



# EUROPEAN PLASMA RESEARCH ACCELERATOR WITH EXCELLENCE IN APPLICATIONS

## Transfer lines status

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- A lot of different transfer lines are to be designed (plasma to FEL, inter-stage lines, PWFA, different initial beam distributions,...).
- Problem: optimization of the line is dependent on the initial conditions.
- If use of traditional methods (simplex, conjugate gradient), how to make sure that the solution is not a local minimum?
  - Better to use genetic algorithms (like GIOTTO), particle swarm optimization (PSO) or artificial bees to explore the domain.
  - Use of PSO to find an initial working point.
- Use of a conjugate gradient to speed up the convergence when near an optimum.
- Currently 10 minutes to find a transfer line on a serial computer (convergence criteria and method can still be improved).
- When a few lines are selected as the baseline, these transfer lines will be improved with additional criteria (like flexibility with different initial distributions).

## Input

- Total length and minimum distance between elements.
- # permanent Qpoles (PMQ) and electromagnetic Qpoles (EMQ).
- Minimum and maximum gradient.
- Initial distribution (Twiss parameters, momentum spread,...).

## Variables

- Gradient and positions of the quadrupoles.

## Constraints

- Final Twiss parameters (or matrix terms).
- Minimisation of the emittance growth (case  $\alpha_{xy,0} = 0$ ):

$$\epsilon_{xy,1} \approx \epsilon_{xy,0} \left\{ 1 + \beta_{xy,1} \gamma_{xy,0} \sigma_{\delta}^2 \left[ \left( \frac{T_{126}}{\beta_{xy,1}} \right)^2 + \left( T_{226} + \alpha_{xy,1} \frac{T_{126}}{\beta_{xy,1}} \right)^2 \right] \right\}^{1/2} \quad (1)$$

## Input

- Total length: from 4 meters to 8 meters.
- Min: 30 mm between PMQs, 100 mm between EMQs, 50 mm after plasma.
- Length PMQ: 100 mm, length EMQ: 400 mm
- 2-8 PMQs and 4 EMQs.
- Maximum gradient of 700 T/m PMQs and 100 T/m in the EMQs.

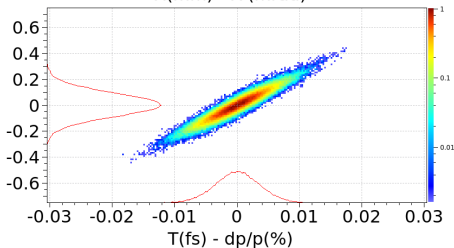
## Variables

- Gradient and positions of the quadrupoles.

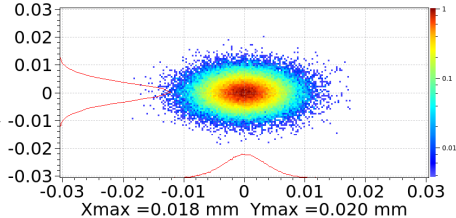
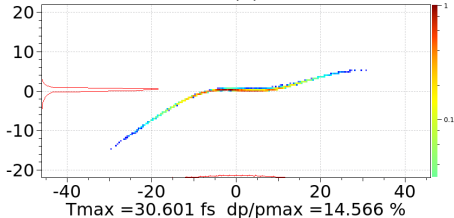
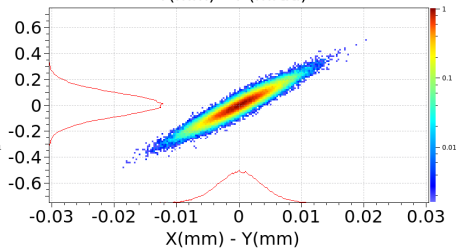
## Constraints

- Final Twiss parameters.  
 $\beta_{x,1} = 5.04 \text{ m}, \quad \beta_{y,1} = 2.11 \text{ m}, \quad \alpha_{x,1} = 1.48, \quad \alpha_{y,1} = -0.65$
- Minimisation of the emittance growth

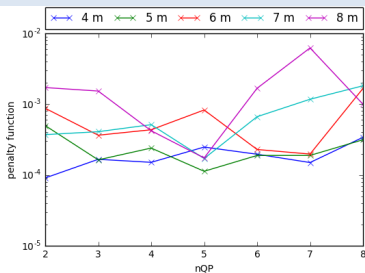
File #0 [0 m] NGOOD · 100151 / 100151  
 X(mm) - X'(mrad)



Y(mm) - Y'(mrad)

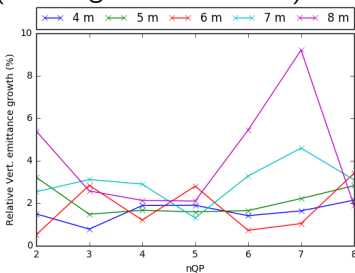
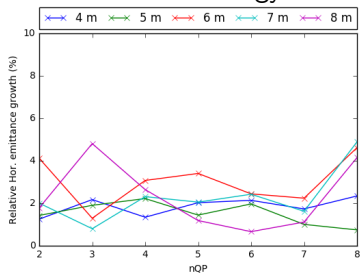


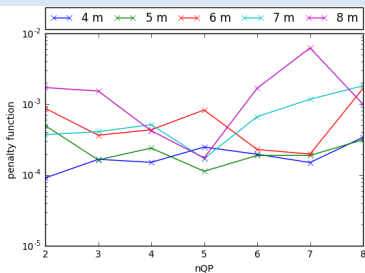
$$\beta_{x,0} = 127 \text{ mm}, \quad \beta_{y,0} = 127 \text{ mm}, \quad \alpha_{x,0} = -3.0, \quad \alpha_{y,0} = -3.0, \quad \gamma_{x,0} = 79 \text{ m}^{-1}, \quad \gamma_{y,0} = 79 \text{ m}^{-1}$$



- Shorter transfer line is better.
- No gain in increasing the number of quadrupoles.
- Baseline: 2 PMQs followed by 4 EMQs for a total length of 4 m.
- Other solution if emittance growth balanced in both planes.

