



# Flow coefficients of identified particles in large and small systems

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# Flow of identified particles...

Is a rather **broad** topic ... especially for 30 minutes

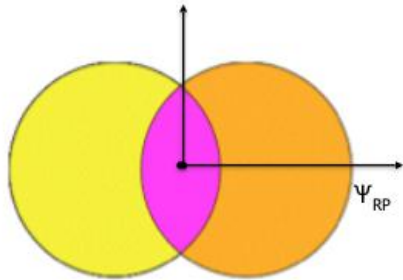
These slides: very **incomplete** overview of some **recent** results

**Apologies** in advance if I **miss** something .... or lean too much towards ALICE

That's what the **discussion** is for !

# Starting with a QM2018 slide from You Zhou ... :

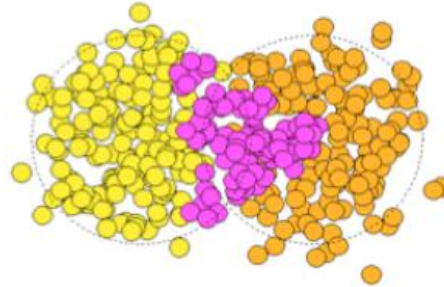
1992



$$v_2\{\Psi_{RP}\} = \langle \cos 2(\phi - \Psi_{RP}) \rangle$$

$\Psi_{RP}$ : Reaction Plane

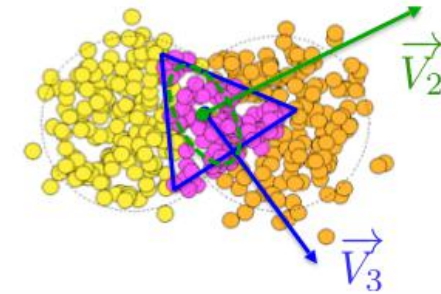
2010



$$v_n = \langle \cos n(\varphi - \Psi_n) \rangle$$

- Flow coefficient  $v_n$
- E-by-E  $v_n$  fluctuations

2014

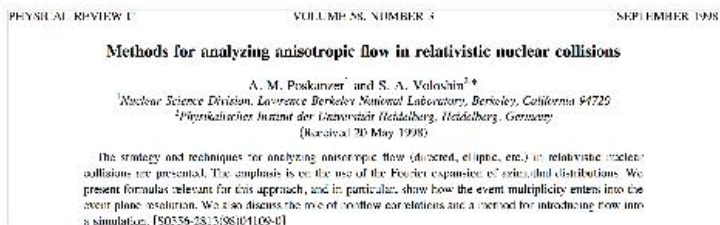


$$\vec{V}_m = v_m e^{-im\Psi_m}$$

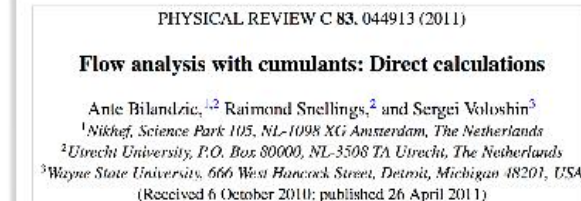
$$\vec{V}_n = v_n e^{-in\Psi_n}$$

- de-correlations of  $V_n$  vs  $p_T$  &  $\eta$
- correlations between  $v_n$  and  $v_m$ ?
- correlations between  $\Psi_n$  and  $\Psi_m$ ?

## Event-plane (1998)



## Q-Cumulant (2010)



## Generic framework (2014)



stealing a QM slide from You ... :

1992

2010

2014

A lot has changed in the last years!

1992: (before my time) : ' $v_n = v_{n2}$  and is straightforward to measure, easy to understand'

201\* : ' $v_{nmk}$ , global correlations in **all** systems?'

what does PID add to flow?

-> probing **radial** expansion velocity

-> hypothesis of particle production through **coalescence**

-> exploit different generation and freeze-out times of different species

-> ... etc

#### Methods for analyzing anisotropic flow in relativistic nuclear collisions

A. M. Poskanzer<sup>1</sup> and S. A. Voloshin<sup>2,\*</sup>

<sup>1</sup>Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720  
<sup>2</sup>Physikalisches Institut der Universität Heidelberg, Heidelberg, Germany

(Received 20 May 1998)

The strategy and techniques for analyzing anisotropic flow (directed, elliptic, etc.) in relativistic nuclear collisions are presented. The emphasis is on the use of the Fourier expansion of azimuthal distributions. We present formulas relevant for this approach, and in particular, show how the event multiplicity enters into the event plane resolution. We also discuss the role of flow correlations and a method for introducing flow into a simulation. [S0355-2815(98)04109-0]

#### Flow analysis with cumulants: Direct calculations

Ante Bilandzic,<sup>1,2</sup> Raimond Snellings,<sup>2</sup> and Sergei Voloshin<sup>3</sup>

<sup>1</sup>Nikhef, Science Park 105, NL-1098 XG Amsterdam, The Netherlands

<sup>2</sup>Utrecht University, P.O. Box 80000, NL-3508 TA Utrecht, The Netherlands

<sup>3</sup>Wayne State University, 666 West Hancock Street, Detroit, Michigan 48201, USA

(Received 6 October 2010; published 26 April 2011)

#### Generic framework for anisotropic flow analyses with multiparticle azimuthal correlations

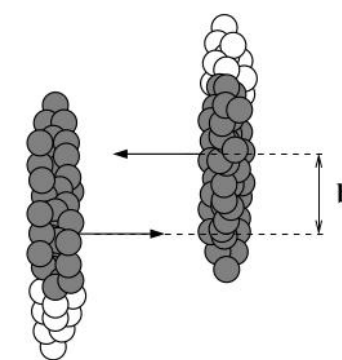
Ante Bilandzic,<sup>1</sup> Christian Holm Christensen,<sup>1</sup> Kristjan Gulbraadsen,<sup>1</sup> Alexander Hansen,<sup>1</sup> and You Zhou<sup>2,3</sup>

<sup>1</sup>Niels Bohr Institute, Blegdamsvej 17, 2100 Copenhagen, Denmark

<sup>2</sup>Nikhef, Science Park 105, 1098 XG Amsterdam, The Netherlands

<sup>3</sup>Utrecht University, P.O. Box 80000, 3508 TA Utrecht, The Netherlands

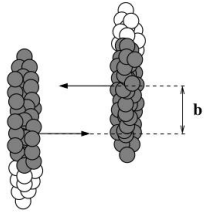
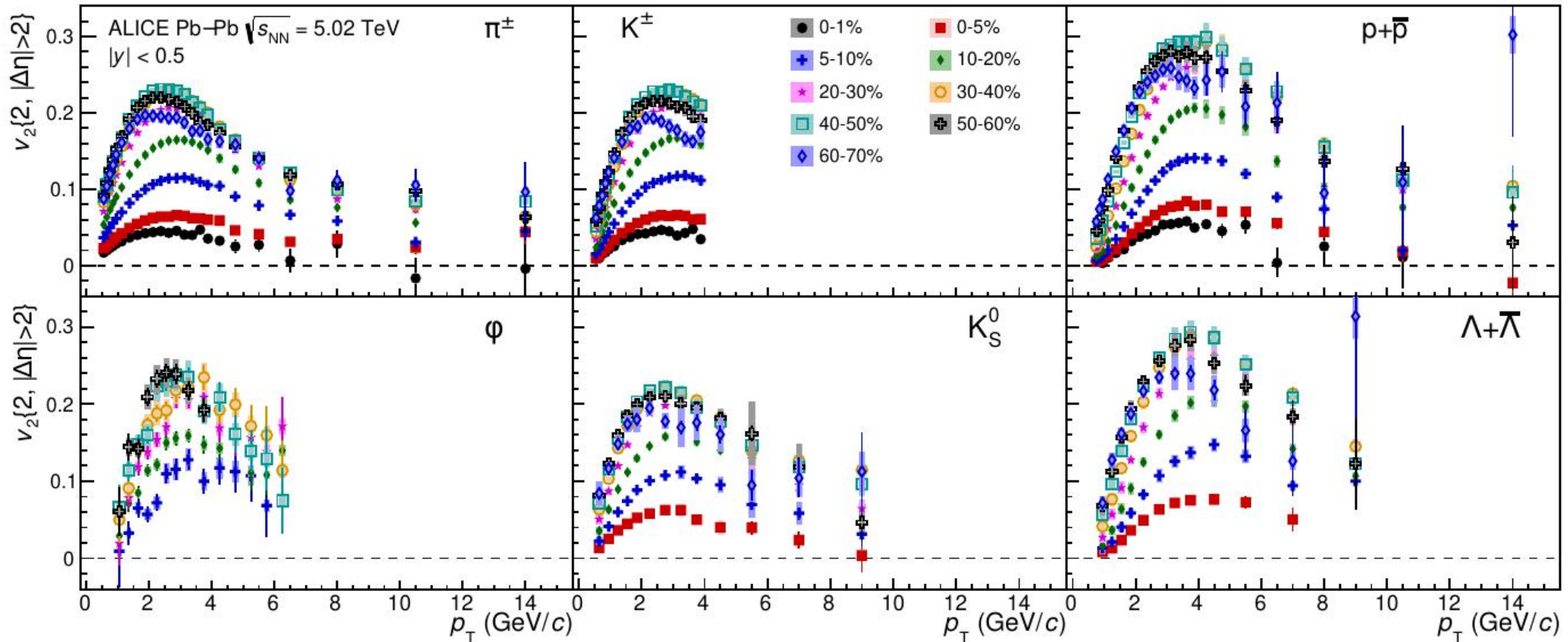
(Received 20 December 2013; revised manuscript received 6 May 2014; published 9 June 2014)



# PID $v_n$ : 'The basics': Pb-Pb collisions @ 5.02 TeV

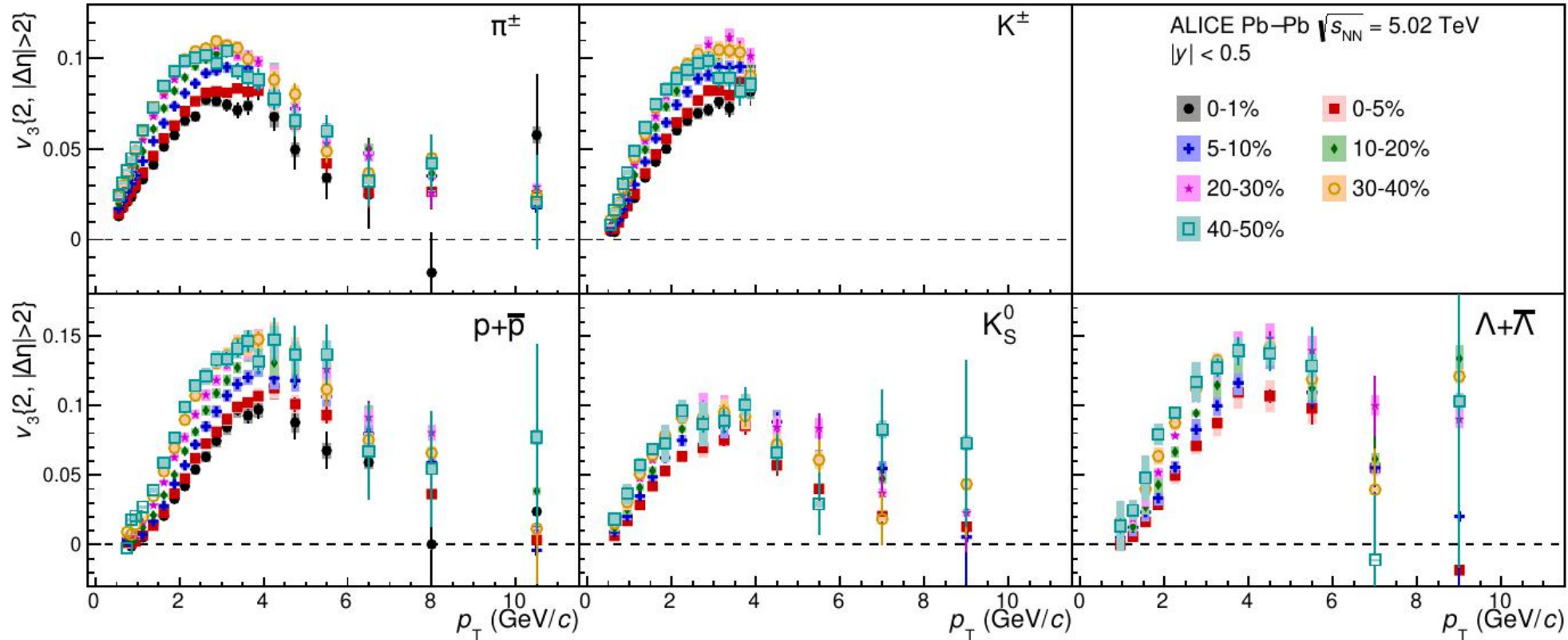
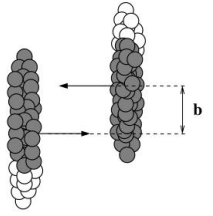
recent results from the ALICE collaboration - arXiv 1805.04390

# $V_2$ of identified particles @ 5.02 TeV



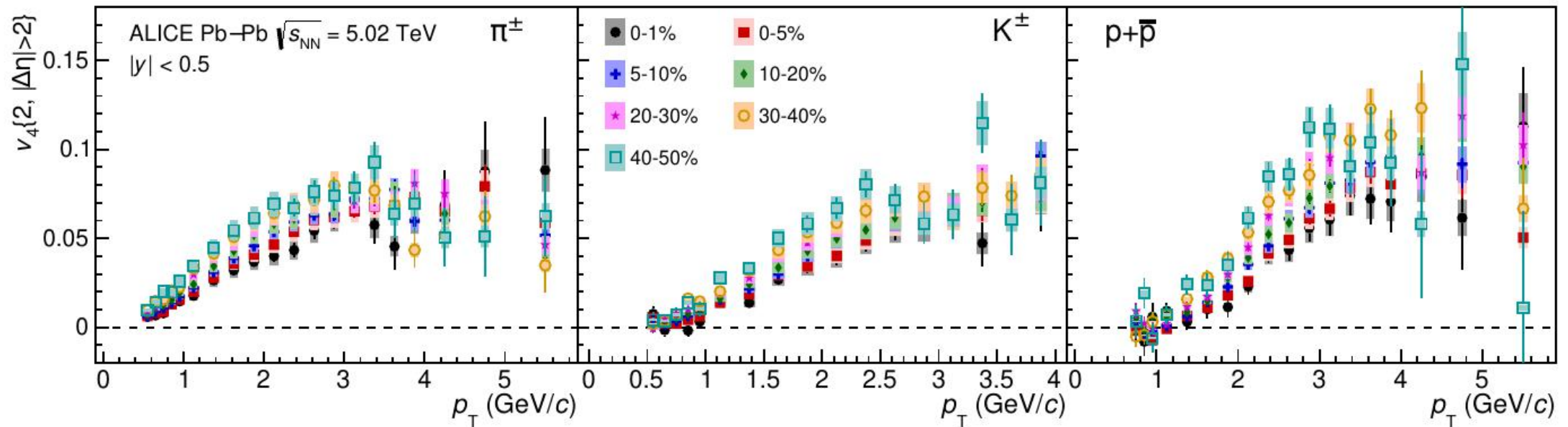
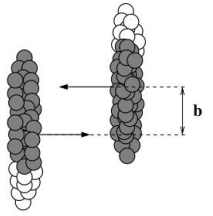
$v_2$  increases with centrality up to ~40-50% - linear scaling with eccentricity  
more peripheral: shorter system lifetime  
ultra-central (0-1%) positive  $v_2$  reflection of initial state inhomogeneities

# $V_3$ of identified particles @ 5.02 TeV



non-zero  $v_3$  up to  $\sim 8$  GeV/c, no centrality dependence  
 non-zero  $v_3$ : inhomogeneities in initial quark and gluon density  
 dampening of  $\eta/s$  more strongly reflected in  $v_3$  than  $v_2$

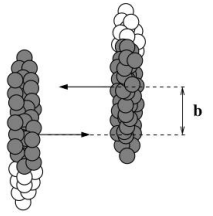
# $V_4$ of identified particles @ 5.02 TeV



