

# Improved analysis for CLFV processes $\mu N(eN) \rightarrow \tau X$ with gluon operators

Masato Yamanaka (Kyushu Sangyo Univ.)

M. Takeuchi, Y. Uesaka, M.Y., Phys. Lett. B772 (2017)

Analysis on CLFV scattering  $\mu N(eN) \rightarrow \tau X$  including

(1) new subprocess  $\ell g \rightarrow \tau g$  ( $\ell \ni e, \mu$ )

(2) quark number conserving subprocess  $\ell g \rightarrow \tau q \bar{q}$

# Search for LFV through $eN(\mu N)$ scattering

Focus : LFV via mediators which mainly interacts with heavy fermions

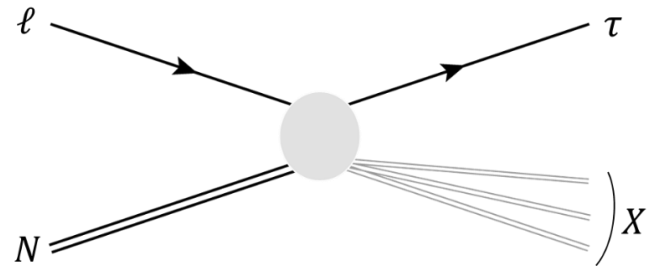
e.g., Higgs, KK gauge boson,  
flavon, leptoquark, ...

A promising way to search for tau LFV

$$\ell + N \rightarrow \tau + X \quad (N: \text{Nucleus})$$

Many exp. launch, e.g., ILC, LHeC, etc.

Can reach high sensitivity beyond the Belle-II sensitivity limit for tau LFV

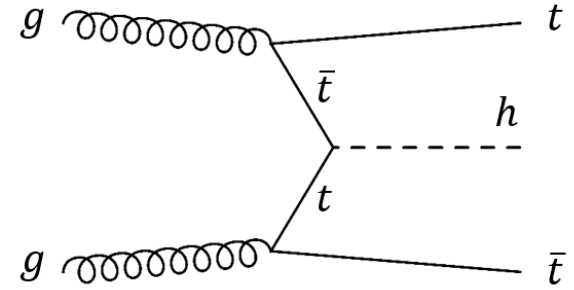
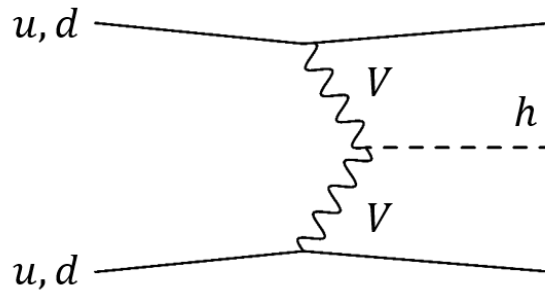
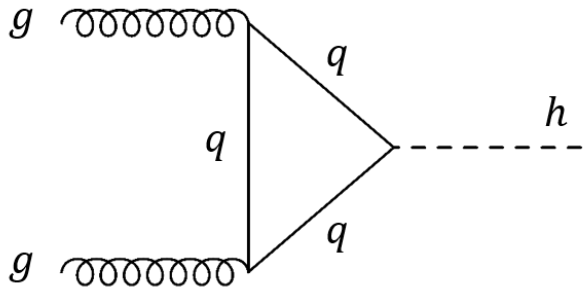


**Precisely relate the LFV parameter  
and the event rate of  $\ell N \rightarrow \tau X$  !!**

Which is correct sub-process for  
LFV lepton-nucleus scattering  $\ell N \rightarrow \tau X$  ?

