



# Anisotropies from Low Density Scattering

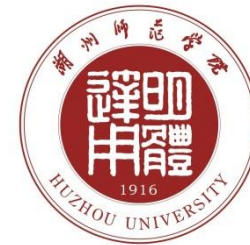
Fuqiang Wang 王福强

University Purdue, Huzhou University

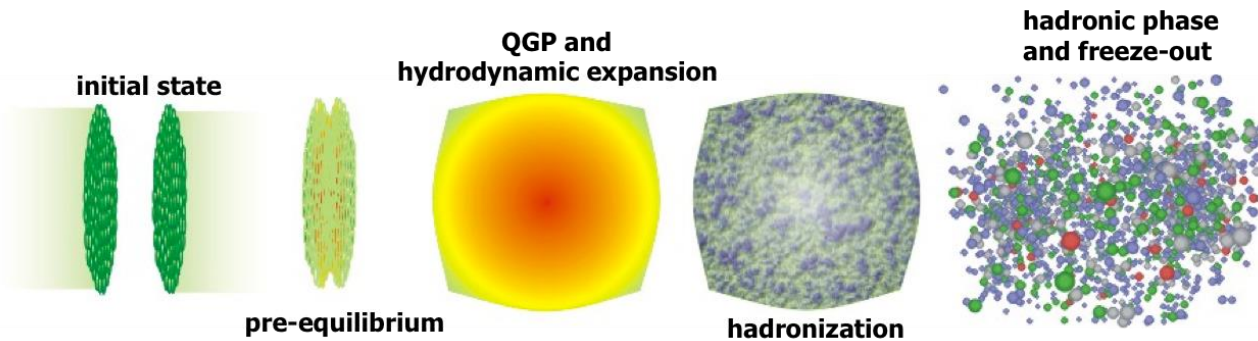


## Outline

Introduction  
Hydrodynamic flow  
Escape mechanism  
Summary



# Azimuthal Anisotropy

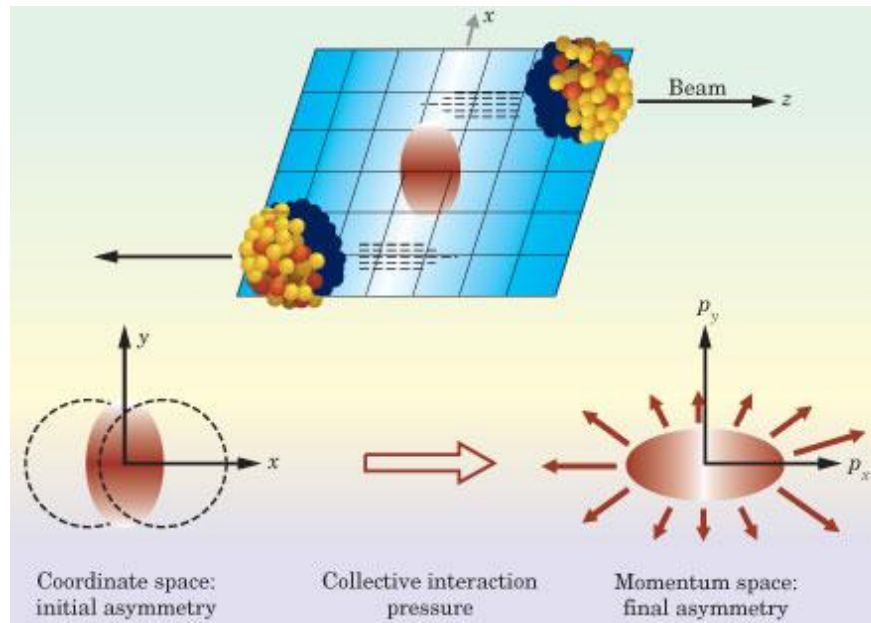


$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

$$v_2 = \frac{\langle p_x^2 - p_y^2 \rangle}{\langle p_x^2 + p_y^2 \rangle}$$

$$\equiv \langle \cos 2\varphi \rangle$$

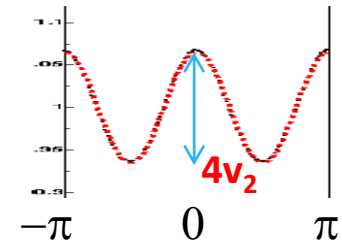
$$\varphi = \tan^{-1} \left( \frac{p_y}{p_x} \right)$$



$\vec{x}$ -anisotropy  $\Rightarrow$   $\vec{p}$ -anisotropy  
interaction

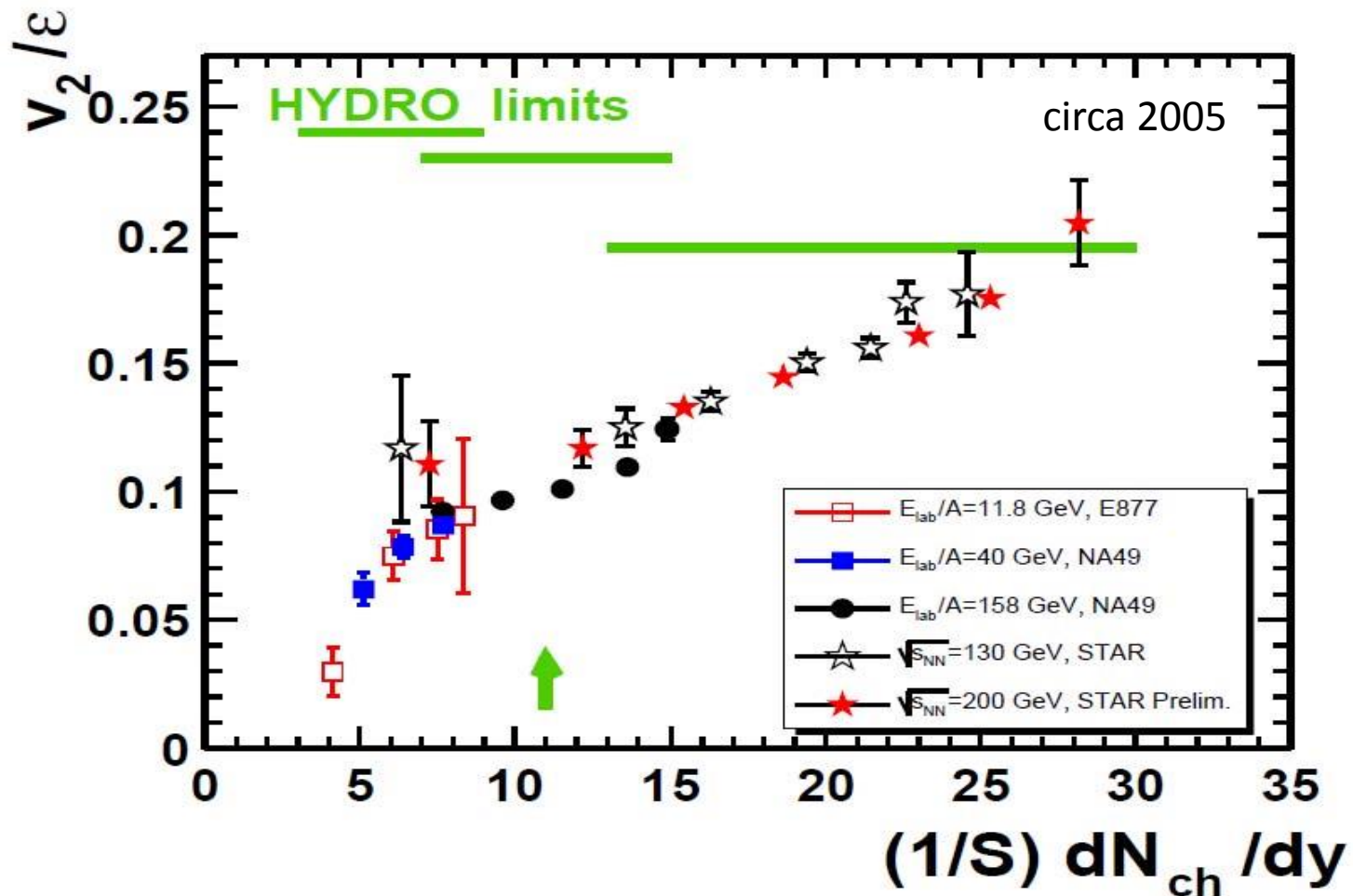
Common thinking:

High density, pressure  
Pressure grad. anisotropy  
Hydrodynamic expansion  
Strongly interacting QGP

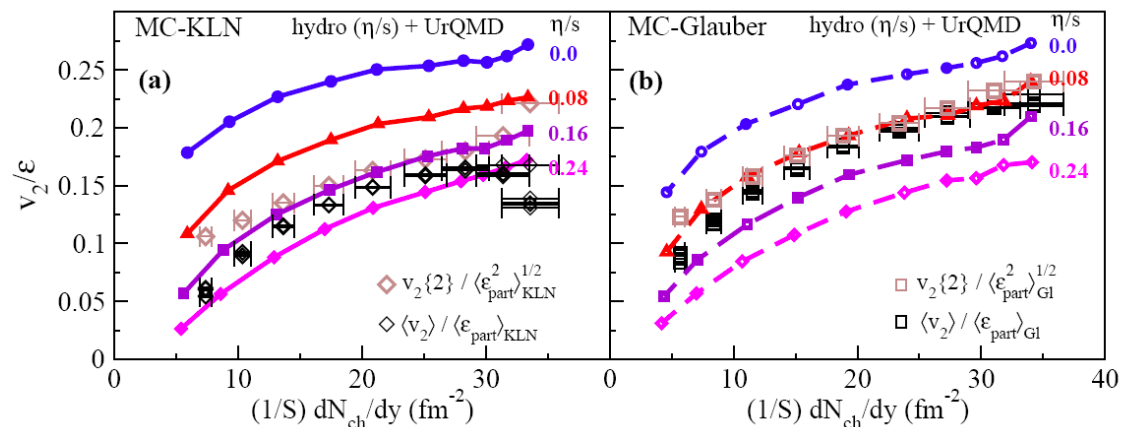
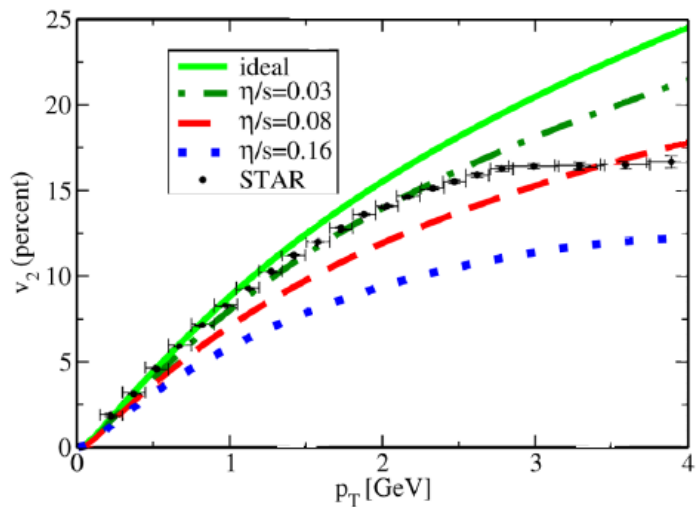
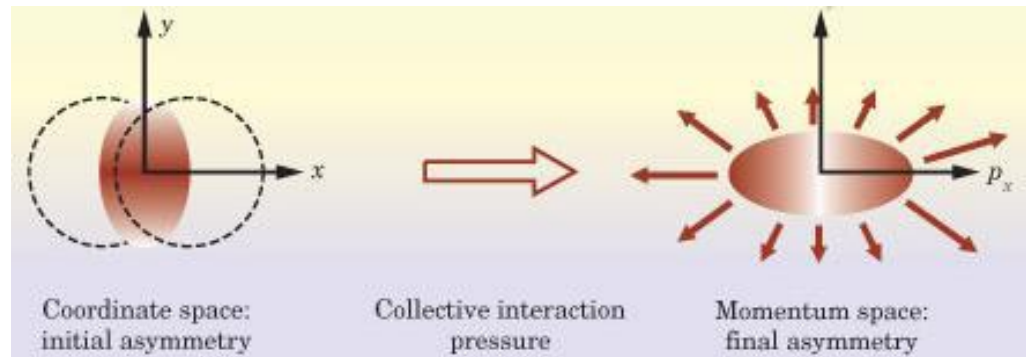
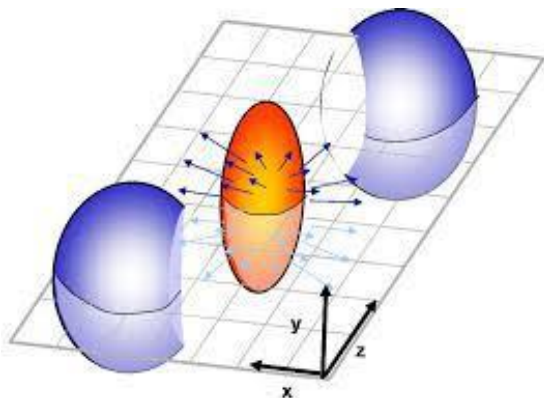


