



# Lepton flavor violation induced by a neutral scalar at future lepton colliders

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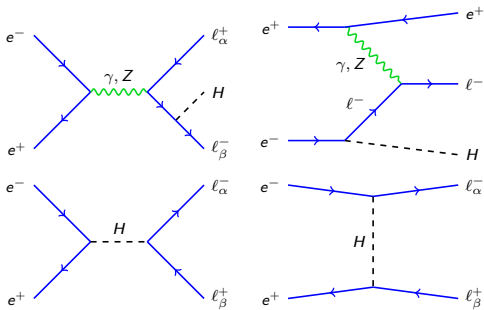
based on

P. S. B. Dev, R. N. Mohapatra & YCZ, 1711.08430, accepted by **PRL**  
(See also P. S. B. Dev, R. N. Mohapatra & YCZ, 1803.11167)

contributing to **CEPC CDR** & **CLIC CERN Yellow Book**

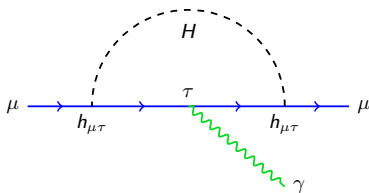
# Outline

- Motivations
- Effective LFV couplings of a (light) BSM neutral scalar  $H$
- On-shell production of  $H$  at CEPC & ILC
- Off-shell production of  $H$  at CEPC & ILC
- Prospects and discussions



# Motivation: LFV beyond SM

- muon  $g - 2$  [Carena, Giudice, Wagner '96; Raidal+ '08; Wolfgang Altmannshofer, Carena, Crivellin '16]



$H$ : beyond SM scalar

- neutrino mass generation [Dreiner, Nickel, Staub+ '12; de Gouvea, P. Vogel '13; Vicente '15; Lindner, Platscher, Queiroz '16]

charged LFV is always connected to neutrino mass generation  
by beyond SM scalars.

see also Altmannshofer, Gori Kagan+ '15; Altmannshofer, Eby, Gori '16

# Well-motivated underlying models

- RPV SUSY: LFV couplings of sneutrino to the charged leptons

[Aulakh, Mohapatra '82; Hall, Suzuki '84; Ross, Valle '85; Barbier+ '04; Duggan, Evans, Hirschauer '13]

$$\mathcal{L}_{\text{RPV}} = \frac{1}{2} \lambda_{\alpha\beta\gamma} \widehat{L}_\alpha \widehat{L}_\beta \widehat{E}_\gamma^c$$

- Left-right symmetric models: the  $SU(2)_R$ -breaking scalar  $H_3$

[Dev, Mohapatra, YCZ '16; '16; '17; Maiezza, Senjanović, Vasquez '16]

LFV couplings are generated through mixing of  $H_3$   
with other heavy scalars

- 2HDM: CP-even or odd (heavy) scalars from the 2nd doublet

[Branco+ '11; Crivellin, Heeck, Stoffer '15]

LFV couplings are induced from small deviation  
from the lepton-specific structure.

- Mirror models: singlet scalar connecting the SM leptons to heavy mirror leptons [Hung '06, '07; Bu, Liao, Liu '08; Chang, Chang, Nugroho+ '16; Hung, Le, Tran+ '17]

LFV couplings arise from the SM-heavy lepton mixing

# Beyond SM neutral Higgs & effective LFV couplings

- The most efficient way to probe the LFV couplings:  
future lepton colliders: CEPC, ILC, FCC-ee, CLIC  
if the beyond scalar  $H$  is hadrophobic and does not mixing sizably with the SM Higgs.
- Model-independent effective LFV couplings of  $H$

$$\mathcal{L}_Y = h_{\alpha\beta} \bar{l}_{\alpha,L} H l_{\beta,R} + \text{H.c.}$$

For simplicity, we assume  $h_{\alpha\beta}$  are real, symmetric,  $H$  is CP-even.

*$H$  might originate from a isospin singlet, doublet or triplet, depending on specific underlying models.*

Effective Dim-4 couplings  $\neq$  Effective 4-fermion couplings like  $\frac{1}{\Lambda^2} (\bar{e}e)(\bar{e}\mu)$

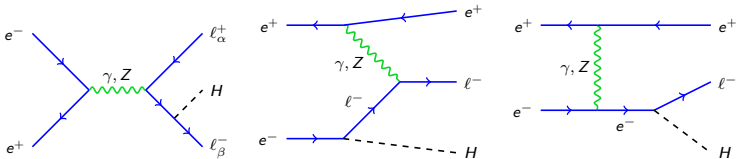
[Kabachenko, Pirogov '97; Ferreira, Guedes, Santos '06; Aranda, Flores-Tlalpa, Ramirez-Zavaleta+ '09; Murakami, Tait '14; Cho, Shimo '14]

$$m_H < \sqrt{s} \Rightarrow \text{on-shell production}$$

# On-shell & off-shell production

- On-shell production (based on the process  $ee \rightarrow \ell\ell$ )

