

11<sup>th</sup> International Workshop on Top Quark Physics  
September 19, 2018

## Extraction of top quark mass and strong coupling constant from inclusive $t\bar{t}$ cross section

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on behalf of the CMS Collaboration

calculations of  $t\bar{t}$  production depend on:

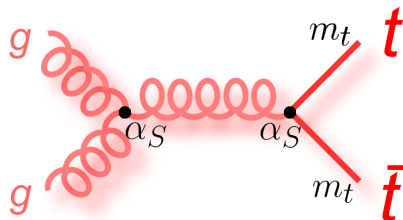
- ① strong coupling  $\alpha_S$
- ② top quark mass  $m_t$
- ③ gluon (quark) PDF in the proton

→ measurements of  $\sigma_{t\bar{t}}$  can be used to constrain these parameters

### strong coupling

- $\alpha_S$  known with sub-percent precision
- significant contribution to uncertainty for several QCD predictions
- can be measured at NNLO from  $\sigma_{t\bar{t}}$  (at NLO from hadronic production)

→ **NB:**  $\alpha_S$  and  $m_t$  cannot be determined simultaneously from inclusive  $\sigma_{t\bar{t}}$



### top quark mass

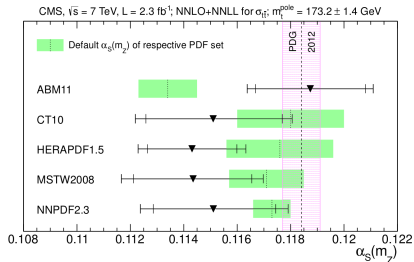
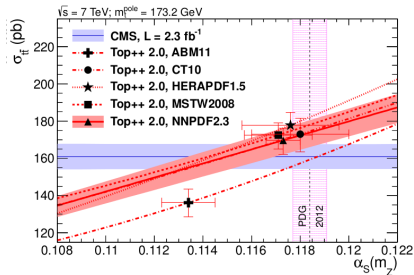
- consistency test of Standard Model
- can be determined in well defined scheme ( $\overline{\text{MS}}$ , on-shell) from  $\sigma_{t\bar{t}}$  (see [talk](#) by Paolo Nason)
- avoid interpretation problems of  $m_t^{\text{MC}}$  (see [talk](#) by André Hoang)

# determination of $\alpha_S(M_Z)$ from $\sigma_{t\bar{t}}$ at 7 TeV

Phys. Lett. B 728 (2013) 496

- using CMS measurement at 7 TeV in dilepton channel with  $2.3 \text{ fb}^{-1}$ , 4.1% accuracy (JHEP 11 (2012) 067)
- theory prediction with Top++2.0, NNLO+NNLL precision
- several different PDF sets considered
- $\alpha_S(M_Z)$  varied consistently in calculation and PDF
- experimental dependence of  $\sigma_{t\bar{t}}$  on  $\alpha_S(M_Z)$  found to be negligible
- assumed  $m_t^{\text{pole}} = 173.2 \pm 1.4 \text{ GeV}$  (Tevatron average  $\oplus 1 \text{ GeV}$  to account for difference between  $m_t^{\text{pole}}$  and  $m_t^{\text{MC}}$ )

$$\alpha_S(M_Z) = 0.1151^{+0.0028}_{-0.0027} \quad (\text{NNPDF2.3})$$



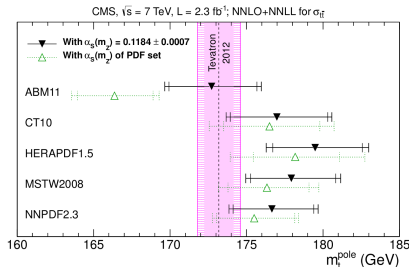
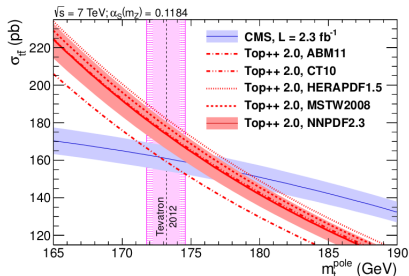
Phys. Lett. B 728 (2013) 496

- same procedure used to extract  $m_t^{\text{pole}}$
- assumed world average strong coupling:  $\alpha_S(M_Z) = 0.1184 \pm 0.0007$
- measured  $\sigma_{t\bar{t}}$  depends on  $m_t^{\text{MC}}$  through acceptance corrections
- effect has to be taken into account