# Finally “hydro” at RHIC...

The question is: **how strong is the interaction?**



# Hydrodynamic calculation

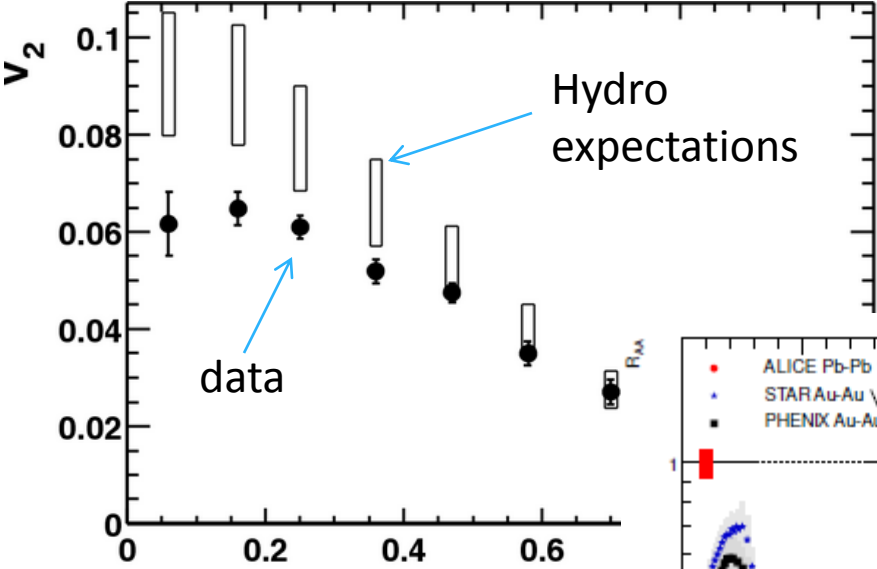


- ➔ **Small value** of viscosity over entropy density  $\eta/s$
- ➔ Model uncertainty dominated by **initial ecc.  $\epsilon$**

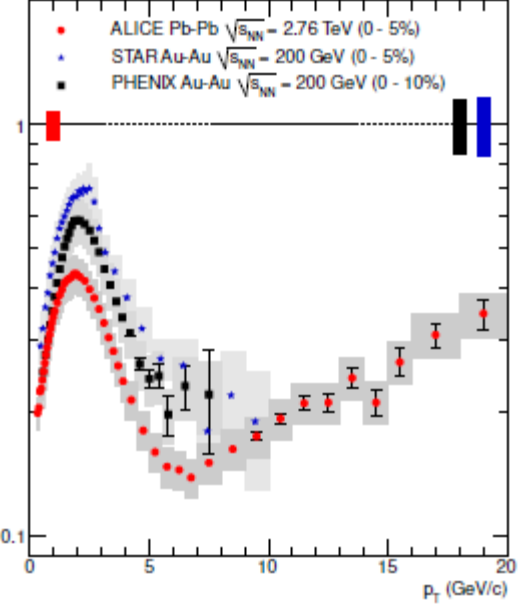
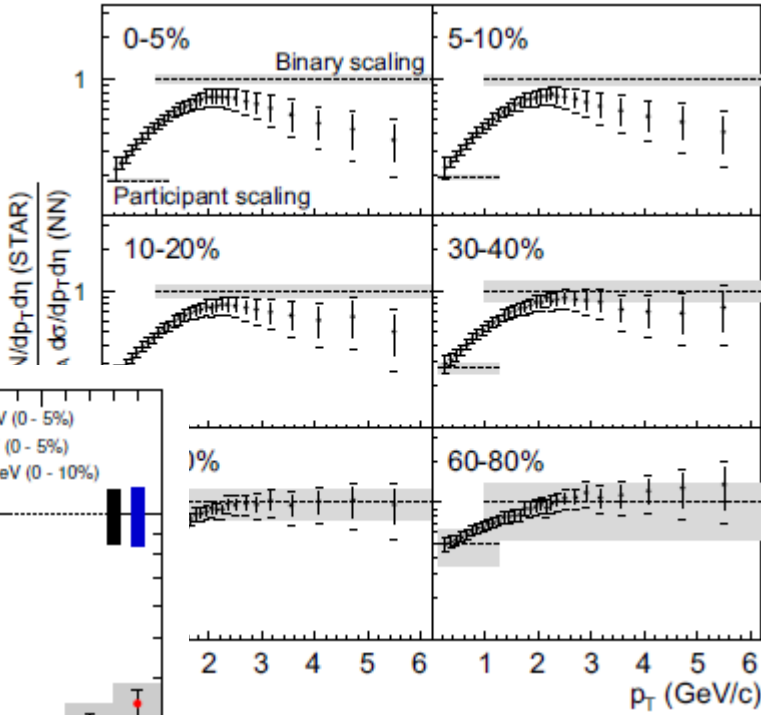
Model: Song *et al.* [arXiv:1011.2783](https://arxiv.org/abs/1011.2783)