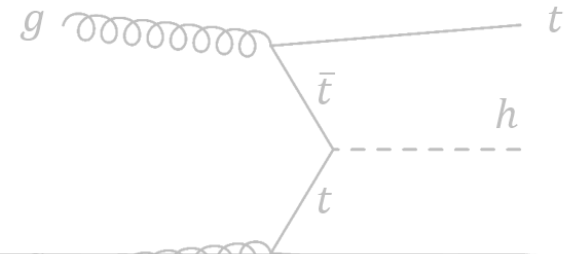
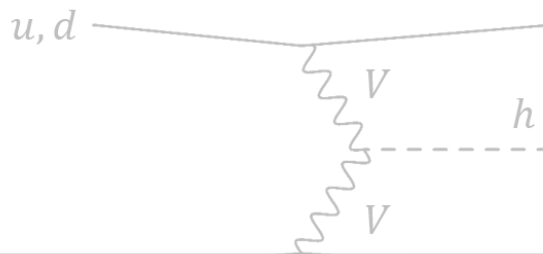
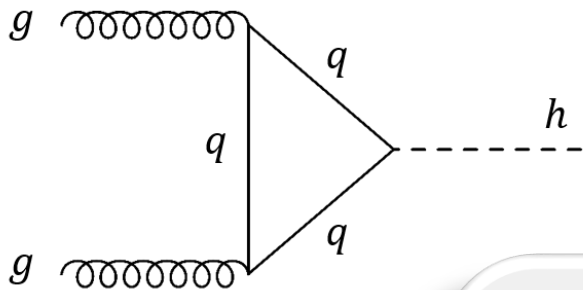
# Higgs production@LHC

Which is dominant sub-process?



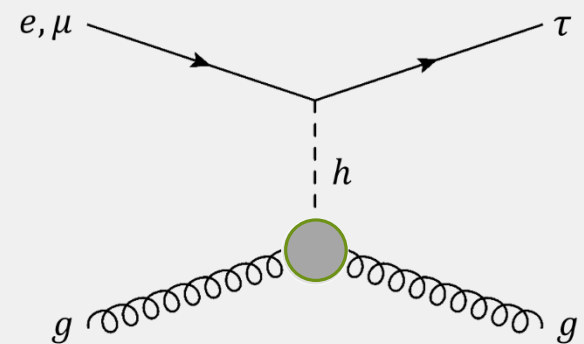
# New sub-process for $\ell N$ scattering

Which is dominant sub-process?



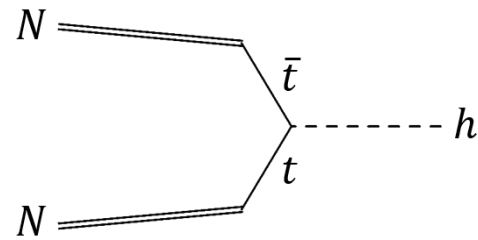
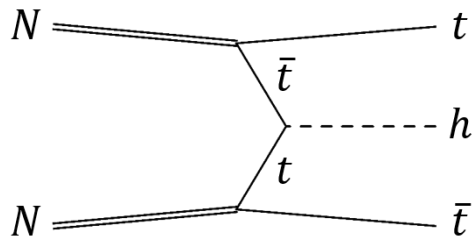
**New sub-process for  
 $eN (\mu N) \rightarrow \tau X$**

Dominant sub-process  
for fixed target exp.



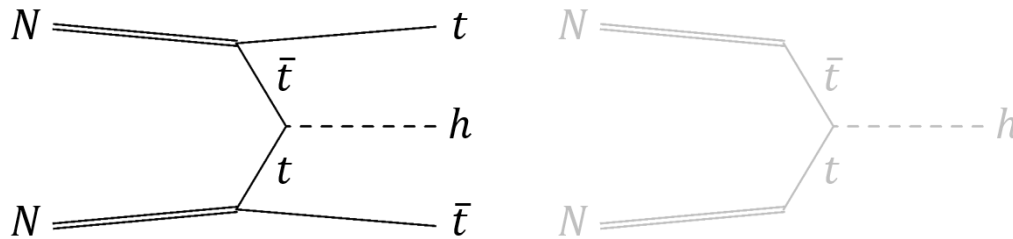
# Higgs production@LHC

Which is correct sub-process?



# Correct sub-process for $\ell N$ scattering

Which is correct sub-process?