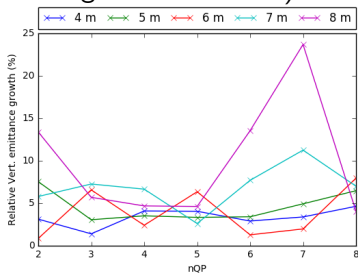
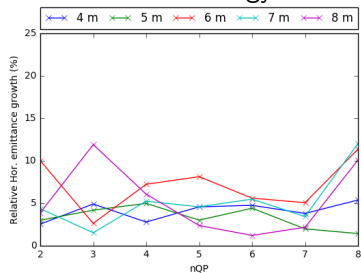
Cut in energy at  $\pm 0.2\%$  (tracking with TraceWin)

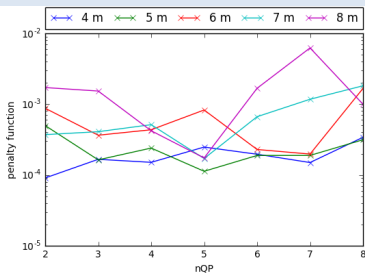




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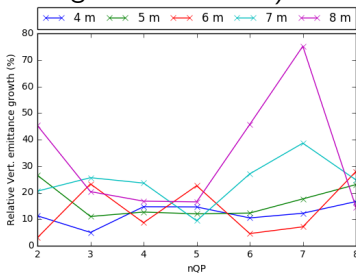
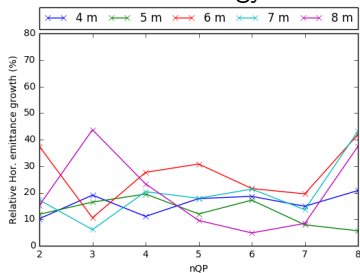
Cut in energy at  $\pm 0.4\%$  (tracking with TraceWin)



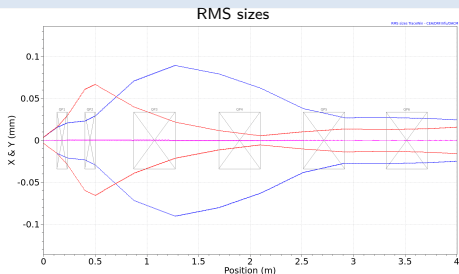


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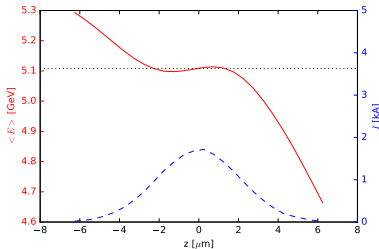
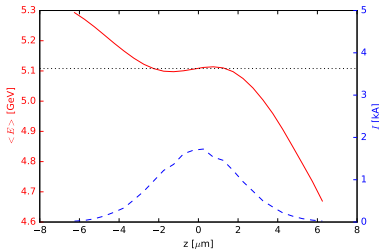


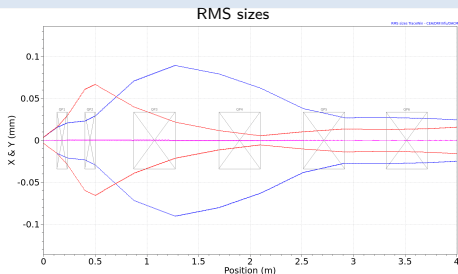




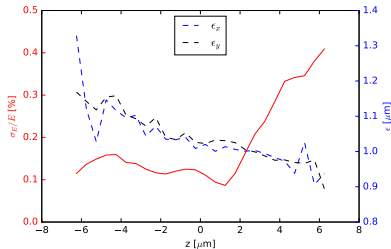
Initial/Final Current (bin:  $0.5 \mu\text{m}$ ) (from ASTRA).

- Ref energy: **5.11 GeV**.
- ⇒ Max. PMQ gradient: **713 T/m**.
- Can be cured by lengthening a bit the PMQs or with a loop with WP2 to reduce final energy.
- Max. EMQ gradient: **83 T/m**.

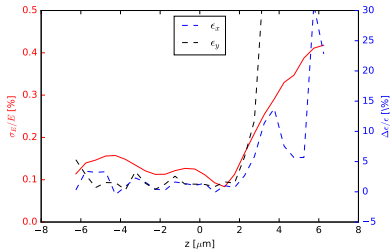




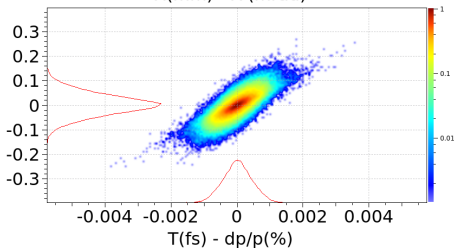
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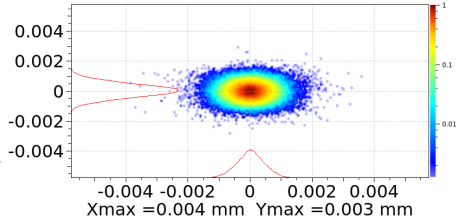
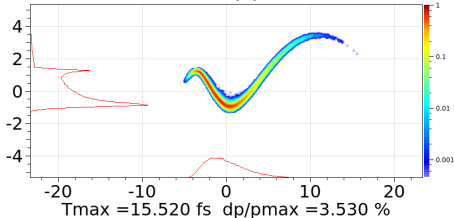
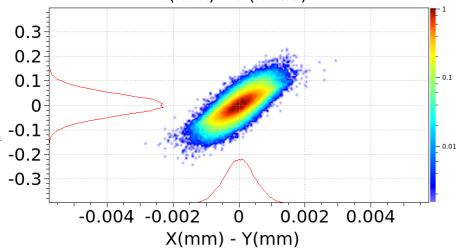
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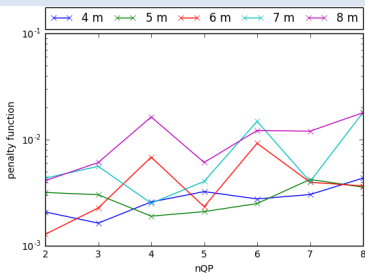
File #0 [0 m] NGOOD · 126469 / 126469  
X(mm) - X'(mrad)



