



Chiral Edge Mode in the Coupled Dynamics of Magnetic Solitons

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Vortex ground state of a permalloy microdisk

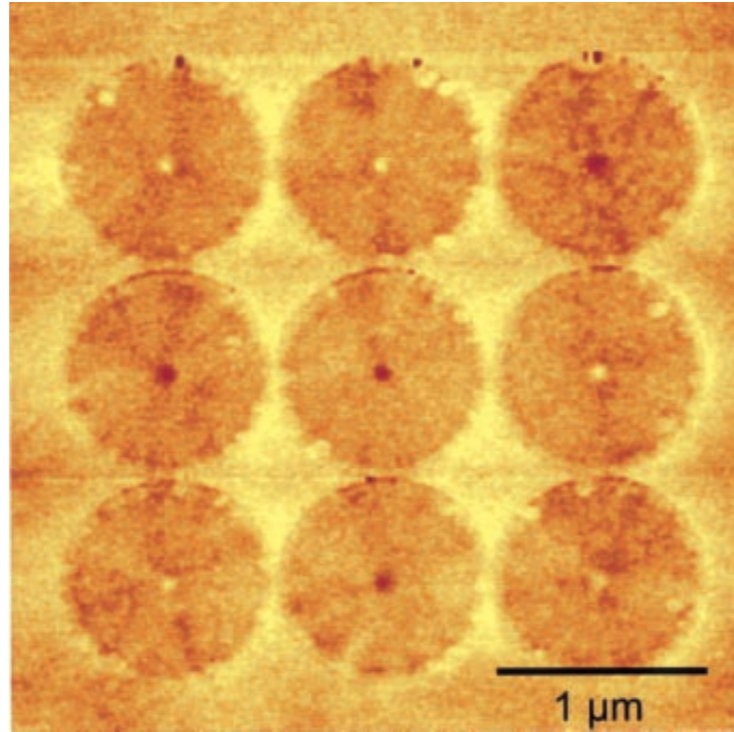
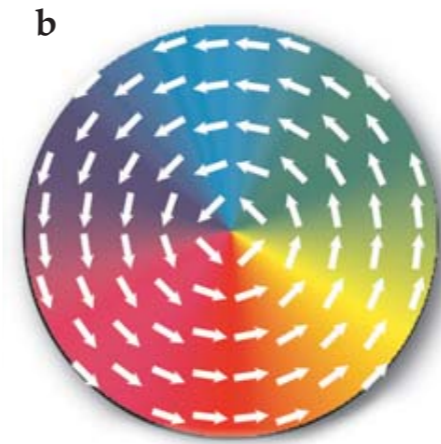


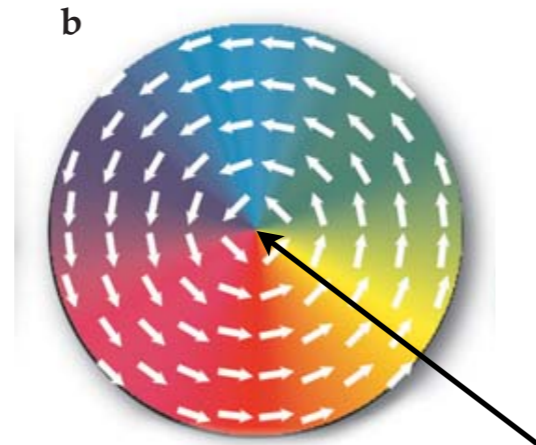
Fig. 2. MFM image of an array of permalloy dots 1 μm in diameter and 50 nm thick.

Shinjo et al, *Science* (2000)



Chien et al, *Physics Today* (2007)

