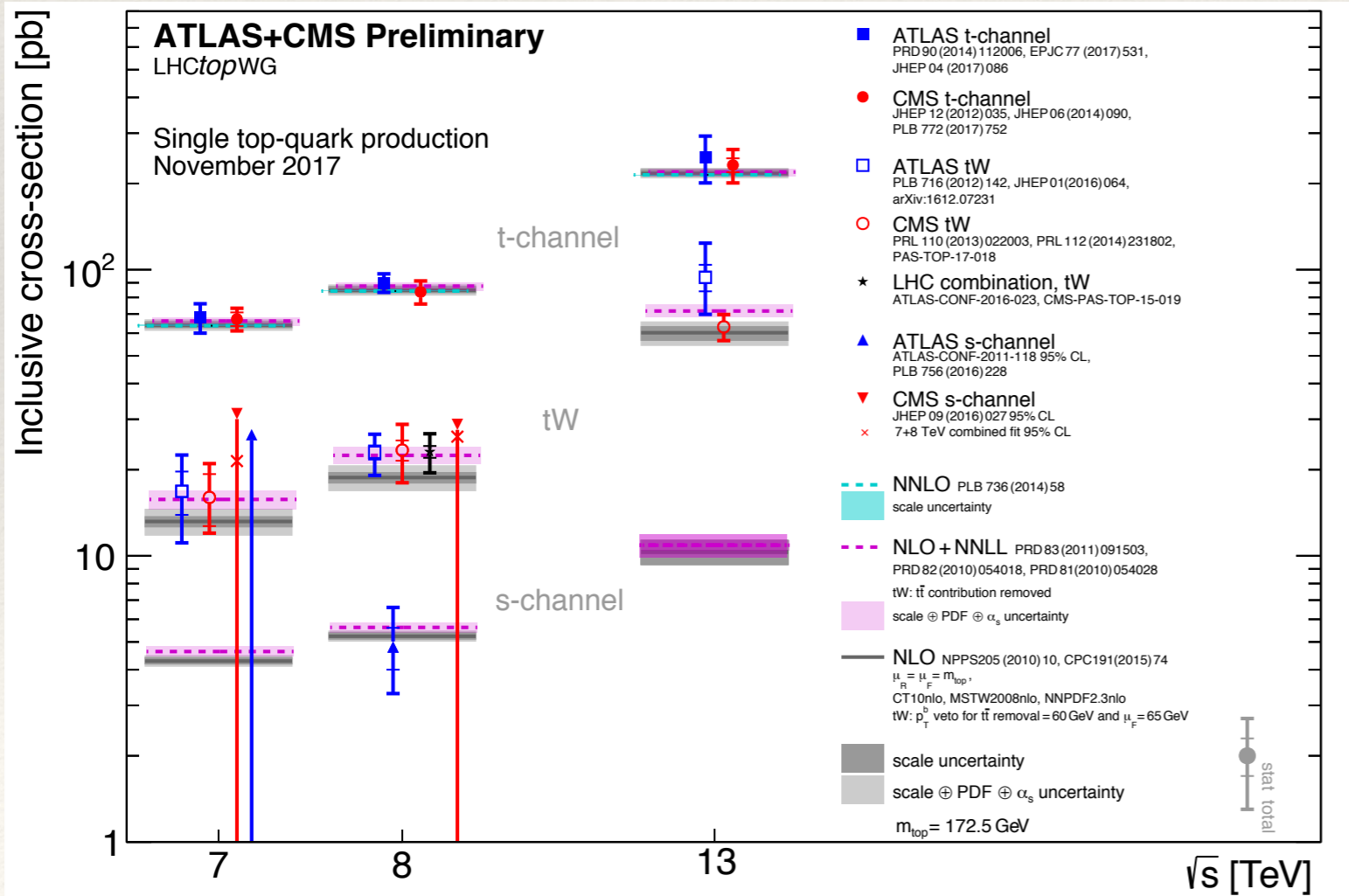
Jet reconstruction and signal modeling  
 dominant systematic errors.



# Single top processes and the $Wtb$ vertex



The  $Wtb$  vertex occurs both at production and decay in all single top processes. Direct measurement of  $|V_{tb}|$   
 All consistent with SM value  $|V_{tb}|=1$





