

# Primordial Black Holes

from the

# QCD axion

Fabrizio Rompineve

IFAE Barcelona

based on: Francesc Ferrer, Eduard Massó, Giuliano Panico, Oriol Pujolàs and FR, [arXiv:1807.01707](https://arxiv.org/abs/1807.01707)



SUSY 2018, Barcelona, July 26, 2018

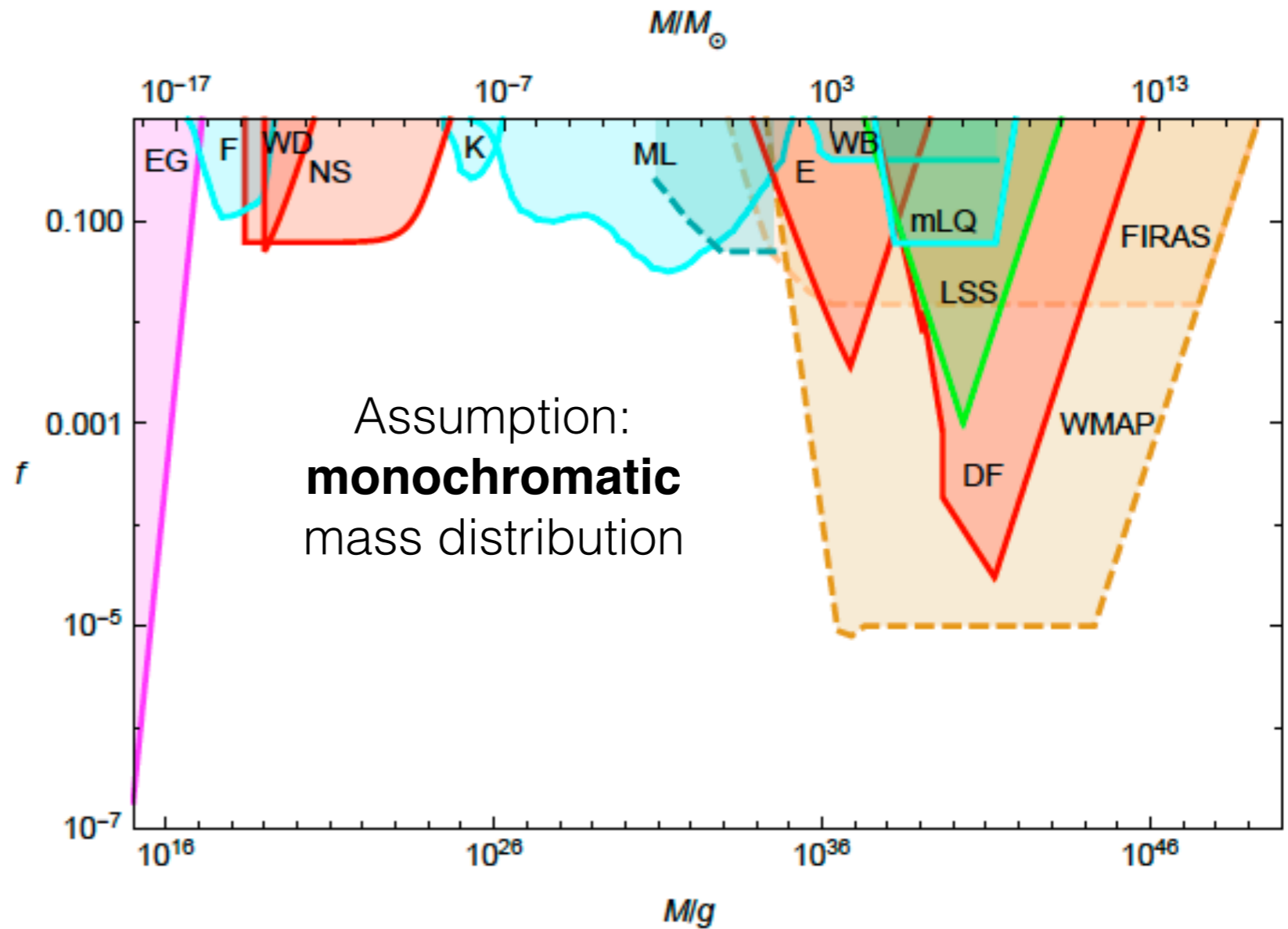
# PBHs as DM

- **Interest:** alternative, traditionally **astrophysical**, DM candidate.



**However:**

$$f \equiv \frac{\Omega_{PBH}}{\Omega_{DM}}$$



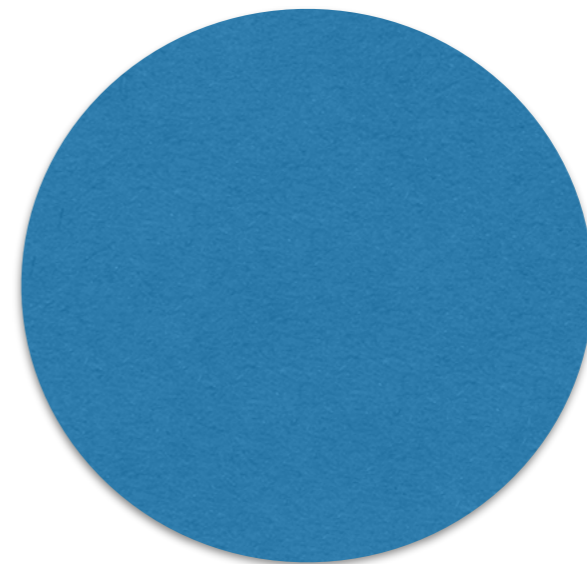
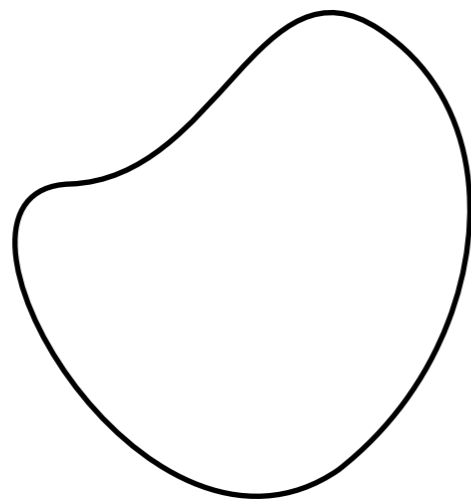
Taken from: Carr et al., arXiv:1607.06077

# Interest in heavy BHs

- We (can) hear them! (LIGO-LISA-etc)
- We “see” them! (Super-Massive BHs at the centre of galaxies, maybe primordial?)
- **Small fraction** of **very heavy** ( $\gtrsim 10^5 M_{\odot}$ ) PBHs: helps in generation of cosmological structures *and* may alleviate problems of CDM on sub-galactic scales! (Clesse et al. '15, Carr and Silk '18).

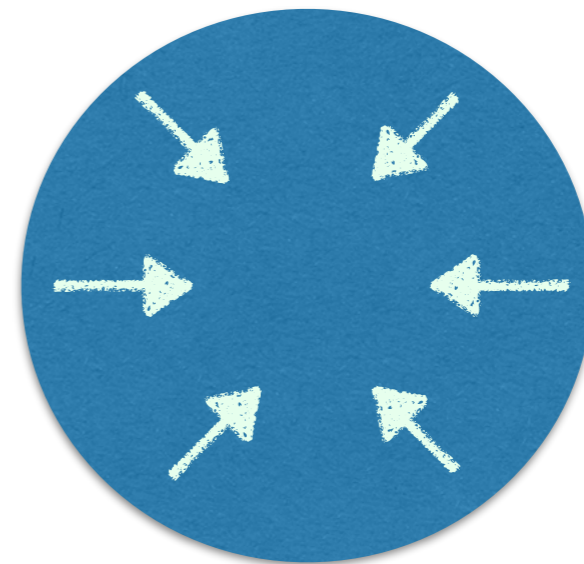
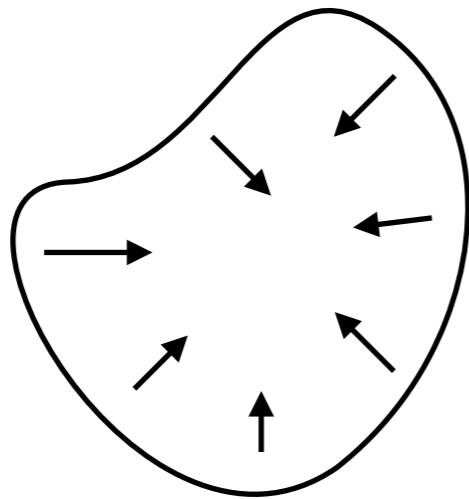
# Focus of this talk

- **Most studied** formation mechanism: **gravitational collapse** of density fluctuations from **Inflation**.
- **Alternative** formation mechanism: collapse of topological defects in the early Universe.
- **Examples**: strings (Vilenkin '81, ...), domain walls (Khlopov '05, ..., Deng et al. '17).



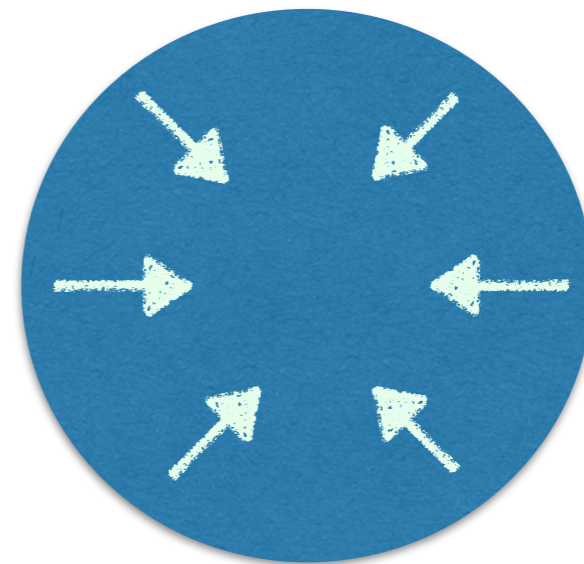
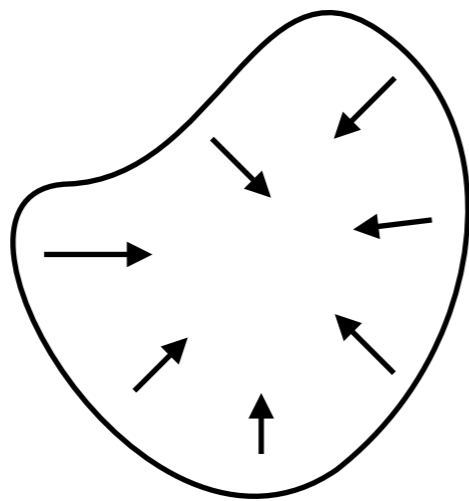
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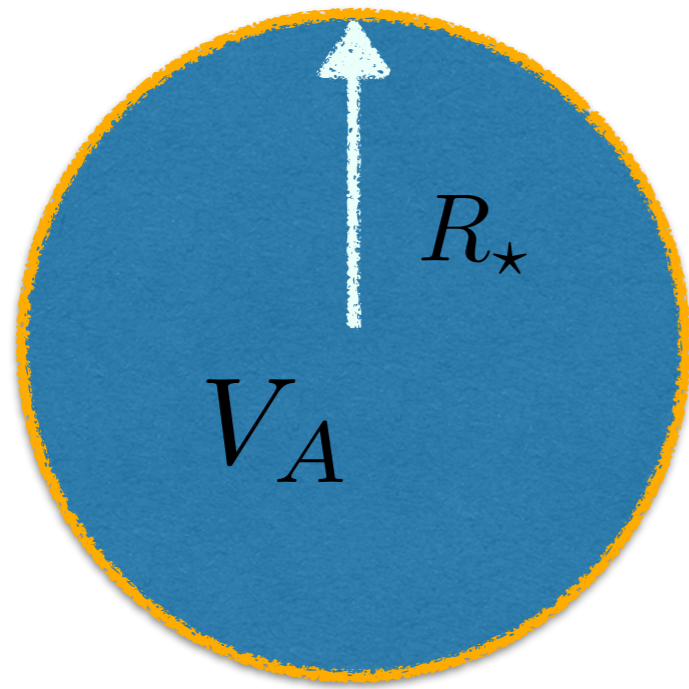
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Collapse driven by **tension!**