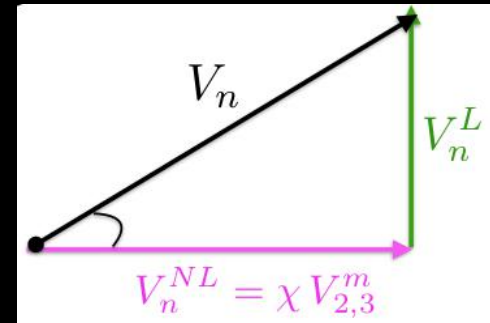
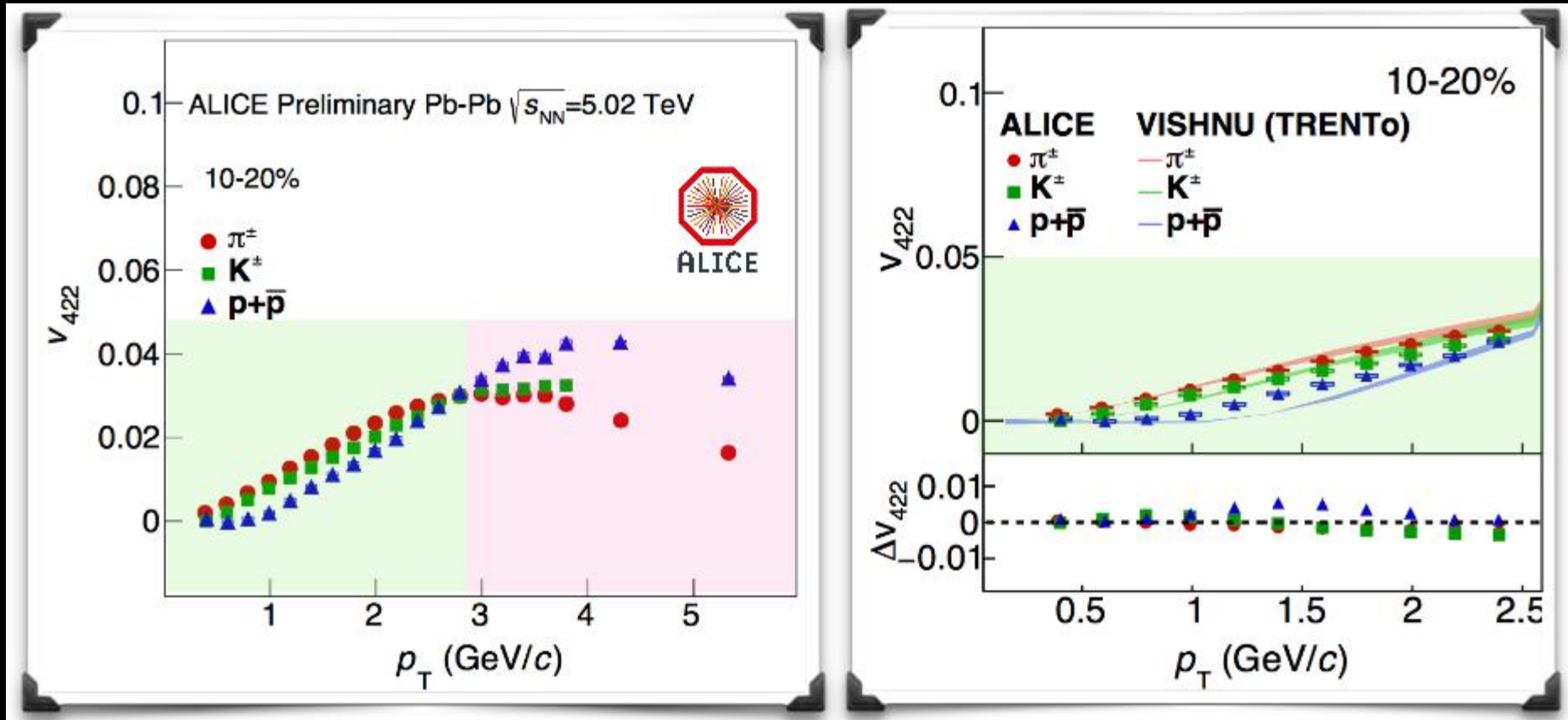
$v_4$ : a special harmonic  
generated by initial geometry but also fluctuations and non-linear response of the medium  
non-zero over full (albeit limited) momentum range for all species



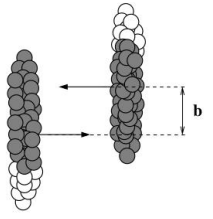
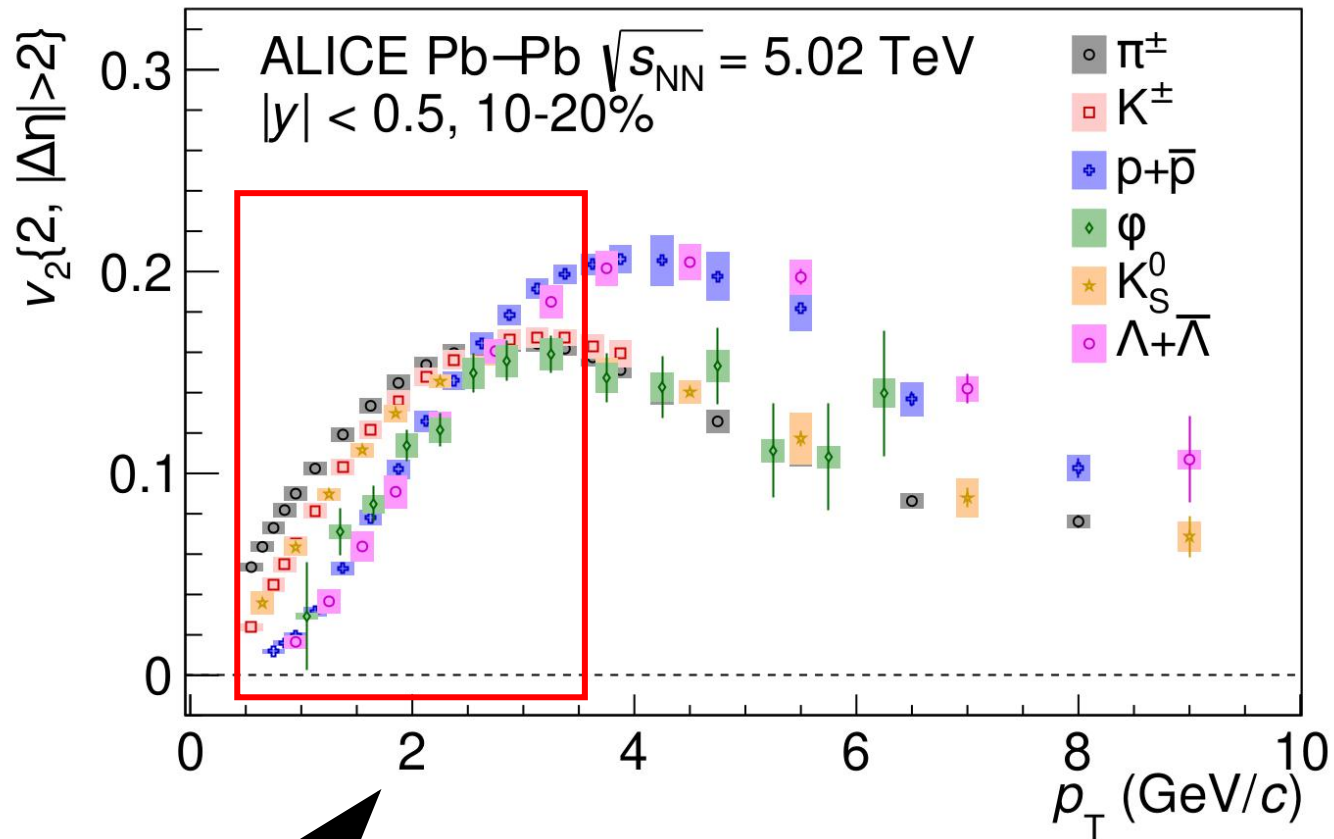
# $v_2$ of identified particles @ 5.02 TeV



non-linear flow modes:  
first measurements of  $v_{n,mk}(p_T)$  for identified particles



$$V_n = V_n^{NL} + V_n^L$$



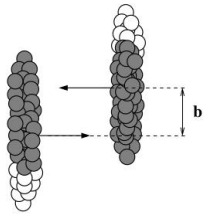
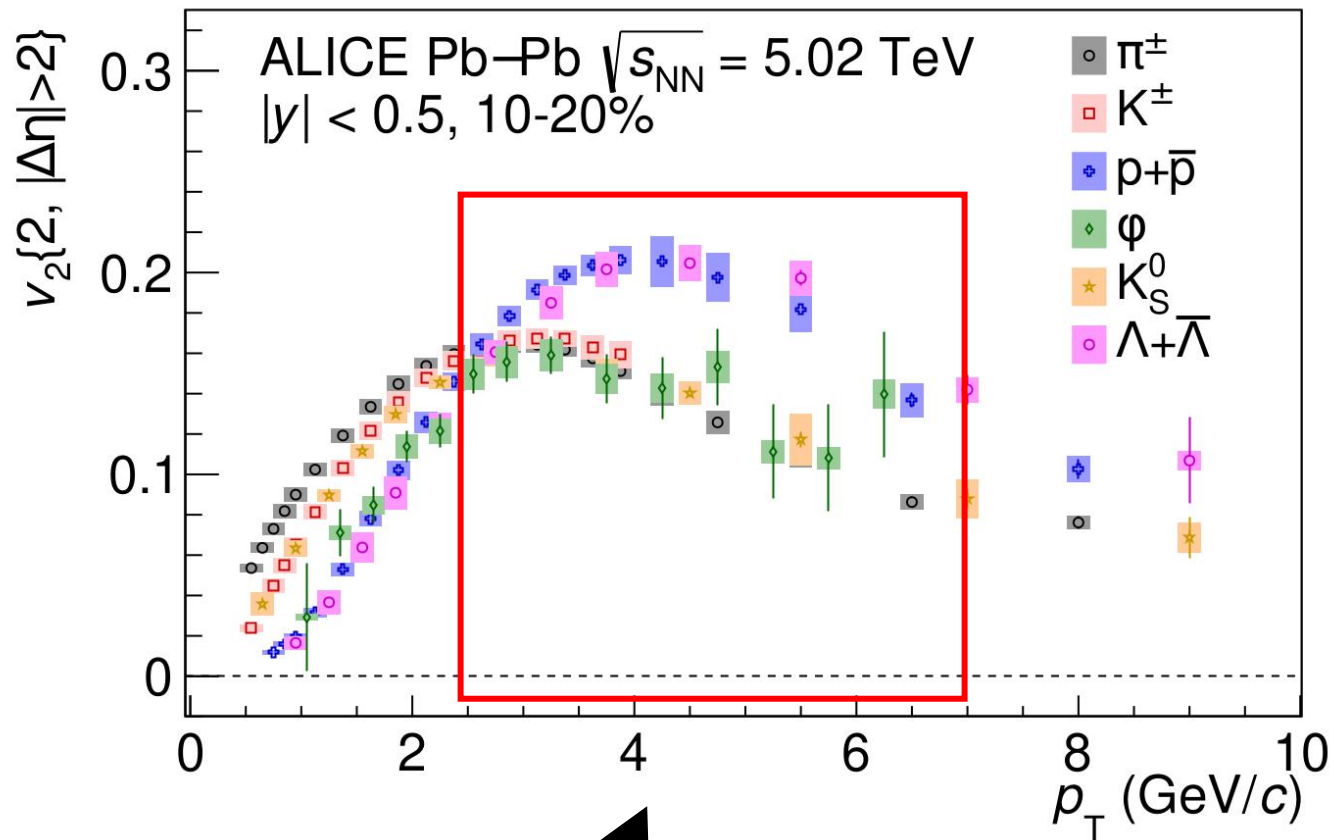
mass ordering from radial flow

$v_n$  are sensitive to the **full evolution** of the collision system

- Initial conditions  $\rightarrow$  QGP phase  $\rightarrow$  hadronization

Three kinematic regions of interest

- Low  $p_T$  ( $\lesssim 2$  GeV/c) - **hydrodynamic** expansion
- Intermediate  $p_T$  ( $2 \lesssim p_T \lesssim 7$  GeV/c) - quark **scaling** ?
- High  $p_T$  ( $\gtrsim 7$  GeV/c) - parton **energy loss**



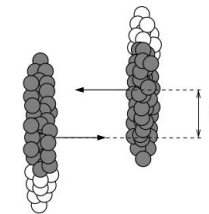
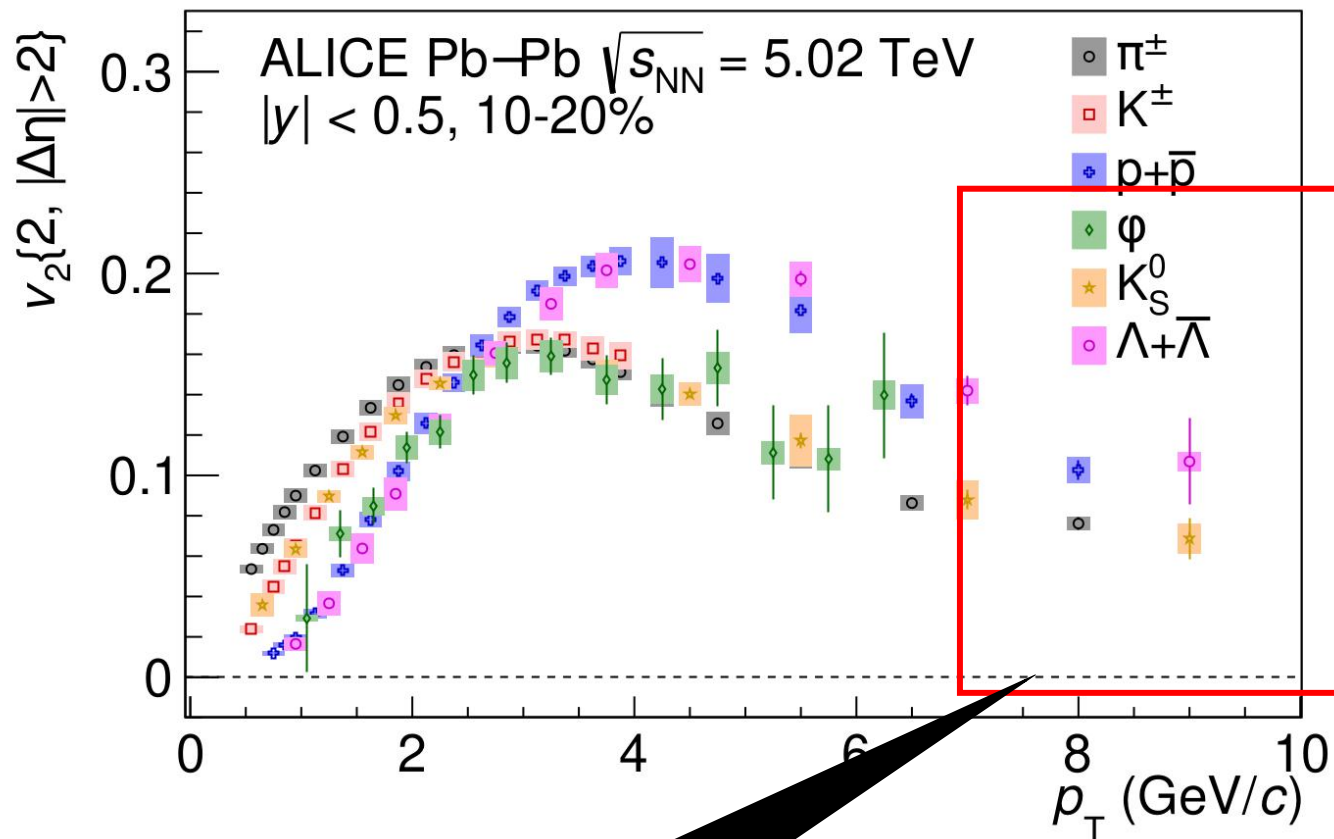
baryon / meson splitting  
 quark coalescence ?