Y(mm) - Y'(mrad)

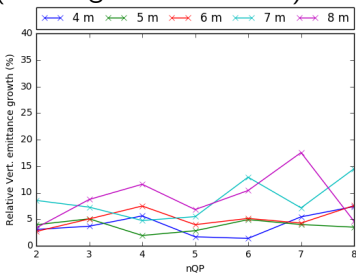
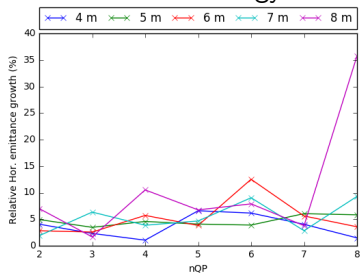


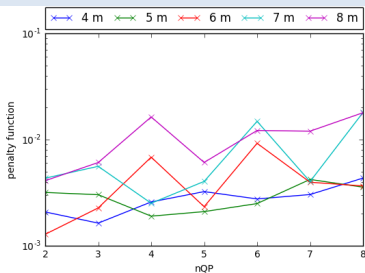
$$\beta_{x,0} = 16 \text{ mm}, \quad \beta_{y,0} = 16 \text{ mm}, \quad \alpha_{x,0} = -1.3, \quad \alpha_{y,0} = -1.3, \quad \gamma_{x,0} = 162 \text{ m}^{-1}, \quad \gamma_{y,0} = 162 \text{ m}^{-1}$$



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- No gain in increasing the number of quadrupoles.
- Baseline: 2 PMQs followed by 4 EMQs for a total length of 4 m.
- Other solution if emittance growth balanced in both planes.

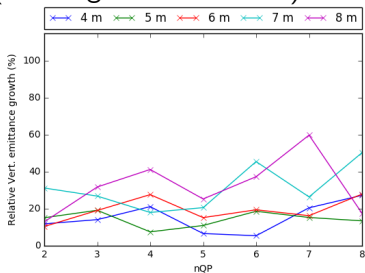
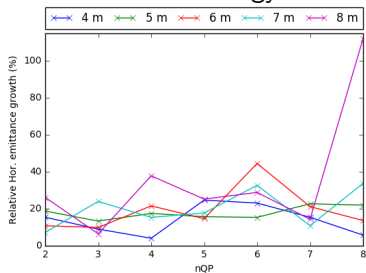
Cut in energy at  $\pm 0.2\%$  (tracking with TraceWin)

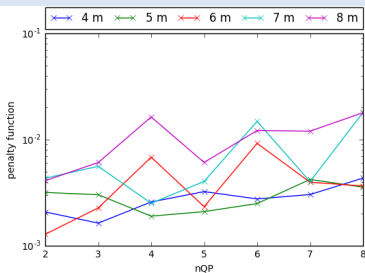




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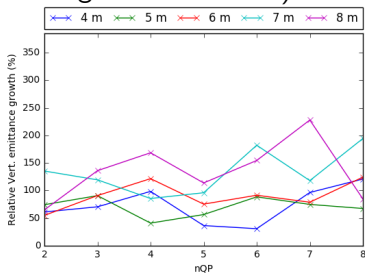
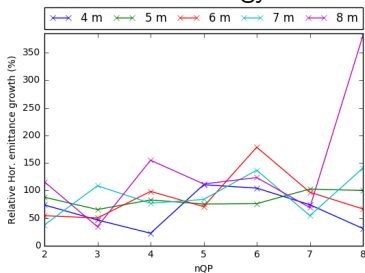
Cut in energy at  $\pm 0.4\%$  (tracking with TraceWin)

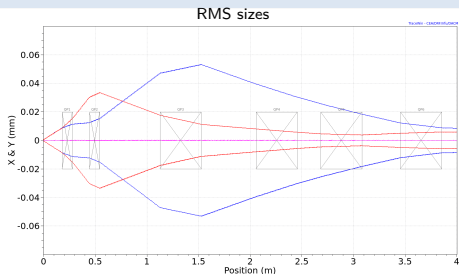




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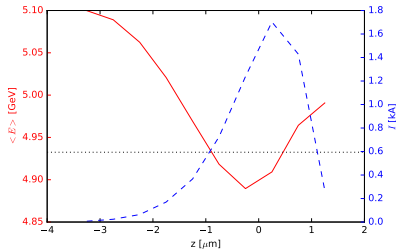
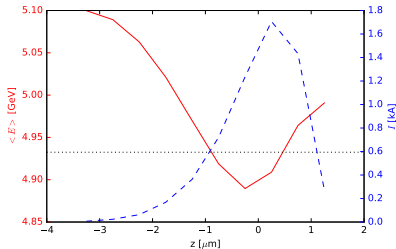
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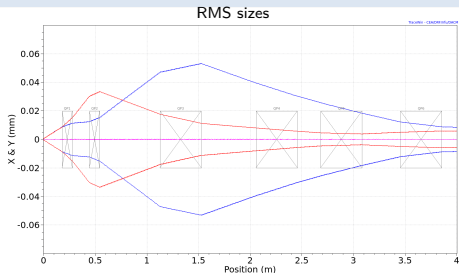




- Ref energy: **4.93 GeV**.
- ⇒ Max. PMQ gradient: **637 T/m**.
- Max. EMQ gradient: **63 T/m**.
- Two weak EMQs ( $<10$  T/m)

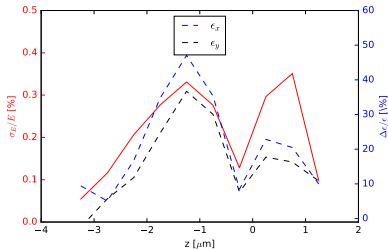
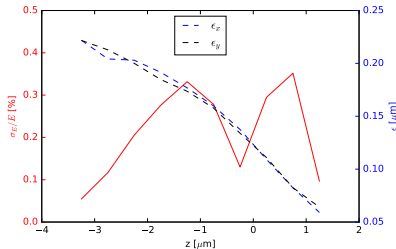
Initial/Final Current (bin:  $0.5 \mu\text{m}$ ) (from ASTRA).