# PBHs from domain walls (DWs)

$$V_B \lesssim V_A$$



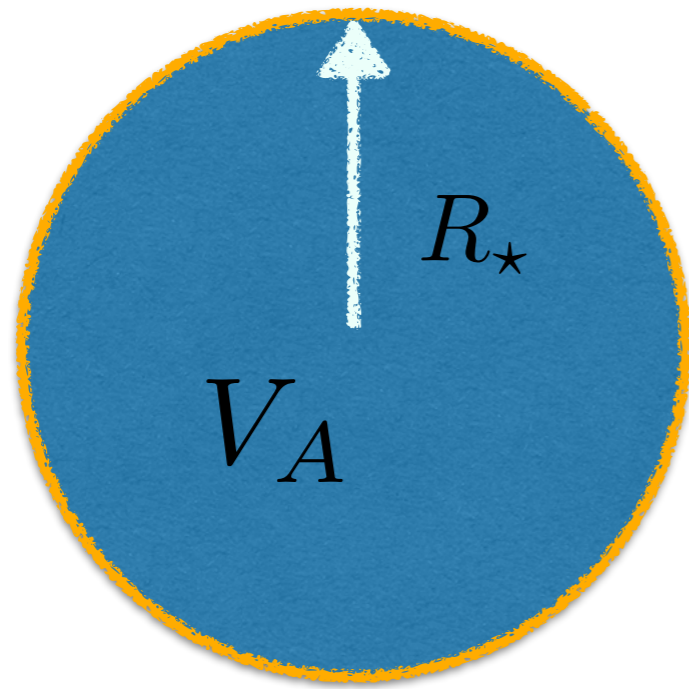
$\sigma$   
Wall **tension**

- DW collapses once

$$H_*^{-1} \equiv H^{-1}(T_*) \sim R_*$$

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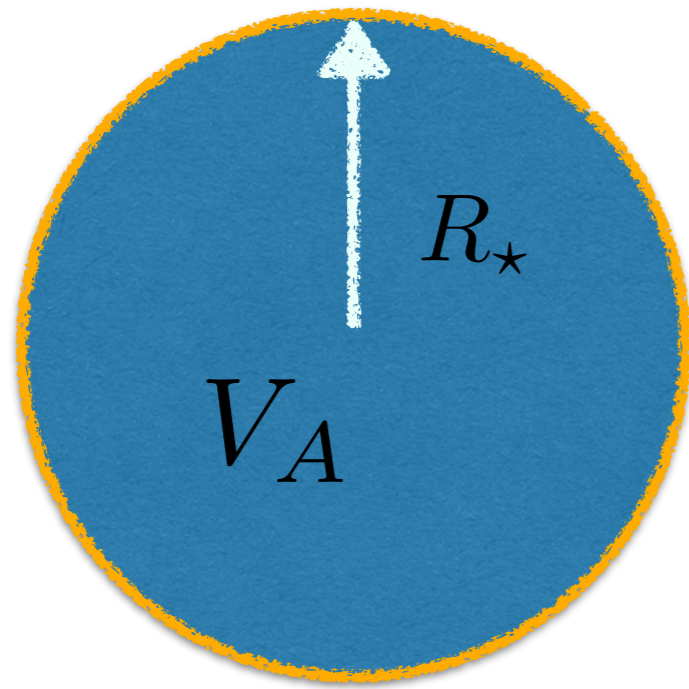
- Collapsing **mass**

$$M_{\star} \simeq 4\pi\sigma H_{\star}^{-2} + \frac{4}{3}\pi\Delta V H_{\star}^{-3}$$



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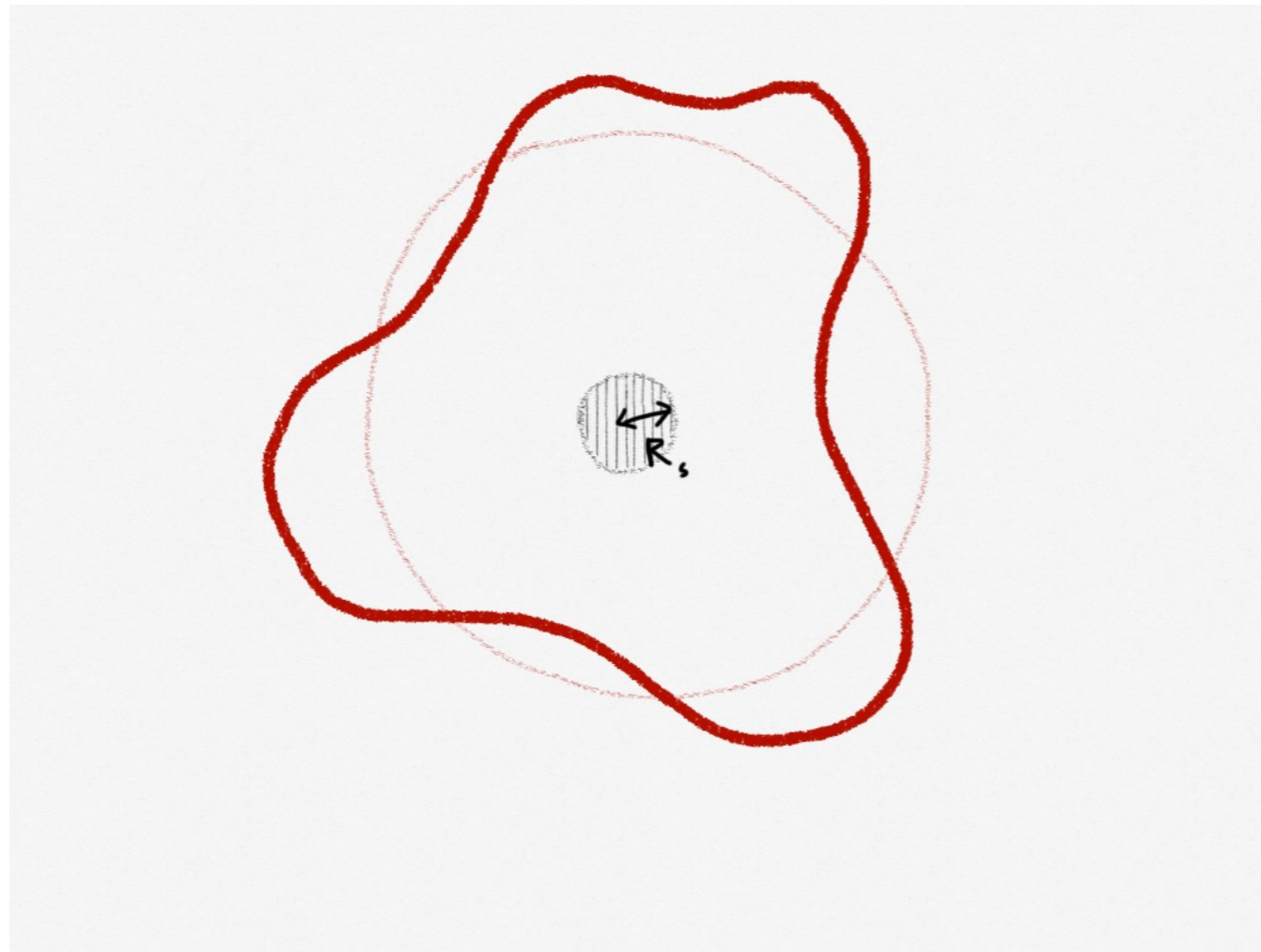
↓

$$\sim T_*^{-4}$$

↓

$$\sim T_*^{-6}$$

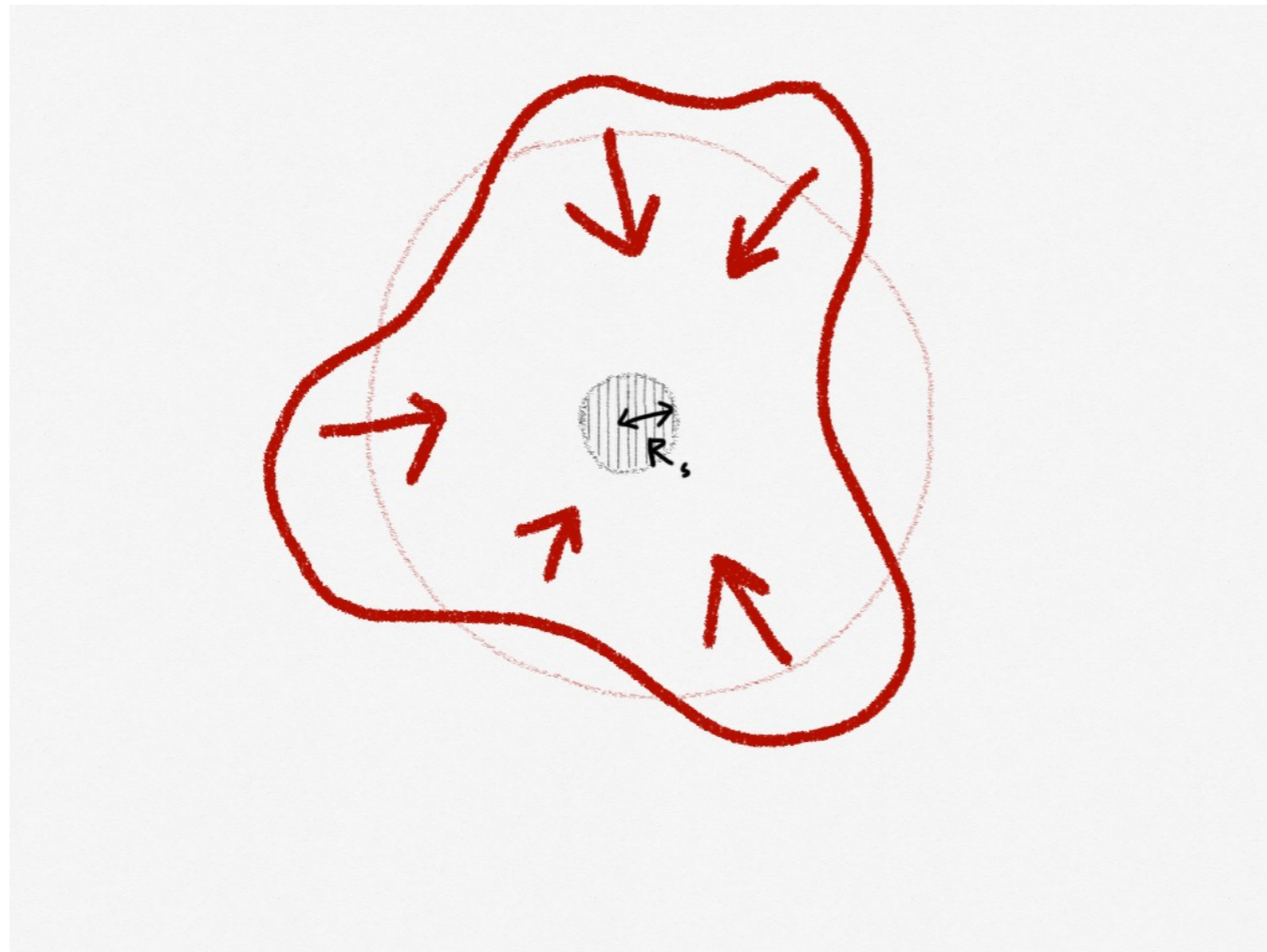
# Figure of merit



Pictures by P. Baratella

$$\begin{aligned} p &\equiv \frac{R_S}{R_\star} \sim \frac{2G_N M_\star}{H_\star^{-1}} \\ &\sim \frac{\sigma H_\star^{-1}}{M_p^2} + \frac{\Delta V H_\star^{-2}}{3M_p^2} \\ &\quad \downarrow \qquad \qquad \downarrow \\ &\sim T_\star^{-2} \qquad \sim T_\star^{-4} \end{aligned}$$