$v_n$  are sensitive to the **full evolution** of the collision system

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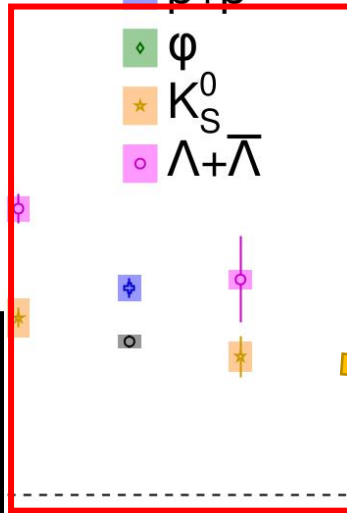
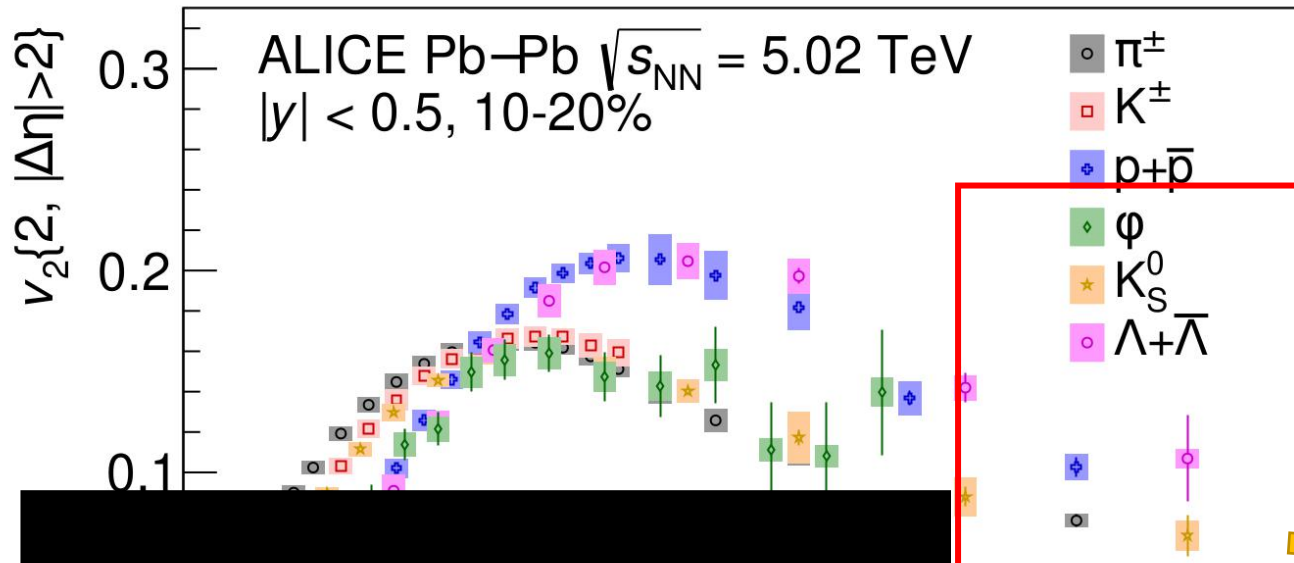
jet quenching

$V_n$  are sensitive to the **full evolution** of the collision system

- Initial conditions  $\rightarrow$  QGP phase  $\rightarrow$  hadronization

Three kinematic regions of interest

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- Intermediate  $p_T$  ( $2 \lesssim p_T \lesssim 7$  GeV/c) - quark **scaling** ?
- High  $p_T$  ( $\gtrsim 7$  GeV/c) - parton **energy loss**



$$R_{AA} = \frac{d^2 N^{AA} / dp_T d\eta}{\langle T_{AA} \rangle \cdot d^2 \sigma_{pp} / dp_T d\eta}$$

$$\approx \frac{\text{QCD in medium}}{\text{QCD in vacuum}}$$

$R_{AA}$ 's and  $v_2$  differ up to  $p_T \sim 10$  GeV, then converge

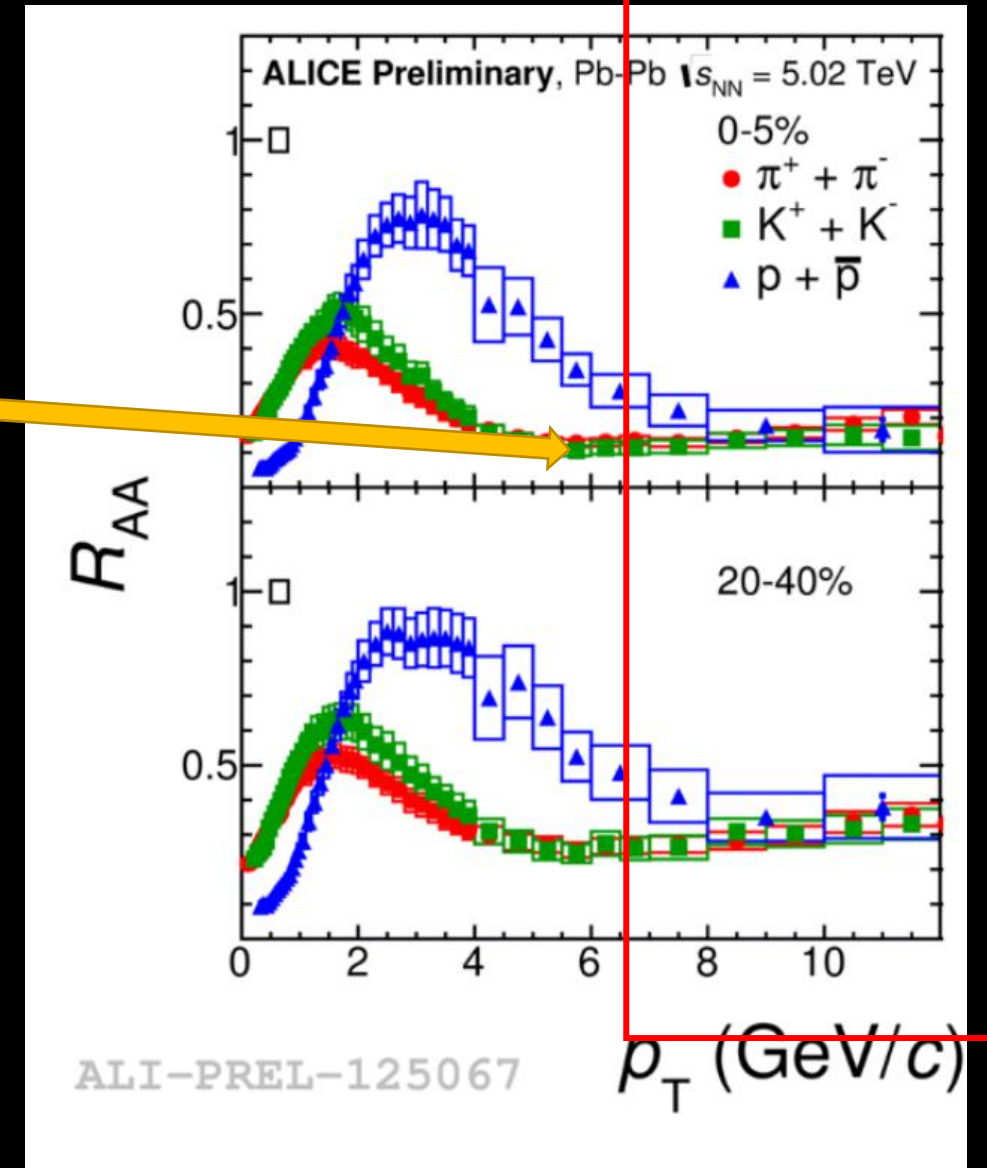
energy loss 'species blind': incurred prior to hadronization

$p_T$  (GeV/c)

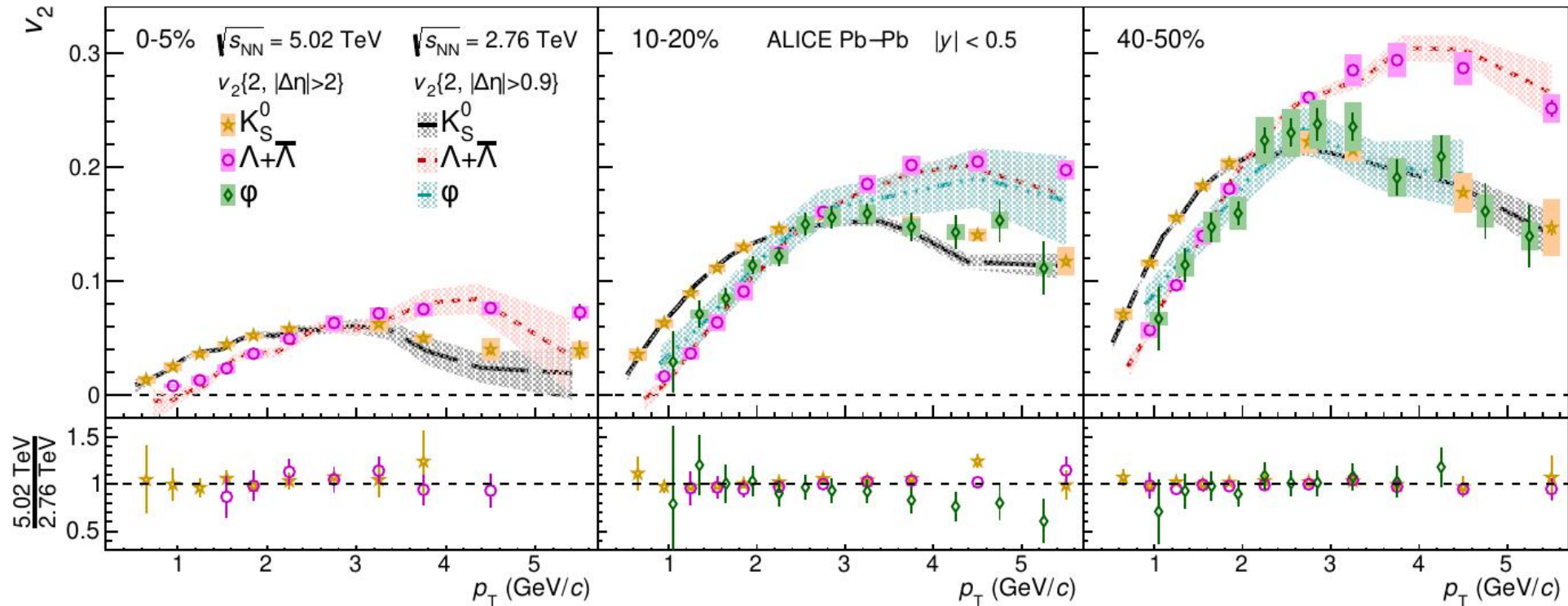
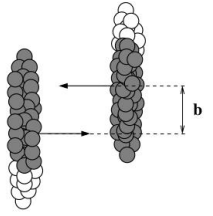
$V_n$  are sensitive to initial conditions

Three kinematic regions

- Low  $p_T$
- Intermediate  $p_T$
- High  $p_T$

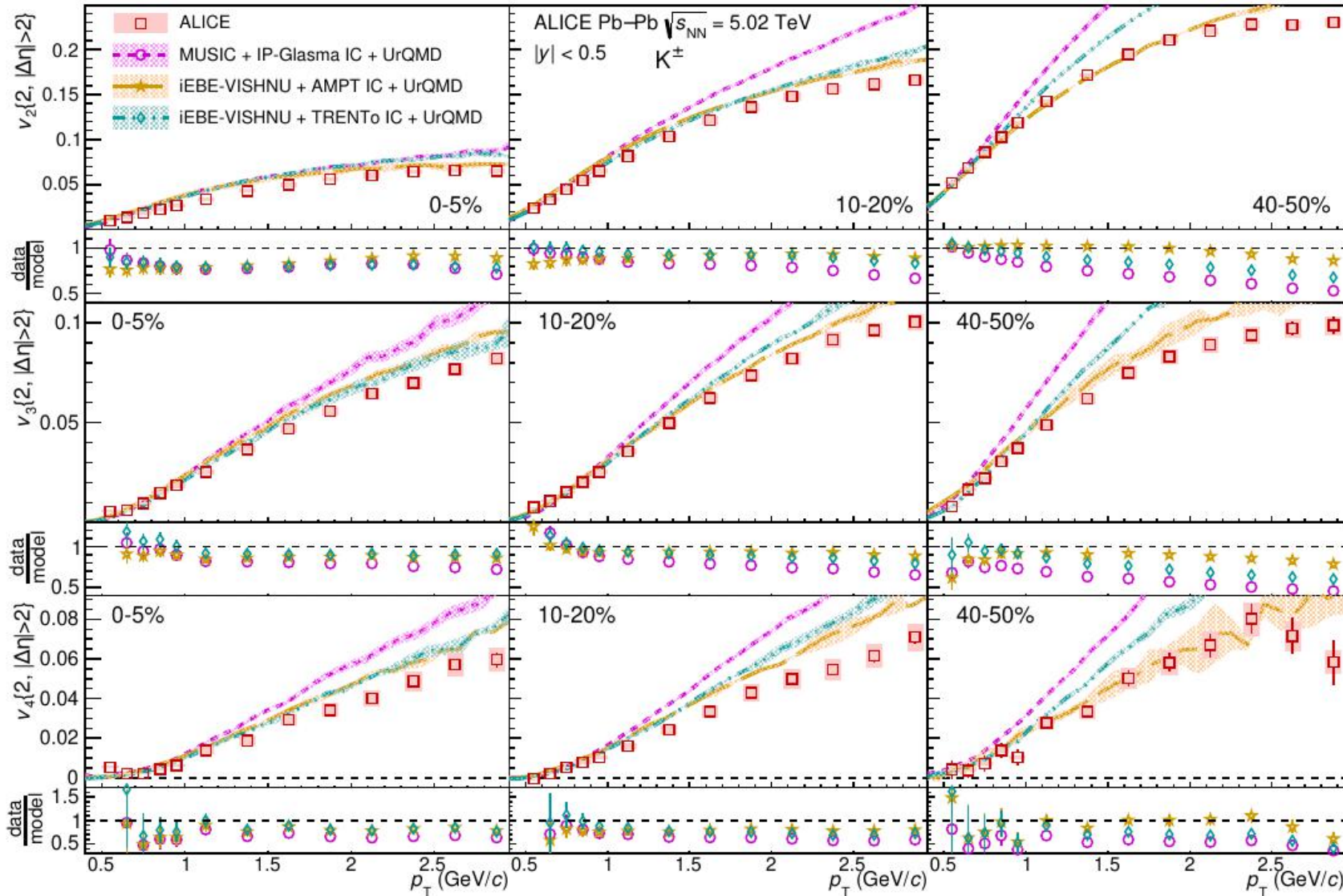
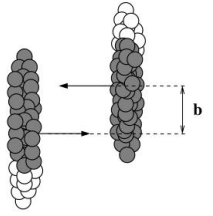


# Collision energy dependence of $v_n$



does a **higher center-of-mass energy** lead to a **larger radial flow**?  
 hypothesis:  $v_n$  of heavier particles suppressed at low  $p_T$  for higher collision energy  
**not possible to resolve**: precision gain mostly at high  $p_T$  - solves ' $\phi$  puzzle' though

# What do we learn from this ?



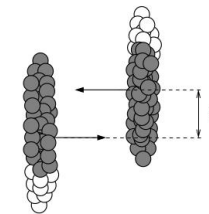
Novel constraints via model comparisons

- 1) MUSIC hydro, IP-Glasma initial state
- 2) iEBE-VISHNU using AMPT initial conditions
- 3) iEBE-VISHNU using TrENTo initial conditions

> Good agreement for **2)** for  $\pi$ ,  $p$ ,  $K$   $v_n$  ( $v_3$  and  $v_4$  in paper)  
 > Comparison to MUSIC suggests bulk viscosity plays limited role ?