The dynamics of a vortex core

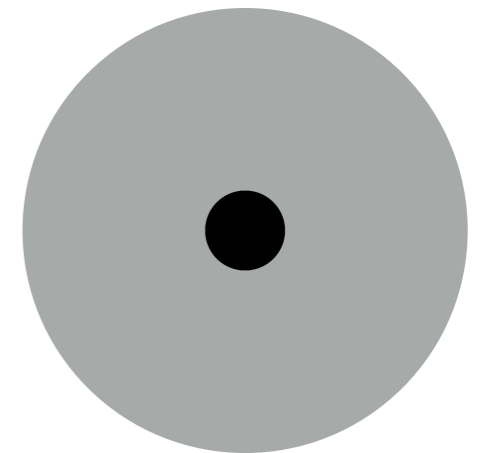


$$\mathbf{R}(t) = (X(t), Y(t))$$

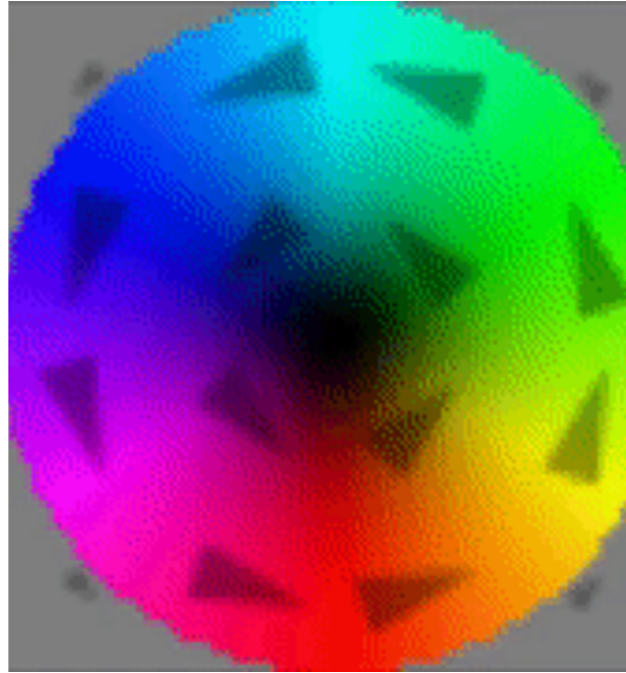
The low-energy dynamics of a vortex disks can be captured by the dynamics of the vortex-core position.

Pinning potential: $U(\mathbf{R}) = K\mathbf{R}^2/2$

Force: $F = -K\mathbf{R}$



The gyrotopic dynamics of a vortex core



Force:

$$\mathbf{F} = -K\mathbf{R}$$

Velocity:

$$\frac{d\mathbf{R}}{dt} \perp \mathbf{F}$$

Why is the velocity perpendicular to the force?

The gyrotropic dynamics of a vortex core

equations of motion: $G \frac{d\mathbf{R}}{dt} \times \hat{\mathbf{z}} = \mathbf{F} = -K\mathbf{R}$ resonant frequency: $\omega \equiv K/G$