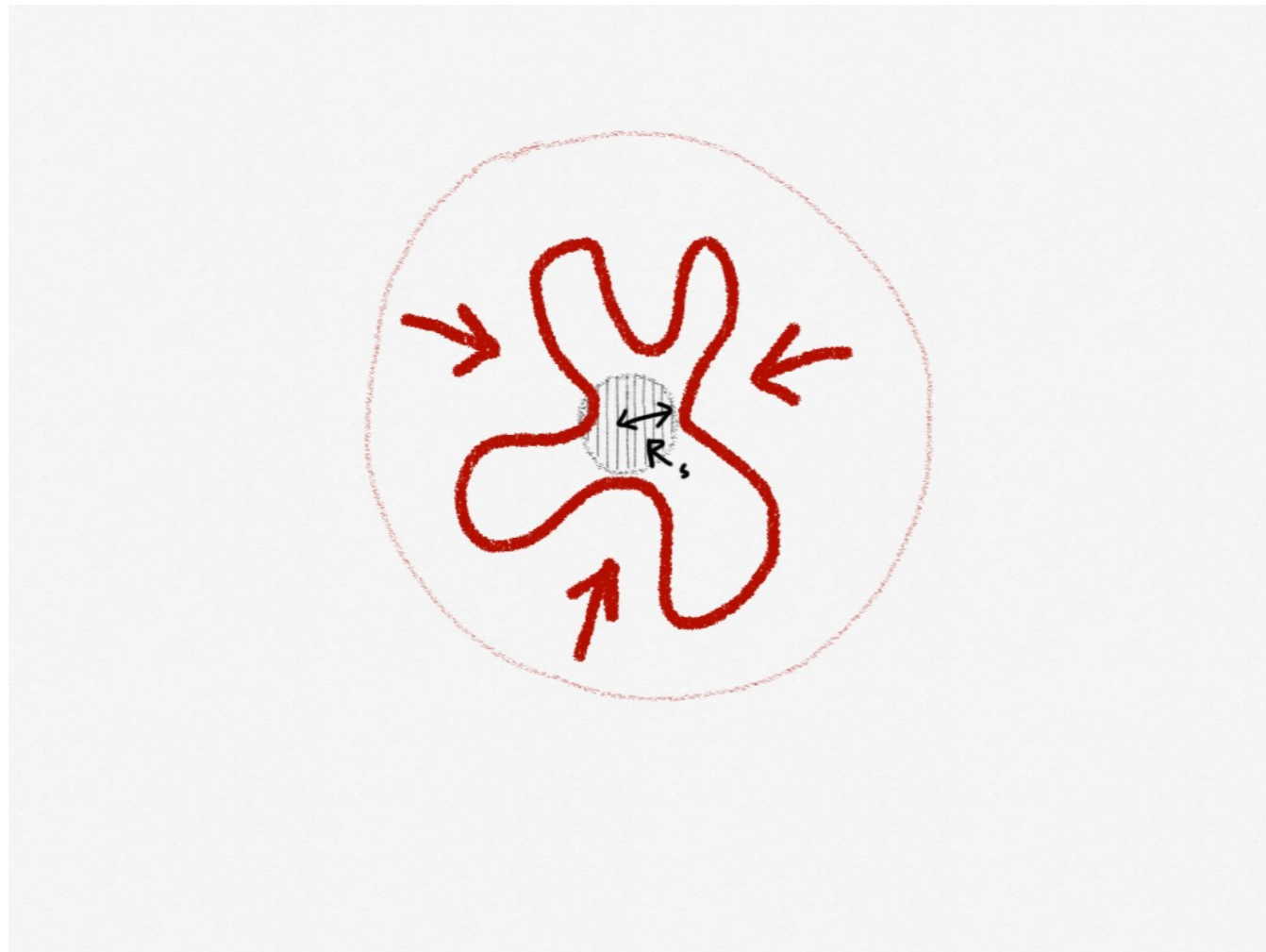
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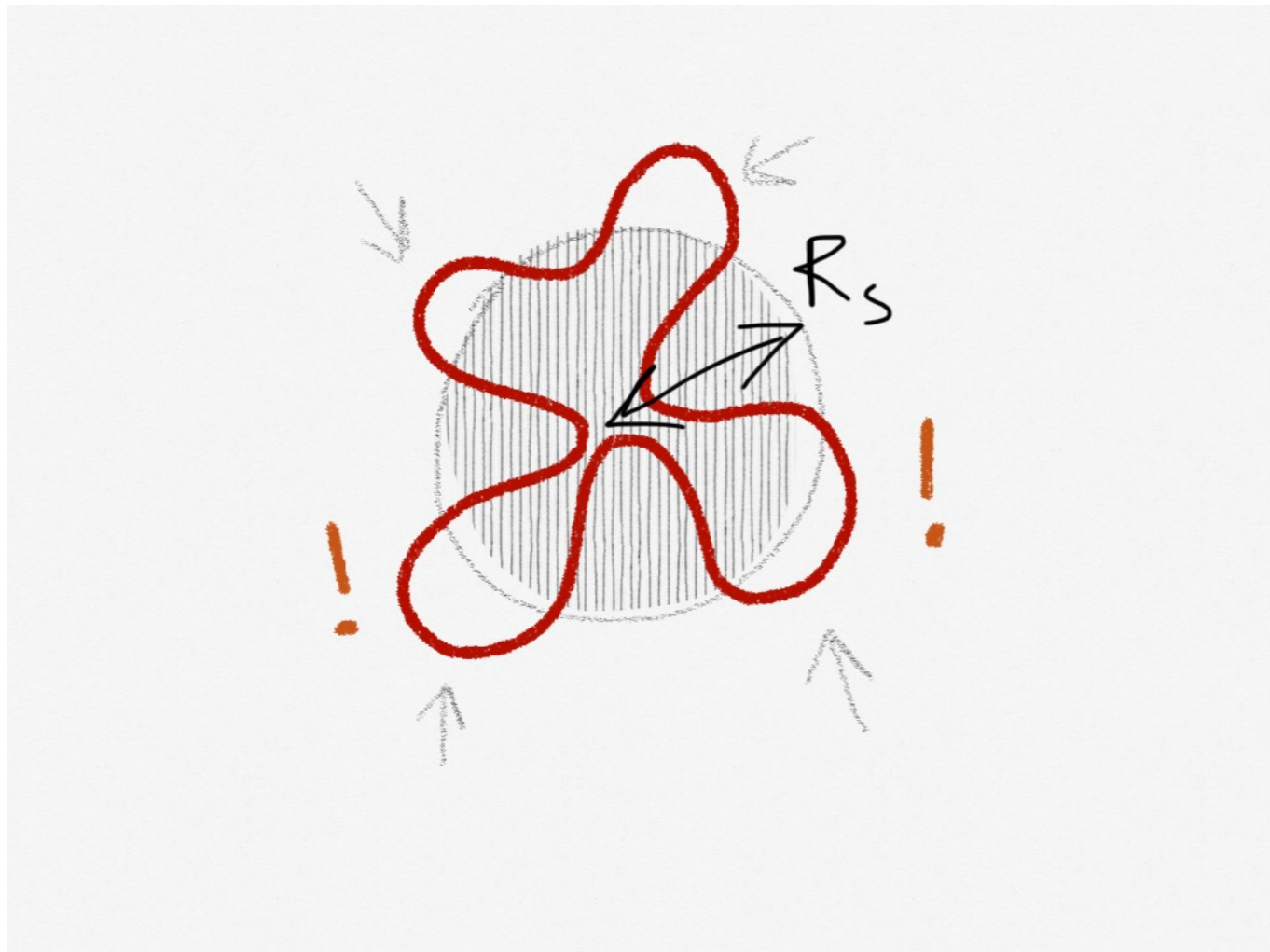
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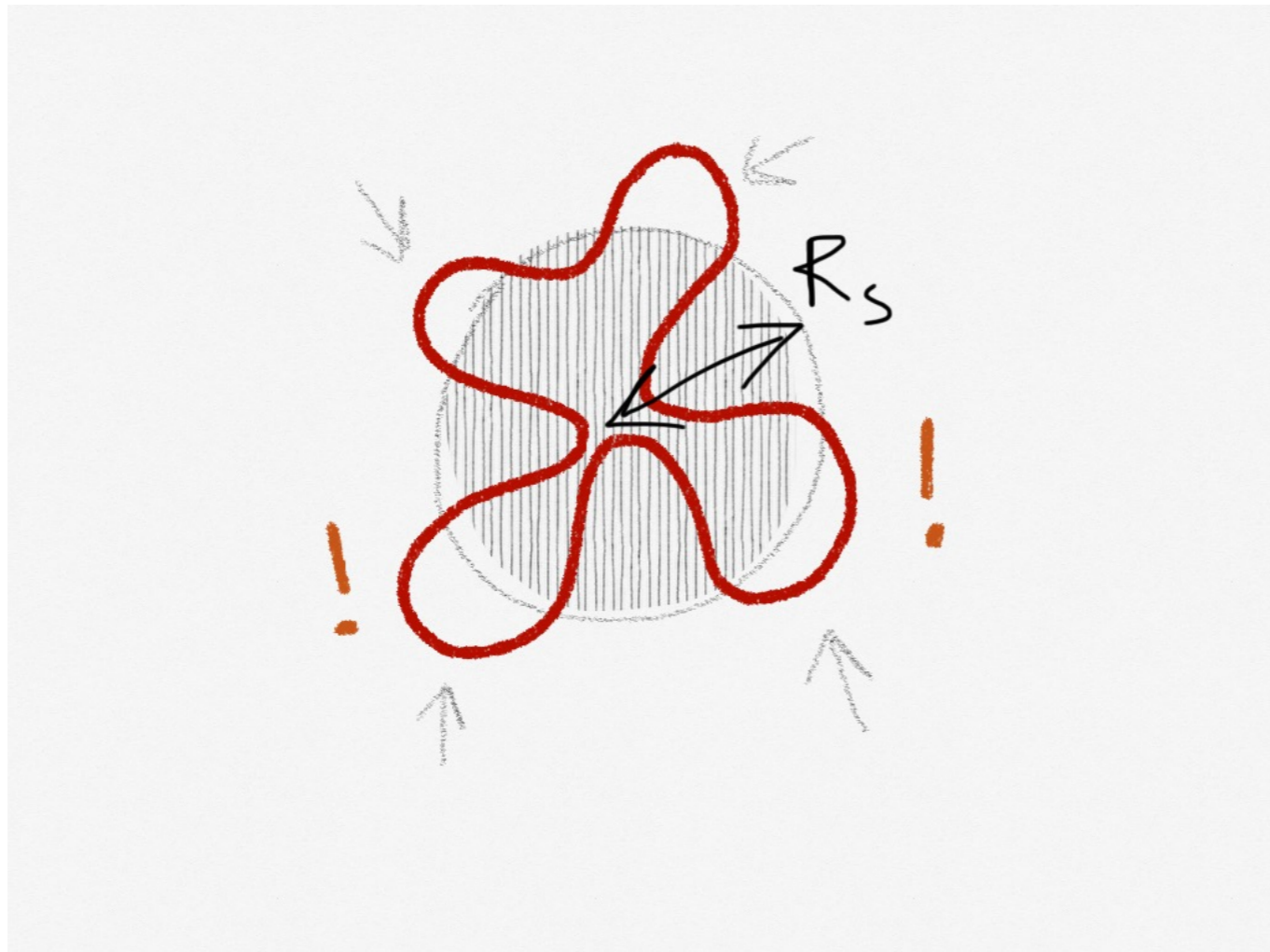
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**PBHs more likely to form ( $p \sim 0.1$ ) if collapse occurs late!**

# Focus of this talk

- **New here:** PBH formation from **axionic** hybrid string-domain wall **network**.
- Framework: **QCD axion** with domain wall number  $>1$  (**DFSZ** and generalisations of **KSVZ**, see **Vachaspati '17** for  $=1$  case).

$$\mathcal{L}_a \supset -N_{DW} \frac{a(t, \mathbf{x})}{v} \int d^3x G_{\mu\nu} \tilde{G}^{\mu\nu}$$

- Mechanism is **independent** of inflation!
- DM made of **axions** and **heavy PBHs**!