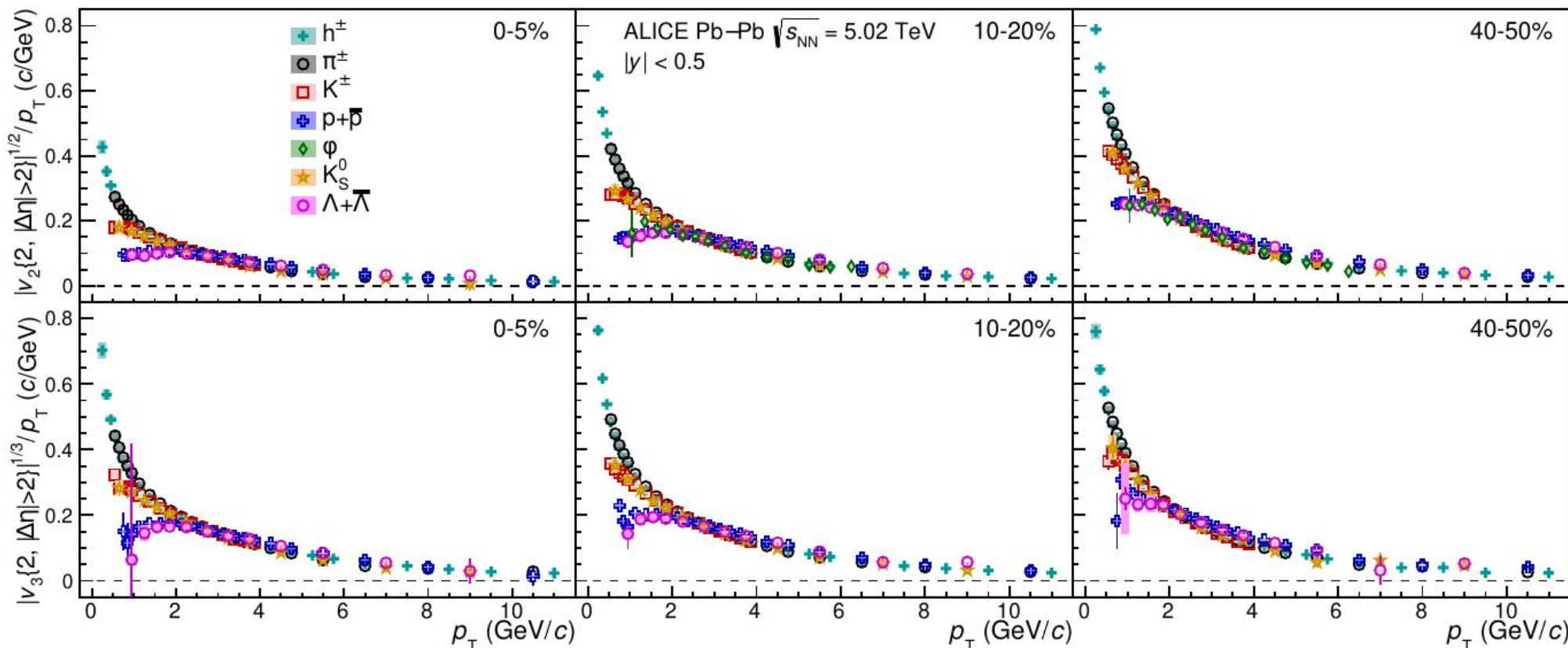
**Strong feeddown?  
 Contaminations? Methods?**

# A purely hydrodynamical system ?



PLB477 51-58 'in ideal hydrodynamics,  $v_n \sim p_T^n$  up to  $p_T \sim M$  for particles with mass  $M$ '

$v_2$

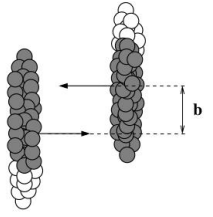


$v_3$

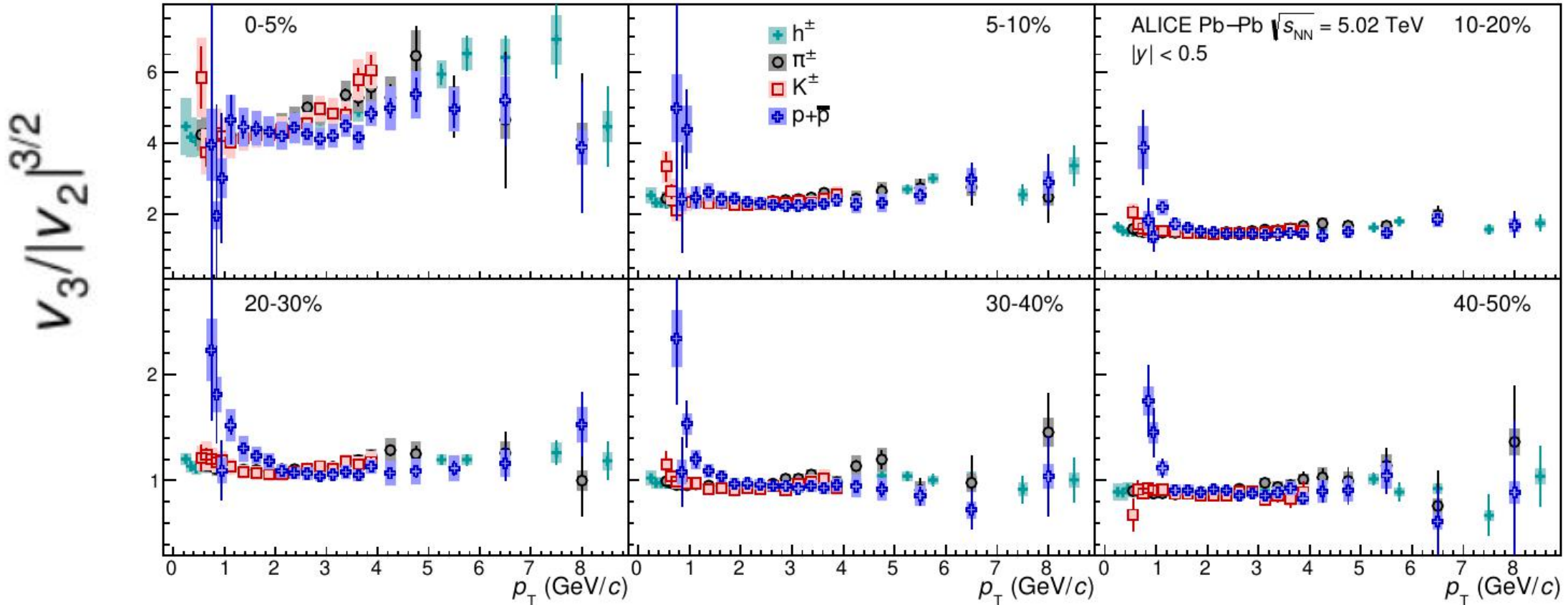
Idea:  $v_n \sim p_T^n$  so,  $|v_n|^{1/n} / p_T$  should be **constant**  
Only holds at very low momenta - pure hydro limit ?



# A purely hydrodynamical system ?

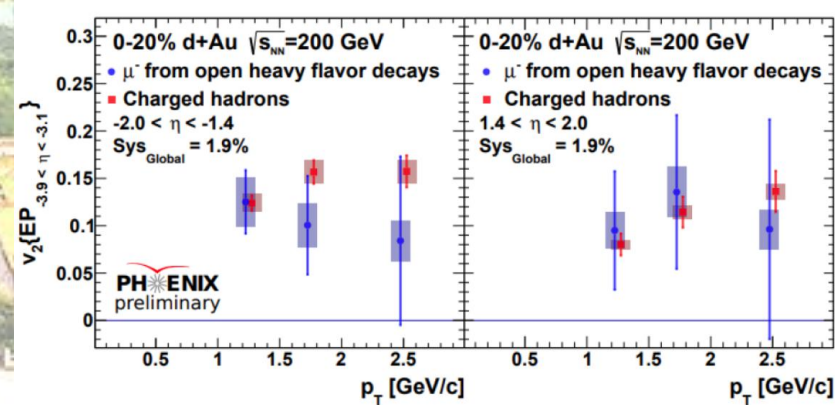
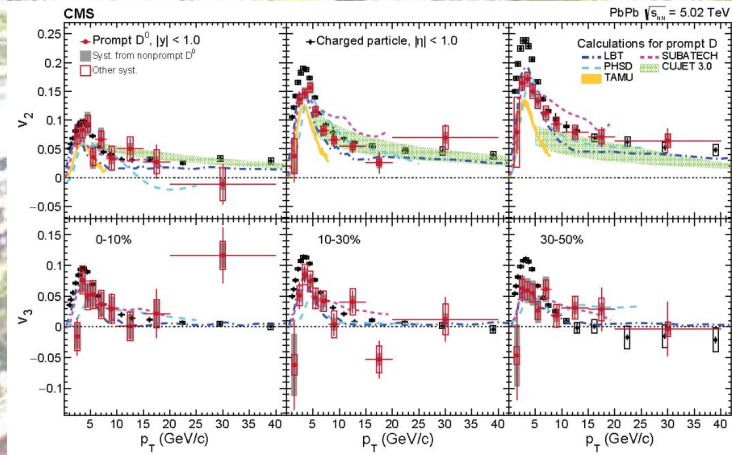


Taking it further: if  $v_n \sim p_T^n$ ,  $v_n / |v_m|^{n/m}$  is constant'



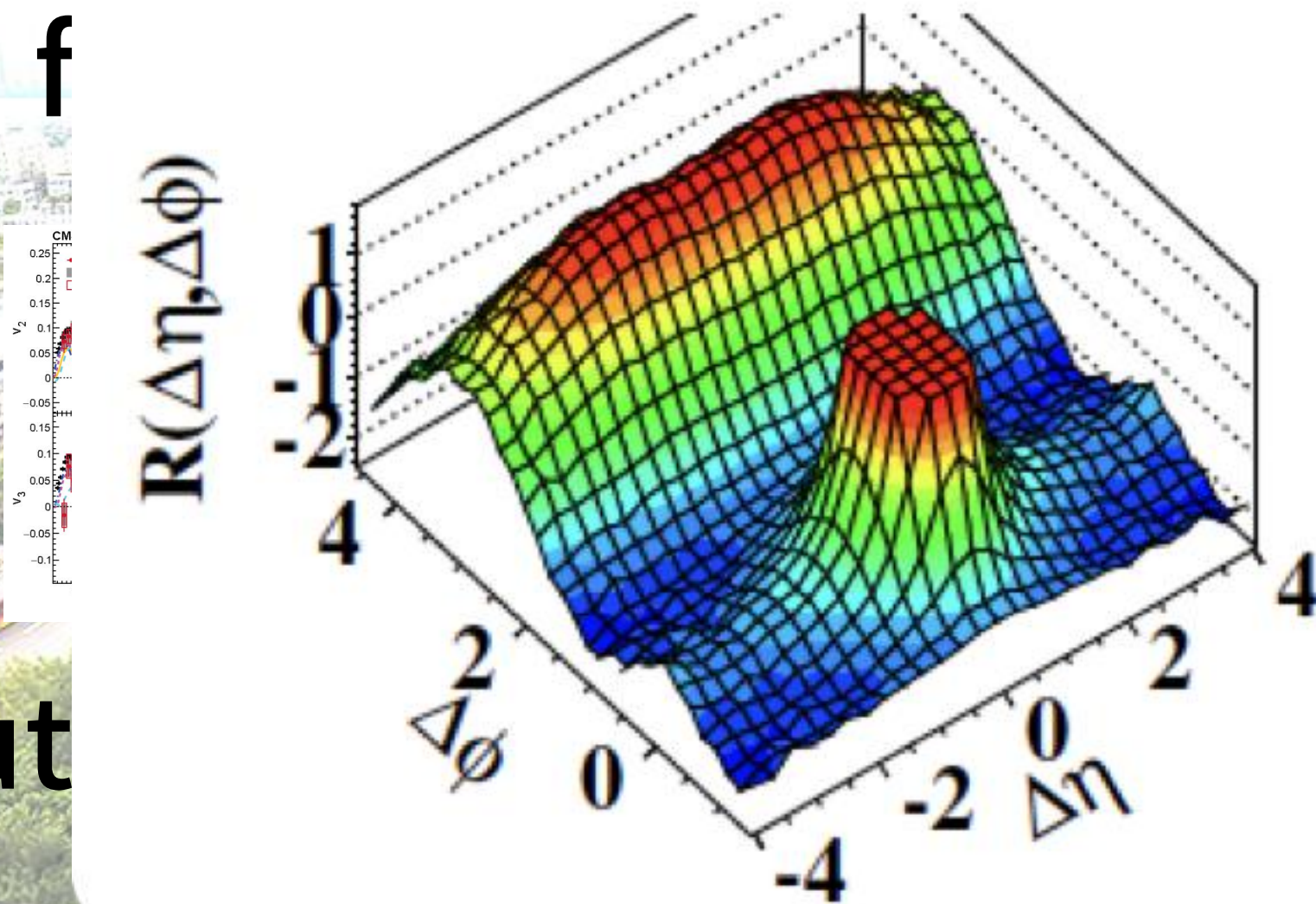
no obvious  $p_T$  dependence for charged hadrons for > 5% centrality  
 cenral collisions: deviations because of fluctuating initial geometry?  
 proton band not constant at low  $p_T$ : signature of radial flow ?

# so far the 'conventional' part



# but what about small systems ?

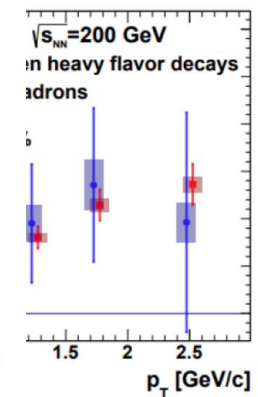
(d) CMS  $N \geq 110$ ,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



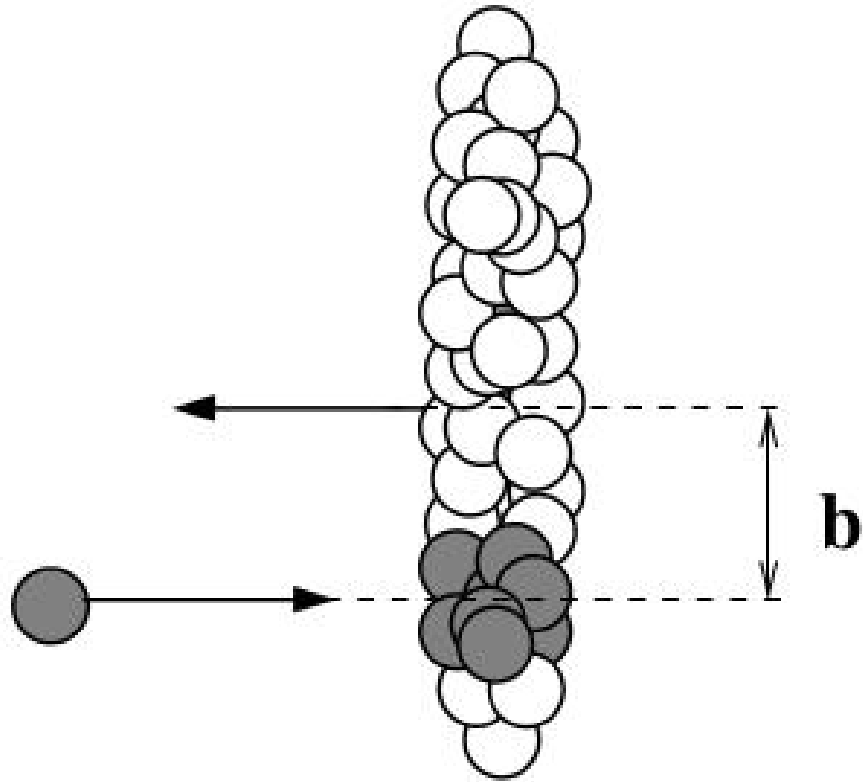
so f

but

part

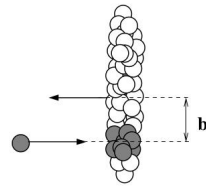


systems ?