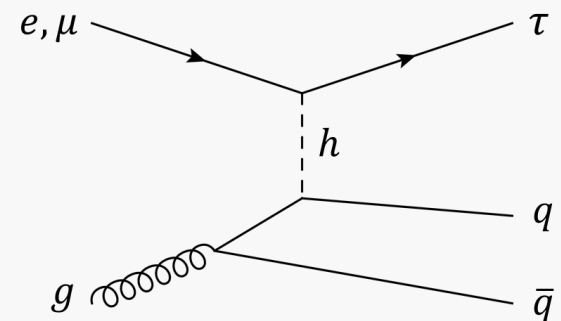
## Correct quark final state sub-process with quark-number conservation

Not  $\ell q \rightarrow \tau q$ !

Threshold and cross section are corrected

e.g.,  $E_{e(\mu)}^{\text{beam}} > 19 \text{ GeV}$  for  $\ell b \rightarrow \tau b$

$E_{e(\mu)}^{\text{beam}} > 55 \text{ GeV}$  for  $\ell g \rightarrow \tau b\bar{b}$

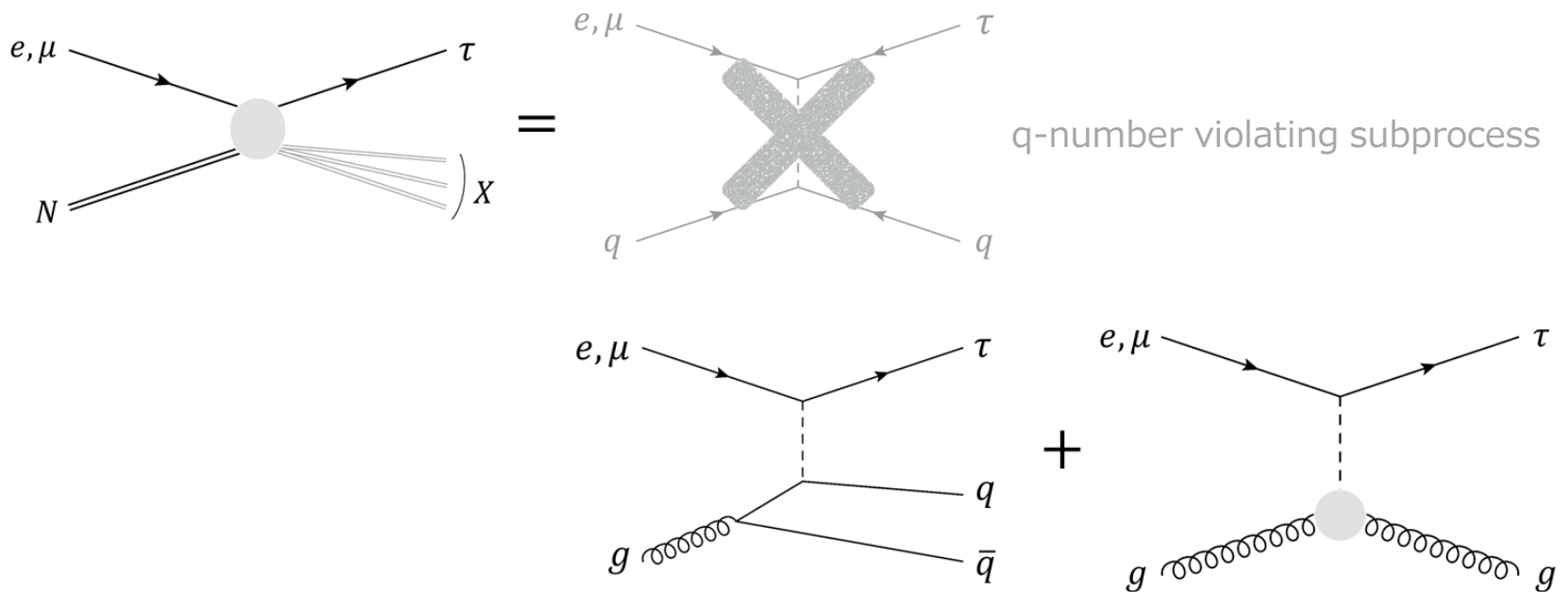


# Aim of this work and outline

## Reformulation of LFV lepton-nucleus scattering taking into account

(1) new sub-process  $\ell g \rightarrow \tau g$

(2) quark-number conservation sub-process  $\ell g \rightarrow \tau q \bar{q}$





Reformulation of  $\sigma(\ell N \rightarrow \tau X)$

# Lagrangian for $\ell g \rightarrow \tau g$ and $\ell g \rightarrow \tau q \bar{q}$

Important : momentum transfer dependence of  $hgg$  effective coupling

