

# (In)dependence of various LFV observables in the non-minimal SUSY

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*SUSY 2018,  
July 24, 2018, Barcelona, Spain*

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in collaboration with D. Stöckinger and H. Stöckinger-Kim

# R-symmetry

- ◆ additional symmetry of the SUSY algebra allowed by the Haag - Łopuszański - Sohnius theorem
- ◆ for  $N=1$  it is a global  $U_R(1)$  symmetry under which the SUSY generators are charged
- ◆ implies that the spinorial coordinates are also charged  $Q_R(\theta) = 1, \theta \rightarrow e^{i\alpha}\theta$
- ◆ superpotential example

$$\mathcal{L} \ni \int d^2\theta W$$

- ◆ Superpotential is polynomial in fields. For  $W$  to transform homogeneously superfields must have definite R-charges

$$e^{i\alpha Q_R} \quad \quad \quad e^{i\alpha Q_R} \quad \quad \quad e^{i\alpha(Q_R-1)}$$
$$\Phi \quad = \quad \phi(y) \quad + \quad \sqrt{2}\theta\psi(y) \quad + \quad \theta\bar{\theta}F(y)$$

- ◆ Similarly one can work out other parts of the Lagrangian

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 $\mathcal{R}$ -invariant  $\longrightarrow$   $\mathcal{L}$   $\ni \int d^2\theta W$

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$$e^{i\alpha Q_R} \Phi = e^{i\alpha Q_R} \phi(y) + \sqrt{2}\theta\psi(y) + \theta\theta F(y)$$

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(we want it to be)  
 $\mathcal{R}$ -invariant

$\rightarrow$   $\mathcal{L}$   $\ni$   $\int d^2\theta$   $W$  transforms as  $e^{-2i\alpha}$

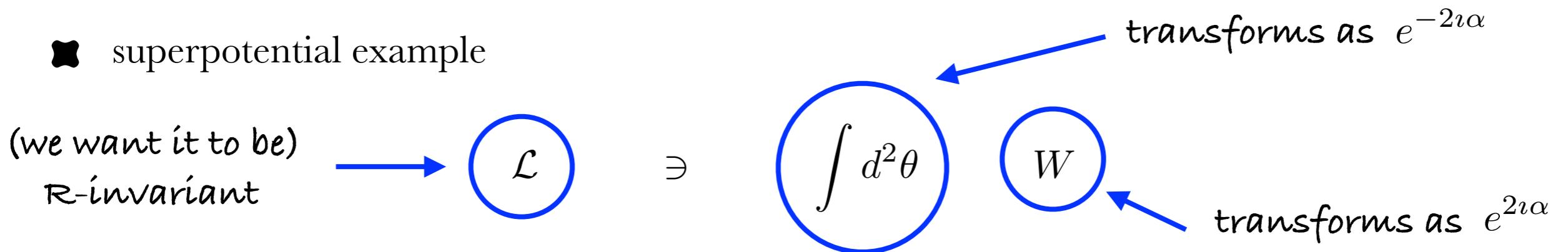
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# Low-energy R-symmetry realization

- Different possible models that one can construct

- “Natural” choice

$$e^{i\alpha Q_R} \quad e^{i\alpha Q_R} \quad e^{i\alpha(Q_R-1)}$$

$$\Phi = \phi(y) + \sqrt{2}\theta\psi(y) + \theta\theta F(y)$$

leptons and quarks	$Q_R = 1$	$Q_R = 1$	$Q_R = 0$
Higgs	$Q_R = 0$	$Q_R = 0$	$Q_R = -1$

- Good: no barion and lepton number violating terms

- Bad: No Majorana masses for higgsinos and gauginos

One way to fix it: [Dirac masses](#)  
**Minimal R-Symmetric Supersymmetric Standardmodel (MRSSM)**  
Kribs et.al. arXiv:0712.2039

		$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_R$
Additional fields:	Singlet	$\hat{S}$	1	1	0
	Triplet	$\hat{T}$	1	3	0
	Octet	$\hat{O}$	8	1	0
	R-Higgses	$\hat{R}_u$	1	2	-1/2
		$\hat{R}_d$	1	2	1/2

$$W = \mu_d \hat{R}_d \hat{H}_d + \mu_u \hat{R}_u \hat{H}_u$$

$$\begin{aligned}
 &+ \Lambda_d \hat{R}_d \hat{T} \hat{H}_d + \Lambda_u \hat{R}_u \hat{T} \hat{H}_u + \lambda_d \hat{S} \hat{R}_d \hat{H}_d + \lambda_u \hat{S} \hat{R}_u \hat{H}_u \\
 &- Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + Y_u \hat{u} \hat{q} \hat{H}_u
 \end{aligned}$$

# MSSM vs. MRSSM

◆ superpotencial

$$\mu \hat{H}_u \hat{H}_d$$
!
  

$$-Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + Y_u \hat{u} \hat{q} \hat{H}_u$$
✓

◆ superpotencial

$$\mu_d \hat{R}_d \hat{H}_d + \mu_u \hat{R}_u \hat{H}_u$$

$$-Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + Y_u \hat{u} \hat{q} \hat{H}_u$$

$$\Lambda_d \hat{R}_d \hat{T} \hat{H}_d + \Lambda_u \hat{R}_u \hat{T} \hat{H}_u + \lambda_d \hat{S} \hat{R}_d \hat{H}_d + \lambda_u \hat{S} \hat{R}_u \hat{H}_u$$

◆ soft-SUSY breaking terms

- $B_\mu$  - term ✓
- soft scalar masses ✓
- Majorana gaugino masses !
- A - terms !

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$$\begin{aligned} & \mu \hat{H}_u \hat{H}_d \\ -Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + Y_u \hat{u} \hat{q} \hat{H}_u \end{aligned}$$



◆ superpotencial

$$\begin{aligned} & \mu_d \hat{R}_d \hat{H}_d + \mu_u \hat{R}_u \hat{H}_u \\ -Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + Y_u \hat{u} \hat{q} \hat{H}_u \\ & \Lambda_d \hat{R}_d \hat{T} \hat{H}_d + \Lambda_u \hat{R}_u \hat{T} \hat{H}_u + \lambda_d \hat{S} \hat{R}_d \hat{H}_d + \lambda_u \hat{S} \hat{R}_u \hat{H}_u \end{aligned}$$

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# Particle content summary: MSSM vs. MRSSM

**different number of physical states**      **completely new states**

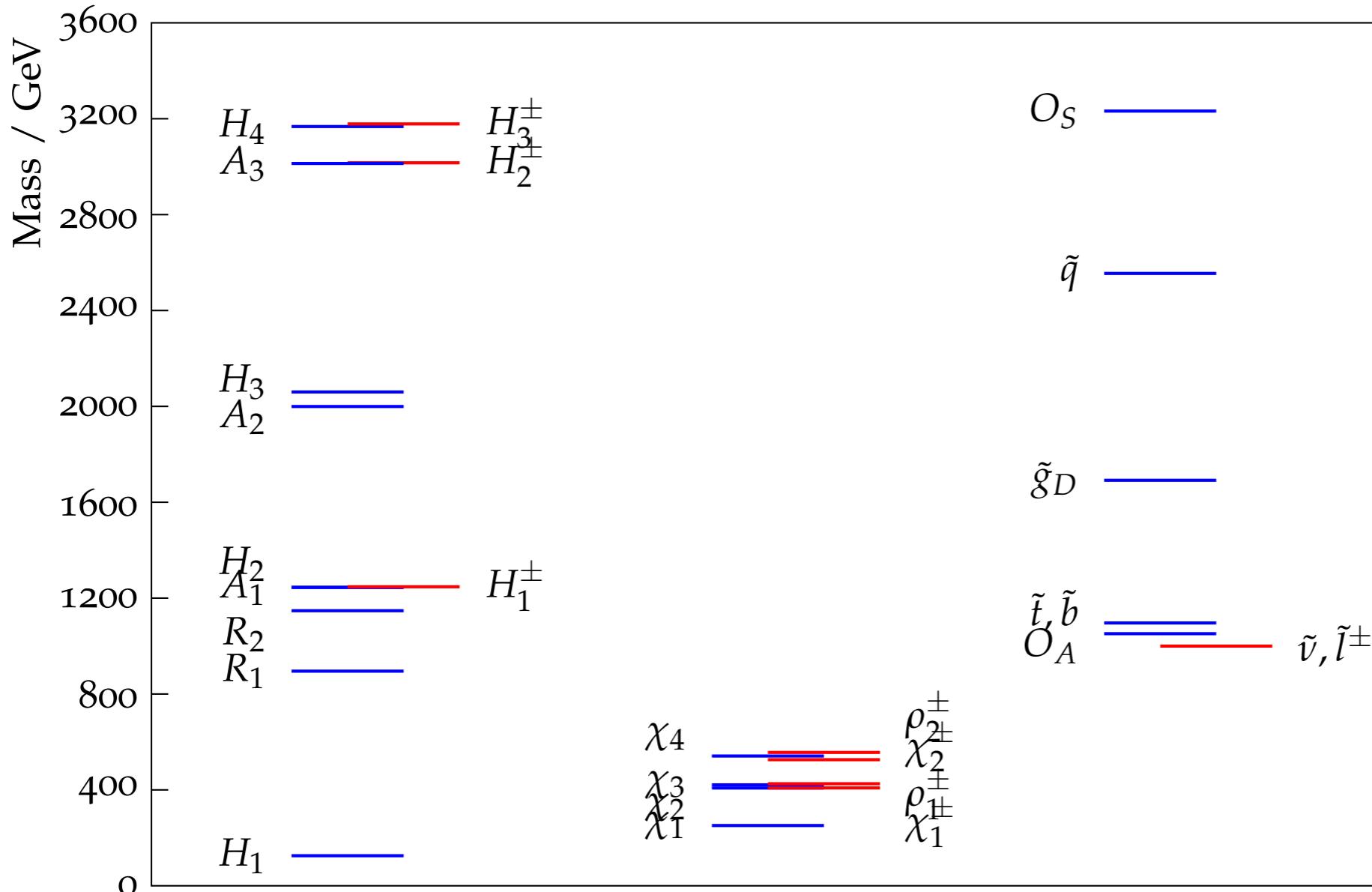
	Higgs			R-Higgs			
	CP-even	CP-odd	charged	charginos	neutral	charged	s gluon
MSSM	2	1	1	2	0	0	0
MRSSM	4	3	3	2+2	2	2	1

	neutralino	gluino
MSSM	4	1
MRSSM	4	1

**Majorana fermions**

**Dirac fermions**

# Exemplary mass spectrum



arXiv:1410.4791  
Higgs mass at 1-loop  
level + EWPO

arXiv:1504.05386  
2-loop corrections to  
Higgs mass

arXiv:1511.09334  
DM in light single  
scenario

arXiv:1707.04557  
NLO SQCD corrections  
to squark -  
(anti)squark pair  
production

# Previous and future low energy experiments

- As the LHC still sees nothing, we look into low energy experiments:

- prospects for g-2 measurement

$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (28.1 \pm 6.3^{\text{exp}} \pm 3.6^{\text{th}}) \times 10^{-10}$$

$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (??? \pm 1.6^{\text{exp}} \pm 3.4^{\text{th}}) \times 10^{-10}$$