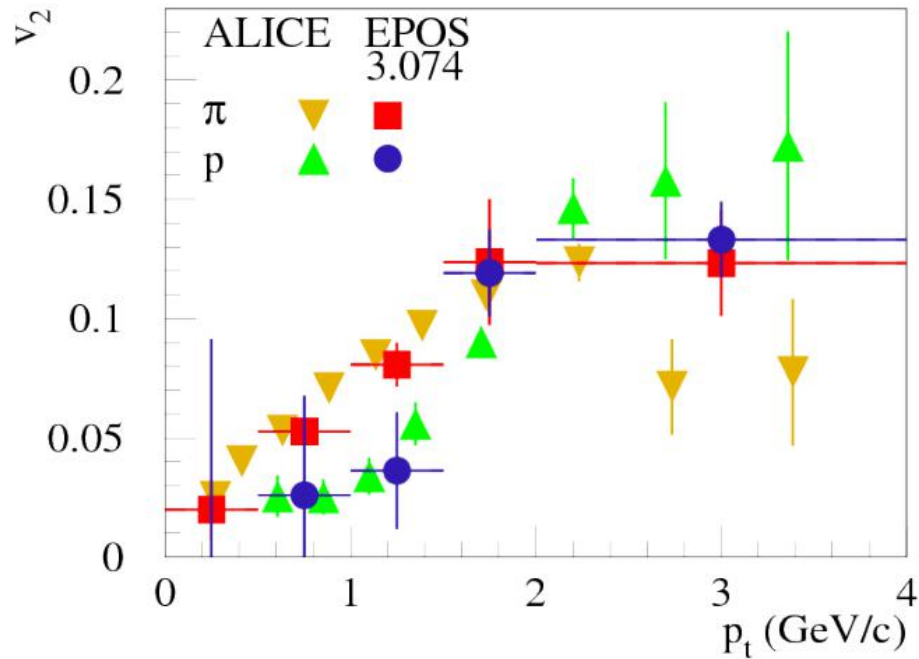


# Run II @ the LHC, PID flow

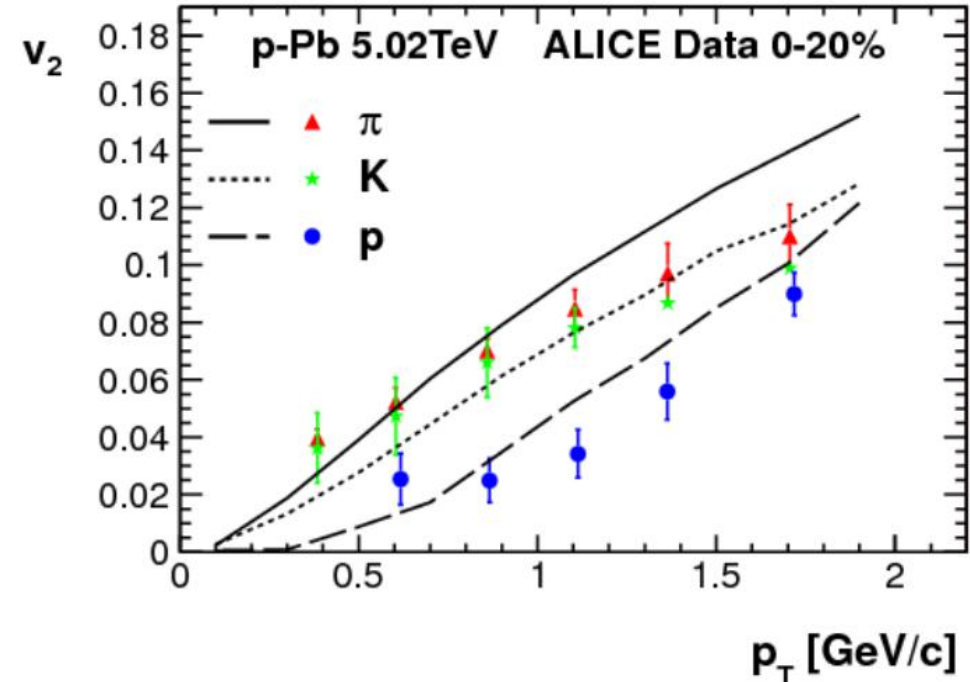
# Starting off ... what to expect ?



[Werner et al., PRL 112 (2014) no. 23]

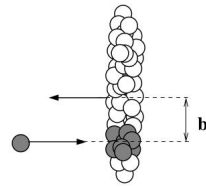


[Bozek et al., PRL 111 (2013) 172303]



mass splitting: evidence of long-range collectivity in p-Pb collisions?  
**small** experimental uncertainties crucial for model validation

# Starting off ... what to expect ?



## Initial state effects → “CGC picture”

- Target and projectiles described as dense coloured objects
- Anisotropy induced by scattering off domains of e-by-e fluctuating color charged fields (classical YM equations)

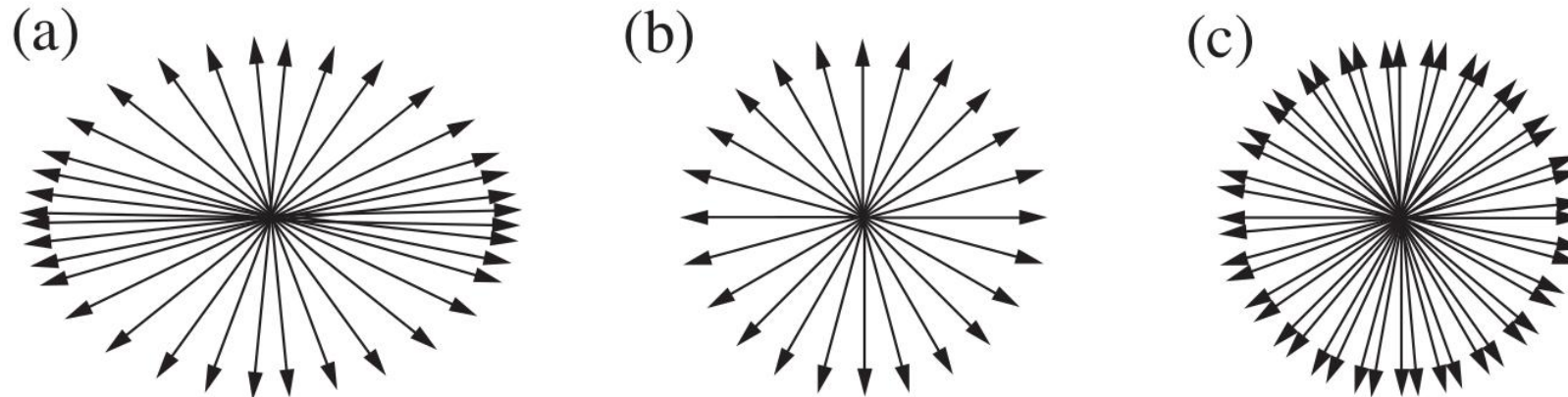
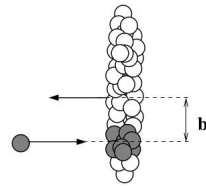
**Particles are produced from initial state non-homogeneous momentum-space distribution**

## Final state effects → “hydrodynamical picture”

- $\lambda_{\text{mfp}} \ll$  system size,  $K_n \ll 1$  (Knudsen number → ratio of micro to macroscopic scales e.g. relaxation time  $\lambda_{\text{mfp}} \sim v$  vs inverse of expansion rate)
- Conversion of structures/correlations in coordinate space into structures/correlations in momentum space

**Applicability of hydro: particles get their momentum-space correlations from final state interactions during the evolution of the system**

# Non-flow: an ilusive intruder



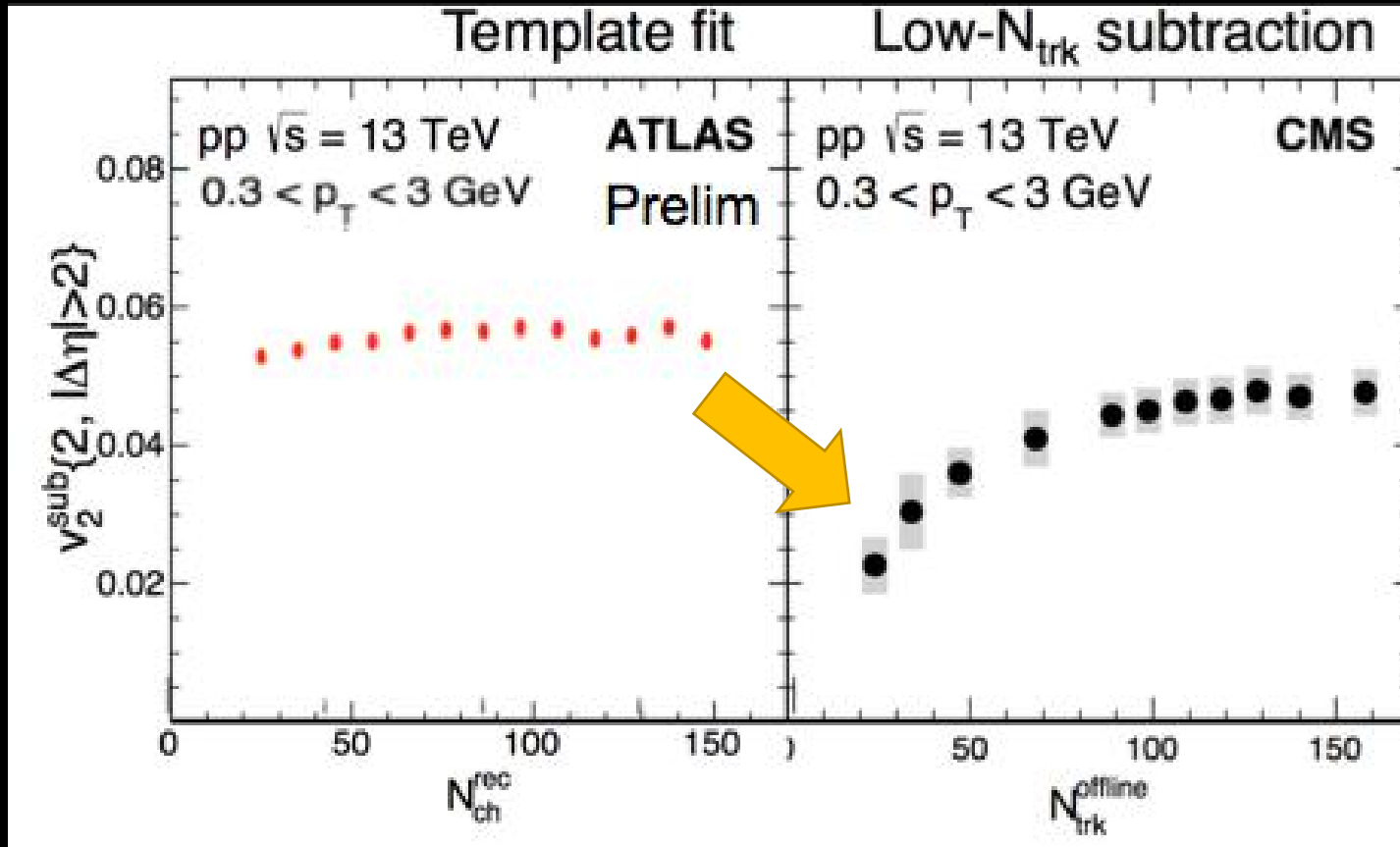
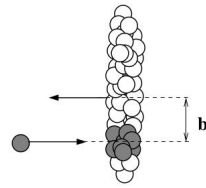
Template fitting → 'ATLAS method'

- Subtract the low multiplicity class **including** low multiplicity "pedestal"
- Assumes that the low multiplicity class has **residual "flow"**

"Peripheral" subtraction method → 'CMS (and ALICE p-Pb) method'

- Subtract the low multiplicity class **not including** low multiplicity "pedestal"
- Assumes that the low multiplicity class has **no residual "flow"**

# Non-flow: an elusive intruder

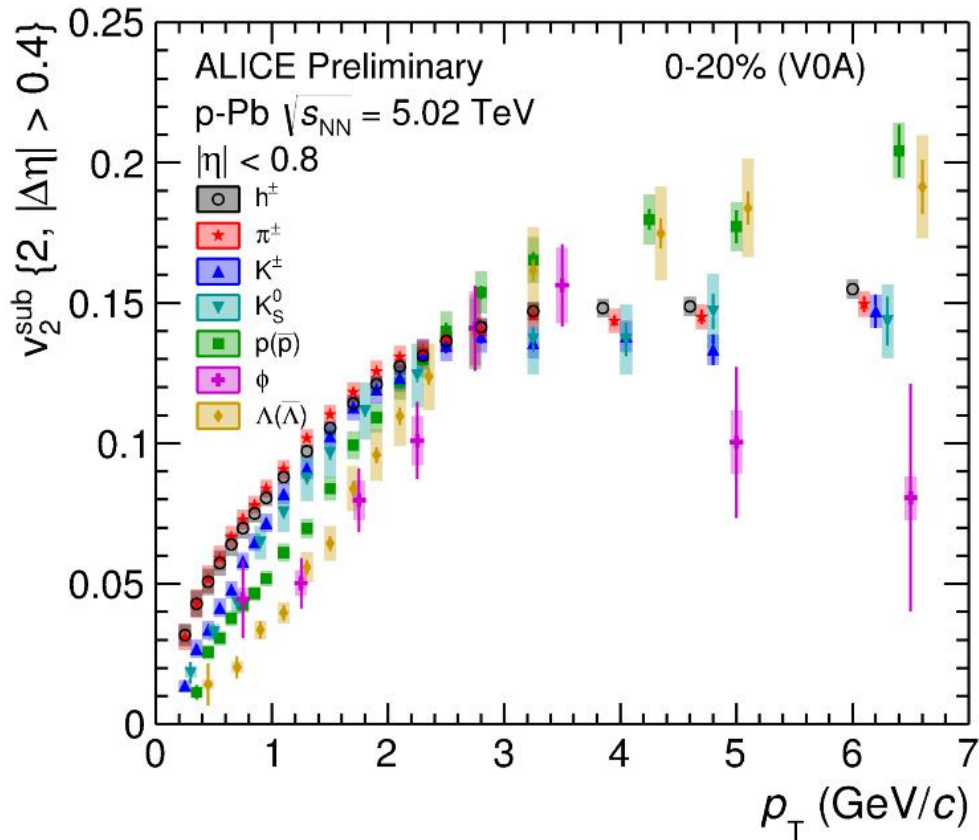
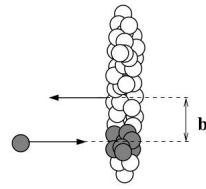


Template fit  
 Subtract  
 including  
 Assu  
 class

d → CMS (and LICE)  
 y class **not**  
 'pedestal'  
 multiplicity class



# PID $v_2$ in pPb collisions @ 5.02 TeV

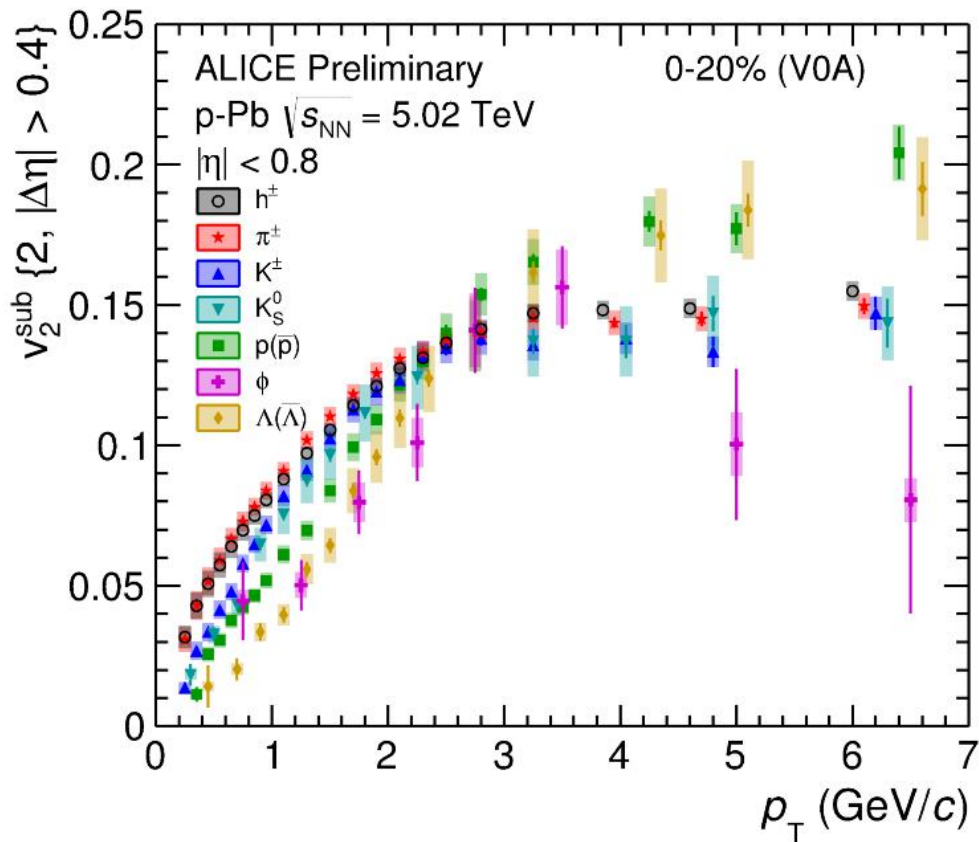
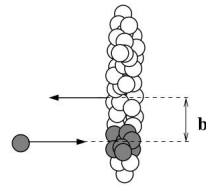


ALI-PREL-156487

- $v_2(p_T)$  of identified hadrons in 5.02 TeV p-Pb using Run II data
- Non-flow subtracted results using MB 13 TeV pp collisions
- First ALICE measurement of  $K_S^0$ ,  $\Lambda(\bar{\Lambda})$  and  $\phi$   $v_2$  in small systems
- Similar features as Pb-Pb measurements
  - Clear mass ordering (low  $p_T$  region)
  - Qualitatively predicted by hydrodynamic models
  - Indication of baryon/meson grouping (intermediate  $p_T$ )

