

B_c at LHC

B_c ATLAS Workshop, CERN

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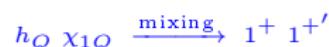
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B_c properties

B_c family have a spectroscopy similar to $c\bar{c}$ or $b\bar{b}$ quarkonium spectroscopy and decays like B meson

- ➊ All excitations below the threshold decay to the ground state 1^1S_0 .
- ➋ The absence of strong annihilation channels leads the very narrow ground state (practically as B -meson).
- ➌ Spectroscopy can be investigated within the same frame work as for $c\bar{c}$ and $b\bar{b}$ quarkoniums.
- ➍ The small total yield comparing to the $c\bar{c}$ and $b\bar{b}$ quarkonia case.
- ➎ The small relative yield of P -wave excitations comparing to the $c\bar{c}$ and $b\bar{b}$ quarkonia case.

- ➏ The main difference in decays (comparing to B meson): the both quarks in B_c are heavy.
- ➐ The main difference in spectroscopy (comparing to $c\bar{c}$ and $b\bar{b}$ quarkonia): charge parity can not be determined.



$$|2P, 1^{' +}\rangle = 0.294|S = 1\rangle + 0.956|S = 0\rangle$$

$$|2P, 1^+ \rangle = 0.956|S = 1\rangle - 0.294|S = 0\rangle$$

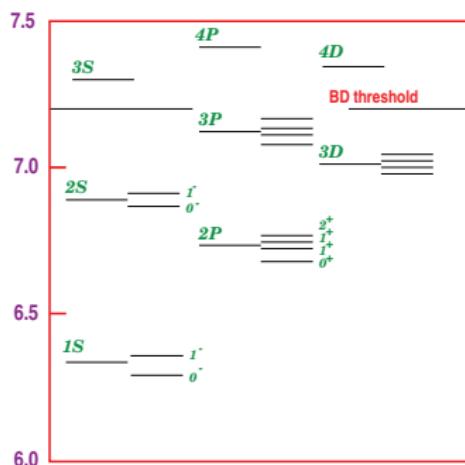
$$|3P, 1^{' +}\rangle = 0.371|S = 1\rangle + 0.929|S = 0\rangle$$

$$|3P, 1^+ \rangle = 0.929|S = 1\rangle - 0.371|S = 0\rangle$$

[Kiselev et al.(1995) Kiselev, Likhoded, and Tkabladze,
Gershtein et al.(1995) Gershtein, Kiselev, Likhoded, and Tkabladze]

B_c family

- All excitations below the threshold decay into 1^1S_0 .
- Charge parity can not be determined: $h_Q \chi_{1Q} \xrightarrow{\text{mixing}} 1^+ 1^{+/-}$.



state	Martin	BT
1^1S_0	6.253	6.264
1^3S_1	6.317	6.337
2^1S_0	6.867	6.856
2^3S_1	6.902	6.899
2^1P_0	6.683	6.700
$2P\ 1^+$	6.717	6.730
$2P\ 1^{+/-}$	6.729	6.736
2^3P_2	6.743	6.747
3^1P_0	7.088	7.108
$3P\ 1^+$	7.113	7.135
$3P\ 1^{+/-}$	7.124	7.142
3^3P_2	7.134	7.153
$3D\ 2^-$	7.001	7.009
3^5D_3	7.007	7.005
3^3D_1	7.008	7.012
$3D\ 2^-$	7.016	7.012

Figure 1: The mass spectrum of $(\bar{b}c)$ with account for the spin-dependent splittings.

[Gouz et al.(2004) Gouz, Kiselev, Likhoded, Romanovsky, and Yushchenko, Godfrey(2004)]

B_c decays types

B_c -meson decay types:

- ① the \bar{b} -quark decay with the spectator c -quark
- ② the c -quark decay with the spectator \bar{b} -quark
- ③ the weak annihilation channel ($B_c^+ \rightarrow l^+ \nu_l (c\bar{s}, u\bar{s})$)
- ④ Pauli interference with the c -quark from the initial state ($\bar{b} \rightarrow \bar{c}c\bar{s}$)

The effects of Pauli interference:

Mode	$\Delta\Gamma/\Gamma_0$, %
$B_c^+ \rightarrow \eta_c D_s^+$	-48
$B_c^+ \rightarrow \eta_c D_s^{*+}$	-39
$B_c^+ \rightarrow J/\psi D_s^+$	-53
$B_c^+ \rightarrow J/\psi D_s^{*+}$	-50
$B_c^+ \rightarrow \eta_c D^+$	-38
$B_c^+ \rightarrow \eta_c D^{*+}$	-45
$B_c^+ \rightarrow J/\psi D^+$	-43
$B_c^+ \rightarrow J/\psi D^{*+}$	-46

Γ_0 is width without taking into account the Pauli interference

Inclusive B_c decays within different models:

B_c decay mode	OPE, %	PM, %	SR, %
$\bar{b} \rightarrow \bar{c}l^+\nu_l$	3.9 ± 1.0	3.7 ± 0.9	2.9 ± 0.3
$\bar{b} \rightarrow \bar{c}ud$	16.2 ± 4.1	16.7 ± 4.2	13.1 ± 1.3
$\sum \bar{b} \rightarrow \bar{c}$	25.0 ± 6.2	25.0 ± 6.2	19.6 ± 1.9
$c \rightarrow sl^+\nu_l$	8.5 ± 2.1	10.1 ± 2.5	9.0 ± 0.9
$c \rightarrow sud$	47.3 ± 11.8	45.4 ± 11.4	54.0 ± 5.4
$\sum c \rightarrow s$	64.3 ± 16.1	65.6 ± 16.4	72.0 ± 7.2
$B_c^+ \rightarrow \tau^+\nu_\tau$	2.9 ± 0.7	2.0 ± 0.5	1.8 ± 0.2
$B_c^+ \rightarrow c\bar{s}$	7.2 ± 1.8	7.2 ± 1.8	6.6 ± 0.7

c-quark decays: $\sim 70\%$
weak annihilation: $\sim 20\%$
b-quark decays: $\sim 10\%$