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{CLFV}},$$

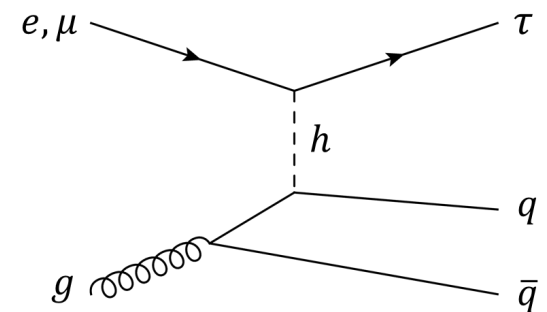
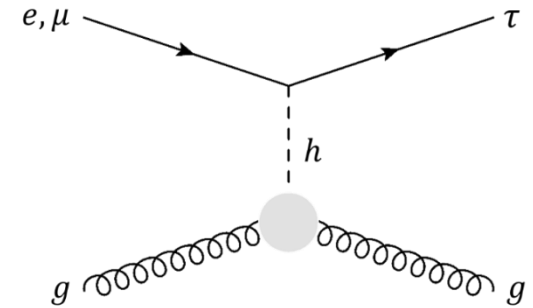
$$\mathcal{L}_{\text{SM}} = - \sum_q y_q h \bar{q} q + g_{hgg} h G_{\mu\nu}^a G^{a\mu\nu},$$

$$\mathcal{L}_{\text{CLFV}} = -\rho_{ij} \bar{\ell}_j P_L \ell_i h - \rho_{ji} \bar{\ell}_j P_R \ell_i h$$

$\rho_{ij}, \rho_{ji}$  : LFV parameter ( $i, j$  : flavor index)

Current bound  $\sqrt{|\rho_{\ell\tau}|^2 + |\rho_{\tau\ell}|^2} = 2.4 \times 10^{-3}$

Note: stronger than the Belle-II sensitivity for tau CLFV search



# Higgs-gluon-gluon coupling

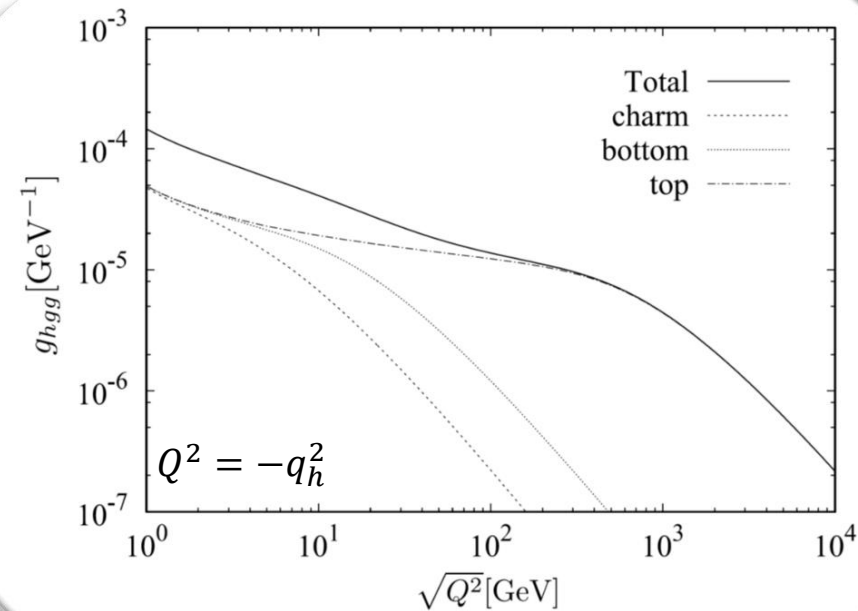
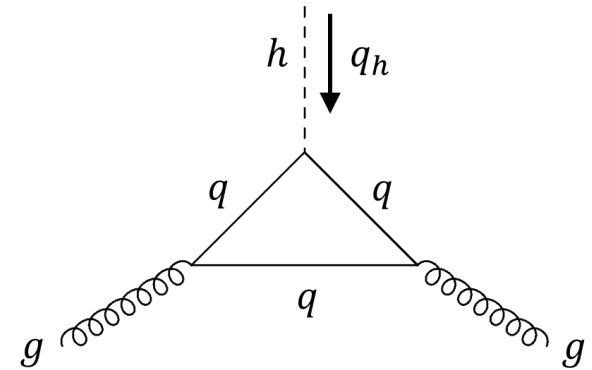
$hgg$  effective coupling