- prospect for  $\mu \rightarrow e\gamma$

current:  $4.2 \times 10^{-13}$  (MEG)

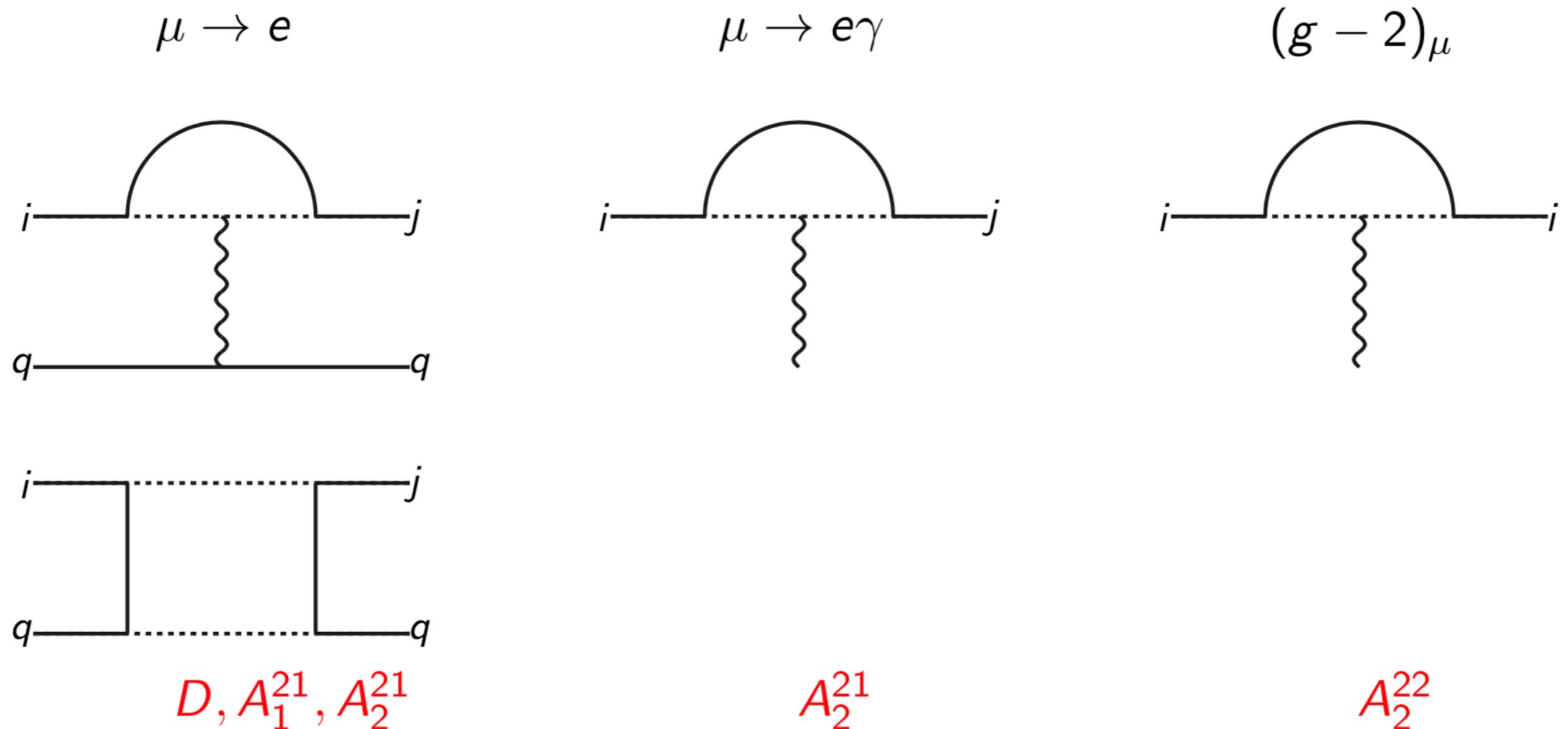
future:  $\approx 4 \times 10^{-14}$

- prospect for  $\mu \rightarrow e$  conversion

current:  $7 \times 10^{-13}$  (SINDRUM-II)

future:  $\lesssim 10^{-16}$

# Relation between $(g - 2)_\mu$ and LFV observables

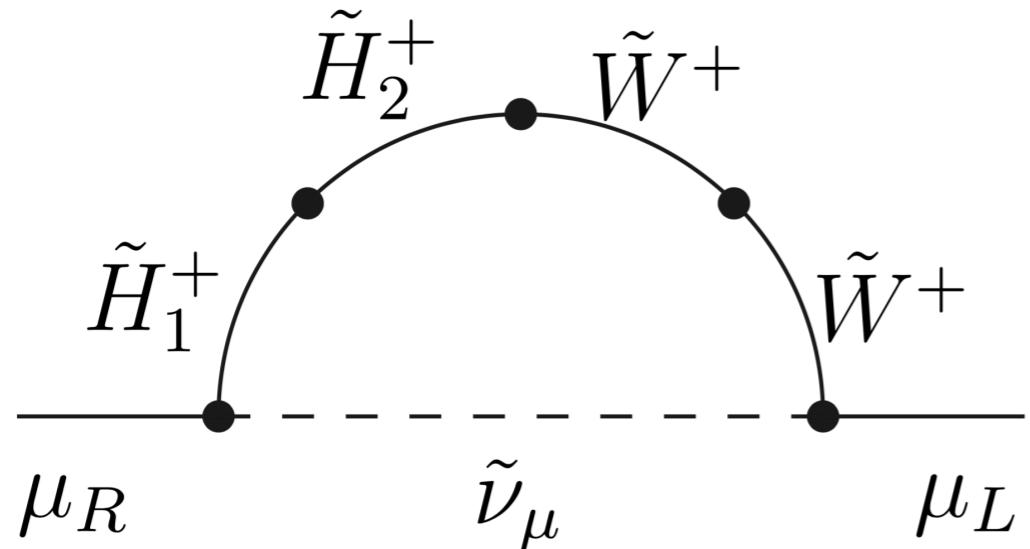


each observable requires a dedicated experiment

# $(g - 2)_\mu$ in the MSSM

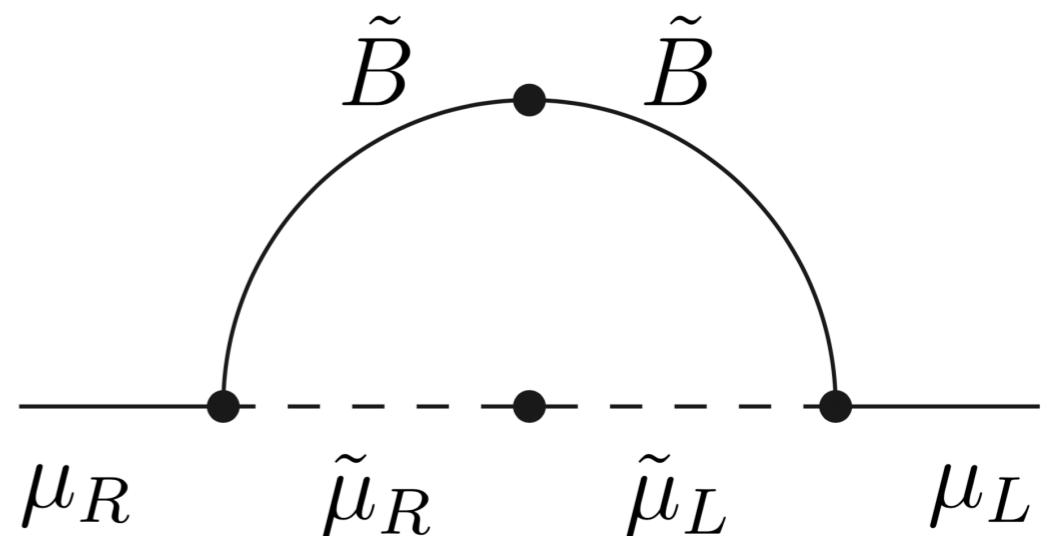
chargino

$$\propto m_\mu^2 \tan \beta \mu M_2$$



neutralino

$$\propto m_\mu^2 \tan \beta \mu M_1$$

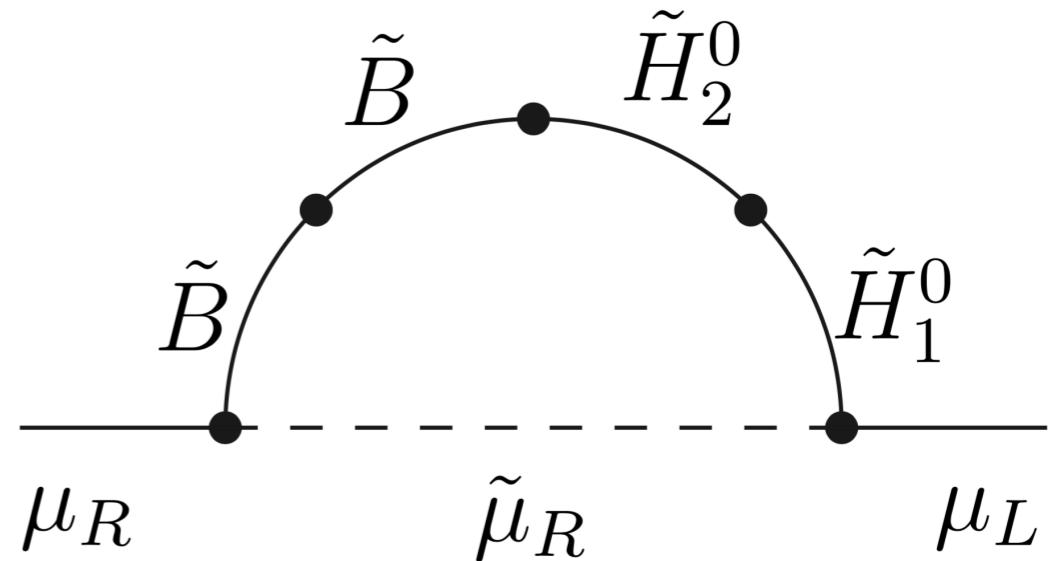


and similarly for  $\mu \rightarrow e\gamma$  and  $\mu \rightarrow e^-$  - as long as  $\tan \beta$  is not very small all considered observables are dominated by the dipole contributions and therefore strongly correlated

$$\text{CR}(\mu \rightarrow e) \propto \alpha \cdot \text{BR}(\mu \rightarrow e\gamma)$$

