

Associated production of a top quark pair with a W or Z boson at the LHC at NNLL+NLO

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with a massive boson $pp \rightarrow t\bar{t}W/Z/H$



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Associated production of $t\bar{t}$

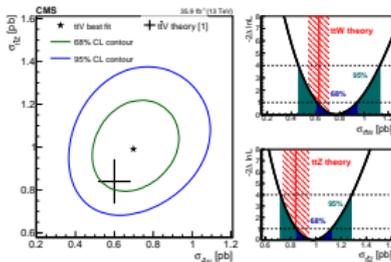
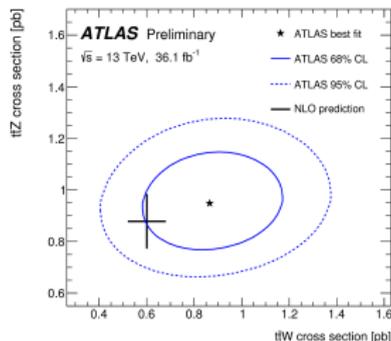
with a massive boson $pp \rightarrow t\bar{t}W/Z/H$

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- ▶ $t\bar{t}W/Z$ important background for new physics searches



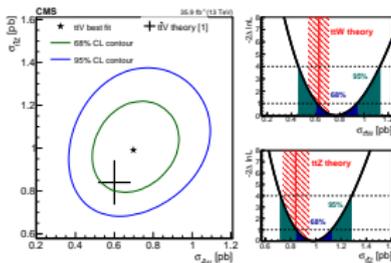
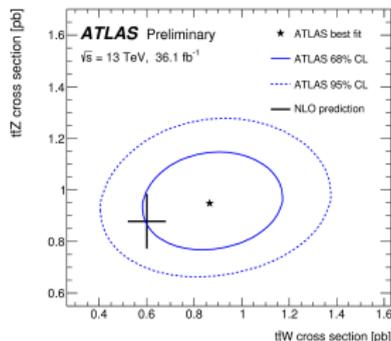
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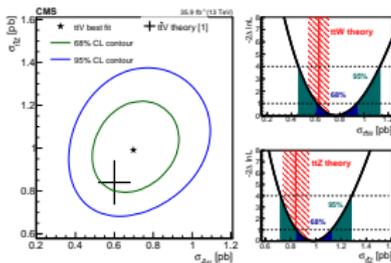
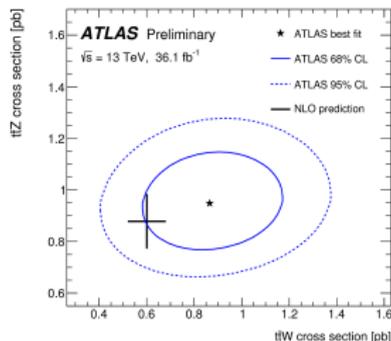
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- ▶ Resummation: class of corrections beyond NLO





Status of $t\bar{t}V$

$t\bar{t}W/t\bar{t}Z$:

- ▶ NLO QCD

[Lazopoulos, Melnikov, Petriello, '08] [Lazopoulos, McElmurry, Melnikov, Petriello, '08] [Kardos, Trocsanyi, Papadopoulos '12] [Campbell, Ellis, '12]

- ▶ NLO QCD matched to PS

[Garzelli, Kardos, Papadopoulos, Trocsanyi, '12] [Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Shao, Stelzer, Torrielli, Zaro '14] [Maltoni, Mangano, Tsinikos, Zaro, '14]

- ▶ EW and QCD NLO corrections

[Frixione, Hirschi, Pagani, Shao, Zaro, '15] [Frederix, Pagani, Zaro, '18] [Frederix, Frixione, Hirschi, Pagani, Shao, Zaro, '18]

Status of $t\bar{t}V$



Resummation:

- ▶ $t\bar{t}H$:
 - ▶ Direct QCD approach (Mellin space approach) [Kulesza, Motyka, Stebel, Theeuwes, '15 '16 '17]
 - ▶ SCET-based methods [Broggio, Ferroglia, Pecjak, Signer, Yang, '16] [Broggio, Ferroglia, Pecjak, Yang, '17]
- ▶ $t\bar{t}W/t\bar{t}Z$:
 - ▶ SCET-based methods [H. T. Li, C. S. Li, S. A. Li, '14] [Broggio, Ferroglia, Ossola, Pecjak, '16] [Broggio, Ferroglia, Ossola, Pecjak, Sameshima '17]

Soft gluon resummation



- ▶ Direct QCD approach



Soft gluon resummation

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- ▶ Invariant mass threshold limit $\hat{\tau} = \frac{(p_t + p_{\bar{t}} + p_V)^2}{\hat{s}} = \frac{Q^2}{\hat{s}} \rightarrow 1$



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- ▶ Invariant mass threshold limit $\hat{\tau} = \frac{(p_t + p_{\bar{t}} + p_V)^2}{\hat{s}} = \frac{Q^2}{\hat{s}} \rightarrow 1$
→ soft gluon resummation
- ▶ Resummed logarithms

$$\alpha_S^m \left(\frac{\log^n(1 - \hat{\tau})}{1 - \hat{\tau}} \right)_+ \quad m \leq 2n - 1$$
$$\int_0^1 dx (f(x))_+ = \int_0^1 dx (f(x) - f(x_0))$$

Soft gluon resummation



process $pp \rightarrow t\bar{t}V$:



Soft gluon resummation

process $pp \rightarrow t\bar{t}V$:

- ▶ Factorization principle holds for any number of jets/particles in the final state [Kidonakis, Oderda, Sterman '98][Bonciani, Catani, Mangano, Nason '03]



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- ▶ Same colour structure as $pp \rightarrow t\bar{t}$



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Resummed cross section in Mellin space:

$$\frac{d\tilde{\sigma}_{ij \rightarrow t\bar{t}V}^{res}}{dQ^2} = \text{Tr}[\mathbf{H}_{ij \rightarrow t\bar{t}V} \mathbf{S}_{ij \rightarrow t\bar{t}V}] \Delta_i \Delta_j$$



