

# Decays of (more or less) exotic Higgs bosons

Heidi Rzehak

CP3 Origins, SDU, Odense



- ▶ Discovery of a Higgs boson
  - ▶ Many searches for new particles
    - Many exclusion limits
  - ▶ Open questions:
    - Dark matter
    - Matter-antimatter asymmetry
    - ...
    - Models addressing these questions often require an extended Higgs sector
- ⇒
- ★ Study properties of discovered Higgs boson
  - ★ Continue searching, also for additional Higgs bosons
- Need precise theory predictions

# Higgs sectors

- Standard Model:

1 CP-even Higgs boson



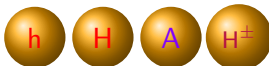
- Singlet extension:

2 CP-even Higgs bosons



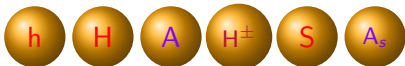
- Two-Higgs-Doublet Model (2HDM):

2 CP-even, 1 CP-odd,  
1 charged Higgs bosons



- Singlet-extended 2HDM:

3 CP-even, 2 CP-odd,  
1 charged Higgs bosons



- Further extensions, e.g. Higgs triplet with doubly charged Higgs boson

→ One Standard Model (like) Higgs boson + possibly “exotic” Higgs bosons

# Higgs sectors

- Standard Model:

1 CP-even Higgs boson



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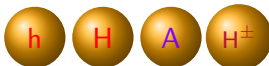
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- Two-Higgs-Doublet Model (2HDM):

MSSM

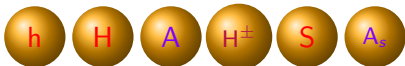
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- Singlet-extended 2HDM:

NMSSM

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# Higgs decays: Partial decay widths

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Many tools include QCD corrections:

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Partly included in spectrum generators:

- SOFTSUSY (MSSM, NMSSM) [Allanach, Cridge 1703.09717]
- SPheno (MSSM — but extendable using Sarah [Staub 1309.7223])  
[Porod hep-ph/0301101; Porod, Staub 1104.1573]
- FeynHiggs (MSSM Higgs spectrum generator  
— partly complete one-loop decays)  
[Bahl, Hahn, Heinemeyer, Hollik, Paßehr, H.R., Weiglein]
- NMSSMTOOLS with NMHDECAY (NMSSM)  
[Ellwanger, Gunion, Hugonie hep-ph/0406215]
- NMSSMCALC (NMSSM Higgs spectrum generator)  
[Baglio, Gröber, Mühlleitner, Nhung, H.R., Spira, Streicher, Walz 1312.4788]

decays  
based on  
HDECAY  
[1003.1643]

# Higgs decays: Partial decay widths

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Many tools include QCD corrections:

HDECAY family: [Djouadi, Kalinowski, (Mühlleitner,) Spira  
hep-ph/9704448, 1003.1643]

Partial decay widths and branching ratios for different models

- MSSM: HDECAY: “mother” program
- sHDECAY: singlet extension  
(different types, also for CP-violation)  
[Costa, Mühlleitner, Sampaio, Santos 1512.05355]
- C2HDECAY: 2HDM extension (also for CP-violation)  
[Fontes, Mühlleitner, Romão, Santos, Silva, Wittbrodt 1711.09419]
- N2HDECY: Singlet extended 2HDM  
[Mühlleitner, Sampaio, Santos, Wittbrodt 1612.01309]
- eHDECAY: minimal composite Higgs models  
(partly also electroweak corrections)  
[Contino, Ghezzi, Grojean, Mühlleitner, Spira 1403.3381]

# Higgs decays: Partial decay widths

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Many tools include QCD corrections:

For distributions:

- MadGraph5\_aMC@NLO

[Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Shao, Stelzer, Torrielli,  
Zaro 1405.0301]

- combining amplitude generator and event generator tools  
(e.g. SHERPA or Herwig++ with OpenLoops)

[SHERPA: Bothmann, Hoeche, Krauss, Kuttimalai, Schoenherr, Schumann,  
Siegert, Thompson, Winter, Zapp;

Herwig++: Bellm, Gieseke, Grellscheid, Kirchga er, Loshaj,  
Nail, Papaefstathiou, Pl tzer, Podskubka, Rauch, Reuschle, Richardson,  
Schichtel, Seymour, Si dmok, Webster;

OpenLoops: Cascioli, Lindert, Maierh fer, Pozzorini]



# Including electroweak (EW) corrections

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Full one-loop corrections using a  $\overline{\text{DR}}$  scheme:

- HFOLD [Eberl, Frisch, Hlucha 1012.5025]
- SARAH [Goodsell, Lieber, Staub 1703.09237]

Problem with  $\overline{\text{DR}}$  scheme:

LSZ theorem requires on-shell properties for external particles

→ shift from  $\overline{\text{DR}}$  mass to on-shell mass mixes orders

→ use as many on-shell conditions as possible

for example for the MSSM [Heinemeyer, Schappacher 1503.02996]

for the NMSSM [Domingo, Heinemeyer, Paßehr, Weiglein 1807.06322]

→ see talk by Sven Heinemeyer

More general tool: RECOLA2 for processes incl. EW corrections

[Denner, Lang, Uccirati 1705.06053]

# Two-Higgs-Doublet Model

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Simple extension of the Standard Model:

- Only one Higgs doublet added to the Standard Model
- Simplest extension containing a charged Higgs boson (3 neutral, 2 charged)
- Embedded in other, more “complete” theories, e.g. supersymmetric extensions such as the MSSM

# Two-Higgs-Doublet Model

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Higgs potential:

$$\begin{aligned} V = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 + m_{12}^2 (\Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ & + \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) \\ & + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \lambda_5 \left[ (\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2 \right] \end{aligned}$$

- CP conserving
- invariant under  $\Phi_1 \rightarrow -\Phi_1$  for  $m_{12}^2 = 0$  (we use  $m_{12} \neq 0$ )

with the complex scalar  $SU(2)$  doublets:

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1^+ \\ v_1 + \eta_1 + i\chi_1 \end{pmatrix} \quad \Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_2^+ \\ v_2 + \eta_2 + i\chi_2 \end{pmatrix}$$

# Two-Higgs-Doublet Model

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- CP conserving
  - invariant under  $\Phi_1 \rightarrow -\Phi_1$  for  $m_{12}^2 = 0$  (we use  $m_{12} \neq 0$ )
  - $m_{11}^2, m_{22}^2$  fixed by minimum condition  
 $m_{12}^2, \lambda_1, \dots, \lambda_5$  free parameters
- $\Rightarrow$  enough free parameters to define all Higgs masses independently
- $\Rightarrow$  all Higgs masses can be chosen as pole masses (on-shell)

# Higgs-mass eigenstates

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CP-even Higgs bosons:

$$\begin{pmatrix} H \\ h \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \eta_1 \\ \eta_2 \end{pmatrix}$$

CP-odd Higgs bosons:

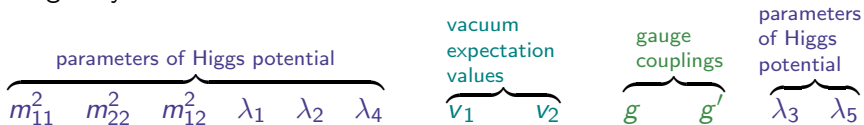
$$\begin{pmatrix} G^0 \\ A^0 \end{pmatrix} = \begin{pmatrix} \cos \beta_n & \sin \beta_n \\ -\sin \beta_n & \cos \beta_n \end{pmatrix} \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix} \quad \text{with} \quad \tan \beta_n = \tan \beta = \frac{v_2}{v_1} \text{ at LO}$$

Charged Higgs bosons:

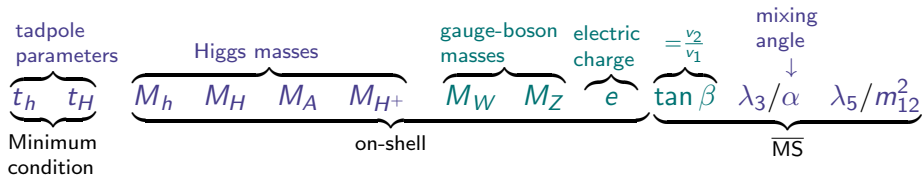
$$\begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix} = \begin{pmatrix} \cos \beta_c & \sin \beta_c \\ -\sin \beta_c & \cos \beta_c \end{pmatrix} \begin{pmatrix} \phi_{1^\pm} \\ \phi_{2^\pm} \end{pmatrix} \quad \text{with} \quad \tan \beta_c = \tan \beta \text{ at LO}$$

# Input parameters

Originally:



Chosen:



# Renormalization

see also [Santos, Barroso 97; Kanemura, Okada, Senaha, Yuan hep-ph/0408364; Lopez-Val, Sola 0908.2898; Degrande 1406.3030]

On-shell renormalization: [Krause, Mühlleitner, Lorenz, Santos, Ziesche 1605.04853; Denner, Jenniches, Lang, Sturm 1607.07352; Krause, Mühlleitner, Santos, Ziesche 1609.04185; Altenkamp, Dittmaier, H.R. 1704.02645]

- Masses  $M_h, M_H, M_A, M_{H^\pm}, M_W, M_Z$ : Pole masses
- Fields exploiting matrix-valued renormalization:

$$\begin{pmatrix} H_0 \\ h_0 \end{pmatrix} = \begin{pmatrix} 1 + \frac{1}{2}\delta Z_H & \frac{1}{2}\delta Z_{Hh} \\ \frac{1}{2}\delta Z_{hH} & 1 + \frac{1}{2}\delta Z_h \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix} \text{ etc.}$$

→ no mixing of external on-shell fields

- Electric charge: via  $ee\gamma$  vertex in the Thomson limit

$\overline{\text{MS}}$  renormalization:

- $\tan \beta$
  - $\lambda_3$  or  $\alpha$
  - $\lambda_5$  or  $m_{12}^2$  or  $M_{ab}^2$
- } → renormalization-scale dependent parameter

## Remark about mixing angles

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A priori: at NLO not well-defined:

can be absorbed by field-renormalization constants

→ no need to renormalize mixing angles

**But:** If original parameters replaced by mixing angles

→ mixing angle fixed via the relation between  
original parameter and  $\alpha$



# Tadpole renormalization

Two variants:

a) Vanishing renormalized tadpoles:  $t_{S,0} = \overbrace{t_S}^{=0} + \delta t_S$

Condition:  $\delta t_S + (\text{explicit tadpole loops}) = 0$

Advantage: No explicit tadpole diagrams need to be included

Disadvantage:  $t_{S,0} = \delta t_S$  enters in relations between bare input parameters