Some theoretical predictions for B_c branchings

Mode	BR, %	Mode	BR, %	Mode	BR, %
$B_c^+ \rightarrow \eta_c e^+ \nu$	0.75	$B_c^+ \rightarrow J/\psi K^+$	0.011	$B_c^+ \rightarrow B_s^0 K^+$	1.06
$B_c^+ \rightarrow \eta_c \tau^+ \nu$	0.23	$B_c^+ \rightarrow J/\psi K^{*+}$	0.022	$B_c^+ \rightarrow B_s^{*0} K^+$	0.37
$B_c^+ \rightarrow \eta'_c e^+ \nu$	0.041	$B_c^+ \rightarrow D^+ \bar{D}^0$	0.0053	$B_c^+ \rightarrow B_s^0 K^{*+}$	-
$B_c^+ \rightarrow \eta'_c \tau^+ \nu$	0.0034	$B_c^+ \rightarrow D^+ \bar{D}^{*0}$	0.0075	$B_c^+ \rightarrow B_s^{*0} K^{*+}$	-
$B_c^+ \rightarrow J/\psi e^+ \nu$	1.9	$B_c^+ \rightarrow D^{*+} \bar{D}^0$	0.0049	$B_c^+ \rightarrow B_s^0 \pi^+$	1.06
$B_c^+ \rightarrow J/\psi \tau^+ \nu$	0.48	$B_c^+ \rightarrow D^{*+} \bar{D}^{*0}$	0.033	$B_c^+ \rightarrow B^0 \rho^+$	0.96
$B_c^+ \rightarrow \psi' e^+ \nu$	0.132	$B_c^+ \rightarrow D_s^+ \bar{D}^0$	0.00048	$B_c^+ \rightarrow B^{*0} \pi^+$	0.95
$B_c^+ \rightarrow \psi' \tau^+ \nu$	0.011	$B_c^+ \rightarrow D_s^+ \bar{D}^{*0}$	0.00071	$B_c^+ \rightarrow B^{*0} \rho^+$	2.57
$B_c^+ \rightarrow D^0 e^+ \nu$	0.004	$B_c^+ \rightarrow D_s^{*+} \bar{D}^0$	0.00045	$B_c^+ \rightarrow B^0 K^+$	0.07
$B_c^+ \rightarrow D^0 \tau^+ \nu$	0.002	$B_c^+ \rightarrow D_s^{*+} \bar{D}^{*0}$	0.0026	$B_c^+ \rightarrow B^0 K^{*+}$	0.015
$B_c^+ \rightarrow D^{*0} e^+ \nu$	0.018	$B_c^+ \rightarrow \eta_c D_s^+$	0.86	$B_c^+ \rightarrow B^{*0} K^+$	0.055
$B_c^+ \rightarrow D^{*0} \tau^+ \nu$	0.008	$B_c^+ \rightarrow \eta_c D_s^{*+}$	0.26	$B_c^+ \rightarrow B^{*0} K^{*+}$	0.058
$B_c^+ \rightarrow B_s^0 e^+ \nu$	4.03	$B_c^+ \rightarrow J/\psi D_s^+$	0.17	$B_c^+ \rightarrow B^+ \bar{K}^0$	1.98
$B_c^+ \rightarrow B_s^{*0} e^+ \nu$	5.06	$B_c^+ \rightarrow J/\psi D_s^{*+}$	1.97	$B_c^+ \rightarrow B^+ \bar{K}^{*0}$	0.43
$B_c^+ \rightarrow B_s^0 \pi^+ \nu$	0.34	$B_c^+ \rightarrow \eta_c D^+$	0.032	$B_c^+ \rightarrow B^{*+} \bar{K}^0$	1.60
$B_c^+ \rightarrow B_s^{*0} e^+ \nu$	0.58	$B_c^+ \rightarrow \eta_c D^{*+}$	0.010	$B_c^+ \rightarrow B^{*+} \bar{K}^{*0}$	1.67
$B_c^+ \rightarrow \eta_c \pi^+$	0.20	$B_c^+ \rightarrow J/\psi D^+$	0.009	$B_c^+ \rightarrow B^+ \pi^0$	0.037
$B_c^+ \rightarrow \eta_c \rho^+$	0.42	$B_c^+ \rightarrow J/\psi D^{*+}$	0.074	$B_c^+ \rightarrow B^+ \rho^0$	0.034
$B_c^+ \rightarrow J/\psi \pi^+$	0.13	$B_c^+ \rightarrow B^0 \pi^+$	16.4	$B_c^+ \rightarrow B^{*+} \pi^0$	0.033
$B_c^+ \rightarrow J/\psi \rho^+$	0.40	$B_c^+ \rightarrow B_s^0 \rho^+$	7.2	$B_c^+ \rightarrow B^{*+} \rho^0$	0.09
$B_c^+ \rightarrow \eta_c K^+$	0.013	$B_c^+ \rightarrow B_s^{*0} \pi^+$	6.5	$B_c^+ \rightarrow \tau^+ \nu_\tau$	1.6
$B_c^+ \rightarrow \eta_c K^{*+}$	0.020	$B_c^+ \rightarrow B_s^{*0} \rho^+$	20.2	$B_c^+ \rightarrow c\bar{s}$	4.9

The applied B_c production model

δ -approximation:

- the matrix element of S wave state production is proportional to the matrix element of $b\bar{c}c\bar{c}$ production timed by S wave function at origin¹,
- \bar{b} and c quark moves with the same velocities,
- \bar{b} and c quarks are in appropriate spin state.