# Defects of the QCD axion

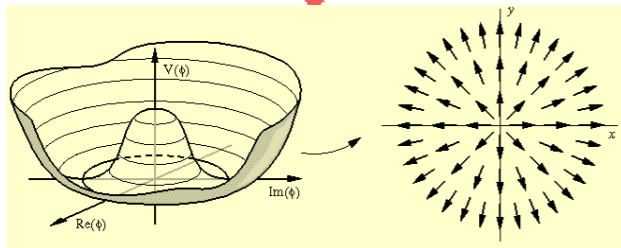
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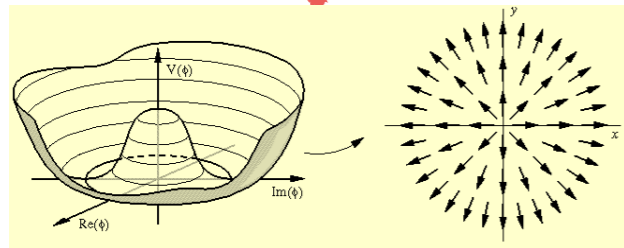


**Strings**

# Defects of the QCD axion

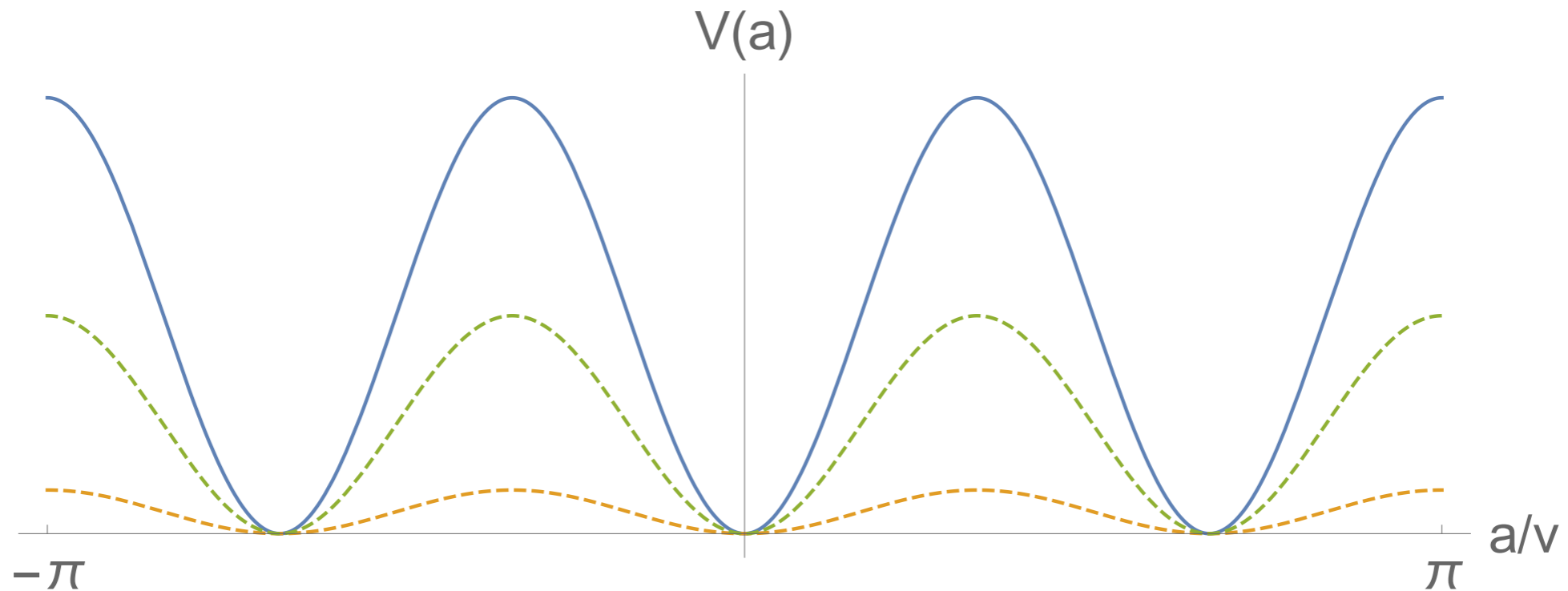
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$$T_1 \sim \text{GeV} : 3H(T_1) = m(T_1)$$



**Strings**

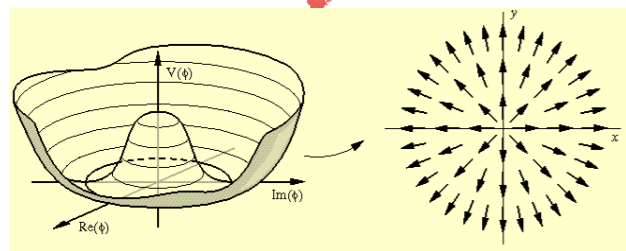
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# Defects of the QCD axion

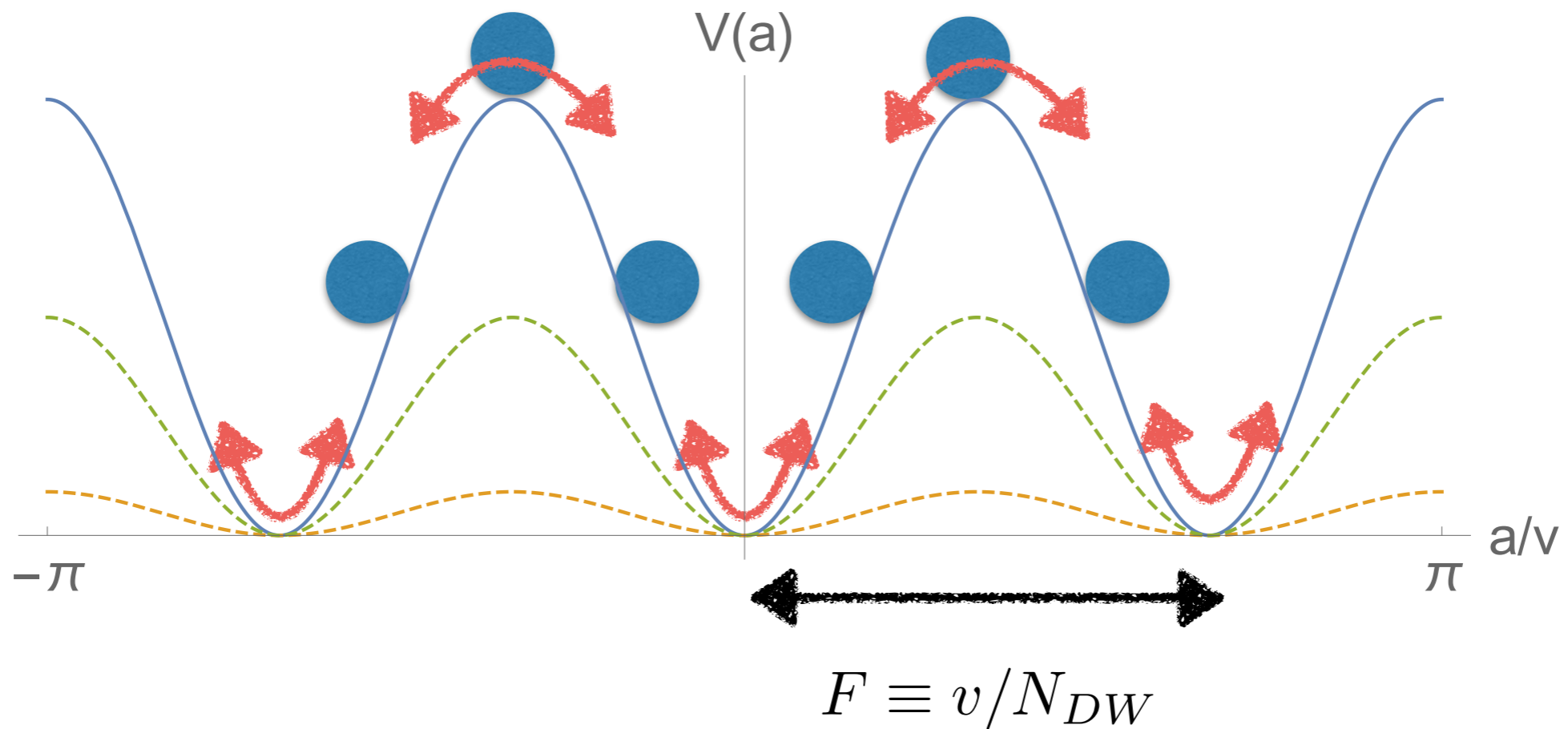
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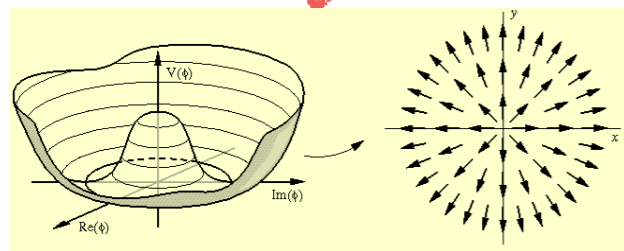


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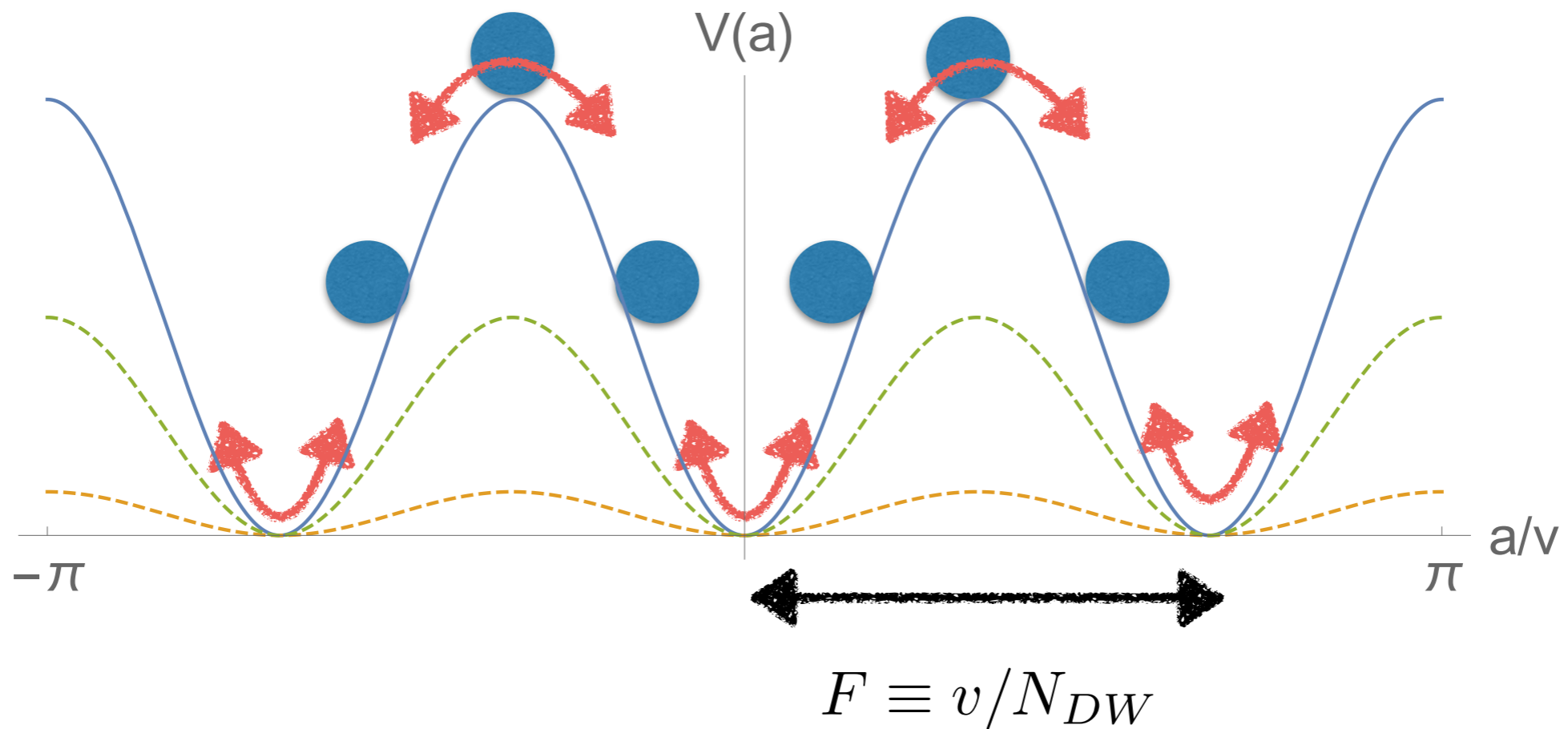
$$T_2$$