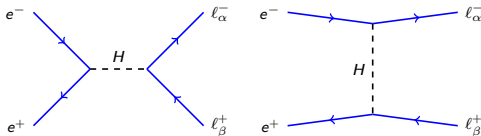
$$e^+e^- \rightarrow \ell_\alpha^\pm \ell_\beta^\mp + H$$



- Off-shell production (at resonance when  $m_H \simeq \sqrt{s}$ )

might also be mediated by a (light) gauge boson  $Z'$  with LFV couplings [Heeck '16]

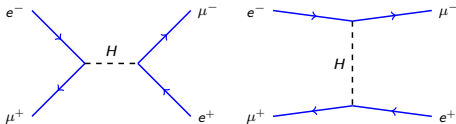
$$e^+e^- \rightarrow \ell_\alpha^\pm \ell_\beta^\mp$$



# Constraints on the LFV couplings: on-shell

On-shell production amplitudes depend *linearly* on the LFV couplings

- muonium anti-muonium oscillation:  $(\bar{\mu}e) \leftrightarrow (\mu\bar{e})$  ( $h_{e\mu}$ )



Oscillation probability [Clark, Love '03]

$$\mathcal{P} = \frac{2(\Delta M)^2}{\Gamma_\mu^2 + 4(\Delta M)^2}$$

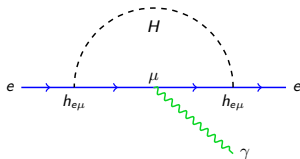
with the  $H$ -induced mass splitting

$$\Delta M = \frac{2\alpha_{\text{EM}}^3 h_{e\mu}^2 \mu^3}{\pi m_H^2}, \quad \mu = \frac{m_e m_\mu}{m_e + m_\mu}$$

# Constraints on the LFV couplings: on-shell

- Electron and muon  $g - 2$  ( $h_{e\ell}, h_{\mu\ell}$ )

[Lindner, Platscher, Queiroz '16]



$$\Delta a_e \simeq \frac{h_{e\mu}^2 m_e m_\mu}{16\pi^2 m_H^2} \left[ 2 \log \left( \frac{m_H^2}{m_\mu^2} \right) - 3 \right].$$

The value of  $h_{e\mu}$  to explain  $(g - 2)_\mu$  discrepancy is excluded by the  $(g - 2)_e$  constraint.

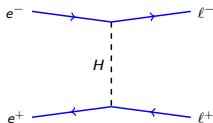
$$\Delta a_\mu \equiv \Delta a_\mu^{\text{exp}} - \Delta a_\mu^{\text{th}} = (2.87 \pm 0.80) \times 10^{-9}$$



# Constraints on the LFV couplings: on-shell

- Bhabha scattering, LEP  $ee \rightarrow \ell\ell$  data ( $h_{e\ell}$ )

[OPAL '03; L3 '03; DELPHI '05]



Effective 4-fermion interaction

$$\sim \frac{h^2}{m_H^2} (\bar{e}\ell)(\bar{e}\ell) \xrightarrow{\text{Fierz transformation}} \frac{1}{\Lambda^2} (\bar{e}\gamma_\mu e)(\bar{\ell}\gamma^\mu \ell)$$

If  $m_H \lesssim \sqrt{s}$ , the LEP limits on the cut-off scale  $\Lambda$  do not apply, and we have to consider the kinetic dependence

$$\frac{1}{m_H^2} \rightarrow \frac{1}{q^2 - m_H^2} \simeq \frac{1}{-s \cos^2 \theta/2 - m_H^2}$$

# SM backgrounds: on-shell

Main SM backgrounds are particle misidentification for

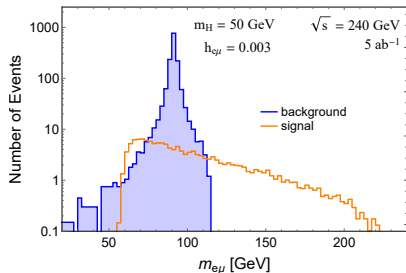
$$e^+e^- \rightarrow \ell_\alpha^+ \ell_\beta^- + X, \quad (\alpha \neq \beta)$$

The mis-identification rate is expected to be small, of order  $10^{-3}$

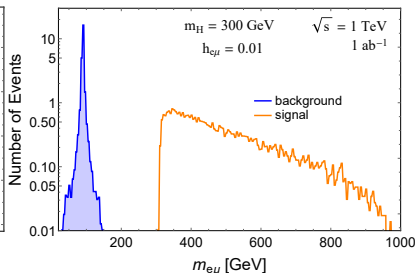
[Milstene, Fisk, Para '06; Hammad, Khalil, Un '16; Yu, Ruan, Boudry+ '17]