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Colour matrices $\mathbf{H}_{ij \rightarrow t\bar{t}V}$, $\mathbf{S}_{ij \rightarrow t\bar{t}V}$

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Δ_j : (soft-)collinear radiation



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Soft gluon resummation

Δ_j : (soft-)collinear radiation

- ▶ Logarithmic contributions from (soft-)collinear radiation
- ▶ Included for the two incoming partons
- ▶ Universal function, depends only on emitting parton (quark or gluon)
- ▶ Here needed at NLL/NNLL, known [Catani, Mangano, Nason, Trentadue '96], [Bonciani, Catani, Mangano, Nason '98]/[Catani, de Florian, Grazzini, Nason '03]

Soft gluon resummation



$$\mathbf{H}_{ij \rightarrow t\bar{t}V} = \mathbf{H}_{ij \rightarrow t\bar{t}V}^{(0)} + \frac{\alpha_S}{\pi} \mathbf{H}_{ij \rightarrow t\bar{t}V}^{(1)} + \dots : \text{hard contributions}$$



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- ▶ $\mathbf{H}_{ij \rightarrow t\bar{t}V}^{(0)}$: leading order cross section



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- ▶ $\mathbf{H}_{ij \rightarrow t\bar{t}V}^{(1)}$: non-logarithmic contributions of $\mathcal{O}(\alpha_S)$
- ▶ $\mathbf{H}_{ij \rightarrow t\bar{t}V}^{(1)}$ includes virtual loop corrections, numerically extracted from PowHel [Garzelli, Kardos, Papadopoulos, Trocsanyi '11][Garzelli, Kardos, Papadopoulos, Trócsányi '12]

Soft gluon resummation



$\mathbf{S}_{ij \rightarrow t\bar{t}V}$ soft wide angle radiation:



Soft gluon resummation

$\mathbf{S}_{ij \rightarrow t\bar{t}V}$ soft wide angle radiation:

- ▶ Given by a solution of the renormalization group equation

$$\mathbf{S}_{ij \rightarrow t\bar{t}V} = \bar{\mathbf{U}}_{ij \rightarrow t\bar{t}V} \tilde{\mathbf{S}}_{ij \rightarrow t\bar{t}V} \mathbf{U}_{ij \rightarrow t\bar{t}V}$$



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- ▶ $\mathbf{U}_{ij \rightarrow t\bar{t}V}$: path-ordered exponent

$$\mathbf{U}_{ij \rightarrow t\bar{t}V} = \text{P exp} \left(\int_{\mu_R}^{Q/\bar{N}} \frac{dq}{q} \Gamma_{ij \rightarrow t\bar{t}V}(\alpha_S(q^2)) \right)$$

$$\text{with } \Gamma_{ij \rightarrow t\bar{t}V} = \frac{\alpha_S}{\pi} \Gamma_{ij \rightarrow t\bar{t}V}^{(1)} + \left(\frac{\alpha_S}{\pi}\right)^2 \Gamma_{ij \rightarrow t\bar{t}V}^{(2)} + \dots$$



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- ▶ $\Gamma_{ij \rightarrow t\bar{t}V}^{(1)}$ and $\Gamma_{ij \rightarrow t\bar{t}V}^{(2)}$ known [Ferrogli, Neubert, Pecjak, Yang '09]



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- ▶ $\tilde{\mathbf{S}}_{ij \rightarrow t\bar{t}V} = \tilde{\mathbf{S}}_{ij \rightarrow t\bar{t}V}^{(0)} + \frac{\alpha_S}{\pi} \tilde{\mathbf{S}}_{ij \rightarrow t\bar{t}V}^{(1)} + \dots$

Soft gluon resummation



$\Gamma_{ij \rightarrow t\bar{t}V}$ non diagonal:



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- ▶ Diagonalization of $\Gamma_{ij \rightarrow t\bar{t}V}^{(1)}$ [Kidonakis, Oderda, Sterman '98]



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$$\Gamma_R^{(i)} = \mathbf{R}^{-1} \Gamma_{ij \rightarrow t\bar{t}V}^{(i)} \mathbf{R}$$

$$\mathbf{H}_R = \mathbf{R}^{-1} \mathbf{H}_{ij \rightarrow t\bar{t}V} (\mathbf{R}^{-1})^\dagger$$

$$\tilde{\mathbf{S}}_R = \mathbf{R}^\dagger \tilde{\mathbf{S}}_{ij \rightarrow t\bar{t}V} \mathbf{R}$$



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- ▶ At NLL:

$$\mathbf{S}_{R,IL} = \bar{\mathbf{U}}_{R,IJ} \tilde{\mathbf{S}}_{R,JK} \mathbf{U}_{R,KL} = \tilde{\mathbf{S}}_{R,IL} \exp \left[\frac{\log(1-2\lambda)}{2\pi b_0} \left((\lambda_I^{(1)})^* + \lambda_L^{(1)} \right) \right]$$



Soft gluon resummation

At NNLL additional complexity due to $\Gamma_{ij \rightarrow t\bar{t}V}^{(2)}$:



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At NNLL additional complexity due to $\Gamma_{ij \rightarrow t\bar{t}V}^{(2)}$:

- ▶ Perturbative expansion [Buchalla, Buras, Lautenbacher '96] [Ahrens, Neubert, Pecjak, Yang '10]



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$$\mathbf{U}_R = \left(\mathbf{1} + \frac{\alpha_s(\mu_R^2)}{\pi(1-2\lambda)} \mathbf{K} \right) \left[e^{g_s(N) \vec{\lambda}^{(1)}} \right]_D \left(\mathbf{1} - \frac{\alpha_s(\mu_R^2)}{\pi} \mathbf{K} \right)$$
$$\bar{\mathbf{U}}_R = \left(\mathbf{1} - \frac{\alpha_s(\mu_R^2)}{\pi} \mathbf{K}^\dagger \right) \left[e^{g_s(N) (\vec{\lambda}^{(1)})^*} \right]_D \left(\mathbf{1} + \frac{\alpha_s(\mu_R^2)}{\pi(1-2\lambda)} \mathbf{K}^\dagger \right)$$