$$\text{CR}(\mu \rightarrow e) \leq 3 \cdot 10^{-15}$$

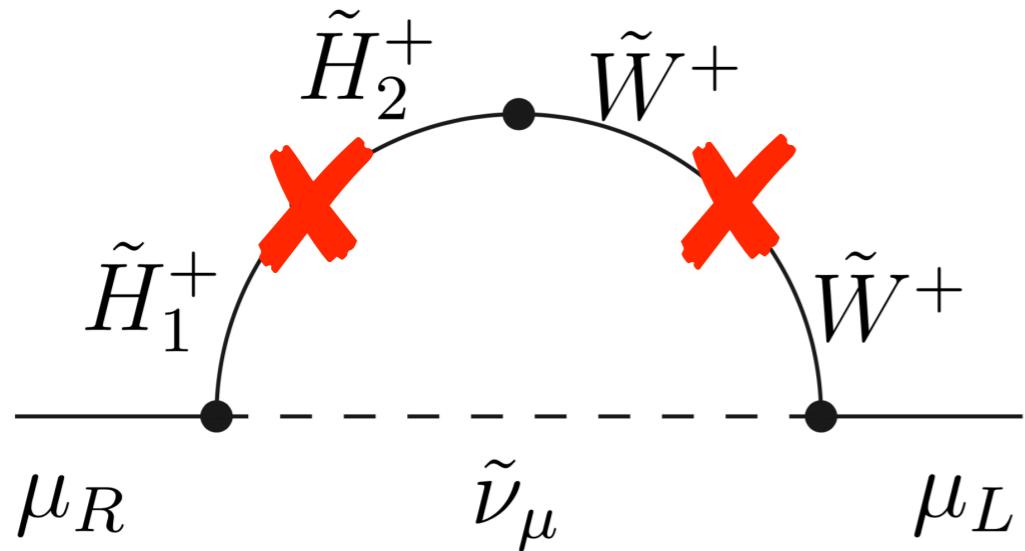
$$\propto m_\mu^2 \tan \beta \mu M_1$$



# $(g - 2)_\mu$ in the MRSSM

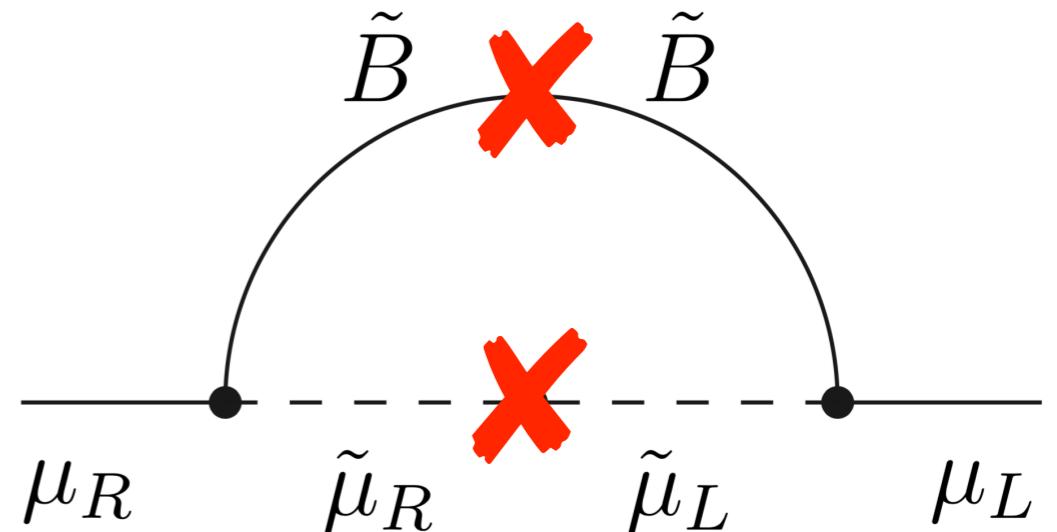
chargino

$$\propto m_\mu^2 \tan \beta \mu M_2$$



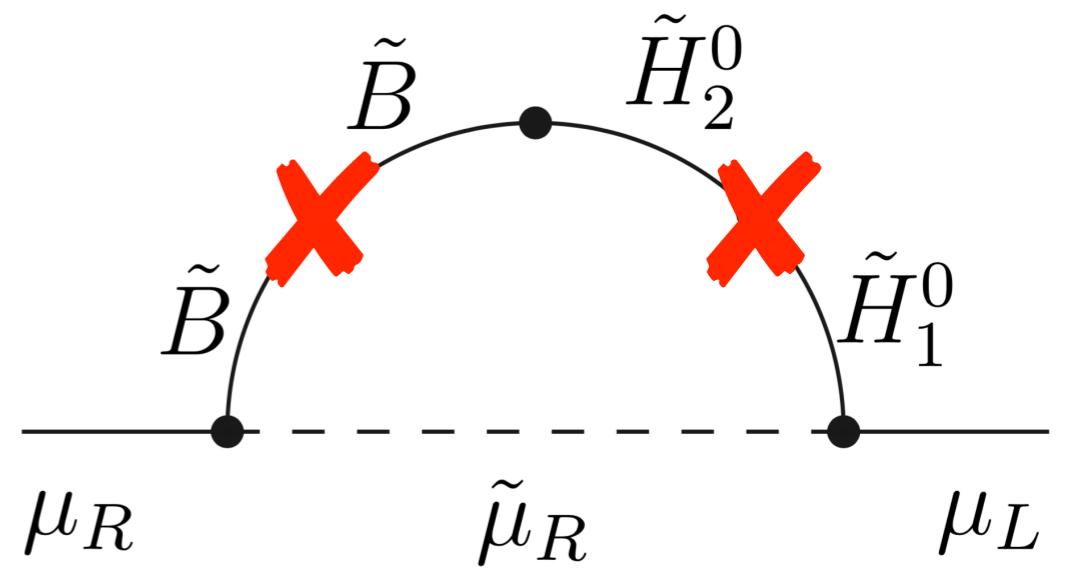
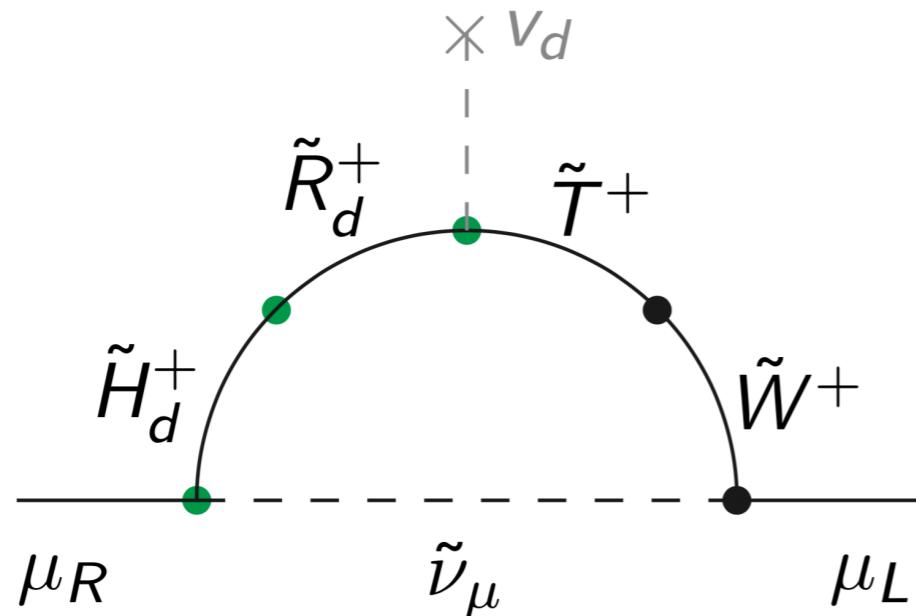
neutralino

$$\propto m_\mu^2 \tan \beta \mu M_1$$



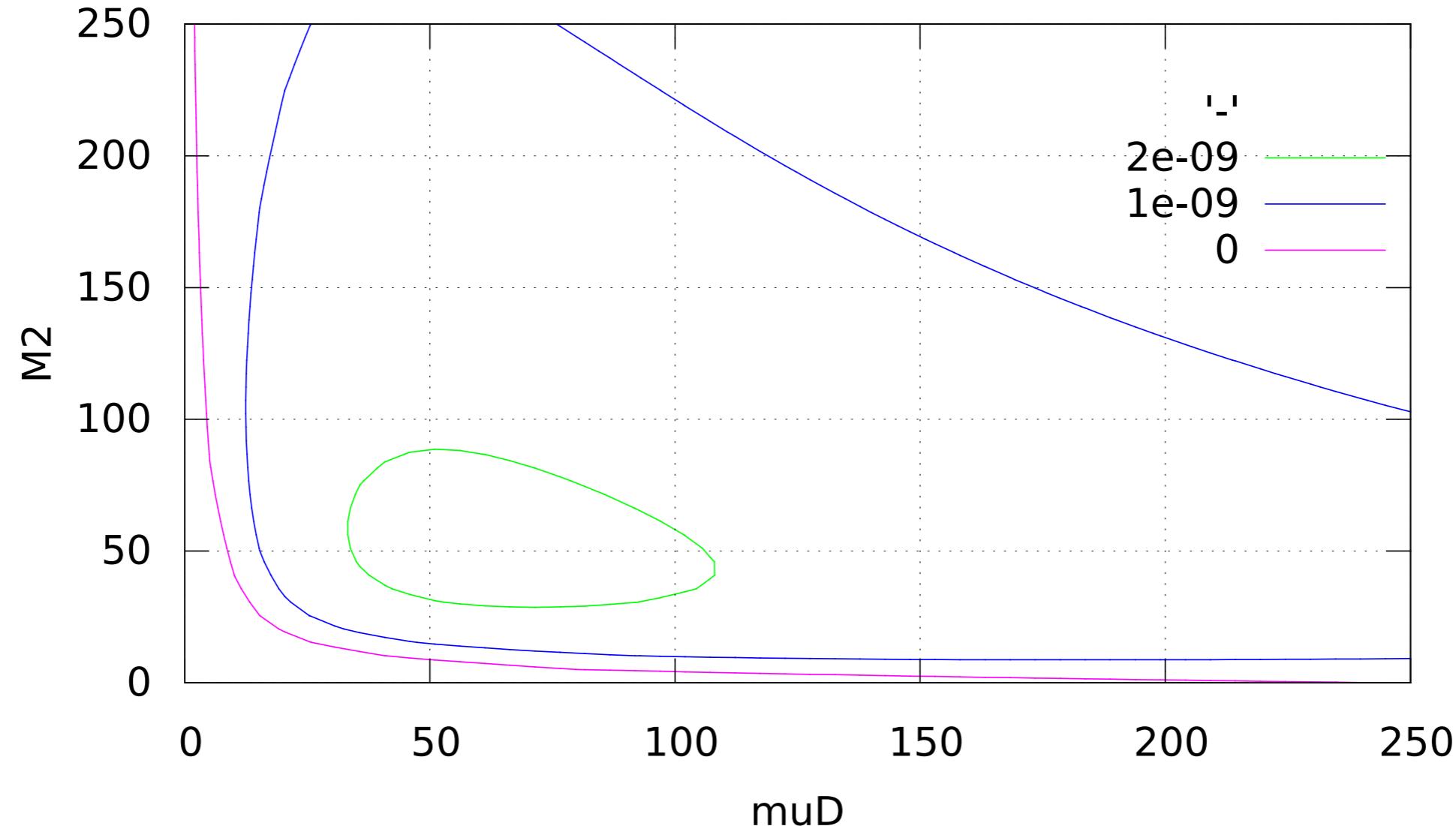
there is one class of  
enhanced diagram though