**assumption:**  $m_t^{\text{pole}} = m_t^{\text{MC}} \pm 1 \text{ GeV}$

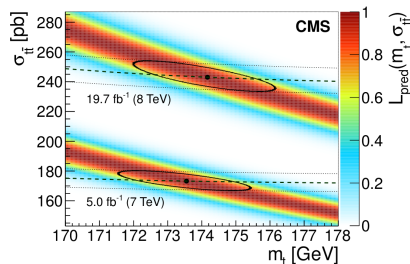
- additional uncertainty corresponding to 1 GeV added to measured  $\sigma_{t\bar{t}}$

$$m_t^{\text{pole}} = 176.7^{+3.0}_{-2.8} \text{ GeV} \quad (\text{NNPDF2.3})$$



JHEP 08 (2016) 029

- simultaneous measurement of  $\sigma_{t\bar{t}}$  at 7 and 8 TeV with template fit of final state distributions
- similar  $m_t^{\text{pole}}$  determination as in 7 TeV measurement
- $m_t^{\text{pole}}$  determined separately from  $\sigma_{t\bar{t}}$  at 7 and 8 TeV
- results combined taking correlations into account



	$m_t$ [ GeV ]
NNPDF3.0	$173.8^{+1.7}_{-1.8}$
MMHT2014	$174.1^{+1.8}_{-2.0}$
CT14	$174.3^{+2.1}_{-2.2}$

	$m_t$ [ GeV ]	
	7 TeV	8 TeV
NNPDF3.0	$173.5^{+1.9}_{-2.0}$	$174.2^{+2.0}_{-2.2}$
MMHT2014	$173.9^{+2.0}_{-2.1}$	$174.4^{+2.1}_{-2.3}$
CT14	$174.1^{+2.2}_{-2.4}$	$174.6^{+2.3}_{-2.5}$

- simultaneous fit of  $\sigma_{t\bar{t}}$  and  $m_t^{\text{MC}}$
- $\sigma_{t\bar{t}}$  determined at **optimal mass point**

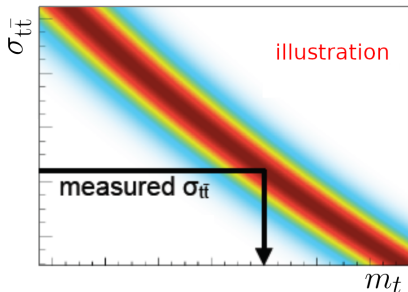
→ see my [talk](#) on Monday

- dependence of  $\sigma_{t\bar{t}}$  on  $m_t^{\text{MC}}$  mitigated
- uncertainty on  $\sigma_{t\bar{t}}$  includes contribution from  $m_t^{\text{MC}}$
- no assumption on relation between  $m_t^{\text{MC}}$  and  $m_t$  needs to be made

## calculations of $\sigma_{t\bar{t}}$

- Hathor2.0 at NNLO precision
- several NNLO PDF sets considered
- $\overline{\text{MS}}$  scheme adopted for  $m_t$ 
  - faster perturbative convergence (see [EPJC 74 \(2014\) 11 3167](#))
- soft gluon resummation not included

PRL 116 (2016) 16 162001



CMS-PAS-TOP-17-001

## measurement results

$$\sigma_{t\bar{t}} = 815 \pm 2 \text{ (stat)} \pm 29 \text{ (syst)} \pm 20 \text{ (lum)} \text{ pb}$$

$$m_t^{\text{MC}} = 172.33 \pm 0.14 \text{ (stat)} \pm_{0.72}^{0.66} \text{ (syst)} \text{ GeV}$$

## CMS-PAS-TOP-17-001

parameters determined from data/theory  $\chi^2$

$\alpha_S$  and  $m_t$  cannot be determined simultaneously

$\Rightarrow m_t$  fixed to native value of PDF

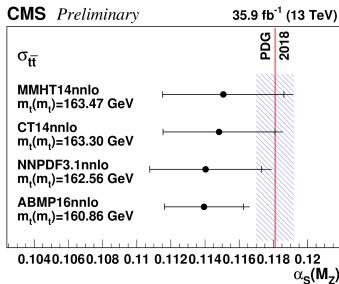
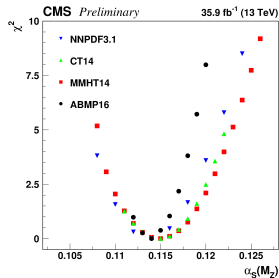
### uncertainties

- experimental: from  $\sigma_{t\bar{t}}$  measurement
- PDF: from eigenvectors
- scale:  $\mu_r$  and  $\mu_f$  variations by factor of 2