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$$K_{IJ} = \delta_{IJ} \lambda_I^{(1)} \frac{b_1}{2b_0^2} - \frac{\left(\Gamma_R^{(2)} \right)_{IJ}}{2\pi b_0 + \lambda_I^{(1)} - \lambda_J^{(1)}}$$

Soft gluon resummation



Numerical Results:

Soft gluon resummation



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- ▶ $\sqrt{S} = 13 \text{ TeV}$, PDF4LHC15



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- ▶ NLO calculated with MadGraph5_aMC@NLO or PowHel



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- ▶ NLL w \mathcal{C} : NLL improved with terms of $\mathcal{O}(\alpha_S)$ from $\mathbf{H}_{ij \rightarrow t\bar{t}V}$ and $\tilde{\mathbf{S}}_{ij \rightarrow t\bar{t}V}$

Soft gluon resummation

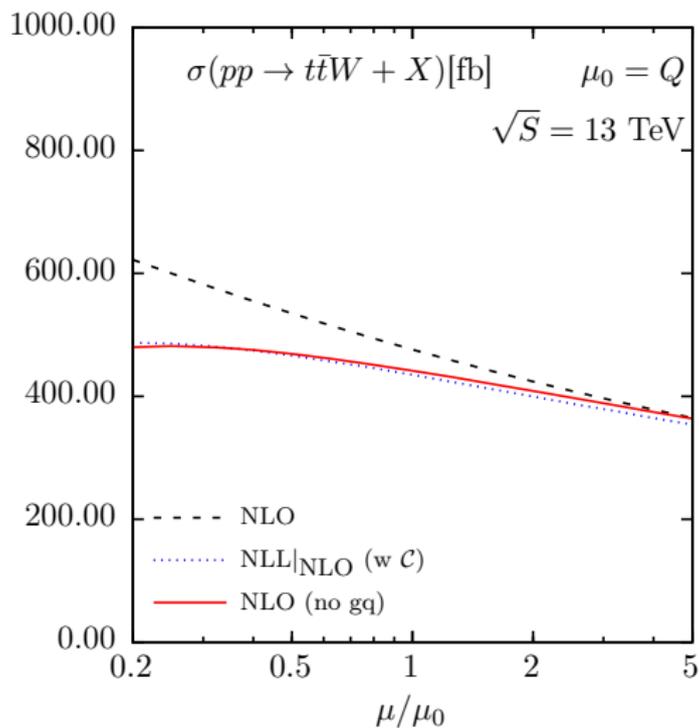


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- ▶ scale choices: $\mu = Q$, $\mu = \frac{2m_t + m_V}{2} = \frac{M}{2}$ and $\mu = \frac{Q}{2}$