$$\propto m_\mu^2 \tan \beta \mu M_1$$



# $(g - 2)_\mu$ in the MRSSM

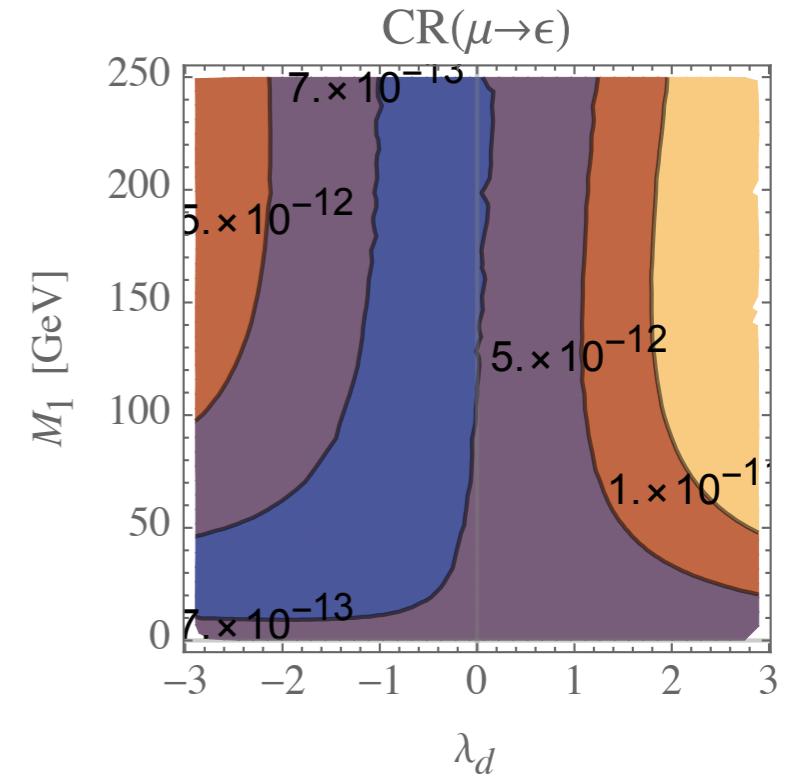
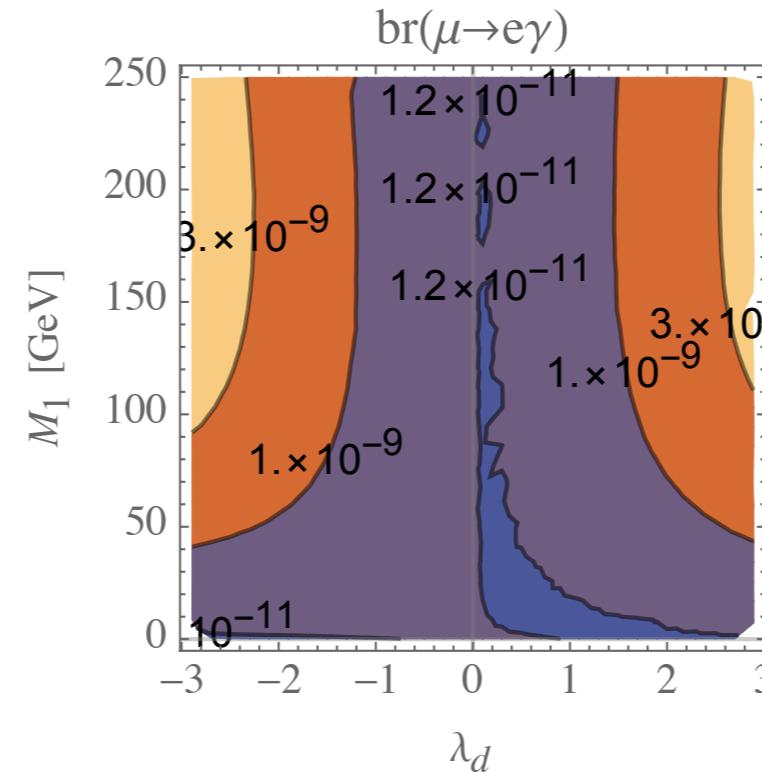
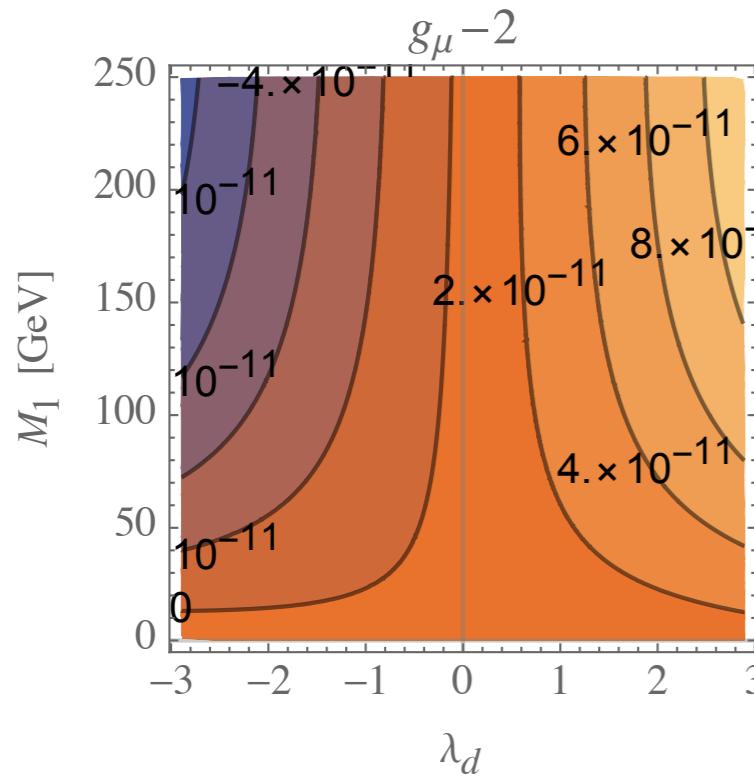
- It is possible to obtain large contribution to  $g-2$



- The price to pay are light EW-inos, in tension with experiment

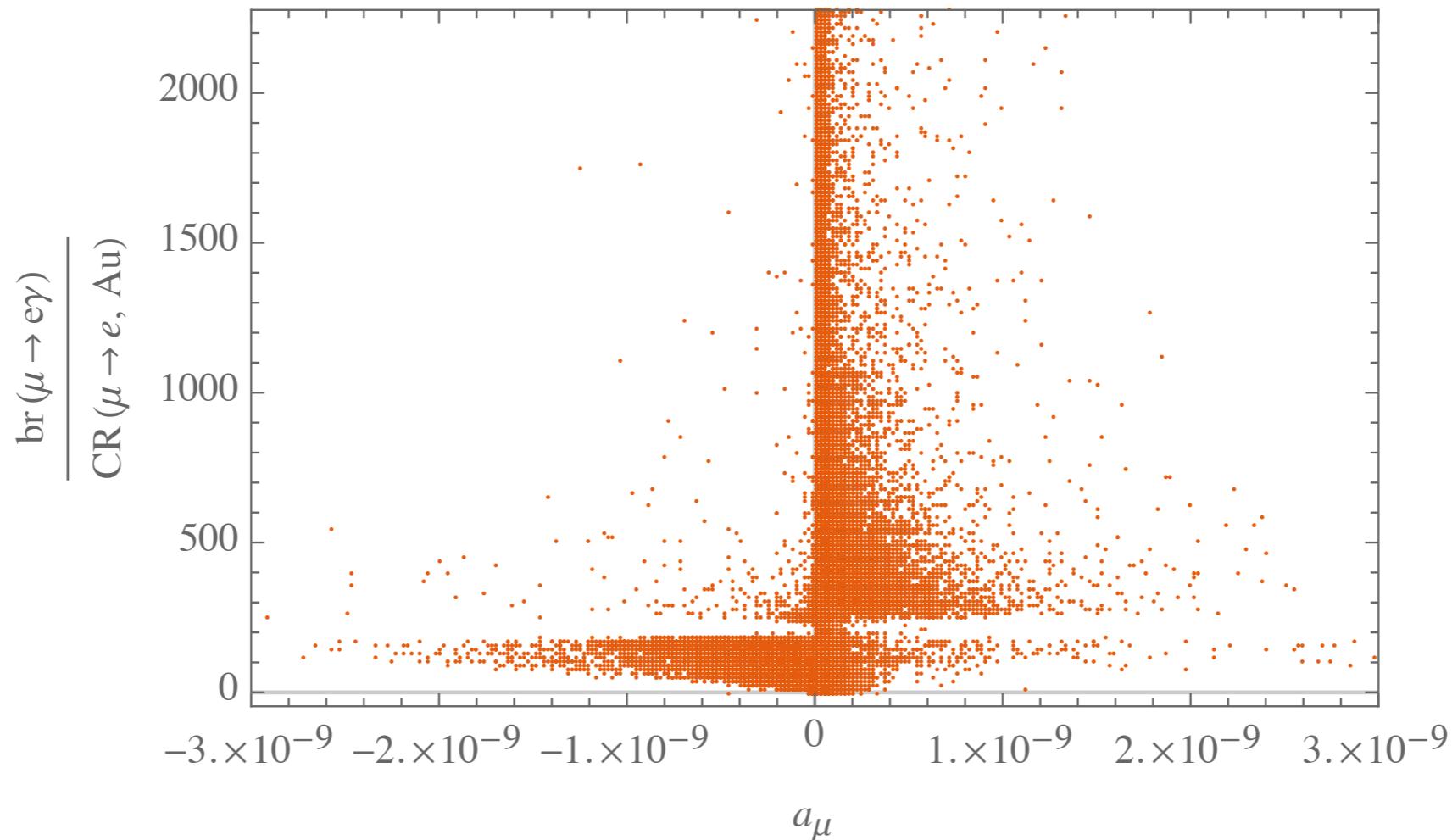
# Photonic penguin dominance

- For  $|\lambda_d| \gtrsim 1$  the dipoles dominate:  $g-2$  scales linearly with  $\lambda_d$ , while  $\mu \rightarrow e\gamma$  and  $\mu \rightarrow e$  quadratically



- For  $|\lambda_d| \gtrsim 1$  the ratio of  $\mu \rightarrow e\gamma$  over  $\mu \rightarrow e$  is of the order 100, as in the MSSM where  $\text{CR}(\mu \rightarrow e) \propto \alpha \cdot \text{BR}(\mu \rightarrow e\gamma)$
- Near  $|\lambda_d| \approx 0$  the ratio is of order 10

$$a_\mu \text{ VS. } \frac{\text{br}(\mu \rightarrow e\gamma)}{\text{CR}(\mu \rightarrow e, \text{Au})}$$



- █ In the region dominated by the dipoles the  $\text{br}(\mu \rightarrow e\gamma) \sim \sin^2 2\theta \cdot a_\mu$
- █ In the MRSSM this is a region of  $|\lambda_d| \gtrsim 1$ , in the MSSM  $\tan \beta \gtrsim 5$

# Conclusions:

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- Two distinct cases:  $|\lambda_d| \approx 0$ ,  $|\lambda_d| > 0$
- For large  $|\lambda_d|$  observables get dominated by photon „penguins” and are strongly correlated
- Generating sufficient contribution to g-2 through large  $\lambda_d$  overshots LFV observables (unless one fine-tunes the mixing angle)
- Similar things happen for  $A_d$
- For  $|\lambda_d| \approx 0$  the g-2 and  $\mu \rightarrow e\gamma$  are still correlated but the  $\mu \rightarrow e$  conversion rate can be dominated by so-called charge radius, Z-penguin and box contributions
- It is therefore possible to find a parameter points not excluded by current experimental results, within reach of the next  $\mu \rightarrow e$  conversion (but not  $\mu \rightarrow e\gamma$ ) experiment