# Corroborated by large energy loss

STAR, PRL86 (2001) 402



STAR, PRL89 (2002) 202301



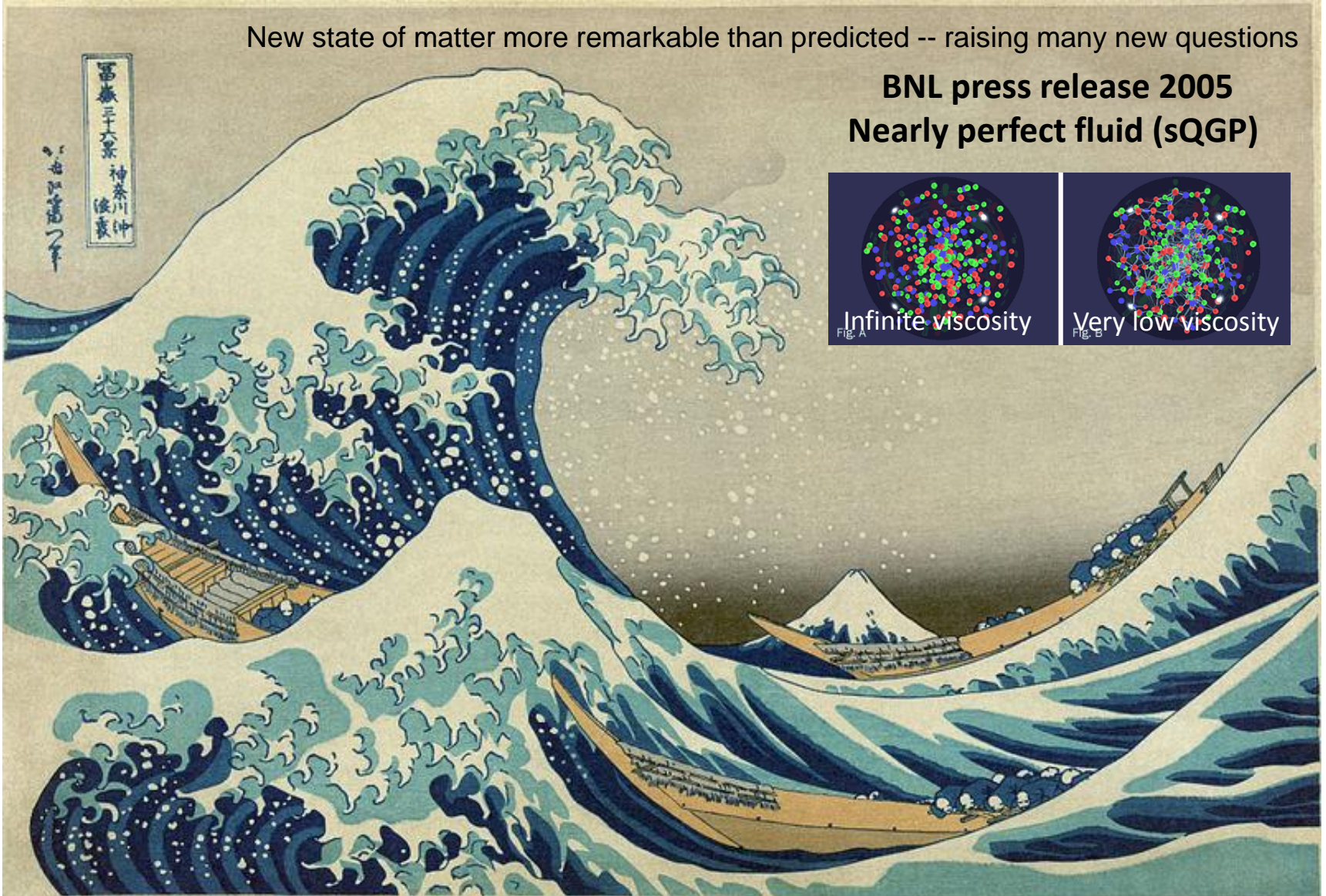


# The Hydrodynamic Paradigm

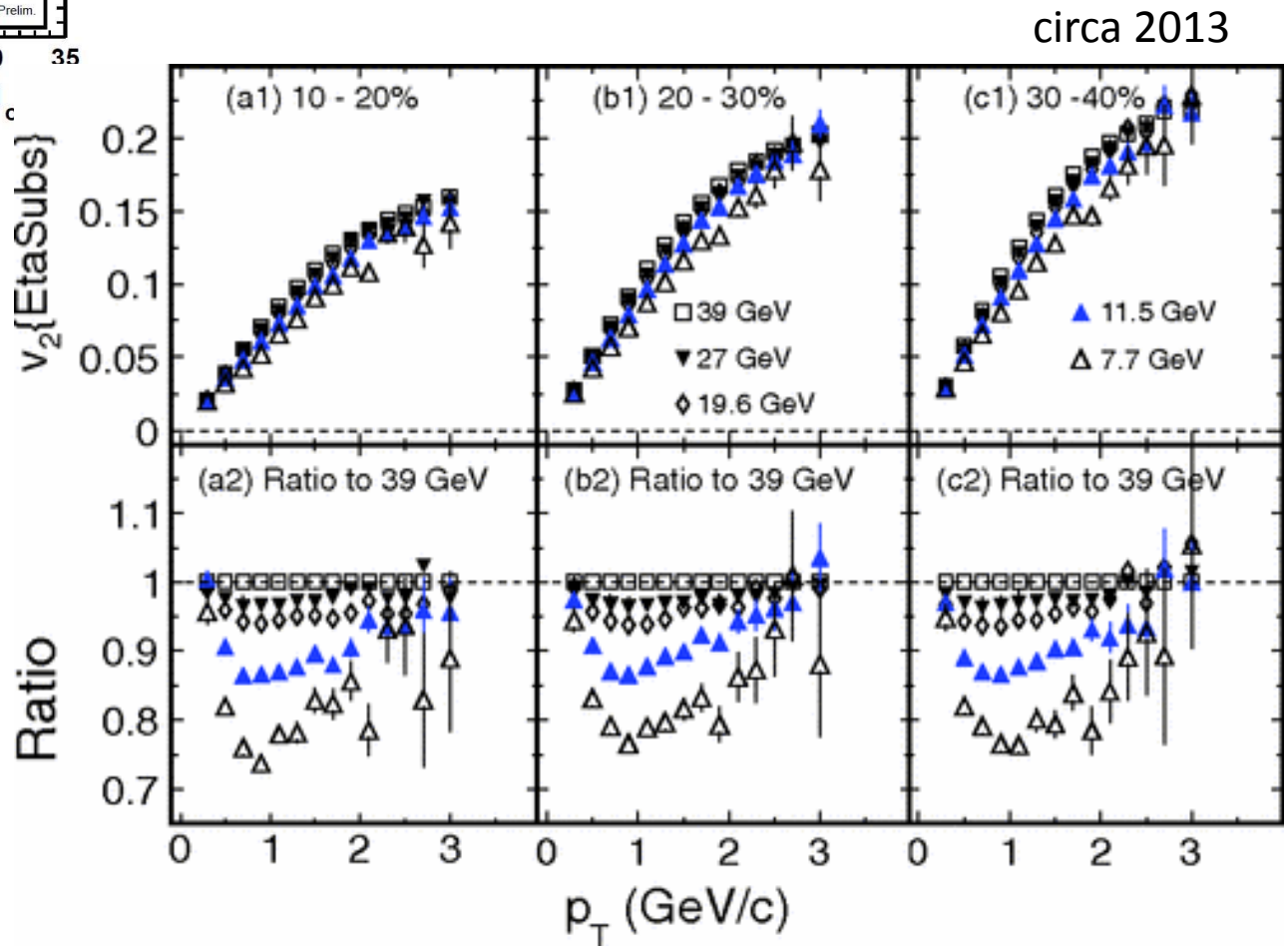
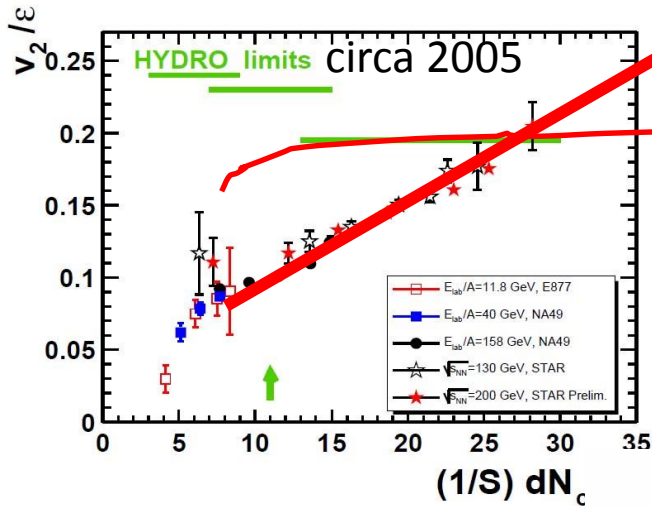
ca 2005

New state of matter more remarkable than predicted -- raising many new questions

**BNL press release 2005**  
**Nearly perfect fluid (sQGP)**

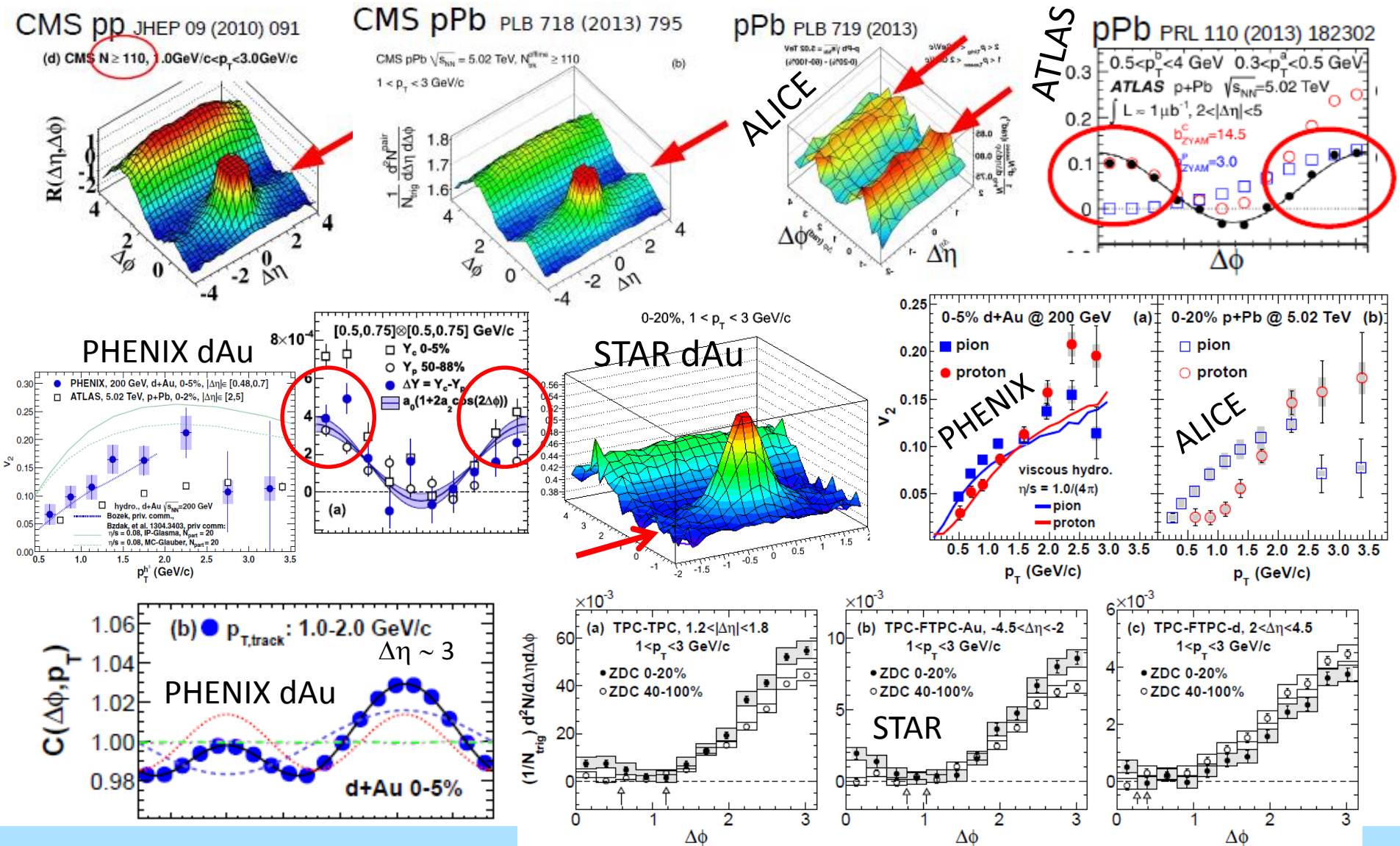


But actually very little energy dependence





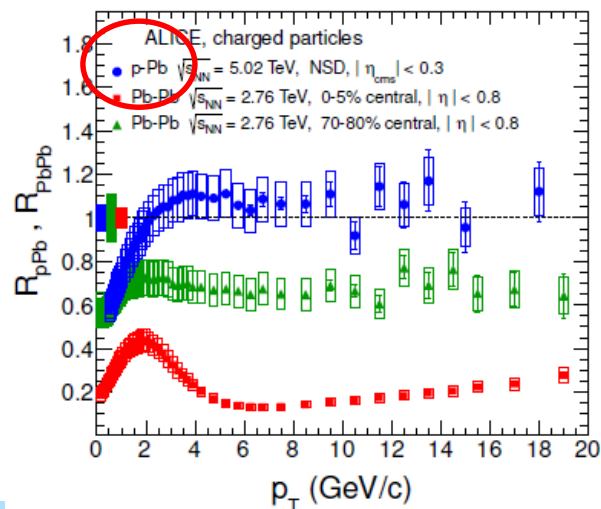
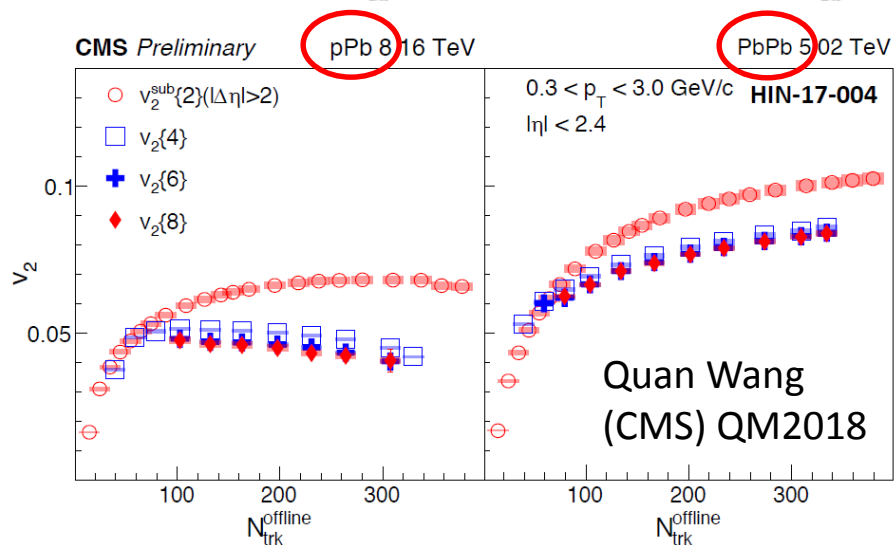
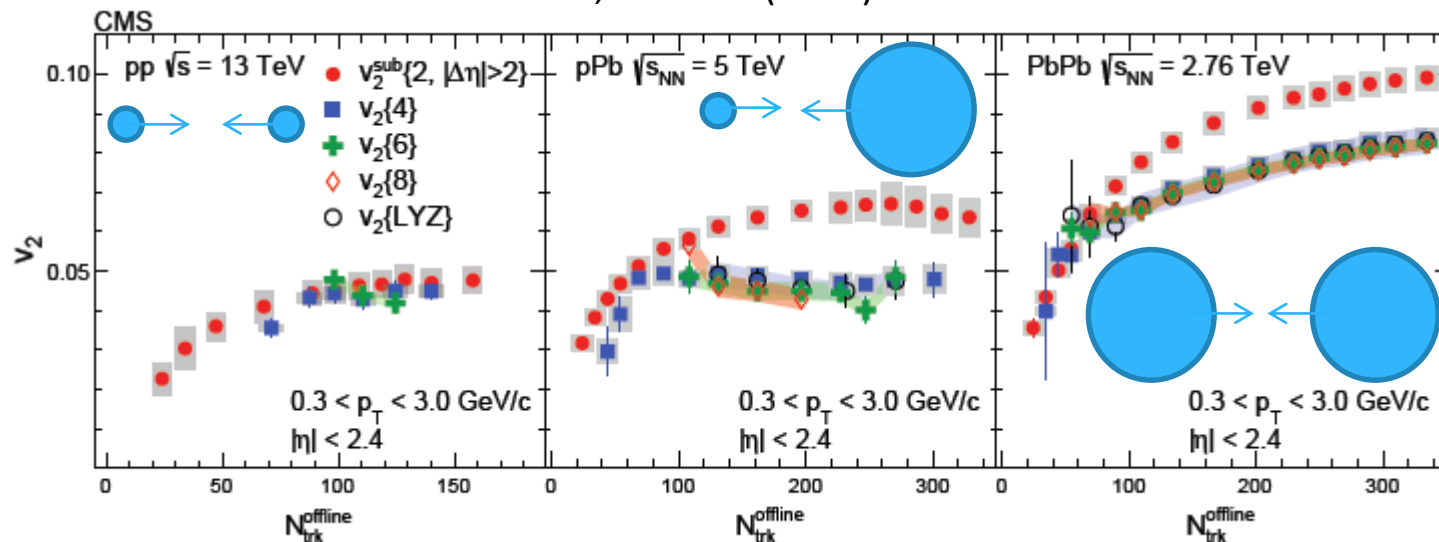
# “flow” everywhere, even in small systems





