

# Spontaneous SUSY breaking in natural SO(10) GUT

Nobuhiro Maekawa (KMI, Nagoya Univ. )  
with Y. Omura, Y. Shigekami, M. Yoshida

arXiv:1808.??????

- 1. Natural (anomalous U(1)) GUT**
- 2. Sp. SUSY breaking in natural GUT**
- 3. SUGRA effects induce gaugino masses**
- 4. Predictions**
- 5. Summary and discussion**

# Natural GUT (Anomalous U(1) GUT)

N.M.01

N.M.&Yamashita,02

1. Doublet-triplet splitting and realistic quark and lepton masses and mixings are realized under **natural** assumption. **Generic interactions (incl. higher dim. Interactions) are introduced with O(1) coefficients. (No  $U(1)_R$ .)**

Once we fix the symmetry of the model, we can predict everything except O(1) coefficients.

2. Natural gauge coupling unification.

Natural GUT gives a new explanation for the success of gauge coupling unification in MSSM.

**The cutoff scale should be taken to be the usual GUT scale.**

$$\Lambda \sim \Lambda_{\text{GUT}}$$

# VEVs in natural GUT?

- ◆ VEVs are determined by the symmetry as

$$\langle Z_+^i \rangle = 0 \quad z_+^i > 0 \quad (i = 1, 2, \dots, N_+)$$

$$\langle Z_-^i \rangle \sim \lambda^{-z_-^i} \quad z_-^i \leq 0 \quad (i = 1, 2, \dots, N_-)$$

$$\lambda = \xi \sim 0.22 \quad \Lambda = 1 \quad \xi: \text{FI parameter}$$

$F_{Z_-} = 0$  is automatically satisfied.

- ◆  $F_{Z_+} = 0, D_A = 0$  determine the VEVs of  $Z_-$

Kim-N.M.-Nishino-Sakurai08

$$N_+ + 1 > N_- \quad \text{Overdetermined meta-stable SUSY breaking}$$

Natural GUT with sp. SUSY breaking

$$N_+ + 1 = N_- \quad \text{Generically no flat direction (all massive)}$$

Natural GUT

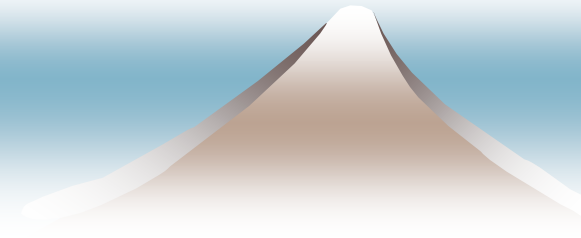
$$N_+ + 1 < N_- \quad \text{Flat direction (massless modes appear)}$$

# Natural SO(10) GUT

## ◆ Natural SO(10) GUT

$SO(10)$	<i>negative</i>
45	$A(a = -1, -)$
16	$C(c = -4, +)$
$\overline{16}$	$\bar{C}(\bar{c} = -1, +)$
10	$H(h = -3, +)$

The minimal Higgs content to break  $SO(10)$  into  $G_{SM}$ .



# Natural SO(10) GUT

## ◆ Natural SO(10) GUT

$SO(10)$	<i>negative</i>	<i>positive</i>
45	$A(a = -1, -)$	$A'(a' = 3, -)$
16	$C(c = -4, +)$	$C'(c' = 3, -)$
$\overline{16}$	$\bar{C}(\bar{c} = -1, +)$	$\bar{C}'(\bar{c}' = 6, -)$
10	$H(h = -3, +)$	$H'(h' = 4, -)$

The minimal Higgs sector in anomalous U(1) (natural) GUT.