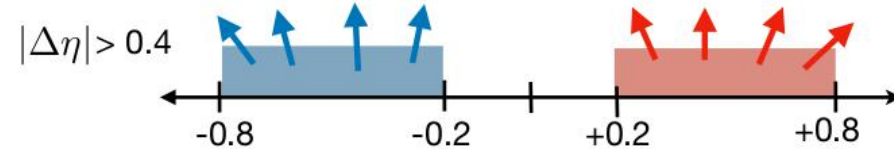
NB credit: V. Pacik, QM2018

# PID $v_2$ in pPb collisions @ 5.02 TeV



ALI-PREL-156487

Pseudorapidity separation partially suppresses short-range correlations



Additional non-flow subtraction performed on cumulants using MB pp collisions

$$v_2^{\text{pPb,sub}}(p_T) = \frac{d_2^{\text{pPb}}\{2\} - k \cdot d_2^{\text{pp}}\{2\}}{\sqrt{c_2^{\text{pPb}}\{2\} - k \cdot c_2^{\text{pp}}\{2\}}}$$

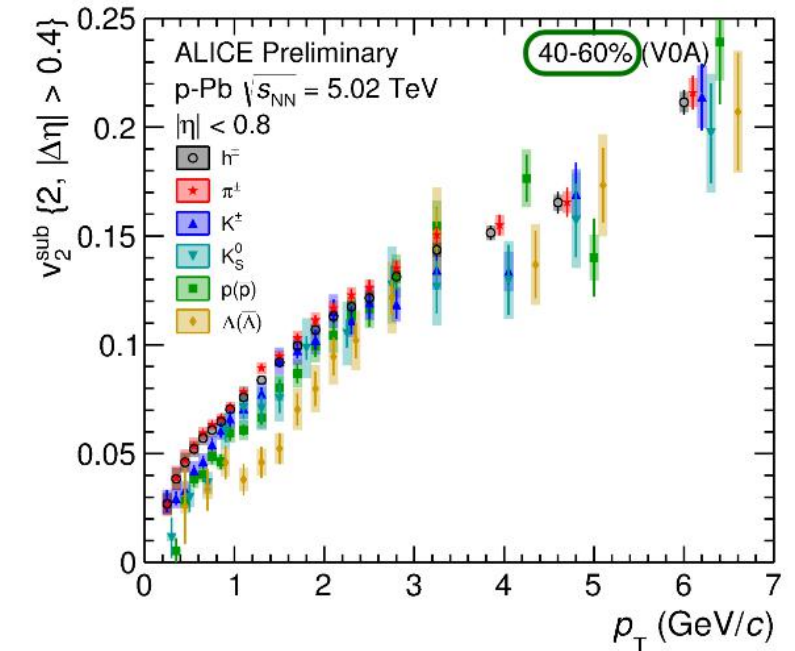
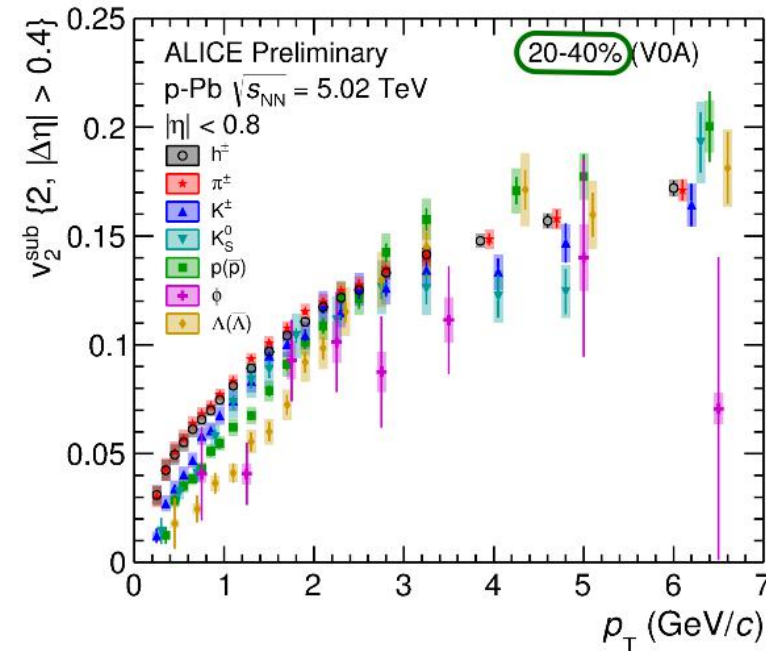
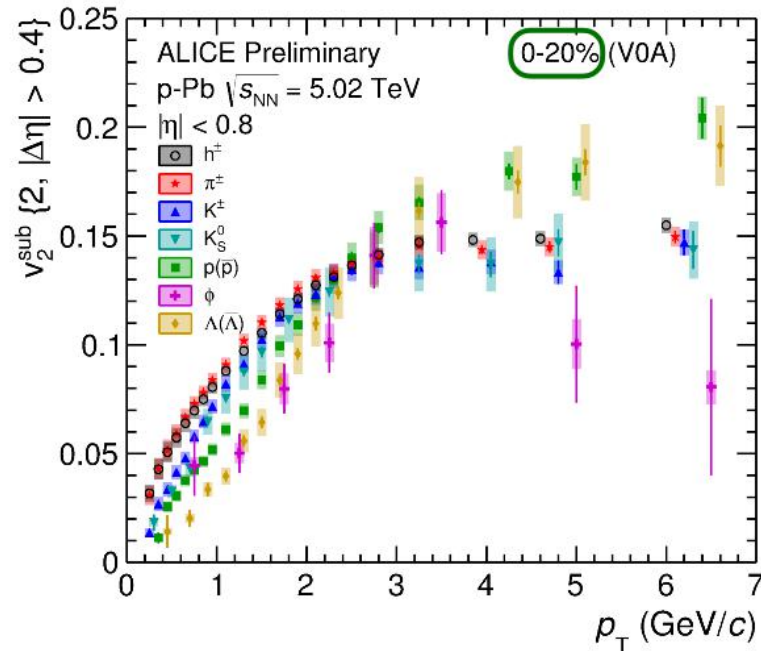
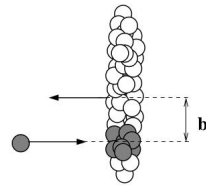
Contribution of non-flow scaled by mean event multiplicities

● Based on assumption for non-flow [Voloshin et al., arXiv:0809.2949]

$$\delta_n \propto \frac{1}{M} \quad \rightarrow \quad k = \frac{\langle M \rangle^{\text{pp}}}{\langle M \rangle^{\text{pPb}}}$$

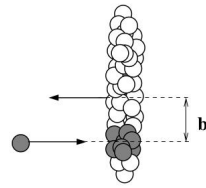
NB credit: V. Pacik, QM2018

# PID $v_2$ in pPb - multiplicity dependence

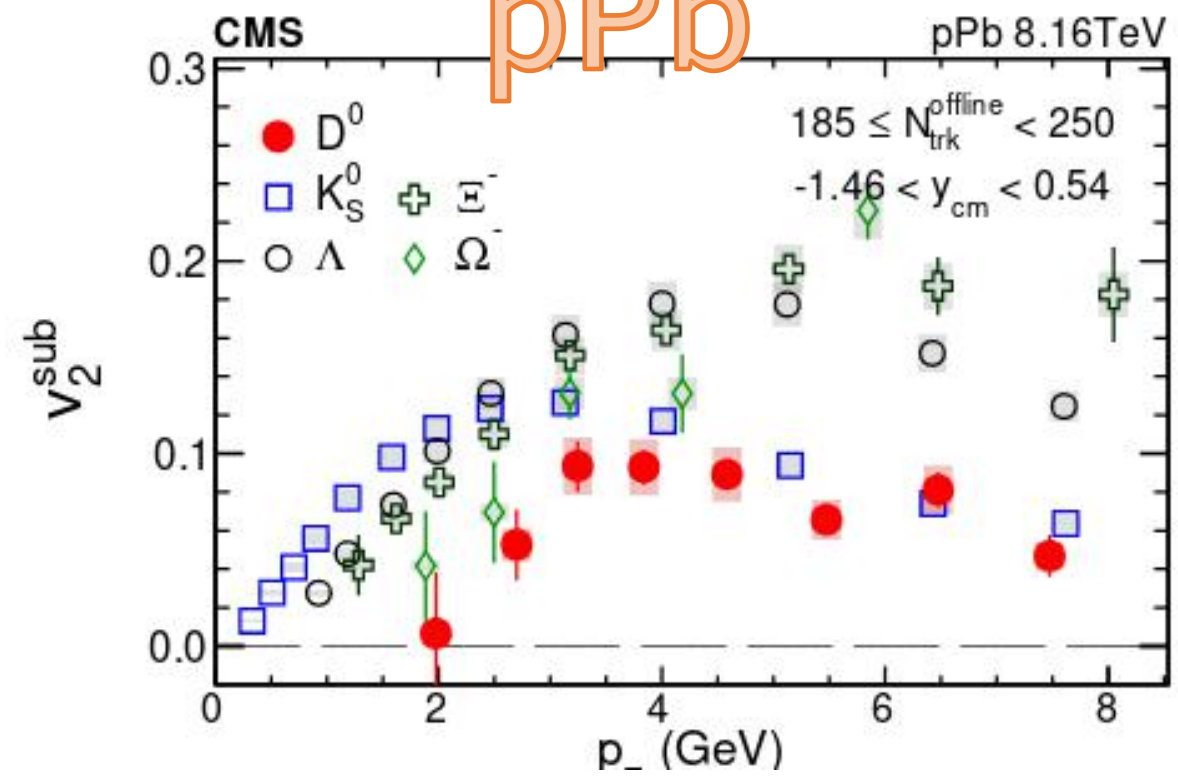


high multiplicity events - mass ordering (low  $p_T$ ) and baryon / meson splitting (high  $p_T$ )  
low multiplicity events - mass ordering persists, baryon / meson splitting vanishes

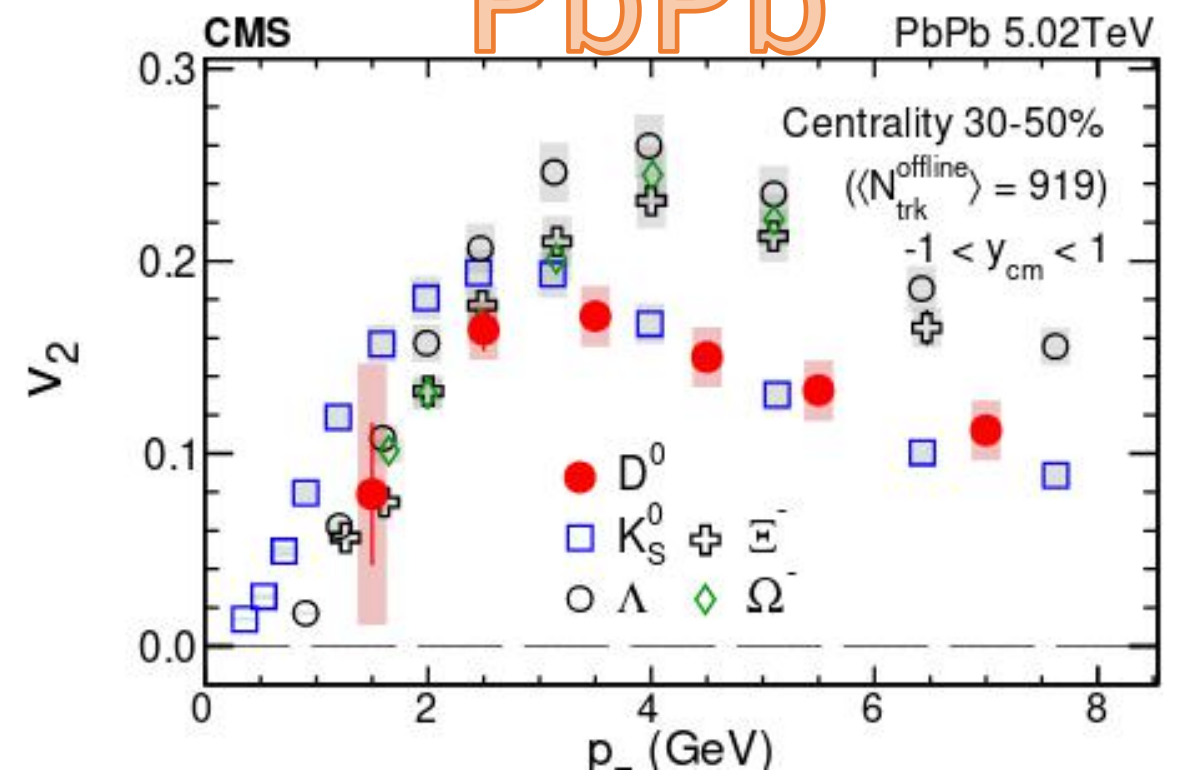
# Strange hadrons in pPb @ CMS



pPb

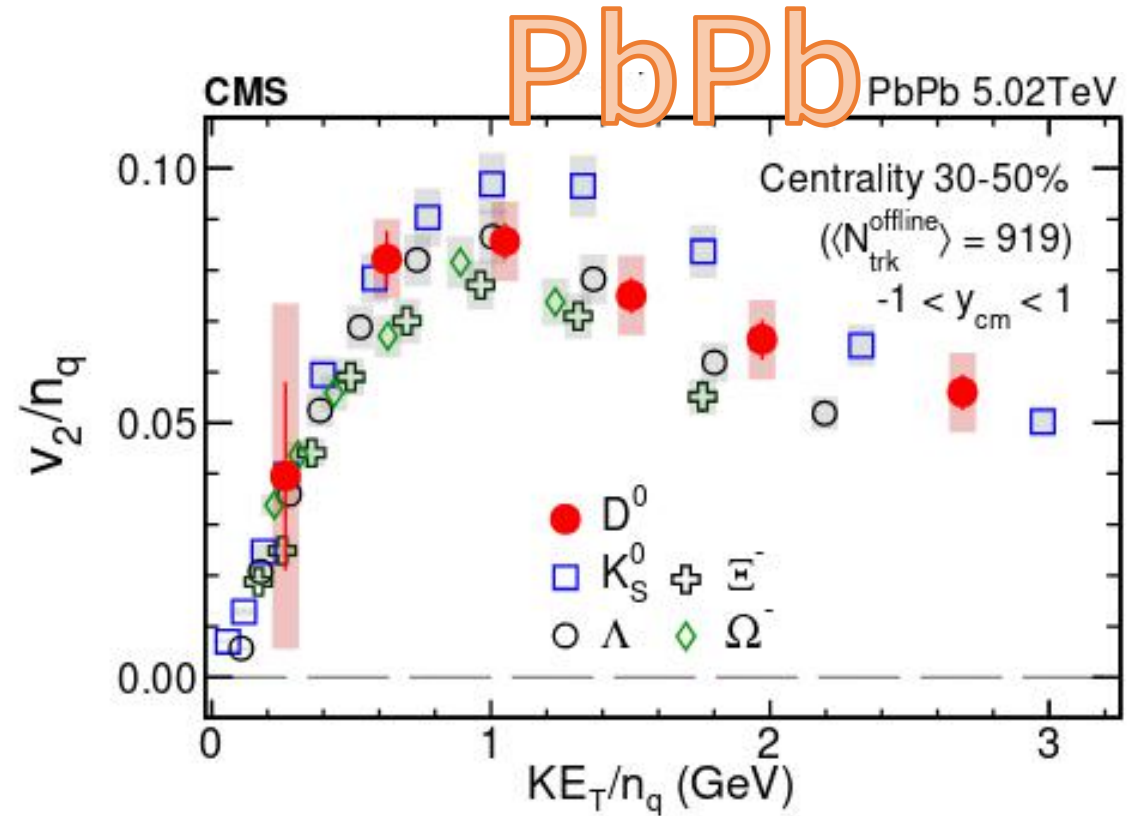
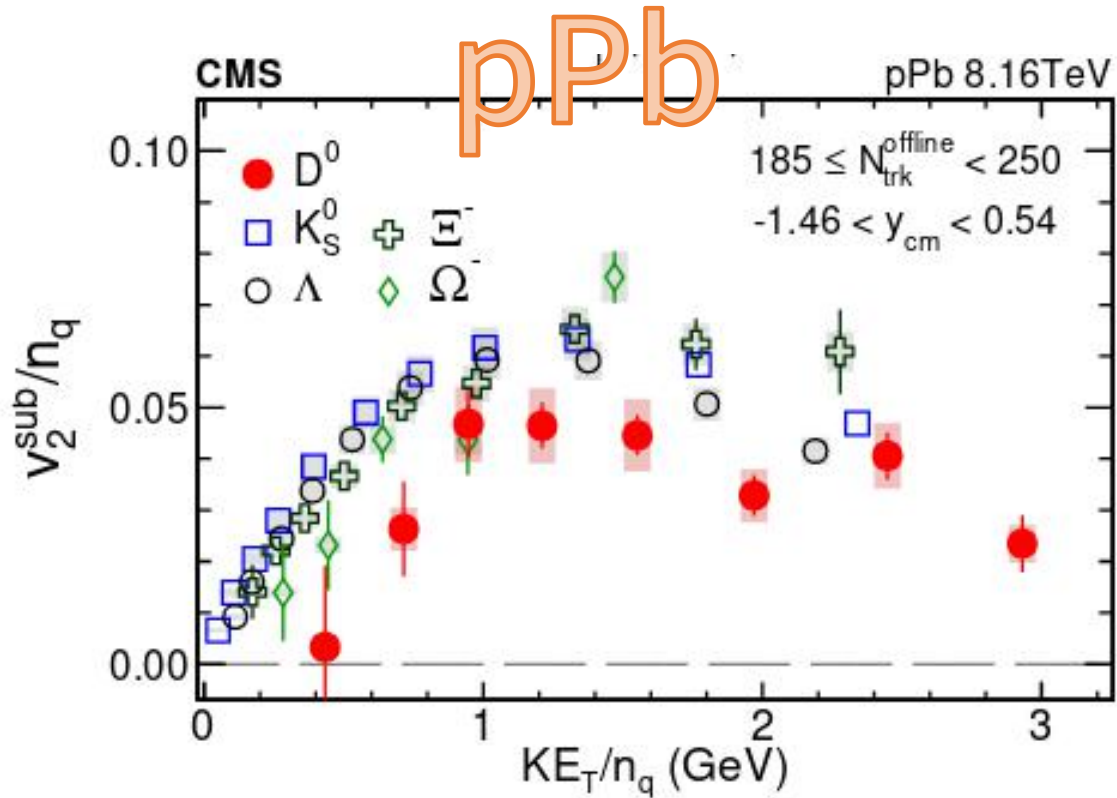
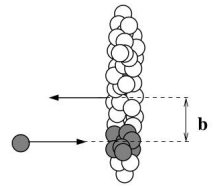