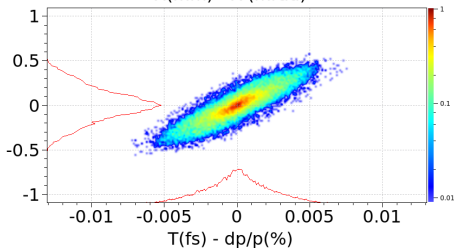
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Initial/Final Norm emittance (bin:  $0.5 \mu\text{m}$ ) (from ASTRA).

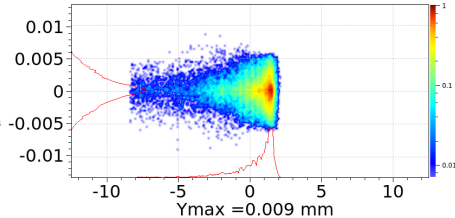
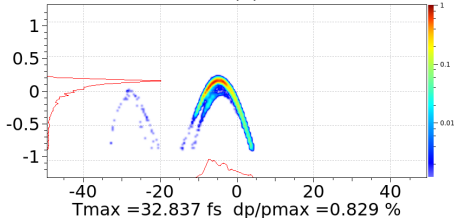
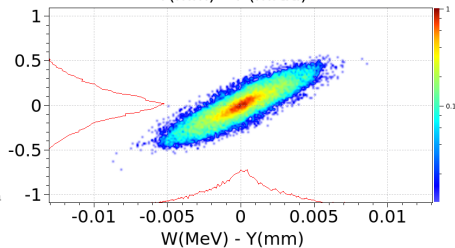




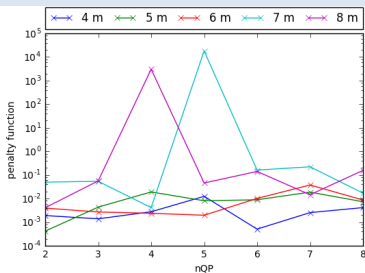
File #0 [0 m] NGOOD · 23119 / 23119  
X(mm) - X'(mrad)



Y(mm) - Y'(mrad)

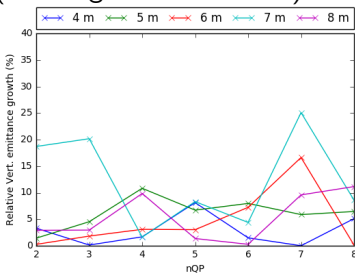
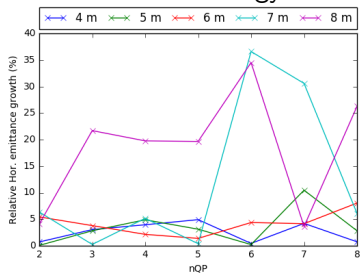


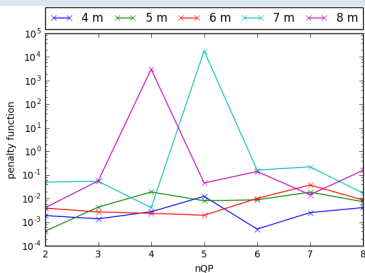
$$\beta_{x,0} = 25 \text{ mm}, \quad \beta_{y,0} = 25 \text{ mm}, \quad \alpha_{x,0} = -1.8, \quad \alpha_{y,0} = -1.8, \quad \gamma_{x,0} = 175 \text{ m}^{-1}, \quad \gamma_{y,0} = 175 \text{ m}^{-1}$$



- Shorter transfer line is better.
- No gain in increasing the number of quadrupoles.
- Baseline: 2 PMQs followed by 4 EMQs for a total length of 4 m.
- Other solution if emittance growth balanced in both planes.

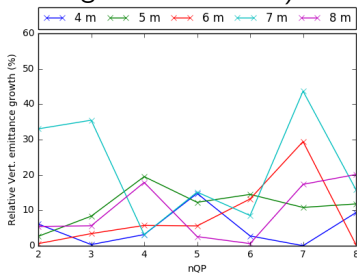
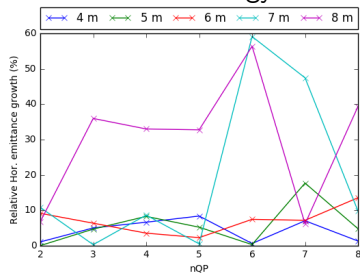
Cut in energy at  $\pm 0.2\%$  (tracking with TraceWin)

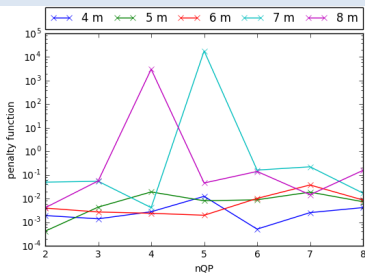




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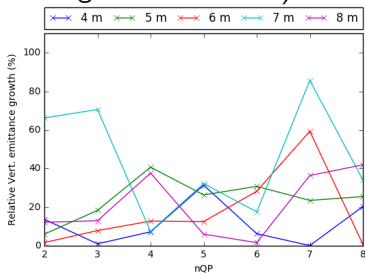
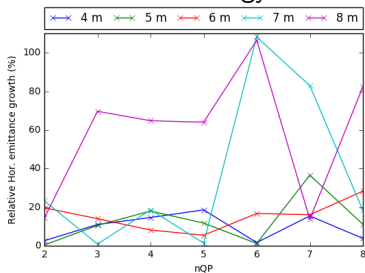
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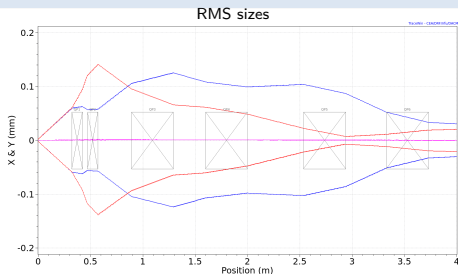