### results

- challenging precision on  $\alpha_S(M_Z)$ , most precise from  $\sigma_{t\bar{t}}$  to date
- better precision with ABMP16

$$\alpha_S(M_Z) = 0.1139^{+0.0027}_{-0.0023} \quad (\text{ABMP16})$$



## CMS-PAS-TOP-17-001

parameters determined from data/theory  $\chi^2$

$\alpha_S$  and  $m_t$  cannot be determined simultaneously

$\Rightarrow m_t$  fixed to native value of PDF

### uncertainties

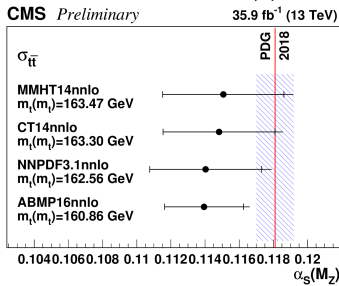
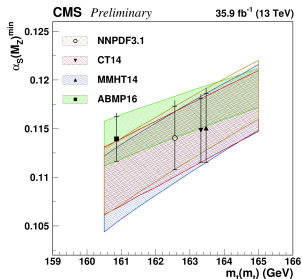
- experimental: from  $\sigma_{t\bar{t}}$  measurement
- PDF: from eigenvectors
- scale:  $\mu_r$  and  $\mu_f$  variations by factor of 2

### results

- dependence of extracted  $\alpha_S$  vs  $m_t$  investigated  $\rightarrow$  linear
- somehow flatter in case of ABMP16

### cross-check

- cross-checked with Top++ (on-shell) as in [EPJC 77 \(2017\) 11 778](#)
- comparable results obtained





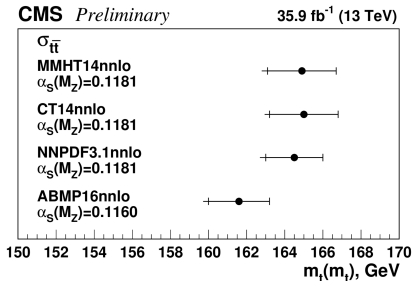
## CMS-PAS-TOP-17-001

- same procedure used to extract top mass in  $\overline{\text{MS}}$  scheme,  $m_t(m_t)$
- $\alpha_S(M_Z)$  fixed at native values of PDF

### results

- most precise direct determination of  $m_t(m_t)$ , to date
- lower  $m_t$  result with ABMP16 due to lower  $\alpha_S(M_Z)$  in PDF determination

$$m_t(m_t) = 161.6^{+1.6}_{-1.9} \text{ GeV (ABMP16)}$$



# extraction of $m_t(m_t)$ from $\sigma_{t\bar{t}}$ at 13 TeV

CMS-PAS-TOP-17-001

- same procedure used to extract top mass in  $\overline{MS}$  scheme,  $m_t(m_t)$
- $\alpha_S(M_Z)$  fixed at native values of PDF

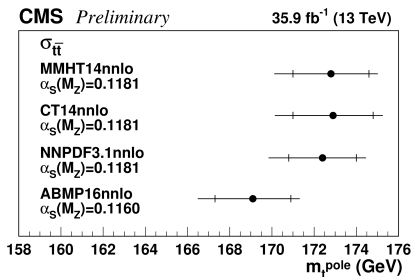
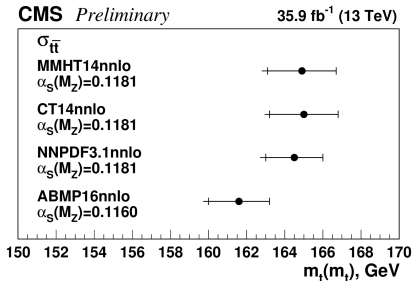
## results

- most precise direct determination of  $m_t(m_t)$ , to date
- lower  $m_t$  result with ABMP16 due to lower  $\alpha_S(M_Z)$  in PDF determination

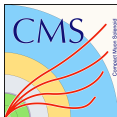
$$m_t(m_t) = 161.6^{+1.6}_{-1.9} \text{ GeV (ABMP16)}$$

## pole mass $m_t^{\text{pole}}$

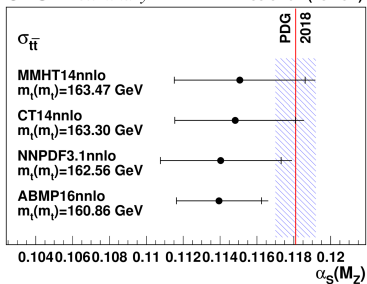
- results consistent with previous measurements
- uncertainties not competitive (scale) due to missing NNLL corrections



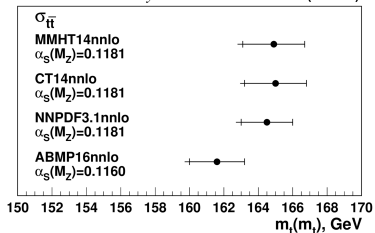
# Thank you for your attention



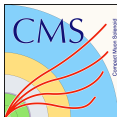
CMS Preliminary 35.9 fb<sup>-1</sup> (13 TeV)