# Helicity fraction measurements in single top t-channel

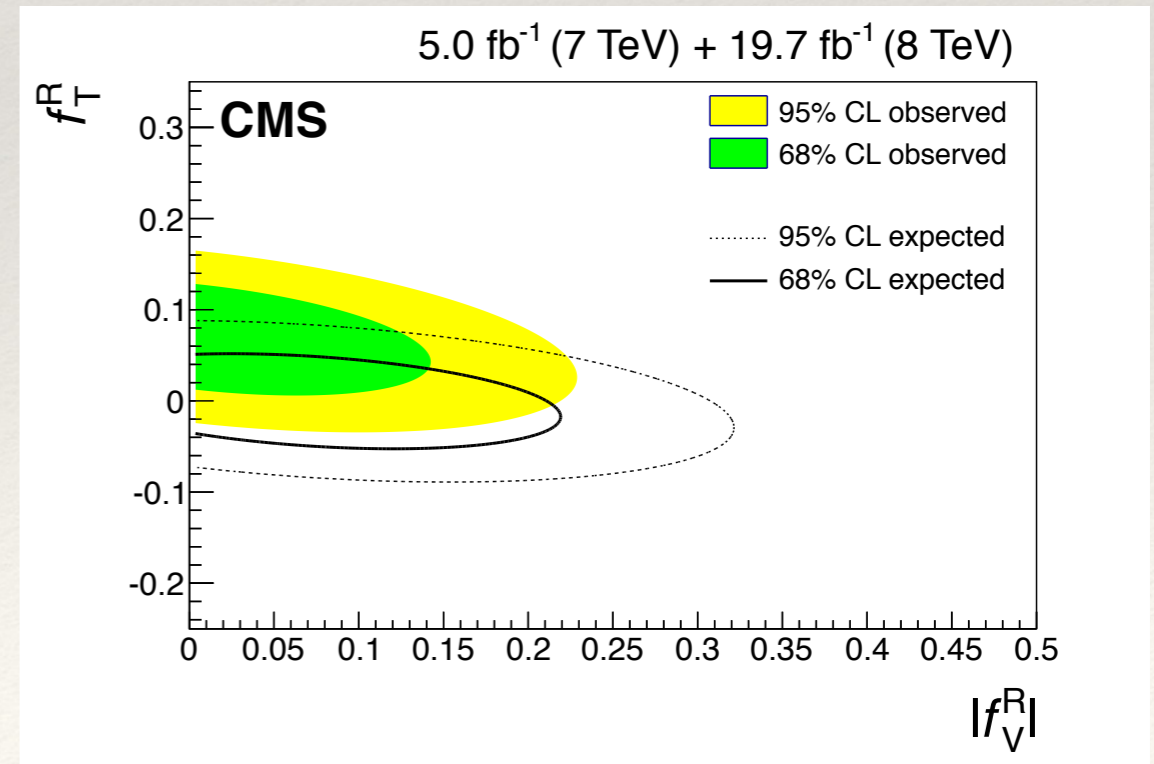
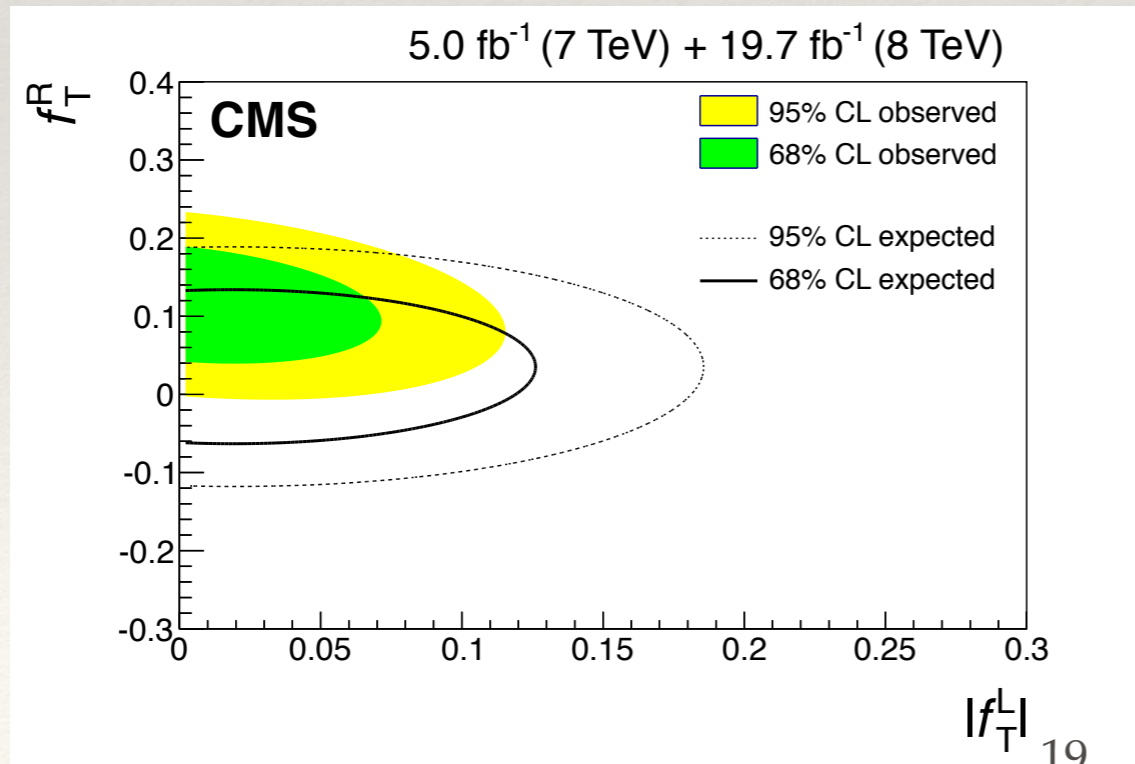
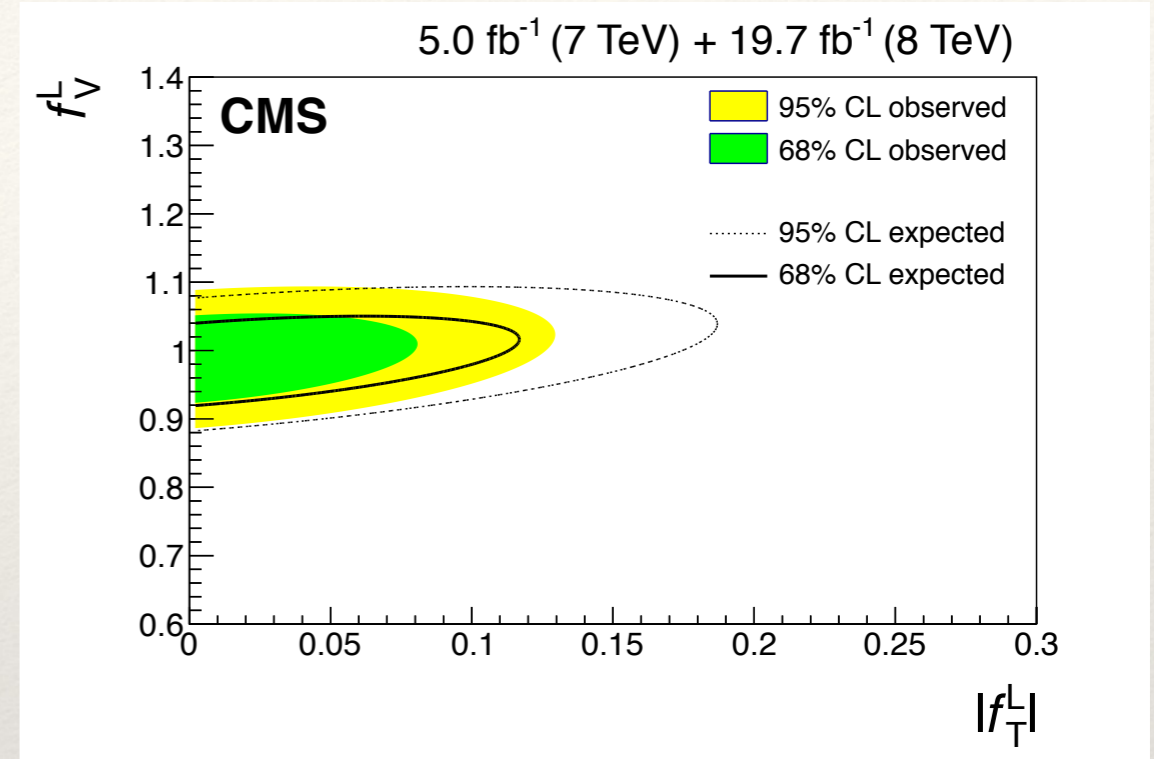
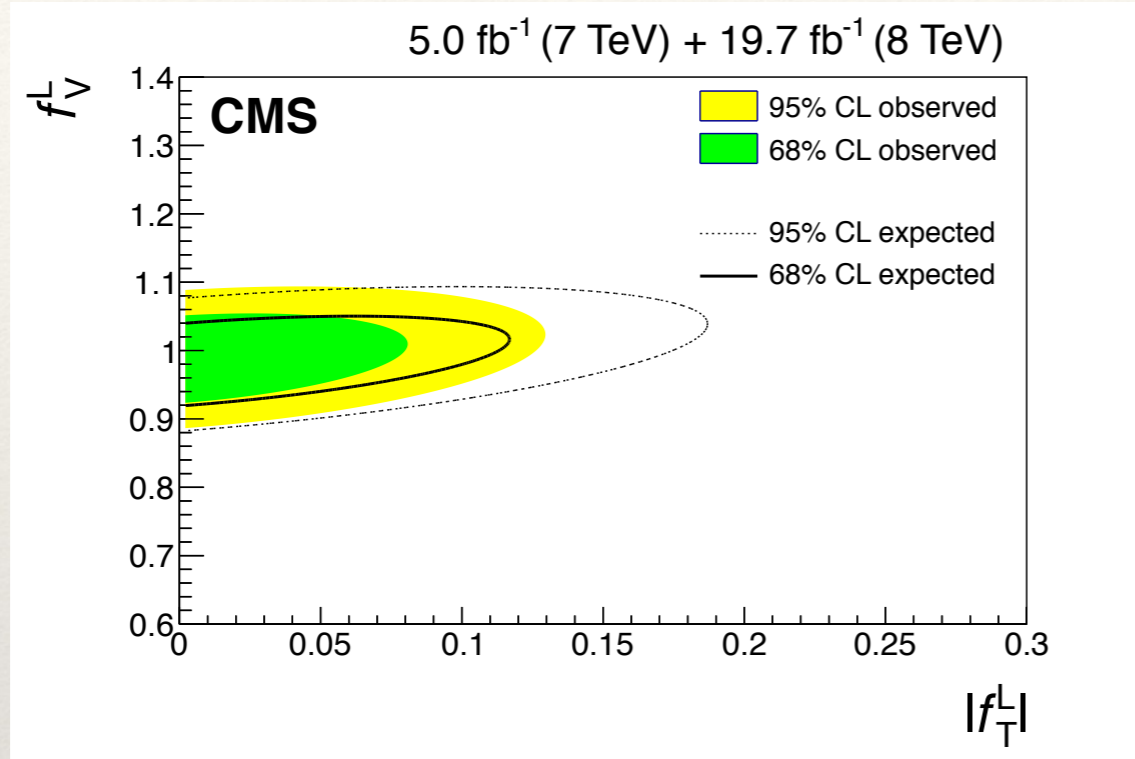
JHEP 02 (2017) 028