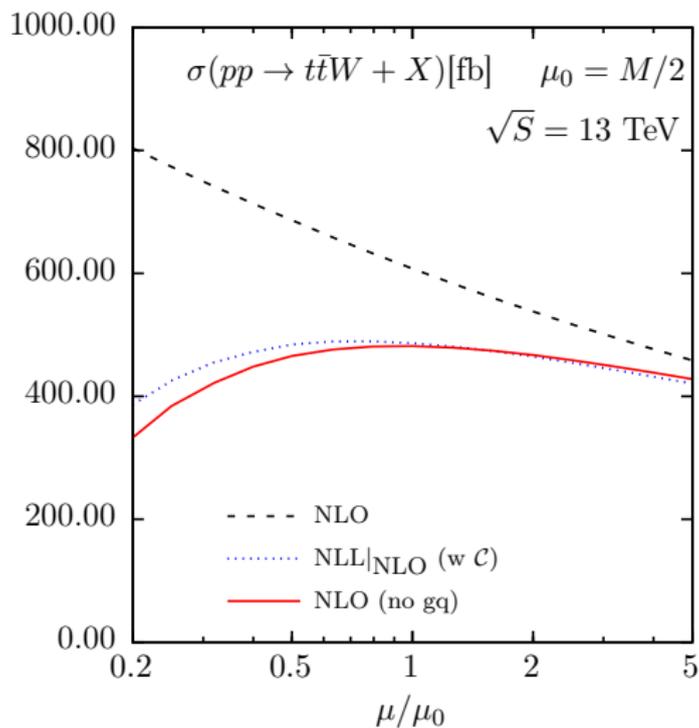
Comparison NLO and expanded $t\bar{t}W$



Preliminary



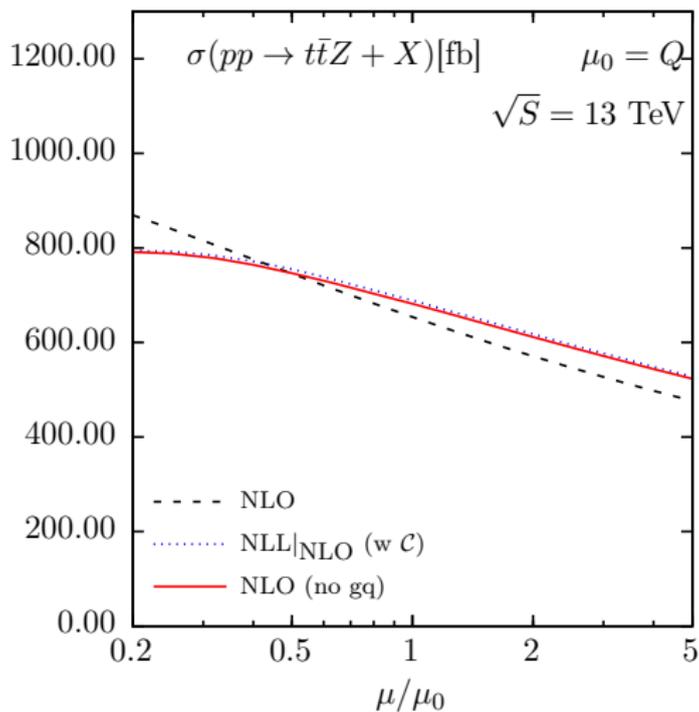
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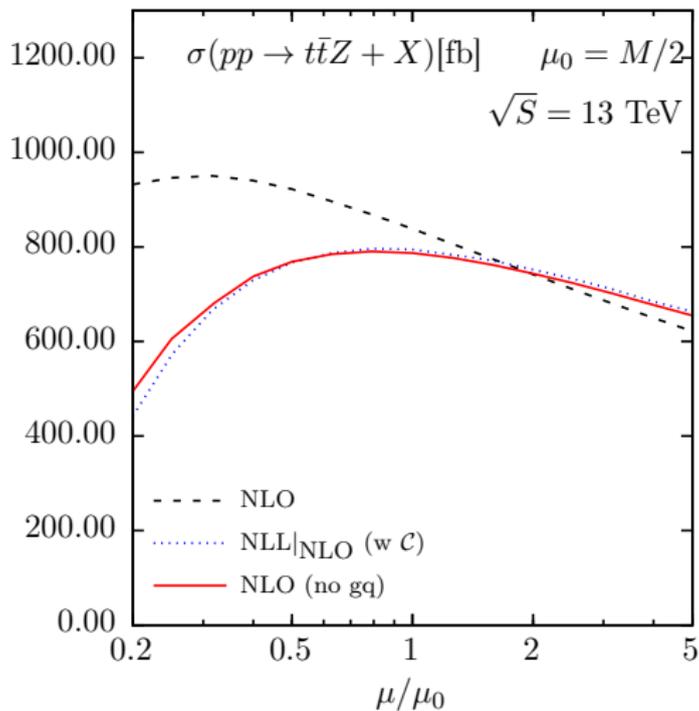
Comparison $t\bar{t}Z$ NLO vs expanded



Preliminary



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Preliminary



Cross sections for $t\bar{t}W/Z$

Total inclusive cross sections, $\mu_F = \mu_R = Q$:

- ▶ $\sigma_{t\bar{t}W^+} = 320^{+12.2\%}_{-10.9\%} \text{ fb}$
- ▶ $\sigma_{t\bar{t}W^-} = 162^{+12.4\%}_{-11.0\%} \text{ fb}$
- ▶ $\sigma_{t\bar{t}Z} = 652^{+14.1\%}_{-12.7\%} \text{ fb}$



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NNLL matched to NLO:

- ▶ $\sigma_{t\bar{t}W^+} = 339_{-8.6\%}^{+8.9\%}$ fb $K_{\text{NNLL}} = 1.06$
- ▶ $\sigma_{t\bar{t}W^-} = 174_{-8.6\%}^{+8.8\%}$ fb $K_{\text{NNLL}} = 1.08$
- ▶ $\sigma_{t\bar{t}Z} = 841_{-8.4\%}^{+8.2\%}$ fb $K_{\text{NNLL}} = 1.29$

Preliminary



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Total inclusive cross sections, $\mu_R = \mu_F = \frac{M}{2}$
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- ▶ $\sigma_{t\bar{t}Z} = 834^{+9.6\%}_{-11.3\%} \text{ fb}$



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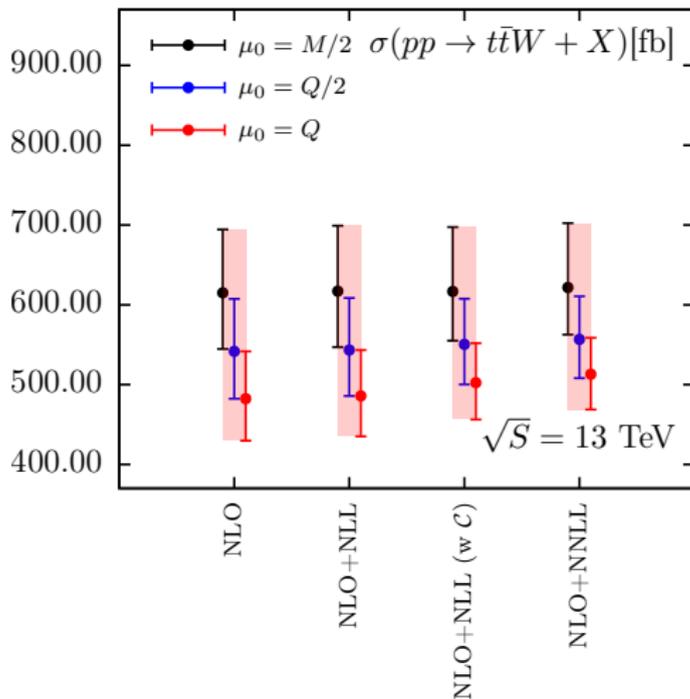
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- ▶ $\sigma_{t\bar{t}W^+} = 412^{+12.9\%}_{-9.6\%}$ fb $K_{\text{NNLL}} = 1.01$
- ▶ $\sigma_{t\bar{t}W^-} = 210^{+13.1\%}_{-9.5\%}$ fb $K_{\text{NNLL}} = 1.02$
- ▶ $\sigma_{t\bar{t}Z} = 868^{+6.8\%}_{-7.9\%}$ fb $K_{\text{NNLL}} = 1.04$