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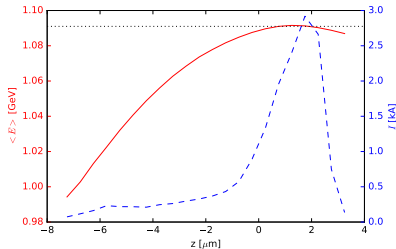
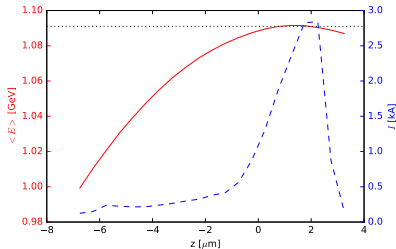
Cut in energy at  $\pm 1.0\%$  (tracking with TraceWin)

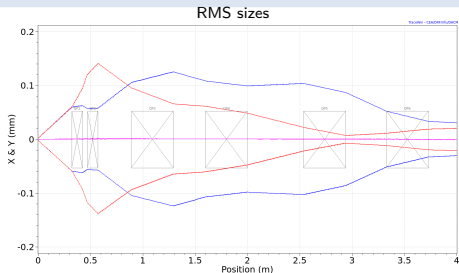




- Ref energy: **1.09 GeV**.
- ⇒ Max. PMQ gradient: **181 T/m**.
- Max. EMQ gradient: **18 T/m**.
- Two weak EMQs ( $<10$  T/m)

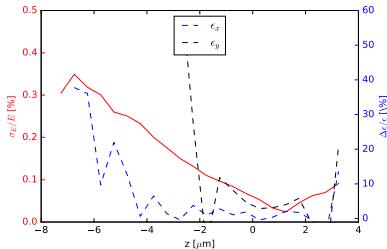
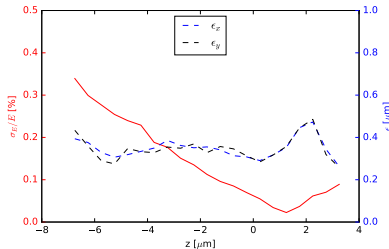
Initial/Final Current (bin:  $0.5 \mu\text{m}$ ) (from ASTRA).



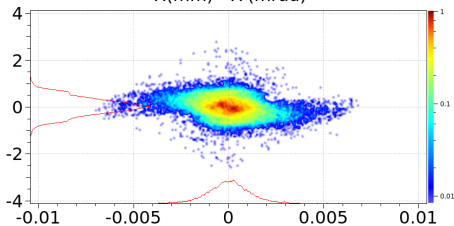


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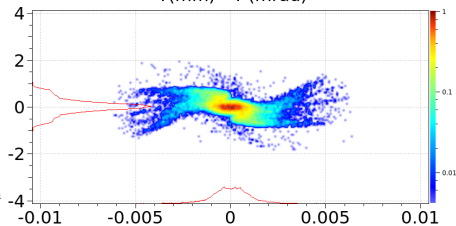
Initial/Final Norm emittance (bin:  $0.5 \mu\text{m}$ ) (from ASTRA).



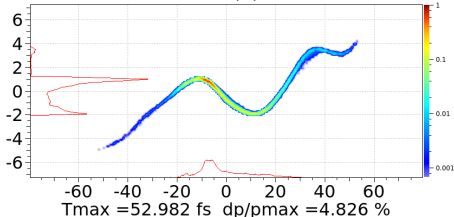
File #0 [0 m] NGOOD · 29193 / 29193  
X(mm) - X'(mrad)



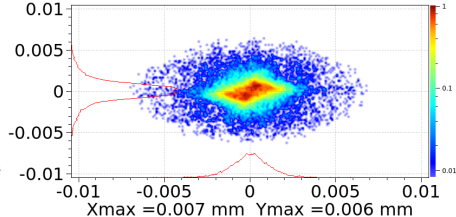
Y(mm) - Y'(mrad)



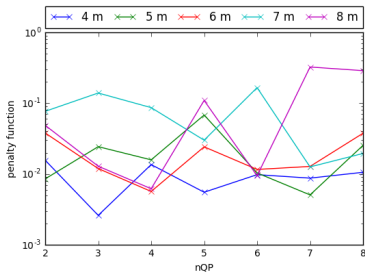
T(fs) - dp/p(%)



X(mm) - Y(mm)

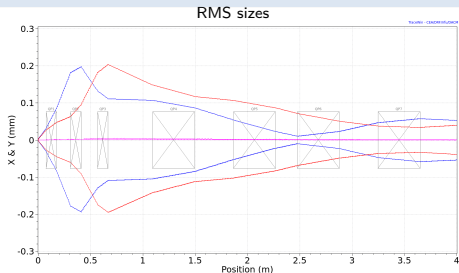


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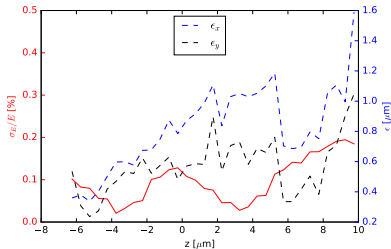
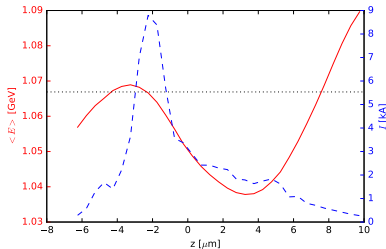
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- Baseline: 3 PMQs followed by 4 EMQs for a total length of 4 m.
- Other solution if emittance growth balanced in both planes.