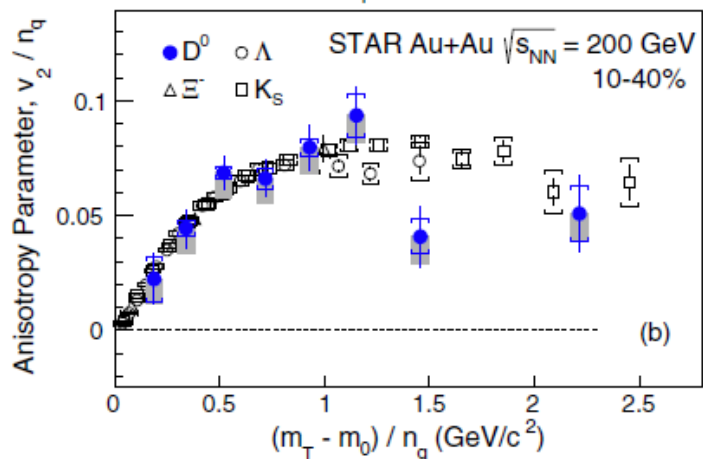
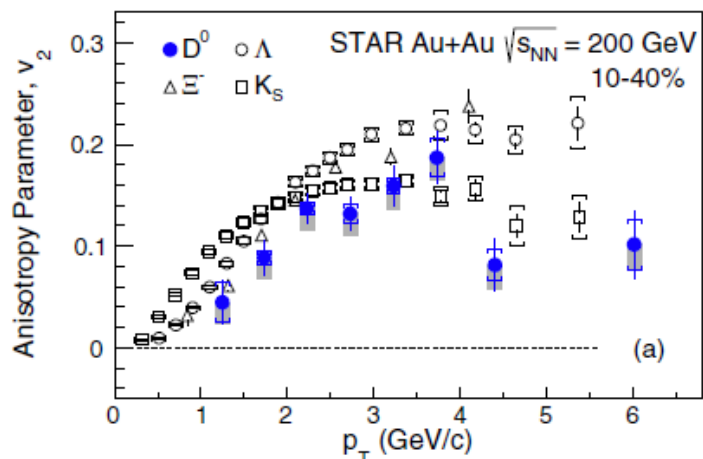
# “Flow” in small systems, but no energy loss

CMS, PLB 765 (2017) 193

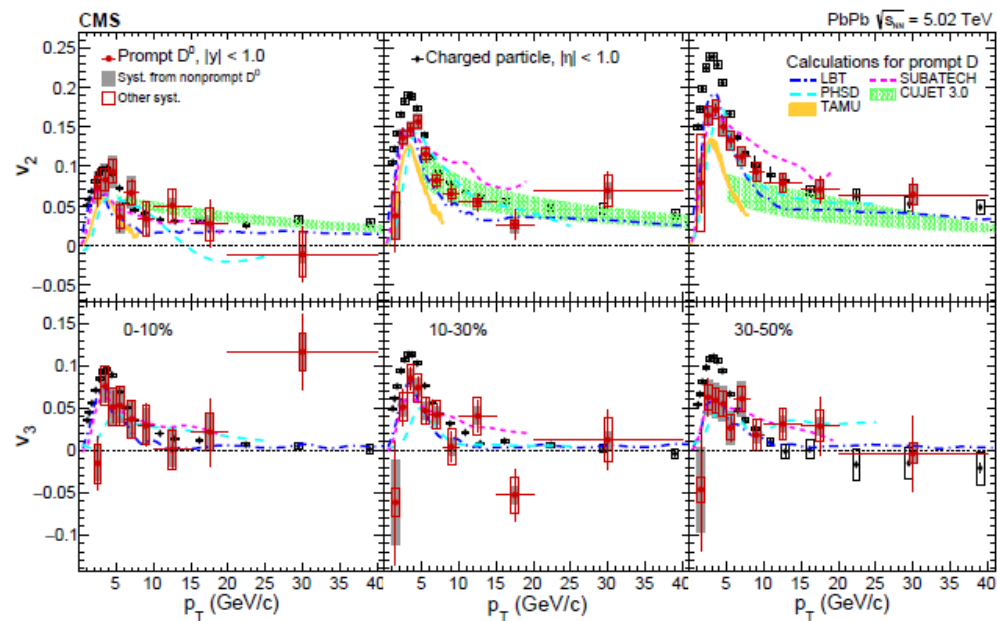


# Heavy flavor “flows”

STAR, PRL 118, 212301 (2017)

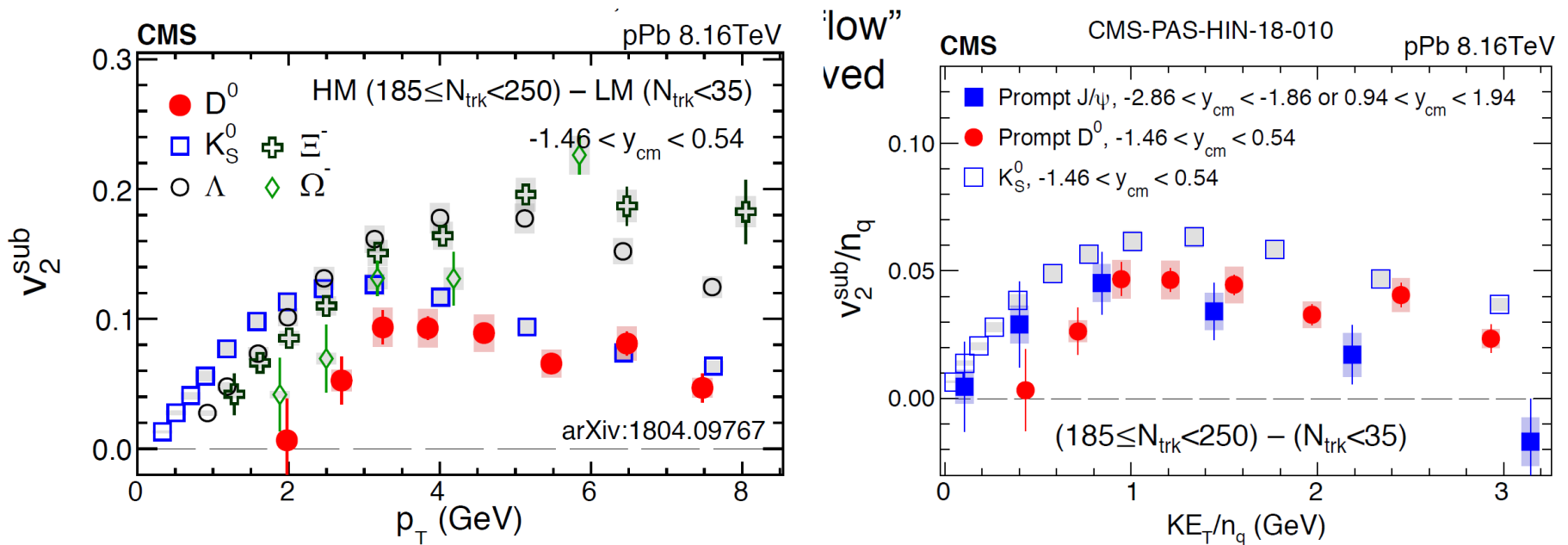


CMS, arXiv:1708.03497



# Heavy flavor flows, AND in small systems

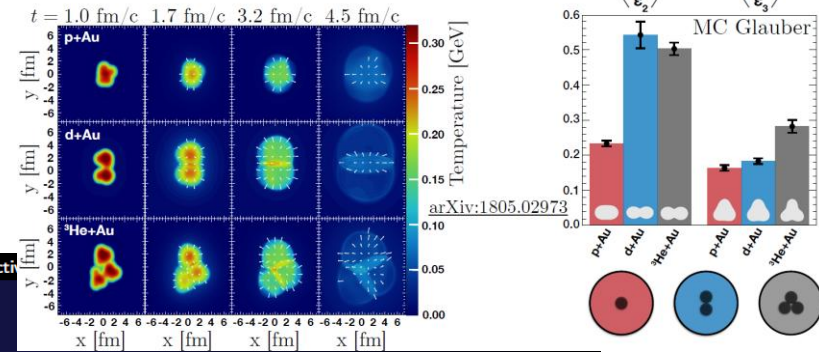
Wei Li (CMS), QM 2018



- Significant  $D^0$   $v_2$ , follow mass ordering at low  $p_T$
- $D^0$  similar to  $K^0$ s (both mesons) at higher  $p_T$
- Significant charmonium  $v_2$

