

# Limits on Top-Higgs Interaction from Multi-Top Final States

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20/09/2018

In collaboration with

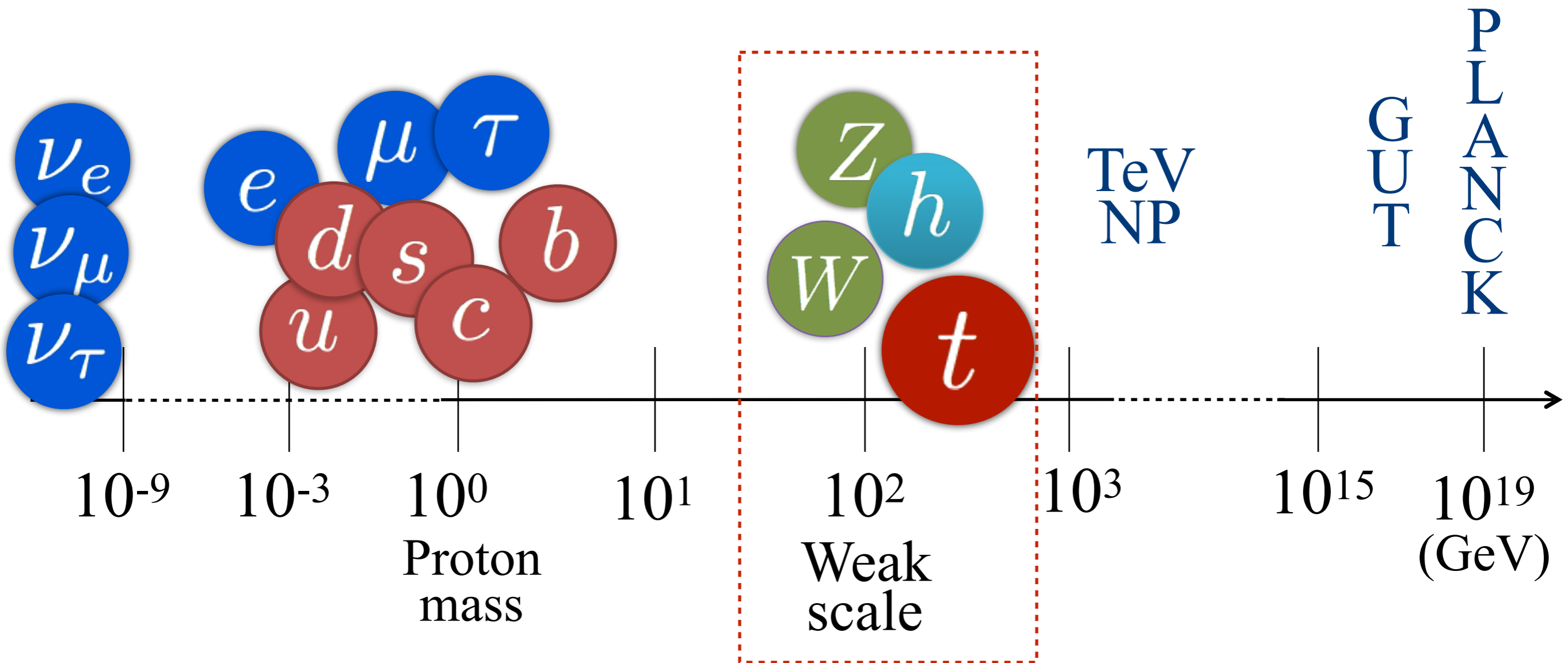
Shao-Long Chen and Yandong Liu, 1602.01934;

Shao-Long Chen, Yandong Liu, Rui Zhang, Ya Zhang, in preparation

# Two outstanding puzzles in SM

Origins of EWSB  
(*W/Z Mass*)

and Flavor breaking  
(*Fermion Mass*)



Top quark is not heavy! It is naturally around weak scale.

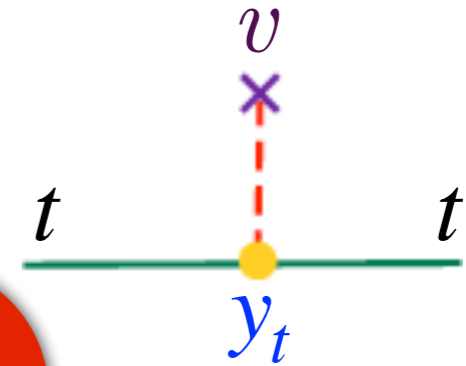
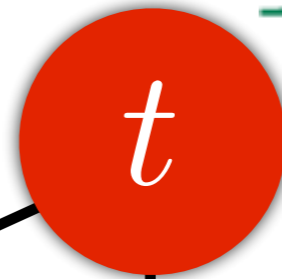
Q: why are the other quarks and leptons so light?

# Testing the SM at weak scale

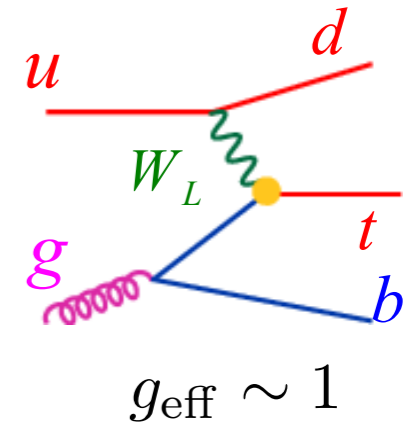
$$\mathcal{L} = (D_\mu \Phi)^\dagger (D^\mu \Phi) - \mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2 + y_f \bar{F}_L \Phi f_r + \dots$$



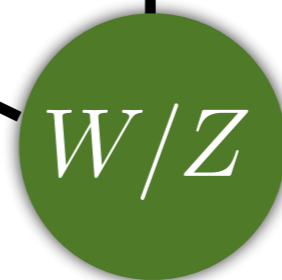
$Y_f$   
Flavor  
breaking



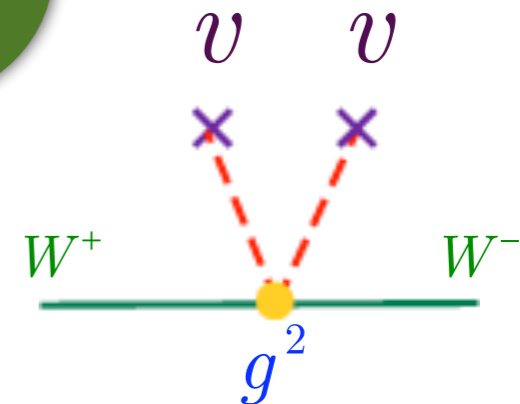
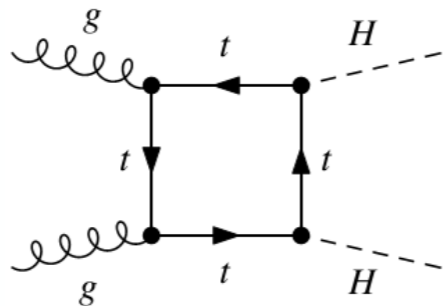
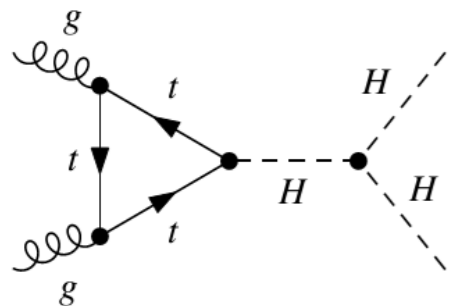
Equivalence  
Theorem



Symmetry  
breaking  
 $g_W g_Y$

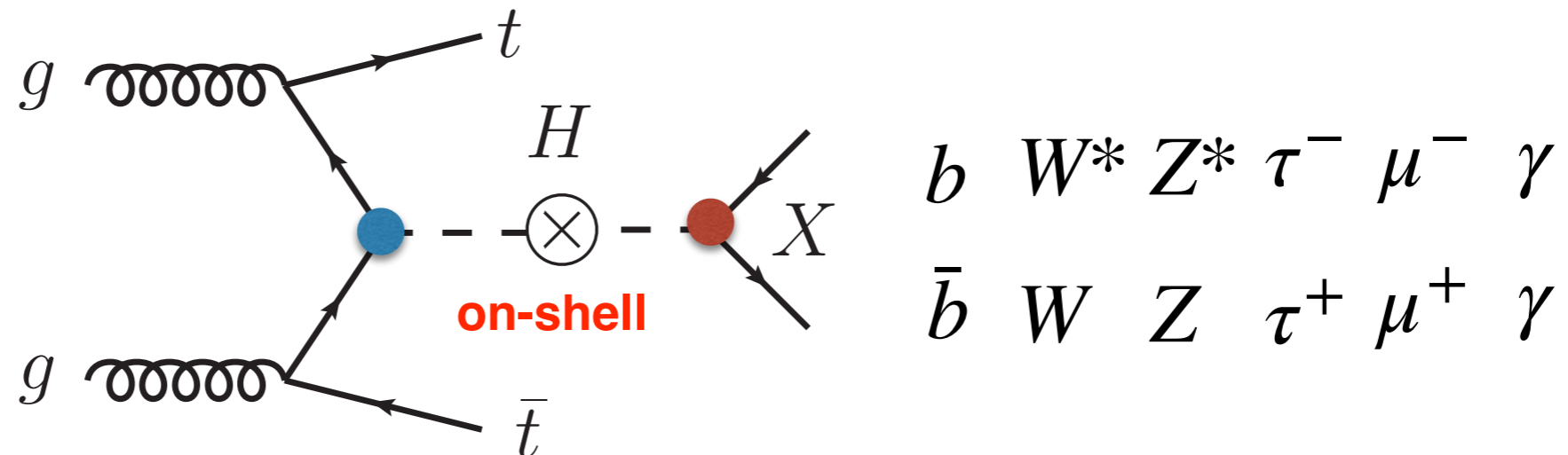


one and only  
self-interaction  
in the SM



# Top-quark Yukawa coupling

directly measured from the  $t\bar{t}H$  production



Narrow width approximation

$$\hat{\sigma} = \sigma(gg \rightarrow t\bar{t}H) \times \frac{\Gamma(H \rightarrow X)}{\Gamma_H} = \frac{\kappa_t^2 \kappa_X^2}{\Gamma_H / \Gamma_H^{\text{SM}}} \hat{\sigma}_{\text{SM}}$$

$$\kappa_t = \frac{y_t}{y_t^{\text{SM}}}$$

$$\kappa_X = \frac{y_X}{y_X^{\text{SM}}}$$

$$\mu \equiv \frac{\hat{\sigma}}{\hat{\sigma}_{\text{SM}}} = \frac{\kappa_t^2 \kappa_X^2}{\Gamma_H / \Gamma_H^{\text{SM}}} \xrightarrow[\kappa_X = 1]{\Gamma_H = \Gamma_H^{\text{SM}}} \mu = \kappa_t^2$$