→ potentially gauge-dependent terms enter relations between renormalized parameters and observables

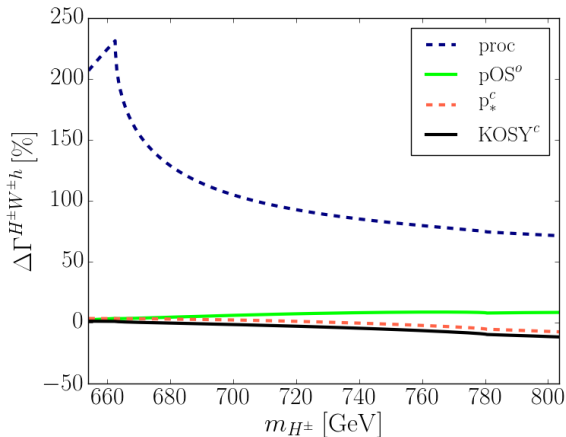
b) Vanishing bare tadpoles:  $t_{S,0} = 0$  [Fleischer, Jegerlehner 80; Actis, Ferroglia, Passera, Passarino hep-ph/0612122]

Now: Explicit tadpole diagrams have to be taken into account

Advantage: No gauge-dependent  $\delta t_S$  enters in relations between bare input parameters

→ relation between renormalized parameters and observables are gauge independent

# $H^+ \rightarrow hW^+$ in 2HDM



- complete EW contributions
- different renormalization schemes:
  - ★ only  $t_S = 0$  for KOSY otherwise  $t_{S,0} = 0$
  - ★  $\alpha, \beta$  renormalized
  - ★ pinch technique for pOS, p<sup>★</sup>
- no parameter conversion taken into account

[Krause, Lorenz, Mühlleitner, Santos, Ziesche 1608.01880]

## Four possibilities for $\lambda_3/\alpha$ and $\beta$

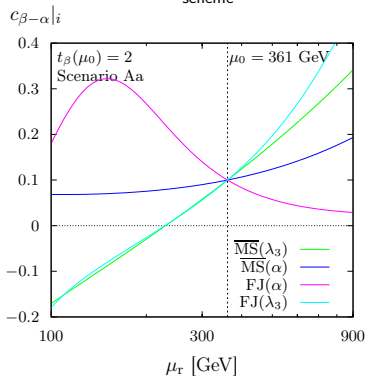
- Scheme  $\lambda_{3\overline{MS}}$ : see [Altenkamp, Dittmaier, H.R. 1704.02645]  
 $\lambda_3 \overline{MS}, \tan \beta \overline{MS}$   
tadpole scheme:  $t_5 = 0$
- Scheme  $\alpha_{\overline{MS}}$ :  
 $\alpha$  instead of  $\lambda_3$ :  $\alpha \overline{MS}, \tan \beta \overline{MS}$   
tadpole scheme:  $t_5 = 0$
- Scheme FJ:  
 $\alpha \overline{MS}, \tan \beta \overline{MS}$   
tadpole scheme:  $t_{5,0} = 0$  see also [Krause, Mühlleitner, Lorenz, Santos, Ziesche 1605.04853; Denner, Jenniches, Lang, Sturm 1607.07352]
- Scheme FJ  $\lambda_3$ :  
 $\lambda_3 \overline{MS}, \tan \beta \overline{MS}$   
tadpole scheme:  $t_{5,0} = 0$

# Running of $\cos(\beta - \alpha)$ in different schemes

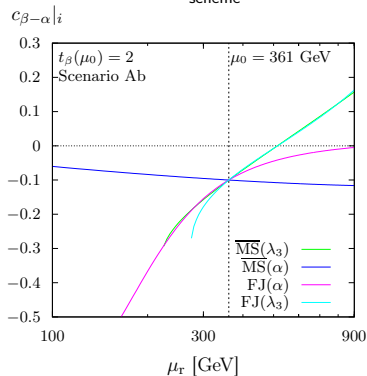
[Altenkamp, Dittmaier, H.R. 1704.02645, 1710.07598]

Scenario A:  $M_h = 125$  GeV,  $M_H = 300$  GeV,  $M_{A_0} = M_{H^+} = 460$  GeV,  $\lambda_5 = -1.9$ ,  $\tan \beta = 2$   
 $\mu_0 = M_h + M_H + M_A + 2M_{H^+}$  for 2HDM type 1, see [Haber, Stål, 1507.04281]

Aa:  $\cos(\beta - \alpha)|_{\text{input scheme}}(\mu_0) = 0.1$ :



Ab:  $\cos(\beta - \alpha)|_{\text{input scheme}}(\mu_0) = -0.1$ :

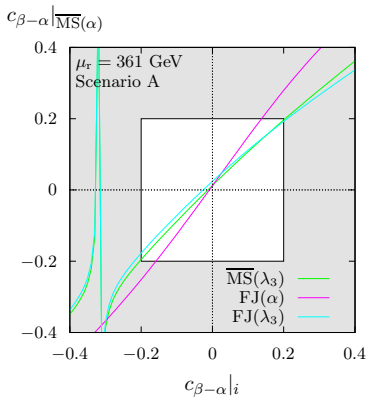
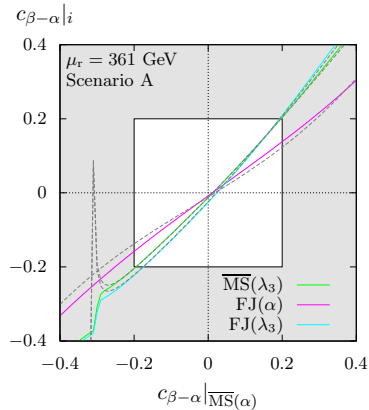