# QGP droplets?

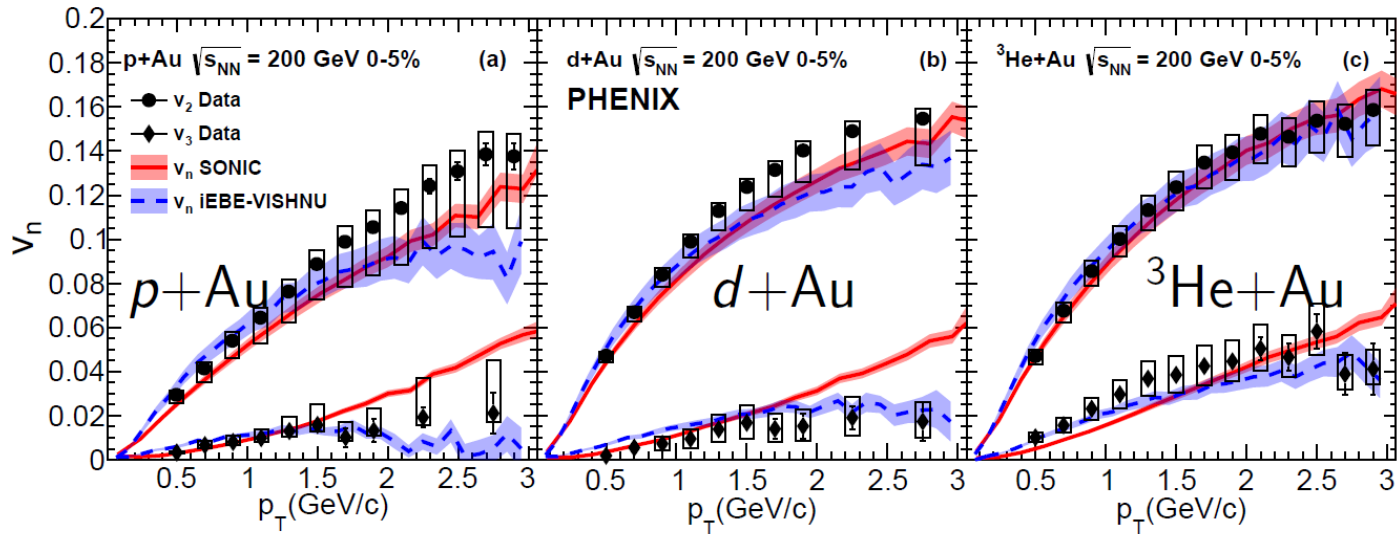
Belmont, QM 2018 PHENIX Highlights  
Morrow (PHENIX) QM 2018



High- $p_T$  hadrons      Heavy flavor      Collectivity

## Testing hydro by controlling system geometry

Sylvia Morrow, Tuesday 15/05/2018, 11:10      arXiv:1805.02973, submitted to Nature Physics



$v_2$  and  $v_3$  vs  $p_T$  described very well by hydro in all three systems  
—Strongly suggests QGP droplets in hydro evolution



# FLOW EVERYWHERE



# Light quark flows, heavy quark flows





# Different views

QGP in pp/pA? As strongly interacting?



[Escape the room](#)

# Materials

Mostly based on:

**L. He, T. Edmonds**, Z.-W. Lin, F. Liu, D. Molnar, F. Wang

**H. Li**, L. He, Z.-W. Lin, D. Molnar, F. Wang, W. Xie

**H. Li**, L. He, Z.-W. Lin, D. Molnar, F. Wang, W. Xie

Z.-W. Lin, L. He, T. Edmonds, F. Liu, D. Molnar, F. Wang

H. Li, Z.-W. Lin, , F. Wang

Z.-W. Lin, H. Li, F. Wang

**H. Li**, Z.-W. Lin, F. Wang

Phys. Lett. **B735** (2016) 506

Phys. Rev. **C93** (2016) 051901(R)

Phys. Rev. **C96** (2017) 014901

Nucl. Phys. **A956** (2016) 316

J.Phys.**779** (2017) 012063, SQM16

charm anisotropy, SQM 2017

arXiv:1804.02681



# Parton cascade history

AMPT can describe bulk data well...  
both AA and pA



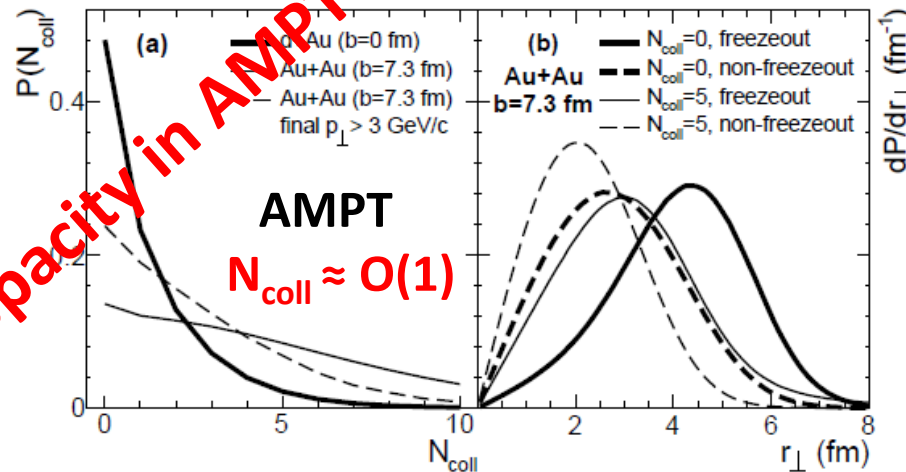
- Get into transport code
- Follow cascading history, microscopic interactions
- Investigate how parton  $v_n$  is generated

$$L_{\text{mfp}} = 1/\rho\sigma$$

Opacity:

$$L/L_{\text{mfp}} = \rho\sigma L$$

Low opacity in AMPT



$$dN/dy \sim 1000$$

$$\rho \sim 1000/\pi R^2 \tau$$

$$\sim 6 \text{ fm}^{-3}$$

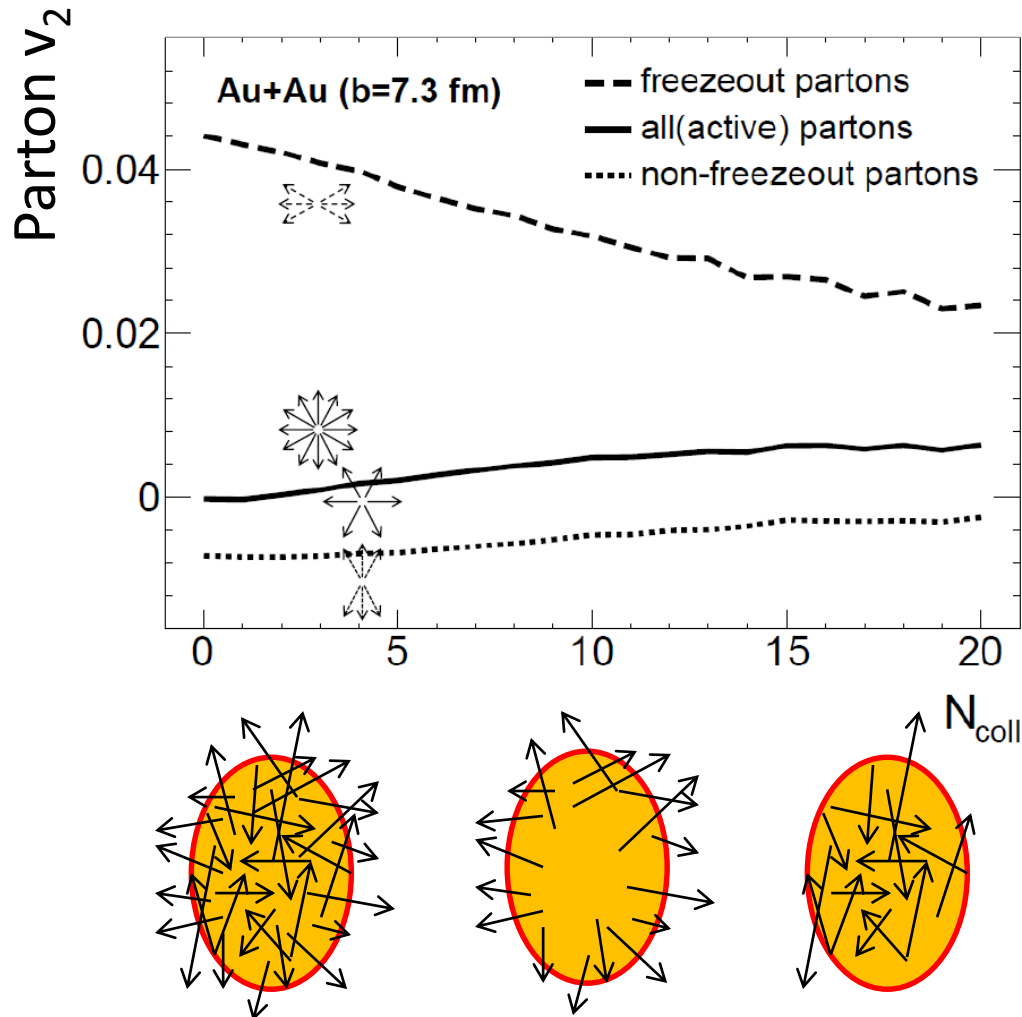
$$\rho\sigma L \sim$$

$$6 \text{ fm}^{-3} * 3 \text{ mb} * 3 \text{ fm}$$

$$\sim 5$$

# How is anisotropy developed in AMPT?

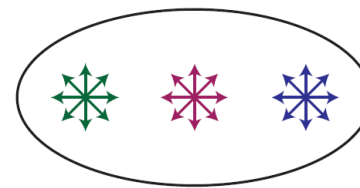
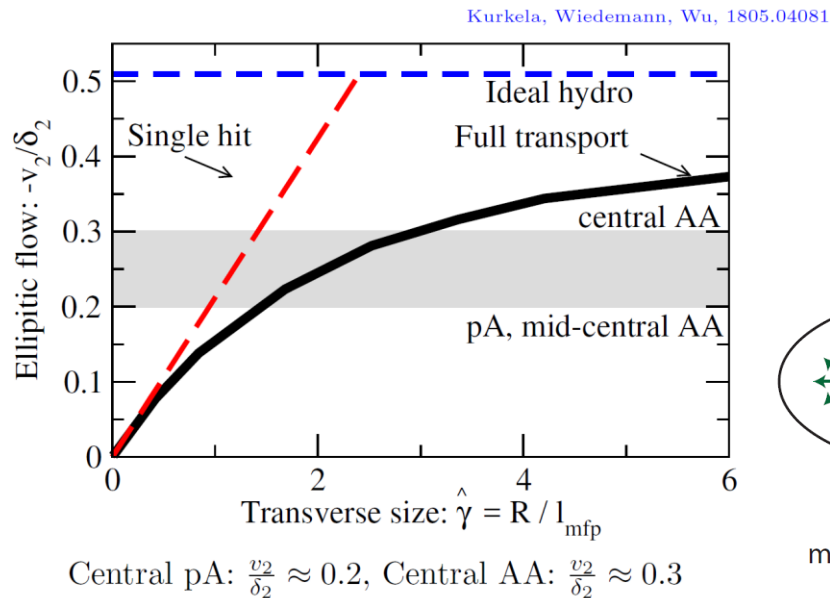
L. He, T. Edmonds, Z.-W. Lin, F. Liu, D. Molnar, FW, arXiv:1502.05572



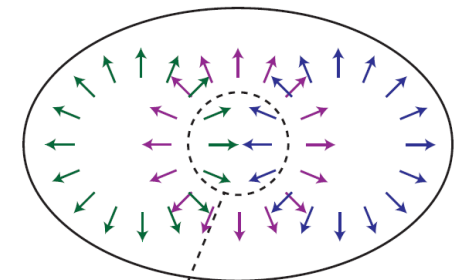
- Partons freeze out with large positive  $v_2$ , even when they do not interact at all.
- This is due to larger escape probability along  $x$  than  $y$ .
- Remaining partons start off with negative  $v_2$ , and become  $\sim$ isotropic ( $v_2 \sim 0$ ) after one more collision.
- Process repeats itself.
- Similar for  $v_3$ .
- Similar for d+Au collisions.