Backup

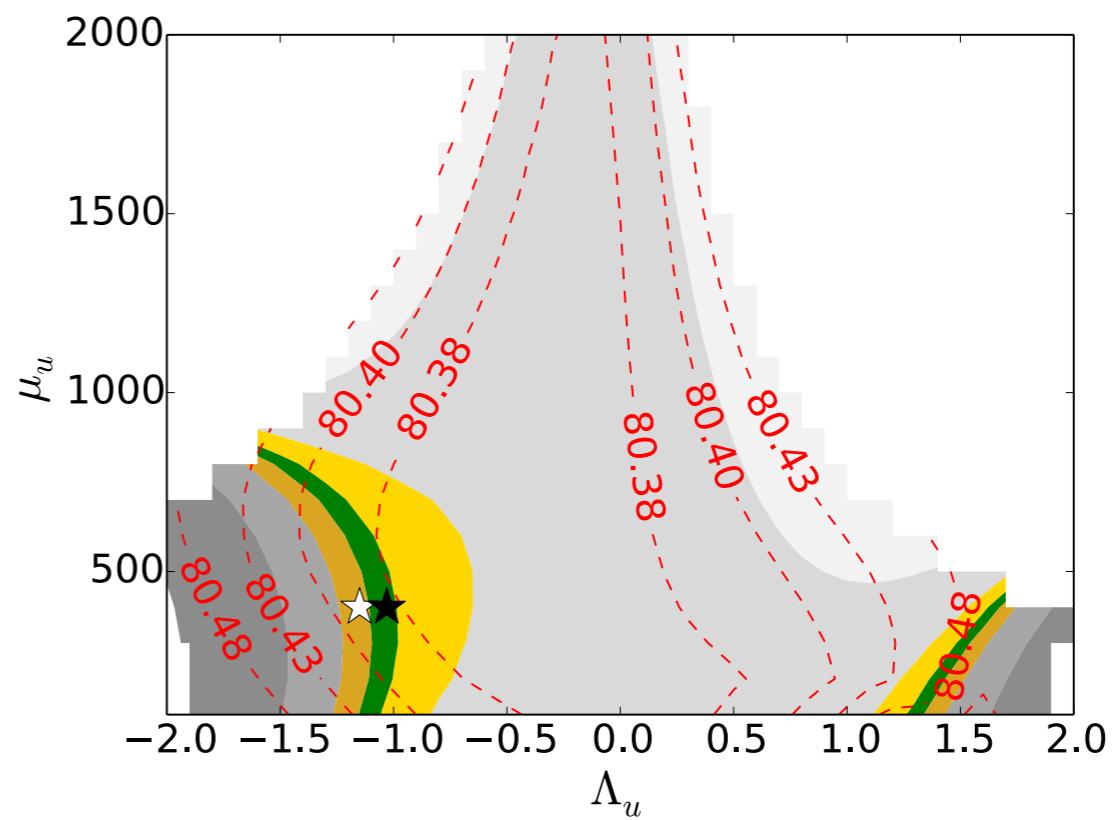
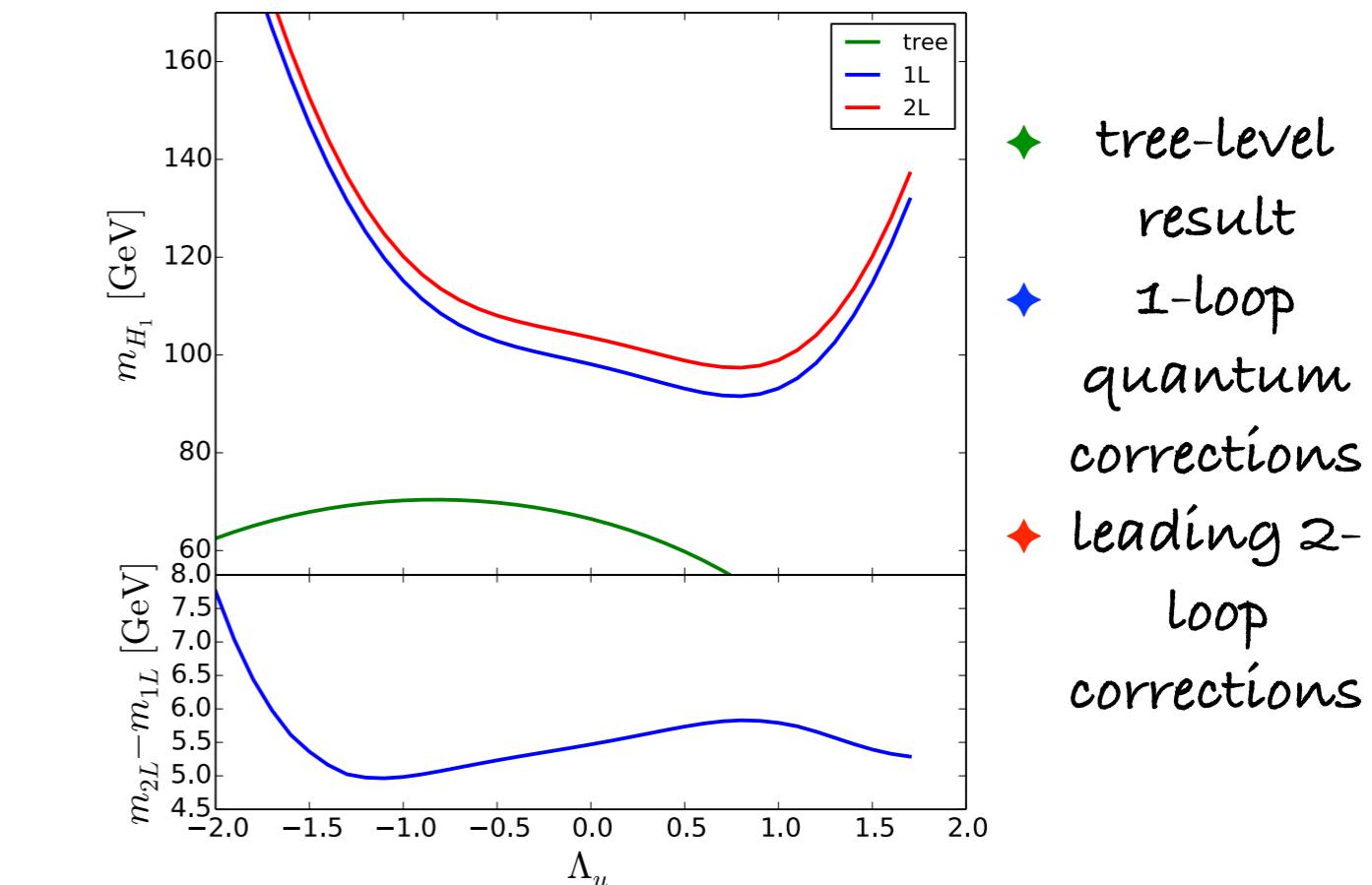
# EW sector of the MRSSM (status)

- The SM-like Higgs boson mass in the MRSSM has been calculated including full 1-loop and leading 2-loop corrections<sup>1,2</sup>
- Impact of EWPO was analyzed<sup>1</sup>
- MRSSM can predict correct dark matter relic density while being in agreement with dark matter direct detection bounds<sup>3</sup>
- Its EW signatures were checked against available 7 and 8 TeV data<sup>3</sup>

**1.** P. Dießner, J. Kalinowski, W. Kotlarski and D. Stöckinger, *JHEP* **1412** (2014) 124

**2.** P. Dießner, J. Kalinowski, W. Kotlarski and D. Stöckinger, *Adv. High Energy Phys.* **2015** (2015) 760729

**3.** P. Dießner, J. Kalinowski, W. Kotlarski and D. Stöckinger, *JHEP* **1603** (2016) 007

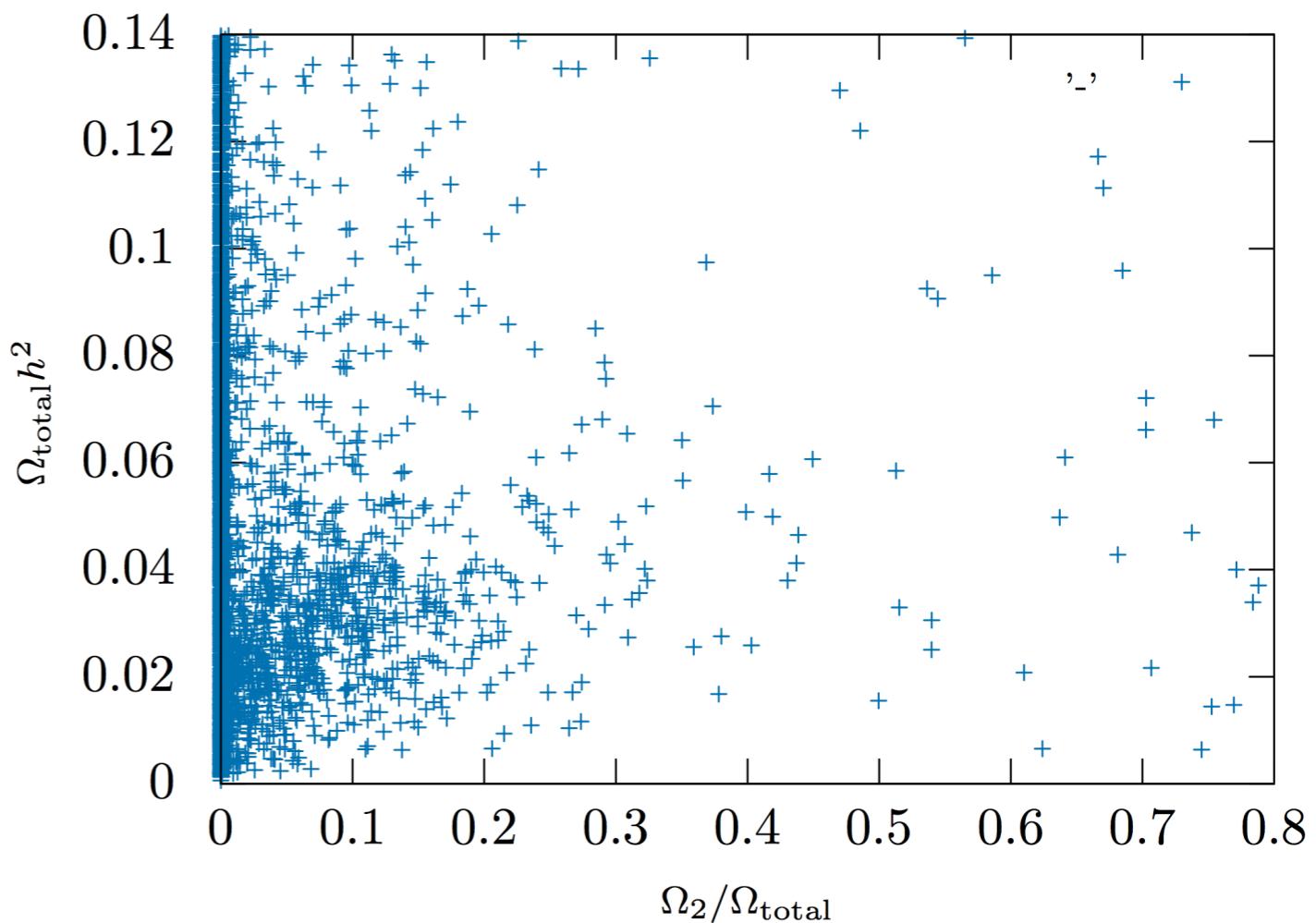


# 2 component dark matter

- consider scenarios where the lightest particle with  $R=1$  is neutralino or sneutrino with mass  $m_{\text{LSP}1}$
- if  $m_{R_1^0} < 2m_{\text{LSP}1}$ , lightest neutral R-Higgs is also stable
- two SUSY dark matter candidates with relic densities  $\Omega_1$  and  $\Omega_2$
- requirements
  - $\Omega_{\text{total}}h^2 \equiv (\Omega_1 + \Omega_2)h^2 \simeq 0.11$
  - substantial fraction  $\Omega_2/\Omega_{\text{total}}$
- (for now) best points are not collinear friendly:

$$m_{\tilde{\chi}_1^0} = 367 \text{ GeV}$$

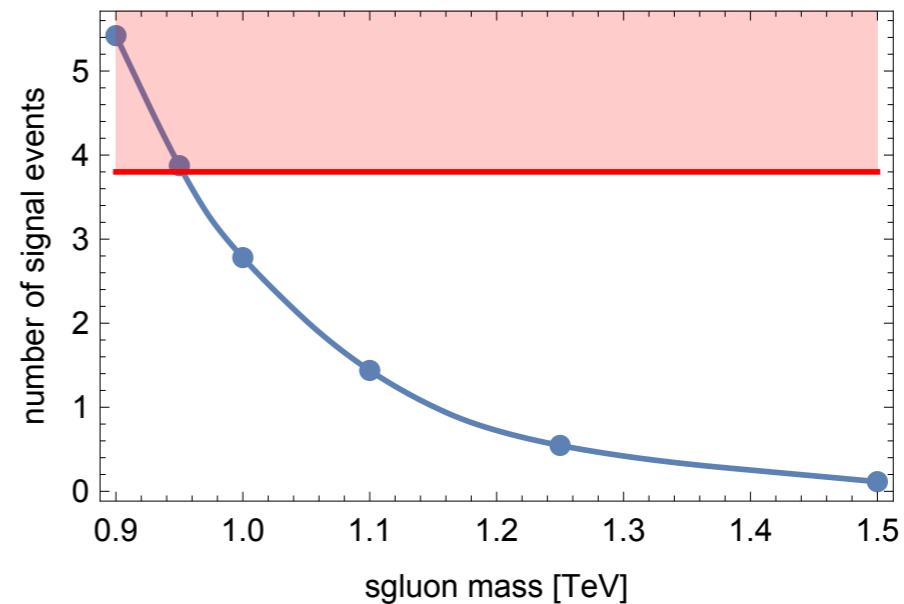
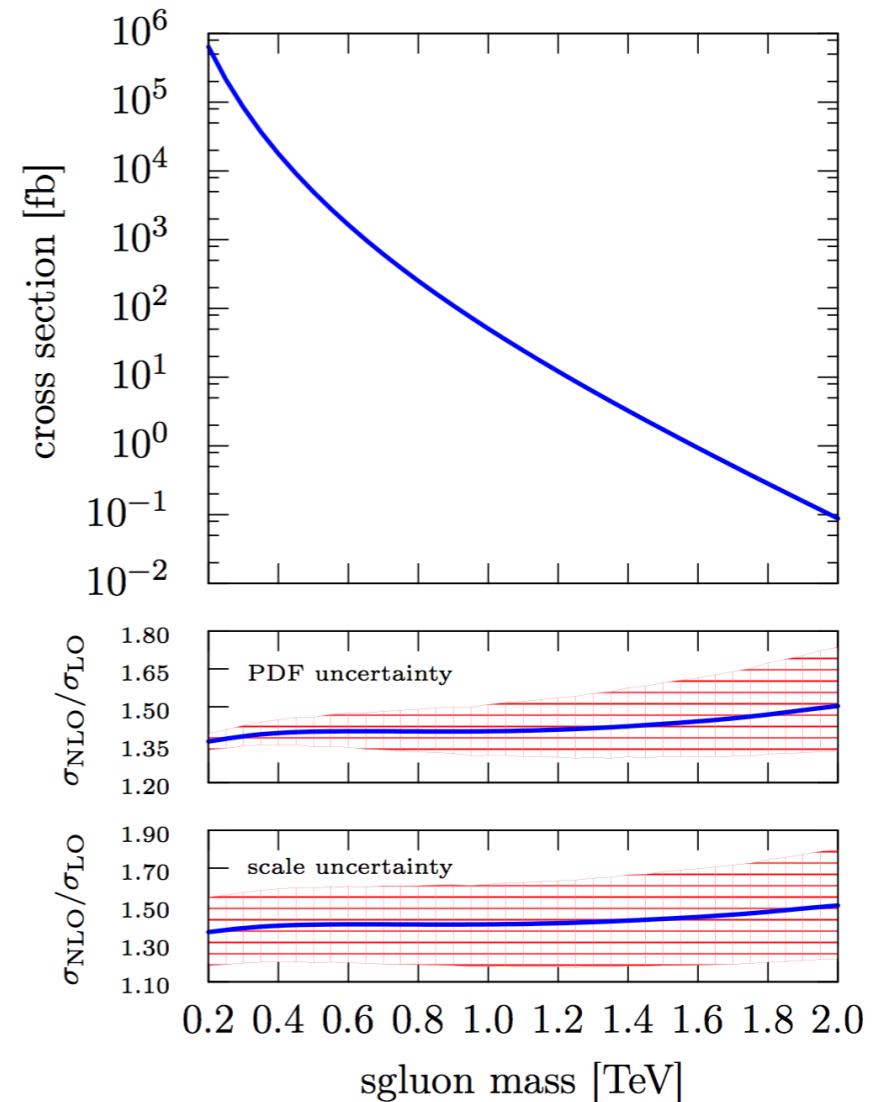
$$m_{R_1^0} = 571 \text{ GeV}$$



# Sgluon pair production at 13 TeV LHC

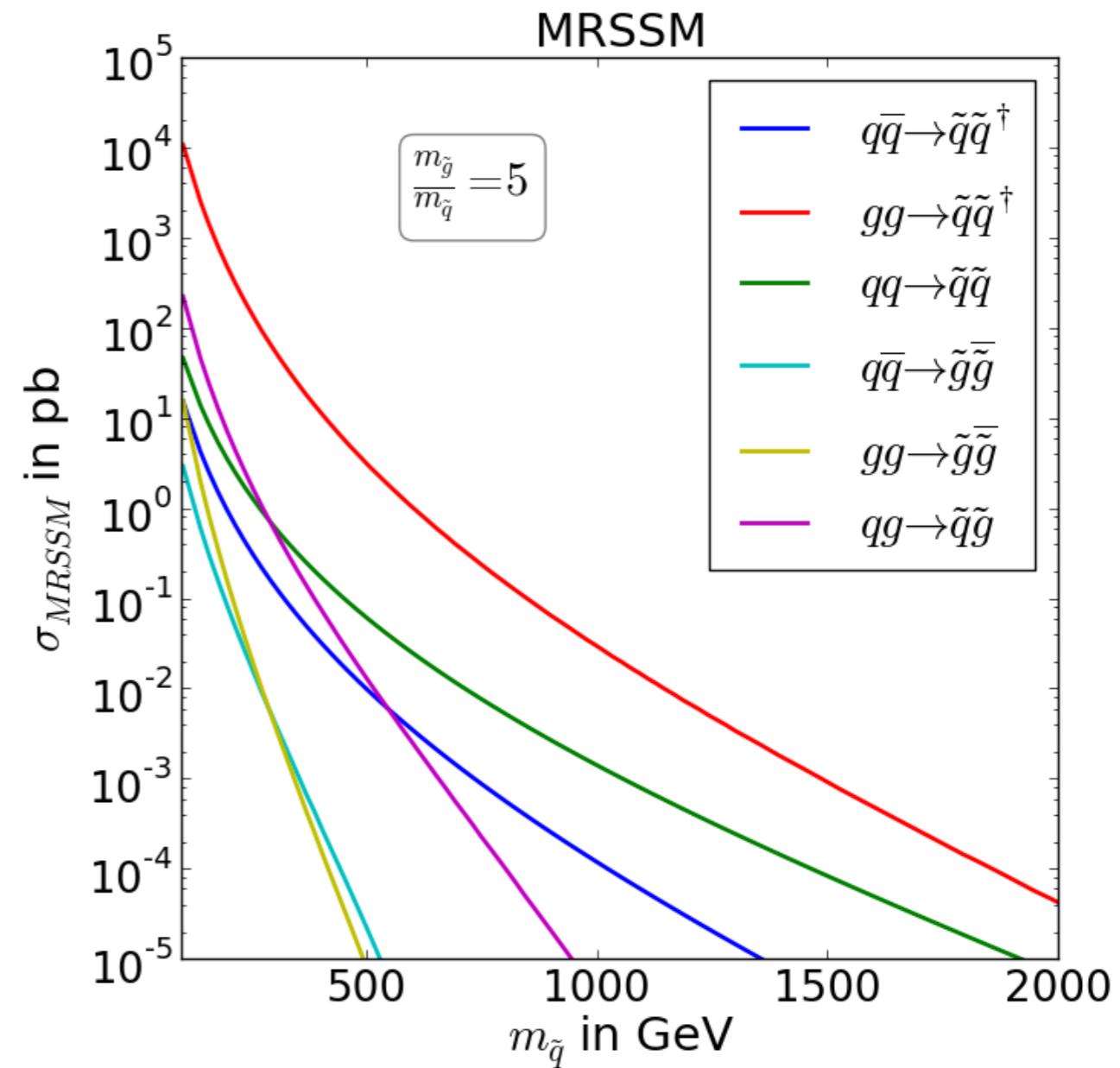
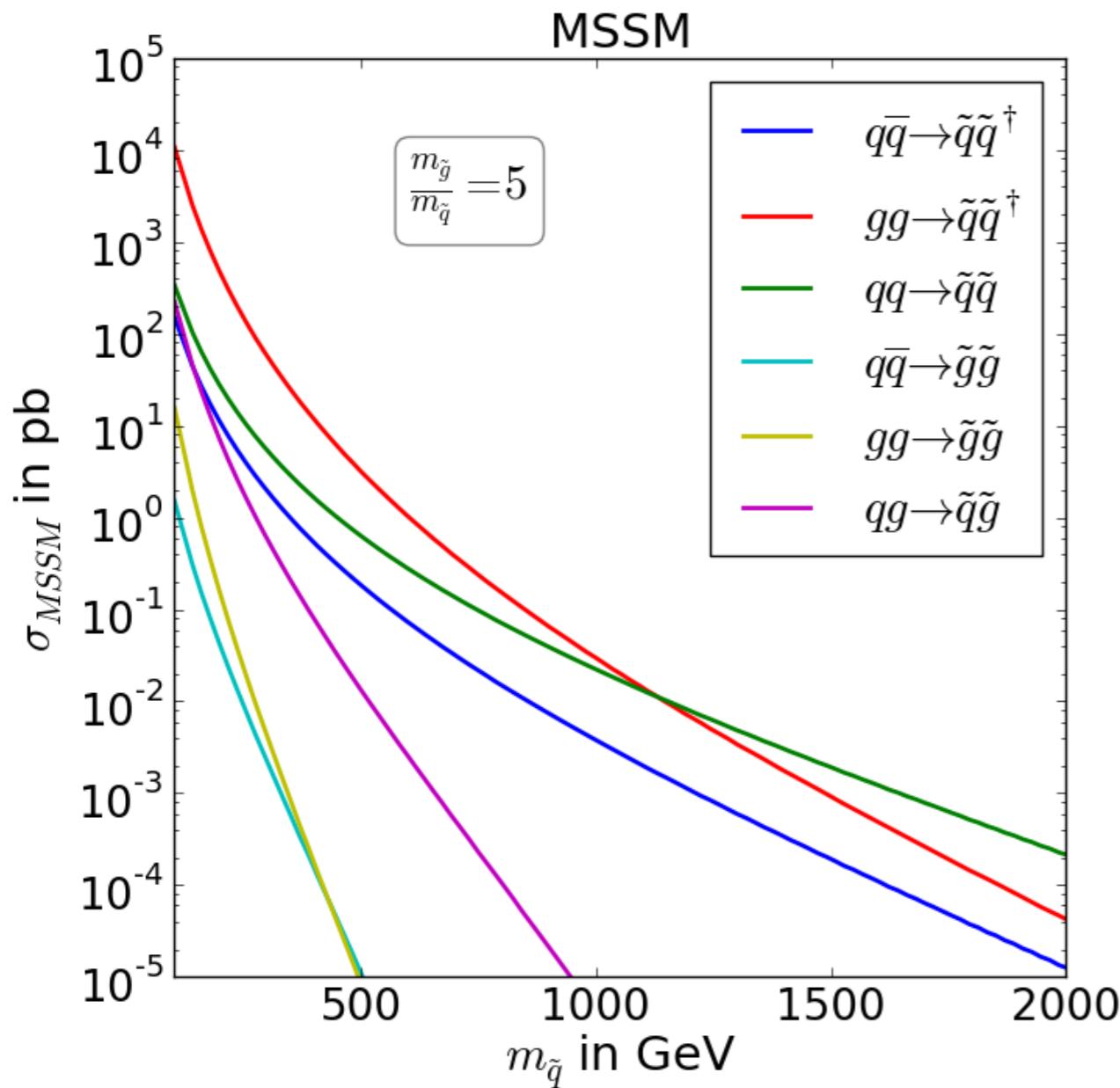
W. Kotlarski [arXiv:1608.00915]