$$g_{hgg} = \sum_{q=c,b,t} \frac{\alpha_s}{8\pi v} \frac{4m_q^2}{q_h^2} \left[ 1 + \left( 1 - \frac{4m_q^2}{q_h^2} \right) f\left(\frac{4m_q^2}{q_h^2}\right) \right]$$

$$f(r) = -\frac{1}{4} \log^2 \left[ -\frac{1 + \sqrt{1-r}}{1 - \sqrt{1-r}} \right] \quad (r < 0)$$

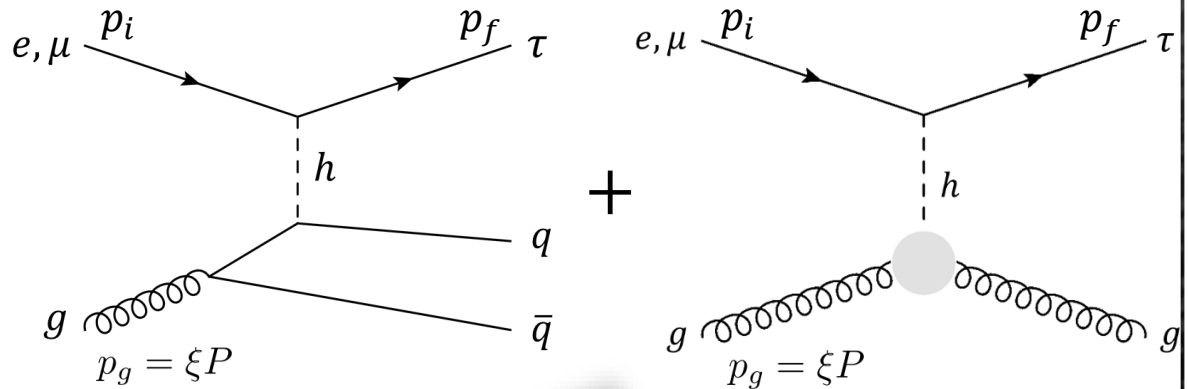
Sizable contributions from  $c$ -quark and  $b$ -quark, in addition to  $t$ -quark

Carefully include the scale dependence of  $hgg$  effective coupling



# Cross section

H. Georgi, H. Politzer, PRL36 (1976)



$$\sigma_{\ell_i N \rightarrow \tau X} = \sum_{\hat{X}=g, q\bar{q}} \int dx dy \int_0^1 d\xi \frac{d^2 \hat{\sigma}_{\ell_i g \rightarrow \tau \hat{X}}}{dx dy} f_g(\xi, Q^2)$$