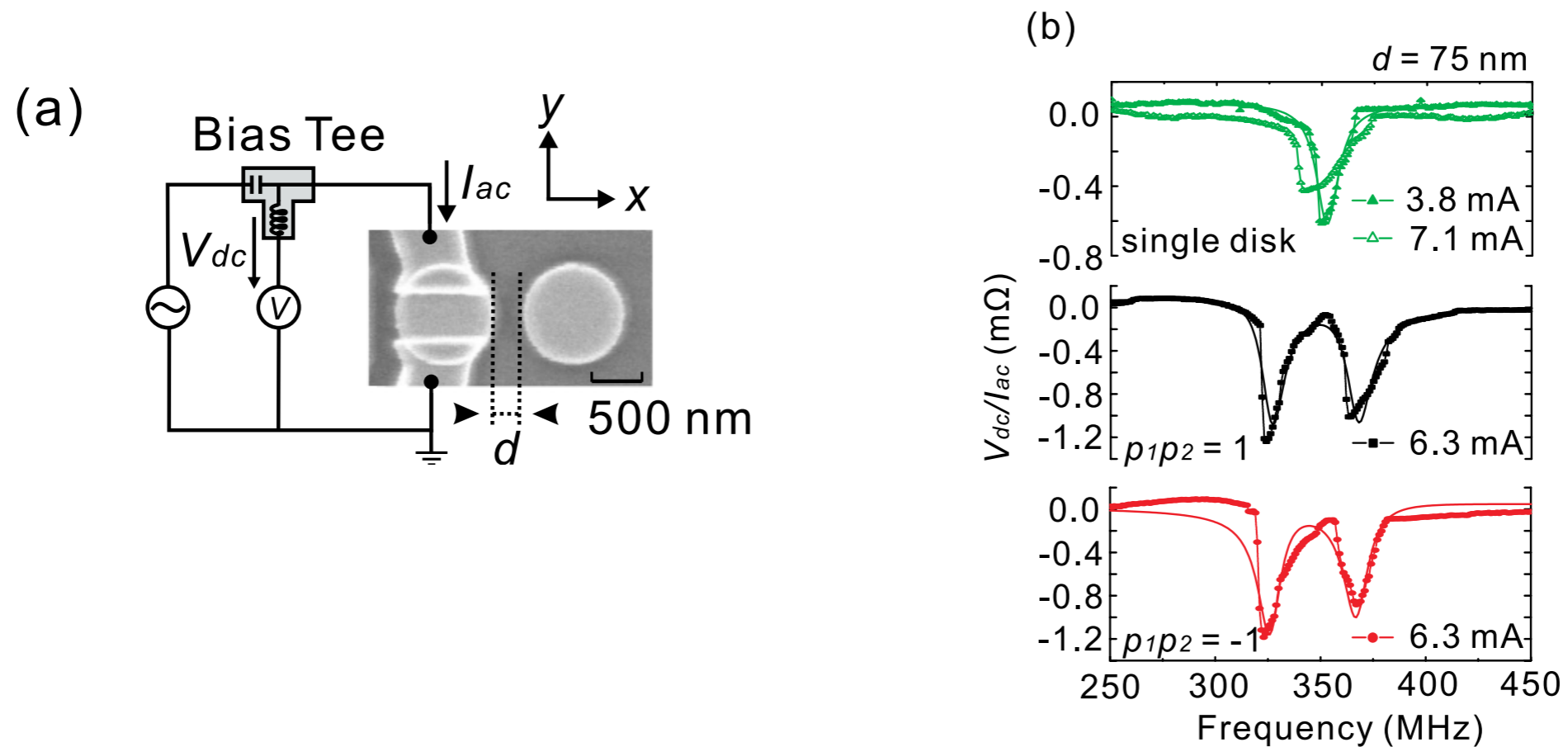
$$G = -2\pi s t p$$

spin density \nearrow \nwarrow polarity (odd in time reversal)
disk thickness \uparrow



The **polarity** of a vortex determines the **gyration direction**.