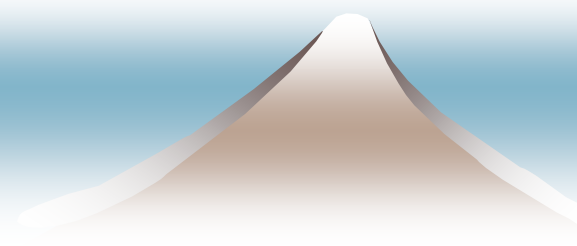


# Natural SO(10) GUT

## ◆ Natural SO(10) GUT

$SO(10)$	<i>negative</i>	<i>positive</i>
45	$A(a = -1, -)$	$A'(a' = 3, -)$
16	$C(c = -4, +)$	$C'(c' = 3, -)$
$\overline{16}$	$\bar{C}(\bar{c} = -1, +)$	$\bar{C}'(\bar{c}' = 6, -)$
10	$H(h = -3, +)$	$H'(h' = 4, -)$
1	$Z, \bar{Z}(Z = \bar{Z} = -2, -), Z'(z' = 5, +)$	

The doublet triplet splitting problem can be solved in the almost minimal Higgs content.



# Natural SO(10) GUT

## ◆ Natural SO(10) GUT

$SO(10)$	<i>negative</i>	<i>positive</i>	<i>matter</i>
45	$A(a = -1, -)$	$A'(a' = 3, -)$	
16	$C(c = -4, +)$	$C'(c' = 3, -)$	$\Psi_a(\psi_1 = \frac{9}{2}, \psi_2 = \frac{7}{2}, \psi_3 = \frac{3}{2}, +)$
$\overline{16}$	$\bar{C}(\bar{c} = -1, +)$	$\bar{C}'(\bar{c}' = 6, -)$	
10	$H(h = -3, +)$	$H'(h' = 4, -)$	$T(t = \frac{5}{2}, +)$
1	$Z, \bar{Z}(Z = \bar{z} = -2, -), Z'(z' = 5, +)$		

The doublet triplet splitting problem can be solved.

Realistic quark and lepton masses and mixings are obtained just by introducing all terms which are allowed by symmetry with  $O(1)$  coefficients.

# Sp. SUSY breaking in natural GUT

## ◆ Natural SO(10) GUT

$SO(10)$	<i>negative</i>	<i>positive</i>	<i>matter</i>
45	$A(a = -1, -)$	$A'(a' = 3, -)$	
16	$C(c = -4, +)$	$C'(c' = 3, -)$	$\Psi_a(\psi_1 = \frac{9}{2}, \psi_2 = \frac{7}{2}, \psi_3 = \frac{3}{2}, +)$
$\overline{16}$	$\bar{C}(\bar{c} = -1, +)$	$\bar{C}'(\bar{c}' = 6, -)$	
10	$H(h = -3, +)$	$H'(h' = 4, -)$	$T(t = \frac{5}{2}, +)$
1	$Z, \bar{Z}(Z = \bar{z} = -2, -), Z'(z' = 5, +)$		

◆ Let us decrease one negatively charged field.

◆ One F of  $W_{C'} = \bar{C}(A + Z)C'$ ,  $W_{\bar{C}'} = \bar{C}'(A + Z)C$  is not vanishing.

For alignment by Barr-Raby mechanism is sufficient if  $F_{C'} = 0$ . Barr-Raby 97

$$\frac{\partial W_{\bar{C}'}}{\partial \bar{C}'} = (A + Z)C \sim \lambda^{\bar{c}' + \frac{1}{2}(c - \bar{c})} = \lambda^{\frac{9}{2}} \sim (2 \times 10^{13} \text{ GeV}) \quad \text{too large}$$

◆ SUSY breaking scale can be smaller by choosing larger  $\bar{c}'$ .



# Gauge messenger gives sizable gaugino mass?

- Massive vector multiplets do not respect SUSY ( $F_{\bar{C}'} \neq 0$ )  
 Generically they induce  $m_{1/2} \sim c_i \frac{\alpha_i}{4\pi} \frac{F_{\bar{C}'}}{\Lambda} \sim 10^{-2} m_0$  (gauge messenger)
- Unfortunately, induced gaugino masses are quite small.  
 because of approximate  $U(1)_R$  symmetry.