Color model:

- $\bar{b}c$ pair is produced in color singlet.

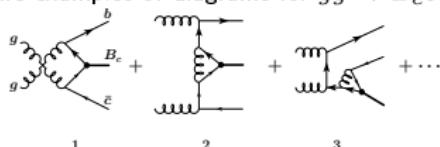
Heavy quark matrix element:

- calculated within leading order of QCD.

¹ For the P wave production the amplitude is proportional to the derivatives of the hard part of amplitudes over internal momentum of quark in quarkonium timed by the derivative of P wave function at origin

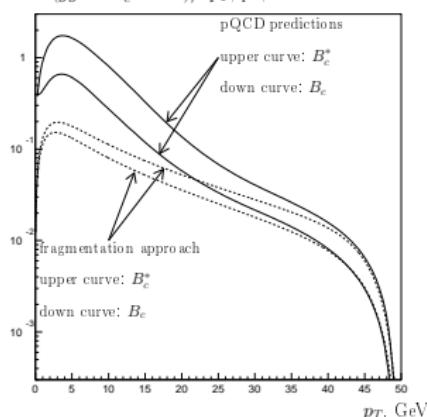
$gg \rightarrow B_c + X$

The examples of diagrams for $gg \rightarrow B_c b\bar{c}$:

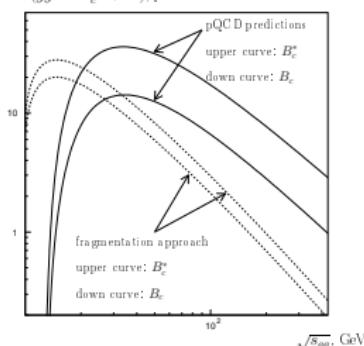


p_T -distribution for $\sqrt{s_{gg}} = 100$ GeV:

$$d\sigma(gg \rightarrow B_c^{(*)} + X)/dp_T, \text{ pb/GeV}$$



$$\sigma(gg \rightarrow B_c^{(*)} + X), \text{ pb}$$



The difference is partially hidden by convolution with PDFs.

For $P_T(B_c) < 35 - 40$ GeV recombination diagrams (such as 1 and 2) dominates and

$$\frac{\sigma(B_c^*)}{\sigma(B_c)} \sim 2.5 \div 3$$

Fragmentation approach is valid for $P_T(B_c) > 35 - 40$ GeV:

$$\frac{\sigma(B_c^*)}{\sigma(B_c)} \sim 1.4$$

What will be observed first: B_c^* or B_c^P ?

$$B_c^*(1^3S_1) \xrightarrow[100\%]{\gamma} B_c(1^1S_0)$$

Seems, that B_c^P family win:

$$\frac{\sigma_{2P}(\omega_T^\gamma > 0.5 \text{ GeV})}{\sigma_{1S}(\omega_T^\gamma > 0.5 \text{ GeV} \iff p_T^{B_c} > 24 \text{ GeV})} \sim 25 \div 50$$

$$M(B_c^*) - M(B_c) \approx 65 \text{ MeV}$$

Maximum transverse energy ω_T of γ in the lab. system:

$$\begin{aligned} \omega_T^{max} &= \left(1 + \frac{\Delta M}{2M_{B_c^*}}\right) \left(\sqrt{M_{B_c^*}^2 + p_T^2} + p_T\right) \frac{\Delta M}{M_{B_c^*}} \\ &\approx 0.01 \left(\sqrt{M_{B_c^*}^2 + p_T^2} + p_T\right) \end{aligned}$$

B_c^* v.s. B_c^P :

- a lot of B_c^* , but high p_T is needed.
- Small amount of B_c^P , but p_T is not essential.

Table : Decays $P \rightarrow 1S + \gamma$

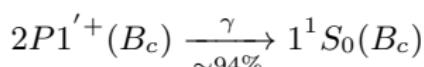
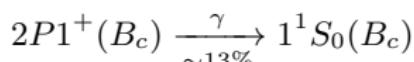
[Godfrey(2004), Gupta and Johnson(1996),

Kiselev et al.(1995) Kiselev, Likhoded, and Tkabladze]

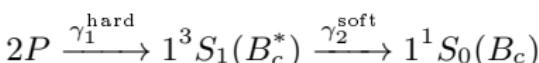
state	decay to 1S	Br, %	ΔM , MeV
2^3P_0	$1^3S_1 + \gamma$	100	363-366
$2P1^+$	$1^3S_1 + \gamma$	87	393-400
	$1^1S_0 + \gamma$	13	393-400
$2P1'^+$	$1^1S_0 + \gamma$	94	472-476
	$1^3S_1 + \gamma$	6	472-476
2^3P_2	$1^3S_1 + \gamma$	100	410-426
3^3P_0	$1^3S_1 + \gamma$	2	741
$3P1^+$	$1^3S_1 + \gamma$	8.5	761
	$1^1S_0 + \gamma$	3.3	820
$3P1'^+$	$1^1S_0 + \gamma$	22.6	825
	$1^3S_1 + \gamma$	0.7	769
3^3P_2	$1^3S_1 + \gamma$	18	778

What to do with the soft photon from B_c^* decay?