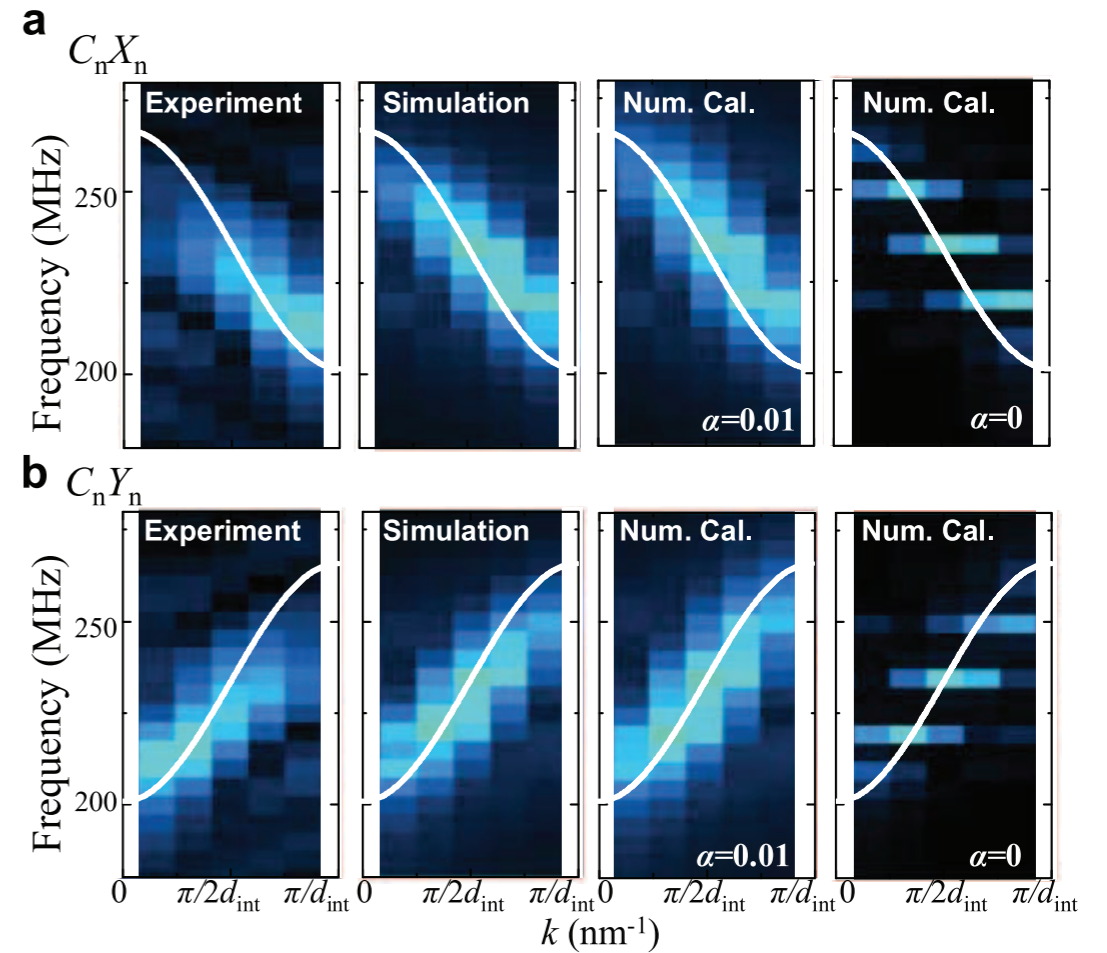
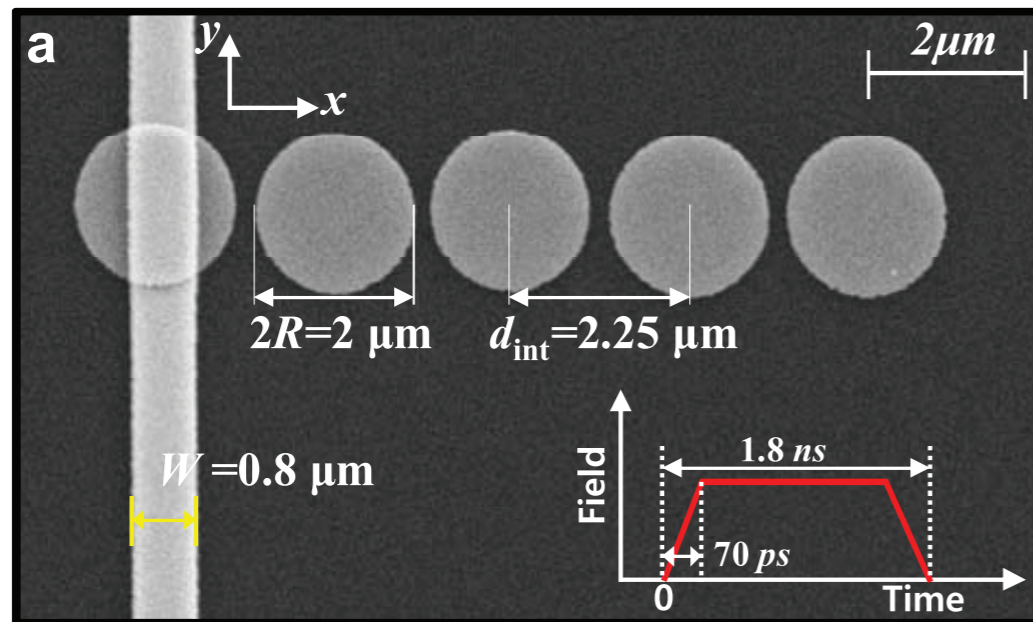
The dipolar-coupled dynamics of two vortices



Sugimoto et al, PRL (2010)