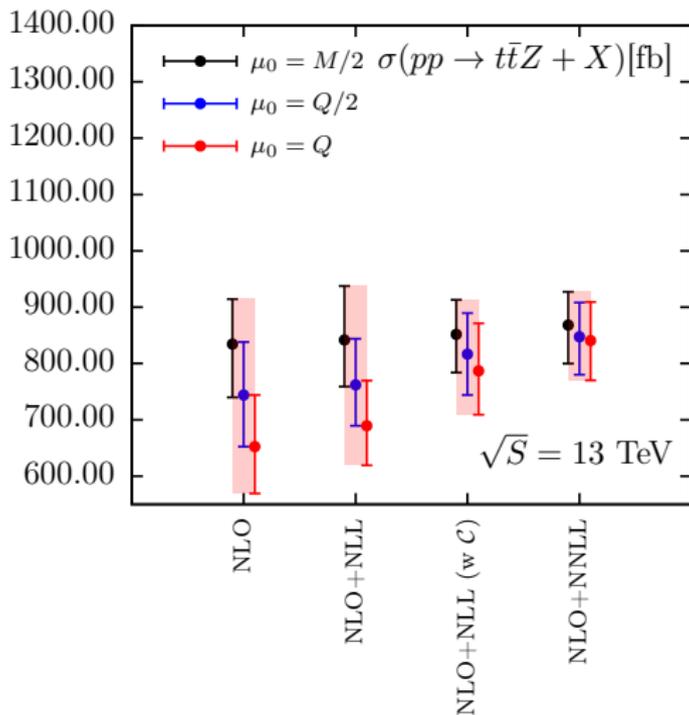
Preliminary

Results for $t\bar{t}W$



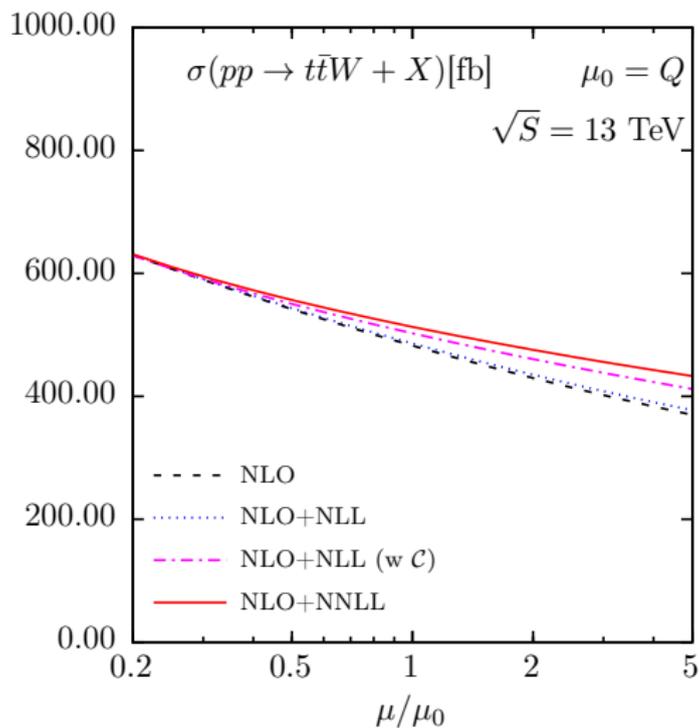
Preliminary

Results for $t\bar{t}Z$



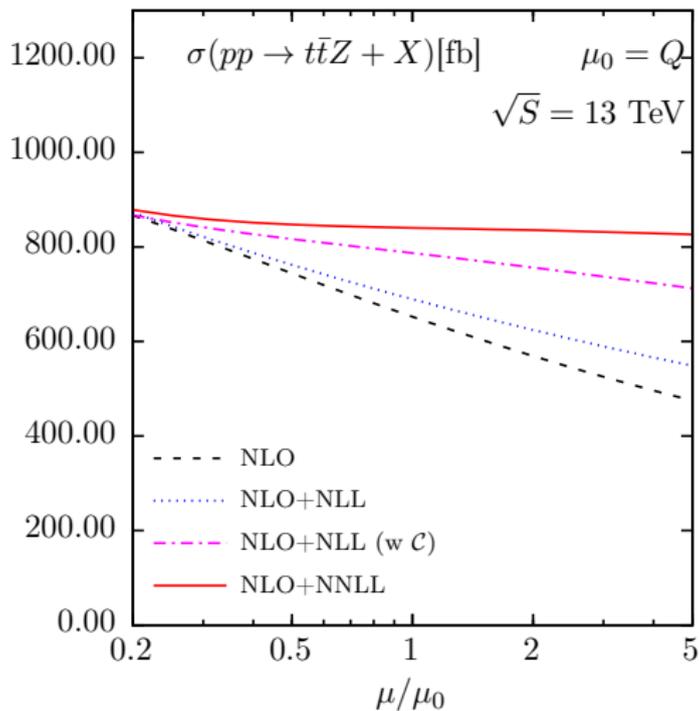
Preliminary

Scale dependence $t\bar{t}W$ $\mu_F = \mu_R$



Preliminary