- Analysis of the sgluon pair production with subsequent decay into  $t\bar{t}$  pairs. Recasting ATLAS search in the same-sign lepton channel using 3.2/fb of integrated luminosity
- Signal simulated at NLO using **MadGraph5\_aMC@NLO + FeynRules + NLOCT** and matched to parton shower in the MC@NLO scheme
- Detector response parametrized using **Delphes3**
- Analysis validated on background processes  $t\bar{t}l^+l^-$ ,  $t\bar{t}l^\pm\nu$
- Mass of pair produced real sgluons decaying with  $\text{BR}(O \rightarrow t\bar{t}) = 1$  excluded up to 950 GeV

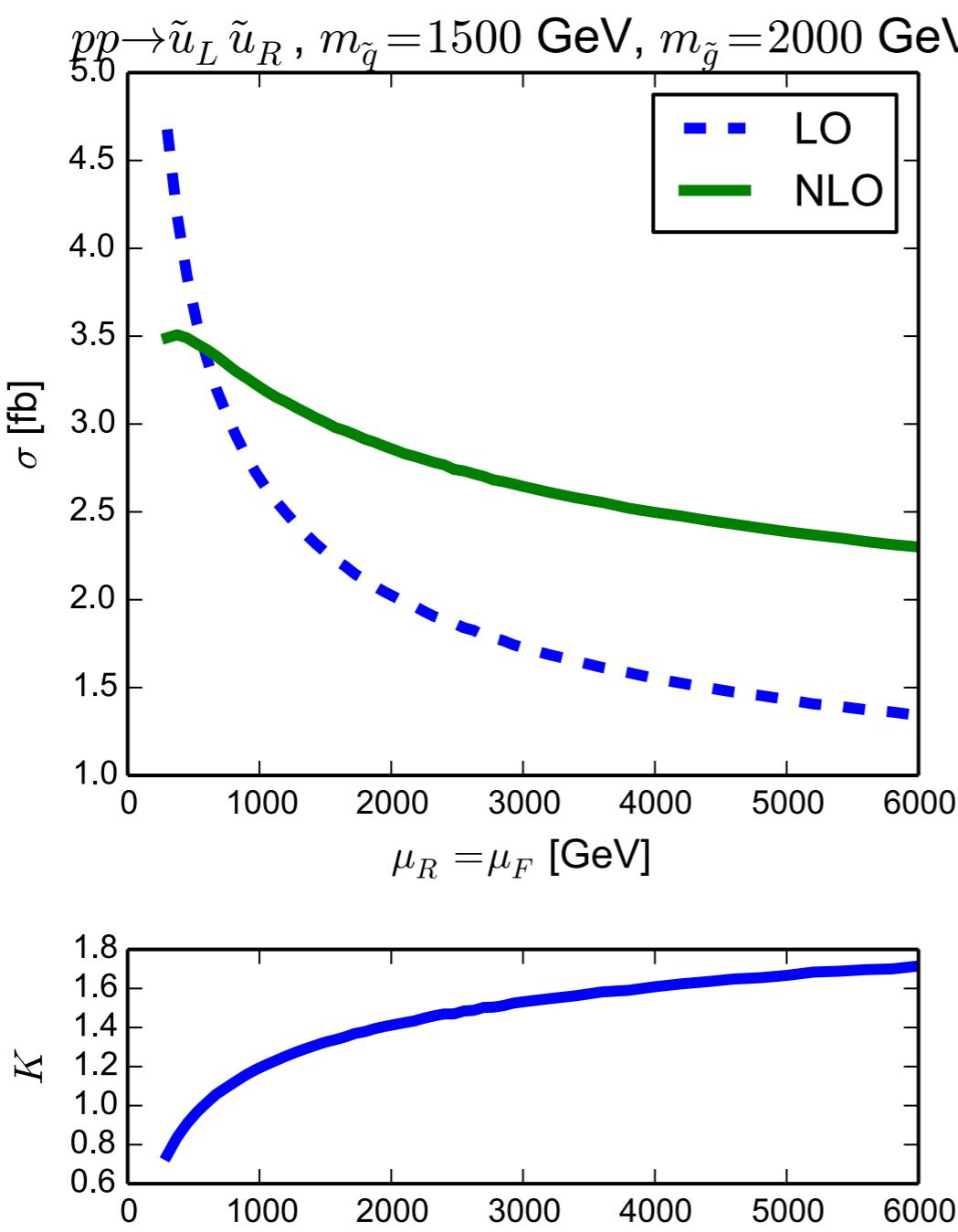


# Leading order analysis

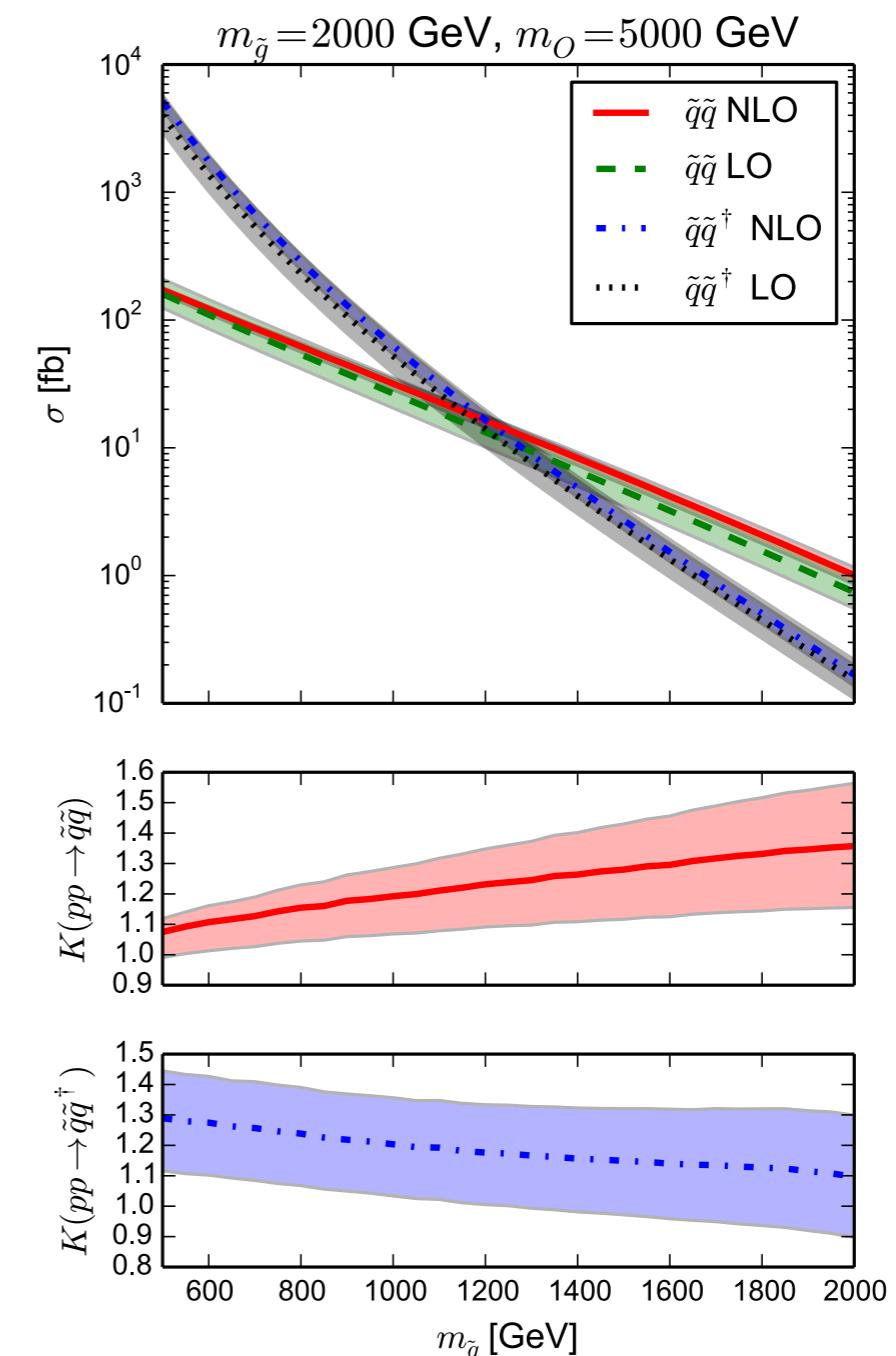
LO cross-sections for sparticle production at the LHC at  $\sqrt{s} = 13\text{TeV}$