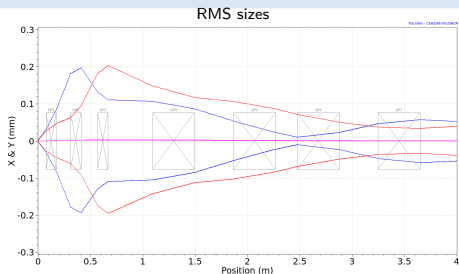




- Ref energy: **1.09 GeV**.
- ⇒ Max. PMQ gradient: **198 T/m**.
- Max. EMQ gradient: **18 T/m**.
- Two weak EMQs ( $<10$  T/m)

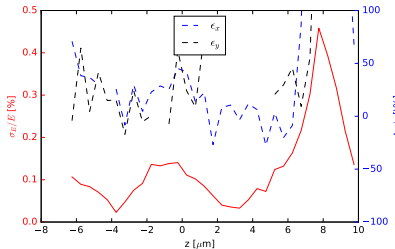
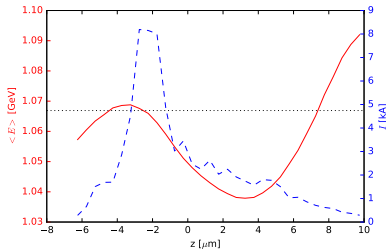
Slice emittance (bin:  $0.5 \mu\text{m}$ ) (from ASTRA). Initial conditions.





- Ref energy: **1.09 GeV**.
- ⇒ Max. PMQ gradient: **198 T/m**.
- Max. EMQ gradient: **18 T/m**.  
Two weak EMQs (<10 T/m)

Slice emittance (bin:  $0.5 \mu\text{m}$ ) (from ASTRA). Final conditions.



## Input

- Total length: from 0.5 meters to 1.5 meters.
- Min: 30 mm between PMQs, 100 mm between EMQs, 50 mm after plasma.
- Length PMQ: 50 mm
- 4-10 PMQs.
- Maximum gradient of 600 T/m in PMQs.

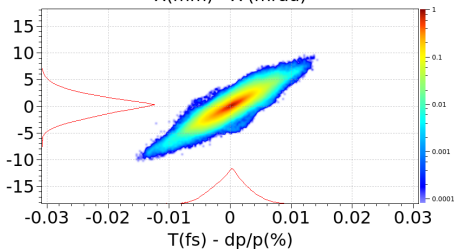
## Variables

- Gradient and positions of the quadrupoles.

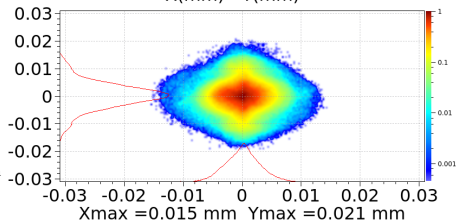
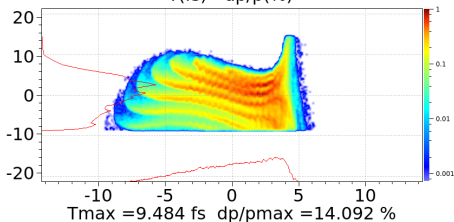
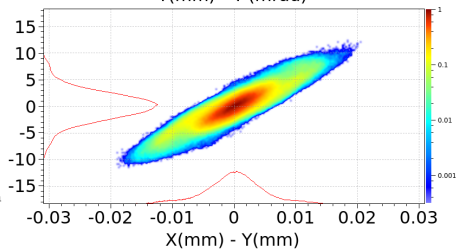
## Constraints

- Final Twiss parameters.  
 $\beta_{x,1} = 30 \text{ mm}, \quad \beta_{y,1} = 30 \text{ mm}, \quad \alpha_{x,1} = 1.0, \quad \alpha_{y,1} = 1.0$
- Minimisation of the emittance growth

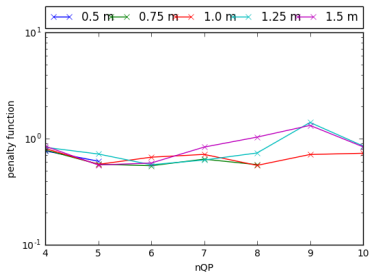
File #0 [0 m] NGOOD · 907716 / 907716  
 X(mm) - X'(mrad)



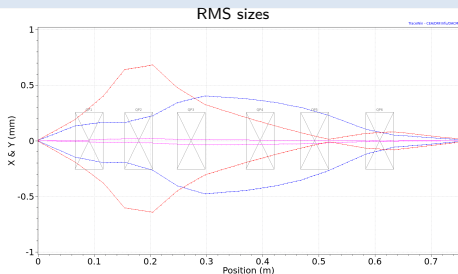
Y(mm) - Y'(mrad)



$$\beta_{x,0} = 3 \text{ mm}, \quad \beta_{y,0} = 4 \text{ mm}, \quad \alpha_{x,0} = -2.0, \quad \alpha_{y,0} = -2.1, \quad \gamma_{x,0} = 1515 \text{ m}^{-1}, \quad \gamma_{y,0} = 1352 \text{ m}^{-1}$$

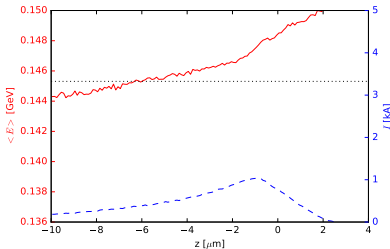
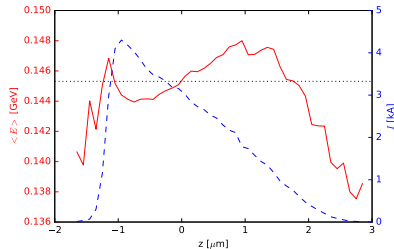


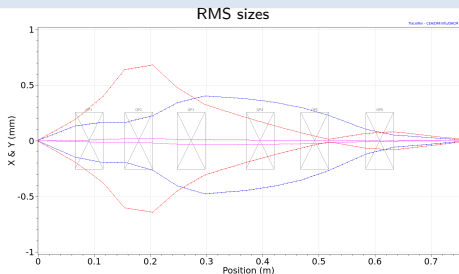
- No gain in increasing the number of quadrupoles.
- Baseline: 6 PMQs for a total length of 0.75 m.
- Other solution if emittance growth balanced in both planes.