$SO(10)$	<i>negative</i>	<i>positive</i>	
45	$A(a = -1, -)$	$A'(a' = 3, -)$	$\langle A \rangle \neq 0$
16	$C(c = -4, +)$	$C'(c' = 3, -)$	$\langle F_{C'} \rangle \neq 0$
$\overline{16}$	$\bar{C}(\bar{c} = -1, +)$	$\bar{C}'(\bar{c}' = 6, -)$	
10	$H(h = -3, +)$	$H'(h' = 4, -)$	massive chiral multiplets do not
1	$Z(Z = -2, -),$	$Z'(z' = 5, +)$	respect SUSY but $m_{1/2} \sim m_0^2/\Lambda$
$U(1)_R$	0	$2(F_{C'}: 0)$	Very small $\langle Z' \rangle, \langle F_Z \rangle$

Very small  $U(1)_R$  breaking like  $\lambda^{c'+\bar{c}'} \bar{C}' C'$  must be picked up for gaugino mass.

Anomaly mediation gives  $m_{1/2} \sim 10^{-2} m_{3/2} \sim 10^{-5} m_0$ . ( $m_{3/2} \sim F_{\bar{C}'}/M_{Pl} \sim 10^{-3} m_0$ )

Ten years ago, we gave up to build model because of too small gaugino mass.

# SUGRA effects induce $m_{1/2} \sim m_{3/2}$

N.M.-Omura-Shigekami-Yoshida17, talk by Omura

- ◆ R symmetry breaking  $\langle W \rangle$  gives larger contribution to gaugino masses
- ◆ SUSY breaking spectrum becomes

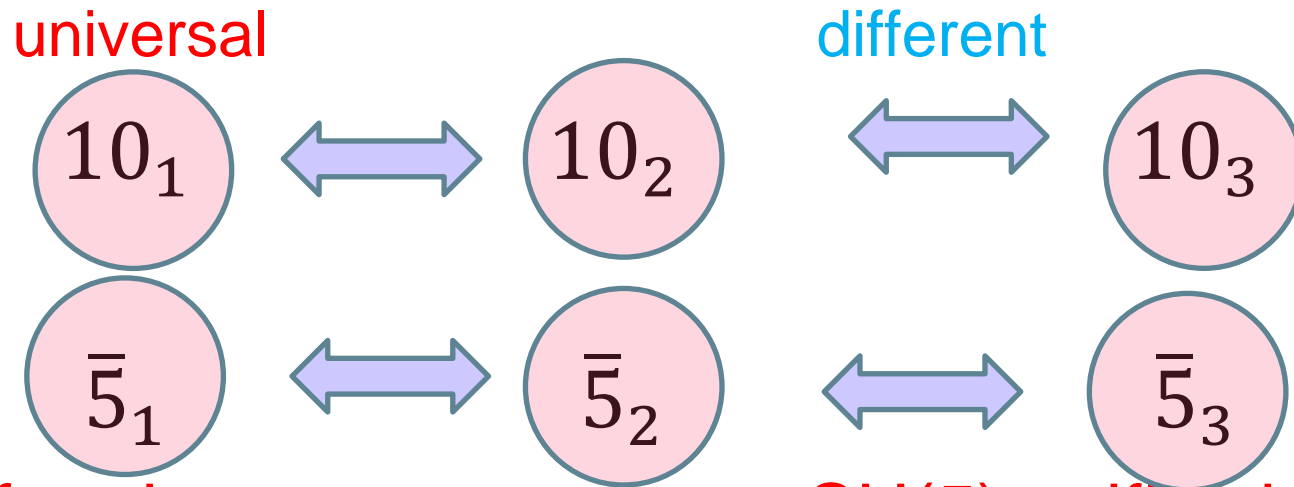
$\bar{c}'$	$F_{\bar{c}'}/\Lambda$	$m_{1/2} \sim m_{3/2}$	$m_0 \sim \sqrt{D_A}$	
18	200 TeV	2TeV	2000TeV	
19	40 TeV	400 GeV	400TeV	

- ◆ High scale SUSY is predicted. ( $D_A$  dominates)  
Roughly  $m_{1/2} \sim 1 \text{ TeV}$ ,  $m_0 \sim (100-1000) \text{ TeV}$
- ◆ No SUSY flavor and CP problem.