# Analytical/numerical kinetic transport

Kurkela, QM 2018



Initially isotropic momentum distribution



More particles moving in  $\pm x$ -direction

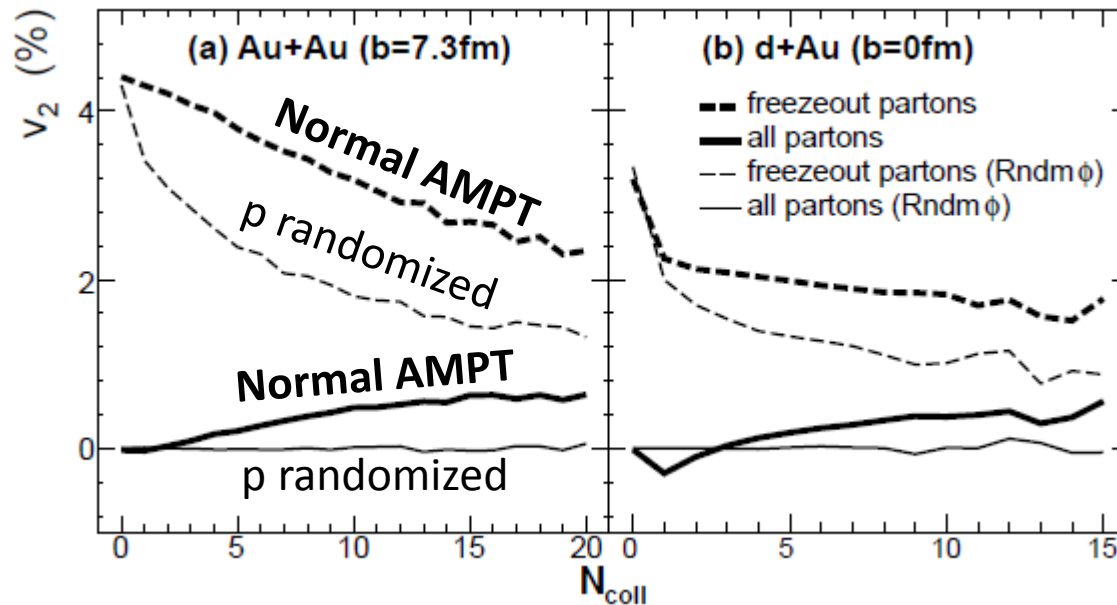
- ▶ Closer to single hit regime than ideal hydro  
 $\eta/s \gtrsim 0.5$

- ▶ Initial condition initially isotropic in momentum space, anisotropic in coordinate space
- ▶ Free streaming makes local patches anisotropic
- ▶ Collisions isotropize the distribution in the center  
 $\Rightarrow$  Reduction of horizontal movers and increase of vertical movers

Related closely to *anisotropic parton escape mechanism*, He et al. PLB753 (2016)

# Majority anisotropy from escape

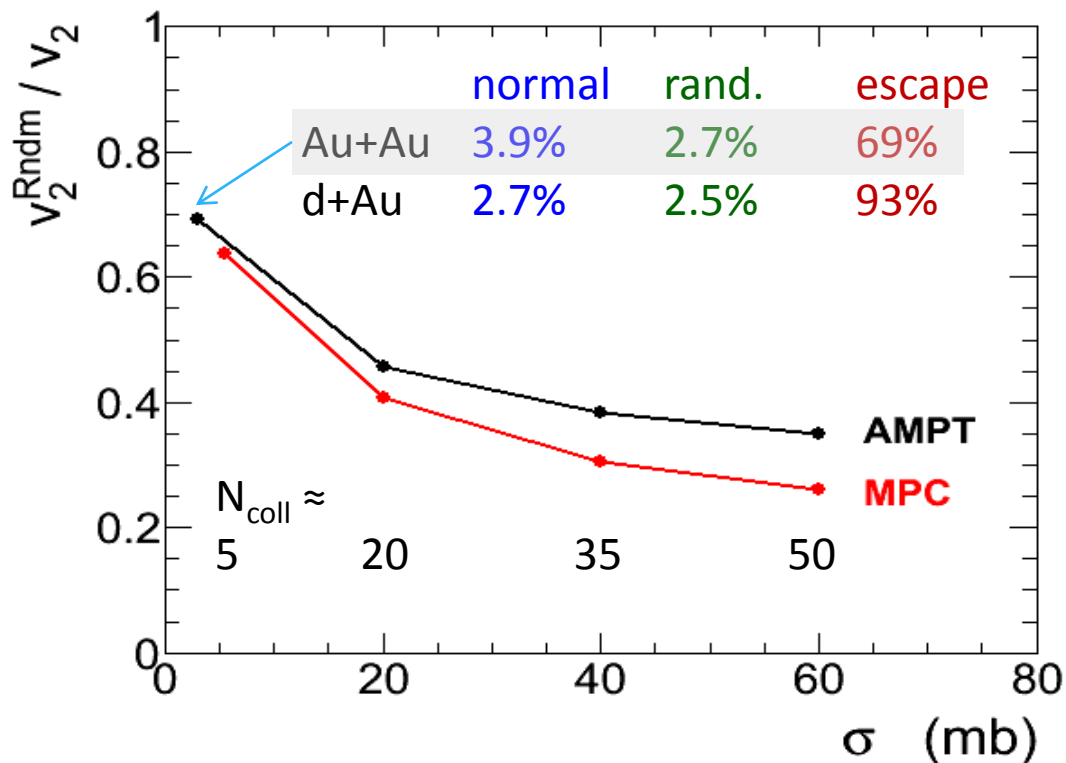
L. He, T. Edmonds, Z.-W. Lin, F. Liu, D. Molnar, FW, arXiv:1502.05572, PLB753(2016)506



- **Majority of anisotropy comes from the final-step “escape” mechanism.**
- The small dynamic  $v_2$  is result of hydrodynamic pressure push. It is this flow that is most relevant. However it plays a minor role.
- **May explain small system data and weak energy dependence.**

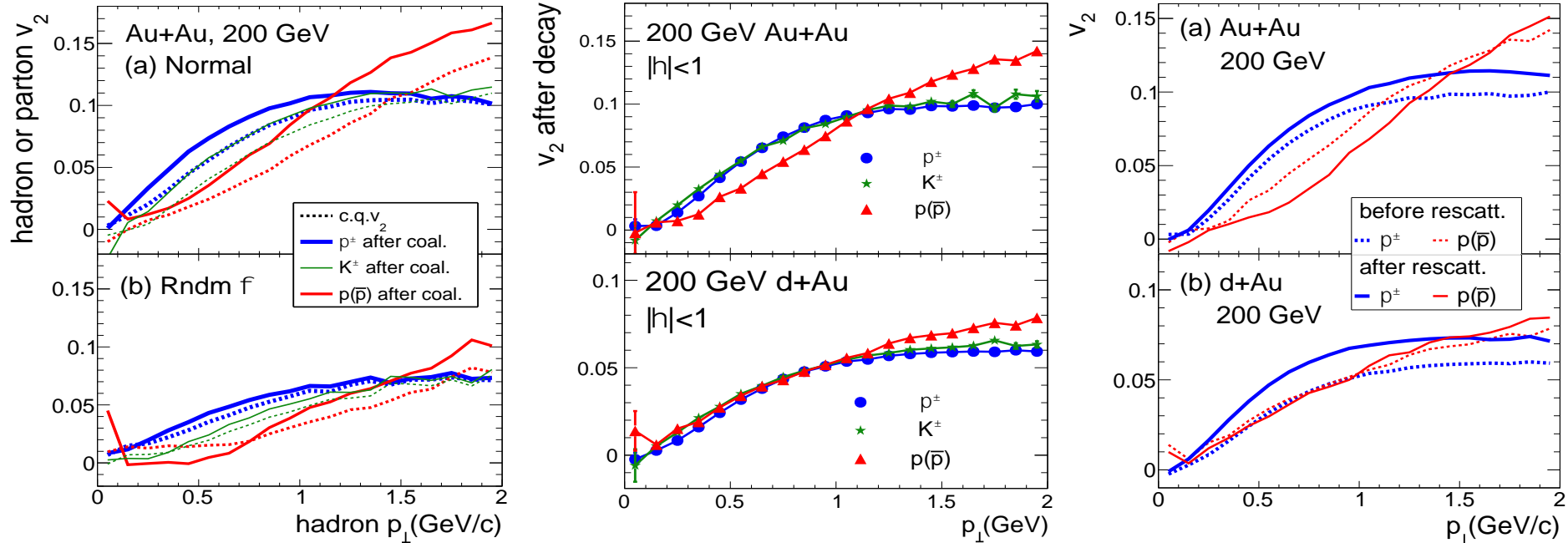


# Relative escape contribution



- **Escape contribution still sizeable even at x10 larger x-sections.**

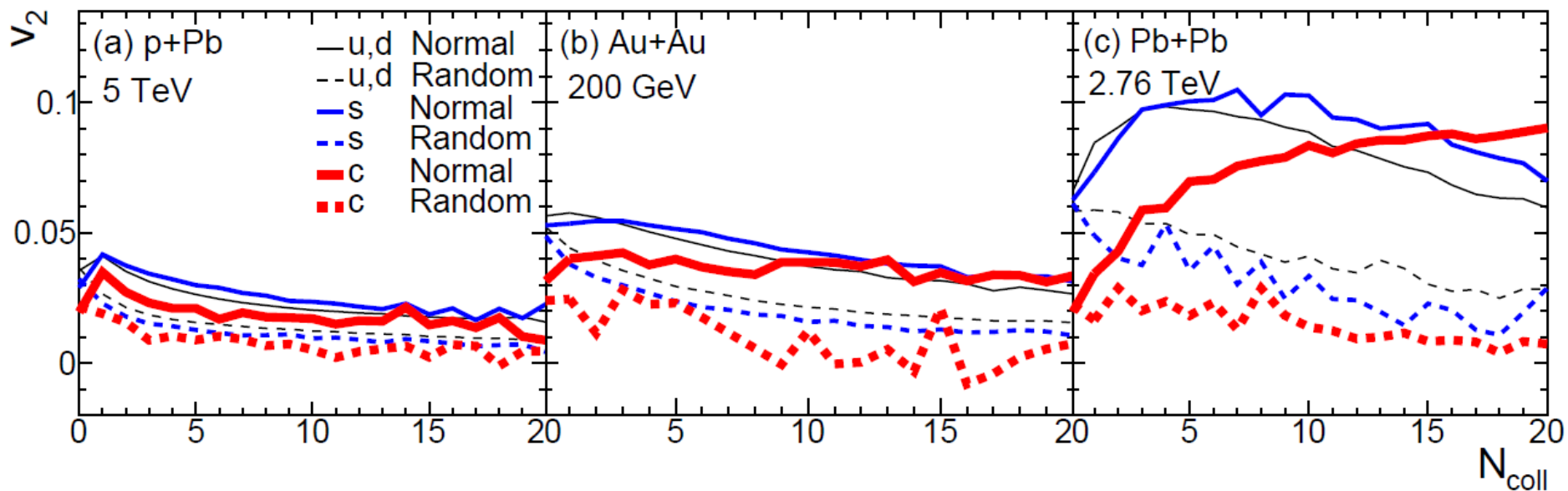
# Mass splitting from hadronic rescattering



H.L. Li et al, Phys. Rev. C 93,051901(R)(2016)

The mass splitting is generated by coalescence, reduced by decays, and then significantly increased by hadronic scatterings.