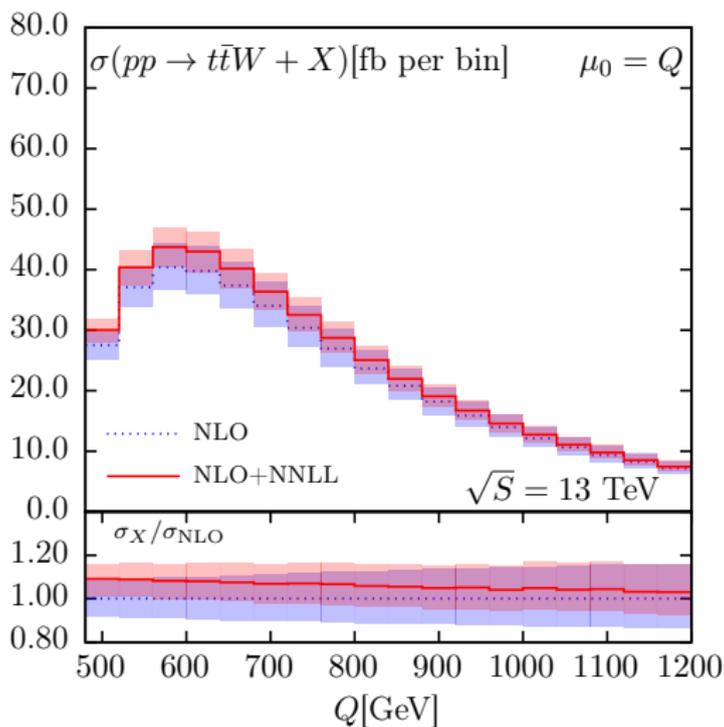
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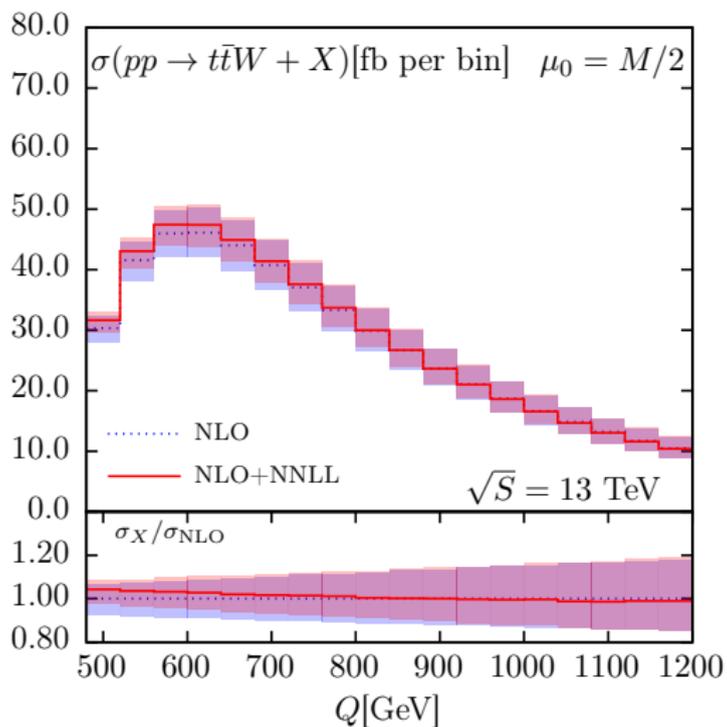


Differential in Q $t\bar{t}W$ $\mu_F = \mu_R = Q$



Preliminary

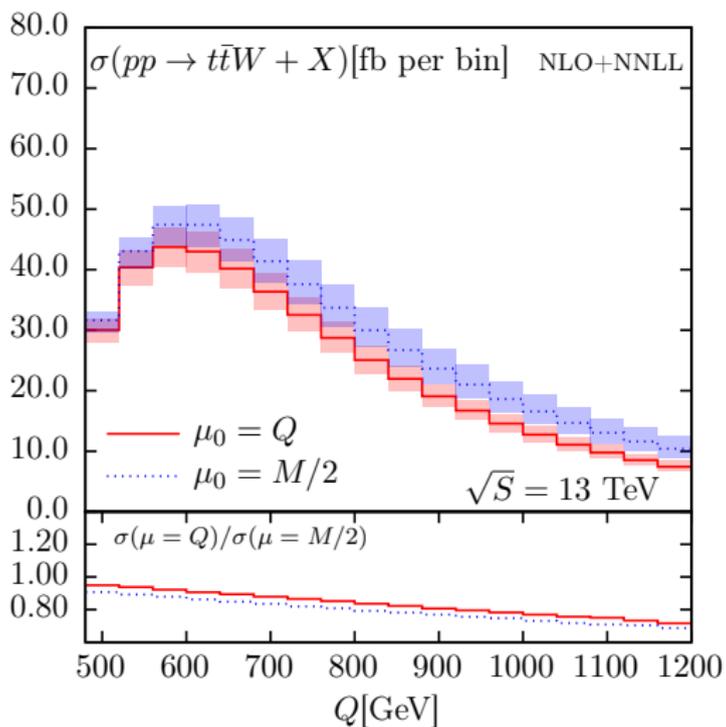
Differential in Q $t\bar{t}W$ $\mu_F = \mu_R = \frac{M}{2}$