Only $\sim 20\%$ of $2P$ -wave states decay radiating only one photon:



In most cases



To find γ_2 the high p_T of B_c^* is needed.

But, it seems that we can see P -wave excitations without the reconstruction of soft γ_2 .

$$\Delta \approx 2 \frac{(M_{B_c(P)} - M_{B_c^*})(M_{B_c^*} - M_{B_c})}{M_{B_c}}$$

width of partially reconstructed B_c^P

$$B_c^P : M_{B_c^P} = M + \Delta M_1 + \Delta M_2$$

$$B_c^* : M_{B_c^*} = M + \Delta M_2$$

$$B_c : M_{B_c} = M$$

$$B_c^P \xrightarrow{\Delta M_1} B_c^* \xrightarrow{\Delta M_2} B_c$$

$$\omega_2 = \left(1 + \frac{\Delta M_2}{2M}\right) \Delta M_2$$

$$\omega_1 = \frac{2M + \Delta M_1}{2M + 2\omega_2(1 - \cos \Theta)} \Delta M_1$$

$$\omega_1^{max} = \left(1 + \frac{\Delta M_1}{2M}\right) \Delta M_1$$

$$\omega_1^{min} = \frac{1 + \frac{\Delta M_1}{2M}}{\left(1 + \frac{\Delta M_2}{M}\right)^2} \Delta M_1$$

\tilde{M} is the mass of $B_c + \gamma_1$ system:

$$\tilde{M}^2 = (M + \omega_1)^2 - \omega_1^2 = M^2 + 2\omega_1 M$$

$$M_{B_c^P}^2 = (M + \Delta M_1 + \Delta M_2)^2 = \\ M^2 + 2(\omega_1 + \omega_2)M + 2\omega_1\omega_2(1 - \cos \Theta)$$

$$\tilde{M}_{max}^2 = (M + \Delta M_1)^2$$

$$M_{B_c^*}^2 = (M + \Delta M_2)^2 = M^2 + 2\omega_2 M$$

$$\tilde{M}_{min}^2 =$$

Θ is the angle between γ_1 and γ_2 in the B_c rest frame.

$$= (M + \Delta M_1)^2 - 4\Delta M_1 \Delta M_2 \frac{\left(1 + \frac{\Delta M_1}{2M}\right) \left(1 + \frac{\Delta M_2}{2M}\right)}{\left(1 + \frac{\Delta M_2}{M}\right)^2}$$

$$\tilde{M}_{max} - \tilde{M}_{min} \approx 2 \frac{\Delta M_1 \Delta M_2}{M}$$

P -wave excitations in $B_c + \gamma$ mass spectrum

Peaks for $2P$ wave excitations ("soft" photon is lost):

- shifted by ~ 65 MeV
- have a width ~ 10 MeV

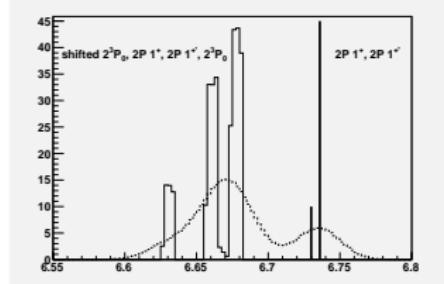
Peaks for $3P$ wave excitations ("soft" photon is lost):

- shifted by ~ 65 MeV
- have a width ~ 20 MeV

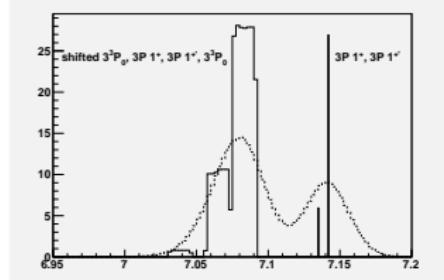
$\sigma(3P) \sim \sigma(2P)$, but only $\sim 20\%$ of $B_c(3P)$ decay electromagnetically into $1^3S_1(B_c^*)$ or $1^1S_0(B_c)$.

ω_T^{\min} , GeV	B_c state	relative yield %
0.3	$B_c(2P)$	~ 5.0
	$B_c(3P)$	~ 1.0
	B_c^*	~ 0.8
0.5	$B_c(2P)$	~ 3.5
	$B_c(3P)$	~ 0.7
	B_c^*	~ 0.06
1.0	$B_c(2P)$	~ 0.9
	$B_c(3P)$	~ 0.4
	B_c^*	~ 0.005

$B_c(2P) \rightarrow B_c + \gamma [+ \gamma_{lost}]$



$B_c(3P) \rightarrow B_c + \gamma [+ \gamma_{lost}]$



$B_c(2S) \rightarrow B_c(B_c^*) + \pi\pi$

$$2^1 S_0(B_c) \xrightarrow[\sim 50\%]{\pi^+ \pi^-} 1^1 S_0(B_c)$$

$$2^3 S_1(B_c) \xrightarrow[\sim 40\%]{\pi^+ \pi^-} 1^3 S_1(B_c)$$

$$\frac{\sigma_{\text{direct}}(B_c(2S))}{(\sigma_{\text{direct}}(B_c(1S)) + \sigma_{\text{direct}}(B_c(2S)))} \sim 15 \div 35 \%$$

$$\sigma(2^3 S_1)/\sigma(2^1 S_0) \sim 2.6$$

Accounting P -wave contributions ($\sim 10 \div 20\%$) one can obtain

$$\mathcal{R} = \frac{\sigma(B_c(2S)) \cdot Br(B_c(2S) \rightarrow B_c \pi^+ \pi^-)}{\sigma_{\text{total}}(B_c)} \sim 6 \div 16\%$$