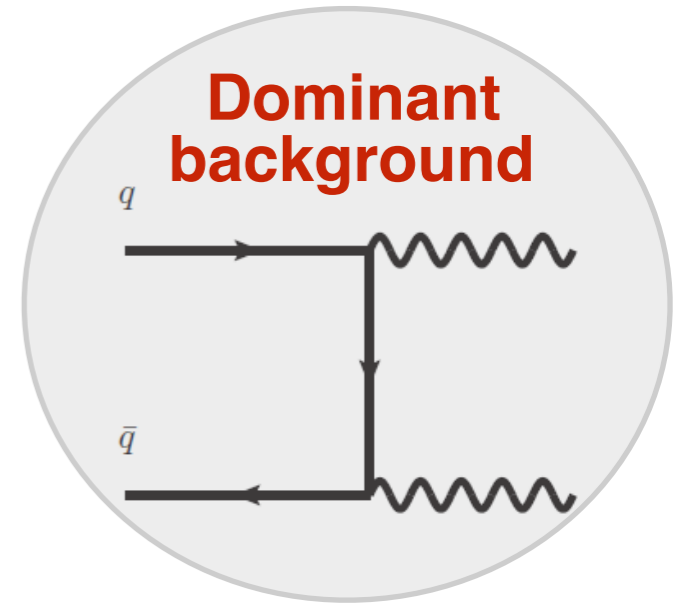
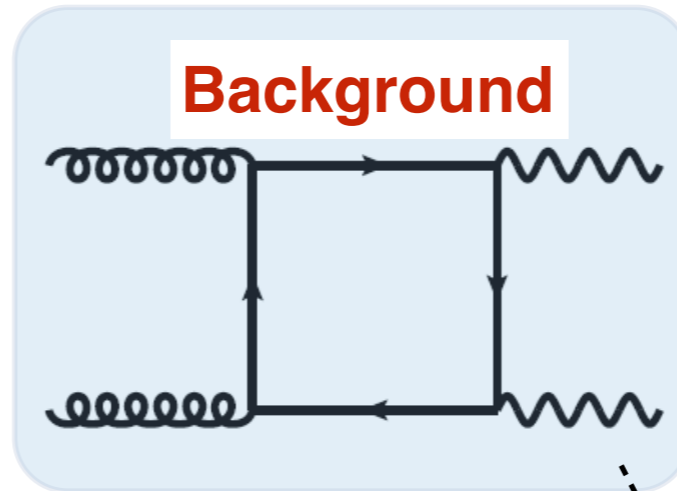
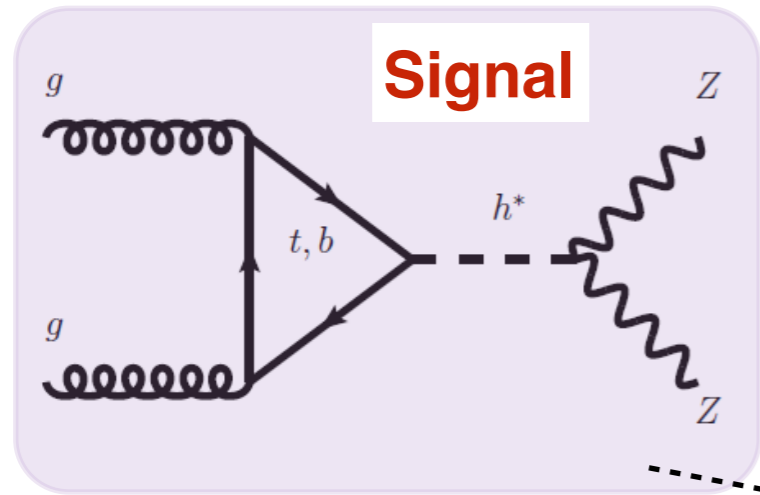
Q1: can we determine  $\kappa_t$  without those assumptions?

# Higgs boson width

Caola, Melnikov (2013)

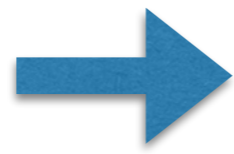
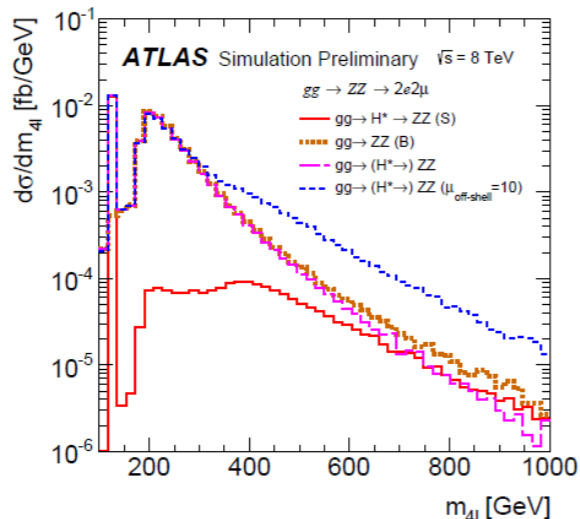
Higgs on-shell production

$$\sigma \sim \frac{g_{ggh}^2 g_{hzz}^2}{m_h \Gamma_h}$$



Higgs off-shell production

$$\frac{d\sigma}{dM_{ZZ}^2} \sim \frac{g_{ggh}^2 g_{hzz}^2}{(M_{ZZ}^2 - m_h^2)^2} |M_1|^2 + \frac{g_{ggh} g_{hzz}}{(M_{ZZ}^2 - m_h^2) M_{ZZ}^2} |M_1 M_2^*|$$

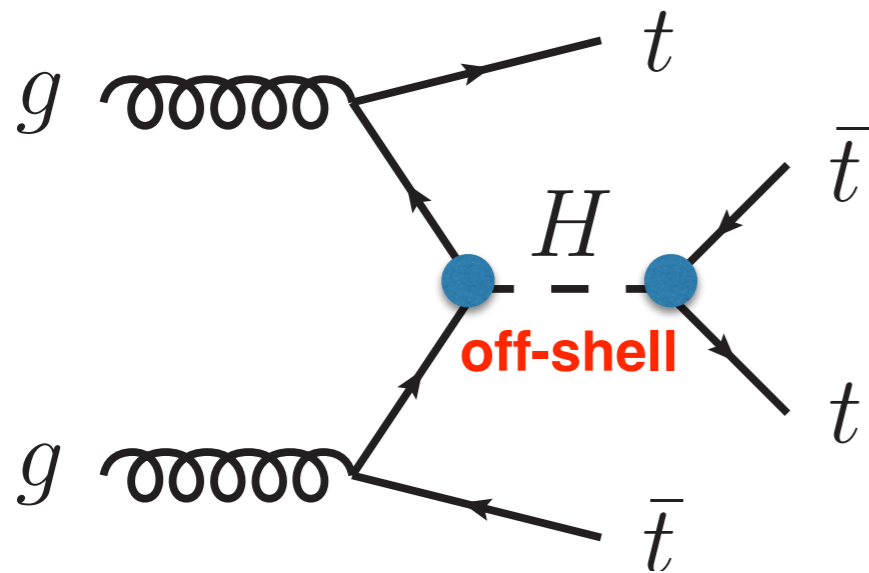


The combination of both on-shell and off-shell measurements of signal strength achieve a significantly higher sensitivity to the total width

Q2: alternative way to measure the Higgs boson width?

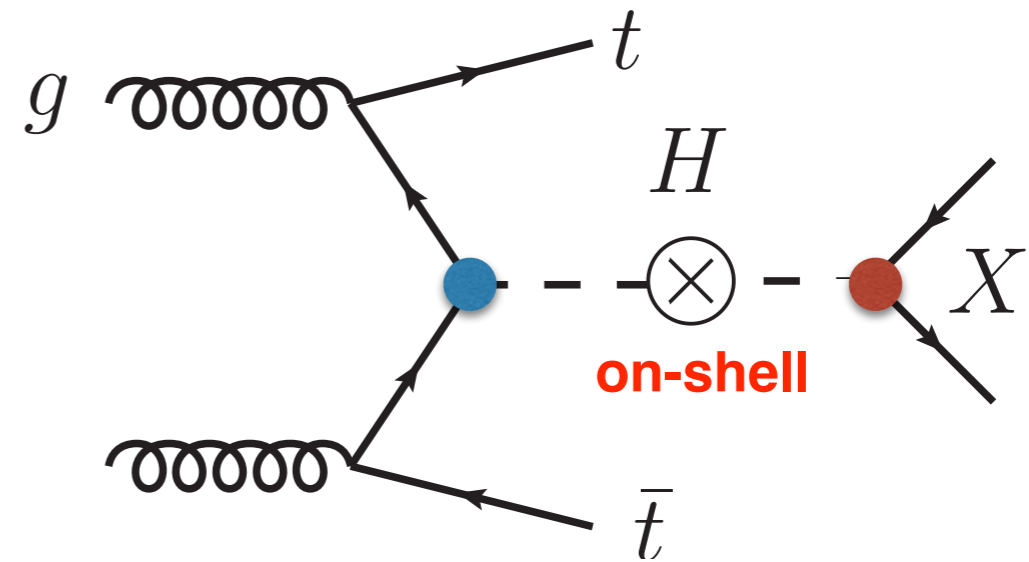
# Four top-quark production

QHC, Chen, Liu, 1602.01934



$$\hat{\sigma}(pp \rightarrow t\bar{t}H \rightarrow t\bar{t}t\bar{t})$$

$$\propto \kappa_t^4 \times \hat{\sigma}(pp \rightarrow t\bar{t}H \rightarrow t\bar{t}t\bar{t})_{\text{SM}}$$



$$\hat{\sigma}(pp \rightarrow t\bar{t}H \rightarrow t\bar{t}X)$$

$$\propto \underbrace{\frac{\kappa_t^2 \kappa_X^2}{\Gamma_H / \Gamma_H^{\text{SM}}}}_{\mu_{t\bar{t}H}^X} \times \hat{\sigma}(pp \rightarrow t\bar{t}H \rightarrow t\bar{t}X)_{\text{SM}}$$