Gluon PDF

$x$  : Bjorken variable

$y$  : measure of inelasticity

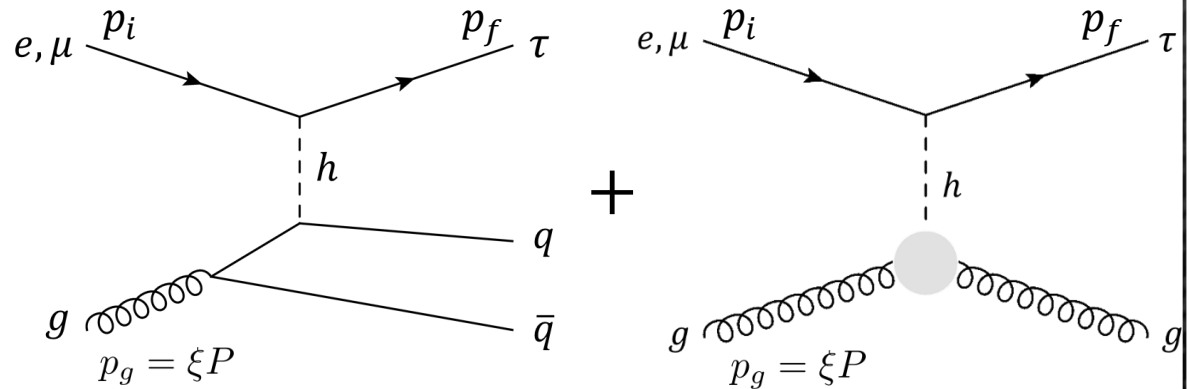
■ Momentum fraction :  $\xi = \frac{Q^2 + w^2}{Q^2} x$

■ Invariant mass of  $q\bar{q}$  :  $w^2 = (p_q + p_{q'})^2$

■ Momentum transfer :  $Q^2 = -(p_i - p_f)^2$

# Cross section

H. Georgi, H. Politzer, PRL36 (1976)



$$\sigma_{\ell_i N \rightarrow \tau X} = \sum_{\hat{X}=g, q\bar{q}} \int dx dy \int_0^1 d\xi \frac{d^2 \hat{\sigma}_{\ell_i g \rightarrow \tau \hat{X}}}{dx dy} f_g(\xi, Q^2)$$