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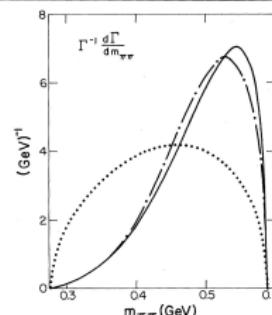


FIG. 1. The decay spectrum $\Gamma^{-1} d\Gamma/dm_{\pi\pi}$ as a function of $m_{\pi\pi}$ given by Eq. (6) (solid line); given by simulating phase space (dotted line); and given by Eq. (6) modified by pion-pion rescattering (dot-dashed line).

[Brown and Cahn (1975), Novikov and Shifman (1981), Voloshin (1975), Voloshin and Zakharov (1980)]

For $2S$ vector, as well as pseudoscalar

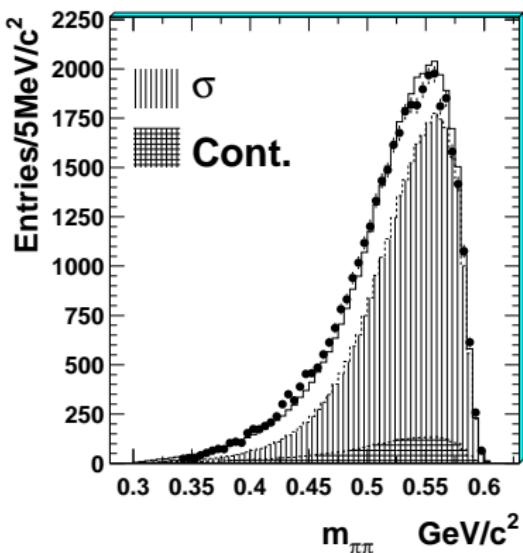
$$\frac{1}{\Gamma} \frac{d\Gamma}{dm_{2\pi}} \sim \frac{|\mathbf{k}_{\pi\pi}|}{M^2} (2x^2 - 1) \sqrt{x^2 - 1}$$

where $x = m_{\pi\pi}/2m_\pi$ and $\mathbf{k}_{\pi\pi}$ is the momentum of $\pi\pi$ -pair in the $B_c(2S)$ rest frame.

$$\langle m_{\pi\pi} \rangle \sim 0.5 \text{ GeV}$$

σ -meson in the quarkonia decays

Distribution over $m_{\pi\pi}$ for the process $\psi' \rightarrow J/\psi\pi\pi$.
The resonance σ ($f_0(500)$) has been included into the fit
(BESII) [Ablikim et al.(2007)].



$f_0(500)$ or σ
 $J^{PC} = 0^{++}$
 $(400 - 550) - i(200 - 350)$ MeB

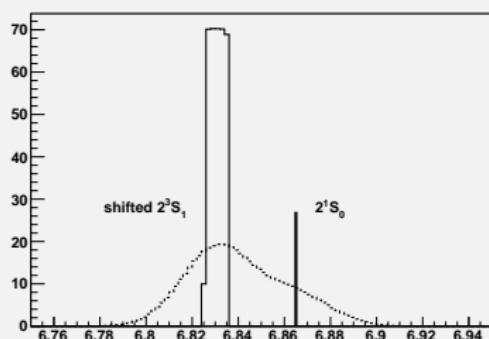
$B_c^*(2S)$ with lost photon

Peak for 2^3S_1 excitation ("soft" photon is lost):

- shifted by ~ 65 MeV \Rightarrow appeared ~ 30 MeV before 2^1S_0
- have a width ~ 10 MeV

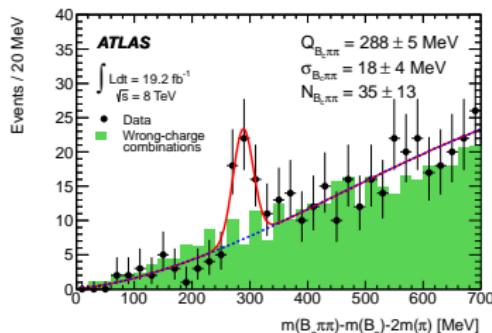
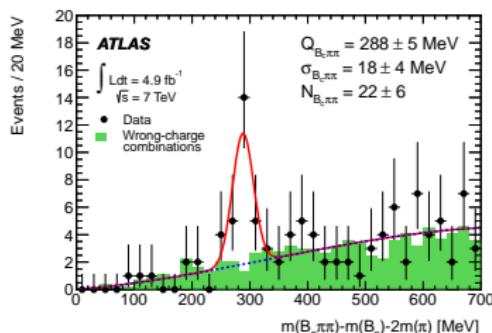
$$\Delta \approx 2 \frac{\sqrt{(M_{B_c^*(2S)} - M_{B_c^*})^2 - 4m_\pi^2} (M_{B_c^*} - M_{B_c})}{M_{B_c}}$$