Preliminary



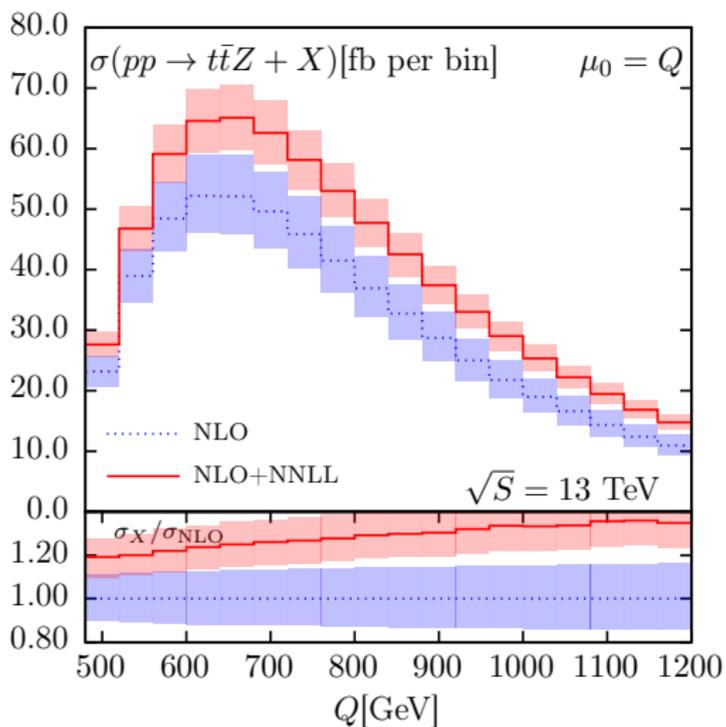
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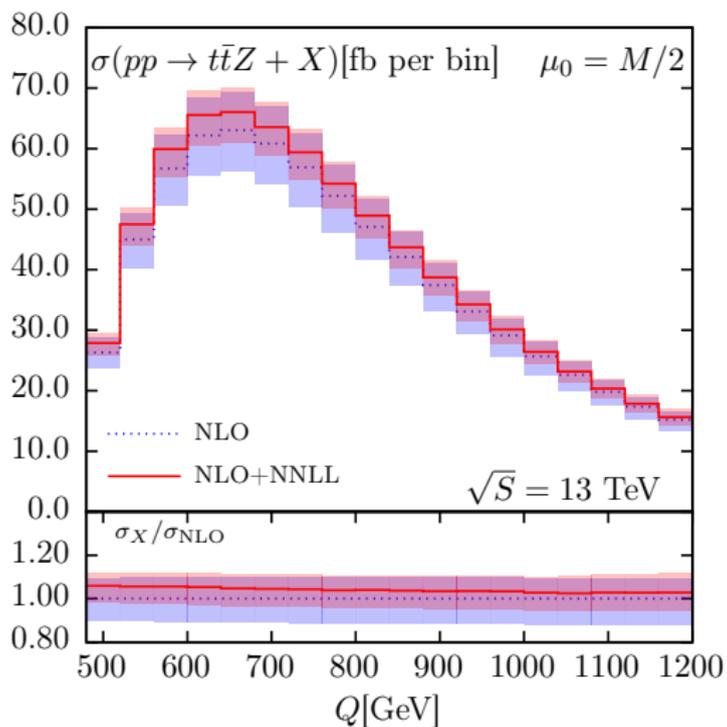
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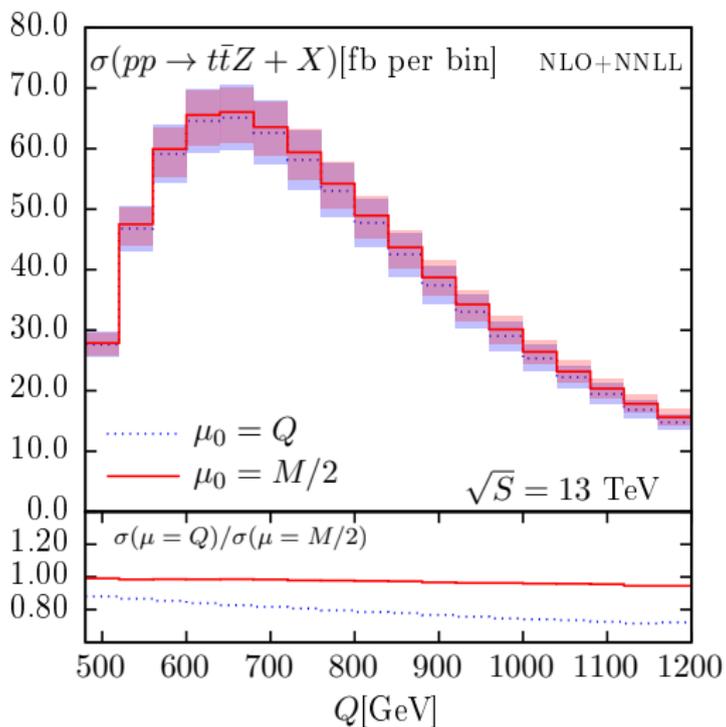
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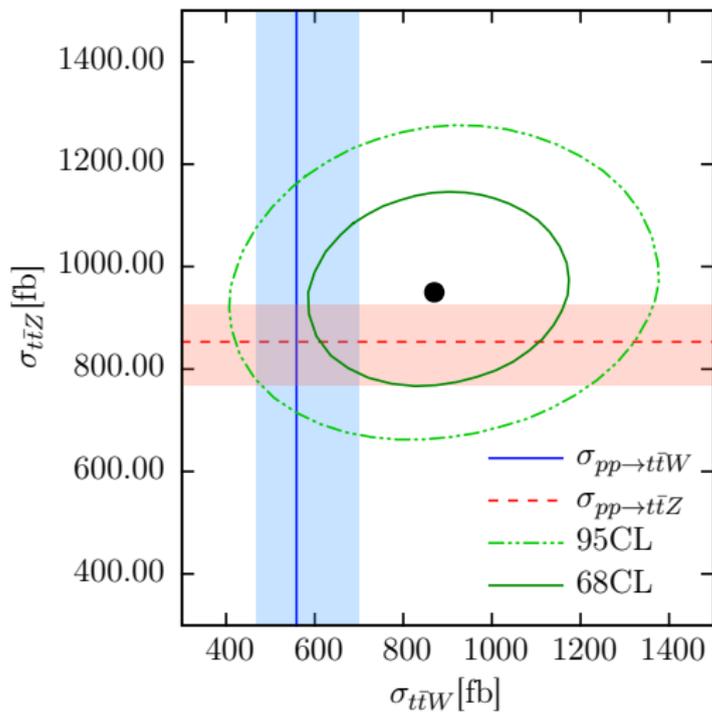
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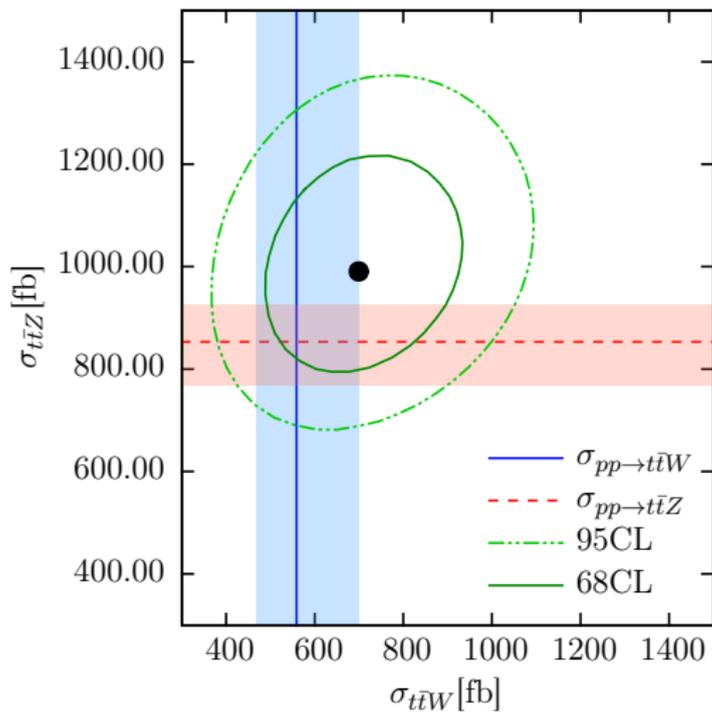
Comparison with ATLAS measurements