$$f_{V=V_L}^L = V_L$$

$$f_{V=V_R}^R = V_R$$

$$f_{T=g_R}^R = g_R$$

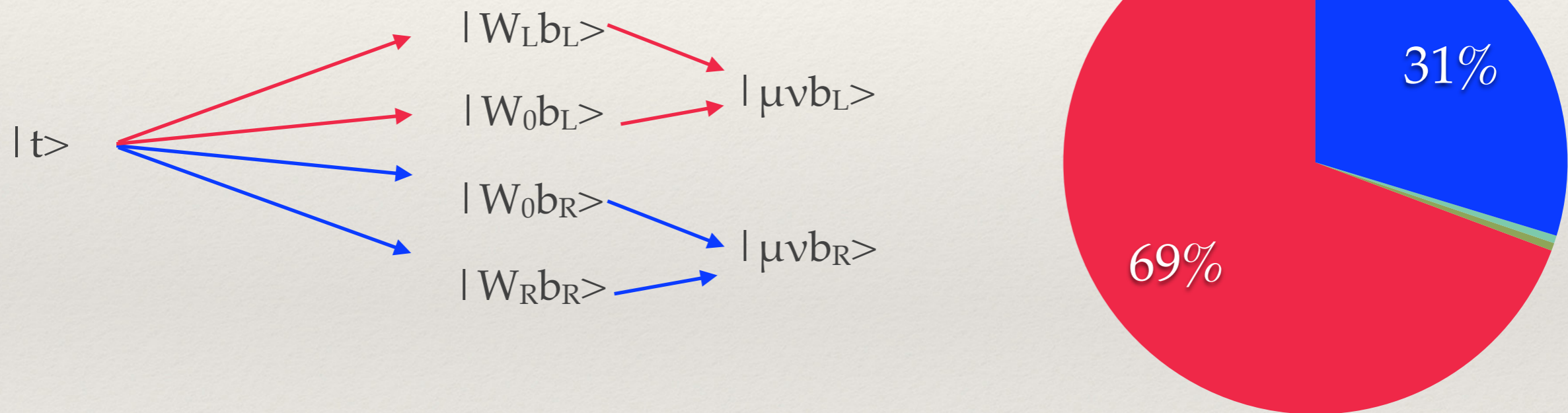
$$f_{T=g_L}^L = g_L$$





# Beyond helicity fractions in single top t-channel

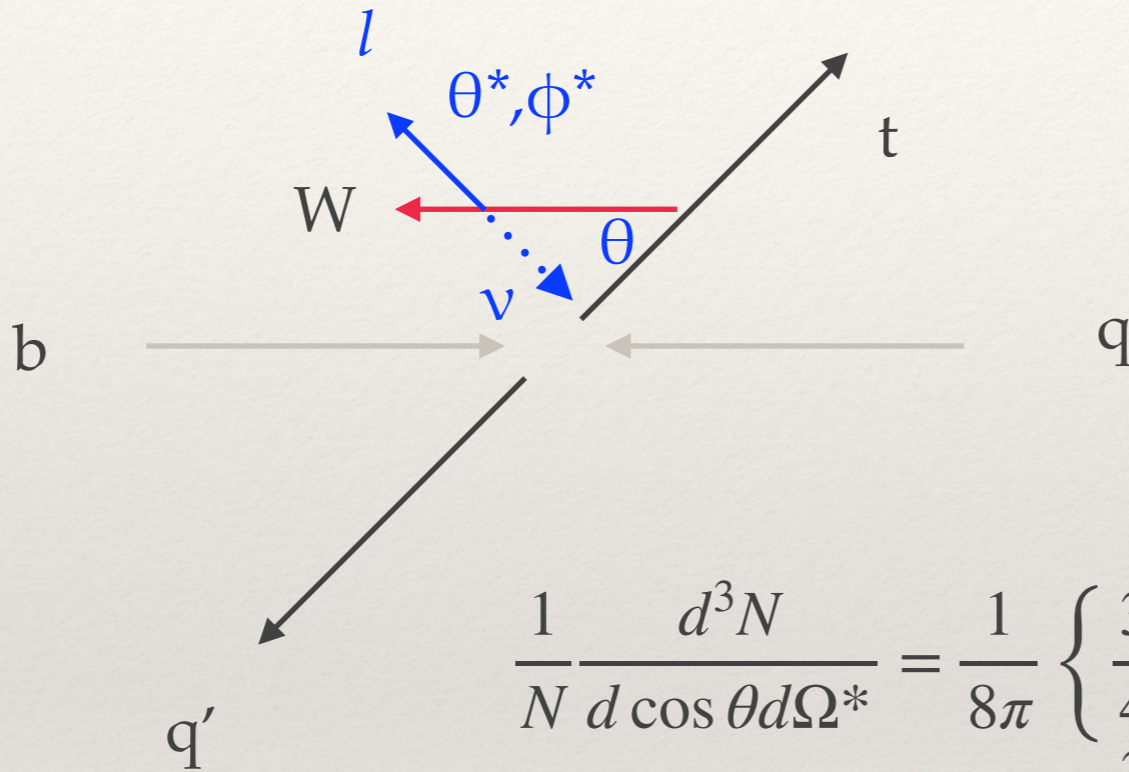
Single top t-channel events have high ( $\sim 90\%$ ) polarization along the spectator quark direction to the V-A structure of the weak interaction. This makes possible a unique set of measurements



Helicity fraction measurements determine the relative strength of three categories (L,R, 0). **One can also separate four categories and determine a relative phase. From there go to constraints on  $V_R$ ,  $g_L$ ,  $g_R$**



# Decay kinematics depend on 3 angles.

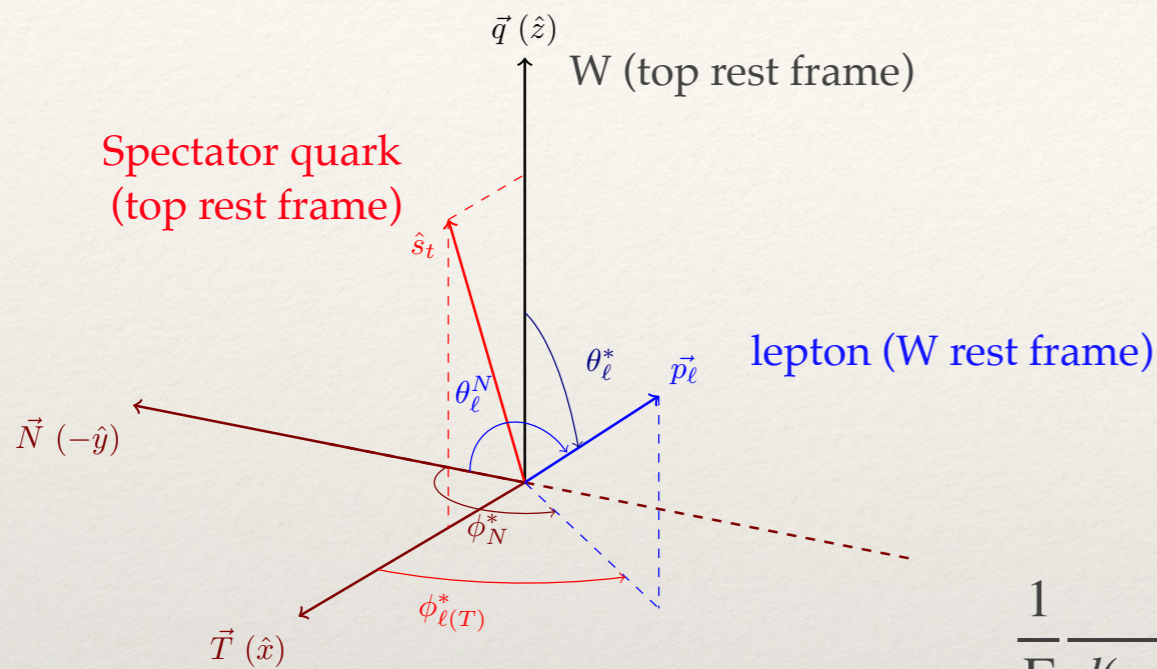


$\theta$ : t decay polar angle  
 $\theta$ : W decay polar angle  
 $\phi^*$ : W decay azimuthal angle

$$\begin{aligned}
 \frac{1}{N} \frac{d^3 N}{d \cos \theta d \Omega^*} &= \frac{1}{8\pi} \left\{ \frac{3}{4} |A_{1,\frac{1}{2}}|^2 (1 + P \cos \theta) (1 + \cos \theta^*)^2 \right. \\
 &\quad \left. + \frac{3}{4} |A_{-1,-\frac{1}{2}}|^2 (1 - P \cos \theta) (1 - \cos \theta^*)^2 \right. \\
 &\quad \left. + \frac{3}{2} \left( |A_{0,\frac{1}{2}}|^2 (1 - P \cos \theta) + |A_{0,-\frac{1}{2}}|^2 (1 + P \cos \theta) \right) \sin^2 \theta^* \right. \\
 &\quad \left. - \frac{3\sqrt{2}}{2} P \sin \theta \sin \theta^* (1 + \cos \theta^*) \operatorname{Re} \left[ e^{i\phi^*} A_{1,\frac{1}{2}} A_{0,\frac{1}{2}}^* \right] \right. \\
 &\quad \left. - \frac{3\sqrt{2}}{2} P \sin \theta \sin \theta^* (1 - \cos \theta^*) \operatorname{Re} \left[ e^{-i\phi^*} A_{-1,-\frac{1}{2}} A_{0,-\frac{1}{2}}^* \right] \right\}
 \end{aligned}$$