⇒ sizeable running effects

# Conversion of parameters

[Altenkamp, Dittmaier, H.R. 1704.02645, 1710.07598]

Conversion:  $p_{RS2} = p_{RS1} + \delta p_{RS1}(p_{RS1}) - \delta p_{RS2}(p_{RS2})$

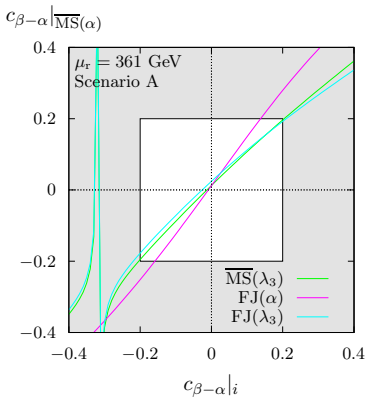
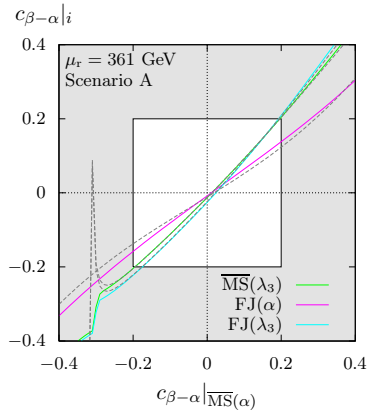


- Scenarios depend on the chosen renormalization scheme.

# Conversion of parameters

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Conversion:  $p_{RS2} = p_{RS1} + \delta p_{RS1}(p_{RS1}) - \delta p_{RS2}(p_{RS2})$



- Peak region:  $\lambda_3$  is a bad input parameter if  $\cos(2\alpha) \approx 0$ ,  
(to avoid the issue: choose different  $\lambda_j$ ).

# Implementation in PROPHECY4F

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PROPHECY4F: A Monte Carlo generator for a

Proper description of the Higgs decay into 4 fermions

[Bredenstein, Denner, Dittmaier, Weber hep-ph/0604011; hep-ph/0607060; hep-ph/0611234]

→ use the functionality of PROPHECY4F for 2HDM

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## Implementation:

- model file generation with and without FeynRules [Christensen, Duhr 0806.4194]



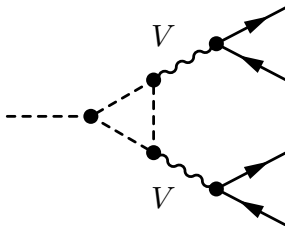
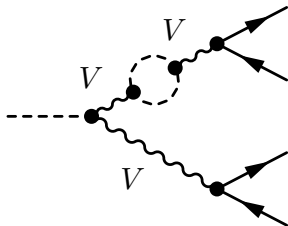
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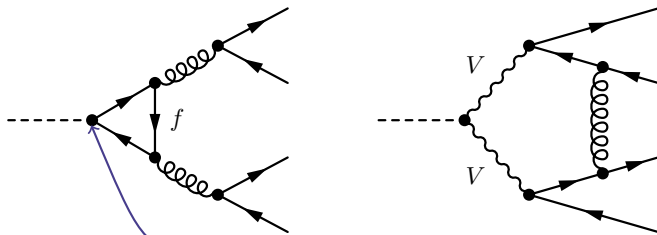
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virtual QCD diagrams: obtained by proper rescaling of Higgs couplings



depends on type of 2HDM: 4 types implemented

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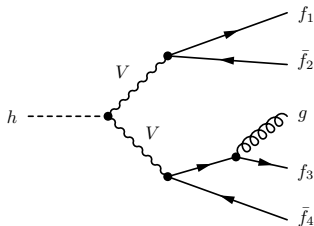
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virtual QCD diagrams: obtained by proper rescaling of Higgs couplings

real diagrams: obtained by rescaling of Higgs coupling  $g_{hVV} = \sin(\beta - \alpha)g_{hVV}^{\text{SM}}$



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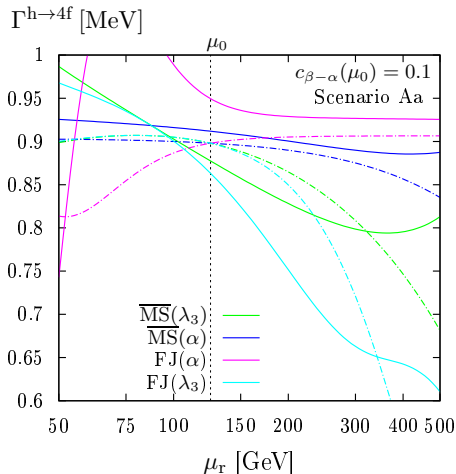
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- $W/Z$  resonances treated in complex-mass scheme
- evaluation of loop integrals with **Collier** [Denner, Dittmaier, Hofer 1604.06792]
- infrared divergences treated with dipole subtraction  
[Catani, Seymour hep-ph/9605323; Dittmaier hep-ph/9904440]