# “Direct” signature for GUT

- ◆  $D$  term dominates sfermion masses.

$$\begin{aligned}\tilde{m}_{10}^2 &\sim \left(\frac{9}{2}, \frac{7}{2}, \frac{3}{2}\right) D_A + D_V & SO(10) \supset SU(5) \times U(1)_V \\ \tilde{m}_{\bar{5}}^2 &\sim \left(\frac{9}{2}, \frac{5}{2}, \frac{7}{2}\right) D_A + (-3, 2, -3) D_V\end{aligned}$$



- ◆ **Sfermion masses respect SU(5) unification!**  
They can be a direct signature of unification of matter in SU(5) GUT.
- ◆ Sfermion masses are fixed by  $D_A$  and  $D_V$ .

# Predictions from $E_6$ GUT

- ◆  $E_6 \supset SO(10) \times U(1)_{V'}$ , has 3  $D$  terms

$$\tilde{m}_{10}^2 \sim \left(\frac{9}{2}, \frac{7}{2}, \frac{3}{2}\right) D_A + D_{V'} + D_V$$

$$\tilde{m}_5^2 \sim \left(\frac{9}{2}, \frac{9}{2}, \frac{7}{2}\right) D_A + (1, -2, 1) D_{V'} + (-3, 2, -3) D_V$$

Bando-N.M.01  
N.M.-Yamashita 02

- ◆  $E_6 \times SU(2)_F$  has 4  $D$  terms

$$\tilde{m}_{10}^2 \sim \left(4, 4, \frac{3}{2}\right) D_A + D_{V'} + D_V + \frac{1}{2} (1, -1, 0) D_F$$

$$\tilde{m}_5^2 \sim (4, 4, 4) D_A + (1, -2, 1) D_{V'} + (-3, 2, -3) D_V + \frac{1}{2} (1, 1, -1) D_F$$

N.M.02  
Ishiduki-Kim-N.M.-Sakurai 09  
N.M.-Muramatsu-Shigekami 14

- ◆ The sfermion mass scale is much smaller than the GUT scale, although it is too large to reach by experiments in near future.
- ◆ Various GUT can be tested.

# An interesting prediction (preliminary)

- ◆ Long-lived heavy electron (R-parity odd)

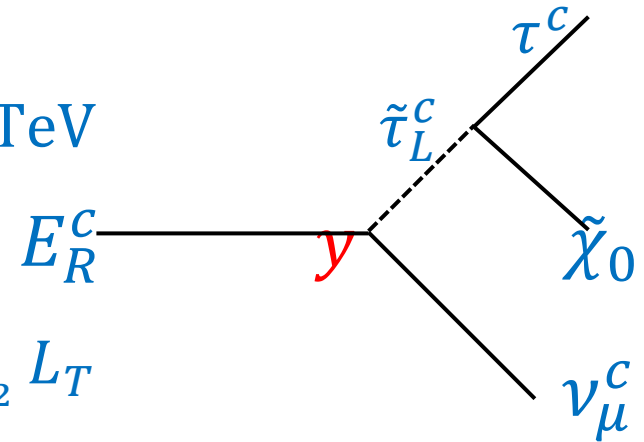
Lightest particle in Higgs sector is  $E_R^c + \overline{E_R^c}$  in  $16_{C'} + \overline{16}_{\overline{C}'}$

Roughly we take

$$m_0 \sim 1000 \text{ TeV}, m_{1/2} \sim 1 \text{ TeV}, m_{E_R^c} \sim 1 \text{ TeV}$$

- ◆ Decay mode is  $\tau^c \nu_\mu^c \tilde{\chi}_0$  or  $\mu^c \nu_\tau^c \tilde{\chi}_0$

$$y = \lambda^{c'+\psi_2+t}, \quad 16_{C'}, 16_{\psi_2}, 10_T \rightarrow E_R^c L_{\psi_2} L_T$$



- ◆  $\tau_{E_R^c} \sim O(1) \text{ sec} \left( \frac{10^{-6}}{y} \right)^2 \left( \frac{m_0}{1000 \text{ TeV}} \right)^4 \left( \frac{1 \text{ TeV}}{m_{E_R^c}} \right)^5 \text{ sec}$

$\tau < 1$  is needed for BBN.