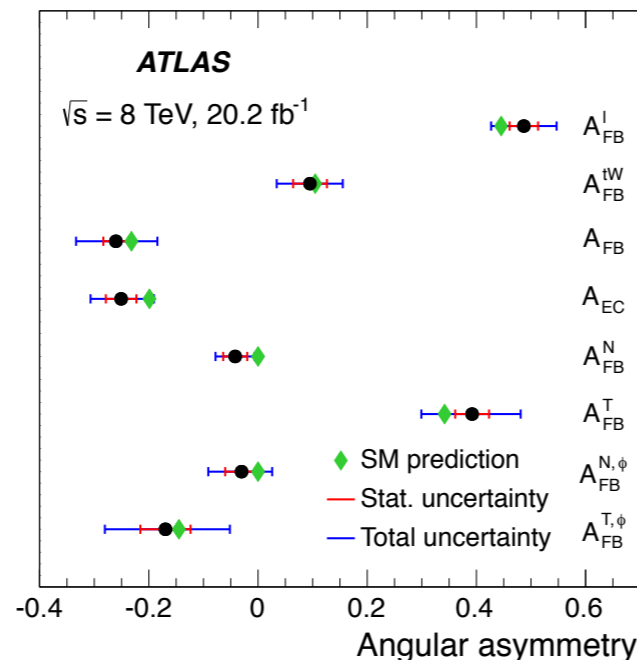
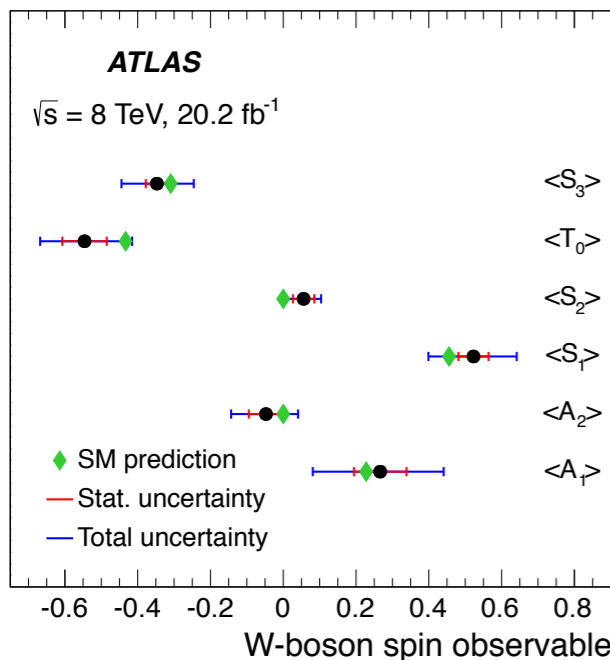


# Asymmetries in single top t-channel



Asymmetry	Angular observable	Polarisation observable	SM prediction
$A_{\text{FB}}^\ell$	$\cos \theta_\ell$	$\frac{1}{2}\alpha_\ell P$	0.45
$A_{\text{FB}}^{tW}$	$\cos \theta_W \cos \theta_\ell^*$	$\frac{3}{8}P(F_R + F_L)$	0.10
$A_{\text{FB}}$	$\cos \theta_\ell^*$	$\frac{3}{4}\langle S_3 \rangle = \frac{3}{4}(F_R - F_L)$	-0.23
$A_{\text{EC}}$	$\cos \theta_\ell^*$	$\frac{3}{8}\sqrt{\frac{3}{2}}\langle T_0 \rangle = \frac{3}{16}(1 - 3F_0)$	-0.20
$A_{\text{FB}}^T$	$\cos \theta_\ell^T$	$\frac{3}{4}\langle S_1 \rangle$	0.34
$A_{\text{FB}}^N$	$\cos \theta_\ell^N$	$-\frac{3}{4}\langle S_2 \rangle$	0
$A_{\text{FB}}^{T,\phi}$	$\cos \theta_\ell^* \cos \phi_T^*$	$-\frac{2}{\pi}\langle A_1 \rangle$	-0.14
$A_{\text{FB}}^{N,\phi}$	$\cos \theta_\ell^* \cos \phi_N^*$	$\frac{2}{\pi}\langle A_2 \rangle$	0

$$\frac{1}{\Gamma} \frac{d\Gamma}{d(\cos \theta_\ell^*) d\phi_\ell^*} = \frac{3}{8\pi} \left\{ \frac{2}{3} + \frac{1}{\sqrt{6}} \langle T_0 \rangle (3 \cos^2 \theta_\ell^* - 1) + \langle S_3 \rangle \cos \theta_\ell^* + \langle S_1 \rangle \cos \phi_\ell^* \sin \theta_\ell^* + \langle S_2 \rangle \sin \phi_\ell^* \sin \theta_\ell^* - \langle A_1 \rangle \cos \phi_\ell^* \sin 2\theta_\ell^* - \langle A_2 \rangle \sin \phi_\ell^* \sin 2\theta_\ell^* \right\}$$



Multiple angular asymmetries measured.

**All consistent with SM.**

CP violation parameter:

$$\text{Im}(g_R) \in [-0.18, 0.06] \quad 95\% \text{C.L.}$$

If all other anomalous couplings zero and  $V_L=1$



# Series of analyses from ATLAS

Double [JHEP 04 (2016) 023] and triple [JHEP 12 (2017) 017] differential decay rates.

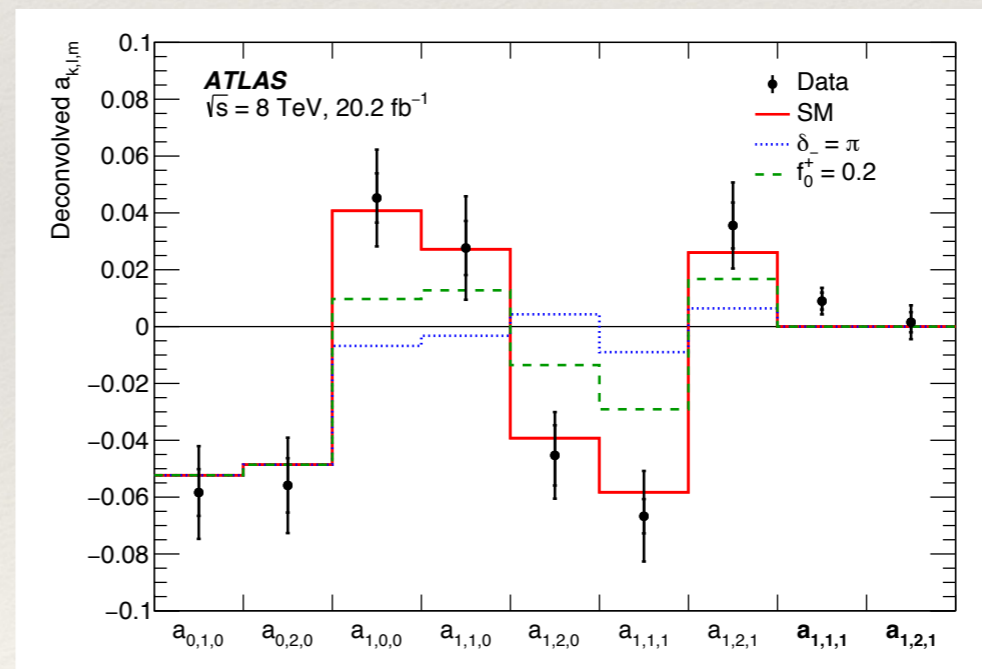
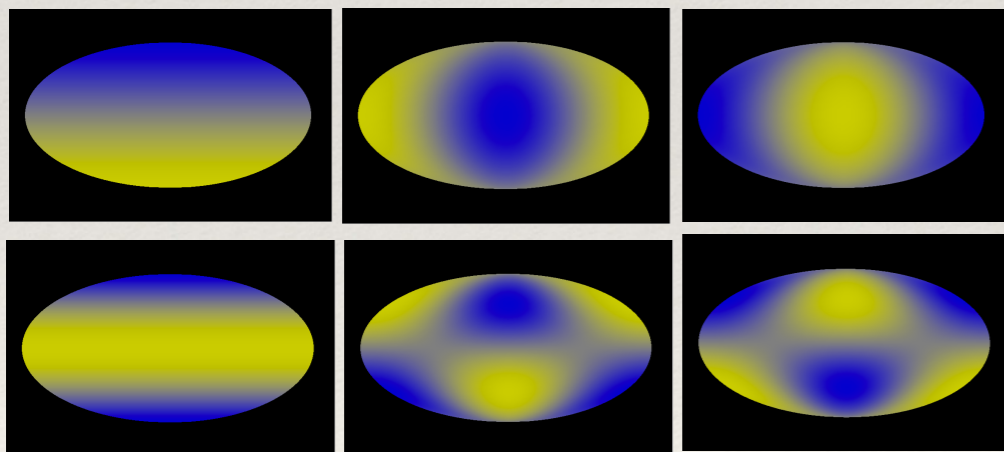
Triple differential cross section:

$$\begin{aligned} \rho(\theta, \theta^*, \phi^*) &\equiv \frac{1}{\Gamma} \frac{d\Gamma}{d\Omega_3} \\ &= a_{k,l}^m M_{k,l}^m(\theta, \theta^*, \phi^*) \end{aligned}$$

$$\begin{aligned} M_{k,l}^m(\theta_1, \theta_2, \phi) &= \sqrt{2\pi} Y_k^m(\theta_1, 0) Y_l^m(\theta_2, \phi) \\ &= \sqrt{2\pi} Y_k^m(\theta_1, \phi) Y_l^m(\theta_2, 0) \end{aligned}$$

Decompose the differential decay rate into orthogonal functions and perform Fourier analysis.