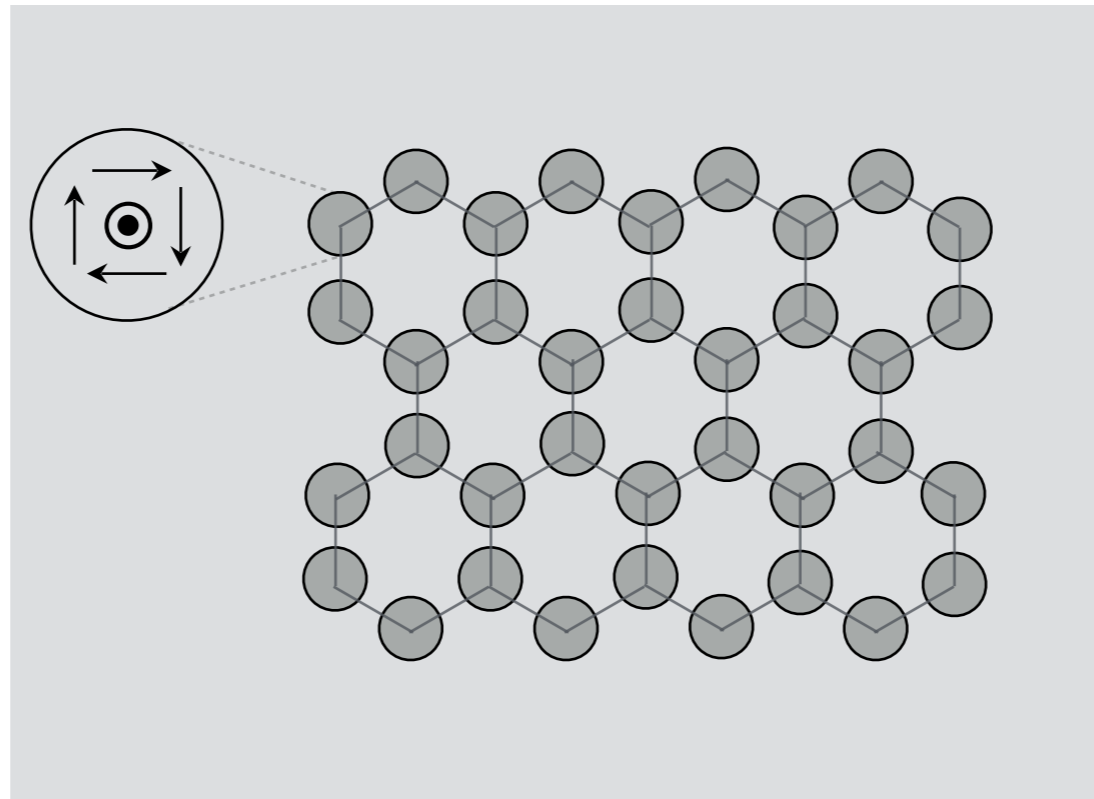
coupled pair of vortices = diatomic molecule with bonding and antibonding states

The dipolar-coupled dynamics of five vortices



dispersion relation of the coupled dynamics

The dipolar-coupled dynamics of many vortices?



SKK and Tserkovnyak, *PRL* (2017)

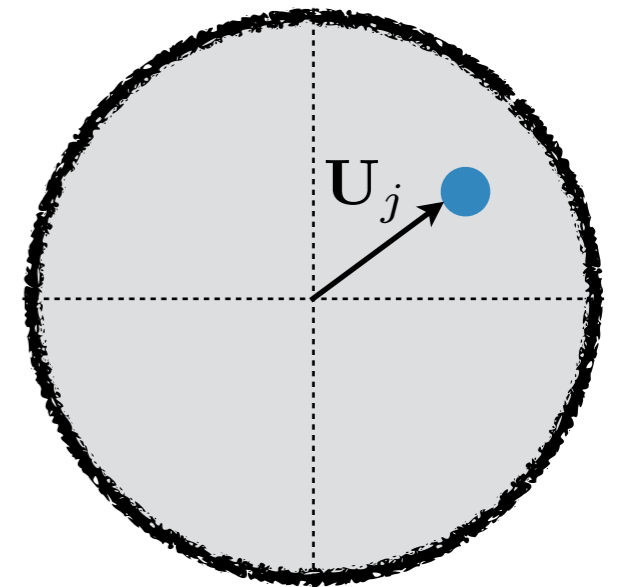
The dipolar-coupled dynamics of many vortices?

equations of motion for j th vortex core: $G\hat{\mathbf{z}} \times \frac{d\mathbf{U}_j}{dt} + \mathbf{F}_j = 0$

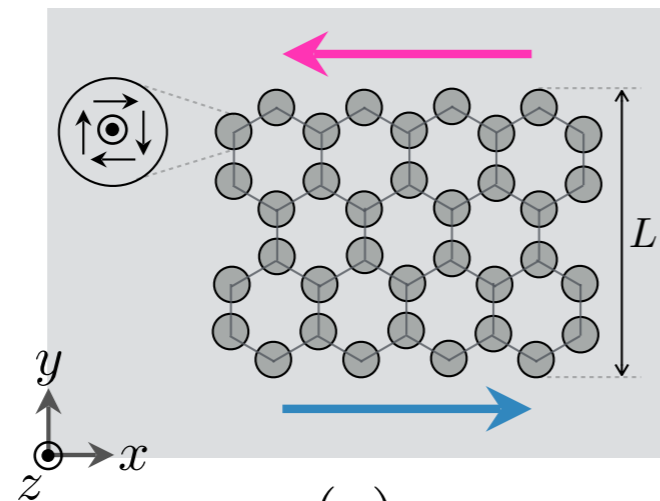
core displacement: $\mathbf{U}_j = \mathbf{R}_j - \mathbf{R}_j^0$