$B_c(2S) \rightarrow B_c + \pi\pi[+\gamma_{\text{lost}}]$



$B_c(2S)$ results: ATLAS v.s. LHCb

ATLAS Coll. [Aad et al.(2014)]



ATLAS value of \mathcal{R} and LHCb upper limits
[Aaij et al.(2017)]

	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 8 \text{ TeV}$
ATLAS	$(0.22 \pm 0.08)/\varepsilon_7$	$(0.15 \pm 0.06/\varepsilon_8$
LHCb	-	$< [0.04, 0.09]$

- The peak mean value can be interpreted as 2^3S_1 shifted by 65 MeV due to the unreconstructed soft photon ($B_c^*(2S) \rightarrow B_c^* + \pi^+ \pi^-$, $B_c^* \rightarrow B_c + \gamma_{\text{lost}}$).
- It could be supposed, that the peak have a quite large width due to additional contribution from 2^1S_0 .
- ATLAS \mathcal{R} value does not contradict recent LHCb results only if the $\pi^+ \pi^-$ registration efficiency $\varepsilon_8 \sim 1$.

\mathcal{R} dependence on kinematical region I

Dependence on $P^* = \sigma(B_c^*)/(\sigma(B_c) + \sigma(B_c^*))$.

Neglecting mass differences between $1S$ and $2S$ states one can obtain and P -wave state contribution one can obtain that $\sigma_{\text{direct}}(2S)/\sigma_{\text{direct}}(1S) = \text{const}$, but

$$\mathcal{R} \simeq \frac{R_{2S}^2(0)}{R_{1S}^2(0) + R_{2S}^2(0)} \cdot [Br - (Br - Br^*)P^*]$$

$$Br = Br(B_c(2S) \rightarrow \pi^+ \pi^-) \sim 50\%$$

$$Br^* = Br(B_c^*(2S) \rightarrow \pi^+ \pi^-) \sim 40\%$$

$$P^* = \sigma(B_c^*)/(\sigma(B_c) + \sigma(B_c^*))$$

P^* slightly decreases with p_T from ~ 0.72 to ~ 0.58 at very high p_T value, and therefore \mathcal{R} slightly decreases. However this effect to small to be taken into account ($\Delta\mathcal{R} < 1\%$).

Contributions from P -states.

P -states contribute to the total cross section value, have slightly different dependence on p_T , and therefore could influence the \mathcal{R} value (seems, also can be neglected).

Internal motion of quark inside quarkonium.

Taking into internal motion of quark in $1S$ -quarkonium and $2S$ -quarkonium could influence \mathcal{R} dependence. Must be investigated (Done only for B_c -pair production).

\mathcal{R} dependence on kinematical region II

Dependence on mass value.

The predicted cross section strongly depends on choice of mass values.

Within the model $M(B_c(nS)) = m_b + m_c$ and therefore quark mass values in estimation of $\sigma(B_c(2S))$ differ from ones in estimation of $\sigma(B_c(1S))$.

$$M_{B_c}(2S) - M_{B_c}(1S) \approx 0.7 \text{ GeV}$$

Toy Monte-Carlo accounting only $gg \rightarrow B_c + X$ leads to

$$\frac{\frac{\sigma_{\text{direct}}(2S)}{\sigma_{\text{direct}}(1S)} [\text{LHCb}]}{\frac{\sigma_{\text{direct}}(2S)}{\sigma_{\text{direct}}(1S)} [\text{ATLAS}]} \sim 0.7 \div 0.8$$

$$\frac{\mathcal{R}_{\text{LHCb}}}{\mathcal{R}_{\text{ATLAS}}} \sim 0.7 \div 0.8$$

(Does it have a physical meaning?)

Anyway, the relative yields of $B_c(2S)$ at LHCb and at ATLAS should be comparable.

m_{B_c} value should be compared not with \sqrt{s} , but with $\sqrt{\hat{s}_{gg}}$.

$b\bar{b}$ production within FONLL as an example of analogous dependence.

$$\frac{\frac{\sigma_{b\bar{b}}(m_b=5.0 \text{ GeV})}{\sigma_{b\bar{b}}(m_b=4.5 \text{ GeV})} [2.5 < y < 4.5, p_T < 10 \text{ GeV}]}{\frac{\sigma_{b\bar{b}}(m_b=5.0 \text{ GeV})}{\sigma_{b\bar{b}}(m_b=4.5 \text{ GeV})} [-1. < y < 1., p_T > 10 \text{ GeV}]} \sim 0.8$$

It is not the official result of FONLL team!
It is the result of my own exercises with a site
<http://www.lpthe.jussieu.fr/~cacciari/fonll/fonllform.html>

[Cacciari et al.(2012) Cacciari, Frixione, Houdeau, M., and Nason]
[Cacciari et al.(2015) Cacciari, Mangano, and Nason]

Conclusions

- The best chance to be found first in the $M_{B_c} + \gamma$ spectrum belongs to $2P$ excitations.
- If $B_c(2S) \rightarrow B_c(B_c^*) + \pi^+\pi^-$ mode is seen at ATLAS, it should be seen at LHCb.
- New results on $B_c(2S)$ production are needed from ATLAS (full data set of Run-I + Run-II). It is very useful to know the efficiency of $\pi^+\pi^-$ registration.
- New results on $B_c(2S)$ production are needed from CMS.

Thank for your attention!