Initial/Final Current (bin: 0.1  $\mu\text{m}$ ) (from ASTRA).

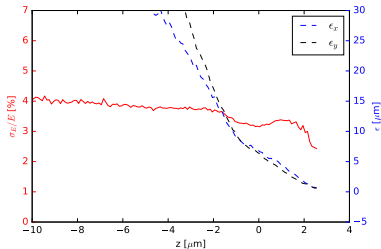
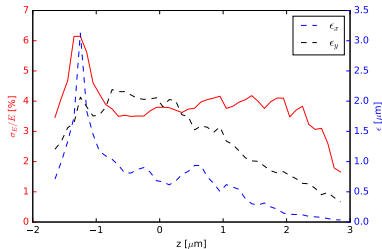
- Ref energy: **145 MeV**.
- ⇒ Max. PMQ gradient: **220 T/m**.
- **The velocity spread is not negligible**: correlation time-energy at the end of the transfer line.

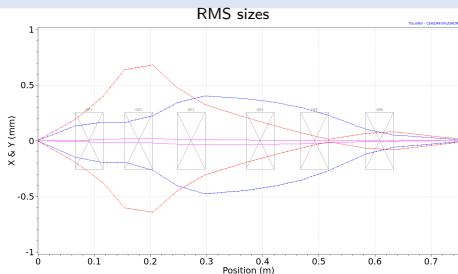




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- ⇒ Max. PMQ gradient: **220 T/m**.
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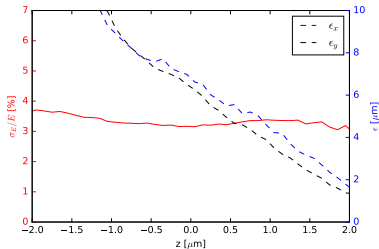
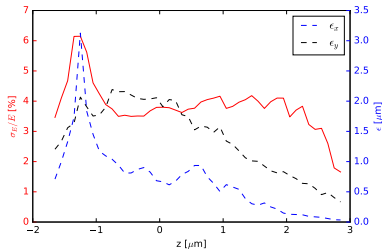
Initial/Final Norm emittance (bin:  $0.1 \mu\text{m}$ ) (from ASTRA).



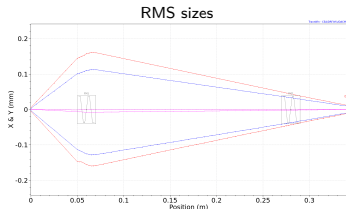


- Ref energy: **145 MeV**.
- ⇒ Max. PMQ gradient: **220 T/m**.
- **The velocity spread is not negligible**: correlation time-energy at the end of the transfer line.

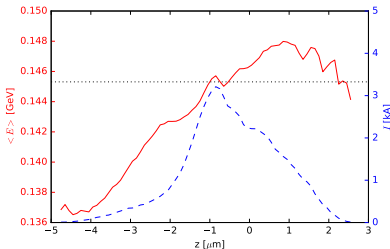
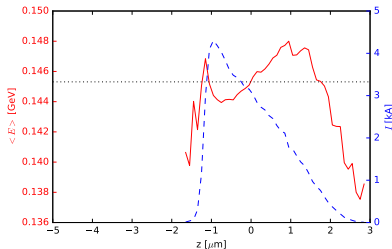
Initial/Final Norm emittance (bin:  $0.1 \mu\text{m}$ ) (from ASTRA).

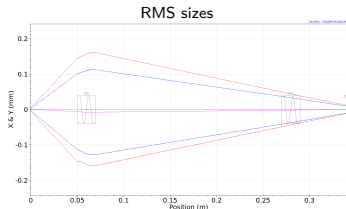






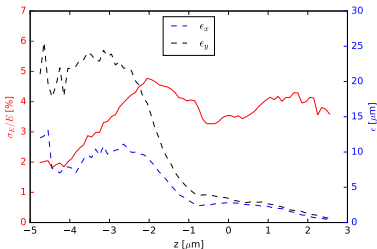
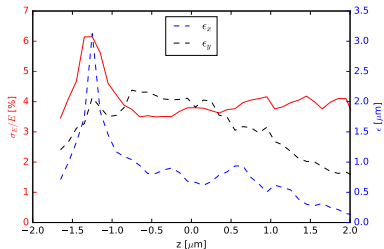
- Ref energy: **145 MeV**.
  - Length of the plasma cell: 20 mm.
  - Minimum aperture:  $\approx 1$  mm.
  - ⇒ Max. gradient: **425 T/m**.
  - Total length: 340 mm.
- Initial/Final Current (bin:  $0.1 \mu\text{m}$ ) (from ASTRA).

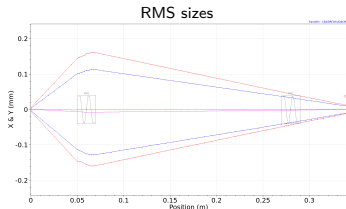




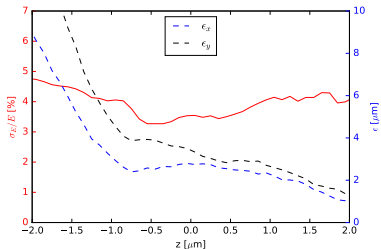
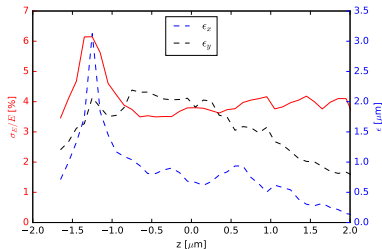
- Ref energy: **145 MeV**.
- Length of the plasma cell: 20 mm.
- Minimum aperture:  $\approx 1$  mm.
- ⇒ Max. gradient: **425 T/m**.
- Total length: 340 mm.

Initial/Final Norm emittance (bin:  $0.1 \mu\text{m}$ ) (from ASTRA).