**Network:**  
each string attached  
to  $N_{DW}$  walls

**Strings**

**DWs**

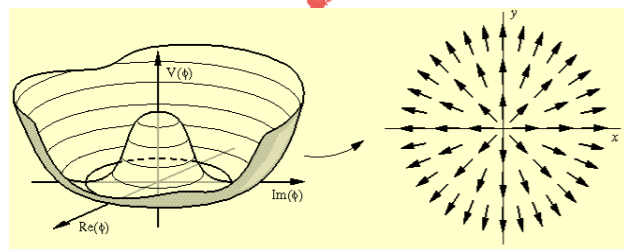


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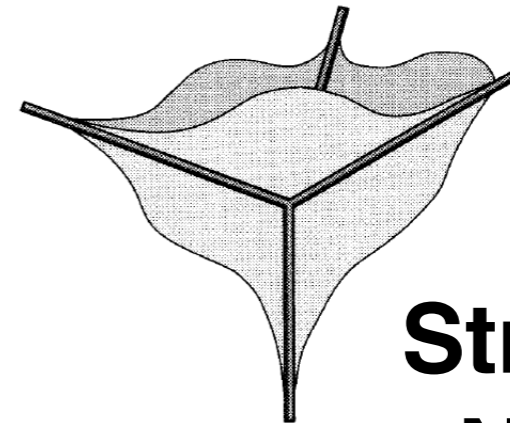
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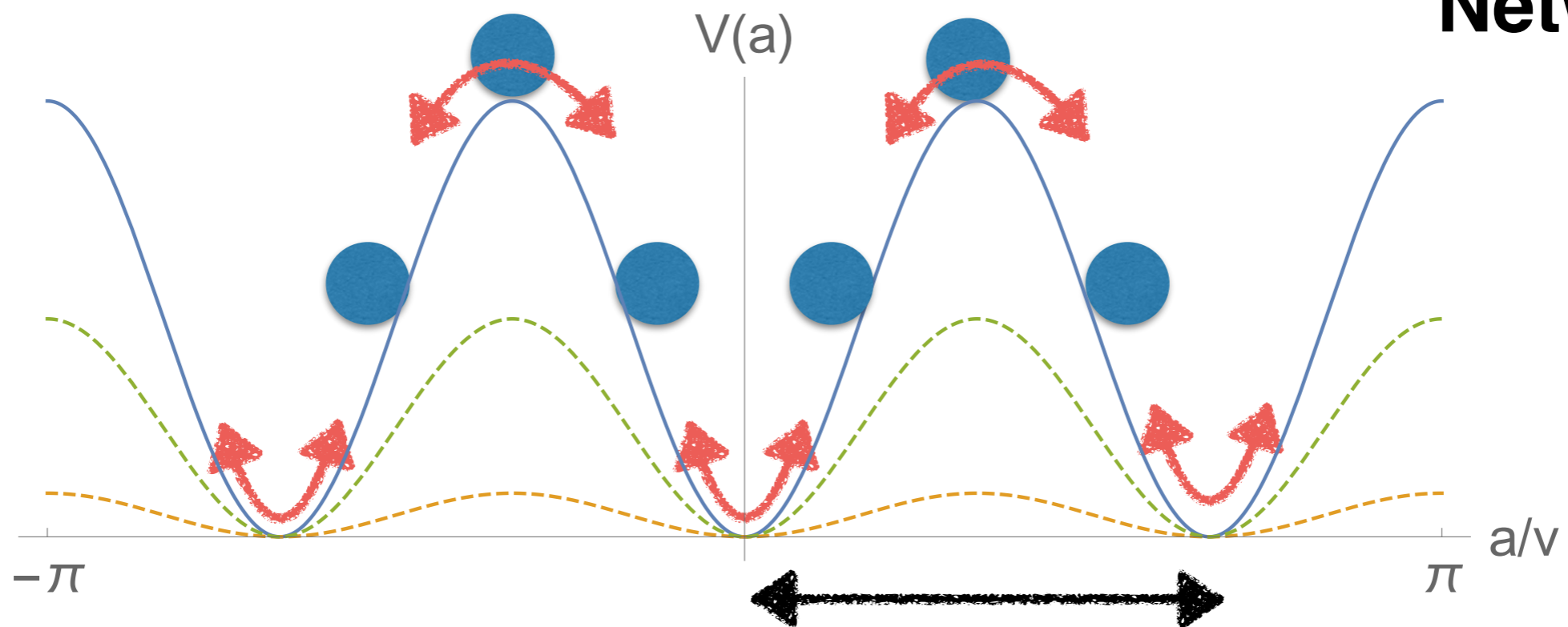


**Strings**

**DWs**



**String-wall Network**



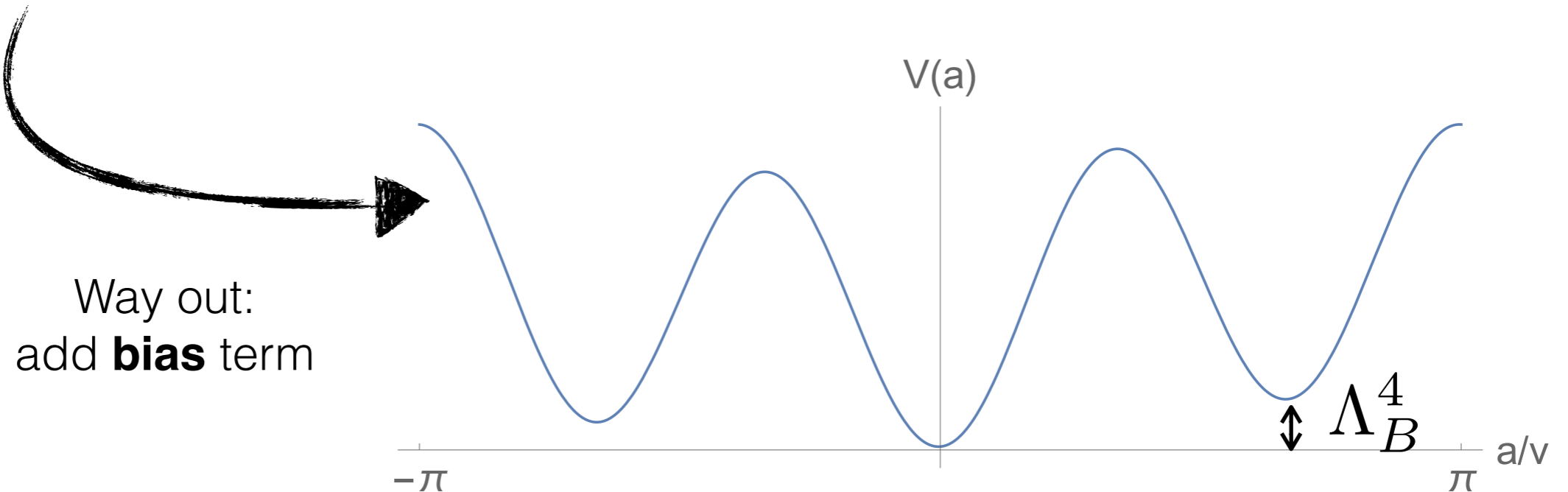
$$F \equiv v/N_{DW}$$

# QCD axion with $N_{DW} > 1$

- $N_{DW} = 1$  : network is **unstable**, rapidly decays.
- $N_{DW} > 1$  : network is **stable, DW problem!**

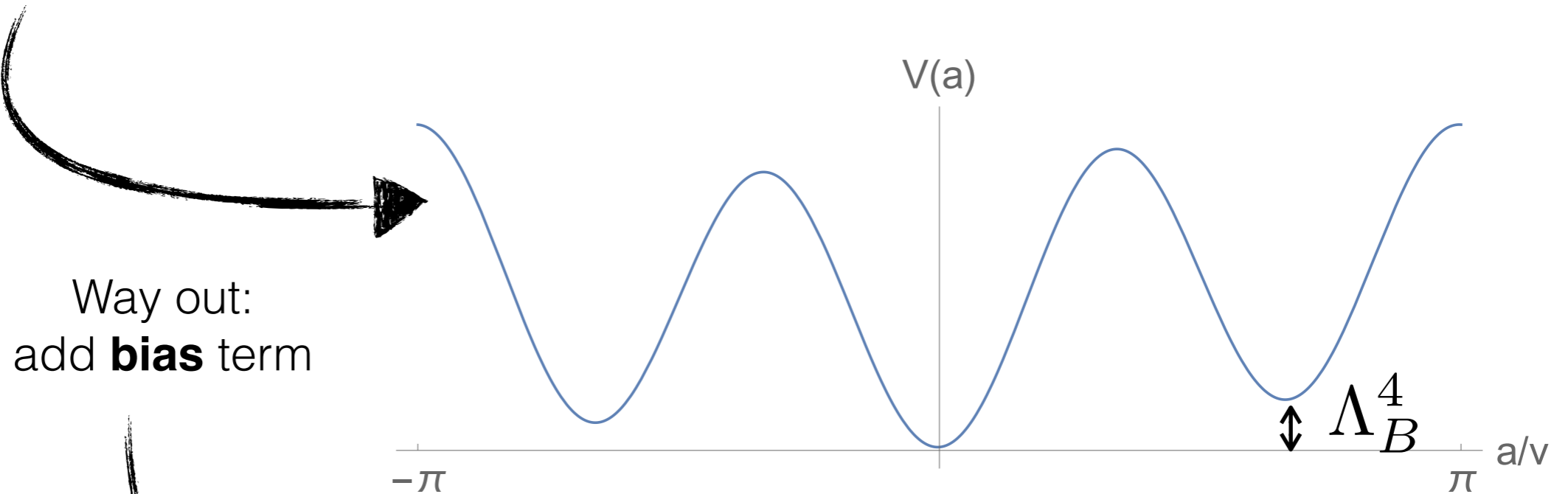
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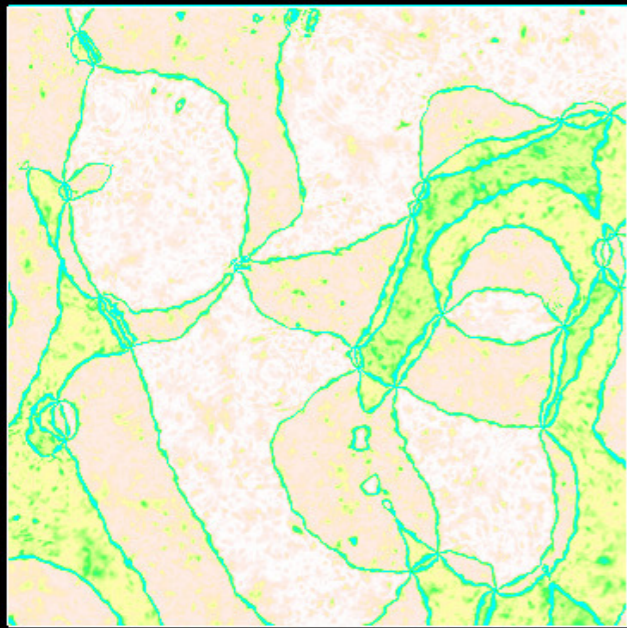
Network starts  
**decaying** when balance  
between tension and  
pressure is achieved!

$$T_2 \simeq \sqrt{\frac{M_p \Lambda_B^4}{\sigma}} < T_1$$



# QCD axion with $N_{DW} > 1$

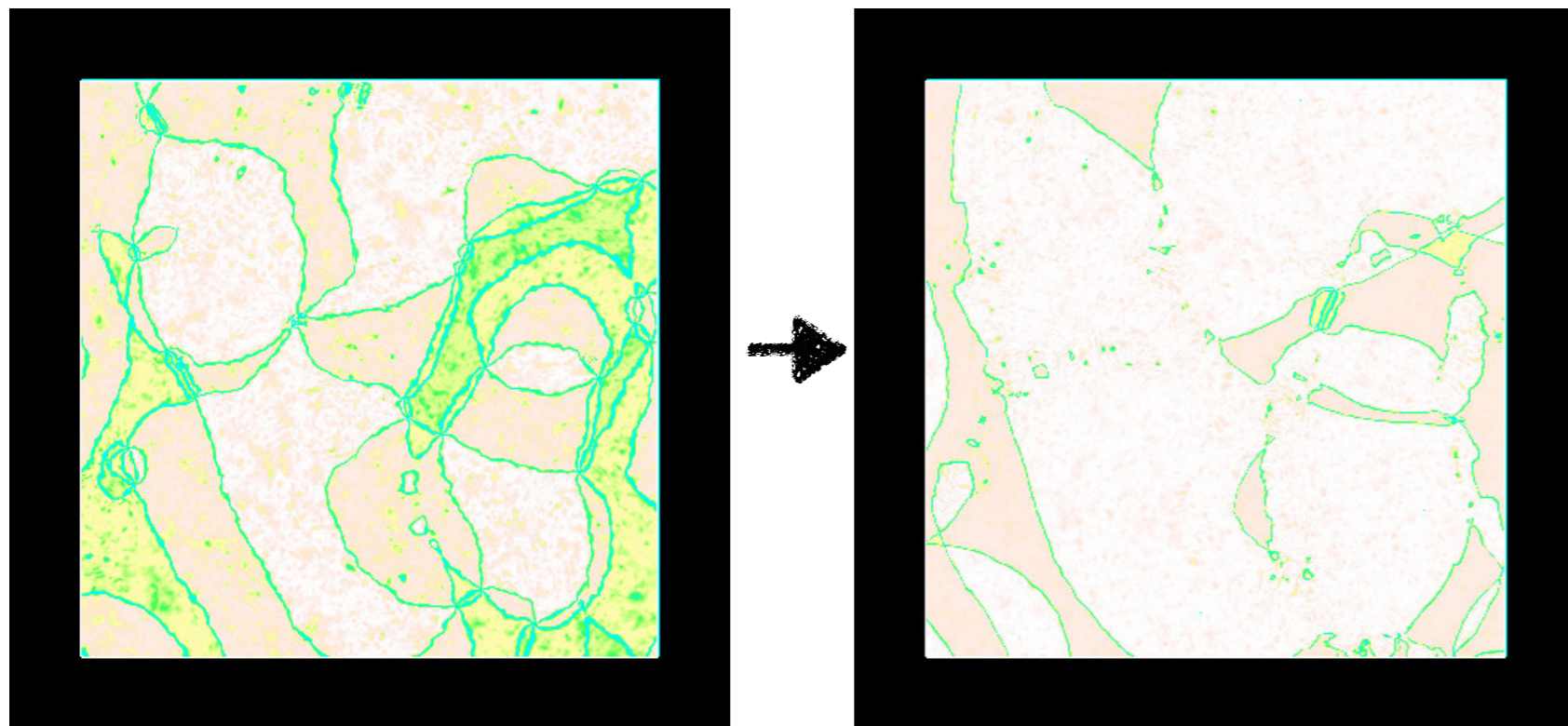
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Taken from: [Kawasaki et al. '14](#), arXiv: **1412.0789**