# $\mu_r$ dependence of $\Gamma(h \rightarrow 4f)$

[Altenkamp, Dittmaier, H.R. 1704.02645]



“naive” scale:  $\mu_0 = M_h$

LO: dashed

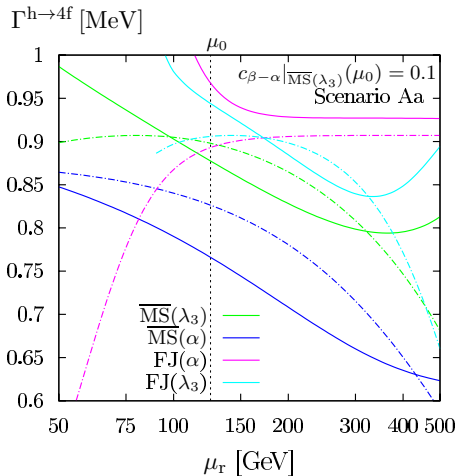
NLO EW: solid

- No conversion: scenario interpreted as given in respective scheme
- No clear plateau around  $\mu_r = \mu_0$  at NLO



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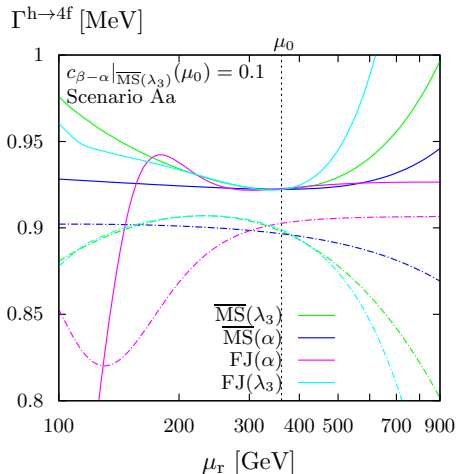
LO: dashed

NLO EW: solid

- Scheme  $\lambda_3 \overline{\text{MS}}$  used
- With conversion:  
Sizeable effects already at LO
- No clear plateau around  
 $\mu_r = \mu_0$  at NLO

# $\mu_r$ dependence of $\Gamma(h \rightarrow 4f)$

[Altenkamp, Dittmaier, H.R. 1704.02645]



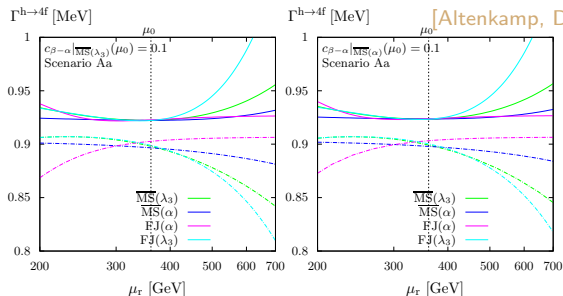
$$\mu_0 = (M_h + M_H + M_{A_0} + 2M_{H^+})/5$$

LO: dashed

NLO EW: solid

- Scheme  $\lambda_3 \overline{\text{MS}}$  used
- Clear plateau around  $\mu_r = \mu_0$  at NLO
- Scale dependence reduced from LO to NLO

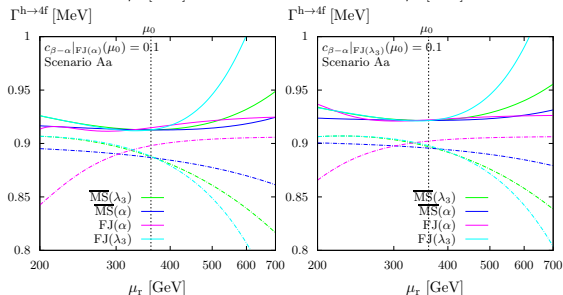
# $\mu_r$ dependence of $\Gamma(h \rightarrow 4f)$



[Altenkamp, Dittmaier, H.R. 1710.07598]

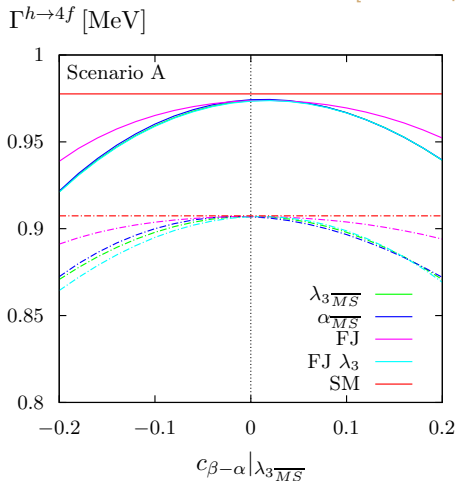
For all input schemes:

- Clear plateau
- Reduction of scale dependence from LO to NLO



# $\cos(\beta - \alpha)$ dependence of $\Gamma(h \rightarrow 4f)$

[Altenkamp, Dittmaier, H.R. 1704.02645, 1710.07598]



$$\mu_0 = (M_h + M_H + M_{A_0} + 2M_{H^\pm})/5$$

LO: dashed

NLO: solid

• Scheme  $\lambda_3 \overline{MS}$  used:

$$\Gamma_{2\text{HDM, LO}}^{h \rightarrow 4f} |_{\lambda_3, \overline{MS}} = s_{\beta-\alpha}^2 \Gamma_{\text{SM, LO}}^{h \rightarrow 4f}$$