PbPb



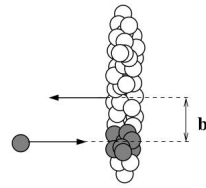
very high precision of  $K_S^0$  and  $\Lambda$   $v_2$   
 first observation of non-zero  $D^0$  meson  $v_2$  in pPb

# NCQ scaling @ CMS

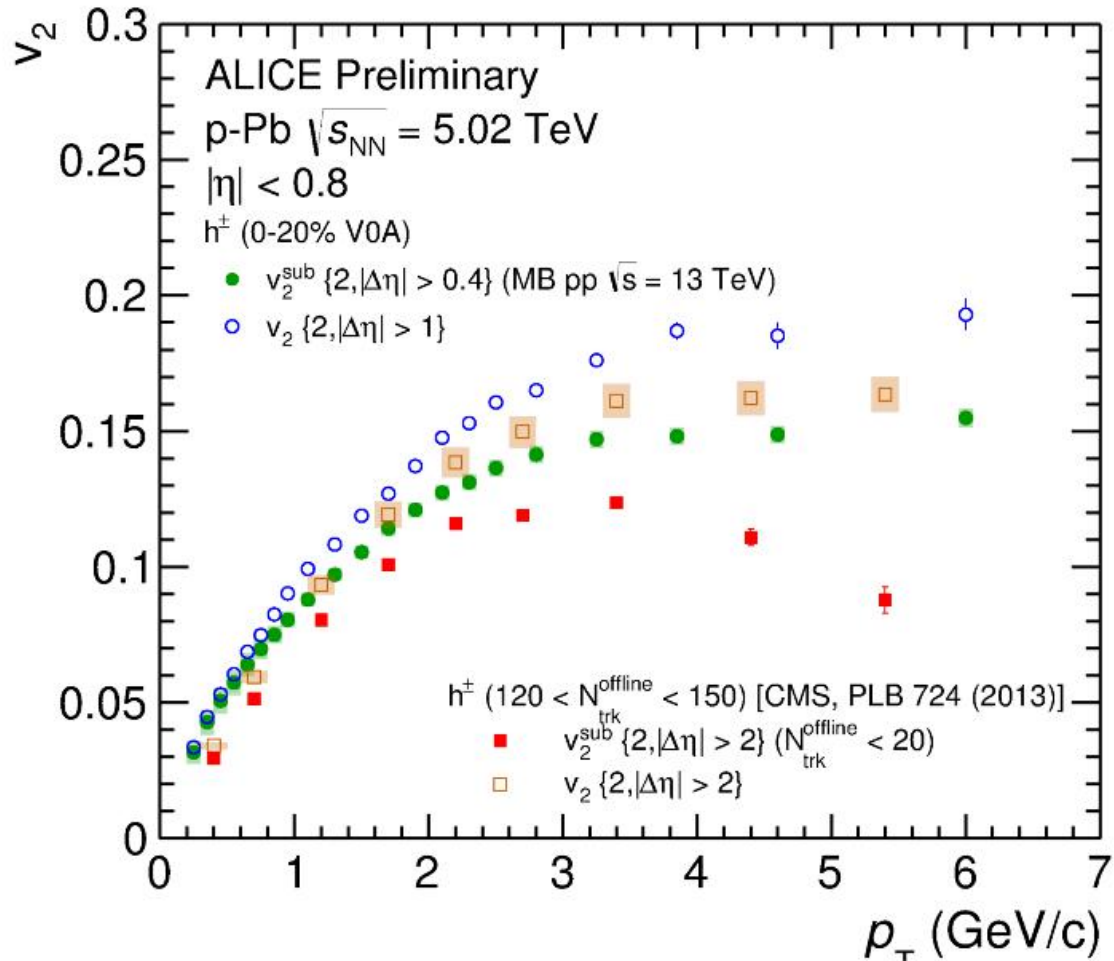


scaling test show that  $D^0$  meson might be less coupled to the medium in small systems

# Comparisons - devils & details



NB credit: V. Pacik, QM2018

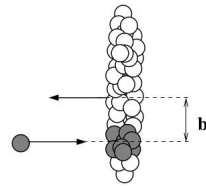


- Differences in methodology
- $v_2$  extraction (2PC vs Q-Cumulants)
- Event classification (selection)
- Pseudo-rapidity regions
- Similar non-flow subtraction prescription ...

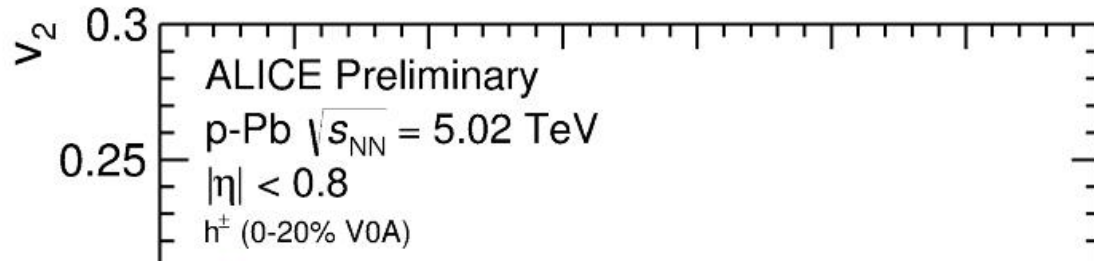
$$V_{n\Delta}^{\text{sub}} = V_{n\Delta} - V_{n\Delta}(N_{\text{trk}}^{\text{offline}} < 20) \times \frac{N_{\text{assoc}}(N_{\text{trk}}^{\text{offline}} < 20)}{N_{\text{assoc}}} \times \frac{Y_{\text{jet}}}{Y_{\text{jet}}(N_{\text{trk}}^{\text{offline}} < 20)}, \quad (9)$$

- ... but additional scaling factor

# Comparisons - devils & details



NB credit: V. Pacik, QM2018



- Differences in methodology
- $v_2$  extraction (2PC vs Q-Cumulants)
- Event classification (selection)

again repeating a fundamental problem of correlation measurements in small systems

⋮

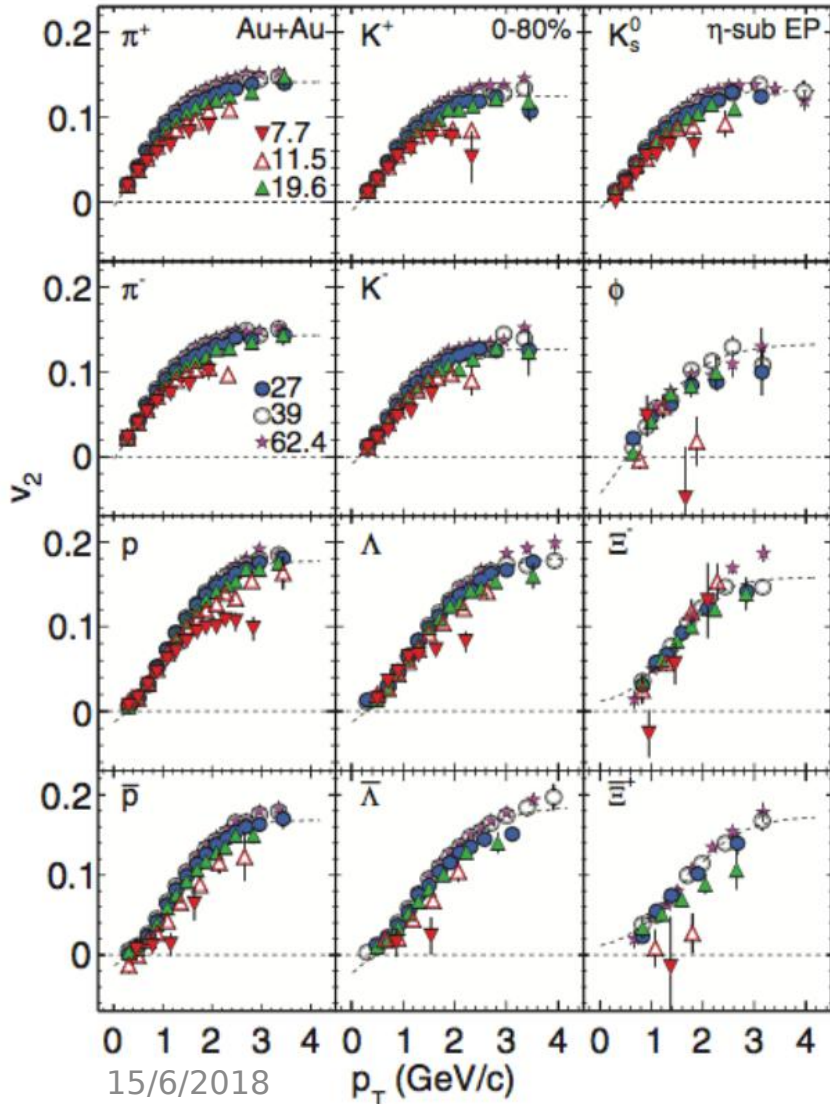
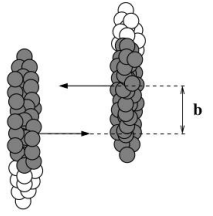
**for a meaningful inter experimental / theoretical definition, we need to have a clear, experimental definition of our observables !**

An aerial photograph of a city, likely in East Asia, featuring traditional Chinese architecture with yellow-tiled roofs and ornate structures. The foreground shows a large, curved stone bridge or walkway leading towards a central plaza with two prominent pavilions. The background shows a dense urban area and a large body of water, possibly a bay or river, under a clear sky.

**if time permits ... the LHC  
doesn't tell the full story**

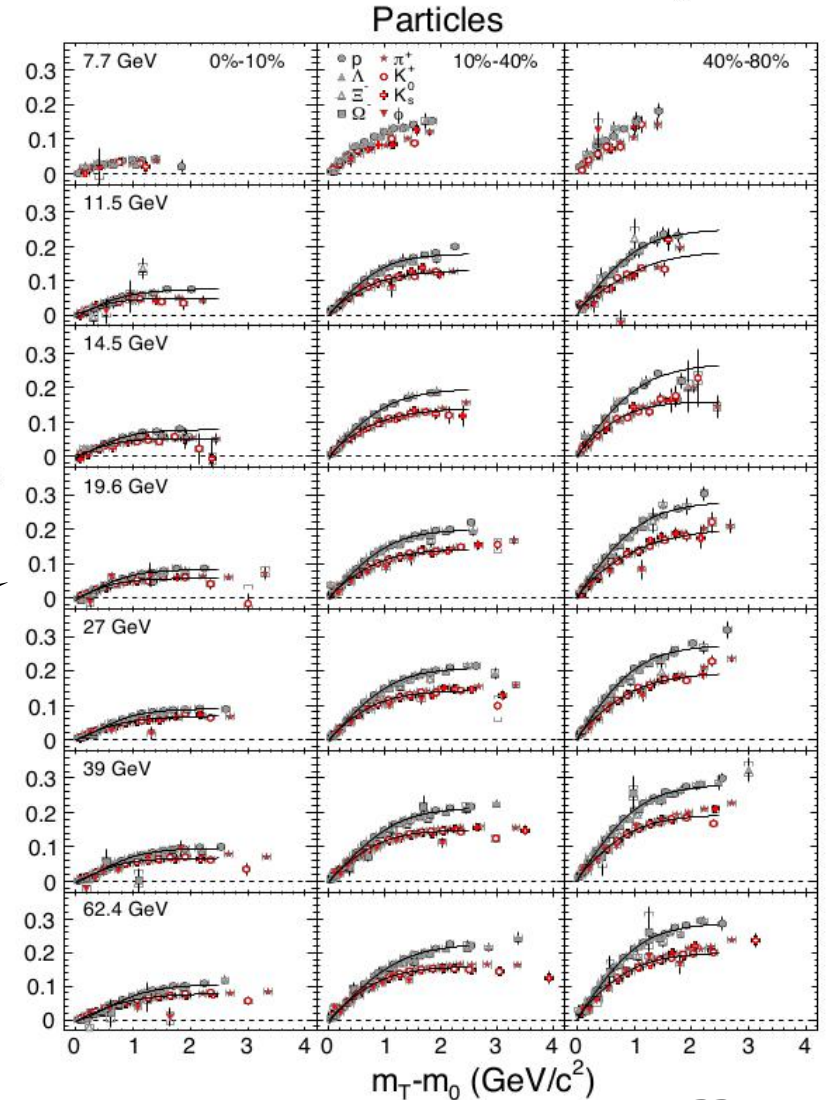


# PID $v_2$ @ STAR beam energy scan



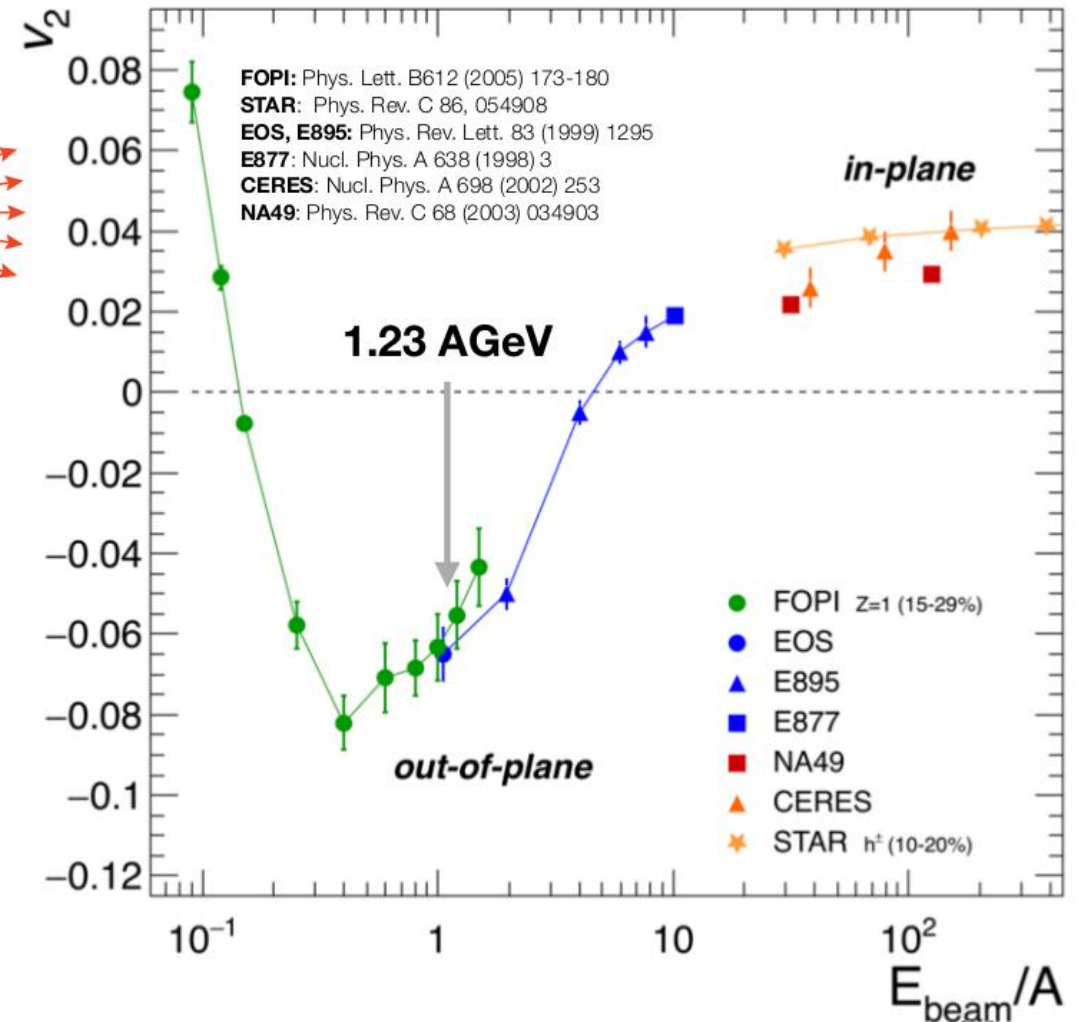
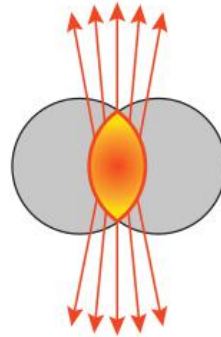
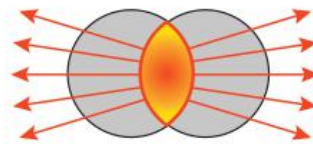
similar  $v_2(p_T)$  shape for various species

baryon / meson splitting only vanishes @ 7.7 GeV !