Use Fourier techniques to deconvolve the detector.



[JHEP 12 (2017) 017]



# Helicity fractions & phases with *no assumptions on other parameters*

$f_0^+$ : the fraction of  $b$ 's which are right-handed in events with longitudinal  $W$ 's

$$f_0^+ < 0.041 \text{ (68\% CL)}$$

$$f_0^+ < 0.085 \text{ (95\% CL) } \textit{unique measurement}$$

$f_1^+$ : the fraction of  $b$ 's which are right-handed in events with transverse  $W$ 's.

$$f_1^+ < 0.053 \text{ (68\% CL)}$$

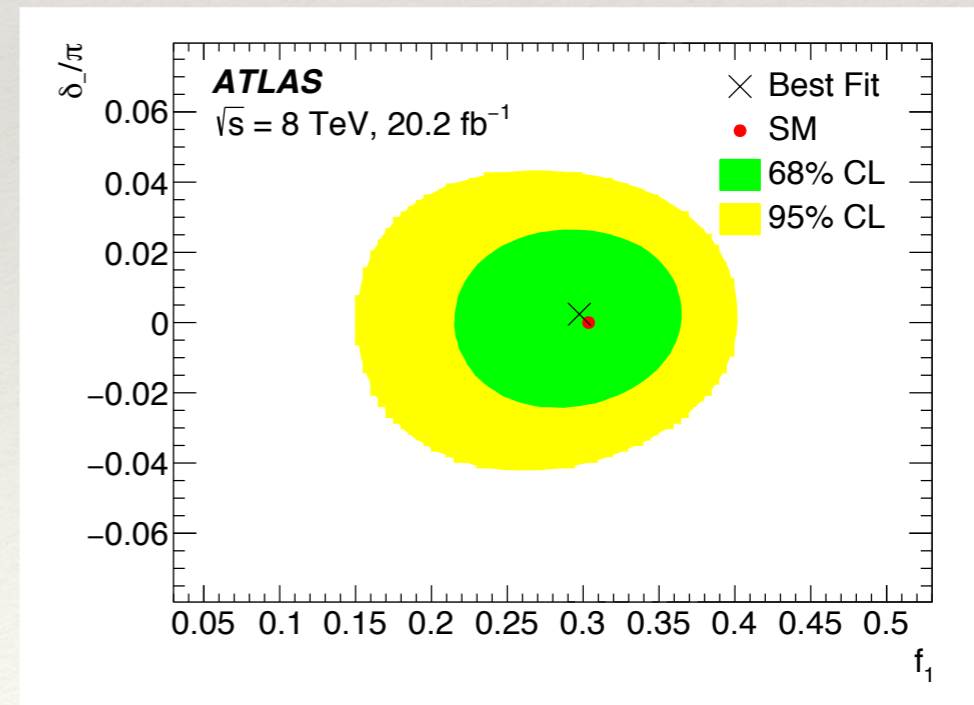
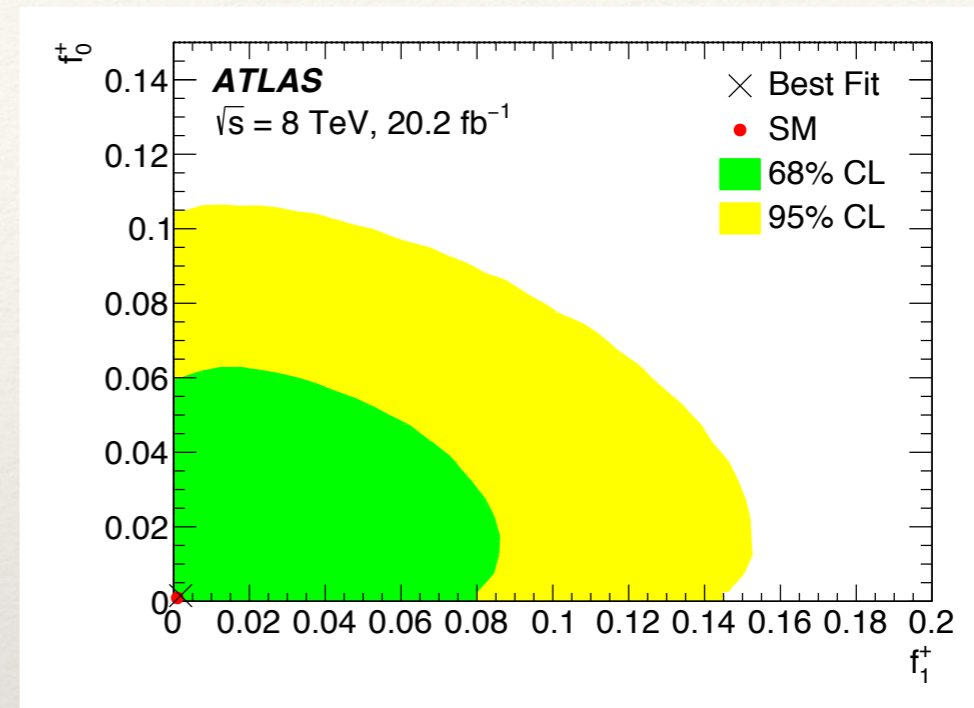
$$f_1^+ < 0.120 \text{ (95\% CL)}$$

$f_1=1-F_L$ : Also measured in standard  $W$  boson polarization analyses.

$\delta_-$ : If nonzero, could signify CP violation in top quark decay.

$$f_1 = 0.296_{-0.023}^{+0.020} \text{ (stat.) } {}_{-0.046}^{+0.043} \text{ (syst.)} = 0.296_{-0.051}^{+0.048}$$

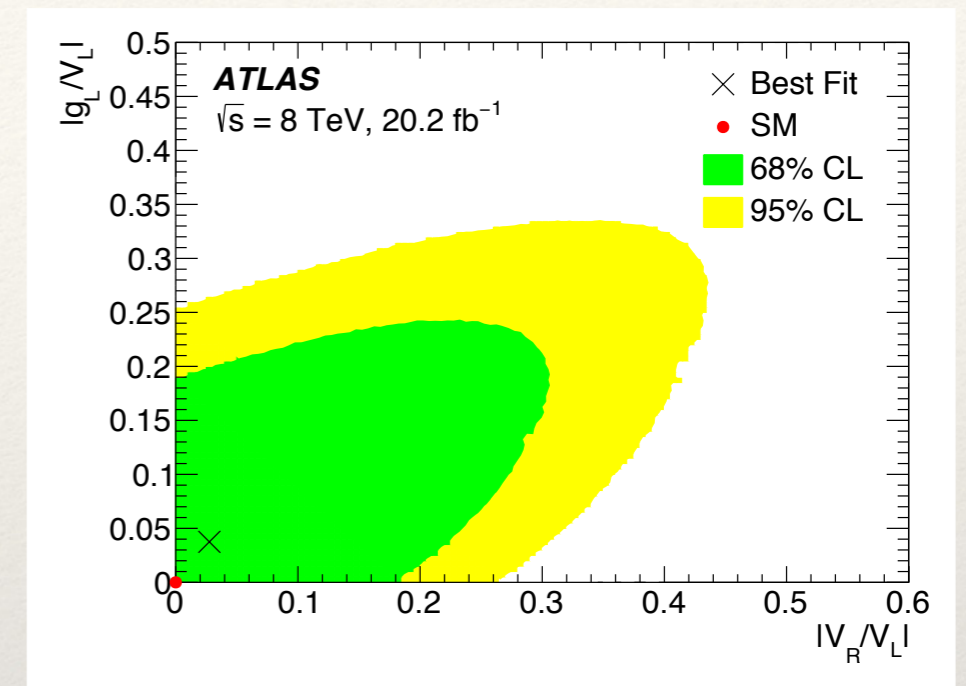
$$\delta_- = 0.002\pi_{-0.014\pi}^{+0.013\pi} \text{ (stat.) } {}_{-0.011\pi}^{+0.010\pi} \text{ (syst.)} = 0.002\pi_{-0.017\pi}^{+0.016\pi}$$