conservative force: $\mathbf{F}_j = \frac{\partial U}{\partial \mathbf{U}_j}$

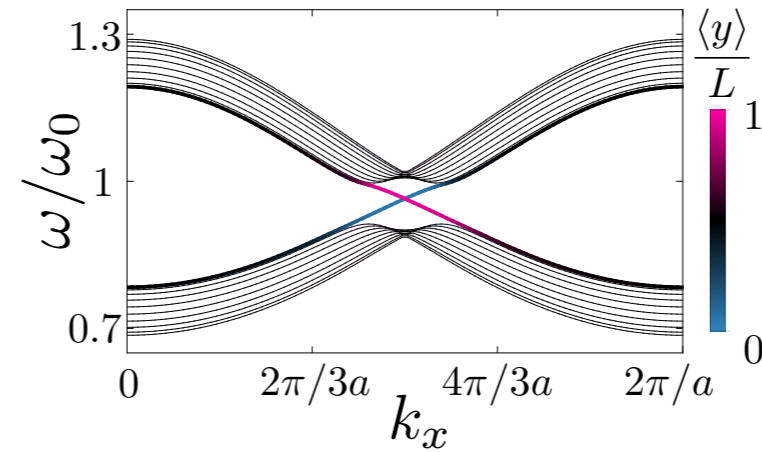
potential energy: $U = \sum_j K\mathbf{U}_j^2/2 + \sum_{j \neq k} U_{jk}/2$



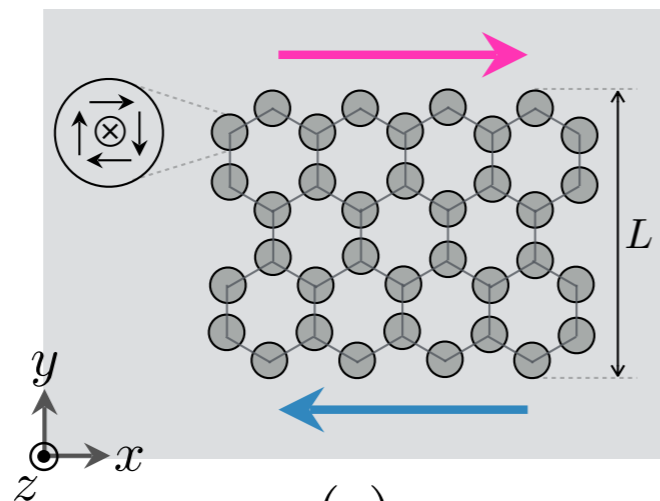
Topological edge mode in honeycomb vortex lattice



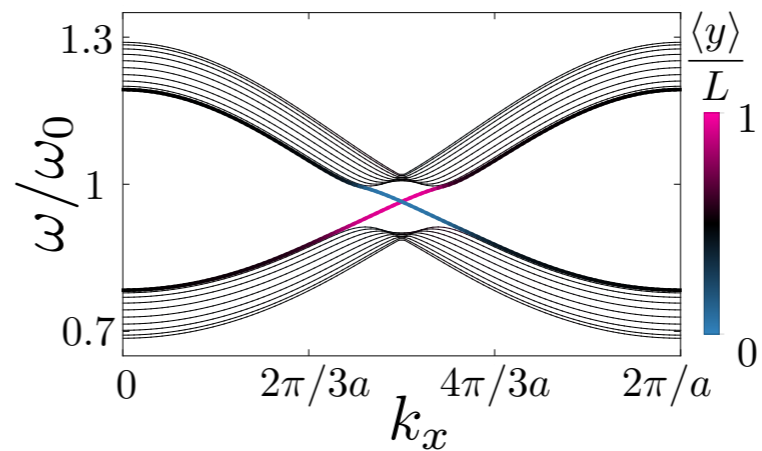
(a)



(b)



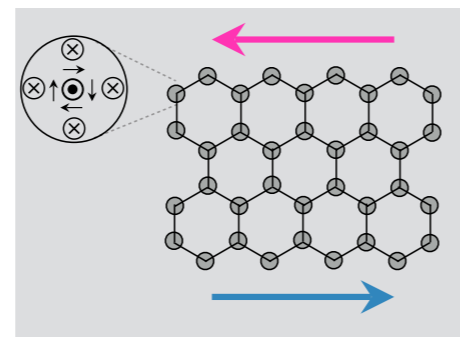
(c)