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B_c production amplitude

$$A^{SJjz} = \int T_{b\bar{b}c\bar{c}}^{Ssz}(p_i, k(\vec{q})) \cdot \left(\Psi_{\bar{b}c}^{Ll_z}(\vec{q}) \right)^* \cdot C_{szl_z}^{Jjz} \frac{d^3\vec{q}}{(2\pi)^3},$$

where $T_{b\bar{b}c\bar{c}}^{Ssz}$ is an amplitude of the hard production of two heavy quark pairs;

$\Psi_{\bar{b}c}^{Ll_z}$ is the quarkonium wave function (color singlet, *in some calculations — color octet*);

J and j_z are the total angular momentum and its projection on z -axis in the B_c rest frame;

L and l_z are the orbital angular momentum of B_c meson and its projection on z -axis;

S and s_z are B_c spin and its projection;

$C_{szl_z}^{Jjz}$ are Clebsch-Gordon coefficients;

p_i are four momenta of B_c meson, b quark and \bar{c} quark;

\vec{q} is three momentum of \bar{b} -quark in the B_c rest frame (in this frame $(0, \vec{q}) = k(\vec{q})$).

Under assumption of small dependence of $T_{b\bar{b}c\bar{c}}^{Ssz}$ on $k(\vec{q})$

$$A \sim \int d^3q \Psi^*(\vec{q}) \left\{ T(p_i, \vec{q})|_{\vec{q}=0} + \vec{q} \frac{\partial}{\partial \vec{q}} T(p_i, \vec{q})|_{\vec{q}=0} + \dots \right\}$$

and, particularly, for the S -wave states

$$A \sim R_S(0) \cdot T_{b\bar{b}c\bar{c}}(p_i)|_{\vec{q}=0},$$

where $R_S(0)$ is a value of radial wave function at origin.

Papers on B_c production

Hadronic S -wave B_c -meson production:

[Chang et al.(2005)Chang, Qiao, Wang, and Wu,
Berezhnoy et al.(1995)Berezhnoy, Likhoded, and Shevlyagin,
Berezhnoy et al.(1997b)Berezhnoy, Kiselev, Likhoded, and Onishchenko,
Kolodziej et al.(1995)Kolodziej, Leike, and Ruckl,
Chang et al.(1995)Chang, Chen, Han, and Jiang, Baranov(1997a),
Baranov(1997b)].

P -wave B_c -meson:

[Berezhnoy et al.(1996)Berezhnoy, Kiselev, and Likhoded,
Berezhnoy et al.(1997a)Berezhnoy, Kiselev, and Likhoded,
Chang et al.(2004)Chang, Wang, and Wu].

Some more papers on B_c production:

[Berezhnoy(2005), Chang et al.(2006)Chang, Wang, and Wu,
Berezhnoy et al.(2011)Berezhnoy, Likhoded, and Martynov,
Chang et al.(2015)Chang, Wang, and Wu].

**First theoretical research of the hadronic four heavy quark production
($gg \rightarrow Q_1\bar{Q}_1Q_2\bar{Q}_2$ and $q\bar{q} \rightarrow Q_1\bar{Q}_1Q_2\bar{Q}_2$):**

[Barger et al.(1991)Barger, Stange, and Phillips]

Fragmentation in e^+e^-

In the special gluonic gauge the only diagram (1) contributes to the cross section at

$$\frac{M_{B_c}^2}{s_{e^+e^-}} \rightarrow 0$$

$$\frac{d\sigma_{B_c}}{dz} = D_{\bar{b} \rightarrow B_c}(z) \cdot \sigma_{b\bar{b}}$$

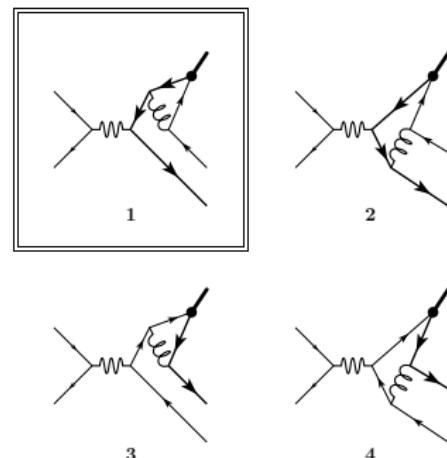
$$D_{\bar{b} \rightarrow B_c^*}(z) =$$

$$\frac{2\alpha^2|R_S(0)|^2}{81\pi m_c^3} \frac{rz(1-z)^2}{(1-(1-r)z)^6} (6 - 18(1-2r)z + (21 - 74r + 68r^2)z^2 - 2(1-r)(6 - 19r + 18r^2)z^3 + 3(1-r)^2(1 - 2r + 2r^2)z^4)$$

$$D_{\bar{b} \rightarrow B_c}(z) =$$

$$\frac{2\alpha^2|R_S(0)|^2}{27\pi m_c^3} \frac{rz(1-z)^2}{(1-(1-r)z)^6} (2 - 2(3 - 2r)z + 3(3 - 2r + 4r^2)z^2 - 2(1-r)(4 - r + 2r^2)z^3 + (1-r)^2(3 - 2r + 2r^2)z^4)$$

$$r = \frac{m_c}{m_c + m_b}$$



[Clavelli(1982), Ji and Amiri(1987),
Amiri and Ji(1987), Chang and Chen(1992a),
Chang and Chen(1992b),
Braaten et al.(1993) Braaten, Cheung, and Yuan,
Kiselev et al.(1994) Kiselev, Likhoded, and Shevlyagin]