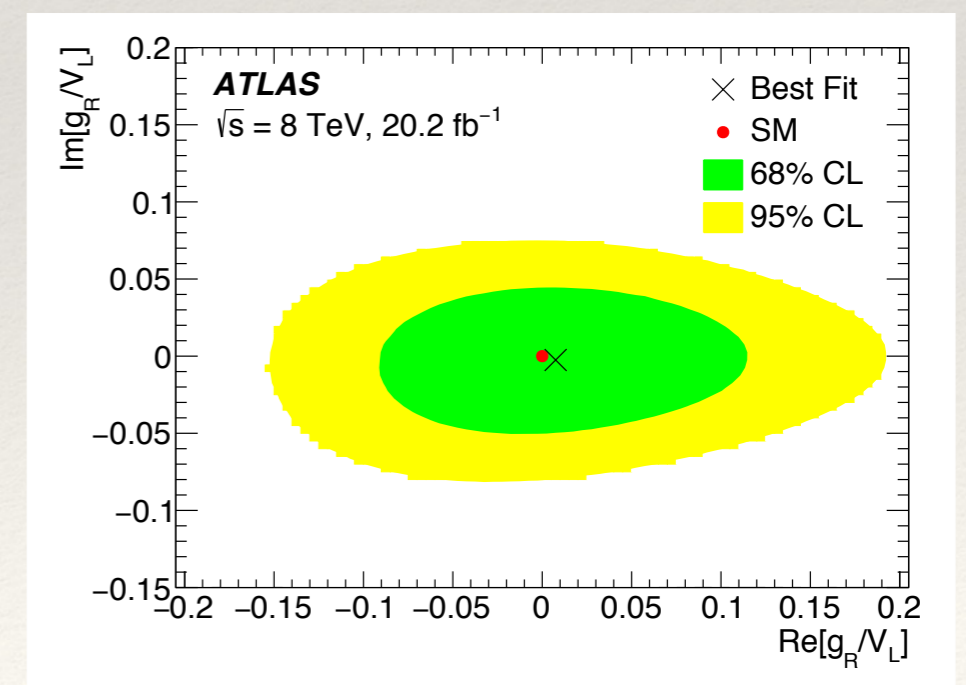


# Anomalous couplings with *no assumptions on other parameters*.

- $|V_R/V_L| < 0.23$  (68% CL)
- $|V_R/V_L| < 0.37$  (95% CL)
  
- $|g_L/V_L| < 0.19$  (68% CL)
- $|g_L/V_L| < 0.29$  (95% CL)
  
- Tighter limits exist from  $b \rightarrow s\gamma$  and from W helicity fractions in  $t\bar{t}$  events, but with assumptions on other parameters.



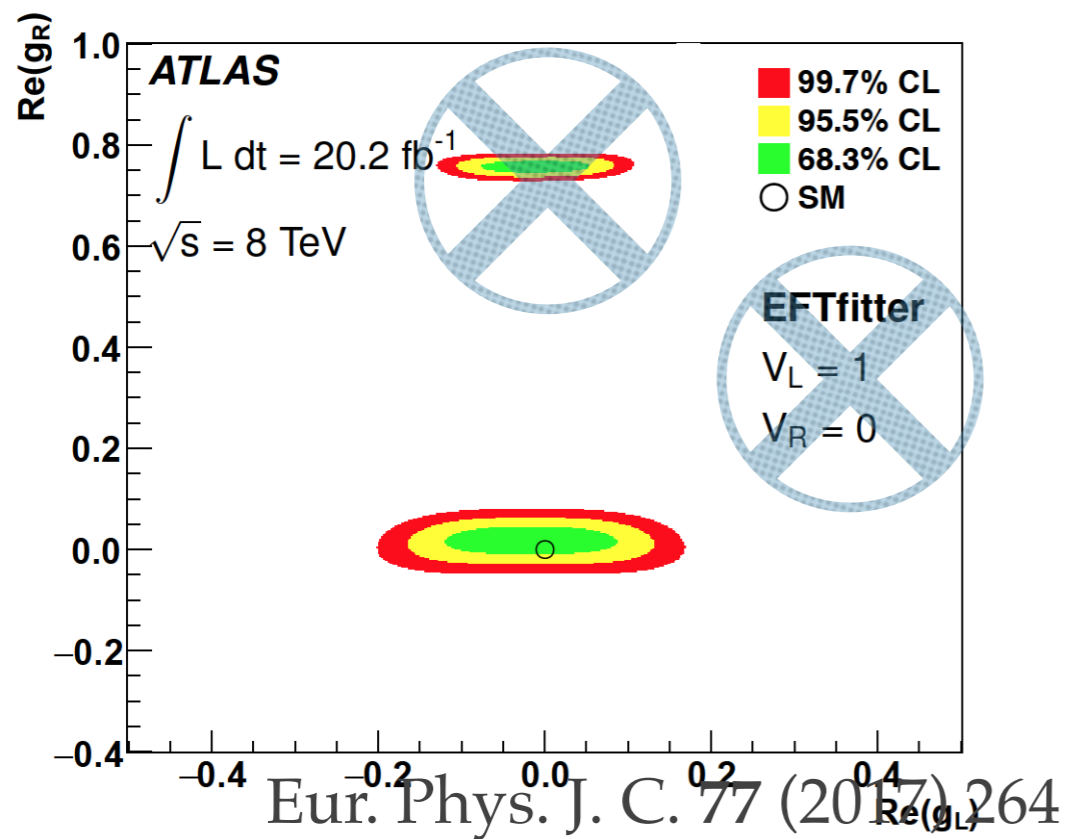
$$\text{Re}\left[\frac{g_R}{V_L}\right] \in [-0.12, 0.17] \quad \text{and} \quad \text{Im}\left[\frac{g_R}{V_L}\right] \in [-0.07, 0.06].$$





# Triple-differential decay rate removes ambiguity from W-boson helicity fraction measurements in $t\bar{t}$ events:

The triple differential decay rate measurement [JHEP 12 (2017) 017] eliminates the secondary, BSM solution of the standard helicity fraction measurement and does so without assumptions on any parameters of the  $Wtb$  vertex.