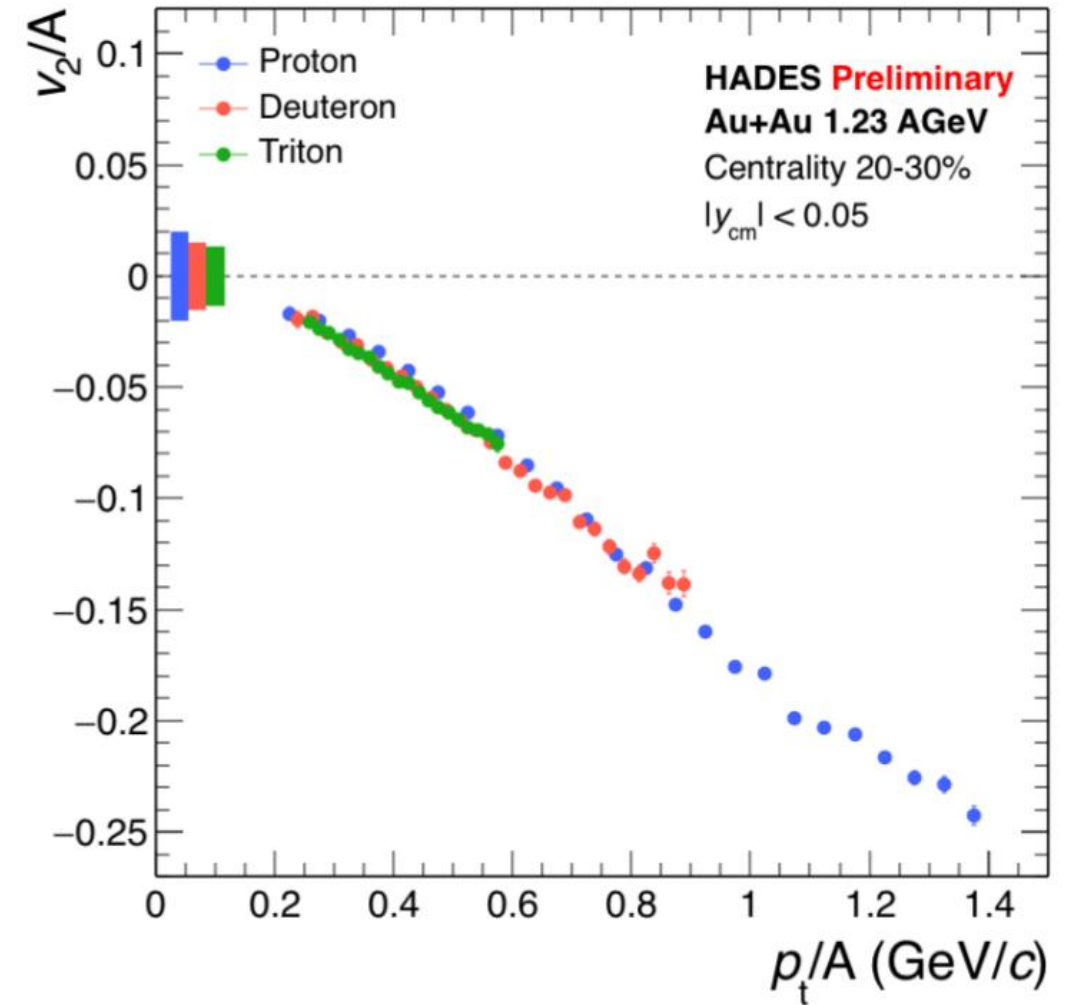
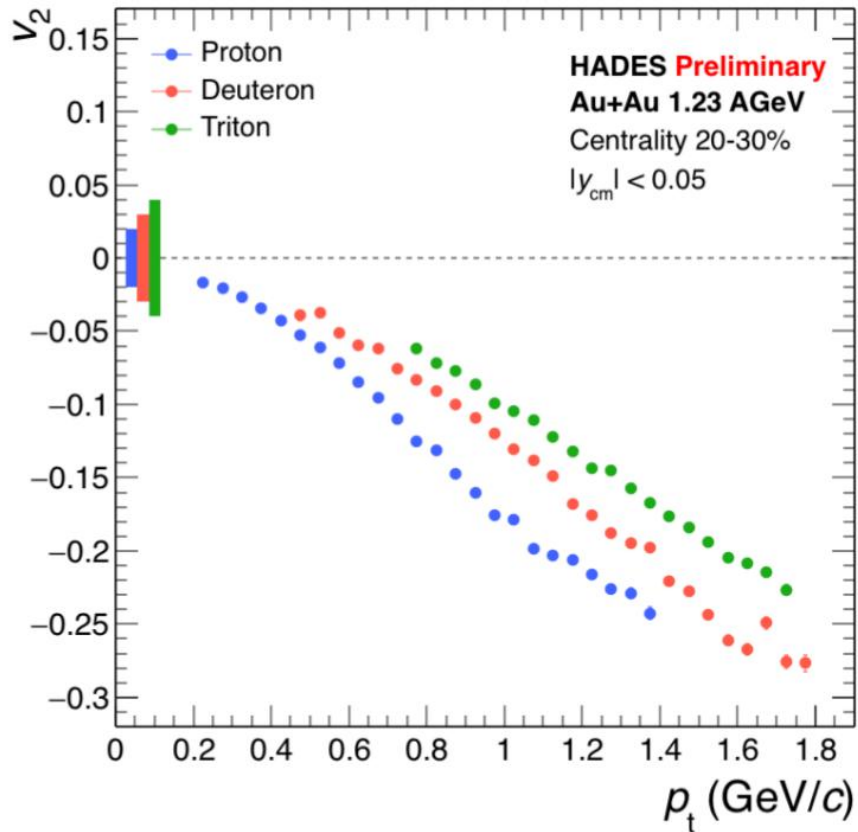
# PID $v_n$ at HADES: exploring (even) lower energies

- In-plane  $v_2 > 0$ 
  - ▶ Short spectator passing time  
 $\tau_{\text{passing}} \ll \tau_{\text{expansion}}$
  - ▶ Pressure gradient
- Out-of-plane  $v_2 < 0$ 
  - ▶ Long spectator passing time  
 $\tau_{\text{passing}} \geq \tau_{\text{expansion}}$
  - ▶ Squeeze-out



NB credit: B. Kardan, QM2018

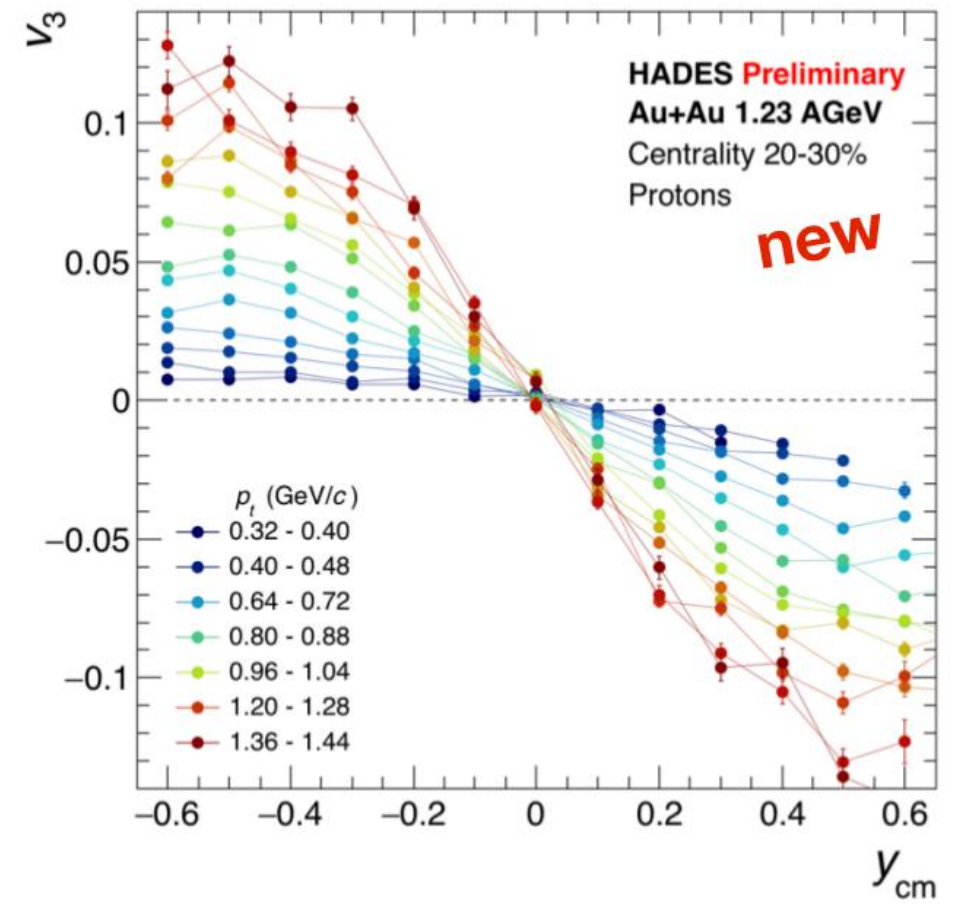
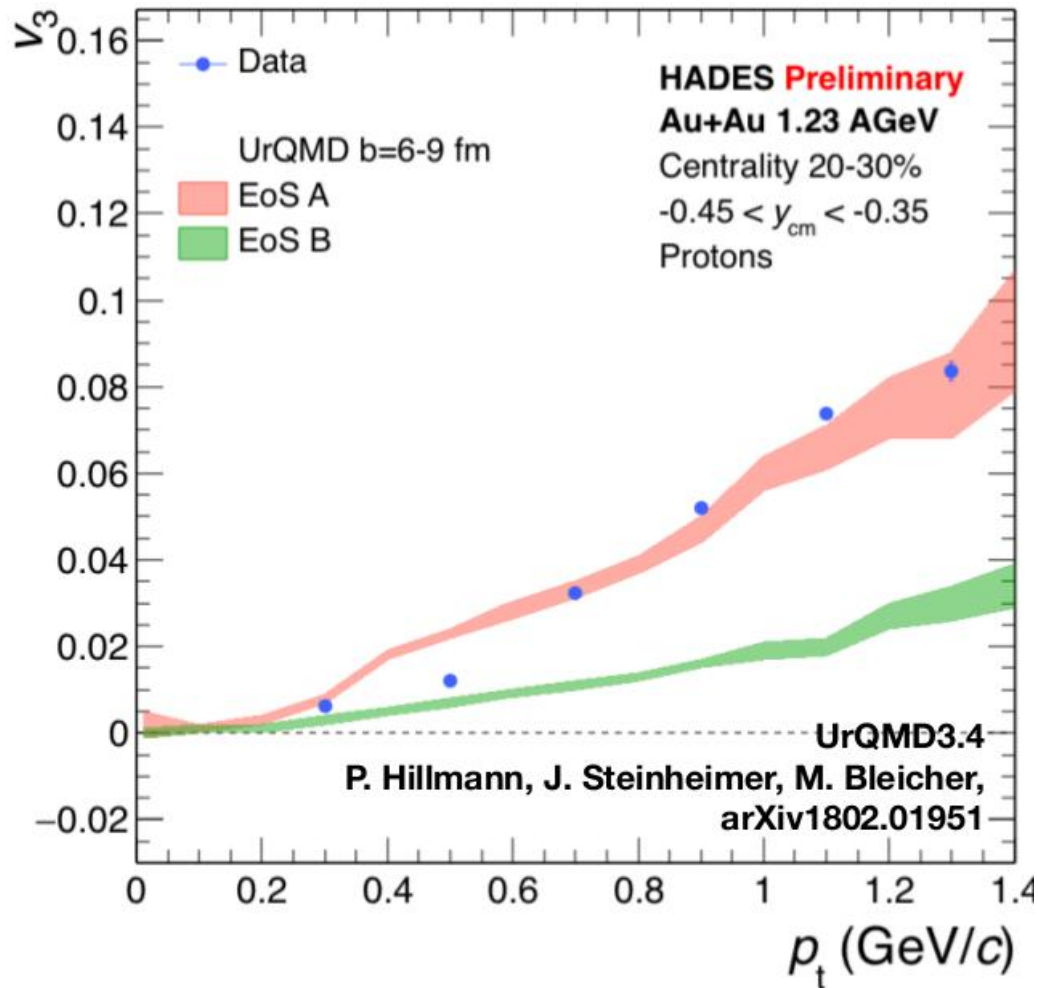
# PID $v_2$ @ 1.23 AGeV



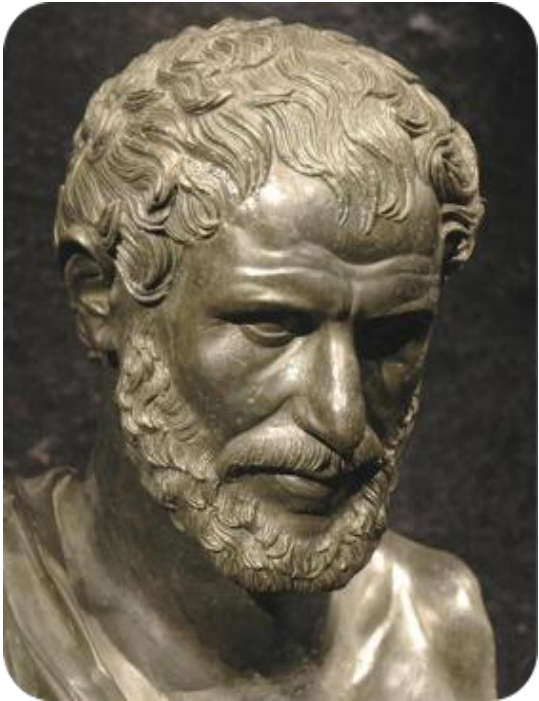
'squeeze-out'  $v_2$  of protons, deuterons and triton  
scaling of  $v_2$  and  $p_t$  with nuclear mass number A  
as expected from nucleon coalescence

# PID $v_3$ @ 1.23 AGeV

UrQMD predicts high sensitivity of  $v_3$  to EoS



Τα πάντα ρει...



**PID flow: wealth of measurements available**

high precision in  $p_T$  centrality from LHC run 2  
high precision as function of beam energy from STAR  
pushing to lowest energies with HADES

**fundamental questions**

- discerning between initial state and final state effects
- treatment of non-flow