# The escape mechanism: *flavor dependence*



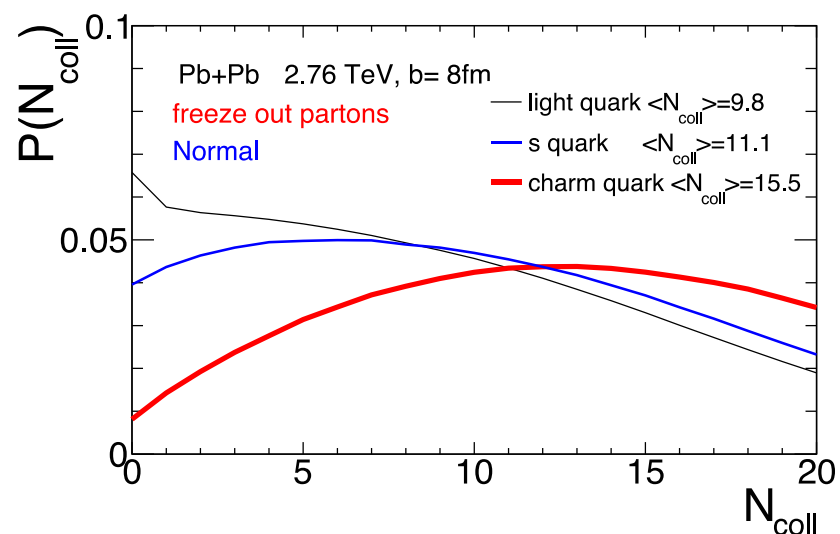
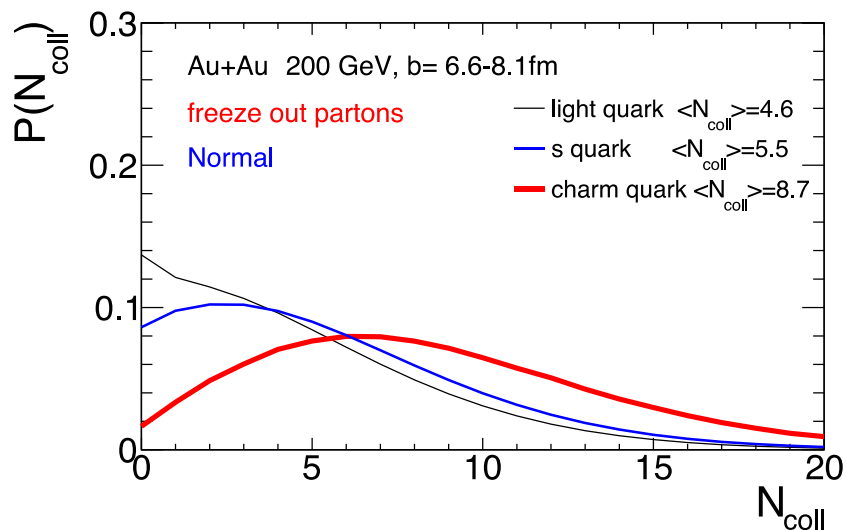
Mass ordering in  $v_2(N_{\text{coll}})$ :

$v_2c < v_2s < v_2ud$  at small  $N_{\text{coll}}$

$v_2c > v_2s > v_2ud$  at large  $N_{\text{coll}}$ , reversed

Escape mechanism is at work for all flavors

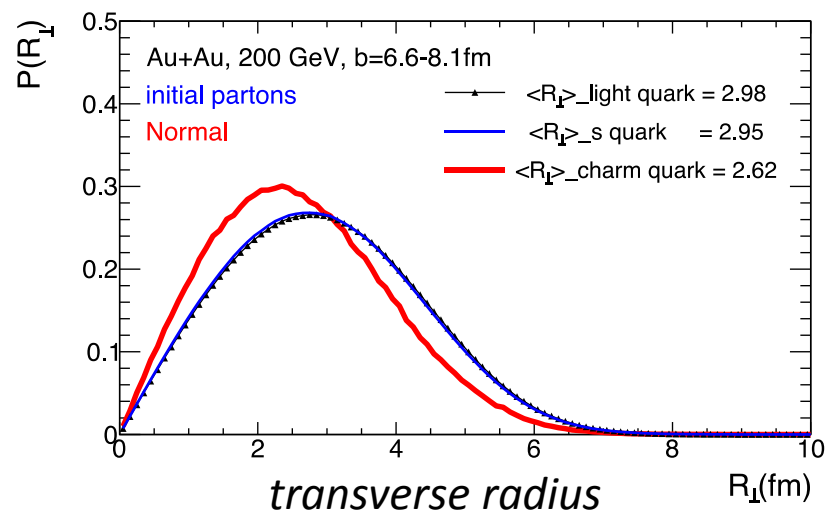
# The escape mechanism: *flavor dependence*



Quark mass ordering in the  $N_{\text{coll}}$  distribution  
for all 3 systems:

$$\langle N_{\text{coll}} \rangle_c > \langle N_{\text{coll}} \rangle_s > \langle N_{\text{coll}} \rangle_{ud}$$

Related to the initial  
(velocity &) spatial distribution





# Toy model: *flavor dependence*

**Initial**  $v_2 = 0$

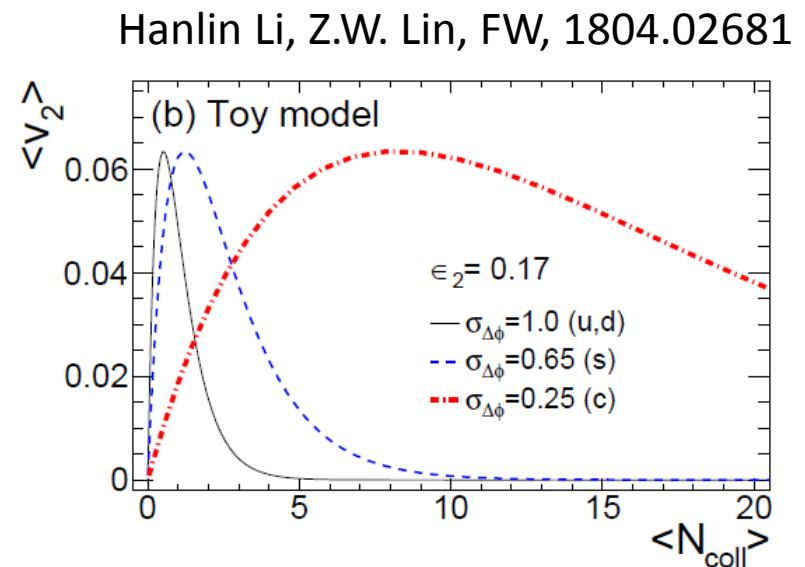
The parton azimuth  $f_f$  after  $\langle N_{coll} \rangle$  collisions

$$f_f = f_i + \text{Gaus}(\sqrt{N_{coll}}(f_i) \cdot Dq)$$

$$N_{coll}(f_i) = \langle N_{coll} \rangle \times (1 - 2e_2 \times \cos(2f_i))$$

$Dq$  parton average azimuthal deflection after each collision

**Final**  $v_2 = \langle \cos(2\phi_f) \rangle$



**With small  $N_{coll}$ , light quark  $v_2 >$  charm  $v_2$ . With large  $N_{coll}$ , it is the opposite.** This is because light quarks are more randomized after each collision due to the large angle deflection.

# Heavy quark flow

Followed the complete parton collision history to study light/strange/charm quark  $v_2$  in AMPT

$\langle v_2 \rangle_{\text{random-}\varphi} / \langle v_2 \rangle_{\text{normal}}$  ratio  $\sim$  fraction from pure escape:

|     | dAu@200GeV<br>b=0 fm | pPb@5TeV<br>b=0 fm | AuAu@200GeV<br>b=6.6-8.1 fm | PbPb@2.76TeV<br>b=8 fm |
|-----|----------------------|--------------------|-----------------------------|------------------------|
| u/d | 93%(all quarks)      | 73%                | 66%                         | 43%                    |
| s   |                      | 59%                | 47%                         | 27%                    |
| c   |                      | 57%                | 22%                         | 9%                     |

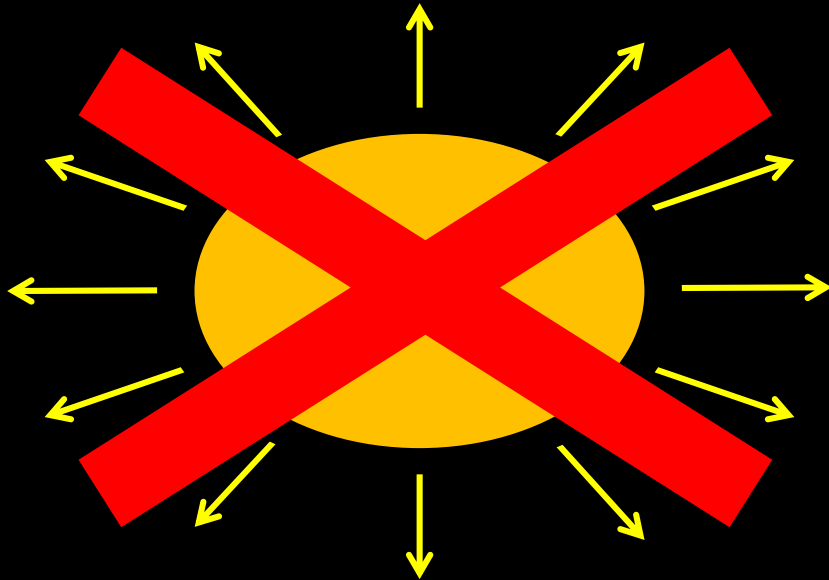
## Light quark $v_2$ :

escape more important for AuAu@RHIC, pPb@LHC, and smaller/lower-energy systems;  
hydro-type flow more important for PbPb@LHC, although still significant escape contribution.