$$\mu_{t\bar{t}H}^X$$

$$X = \gamma\gamma, \mu^+\mu^-, ZZ^*, \dots$$

$$\mu_{t\bar{t}H}^{\gamma\gamma} = 1.00 \pm 0.38$$

$$\mu_{t\bar{t}H}^{ZZ} = 1.00 \pm 0.49$$

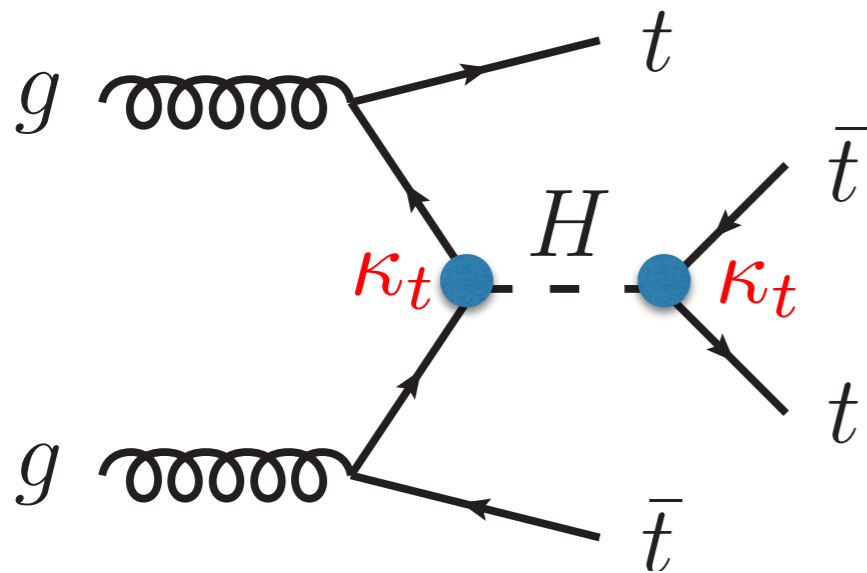
ATLAS-PHYS-PUB-2014-016

$$\mu_{t\bar{t}H}^{\mu\mu} = 1.00 \pm 0.74$$

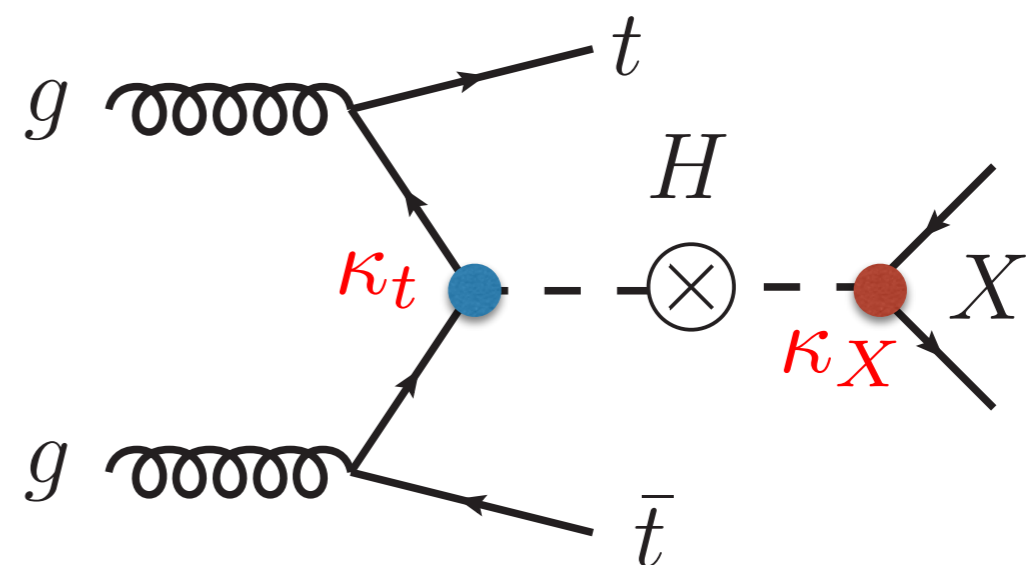
$$\mu_{t\bar{t}H}^{\text{combo}} = 1.00 \pm 0.30$$

14TeV LHC, 300fb<sup>-1</sup>

# Two scenarios



$$\hat{\sigma}(pp \rightarrow t\bar{t}t\bar{t}) \propto \kappa_t^4$$



$$\mu_{t\bar{t}H}^X \equiv \frac{\kappa_t^2 \kappa_X^2}{\Gamma_H / \Gamma_H^{\text{SM}}} = \frac{\kappa_t^2 \kappa_X^2}{R_\Gamma}$$

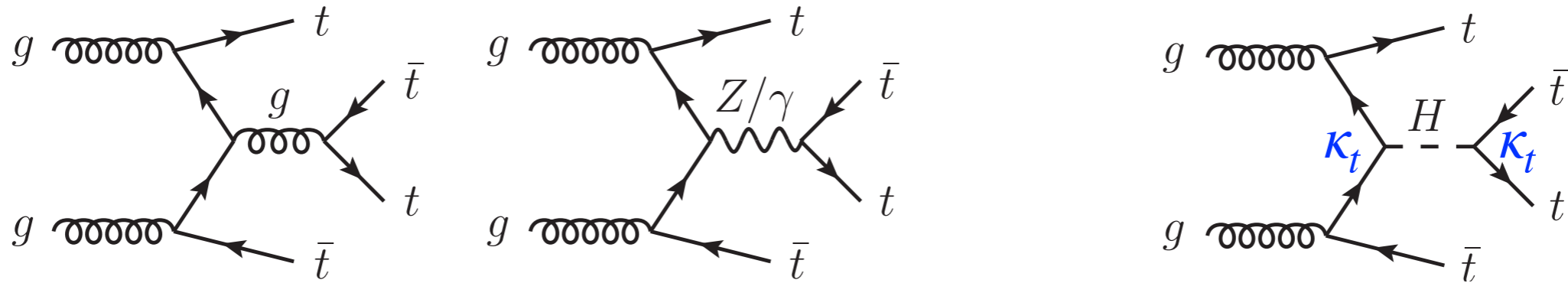
**1)**  $\Gamma_H \simeq \Gamma_H^{\text{SM}}$   
**Rare** modes ( $\gamma\gamma, \mu^+ \mu^-$ )

$$\kappa_t^2 \kappa_X^2 = \mu_{t\bar{t}H}^X$$

**2)**  $\kappa_X \simeq 1$   
**Major** modes ( $b\bar{b}, WW^*$ )

$$\frac{\kappa_t^2}{R_\Gamma} = \mu_{t\bar{t}H}^X$$

# Measuring $\kappa_t$ from four top-quark production



$$\sigma(t\bar{t}t\bar{t}) = \underbrace{\sigma^{\text{SM}}(t\bar{t}t\bar{t})_{g/Z/\gamma}}_{\text{SM}} + \underbrace{\kappa_t^2 \sigma_{\text{int}}^{\text{SM}}}_{\text{SM}} + \underbrace{\kappa_t^4 \sigma^{\text{SM}}(t\bar{t}t\bar{t})_H}_{\text{SM}}$$

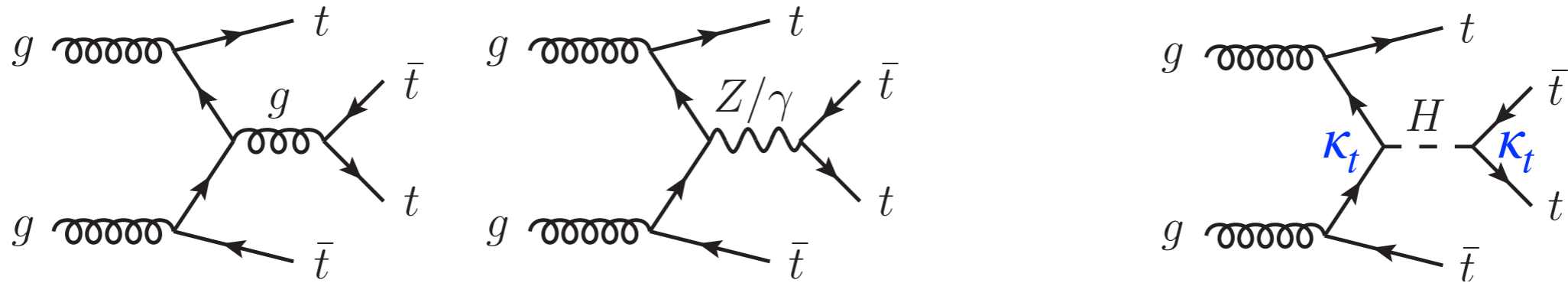
**LO**

Energy	$\sigma^{\text{SM}}(t\bar{t}t\bar{t})_{g/Z/\gamma}$	$\kappa_t^2 \sigma_{\text{int}}^{\text{SM}}$	$\kappa_t^4 \sigma^{\text{SM}}(t\bar{t}t\bar{t})_H$	Unit
8 TeV	1.344	-0.224	0.171	in unit of fb
13 TeV	9.997	-1.547	1.108	
14 TeV	13.14	-2.007	1.515	
27 TeV	115.1	-15.57	11.73	
100 TeV	3276	-356.9	273.1	

NLO corrections: Bevilacqua, Worek (2012);  
Alwall et al (2014); Frederix, Pagani, Zaro (2017)



# Measuring $\kappa_t$ from four top-quark production



$$\sigma(t\bar{t}t\bar{t}) = \underbrace{\sigma^{\text{SM}}(t\bar{t}t\bar{t})_{g/Z/\gamma}}_{\text{SM}} + \underbrace{\kappa_t^2 \sigma_{\text{int}}^{\text{SM}}}_{\text{SM}} + \underbrace{\kappa_t^4 \sigma^{\text{SM}}(t\bar{t}t\bar{t})_H}_{\text{SM}}$$

LO

8 TeV	1.344	-0.224	0.171
13 TeV	9.997	1.517	1.100
14 TeV	13.14		
27 TeV	115.1		
100 TeV	3276	-356.9	273.1

$$\sigma_g^{\text{SM}} = 1.216$$

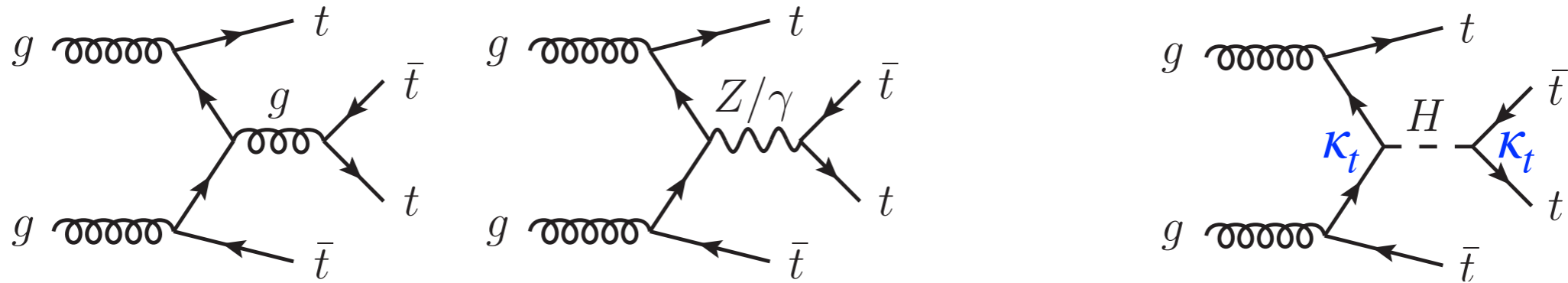
$$\sigma_{Z/\gamma}^{\text{SM}} = 0.412$$

$$\sigma_{g+Z/\gamma}^{\text{SM}} = -0.262$$

NLO corrections: Bevilacqua, Worek (2012);  $K_{\text{factor}} = 1.27$

Alwall et al (2014); Frederix, Pagani, Zaro (2017)