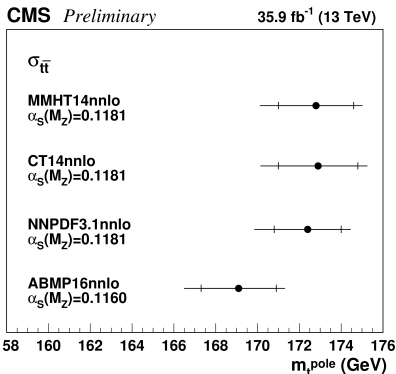


CMS Preliminary 35.9 fb<sup>-1</sup> (13 TeV)

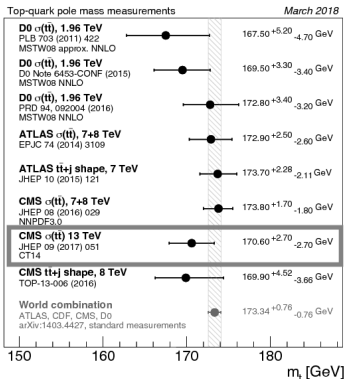


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$$m_t^{\text{pole}} = 172.9^{+2.4}_{-2.8} \text{ GeV} \quad (\text{CT14})$$



- results consistent with previous measurements at Tevatron and LHC

top quark mass in  $\overline{\text{MS}}$  scheme

PDF set (NNLO)	$\alpha_S^{\text{min}}(M_Z)$
ABMP16	$0.1139 \pm 0.0023$ (fit + PDF) $^{+0.0014}_{-0.0001}$ (scale)
NNPDF3.1	$0.1140 \pm 0.0033$ (fit + PDF) $^{+0.0021}_{-0.0002}$ (scale)
CT14	$0.1148 \pm 0.0032$ (fit + PDF) $^{+0.0018}_{-0.0002}$ (scale)
MMHT14	$0.1151 \pm 0.0035$ (fit + PDF) $^{+0.0020}_{-0.0002}$ (scale)

## top quark mass in on-shell scheme

PDF set (NNLO)	$\alpha_S^{\text{min}}(M_Z)$
ABMP16	$0.1164 \pm 0.0021$ (fit + PDF) $^{+0.0024}_{-0.0014}$ (scale)
NNPDF3.1	$0.1184 \pm 0.0027$ (fit + PDF) $^{+0.0037}_{-0.0021}$ (scale)
CT14	$0.1186 \pm 0.0028$ (fit + PDF) $^{+0.0034}_{-0.0019}$ (scale)
MMHT14	$0.1205 \pm 0.0029$ (fit + PDF) $^{+0.0037}_{-0.0021}$ (scale)

top quark  $\overline{\text{MS}}$  mass

PDF set (NNLO)	$m_t(m_t)$ [GeV]
ABMP16	$161.6 \pm 1.6$ (fit + PDF + $\alpha_S$ ) $^{+0.1}_{-1.0}$ (scale)
NNPDF3.1	$164.5 \pm 1.5$ (fit + PDF + $\alpha_S$ ) $^{+0.1}_{-1.0}$ (scale)
CT14	$165.0 \pm 1.7$ (fit + PDF) $\pm 0.6$ ( $\alpha_S$ ) $^{+0.1}_{-1.0}$ (scale)
MMHT14	$164.9 \pm 1.7$ (fit + PDF) $\pm 0.5$ ( $\alpha_S$ ) $^{+0.1}_{-1.1}$ (scale)

## top quark pole mass

PDF set (NNLO)	$m_t^{\text{pole}}$ [GeV]
ABMP16	$169.1 \pm 1.8$ (fit + PDF + $\alpha_S$ ) $^{+1.3}_{-1.9}$ (scale)
NNPDF3.1	$172.4 \pm 1.6$ (fit + PDF + $\alpha_S$ ) $^{+1.3}_{-2.0}$ (scale)
CT14	$172.9 \pm 1.8$ (fit + PDF) $\pm 0.7$ ( $\alpha_S$ ) $^{+1.4}_{-2.0}$ (scale)
MMHT14	$172.8 \pm 1.7$ (fit + PDF) $\pm 0.6$ ( $\alpha_S$ ) $^{+1.3}_{-2.0}$ (scale)

CMS-PAS-TOP-17-001

PDF set (NNLO)	ABMP16	NNPDF3.1	CT14	MMHT14
$m_t^{\text{pole}}$	170.37 GeV	172.5 GeV	173.3 GeV	174.2 GeV
RunDec conversion	3 loops	2 loops	2 loops	3 loops
$m_t(m_t)$	160.86 GeV	162.56 GeV	163.30 GeV	163.47 GeV
$\alpha_S(m_Z)$	0.116	0.118	0.118	0.118
$\alpha_S$ range	0.112–0.120	0.108–0.124	0.111–0.123	0.108–0.128