# Partial decay widths for scenario Ab (scheme $\lambda_3 \overline{\text{MS}}$ )

Final state	$\Gamma_{\text{NLO}}^{h \rightarrow 4f}$ [MeV]	$\delta_{\text{EW}}$ [%]	$\delta_{\text{QCD}}$ [%]	$\Delta_{\text{SM}}^{\text{NLO}}$ [%]	$\Delta_{\text{SM}}^{\text{LO}}$ [%]
<i>inclusive <math>h \rightarrow 4f</math></i>	<i>0.95980(7)</i>	<i>1.87(0)</i>	<i>4.97(1)</i>	<i>-1.82(1)</i>	<i>-1.00(1)</i>
ZZ	0.105464(5)	-0.34(0)	4.90(0)	-1.75(1)	-1.00(0)
WW	0.85938(8)	2.14(0)	5.01(1)	-1.83(1)	-1.00(1)
WW/ZZ int.	-0.00504(5)	0.5(1)	10.7(8)	-2(1)	-1(1)
$\nu_e e^+ \mu^- \bar{\nu}_\mu$	0.010116(1)	2.17(1)	0.00	-1.87(1)	-1.00(1)
$\nu_e e^+ u \bar{d}$	0.031463(4)	2.16(0)	3.76(1)	-1.84(2)	-1.00(1)
$u \bar{d} s \bar{c}$	0.09770(2)	2.11(0)	7.52(1)	-1.81(2)	-1.00(1)
$\nu_e e^+ e^- \bar{\nu}_e$	0.010112(1)	2.27(1)	0.00	-1.87(1)	-1.00(1)
$u \bar{d} d \bar{u}$	0.09972(2)	1.99(0)	7.38(2)	-1.80(2)	-1.00(1)
$\nu_e \bar{\nu}_e \nu_\mu \bar{\nu}_\mu$	0.000943(0)	2.34(0)	0.00	-1.78(1)	-1.00(1)
$e^- e^+ \mu^- \mu^+$	0.000237(0)	0.62(1)	0.00	-1.79(2)	-1.00(1)
$\nu_e \bar{\nu}_e \mu^- \mu^+$	0.000474(0)	1.78(1)	0.00	-1.78(2)	-1.00(1)
$\nu_e \bar{\nu}_e \nu_e \bar{\nu}_e$	0.000565(0)	2.23(0)	0.00	-1.79(2)	-1.00(1)
$e^- e^+ e^- e^+$	0.000131(0)	0.45(1)	0.00	-1.78(2)	-1.00(1)
$\nu_e \bar{\nu}_e u \bar{u}$	0.001668(0)	-0.08(1)	3.76(1)	-1.76(2)	-1.00(1)
$\nu_e \bar{\nu}_e d \bar{d}$	0.002163(0)	1.02(0)	3.76(1)	-1.76(2)	-1.00(1)
$e^- e^+ u \bar{u}$	0.000840(0)	-0.57(1)	3.76(1)	-1.77(2)	-1.00(1)
$e^- e^+ d \bar{d}$	0.001081(0)	-0.21(1)	3.76(1)	-1.76(2)	-1.00(1)
$u \bar{u} c \bar{c}$	0.002952(0)	-2.48(1)	7.51(1)	-1.75(2)	-1.00(1)
$d \bar{d} d \bar{d}$	0.002545(1)	-1.06(0)	4.57(2)	-1.67(3)	-1.00(1)
$d \bar{d} s \bar{s}$	0.004925(1)	-1.04(0)	7.51(1)	-1.74(2)	-1.00(1)
$u \bar{u} s \bar{s}$	0.003828(1)	-1.35(1)	7.51(1)	-1.74(2)	-1.00(1)
$u \bar{u} u \bar{u}$	0.001500(0)	-2.60(1)	4.31(2)	-1.65(3)	-1.00(1)

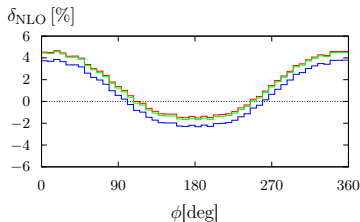
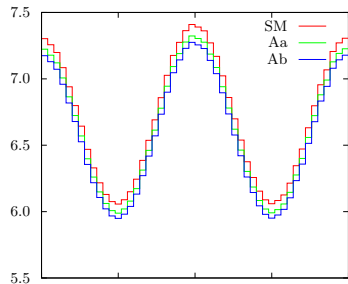
# Example distribution

$$\frac{d\Gamma}{d\phi} \left[ 10^{-7} \frac{\text{MeV}}{\text{deg}} \right] \quad h \rightarrow \mu^- \mu^+ e^- e^+$$

[Altenkamp, Dittmaier, H.R. 1710.07598]

$$\mu_0 = (M_h + M_H + M_{A_0} + 2M_{H^\pm})/5$$

- Scheme  $\lambda_3 \overline{\text{MS}}$  used
- negligible shape differences between SM and 2HDM



# Summary

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- A variety of tools for BSM models available including at least:
  - ★ partly QCD corrections
  - ★ partial decay widths (often no distributions)
- Complete NLO predictions including electroweak corrections are becoming available:

Different renormalization schemes available:

- ⇒ Consistent conversion of parameters between the different renormalization schemes has to be performed
- Useful for theory uncertainty estimate
- ★ Effects of running and conversion of parameters can be sizeable
- For  $\Gamma(h \rightarrow 4f)$ : Deviation from the SM about 0 to -6%  
NLO corrections contribute 1–2%.
- PROPHECY4F: Extended to the 2HDM (& to the singlet extension) available on request

[Altenkamp, Boggia, Dittmaier 1801.07291]

# Mixing angles and field renormalization

$$\begin{pmatrix} \varphi_{1,0} \\ \varphi_{2,0} \end{pmatrix} = \mathbf{R}_\varphi(\theta_0) \begin{pmatrix} h_{1,0} \\ h_{2,0} \end{pmatrix} = \begin{pmatrix} c_{\theta,0} & -s_{\theta,0} \\ s_{\theta,0} & c_{\theta,0} \end{pmatrix} \begin{pmatrix} h_{1,0} \\ h_{2,0} \end{pmatrix},$$

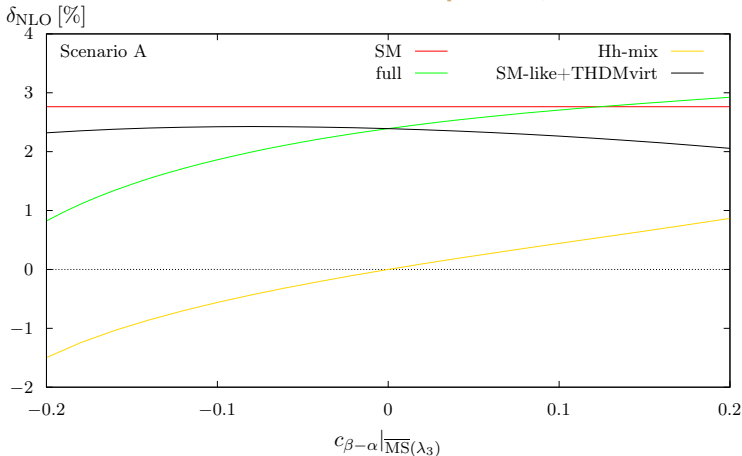
$$\begin{pmatrix} h_{1,0} \\ h_{2,0} \end{pmatrix} = \begin{pmatrix} 1 + \frac{1}{2}\delta Z_{h_1 h_1} & \frac{1}{2}\delta Z_{h_1 h_2} \\ \frac{1}{2}\delta Z_{h_2 h_1} & 1 + \frac{1}{2}\delta Z_{h_2 h_2} \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}, \quad \theta_0 = \theta + \delta\theta.$$

$$\begin{aligned} \begin{pmatrix} \varphi_{1,0} \\ \varphi_{2,0} \end{pmatrix} &= \left[ \begin{pmatrix} c_\theta & -s_\theta \\ s_\theta & c_\theta \end{pmatrix} \begin{pmatrix} 1 + \frac{1}{2}\delta Z_{h_1 h_1} & \frac{1}{2}\delta Z_{h_1 h_2} \\ \frac{1}{2}\delta Z_{h_2 h_1} & 1 + \frac{1}{2}\delta Z_{h_2 h_2} \end{pmatrix} + \begin{pmatrix} -s_\theta & -c_\theta \\ c_\theta & -s_\theta \end{pmatrix} \delta\theta \right] \begin{pmatrix} h_1 \\ h_2 \end{pmatrix} \\ &= \begin{pmatrix} c_\theta & -s_\theta \\ s_\theta & c_\theta \end{pmatrix} \begin{pmatrix} 1 + \frac{1}{2}\delta Z_{h_1 h_1} & \frac{1}{2}(\delta Z_{h_1 h_2} - 2\delta\theta) \\ \frac{1}{2}(\delta Z_{h_2 h_1} + 2\delta\theta) & 1 + \frac{1}{2}\delta Z_{h_2 h_2} \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}. \end{aligned}$$



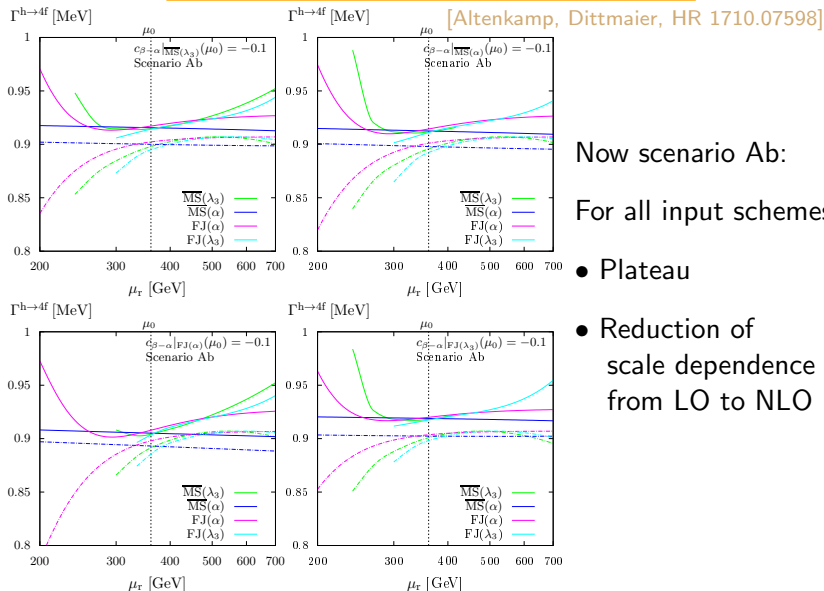
# Contributions to NLO corrections

[Altenkamp, Dittmaier, HR 1710.07598]