# Measuring $\kappa_t$ from four top-quark production



$$\sigma(t\bar{t}t\bar{t}) = \underbrace{\sigma^{\text{SM}}(t\bar{t}t\bar{t})_{g/Z/\gamma}} + \underbrace{\kappa_t^2 \sigma_{\text{int}}^{\text{SM}}} + \underbrace{\kappa_t^4 \sigma^{\text{SM}}(t\bar{t}t\bar{t})_H}$$

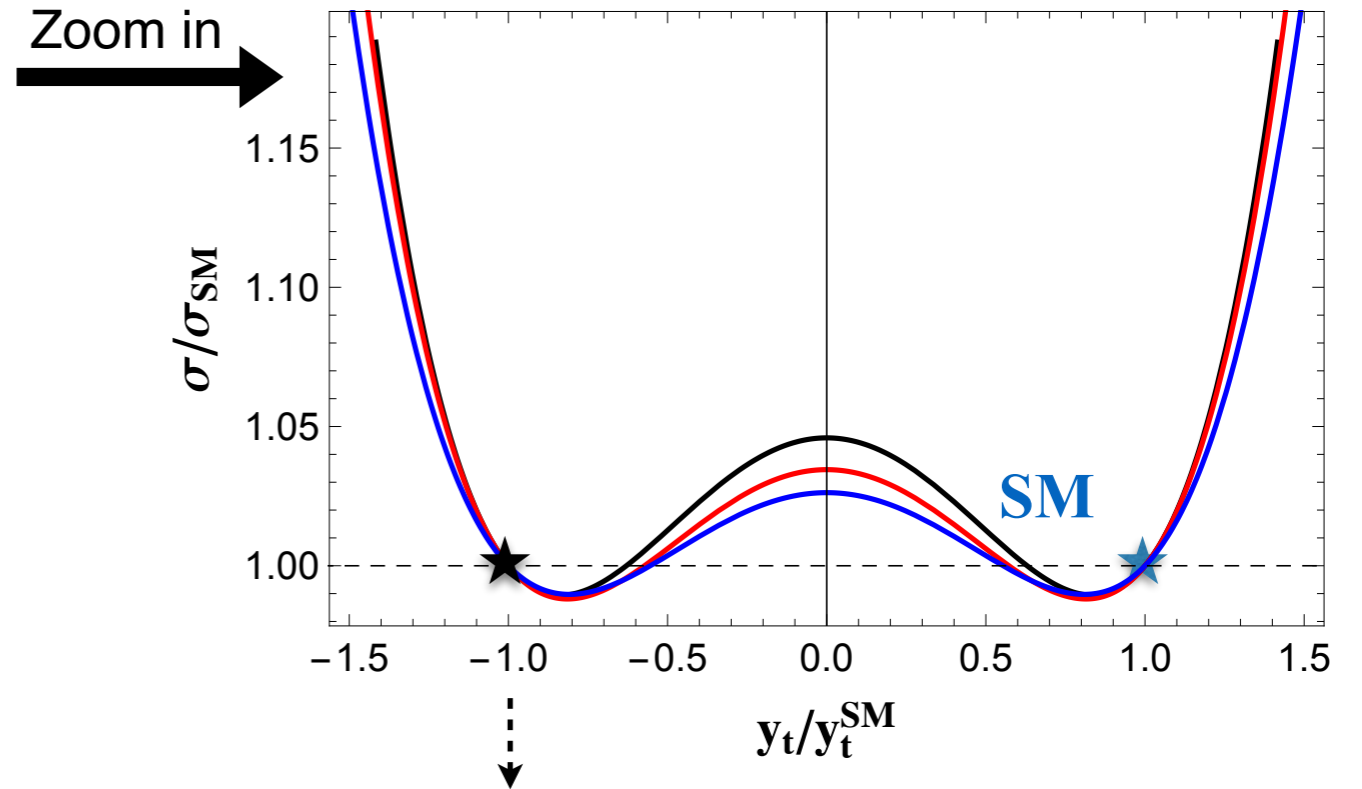
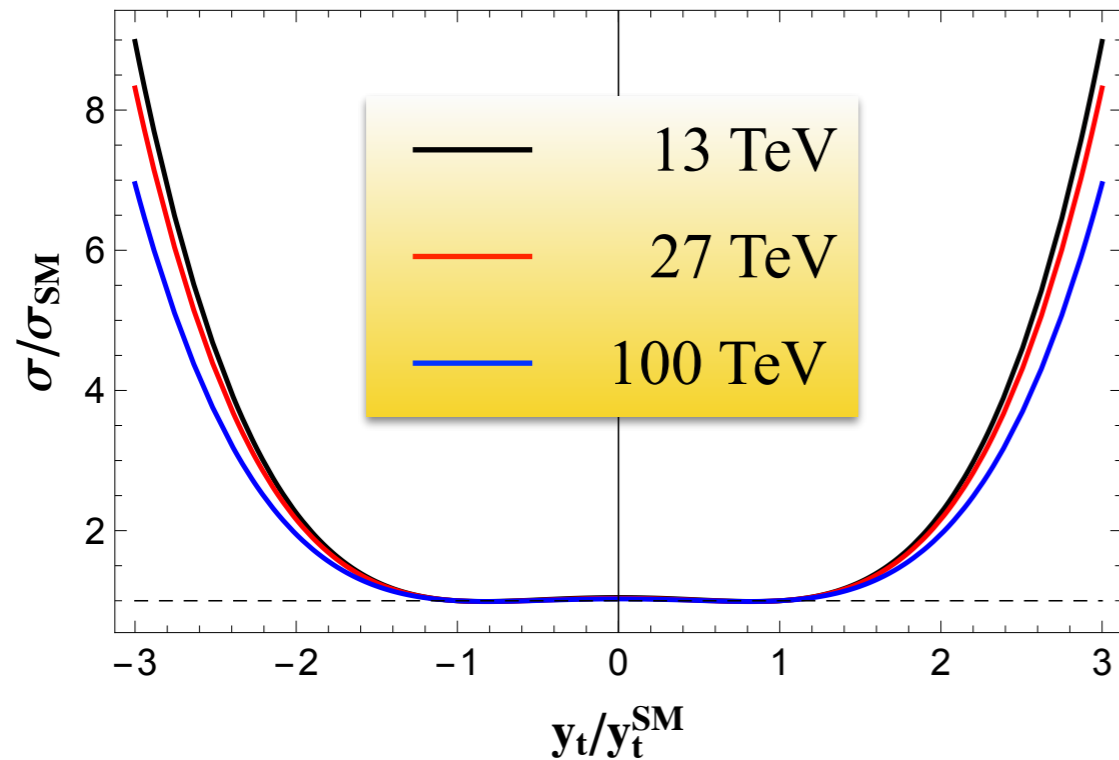
**LO**

8 TeV	1.344	-0.224	0.171	in unit of fb
13 TeV	9.997	-1.547	1.108	
14 TeV	13.14	-2.007	1.515	
27 TeV	115.1	-15.57	11.73	
100 TeV	3276	-356.9	273.1	
Relative ratio	<b>8~12</b>	<b>-1.3</b>	<b>1</b>	

cancel out around SM  $\kappa_t = 1$

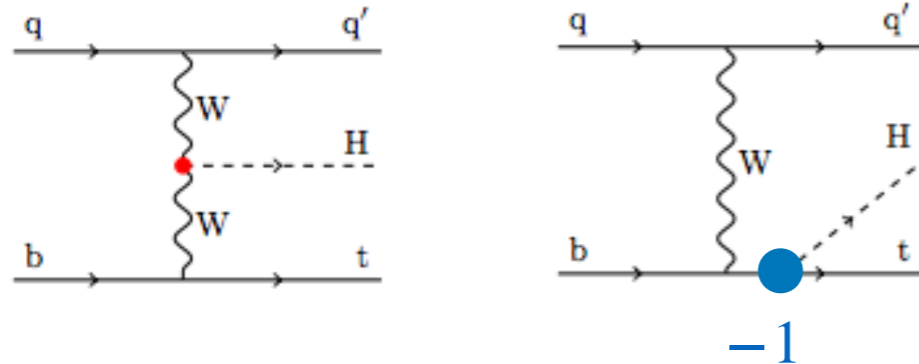
# Dependence of $\sigma/\sigma_{SM}$ on $\kappa_t$

$$\sigma(t\bar{t}t\bar{t}) = \sigma^{SM}(t\bar{t}t\bar{t})_{g/Z/\gamma} + \kappa_t^2 \sigma_{int}^{SM} + \kappa_t^4 \sigma^{SM}(t\bar{t}t\bar{t})_H$$

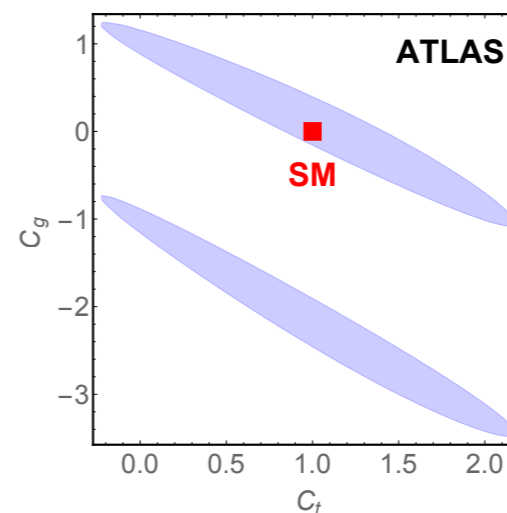


Htq production enhanced

Not supported by global fitting



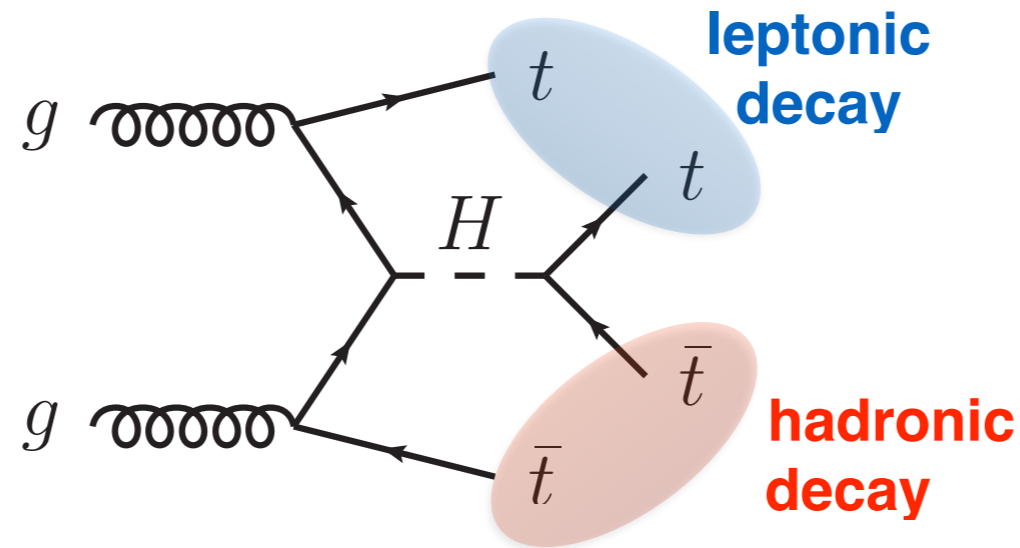
Look and not finding >>> Not looking



Consider  $\kappa_t > 0$  in our study

# Collider simulation

Event Topology: **same-sign charged leptons plus multi-jet (b-jet)**



Event selections:

	13-14TeV	27TeV	100TeV
$p_T^{j,l} \geq 20\text{GeV}$			
$ \eta^{j,l}  < 2.5$			
$N_{l^\pm} = 2$			
$N_{b\text{-jets}} \geq 3$			
	$N_{\text{jets}} \geq 5$	$N_{\text{jets}} \geq 6$	$N_{\text{jets}} \geq 6$
	$\cancel{E}_T \geq 100\text{GeV}$	150GeV	150GeV
	$M_T \geq 100\text{GeV}$		
	$H_T \geq 700\text{GeV}$	700GeV	800GeV

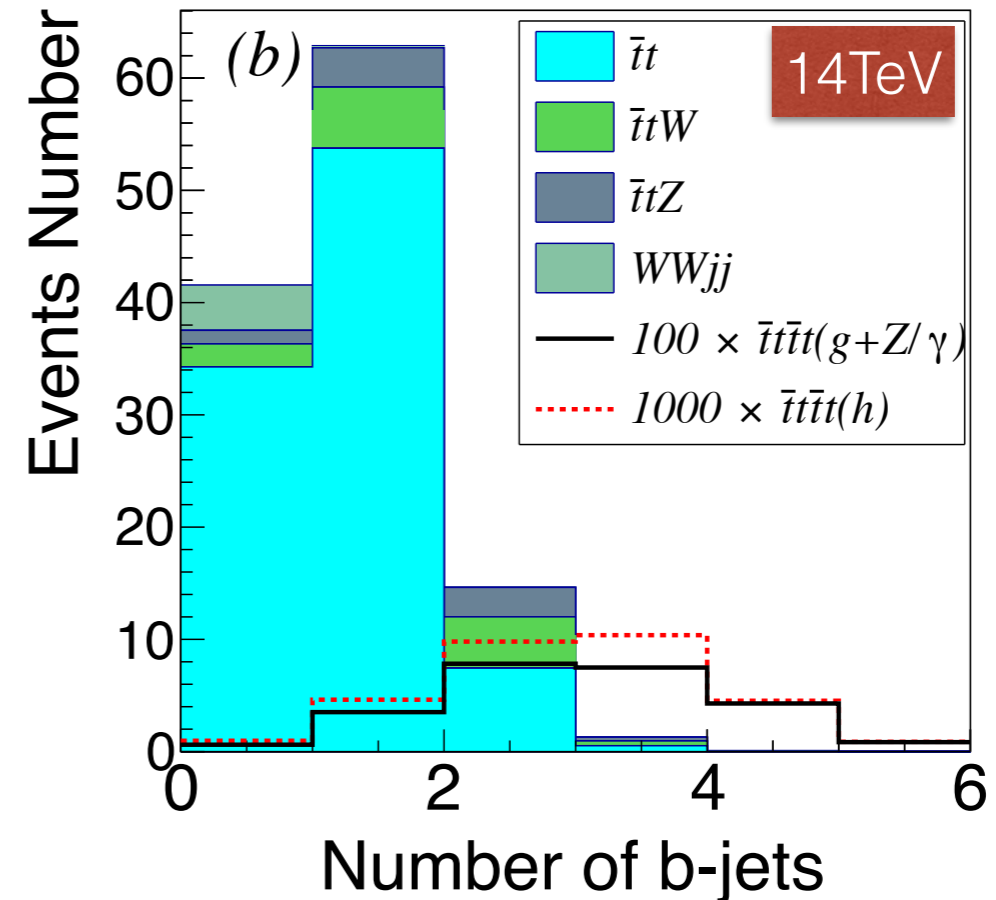
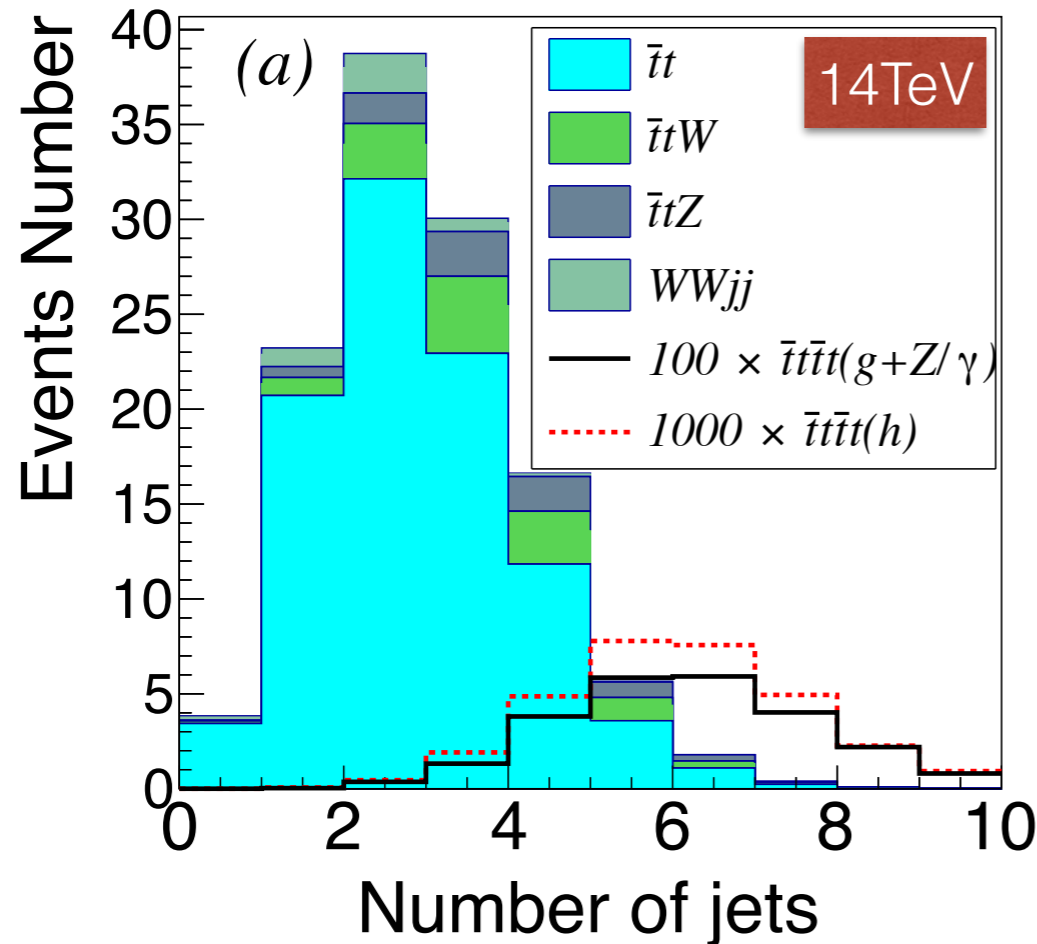
Backgrounds:

$$t\bar{t}Z, t\bar{t}W^\pm, W^\pm W^\pm jj, t\bar{t}$$

$$K_F^{t\bar{t}W^+} = 1.22 \quad K_F^{t\bar{t}W^-} = 1.27 \quad K_F^{t\bar{t}Z} = 1.49 \quad K_F^{W^+W^+jj} = 0.9 \quad K_F^{t\bar{t}} = 1.4 \quad @14\text{TeV}$$

# Collider simulation

Event Topology: **same-sign charged leptons plus multi-jet (b-jet)**



Not adequate to claim a discovery of  $\kappa_t$  at LHC but could set a bound

14 TeV:  $\kappa_t \leq 1.34$  ( $300 \text{ fb}^{-1}$ )

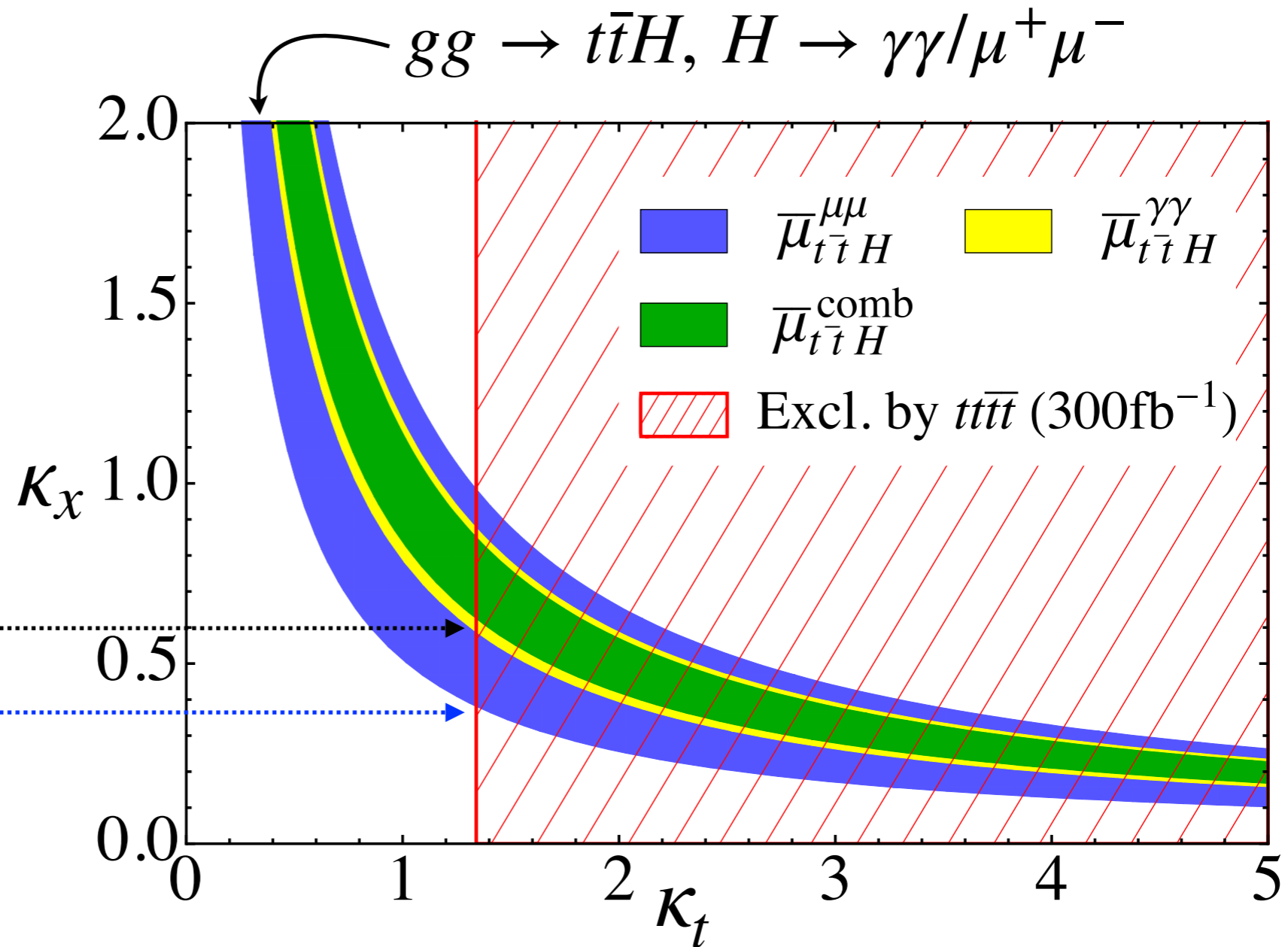
27 TeV:  $\kappa_t \leq 1.17$  ( $10 \text{ ab}^{-1}$ ),  $\kappa_t \leq 1.14$  ( $20 \text{ ab}^{-1}$ ),  $\kappa_t \leq 1.12$  ( $30 \text{ ab}^{-1}$ )