Preliminary



Comparison with CMS measurements



Preliminary

Summary and Outlook



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Cross sections for $t\bar{t}W/Z$

Total inclusive cross sections, $\mu_F = \mu_R = Q$:

- ▶ $\sigma_{t\bar{t}W^+} = 320_{-10.9\% - 3.2\%}^{+12.2\% + 3.2\%}$ fb
- ▶ $\sigma_{t\bar{t}W^-} = 162_{-11.0\% - 3.6\%}^{+12.4\% + 3.6\%}$ fb
- ▶ $\sigma_{t\bar{t}Z} = 652_{-12.7\% - 3.3\%}^{+14.1\% + 3.3\%}$ fb

NNLL matched to NLO:

- ▶ $\sigma_{t\bar{t}W^+} = 339_{-8.6\% - 3.2\%}^{+8.9\% + 3.2\%}$ fb $K_{\text{NNLL}} = 1.06$
- ▶ $\sigma_{t\bar{t}W^-} = 174_{-8.6\% - 3.7\%}^{+8.8\% + 3.7\%}$ fb $K_{\text{NNLL}} = 1.08$
- ▶ $\sigma_{t\bar{t}Z} = 841_{-8.4\% - 3.1\%}^{+8.2\% + 3.1\%}$ fb $K_{\text{NNLL}} = 1.29$

Preliminary



Cross sections for $t\bar{t}W/Z$

Total inclusive cross sections, $\mu_R = \mu_F = \frac{M}{2}$

NLO:

$$\blacktriangleright \sigma_{t\bar{t}W^+} = 409_{-11.4\% -3.4\%}^{+12.7\% +3.4\%} \text{ fb}$$

$$\blacktriangleright \sigma_{t\bar{t}W^-} = 206_{-11.6\% -3.8\%}^{+13.3\% +3.8\%} \text{ fb}$$

$$\blacktriangleright \sigma_{t\bar{t}Z} = 834_{-11.3\% -3.6\%}^{+9.6\% +3.6\%} \text{ fb}$$

NNLL matched to NLO:

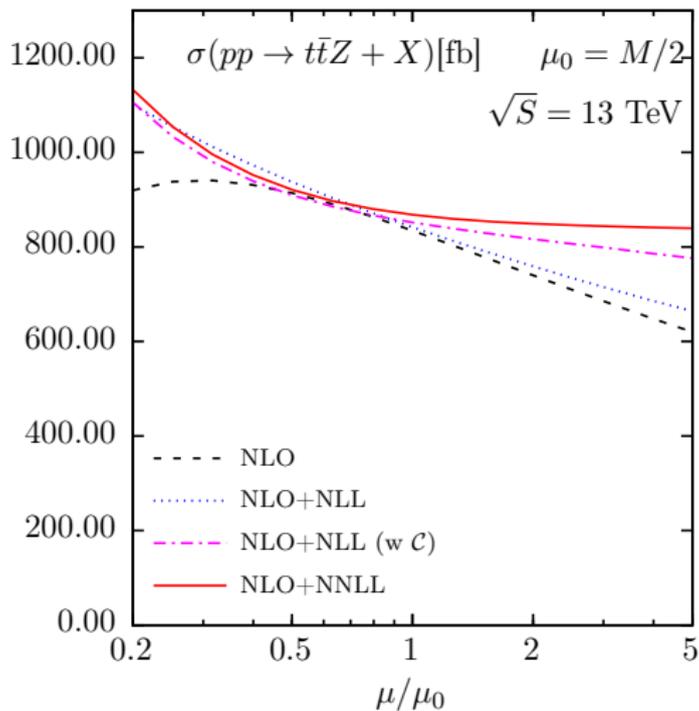
$$\blacktriangleright \sigma_{t\bar{t}W^+} = 412_{-9.6\% -3.4\%}^{+12.9\% +3.4\%} \text{ fb} \quad K_{\text{NNLL}} = 1.01$$

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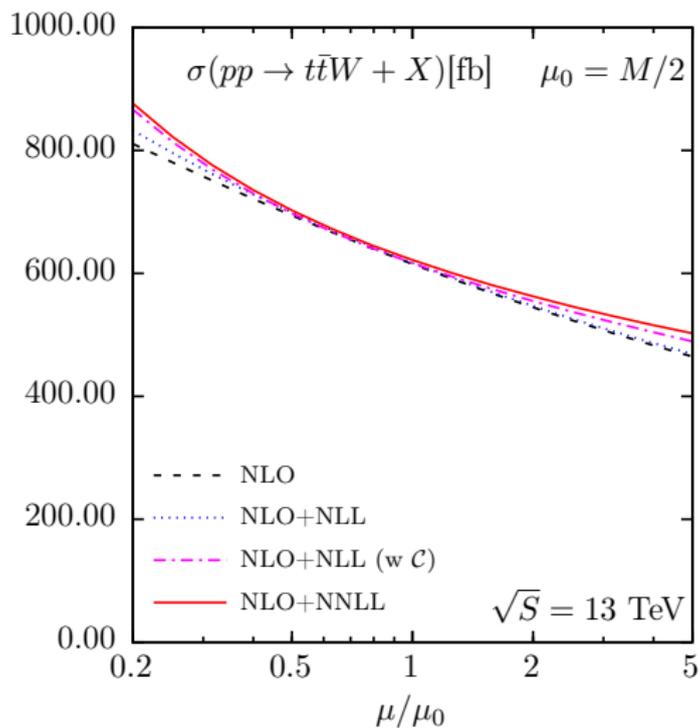
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Scale dependence $t\bar{t}W$ $\mu_F = \mu_R$



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