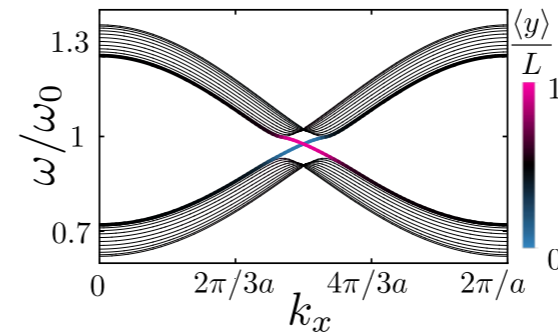
(d)

The honeycomb lattice of vortex disks supports a **chiral edge mode** in the coupled gyration dynamics. The **chirality** is determined by the **polarity** of the constituent vortices.

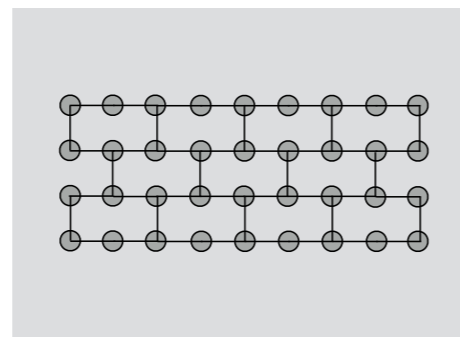
Topological edge mode in honeycomb **skyrmion** lattice



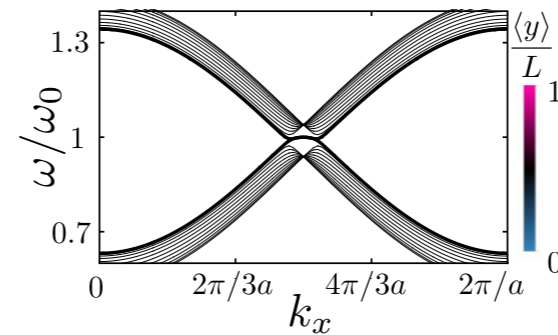
(a)



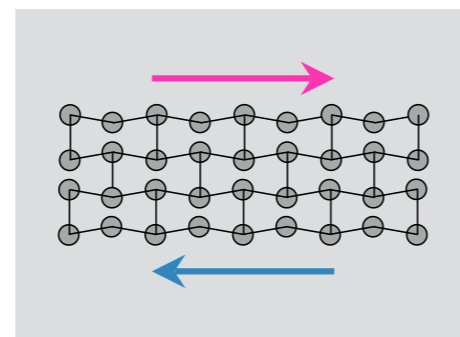
(b)



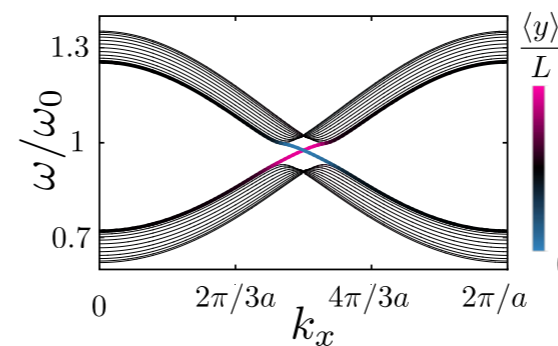
(c)



(d)



(e)



(f)

The **chirality** can be changed by **distorting** the honeycomb lattice.