100 TeV: easy to reach a  $5\sigma$  discovery  $\rightarrow$  precision measurement

# Scenario-I : $\kappa_t^2 \kappa_X^2 = \mu_{t\bar{t}H}^X$

Assume  
 $\Gamma_H = \Gamma_H^{\text{SM}}$   
 rare decays

**14TeV LHC  
 (300fb<sup>-1</sup>)**  
 $\kappa_t \leq 1.34$



$$\kappa_{\gamma\gamma} \geq 0.59$$

$$\kappa_{\mu\mu} \geq 0.38$$

**Lower** bounds  
 on rare decays

$$\mu_{t\bar{t}H}^{\gamma\gamma} = 1.00 \pm 0.38$$

$$\mu_{t\bar{t}H}^{ZZ} = 1.00 \pm 0.49$$

$$\mu_{t\bar{t}H}^{\mu\mu} = 1.00 \pm 0.74$$

$$\mu_{t\bar{t}H}^{\text{combo}} = 1.00 \pm 0.30$$

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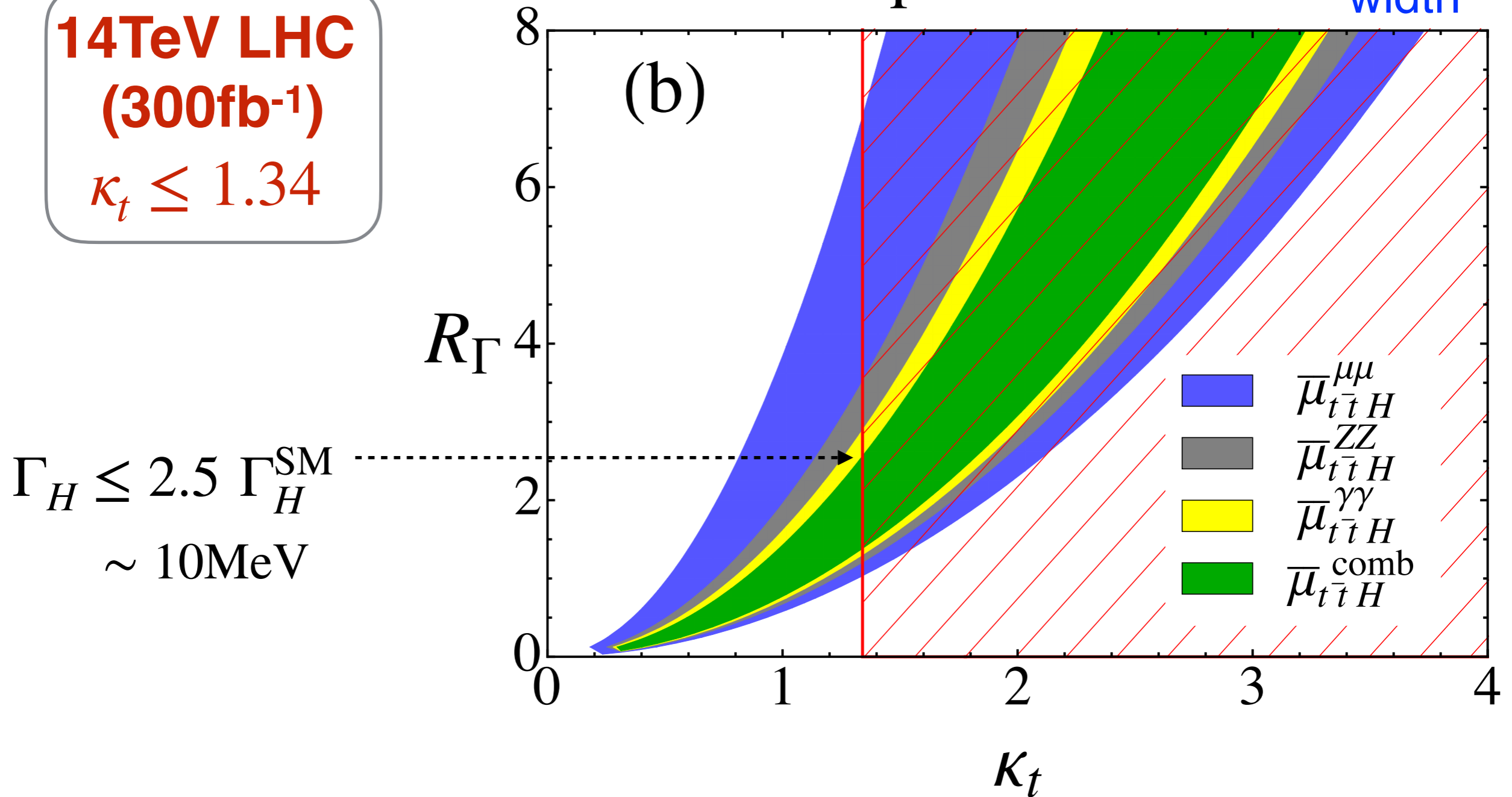
14TeV LHC, 300fb<sup>-1</sup>

# Scenario-II :

$$\frac{\kappa_t^2}{R_\Gamma} = \mu_{t\bar{t}H}$$

Assume  
 $\kappa_X \simeq 1$   
 Invisible  
 width

**14TeV LHC  
 (300fb<sup>-1</sup>)  
 $\kappa_t \leq 1.34$**

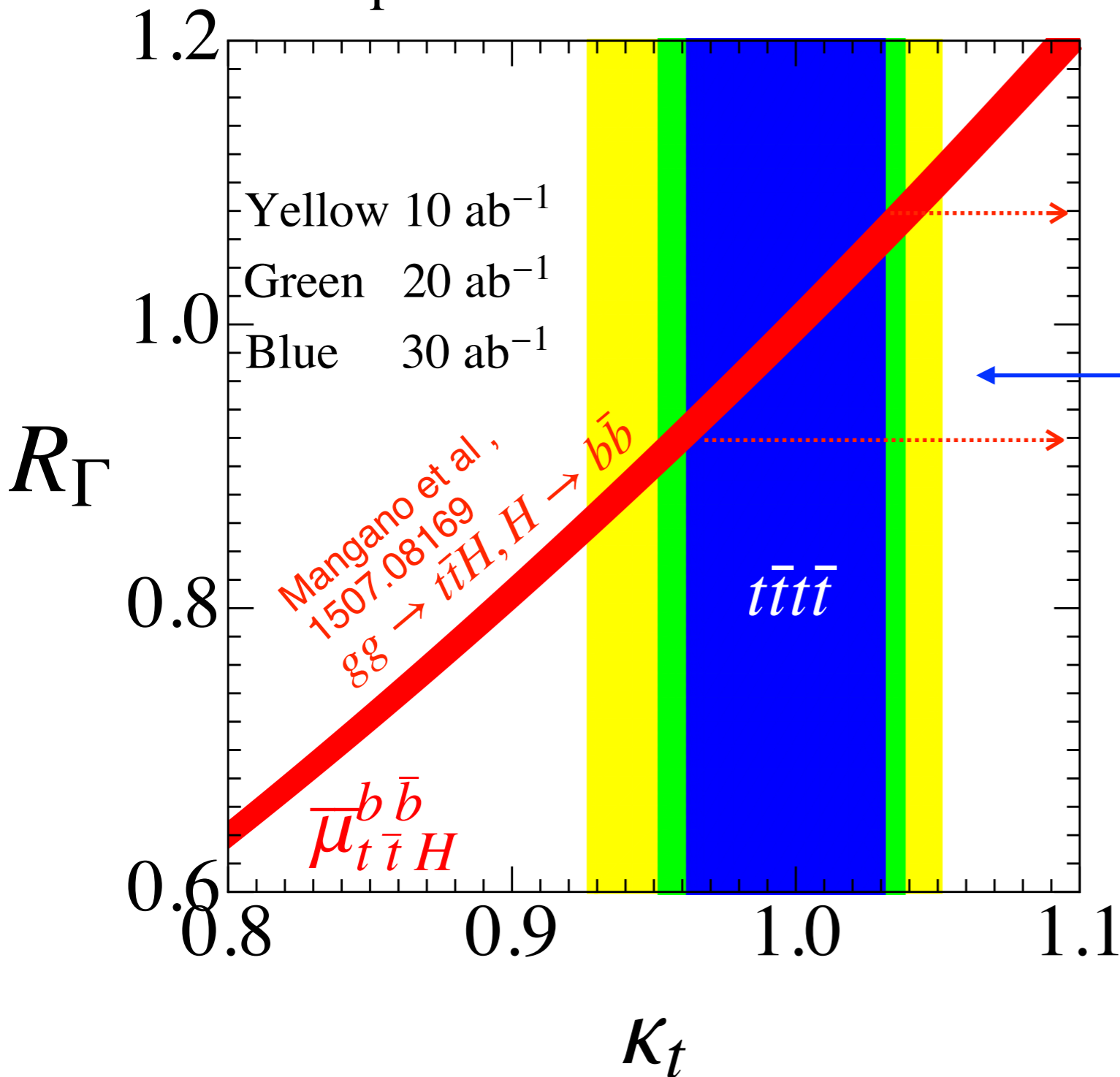


$\mu_{t\bar{t}H}^{\gamma\gamma} = 1.00 \pm 0.38$	$\mu_{t\bar{t}H}^{ZZ} = 1.00 \pm 0.49$	ATLAS-PHYS-PUB-2014-016 14TeV LHC, 300fb <sup>-1</sup>
$\mu_{t\bar{t}H}^{\mu\mu} = 1.00 \pm 0.74$	$\mu_{t\bar{t}H}^{\text{combo}} = 1.00 \pm 0.30$	

# Potential at the 100TeV FCC-HH/SppC

$$\frac{\kappa_t^2}{R_\Gamma} = \mu_{t\bar{t}H} \quad \kappa_b = 1$$

FCC-HH report, 1606.09408



Four-top production reaches 5sigma discovery with an integrated luminosity of  $9\text{fb}^{-1}$ .