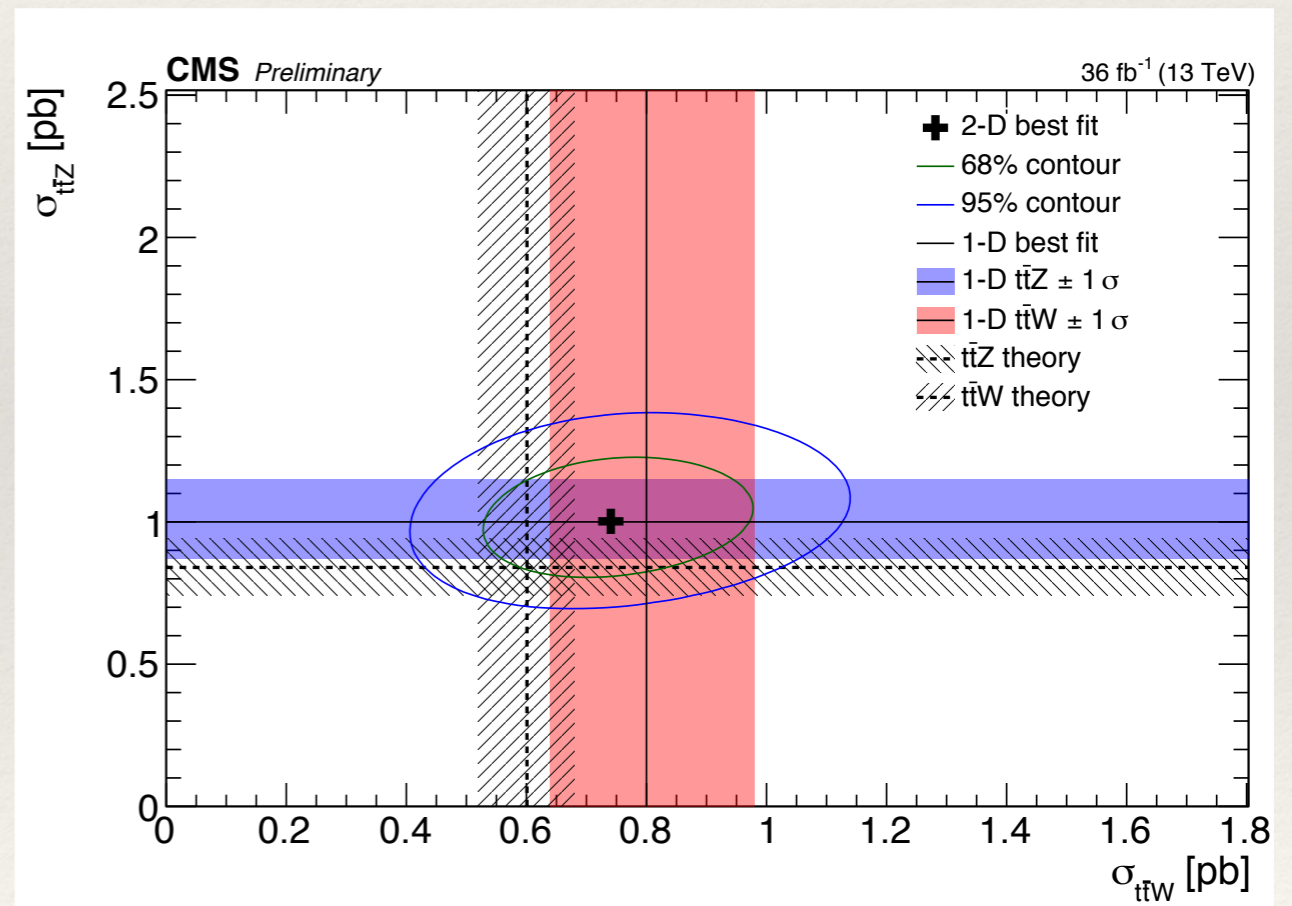
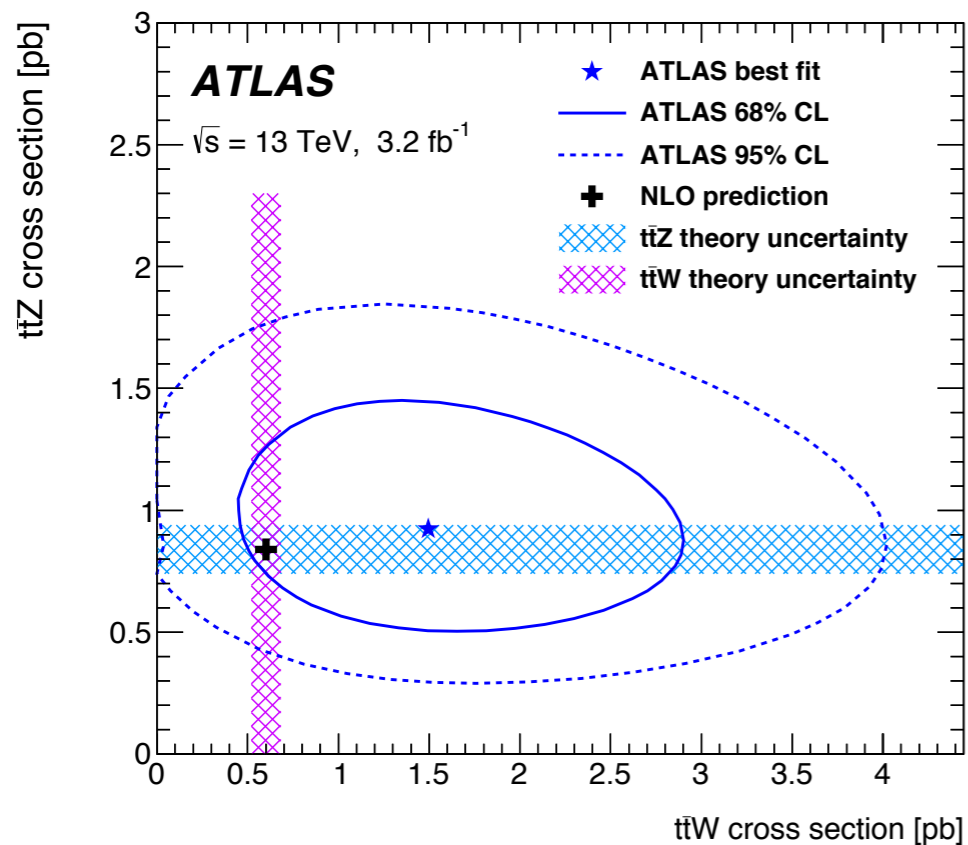
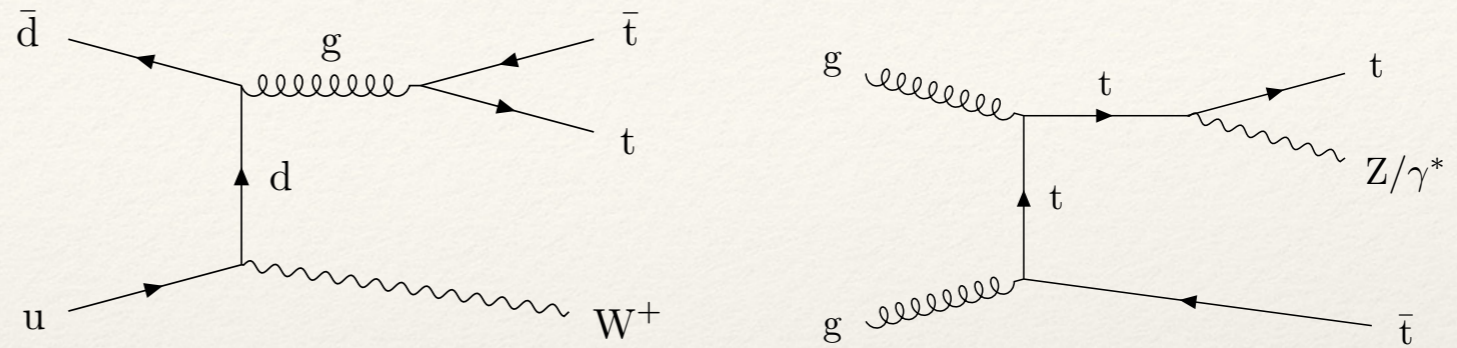
## Sources of systematic error:

Source	Helicity parameters		Coupling ratios	
	$\sigma(f_1)$	$\sigma(\delta_-)/\pi$	$\sigma(\text{Re}[g_R/V_L])$	$\sigma(\text{Im}[g_R/V_L])$
Statistical	0.022	0.013	0.030	0.027
Jets	0.029	0.007	0.039	0.009
Leptons	0.014	0.002	0.017	<0.001
$E_T^{\text{miss}}$	<0.001	<0.001	<0.001	<0.001
Generator	0.027	0.006	0.030	0.010
Parton shower and hadronisation	0.004	0.003	<0.001	0.003
PDF variations	0.008	0.004	<0.001	<0.001
Background normalisation	<0.001	<0.001	<0.001	<0.001
Multijet normalisation	<0.001	<0.001	<0.001	<0.001
W+jets shape	0.015	0.005	0.007	0.009
Luminosity	<0.001	<0.001	<0.001	<0.001
MC sample sizes	0.009	0.006	<0.001	0.013
Other	<0.001	<0.001	<0.001	<0.001
Total systematic uncertainty	0.044	0.010	0.061	0.017
<b>Total</b>	<b>0.049</b>	<b>0.017</b>	<b>0.068</b>	<b>0.032</b>



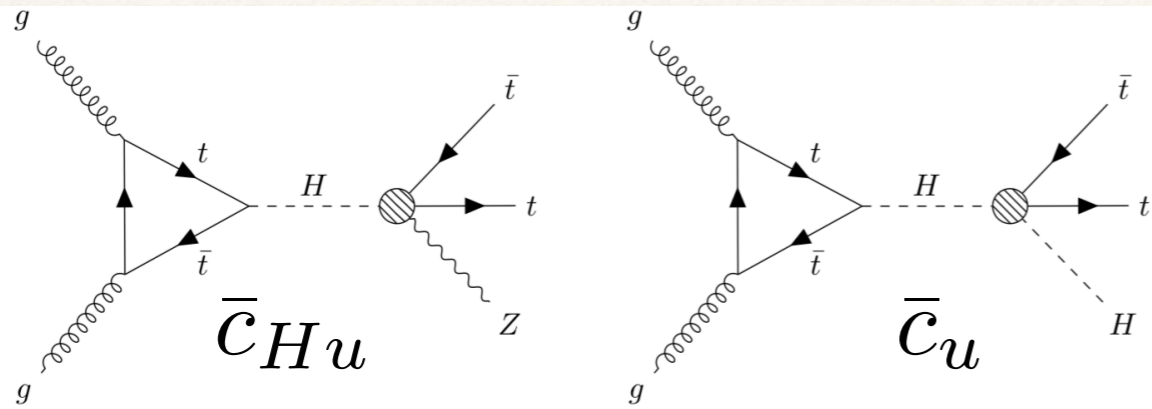
# New information on the $t\bar{t}Z$ , $t\bar{t}W^\pm$ interactions

Signal:  
dilepton ( $t\bar{t}W$ )  
trilepton, 4-lepton ( $t\bar{t}Z$ )