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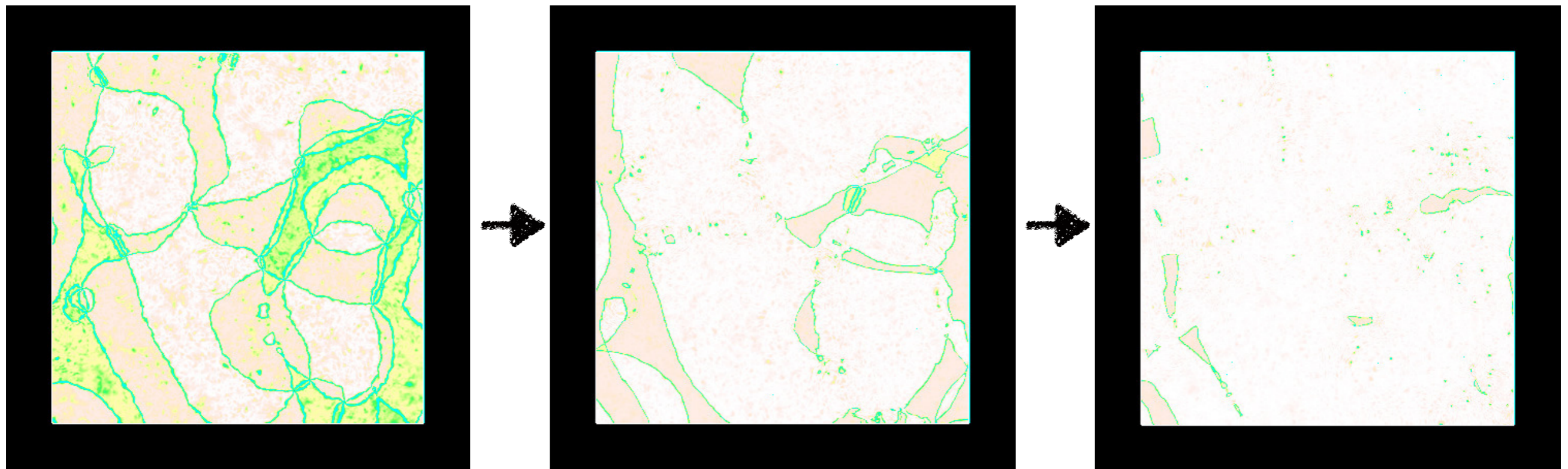
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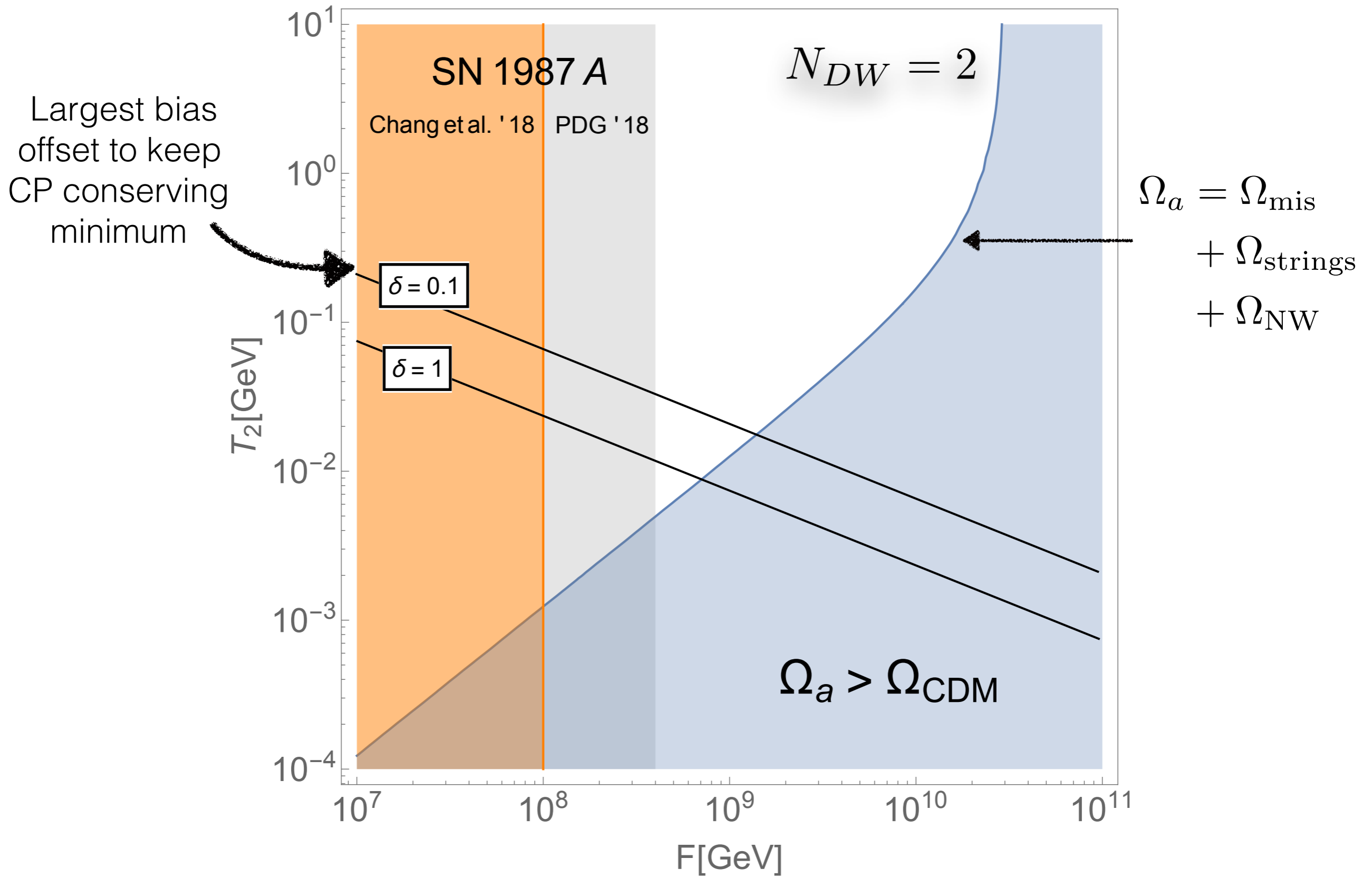
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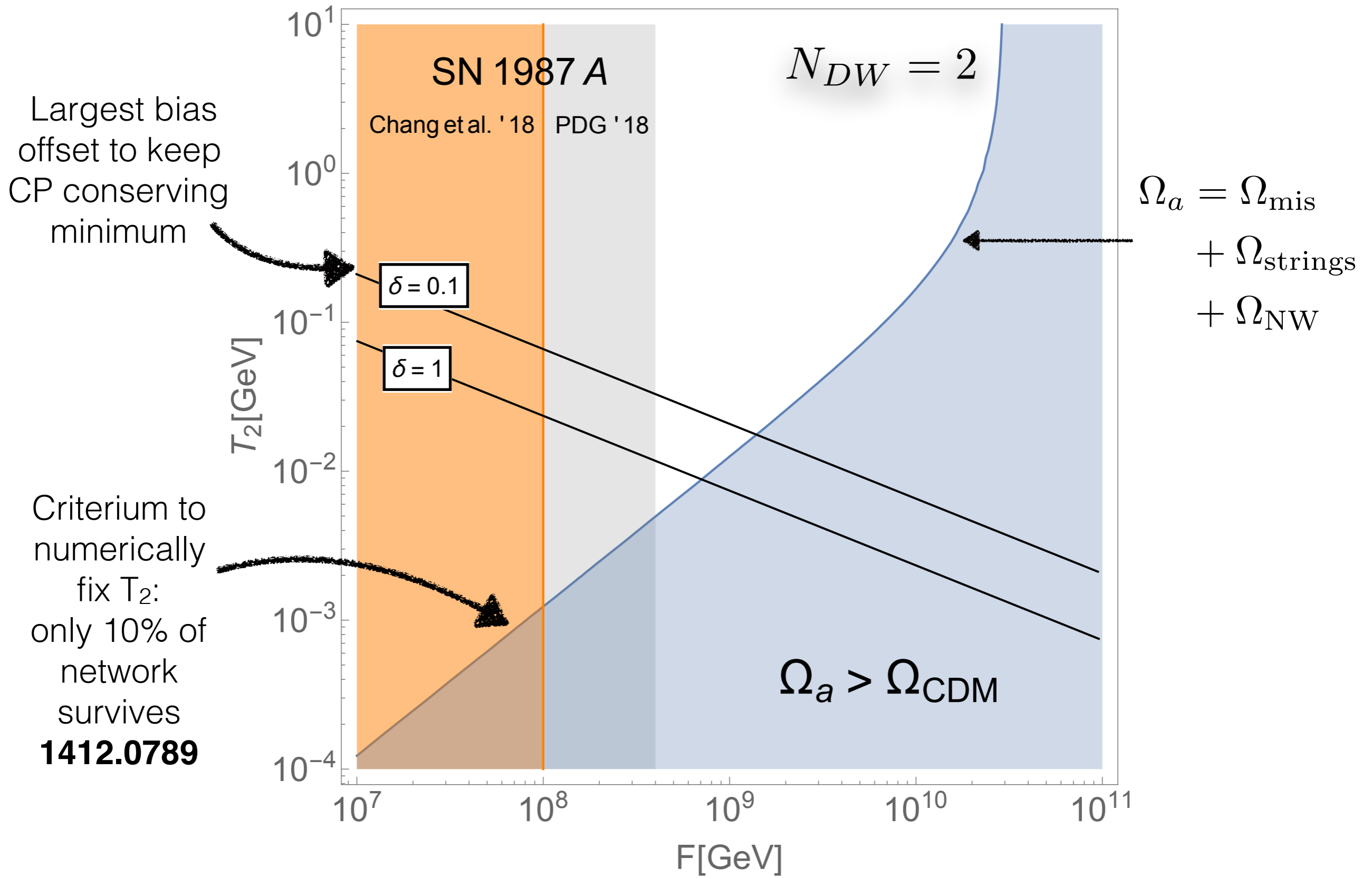