Top Yukawa coupling precision (stat. uncertainty only)

$$\mathcal{L} = 30 \text{ ab}^{-1}$$

$$0.91 \Gamma_H^{\text{SM}} \leq \Gamma_H \leq 1.08 \Gamma_H^{\text{SM}}$$

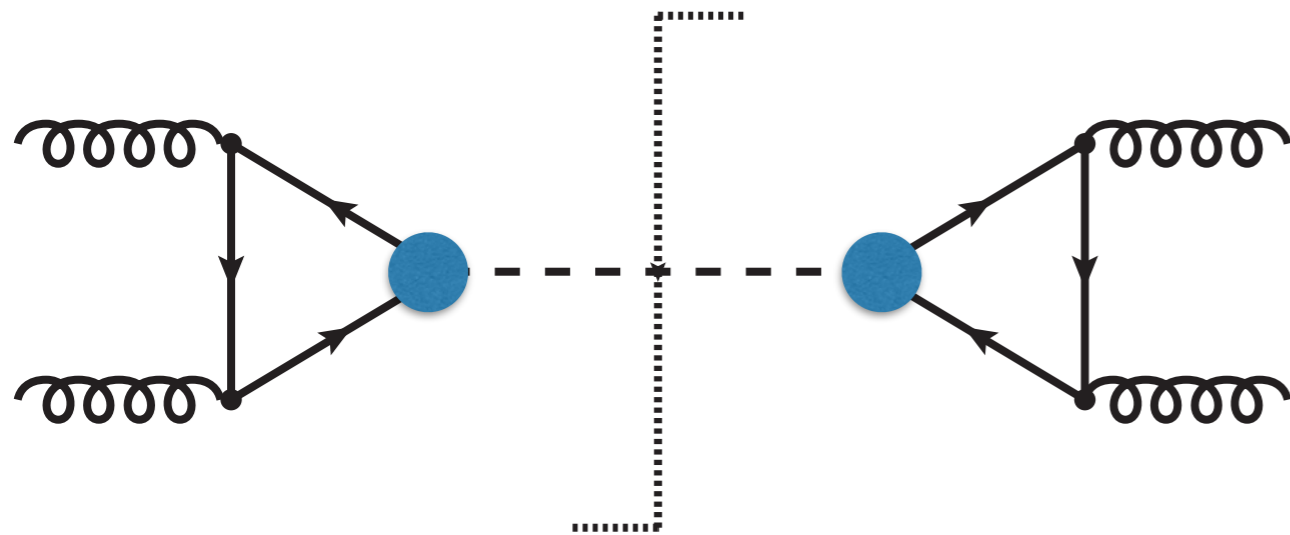
$$0.962 \leq \kappa_t \leq 1.031$$



# Q3: CP property of top-Higgs interaction

$$\mathcal{L}_{Ht\bar{t}} = -\frac{m_t}{v} H\bar{t}(a_t + ib_t\gamma_5)t$$

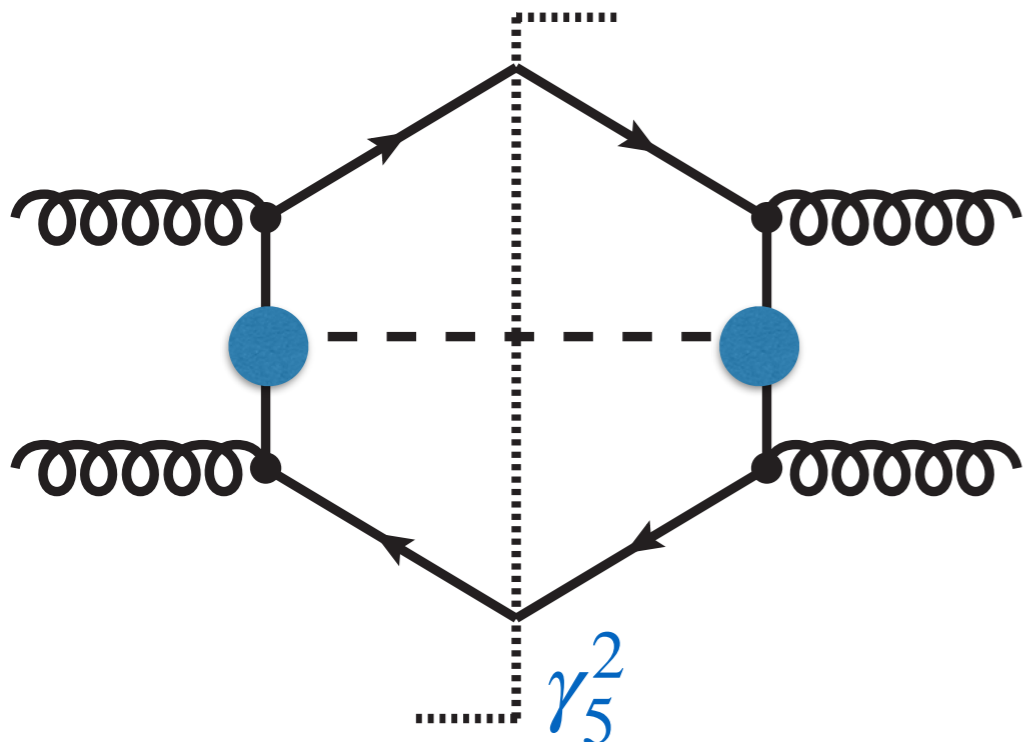
Boudjema, Godbole,  
Guadagnoli, Mohan,  
1501.03157



$$\text{Tr}(\cdots\gamma_5)\text{Tr}(\cdots\gamma_5)$$

$$\frac{\sigma(gg \rightarrow H)}{\sigma(gg \rightarrow H)_{\text{SM}}} \sim a_t^2 + 2.29b_t^2$$

↑  
pseudo-scalar  
dominates



$$\frac{\sigma(gg \rightarrow t\bar{t}H)}{\sigma(gg \rightarrow t\bar{t}H)_{\text{SM}}} \sim a_t^2 + 0.42b_t^2 \quad (14\text{TeV})$$

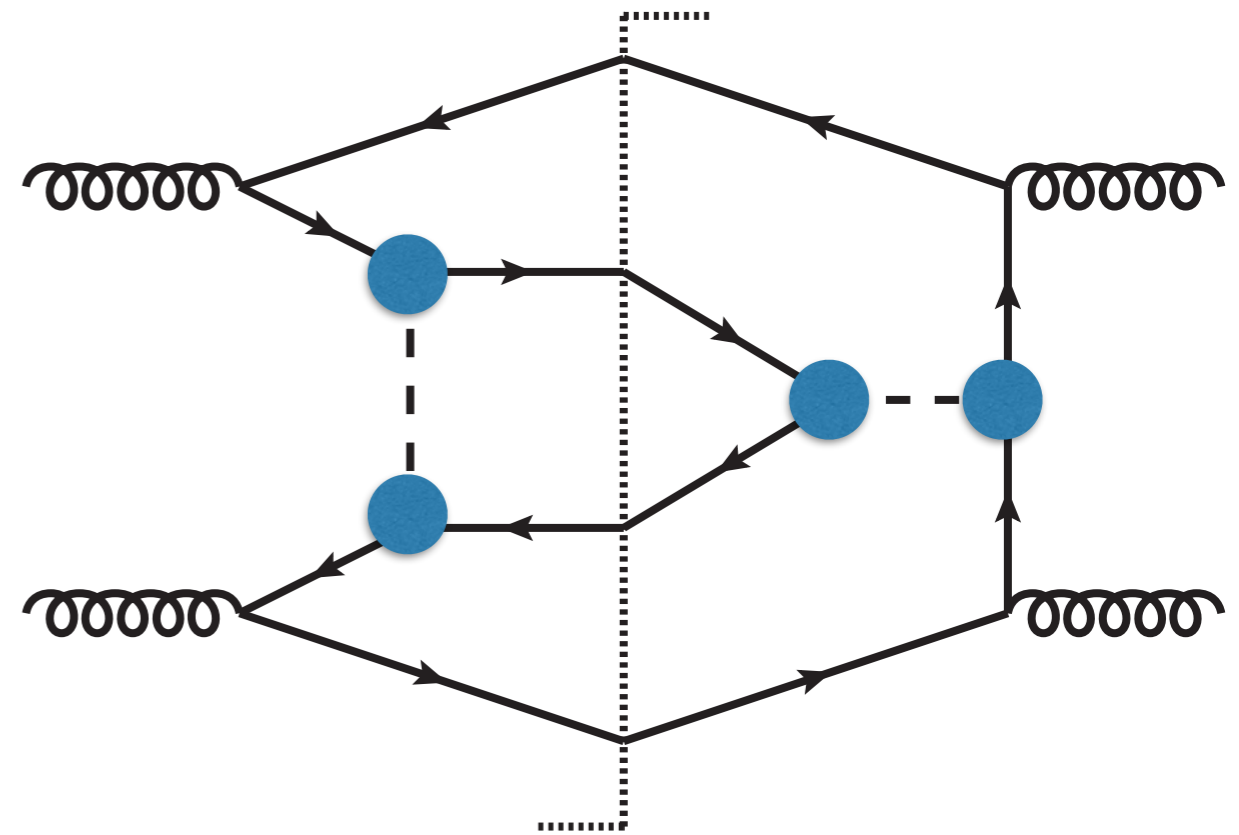
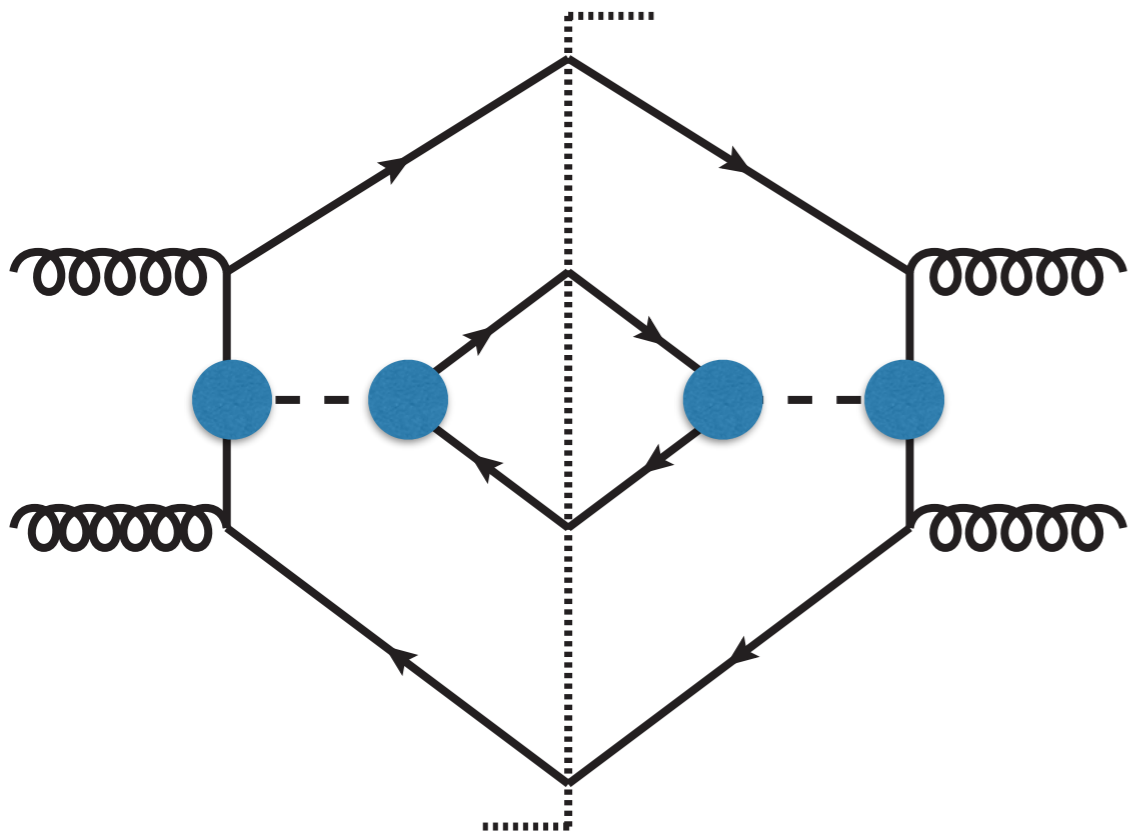
$$\sim a_t^2 + 0.31b_t^2 \quad (8\text{TeV})$$