Example:

$$e^+e^- \rightarrow Zh \rightarrow (e^+e^-/\mu^+\mu^-)h \rightsquigarrow e^\pm \mu^\mp + h$$

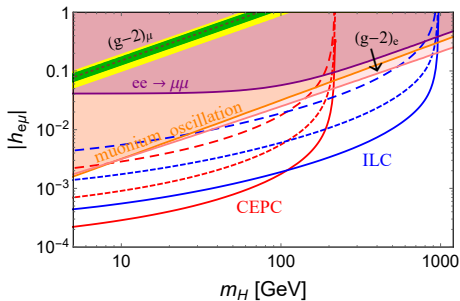


$$S/\sqrt{S+B} = 55$$



$$S/\sqrt{S+B} = 61$$

# CEPC & ILC prospects: on-shell

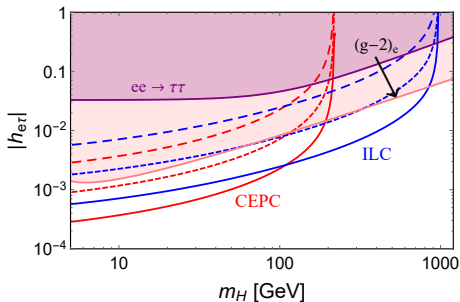


Long-dashed, short-dashed, solid lines:  
1%, 10%, and 100% of the decay products of  $H$  is reconstructible (visible).

Shaded regions are excluded.

Dotted brown line: central values of muon  $g - 2$  anomaly,  
green and yellow bands: the  $1\sigma$  and  $2\sigma$  regions.

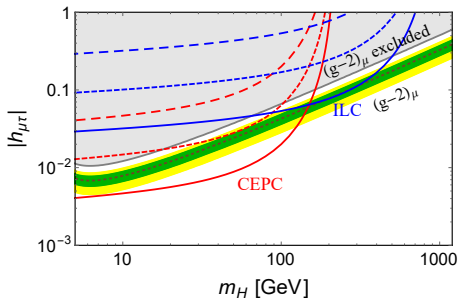
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Dotted brown line: central values of muon  $g - 2$  anomaly,  
green and yellow bands: the  $1\sigma$  and  $2\sigma$  regions.

The muon  $g - 2$  discrepancy can be directly tested at CEPC  
via the searches of  $ee \rightarrow \mu\tau + H$

# Constraints on the LFV couplings: off-shell

Off-shell production amplitudes depend *quadratically* on the LFV couplings

- 3-body LFV decays of muon and tauon, e.g. [Sher, Yuan '91]

$$\Gamma(\tau^- \rightarrow e^+ e^- e^-) \simeq \frac{1}{\delta} \frac{|h_{ee}^\dagger h_{e\tau}|^2 m_\tau^5}{3072\pi^3 m_H^4}, \quad (\delta = 2)$$

- 2-body LFV decays of muon and tauon, e.g. [Harnik, Kopp, Zupan '12]

$$\Gamma(\tau \rightarrow e\gamma) = \frac{\alpha_{\text{EM}} m_\tau^5}{64\pi^4} (|c_L|^2 + |c_R|^2), \quad c_L = c_R \simeq \frac{h_{ee}^\dagger h_{e\tau}}{24m_H^2}.$$

- $h_{ee}, e\mu, e\tau$  contribute to  $(g-2)_e$  & LEP  $ee \rightarrow \ell\ell$  data, [DELPHI '05; Hou, Wong '95]

$$|h_{ee}^\dagger h_{e\tau}| \Rightarrow ee \rightarrow e\tau$$

$$|h_{e\mu}^\dagger h_{e\tau}| \Rightarrow ee \rightarrow \mu\tau \text{ (}t\text{-channel)}$$

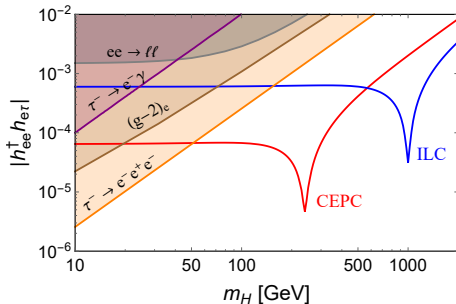
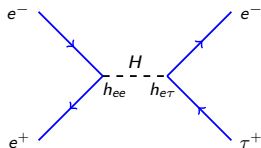
# Constraints on the LFV couplings: off-shell