The analog of Peterson function

To describe heavy quark hadronization into heavy-light meson the Peterson FF is usually used:

$$D_{Q \rightarrow (Q\bar{q})}(z) \sim \frac{1}{z \left(1 - \frac{1}{z} - \frac{\epsilon}{1-z}\right)^2}.$$

The dependence of "nonperturbative" Peterson FF is partially determined by denominator of perturbative propagator for $Q^* \rightarrow (Q\bar{q}) + X$ process:

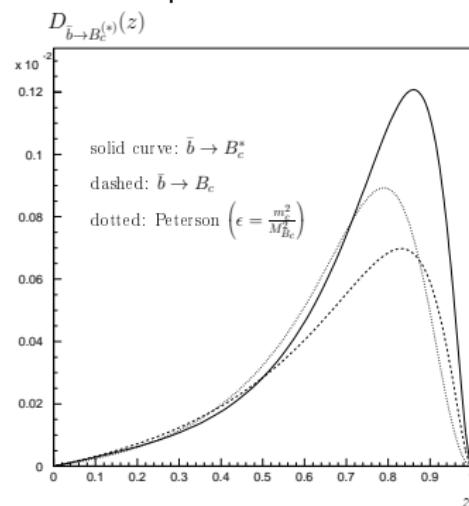
$$m_Q^2 - (P_{(Q\bar{q})} + P_X)^2.$$

$$m_Q^2 - (P_{(Q\bar{q})} + P_X)^2 \approx m_Q^2 - \frac{m_{(Q\bar{q})}^2}{z} - \frac{m_X^2}{1-z}.$$

For $m_Q \approx m_{(Q\bar{q})}$

$$m_Q^2 - (P_{(Q\bar{q})} + P_X)^2 \sim 1 - \frac{1}{z} - \frac{m_X^2}{m_Q^2} \frac{1}{1-z}.$$

FF for $b \rightarrow B_c^{(*)}$ obtained within pQCD vs. Peterson parametrization:



The FFs from the previous slide are used within FONLL to describe $c \rightarrow D$ (r — free parameter).

Additional contributions to B_c hadronic production

Comparable contributions to the B_c production:

- $gg \rightarrow B_c b\bar{c}$
- $\bar{b}(c)g \rightarrow B_c + \bar{c}(b)$
- Pythia gluonic showering $g \rightarrow B_c$.

Small contributions:

- $q\bar{q} \rightarrow B_c b\bar{c}$ (about 10% $gg \rightarrow B_c b\bar{c}$)
- color octet (unessential for B_c inclusive production).

Problems:

- How to avoid double counting?
- How to take into account the mass of $b(\bar{c})$ -quark from the sea in matrix element?
- How to obtain reasonable p_T distribution?

Methods used for b production

- GM-VFNS** General-mass variable-flavor-number scheme (GM-VFNS): The heavy quark is treated as any other massless parton, the mass is taken into account as large logarithms $\ln(p_T/m)$ in parton distribution and fragmentation functions, where they are resummed by imposing DGLAP evolution
[Kniehl et al.(2012)Kniehl, Kramer, Schienbein, and Spiesberger].
- FONLL** NLO (massive quark) + resummation of large logs: at $p_T < 5m_c$ NLO works without logarithm resummation (see eq. 6.1 in [Cacciari et al.(1998)Cacciari, Greco, and Nason]).
- k_T fact.** LO (massive quark) + virtual initial gluons (It seems that sea c quark is not needed) [Baranov et al.(2005)Baranov, Lipatov, and Zotov].

B_c/B ratio

LHCb experimental value [Aaij et al.(2014a)]:

$$R^{\text{exp}} = \frac{\sigma(B_c^+) \times \mathcal{B}(B_c^+ \rightarrow J/\psi\pi^+)}{\sigma(B^+) \times \mathcal{B}(B^+ \rightarrow J/\psi K^+)} = (0.683 \pm 0.018 \pm 0.009)\%$$

$\mathcal{B}(B^+ \rightarrow J/\psi K^+) \approx 0.1\%$ is known experimentally.
 $\mathcal{B}(B_c^+ \rightarrow J/\psi\pi^+)$ is theoretically predicted within different models. The obtained predictions contradict each other :

$$\mathcal{B}(B_c^+ \rightarrow J/\psi\pi^+) = 0.061 \div 0.29\%$$

$$r_c^{\text{theor.}} \sim \frac{\sigma(B_c^+)}{\sigma(B^+)} \sim 0.1 \div 0.3\%$$

The R^{exp} is in agreement the largest predicted value for $\mathcal{B}(B_c^+ \rightarrow J/\psi\pi^+)$:

$$R_{\text{optimistic}}^{\text{theor.}} \sim 0.3 \div 0.9\%$$

However the choice of $\mathcal{B}(B_c^+ \rightarrow J/\psi\pi^+) \sim (0.06 \div 1.1)\%$ looks more reasonable, because these values obtain within the models [Ebert et al.(2003) Ebert, Faustov, and Galkin, Abd El-Hady et al.(2000) Abd El-Hady, Munoz, and Vary], which describe the the experimentally obtained ratio [Aaij et al.(2014b)]:

$$\frac{\mathcal{B}(B_c^+ \rightarrow J/\psi\pi^+)}{\mathcal{B}(B_c^+ \rightarrow J/\psi\mu\nu_\mu)} = 0.0469 \pm 0.0028 \pm 0.0046$$

For this case

$$R_{\text{reasonable}}^{\text{theor.}} \sim 0.06 \div 0.3\%$$

It seems that the theoretical predictions underestimate the experimental values.

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