# NLO improvements



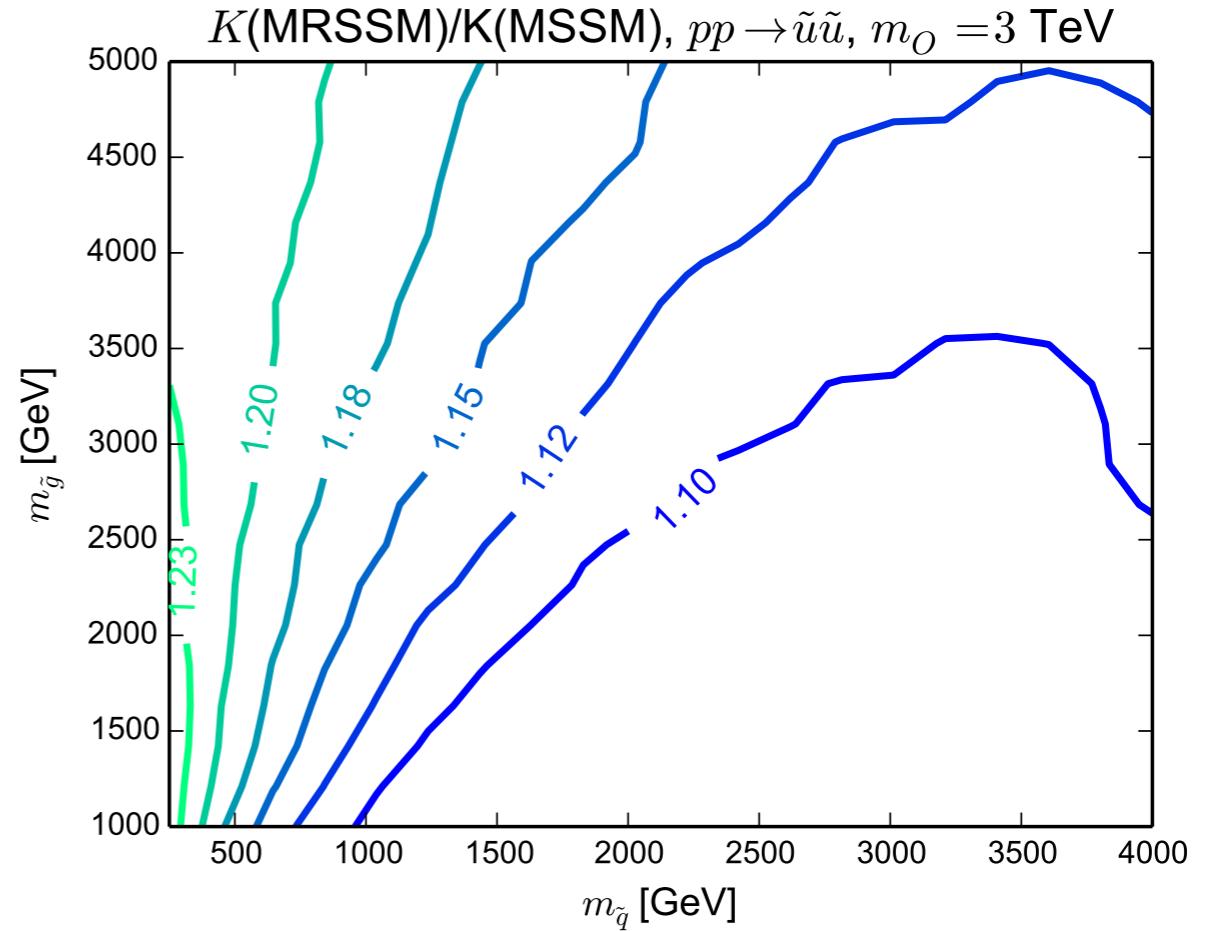
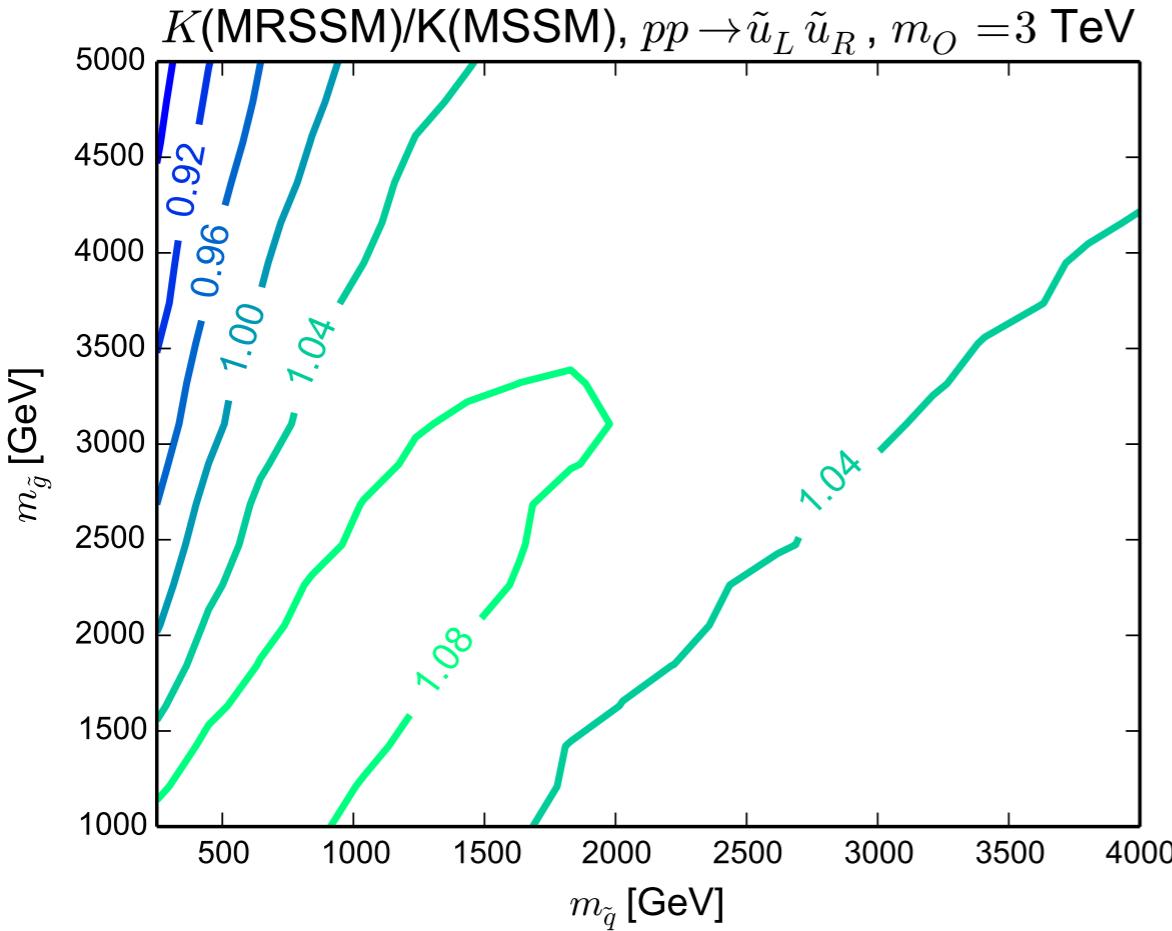
reduction of theoretical uncertainty



right figure  
summed over  
flavors

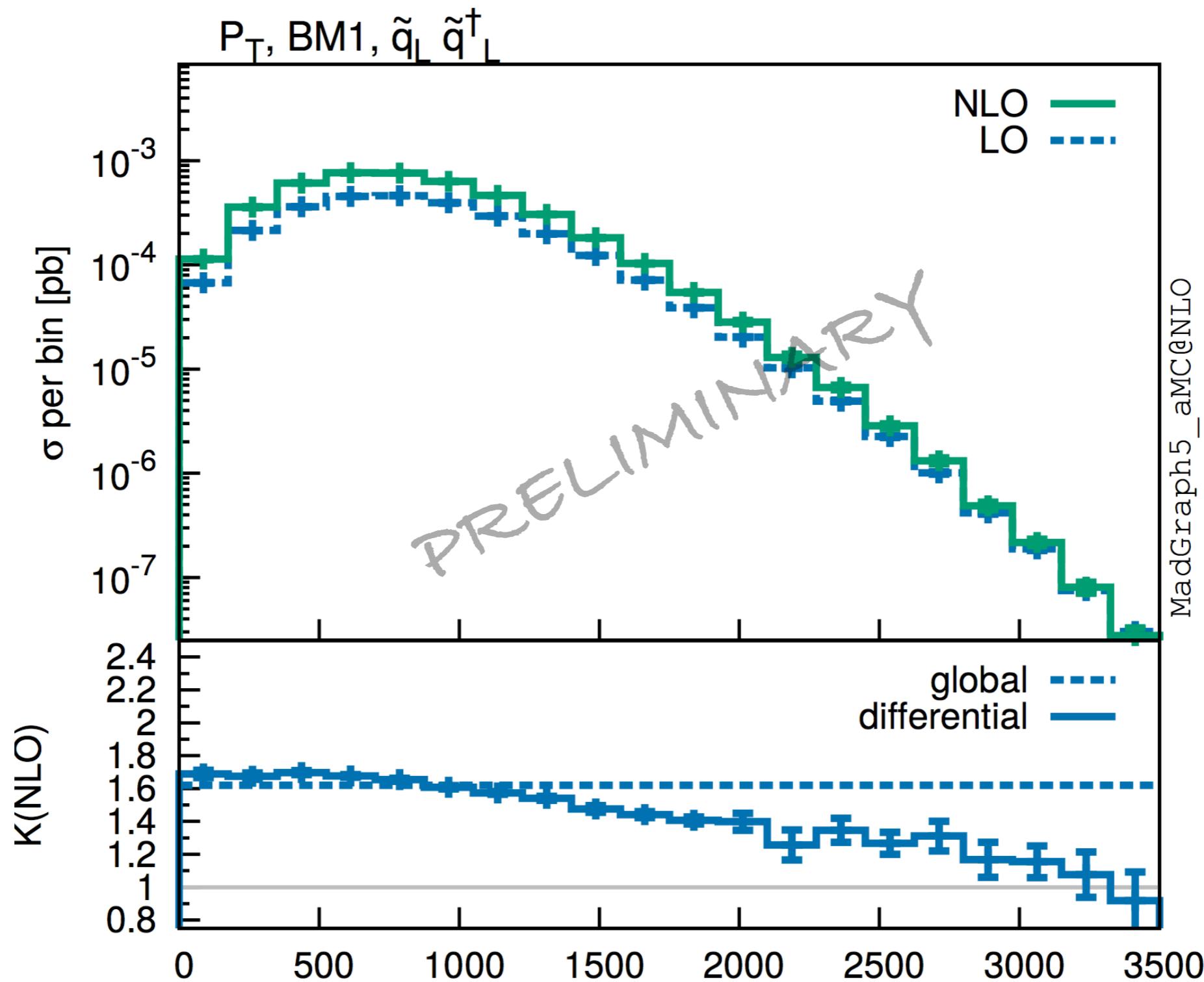
shift of cross-sections

# Comparison with the MSSM



- ✿ Two possible definitions of K-factors:
  - \* unsummed over L- and R-squarks
  - \* summed

# Differential distributions



# $\mu \rightarrow e\gamma$ in the MRSSM

- first analysis performed by Fok and Kribs [*Phys. Rev. D* 82, 035010 (2010)]
- simplifying assumptions:  $M_2, \mu_u \rightarrow \infty$ , only 2 neutralinos containing  $\tilde{B}, \tilde{H}_d$  contribute  
 $m_{\tilde{l}_2} = \frac{3}{2} m_{\tilde{l}}$