■ Momentum fraction :  $\xi = \frac{Q^2 + w^2}{Q^2} x$

$x$  : Bjorken variable

**Different quantities!**

**Calculate with taking into account  $x \neq \xi$  !!**

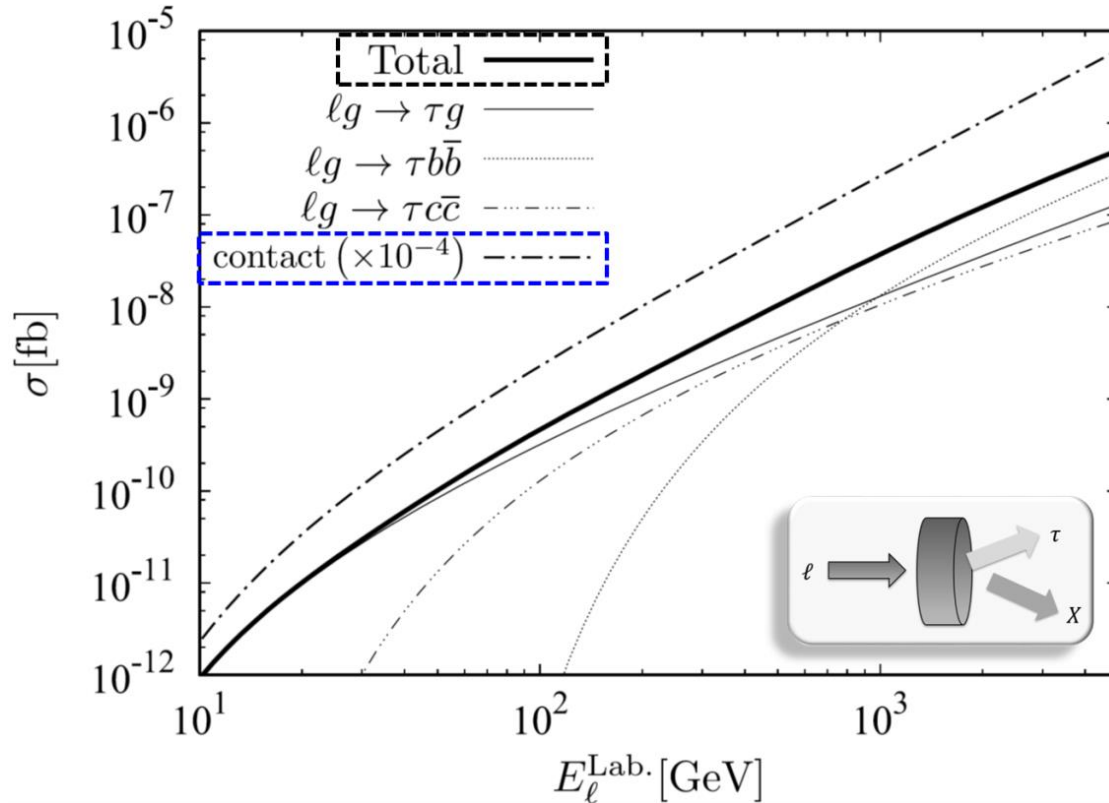
# Numerical analysis

- ☑ For Higgs CLFV@fixed target exp.
- ☑ For general CLFV mediator@fixed target exp.
- ☑ For Higgs CLFV@beam collision exp.

CLFV coupling is taken to be current bound:

$$\sqrt{|\rho_{\ell\tau}|^2 + |\rho_{\tau\ell}|^2} = 2.4 \times 10^{-3}$$

# Cross section vs beam energy for fixed target exp.



**Large enhancement by new sub-process  $\ell g \rightarrow \tau g$**

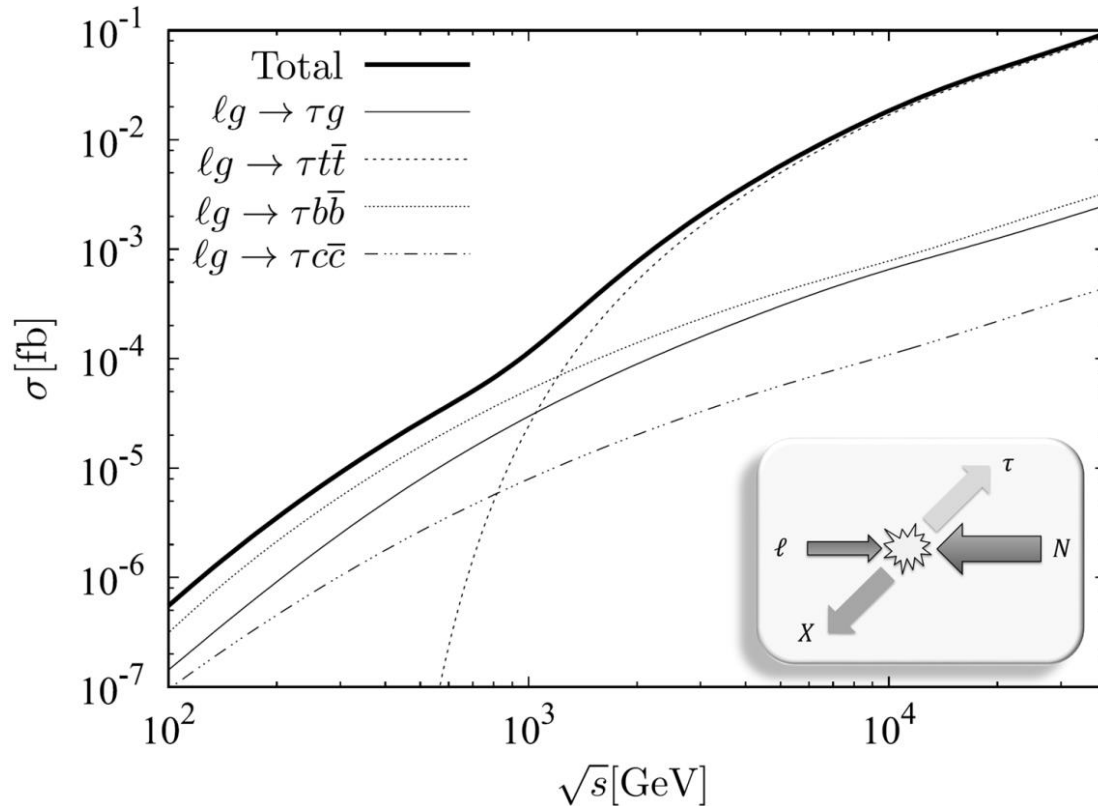
**Large correction of  $\sigma$  arises from  $q$ -number conservation**