New research area: soliton-based metamaterial

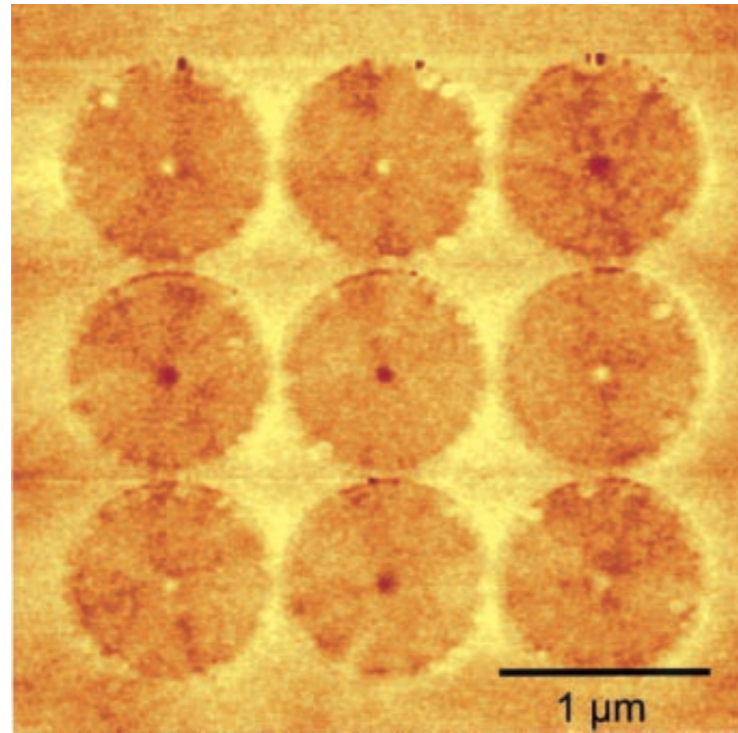
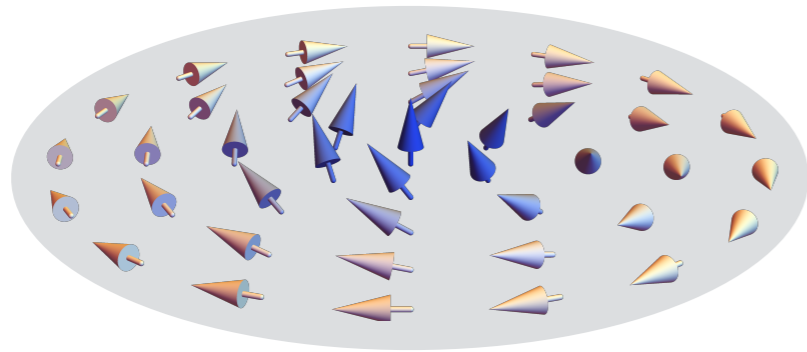


Fig. 2. MFM image of an array of permalloy dots 1 μm in diameter and 50 nm thick.

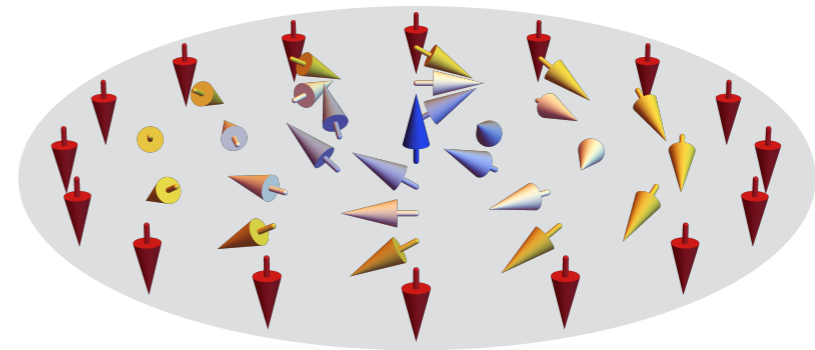
= metataoms with the topological stability

We can create **metamaterials** with **soliton metaatoms**, which can exhibit novel phases and can provide unusual functionalities.

The new collection of metaatoms

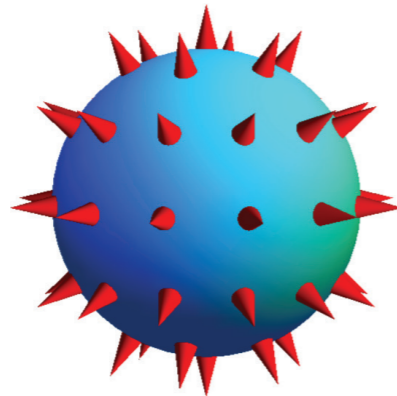


vortex

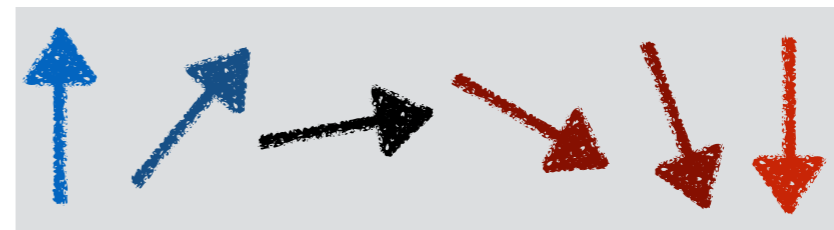


skyrmion

Thank you!



monopole



domain wall