process	current data	constraints [ $\text{GeV}^{-2}$ ]
$\mu^- \rightarrow e^- e^+ e^-$	$< 10^{-12}$	$ h_{ee}^\dagger h_{e\mu} /m_H^2 < 6.6 \times 10^{-11}$
$\tau^- \rightarrow e^- e^+ e^-$	$< 2.7 \times 10^{-8}$	$ h_{ee}^\dagger h_{e\tau} /m_H^2 < 2.6 \times 10^{-8}$
$\tau^- \rightarrow \mu^- e^+ e^-$	$< 1.8 \times 10^{-8}$	$ h_{ee}^\dagger h_{\mu\tau} /m_H^2 < 1.5 \times 10^{-8}$
$\tau^- \rightarrow \mu^+ e^- e^-$	$< 1.5 \times 10^{-8}$	$ h_{e\mu}^\dagger h_{e\tau} /m_H^2 < 1.9 \times 10^{-8}$
$\tau^- \rightarrow e^- \gamma$	$< 3.3 \times 10^{-8}$	$ h_{ee}^\dagger h_{e\tau} /m_H^2 < 1.0 \times 10^{-6}$
$\tau^- \rightarrow \mu^- \gamma$	$< 4.4 \times 10^{-8}$	$ h_{e\mu}^\dagger h_{e\tau} /m_H^2 < 1.2 \times 10^{-6}$
$(g-2)_e$	$< 5.0 \times 10^{-13}$	$ h_{ee}^\dagger h_{e\tau} /m_H^2 < 1.1 \times 10^{-7}$
		$ h_{e\mu}^\dagger h_{e\tau} /m_H^2 < 1.0 \times 10^{-8}$
$ee \rightarrow ee, \tau\tau$	$\Lambda > 5.7 \& 6.3 \text{ TeV}$	$ h_{ee}^\dagger h_{e\tau} /m_H^2 < 1.4 \times 10^{-7}$
$ee \rightarrow \mu\mu, \tau\tau$	$\Lambda > 5.7 \& 7.9 \text{ TeV}$	$ h_{e\mu}^\dagger h_{e\tau} /m_H^2 < 1.3 \times 10^{-7}$

The  $\mu \rightarrow 3e$  limit is so strong that it leaves no hope to see any signal in the channel  $ee \rightarrow e\mu$  at CEPC & ILC.

# CEPC & ILC prospects: off-shell

$$e^+e^- \rightarrow e^\pm\tau^\mp$$



Resonance effect at  $m_H \simeq \sqrt{s}$  for both CEPC & ILC  
 Width  $\Gamma_H = 10$  (30) GeV at CEPC (ILC)

The off-shell scalar could be probed up to few TeV scale.



# CEPC & ILC prospects: off-shell

$$e^+e^- \rightarrow \mu^\pm \tau^\mp$$

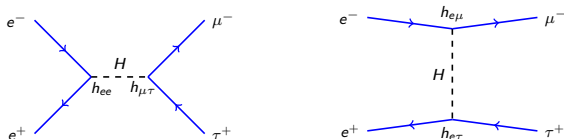
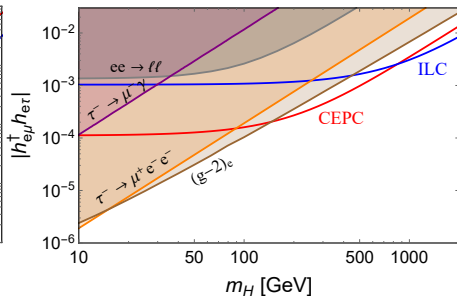
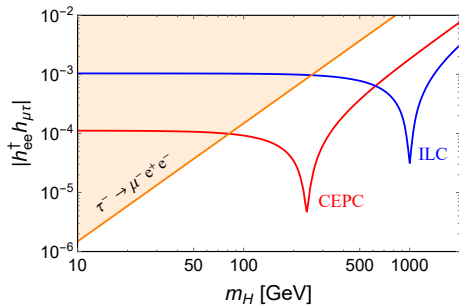


Figure: The s and t channels depend on different  $h^\dagger h$  couplings.



# Conclusion: take-away messages

- A large variety of well-motivated models accommodate a BSM scalar with LFV couplings to the SM leptons, arising at tree or loop level.
- These LFV couplings can be studied in a *model-independent* way at future lepton colliders like CEPC, ILC, FCC-ee & CLIC, which strengthens the physics case for future lepton colliders.
- The BSM neutral scalar  $H$  can be produced on-shell via  $e^+e^- \rightarrow \ell_\alpha^\pm \ell_\beta^\mp + H$  or off-shell via  $e^+e^- \rightarrow \ell_\alpha^\pm \ell_\beta^\mp$ .
- It is promising future lepton colliders could probe a broad region of  $m_H$  and  $h_{\alpha\beta}$  that goes well beyond the existing LFV constraints.
- The scalar mass and couplings for the explanation of the muon  $g-2$  anomaly can be directly tested at future lepton colliders in  $e^+e^- \rightarrow \mu^\pm \tau^\mp + H$ .

Thank you for your attention!