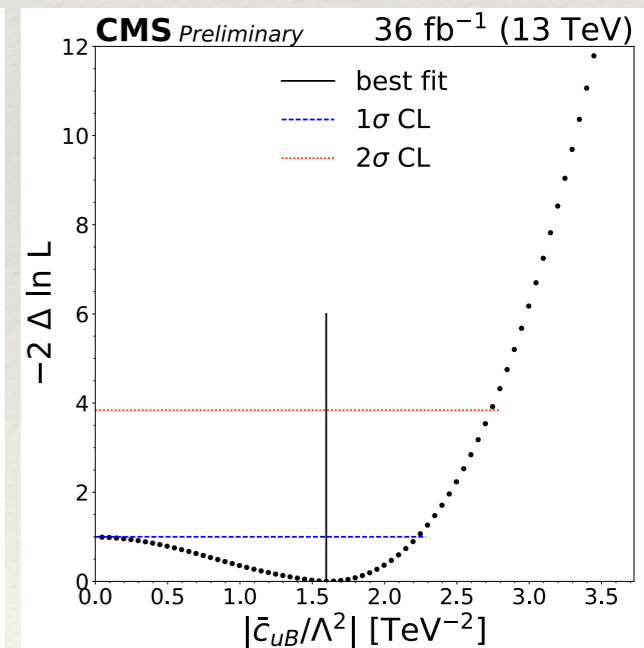
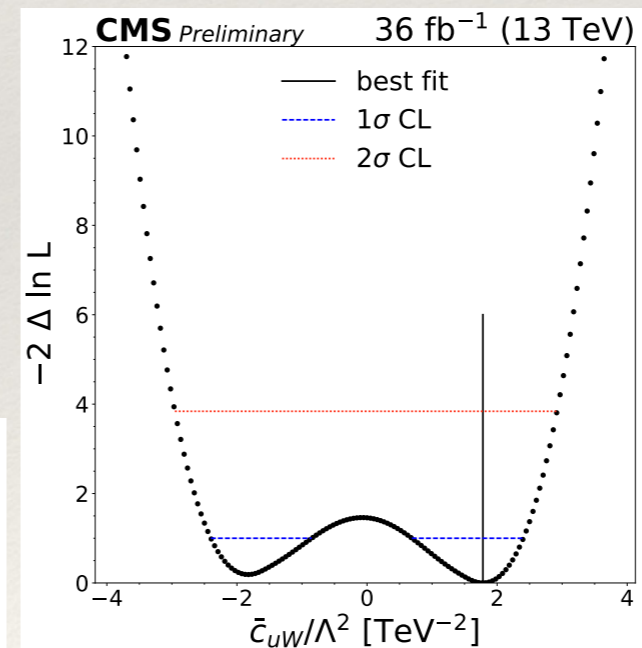
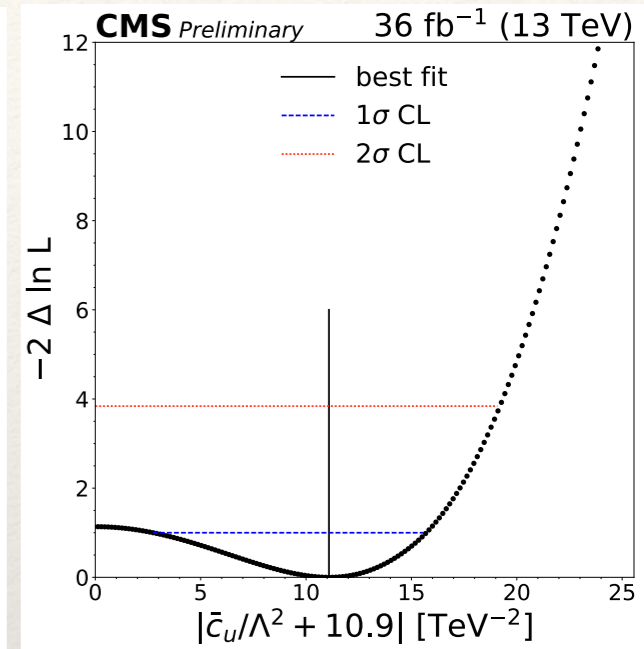
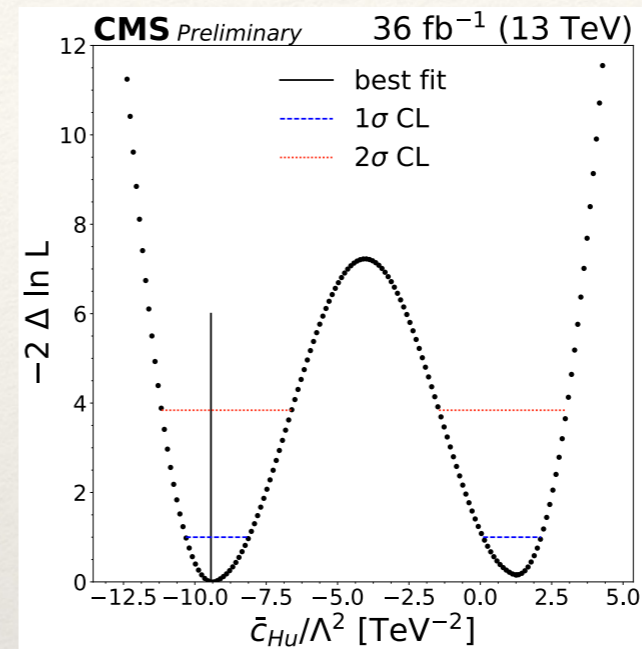
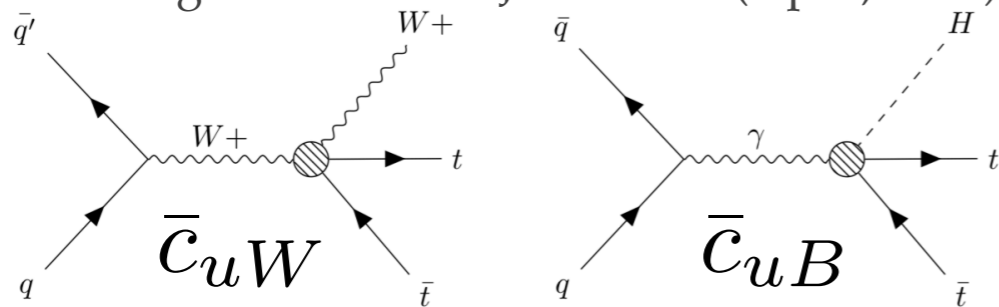




# CMS $t\bar{t}Z$ & $t\bar{t}W$ analysis



Naming scheme from JHEP 2014 (April, 2014) 110



CMS-PAS-TOP-17-005

Wilson coefficient	Best fit [TeV <sup>-2</sup> ]	1σ CL [TeV <sup>-2</sup> ]	2σ CL [TeV <sup>-2</sup> ]
$ \bar{c}_{uB}/\Lambda^2 + 0.1 \text{ TeV}^{-2} $	3.2	[0.0, 4.4]	[0.0, 5.4]
$ \bar{c}_u/\Lambda^2 + 18.5 \text{ TeV}^{-2} $	19.1	[5.0, 26.4]	[0.0, 32.5]
$\bar{c}_{uW}/\Lambda^2$	3.0	[-4.1, -1.5] and [1.2, 4.1]	[-5.1, 5.0]
$\bar{c}_{Hu}/\Lambda^2$	-9.4	[-10.3, -8.1] and [0.1, 2.1]	[-11.1, -6.6] and [-1.4, 3.0]

Discussed in more detail in the talk of Olga Bylund in parallel session

(Likelihood contours assume all other Wilson coefficients are zero.)



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# Conclusions

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- ❖ Measurement of  $t\bar{t}$ , single top,  $ttZ$  and  $ttW$  processes are yielding precision information on  $g_{tt}$ ,  $W_{tb}$ ,  $ttZ$ ,  $ttW^\pm$  interactions in a corner of the standard model not fully explored till now.
- ❖ All measurements consistent with the standard model, but hints of an anomaly at the  $3.2 \sigma$  level in the ATLAS measurement of spin correlations at 13 TeV
- ❖ Measurements are now being cast in the form of constraints on Wilson coefficients of EFT operators.
- ❖ More precision to come with the full 13 TeV dataset, Run 3, and the HL-LHC
  - ❖ Spin correlation measurement at 13 TeV with full dataset
  - ❖ EFT approach becoming more common.
  - ❖ More complete analyses of single top and  $t\bar{t}$  angular distributions
  - ❖ Greater sensitivity to rare decay modes  $ttW$  and  $ttZ$ .
  - ❖ Challenge: gain control over systematic errors.