- Higgs mixing contributions important for dependence of NLO corrections on  $\cos(\beta - \alpha)$

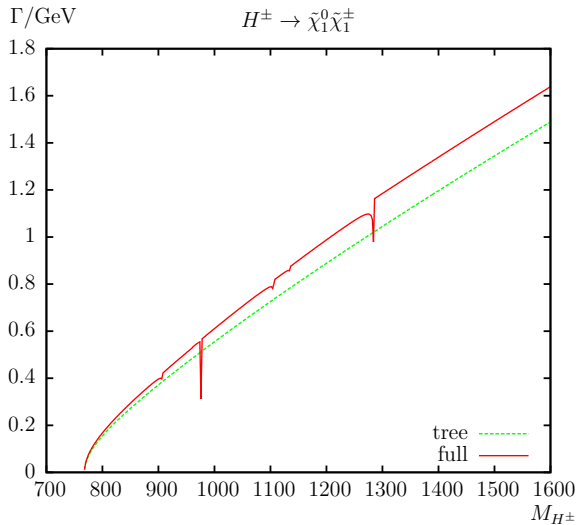
# $\mu_r$ dependence of $\Gamma(h \rightarrow 4f)$



# Partial decay widths for scenario Aa (scheme $\lambda_3 \overline{\text{MS}}$ )

Final state	$\Gamma_{\text{NLO}}^{h \rightarrow 4f}$ [MeV]	$\delta_{\text{EW}}$ [%]	$\delta_{\text{QCD}}$ [%]	$\Delta_{\text{SM}}^{\text{NLO}}$ [%]	$\Delta_{\text{SM}}^{\text{LO}}$ [%]
inclusive $h \rightarrow 4f$	0.96730(7)	2.71(0)	4.96(1)	-1.05(1)	-1.00(1)
ZZ	0.106126(6)	0.34(0)	4.88(0)	-1.13(1)	-1.00(0)
WW	0.86630(8)	3.00(0)	5.01(1)	-1.04(1)	-1.00(1)
WW/ZZ int.	-0.00513(5)	1.3(2)	12.0(8)	-1(1)	-1(1)
$\nu_e e^+ \mu^- \bar{\nu}_\mu$	0.010201(1)	3.03(0)	0.00	-1.04(1)	-1.00(1)
$\nu_e e^+ u \bar{d}$	0.031719(4)	3.02(0)	3.76(1)	-1.04(2)	-1.00(1)
$u \bar{d} s \bar{c}$	0.09847(2)	2.97(0)	7.52(1)	-1.04(2)	-1.00(1)
$\nu_e e^+ e^- \bar{\nu}_e$	0.010197(1)	3.12(0)	0.00	-1.04(1)	-1.00(1)
$u \bar{d} d \bar{u}$	0.10048(2)	2.85(0)	7.35(2)	-1.06(3)	-1.00(1)
$\nu_e \bar{\nu}_e \nu_\mu \bar{\nu}_\mu$	0.000949(0)	3.01(0)	0.00	-1.14(1)	-1.00(1)
$e^- e^+ \mu^- \mu^+$	0.000239(0)	1.30(1)	0.00	-1.13(2)	-1.00(1)
$\nu_e \bar{\nu}_e \mu^- \mu^+$	0.000477(0)	2.45(1)	0.00	-1.13(2)	-1.00(1)
$\nu_e \bar{\nu}_e \nu_e \bar{\nu}_e$	0.000569(0)	2.90(0)	0.00	-1.14(2)	-1.00(1)
$e^- e^+ e^- e^+$	0.000132(0)	1.12(1)	0.00	-1.12(2)	-1.00(1)
$\nu_e \bar{\nu}_e u \bar{u}$	0.001679(0)	0.60(1)	3.76(1)	-1.12(2)	-1.00(1)
$\nu_e \bar{\nu}_e d \bar{d}$	0.002177(1)	1.69(0)	3.76(1)	-1.12(2)	-1.00(1)
$e^- e^+ u \bar{u}$	0.000845(0)	0.11(1)	3.76(1)	-1.12(2)	-1.00(1)
$e^- e^+ d \bar{d}$	0.001088(0)	0.47(1)	3.76(1)	-1.12(2)	-1.00(1)
$u \bar{u} c \bar{c}$	0.002971(0)	-1.80(1)	7.51(1)	-1.11(2)	-1.00(1)
$d \bar{d} d \bar{d}$	0.002556(1)	-0.38(0)	4.38(2)	-1.21(3)	-1.00(1)
$d \bar{d} s \bar{s}$	0.004956(1)	-0.36(0)	7.51(1)	-1.12(2)	-1.00(1)
$u \bar{u} s \bar{s}$	0.003852(1)	-0.66(1)	7.51(1)	-1.11(2)	-1.00(1)
$u \bar{u} u \bar{u}$	0.001506(0)	-1.92(1)	4.06(3)	-1.24(4)	-1.00(1)

# Recent work in MSSM: $H^+ \rightarrow \chi^0 \chi^+$



[Heinemeyer, Schappacher, arXiv:1503.02996]

- complete EW contributions
- dips = threshold effects
- compare also to HFOLD

[Eberl, Frisch, Hlucha,  
arXiv:1012.5025]