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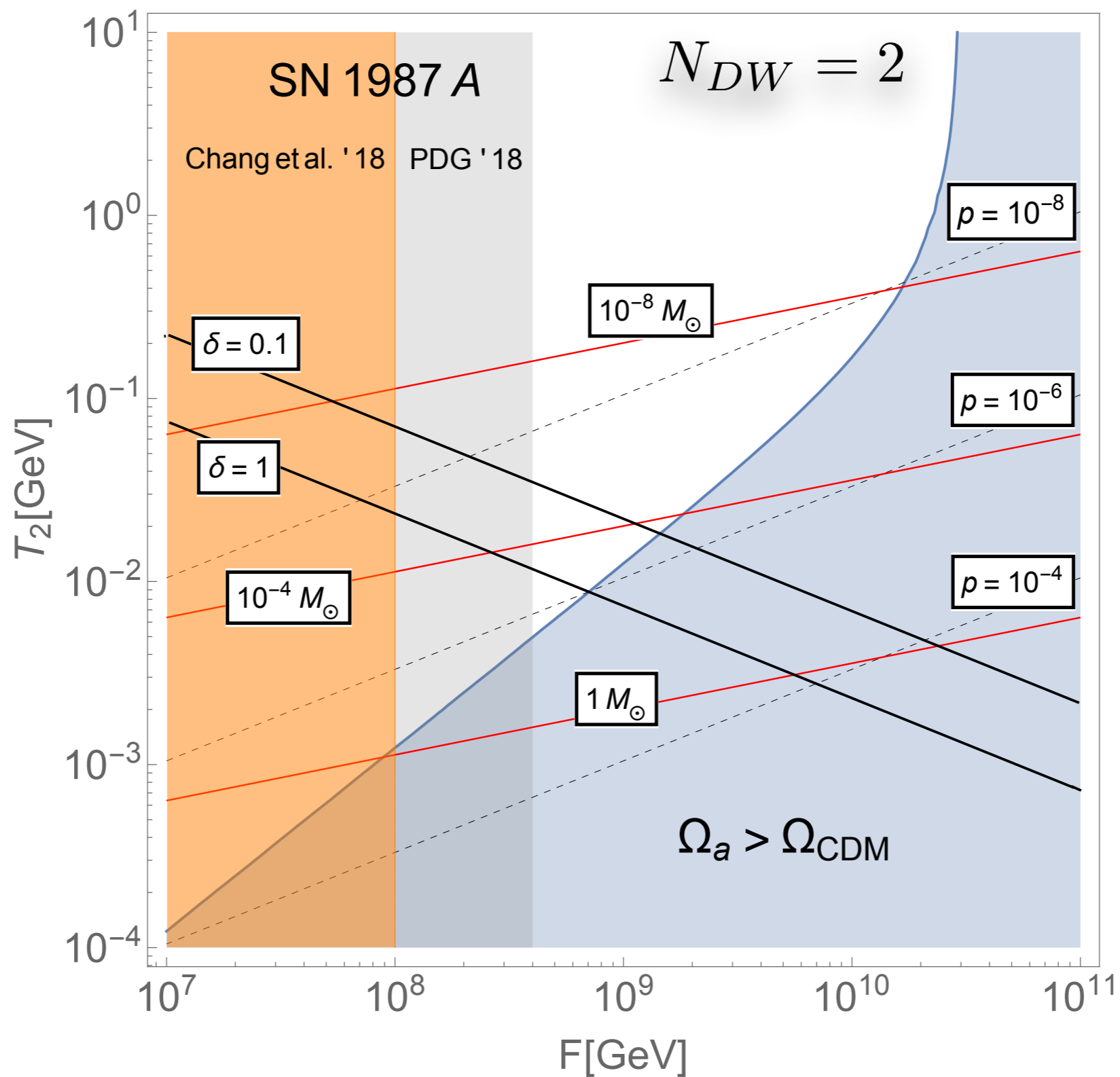
# Axion DM with $N_{DW} > 1$



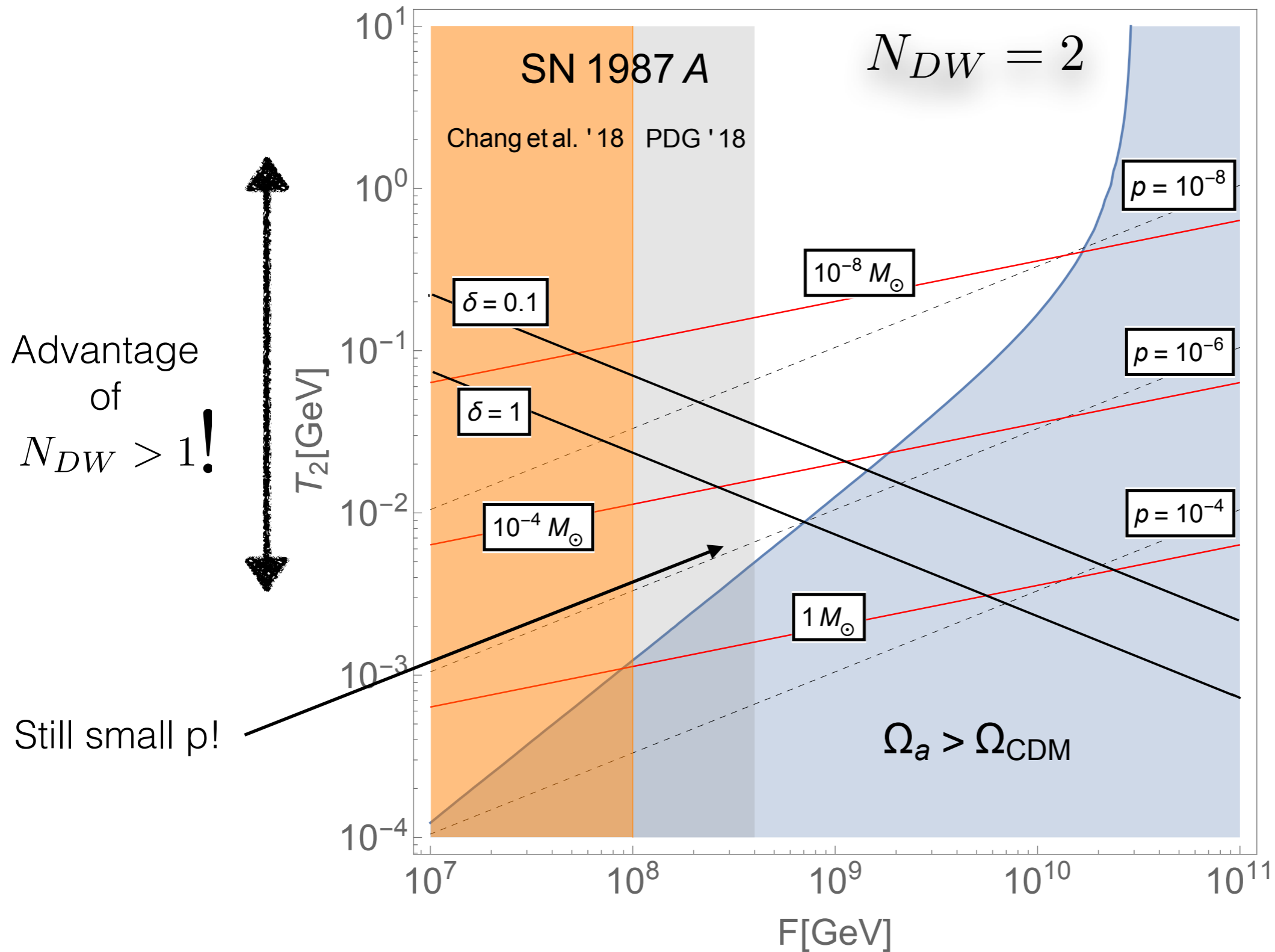
# Axion DM with $N_{DW} > 1$



# PBHs from closed walls in the network collapsing at $T_2$



# PBHs from closed walls in the network collapsing at $T_2$



# Late collapses

- **However:** still around 10% of the network leftover at  $T_2$ !
- For walls collapsing **after  $T_2$** , volume contribution dominates:

$$p \sim T_{\star}^{-4}, \quad M_{\star} \sim T_{\star}^{-6}$$

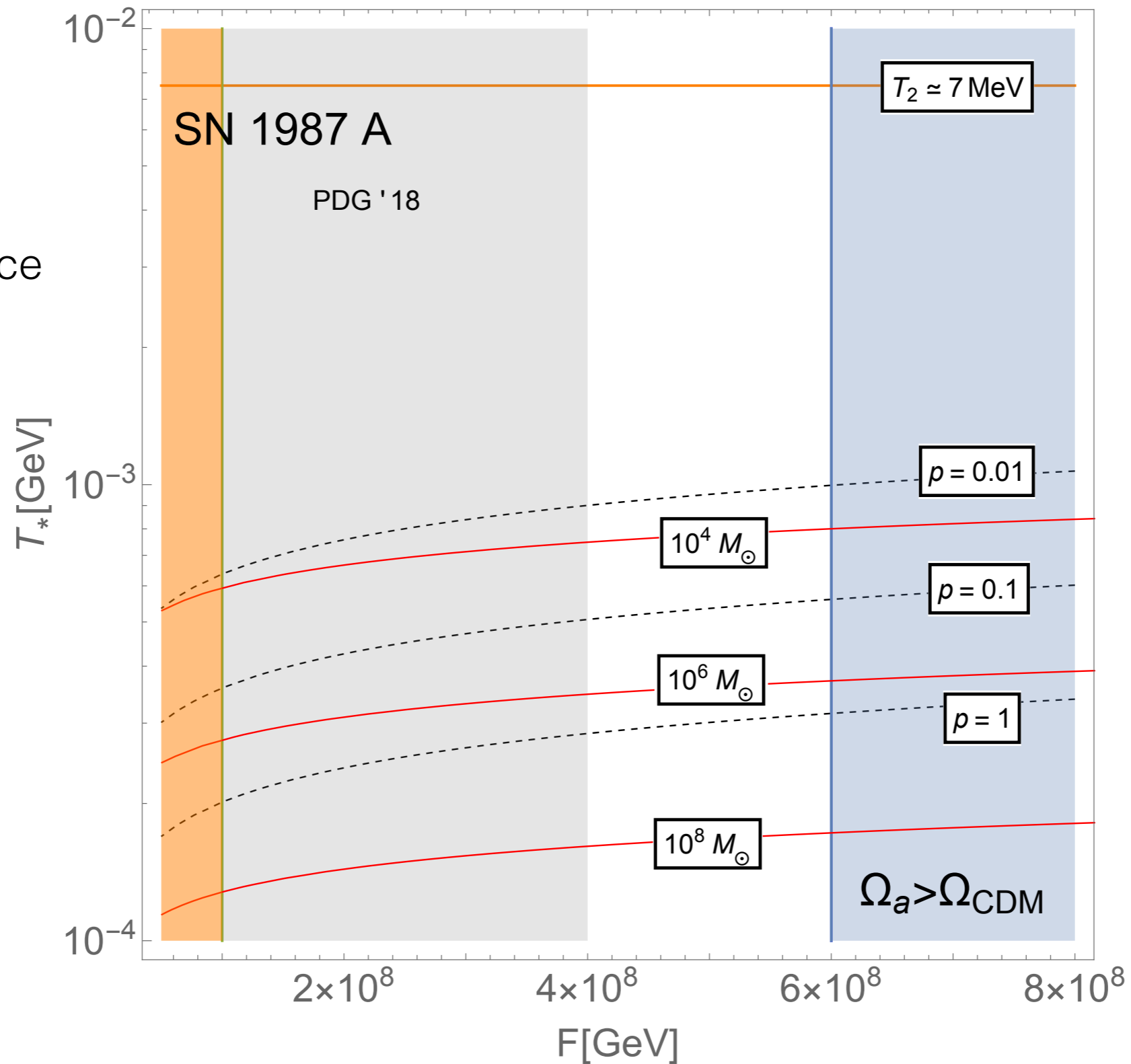
- Need only one order of magnitude in  $T$  to reach