- ◆ LHC gives a constraint for long-lived charged particle.

$$m_{E_R^c} > 574 \text{ GeV} \quad (\text{CMS 1305})$$

- ◆ LHC may find this particle.

# Summary and discussions

## Good points

- ◆ **SUSY and GUT breaking in a model (just by decreasing a singlet).**
- ◆ No R-axion. Constant superpotential is allowed by symmetry. (No  $U(1)_R$ .)
- ◆ It produces gaugino mass by gravity mediation. High scale SUSY!

$$m_{1/2} \sim m_{3/2} \sim 1\text{TeV}, m_0 \sim 1000\text{TeV}.$$

- ◆ Interesting phenomenology.

**Long lived charged lepton** appears.

$$\tau_{E_R^c} \sim O(10^{-2}) \text{ sec} \left( \frac{m_0}{1000\text{TeV}} \right)^4 \left( \frac{1\text{TeV}}{m_{E_R^c}} \right)^5$$

LHC may discover it.

- ◆ “Direct” signatures of GUT in sfermion mass spectrum

## Bad points

- ◆ **High scale SUSY needs finetuning.** It is caused by  $\Lambda \sim \Lambda_G \ll M_{Pl}$ , which is required to explain the success of RGE gauge couplings.
- ◆ Artificial discrete symmetry and singlets are introduced to obtain lower SUSY scale. (E6 GUT may avoid this issue.) Artificially large  $U(1)_A$  charge.
- ◆ Gravitino problem
- ◆ Bino DM (overproduction?)

The upper 2 bad points are based on the assumption of  $O(1)$  coefficients. Suppression factors from extra dimension may avoid these.

# Bino overproduction problem

Why is bino LSP?

- ◆ D term dominates  $\frac{F_{\bar{C}I}}{\Lambda}$  contribution.
- ◆  $\mu$  must be large to cancel the D term contribution to Higgs.
- ◆  $m_{1/2} \sim m_{3/2} \sim 1\text{TeV}, m_0 \sim 1000\text{TeV}$ .
- ◆ Interesting phenomenology.

Long lived charged lepton appears.

$$\tau_{E_R^c} \sim O(1) \text{ sec} \left( \frac{m_0}{1000\text{TeV}} \right)^4 \left( \frac{1\text{TeV}}{m_{E_R^c}} \right)^5$$

LHC may discover it.

- ◆ “Direct” signatures of GUT in sfermion mass spectrum.
- ◆ D term domination is a result of a simple model. This may change in more realistic and complex model.)

Higgsino LSP(DM)

- ◆  $\sqrt{D} \sim \frac{F_{\bar{C}I}}{\Lambda}$ .
- ◆  $\mu$  can be small since D can be cancelled by  $\frac{F_{\bar{C}I}}{\Lambda}$ .
- ◆  $m_{1/2} \sim m_{3/2} \sim 1\text{TeV}, m_0 \sim 100\text{TeV}$ .

Finetuning is improved!

- ◆ Interesting phenomenology.

Long lived charged lepton appears.

$$\tau_{E_R^c} \sim O(0.1) \text{ sec} \left( \frac{m_0}{100\text{TeV}} \right)^4 \left( \frac{1\text{TeV}}{m_{E_R^c}} \right)^5$$

Yukawa suppression is compensated by smaller  $m_0$ .

LHC may discover it.

- ◆ “Direct” signatures of GUT in sfermion mass spectrum. D-term observation becomes indirect.