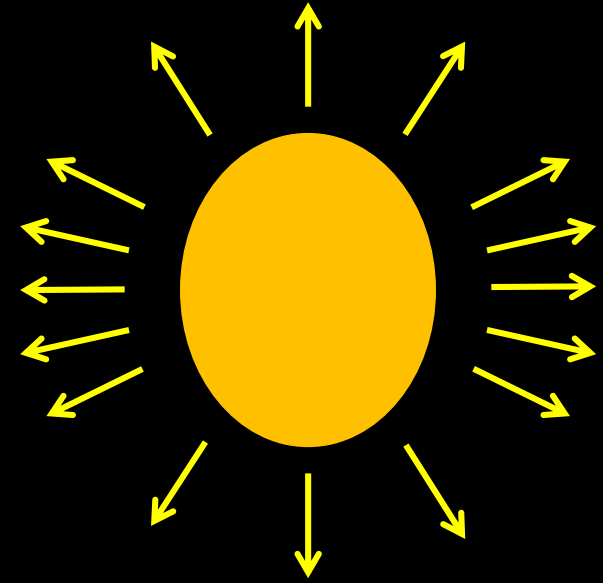
**Charm  $v_2$**  in AuAu@RHIC-200GeV & PbPb@LHC: mostly comes from **collective flow**

→ heavy quarks are more sensitive probes of collective flow & the medium

# Anisotropy mechanism

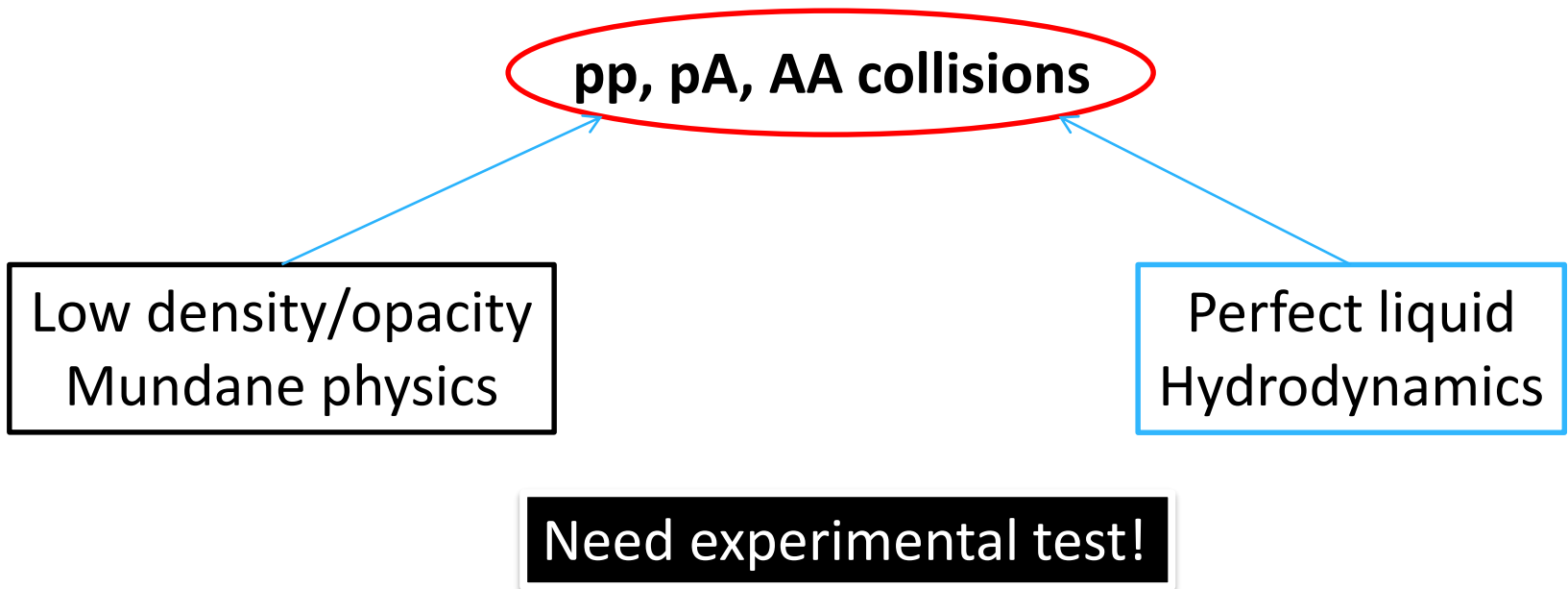


**Expansion, flow  
Hydro paradigm**



**No expansion  
But escape**

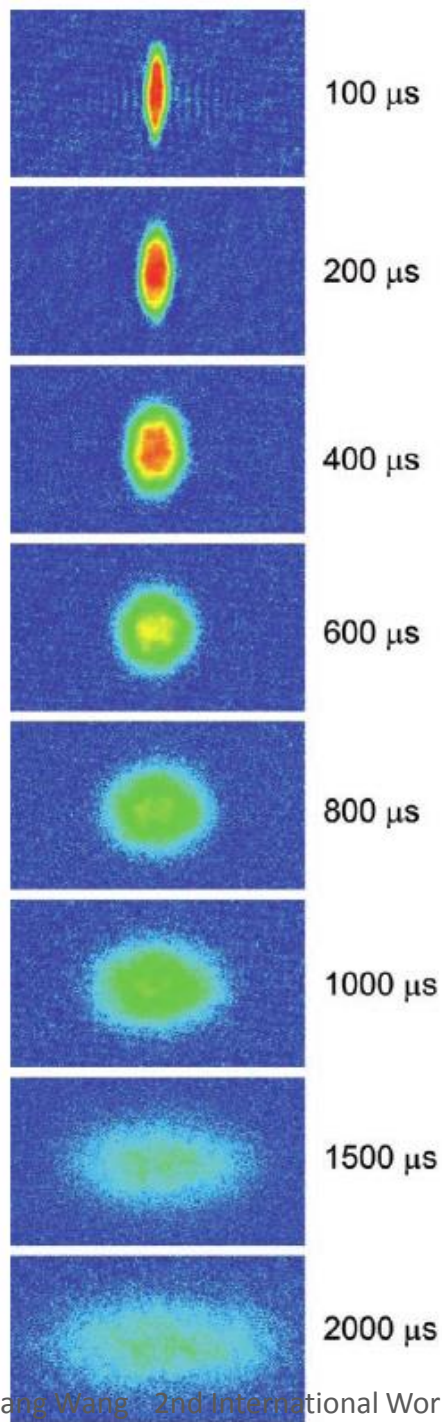
**DATA**





# Cold atom experiment

K. M. O'Hara *et al.*, Science 298, 2179 (2002)



**Large elliptic anisotropy  
in cold atom systems  
consistent with hydrodynamic flow**

# Opacity

Mean free path:  $L_{\text{mfp}} = 1/\rho\sigma$ ,  $N_{\text{coll}} = \text{Opacity} = L/L_{\text{mfp}} = \rho\sigma L$

**Cold atom system:**

$$\begin{aligned}
 a &\approx 5 \times 10^{-5} \text{ cm} \\
 \sigma_{\text{int}} &\approx 10^{-8} \text{ cm}^2 \\
 \rho &\approx 5 \times 10^{13} / \text{cm}^3 \\
 L_{\text{mfp}} &\approx 2 \times 10^{-6} \text{ cm} \\
 L &\approx 2 \times 10^{-3} \text{ cm} \\
 \mathbf{L/L_{\text{mfp}} \approx 1000}
 \end{aligned}$$

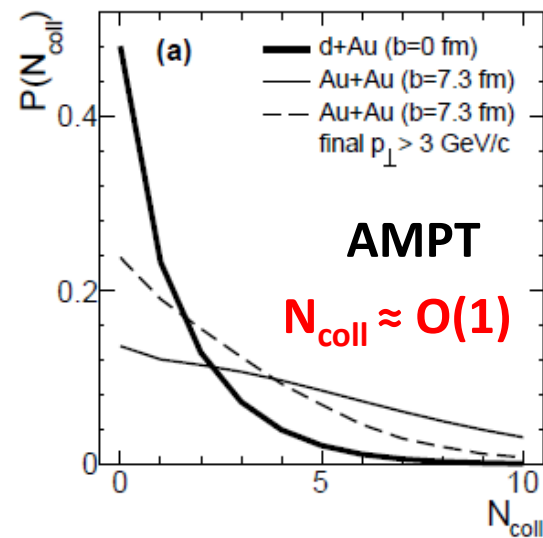
**Very high opacity for the cold atom system**

**Indeed hydro!**

**Heavy ion collision:**

$dN/dy \sim 1000$ ,  $\rho \sim 1000/\pi R^2 \tau \sim 6 \text{ fm}^{-3}$

$\rho\sigma L \sim 7 \text{ fm}^{-3} * 3 \text{ mb} * 3 \text{ fm} \sim 5$

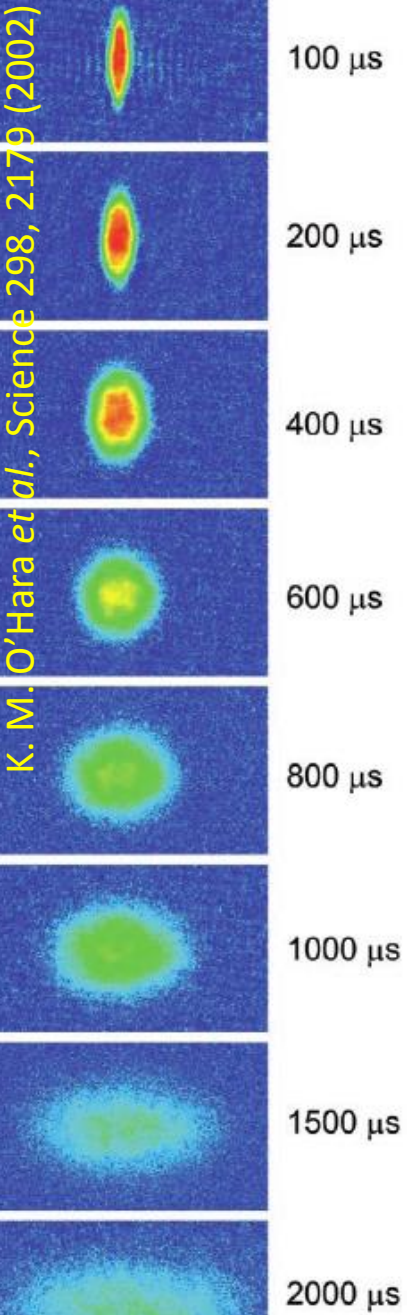


**Low opacity in AMPT**

**Hydro??**

K. M. O'Hara et al., Science 298, 2179 (2002)

# To emulate QGP with cold atoms



K. M. O'Hara et al., Science 298, 2179 (2002)

$\rho\sigma_{\text{int}}L$ : reduce opacity by  $10^3$   
1000  $\rightarrow$  1

Opacity:  $\rho\sigma L$

$a \approx 5 \times 10^{-5} \text{ cm}$

$\sigma_{\text{int}} \approx 10^{-8} \text{ cm}^2$

$\rho \approx 5 \times 10^{13} / \text{cm}^3$

$L_{\text{mfp}} \approx 2 \times 10^{-6} \text{ cm}$

$L \approx 2 \times 10^{-3} \text{ cm}$

$L/L_{\text{mfp}} \approx \text{1000}$

0-1

$\times 10^{-3}$

Very high opacity for the cold atom system



Low opacity for the cold atom system

# Summary

- The **escape mechanism** can simultaneously, most naturally explain  $v_n$  in small/large systems, at low/high energies, for light/heavy flavors.
- Cannot conclude from flow measurements that we have a “nearly perfect fluid.”  
Our paradigm **“nearly perfect fluid” may be wrong.**
- A question we should all ask ourselves:  
**What fundamental physics have we learned?**