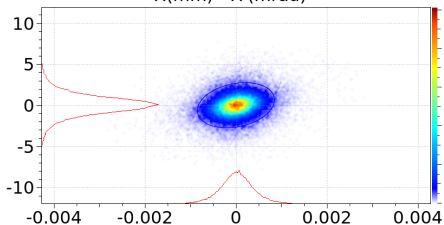




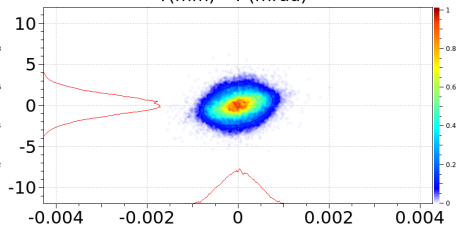
- Ref energy: **145 MeV**.
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  - Total length: 340 mm.
- Initial/Final Norm emittance (bin:  $0.1 \mu\text{m}$ ) (from ASTRA).



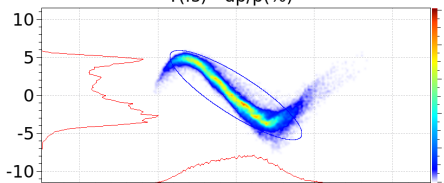
File #0 [0 m] NGOOD · 50000 / 50000  
 X(mm) - X'(mrad)



Y(mm) - Y'(mrad)

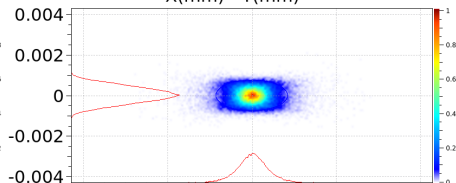


T(fs) - dp/p(%)



Tmax = 8.264 fs dp/pmax = 7.632 %

X(mm) - Y(mm)

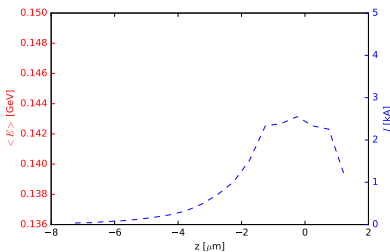
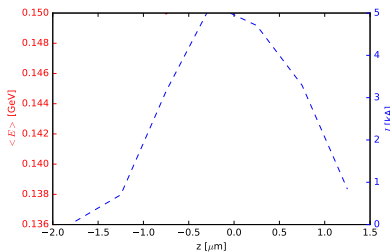


Xmax = 0.003 mm Ymax = 0.002 mm

$$\beta_{x,0} = 0.3 \text{ mm}, \quad \beta_{y,0} = 0.3 \text{ mm}, \quad \alpha_{x,0} = -0.2, \quad \alpha_{y,0} = -0.2, \quad \gamma_{x,0} = 3467 \text{ m}^{-1}, \quad \gamma_{y,0} = 3467 \text{ m}^{-1}$$

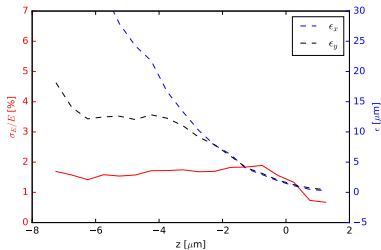
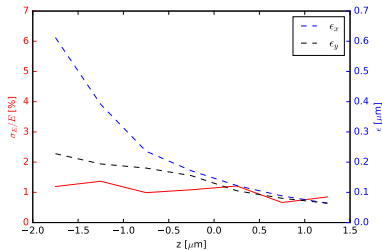
- Ref energy: **145 MeV**.
- ⇒ Max. PMQ gradient: **169 T/m**.
- **The velocity spread is not negligible**: correlation time-energy at the end of the transfer line.

Initial/Final Current (bin:  $0.1 \mu\text{m}$ ) (from ASTRA).



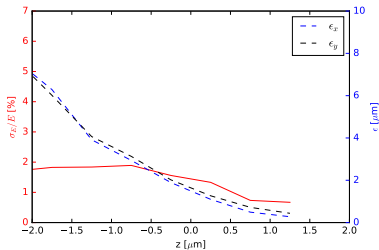
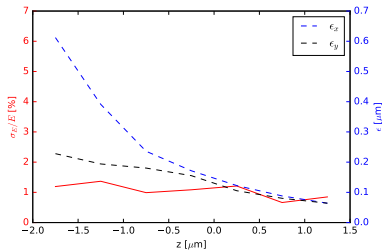
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- ⇒ Max. PMQ gradient: **169 T/m**.
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Initial/Final Norm emittance (bin:  $0.1 \mu\text{m}$ ) (from ASTRA).



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- ⇒ Max. PMQ gradient: **169 T/m**.
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Initial/Final Norm emittance (bin:  $0.1 \mu\text{m}$ ) (from ASTRA).



- Several transfer lines were realized to transport different initial distributions coming from different plasma schemes.
- Currently, the transfer line for a 5 GeV beam to a FEL, for a 1 GeV beam to FEL and 2-stage-scheme for a 150 MeV beam have been addressed.
- Results are encouraging for the 5 GeV beam. With a total of 6 QPs and a total length of 4-5 m, the beam can be transported up to the FEL with a growth of the slice emittance of only a few percent's. As expected, the smaller the initial divergence is, the less the emittance grows.
- At 1 GeV, the LWFA beam fits the specifications. A large amount of work was done by EuSPARC teams for PWFA (see CDR).
- For the 2-stage line, the emittance increase is not negligible (the emittance grows by a factor 4 to 5) because of the energy spread. An alternative with plasma lenses has been investigated.



- To refine the transfer lines: to freeze some parameters to make the comparison easier between different distributions.
- To include space charge effects (relevant at 150 MeV). First studies have begun (strategy was first to see if we can find solutions with no charge effects).
- To improve the model and to check emittance calculation (use of macros developed as discussed in Lisbon on November 2017).
- To iterate with WP6 for FEL performance and to check the magnet parameters is realistic (gradient and inter-distance).
- To realize doglegs to fit WP7 needs.