$$p \gtrsim 0.1$$



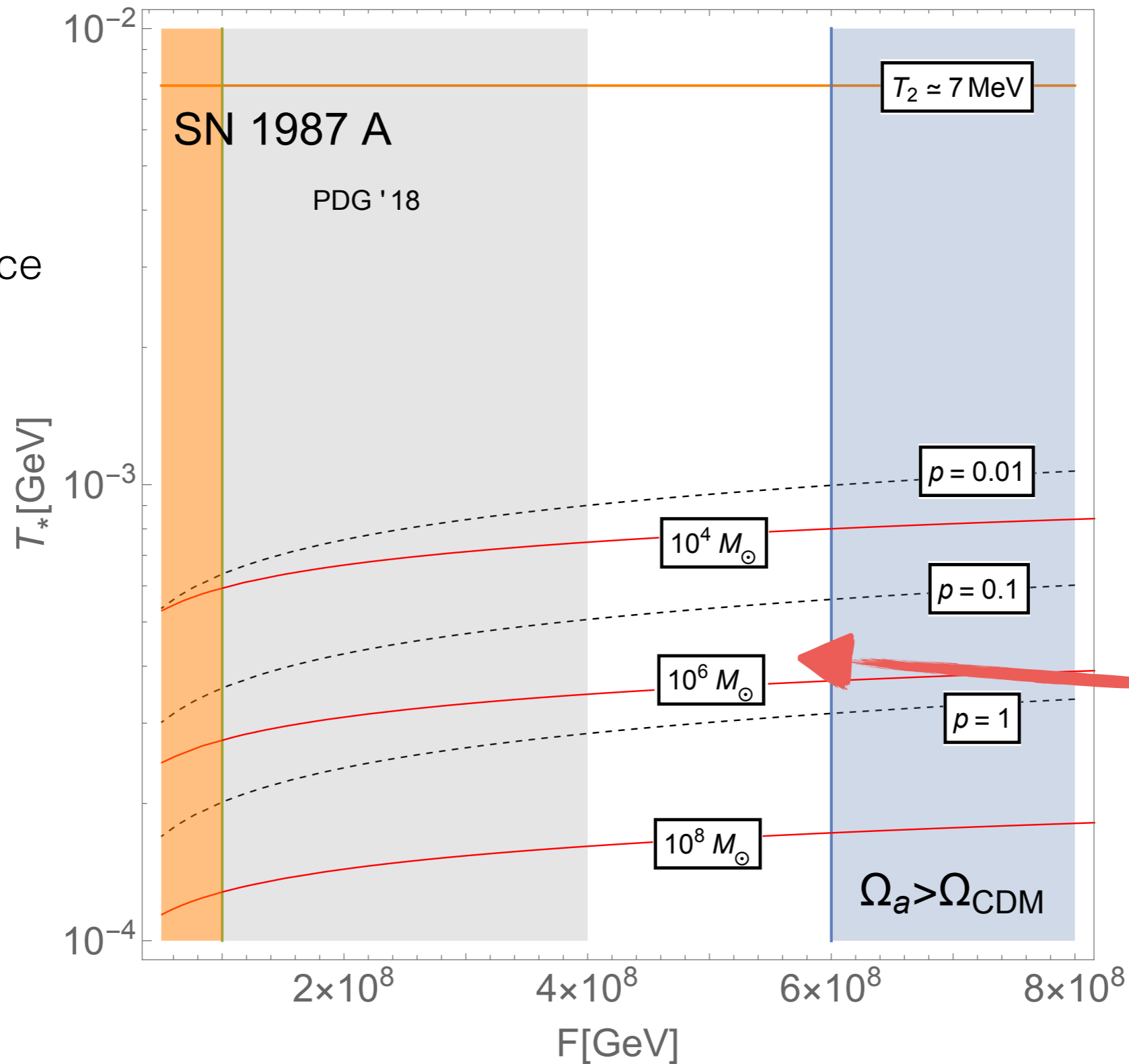
# Collapse after $T_2$

Example  
in the lower  
corner of  
parameter space



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Example  
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parameter space



**Likely** to  
form  
**Heavy**  
PBHs!

# PBH fraction

- Reasonable expectation:

Collapse of single structure

$$f \sim p^N \times \frac{\rho_{nw}(T_\star)}{\rho_{CDM}(T_\star)}$$

Decay of the whole network

- N takes into account *asphericities*, *ang. momentum* etc. For large p, expect  $N \sim O(1)$ .

- After  $T_2$ , network is dominated by bias term

$$\rho_{nw} = P_{nw} \Lambda_B^4$$

Surviving fraction of the network


# PBH fraction

- **For detailed estimate:** need numerical simulations!
- For **simplicity**, assume

$$P_{nw} \sim \left( \frac{T_2}{T_\star} \right)^{-\alpha}$$

- Simulations of [Kawasaki et al. '14](#) suggest  $\alpha \approx 7$ .
- For  $N=2$ ,  $f$  peaks at  $\sim 10^{-6}$ !

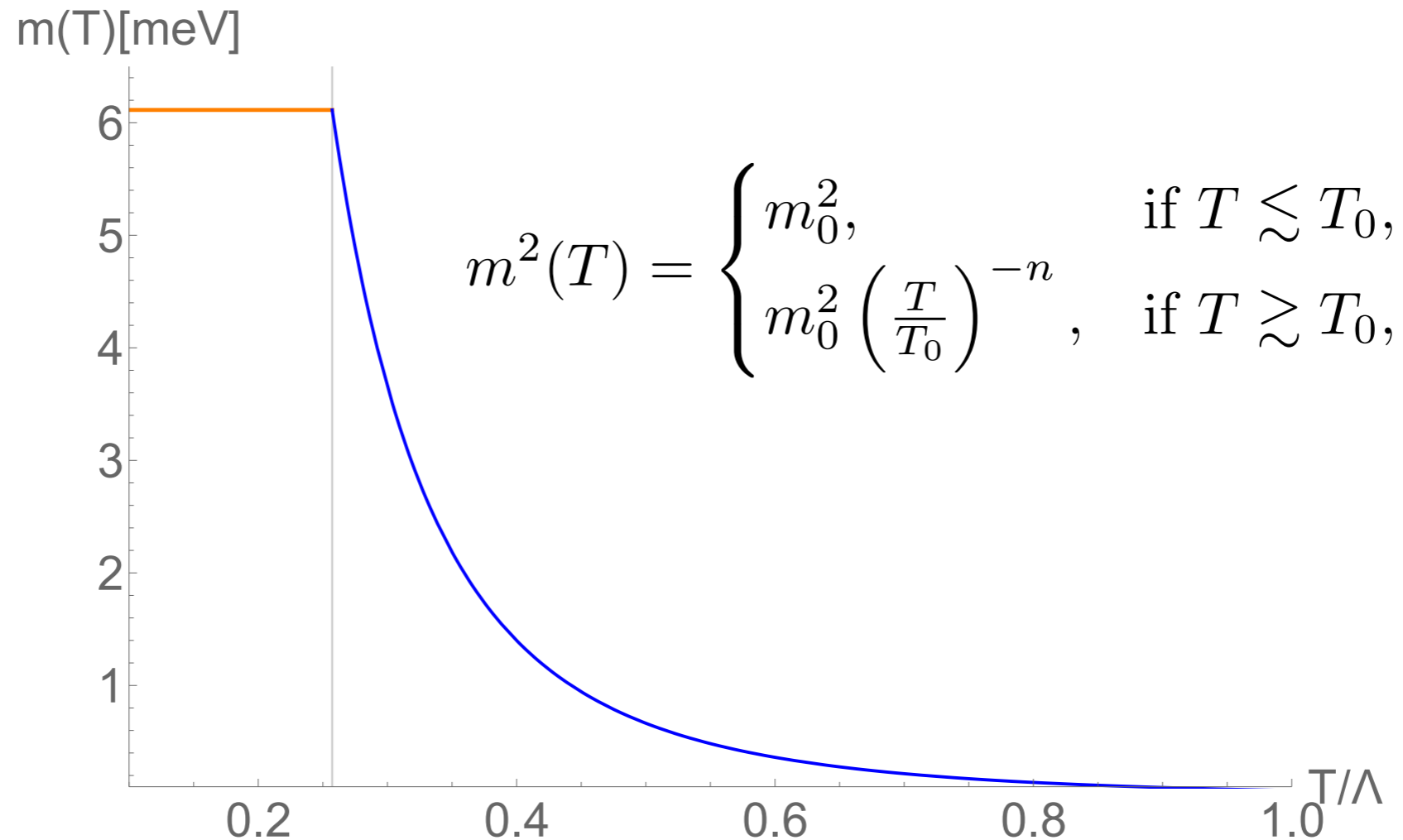
# Conclusions

- **QCD axion** models with  $N_{\text{DW}} > 1$  are characterised by **long-lived** string-domain walls network.
- Under reasonable expectations,  $M \sim 10^4 - 10^7 M_{\odot}$  PBHs can be obtained from the collapse of closed structures in the **network**.
- **Small fraction**,  $f \gtrsim 10^{-6}$ . DM **dominantly** made of axion quanta.
- Preferred region of axion parameter space To be explored at:  
**IAXO, TASTE,**  
**ARIADNE, ALPSII, ...**  
$$F \lesssim 10^9 \text{ GeV} \Rightarrow m \gtrsim \text{meV}$$


**Outlook:** bias term from dark QCD? Details of collapse?

Backup

# Axion mass



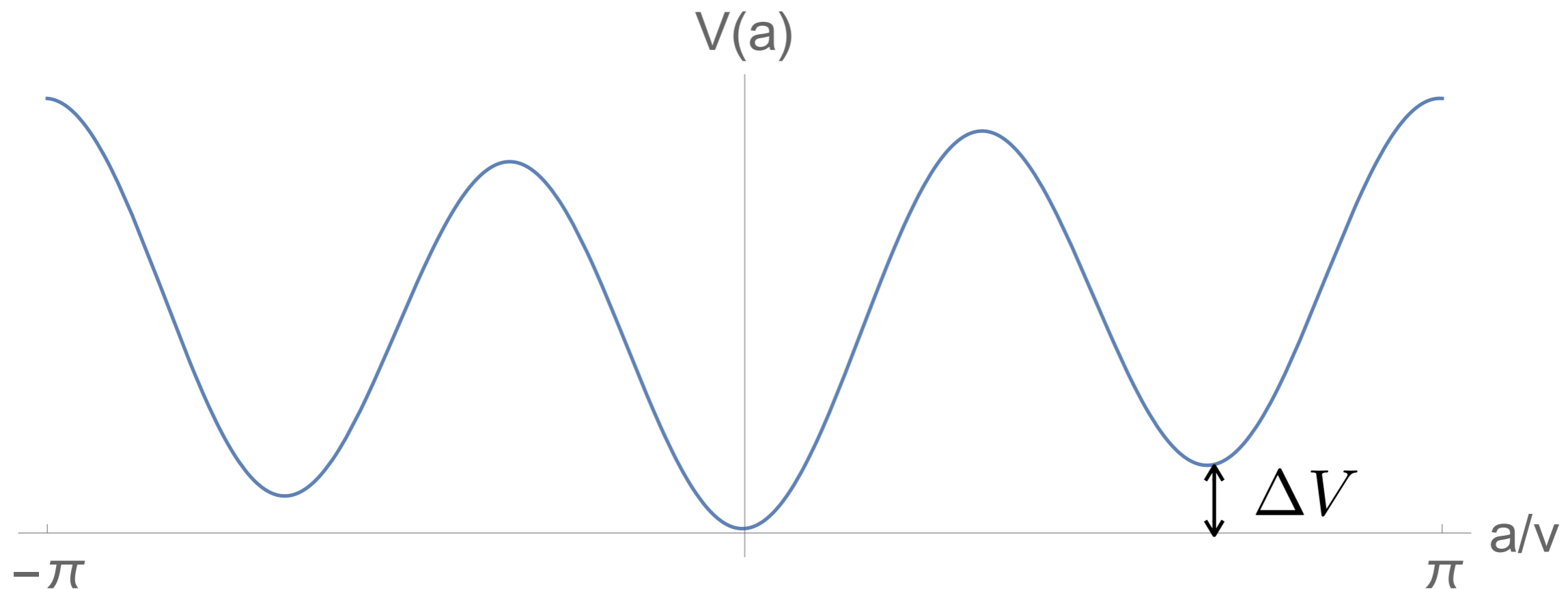
Parameters determined from Dilute Instanton Gas Approximation (High  $T$ , [Wantz et al.'10](#)) and Lattice ([Borsanyi et al.'16](#))

$$n \approx 7, T_0 \approx 100 \text{ MeV}$$

see [Bonati et al.'16](#) for deviations

# Bias term

- $N_{DW} > 1$ :  $\rho_{nw} \sim a^{-2} \longrightarrow$  domain wall problem!
- Need to lift degeneracy of vacua



$\longrightarrow$  Add:  $V_B = \Lambda_B^4 \left[ 1 - \cos \left( \frac{a}{v} + \delta \right) \right]$



# Bias from dark QCD

- Consider dark QCD without light quarks confining below  $T_2$  and coupled to the QCD axion.
- Induce temperature-dependent bias term.

$$\Delta V(T) \simeq m_B(T)^2 F^2$$

- Increases with decreasing temperature!
- Large  $p$  achieved faster! Possibly larger fraction of PBHs with smaller masses!

# Axion relic abundance

$$\Omega_{\text{mis}} h^2 \simeq B_n \sqrt{c_0} c_T^{-\frac{1}{4+n}} \left( \frac{F}{10^9 \text{ GeV}} \right)^{\frac{6+n}{4+n}} \left( \frac{g_{\text{eff}}(T_1)}{80} \right)^{-\frac{6+n}{2(4+n)}} \left( \frac{\Lambda_{QCD}}{400 \text{ MeV}} \right)$$

$$\Omega_{\text{strings}} h^2 \simeq C_n \left( \frac{F}{10^9 \text{ GeV}} \right)^{\frac{6+n}{4+n}} \left( \frac{g_{\text{eff}}(T_1)}{80} \right)^{-\frac{2+n}{2(4+n)}} \left( \frac{\Lambda_{QCD}}{400 \text{ MeV}} \right)$$

$$\Omega_{\text{nw}} h^2 \simeq 0.14 \times \left( \frac{F}{10^9 \text{ GeV}} \right) \left( \frac{\Lambda_{QCD}}{400 \text{ MeV}} \right)^2 \left( \frac{g_{\text{eff}}(T_2)}{10.75} \right)^{-1/4} \left( \frac{10 \text{ MeV}}{T_2} \right)$$