↑  
scalar dominates

# CP property of top-Higgs interaction

$$\mathcal{L}_{Ht\bar{t}} = -\frac{m_t}{v} H\bar{t}(a_t + ib_t\gamma_5)t$$

Four top-quark production ( $gg \rightarrow t\bar{t}t\bar{t}$ ) is complicated.



$$\sigma(t\bar{t}t\bar{t})_{g+H} \propto \#a_t^4 + \#a_t^2b_t^2 + \#b_t^4 + \#a_t^2 + \#b_t^2 + \#$$

# CP property of top-Higgs interaction

$$\mathcal{L}_{Ht\bar{t}} = -\frac{m_t}{v} H\bar{t}(a_t + ib_t\gamma_5)t$$

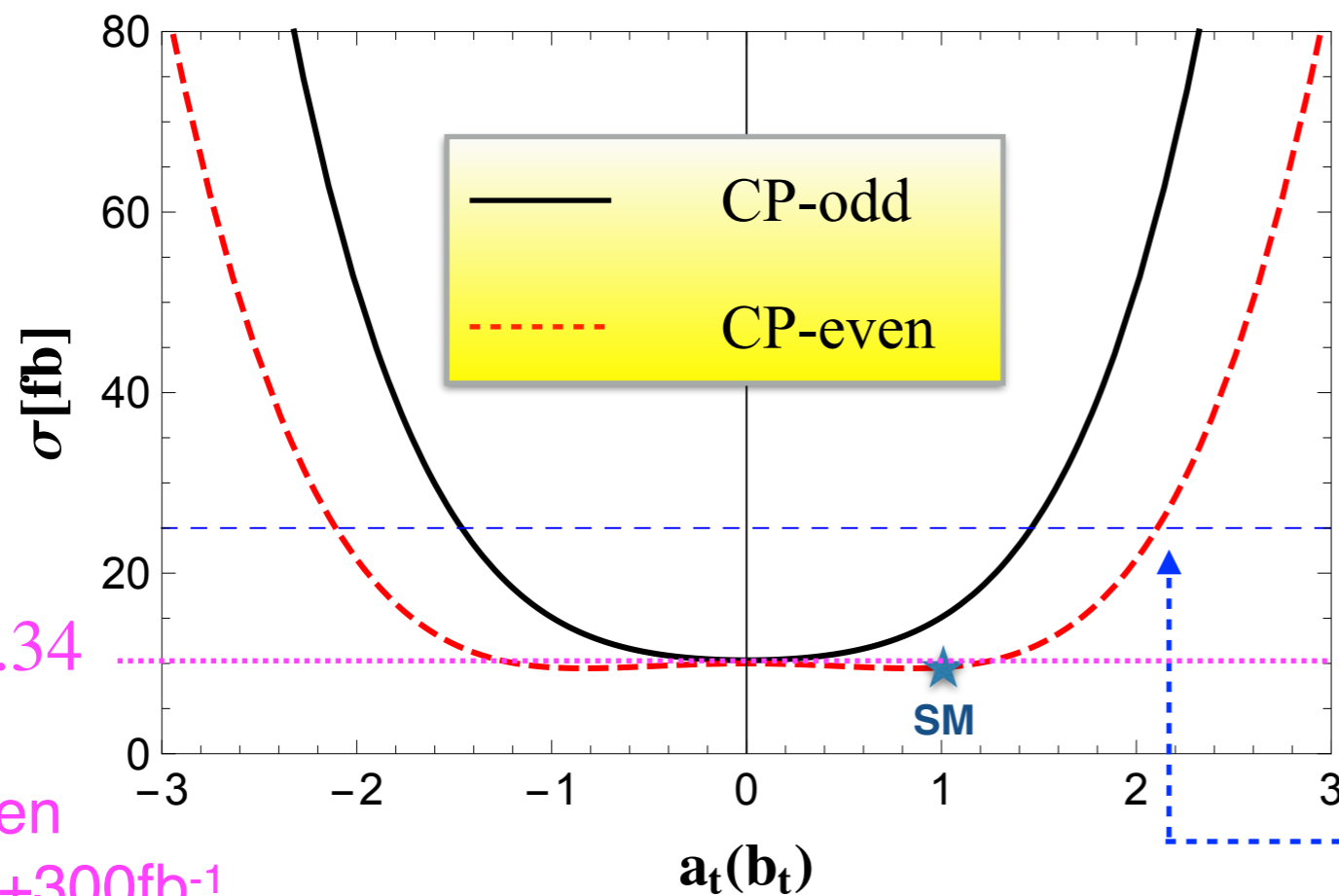
in preparation  
@13TeV

CP-odd  
(a=0, b=1)

$$\sigma(t\bar{t}t\bar{t}) = 9.997 + 2.807 \times b_t^2 + 1.788 \times b_t^4 \text{ (fb)}$$

CP-even  
(a=1, b=0)

$$\sigma(t\bar{t}t\bar{t}) = 9.997 - 1.547 \times a_t^2 + 1.108 \times a_t^4 \text{ (fb)}$$



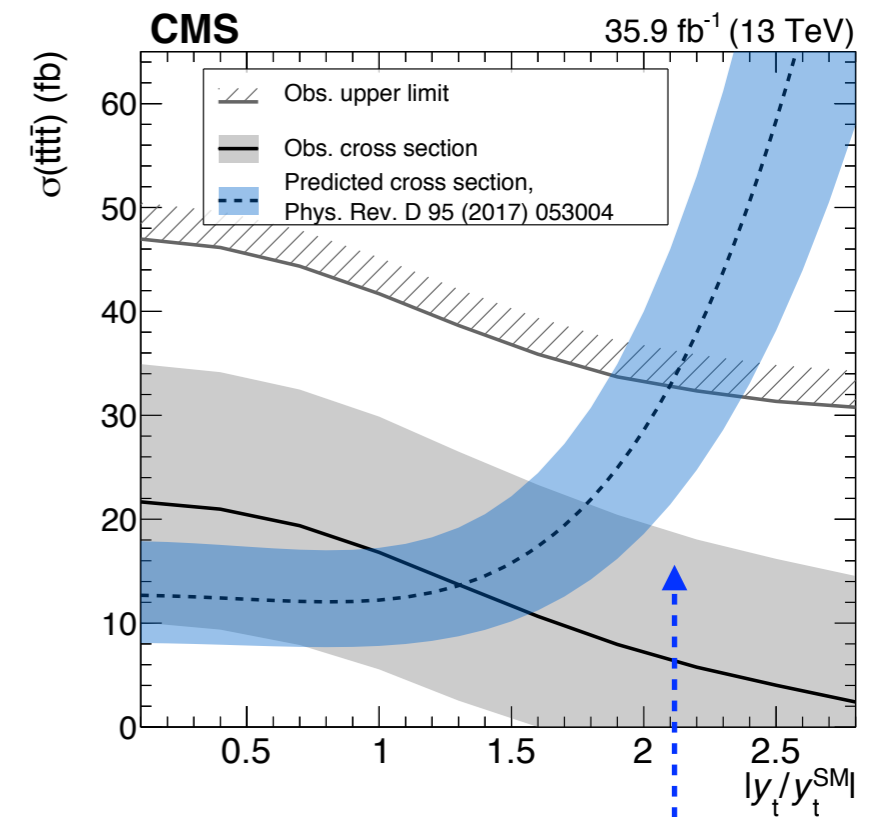
$\kappa_t \leq 1.34$

CP-even  
14TeV+300fb<sup>-1</sup>

almost rule out  
pure CP-odd

Rough estimation:

$b_t \leq 1.5$  for a pure CP-odd coupling



$\kappa_t \leq 2.1$

CP-even

# Summary

The four top-quark production can constrain the top Yukawa coupling without any assumptions on Higgs boson width or decay branching ratios.

The four top-quark production is sensitive to the CP property of top-Higgs interaction.

Combining  $t\bar{t}t\bar{t}$  production and  $t\bar{t}h$  production could constrain  $H\gamma\gamma/H\mu^+\mu^-$  couplings or  $\Gamma_H$ .

$$\begin{array}{l} gg \rightarrow Ht\bar{t}, H \rightarrow \gamma\gamma/\mu\mu \xrightarrow{\Gamma_H = \Gamma_H^{\text{SM}}} g_{H\gamma\gamma} / Y_\mu \\ gg \rightarrow Ht\bar{t}, H \rightarrow b\bar{b} \xrightarrow{y_b = y_b^{\text{SM}}} \Gamma_H \end{array}$$

*Thank You!*