$\tau b \bar{b}$  channel begins to be relevant at  $E_\ell^{\text{Lab}} \simeq 500$  GeV (estimated in previous works as  $E_\ell^{\text{Lab}} \simeq 50$  GeV)

	ILC ( $N_e \simeq 10^{22}$ /year)	$\nu$ factory ( $N_\mu \simeq 10^{20}$ /year)
SM Higgs LFV	$O(10)$ event/year	$O(0.1)$ event/year
LFV via a heavy mediator	$O(10^5)$ event/year	$O(10^3)$ event/year

# Cross section vs collision energy for collider exp.

(Higgs LFV)



$\tau t\bar{t}$  channel dominates over others for  $\sqrt{s} \gtrsim 1$  TeV

**Important to understand the dominant channel with q-number conservation**

TLHeC ( $\sqrt{s} = 1.3$ TeV)	FCC-eh ( $\sqrt{s} = 3.5$ TeV)	FCC-eh ( $\sqrt{s} = 5.9$ TeV)
$O(0.1)$ event/year	$O(1)$ event/year	$O(10)$ event/year



# Summary

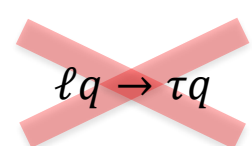
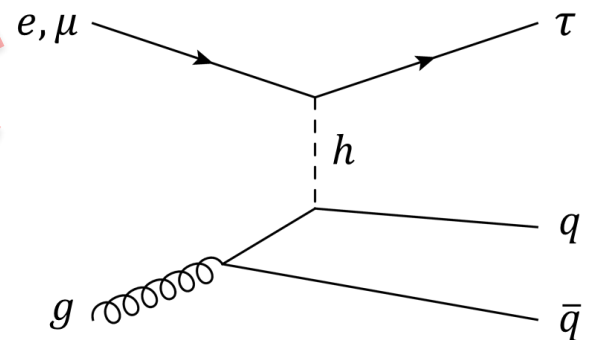
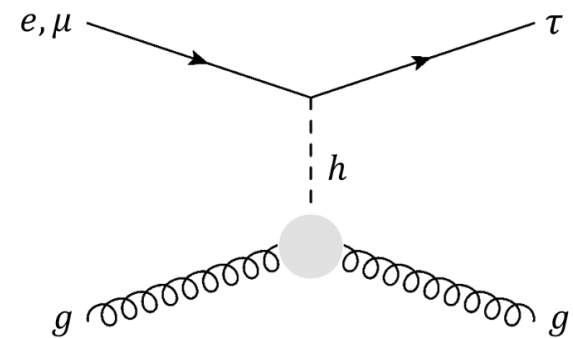
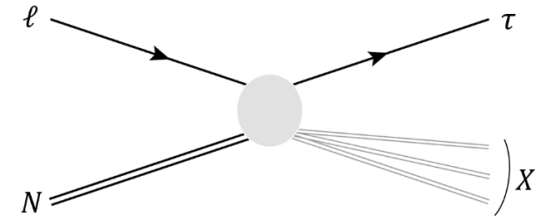
- ☑ We studied tau CLFV by mediators mainly interacting with heavy fermions
- ☑ It's necessary to precisely relate the CLFV parameters and event rate of  $\ell N$  scattering

- ☑ **Reformulation of  $\ell N \rightarrow \tau X$  taking into account important ingredients**

**(1) gluon contribution  $\ell g \rightarrow \tau g$**

**(2) q-number conservation  $\ell g \rightarrow \tau q \bar{q}$**

- ☑ Future experiments (COMPASS, ILC, LHeC,  $\nu$  factory, etc) could shed light on the tau CLFV



Thank you very much!

Backup slides

# Cross sections for each PDF

