

# SU(5) x U(1) Grand Unification with Minimal Seesaw and Z'-portal Dark Matter

Nobuchika Okada

University of Alabama



In collaboration with Satomi Okada (Yamagata Univ.)  
Digesh Raut (Univ. of Alabama)

Ref: NO, S. Okada & D. Raut, Phys. Lett. B 780 (2018) 422

PHENO 2018 @ Univ. of Pittsburgh, May 7-9, 2018

# Problems of the Standard Model

Although the Standard Model (SM) is the best theory so far, New Physics beyond SM is strongly suggested by both experimental & theoretical points of view

## What is missing?

1. Neutrino masses and flavor mixings

2. Dark matter candidate

They must be supplemented by New Physics

# Minimal gauged U(1)<sub>X</sub> extension of the Standard Model

$$SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)_X$$

- Generalization of the minimal U(1) B-L model
- Anomaly free requirement → 3 right-handed neutrinos (RHNs)
- A SM singlet Higgs → U(1)<sub>X</sub> symmetry breaking  
Majorana mass generation for RHNs
- Type I seesaw is implemented
- U(1)<sub>X</sub> breaking at TeV → LHC Physics for Z' boson

# Introducing $Z_2$ symmetry for a Dark Matter candidate

$$SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)_X \times Z_2$$

Assigning  $Z_2$ -odd parity to one RHN, while even for all the others

$J=1,2$	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)_X$	$Z_2$
$N_R^j$	1	1	0	-1	+
$N_R$	1	1	0	-1	-

NO & Seto,  
PRD 82 (2010) 023507

Anisimov & Di Bari,  
PRD 80 (2009) 073017

→ DM candidate

3 right-handed neutrinos → “2+1 scheme”

➤ 2 RHNs for the Minimal Seesaw

King, NPB 576 (2000) 85;  
Frampton, Glashow & Yanagida,  
PLB 548 (2002) 119

✓ Neutrino oscillation data with one massless eigenstate

➤  $Z_2$ -odd 1 RHN for thermal Dark Matter

# TeV-scale minimal U(1)<sub>X</sub> model with RHN DM

NO & S. Okada,  
PRD 95 (2017)035025

	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	U(1) <sub>X</sub>	Z <sub>2</sub>
$q_L^i$	<b>3</b>	<b>2</b>	1/6	$(1/6)x_H + (1/3)$	+
$u_R^i$	<b>3</b>	<b>1</b>	2/3	$(2/3)x_H + (1/3)$	+
$d_R^i$	<b>3</b>	<b>1</b>	-1/3	$-(1/3)x_H + (1/3)$	+
$\ell_L^i$	<b>1</b>	<b>2</b>	-1/2	$(-1/2)x_H - 1$	+
$e_R^i$	<b>1</b>	<b>1</b>	-1	$(-1)x_H - 1$	+
$H$	<b>1</b>	<b>2</b>	-1/2	$(-1/2)x_H$	+
<b>J=1,2</b> $N_R^j$	<b>1</b>	<b>1</b>	<b>0</b>	-1	+
$N_R$	<b>1</b>	<b>1</b>	<b>0</b>	-1	-
$\Phi$	<b>1</b>	<b>1</b>	<b>0</b>	+2	+

➤ U(1)<sub>X</sub> charge:  $Q_X = Y_f x_H + Q_{B-L}^f$

➤ The minimal B-L model is in the limit of  $x_H \rightarrow 0$

# New Yukawa terms in Lagrangian

$$\mathcal{L}_{Yukawa} \supset - \sum_{i=1}^3 \sum_{j=1}^2 Y_D^{ij} \bar{\ell}_L^i H N_R^j$$
$$- \frac{1}{2} \sum_{k=1}^2 Y_N^k \Phi \overline{N_R^k}^C N_R^k - \frac{1}{2} Y_N \Phi \overline{N_R}^C N_R$$

➤ Mass generation for RHNs and Z' boson by

$$\langle \Phi \rangle = \frac{v_X}{\sqrt{2}}$$

$$m_N^j = \frac{Y_N^j}{\sqrt{2}} v_X, \quad m_{DM} = \frac{Y_N}{\sqrt{2}} v_X,$$

$$m_{Z'} = g_X \sqrt{4v_X^2 + \frac{v^2}{4}} \simeq 2g_X v_X$$

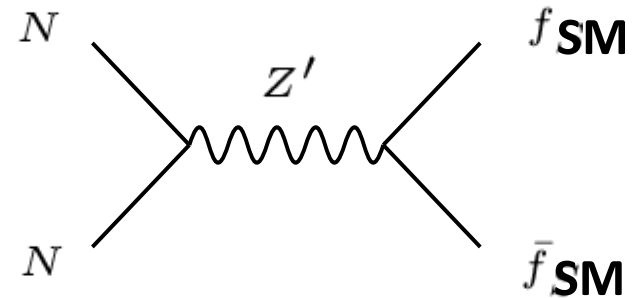
➤ Minimal Seesaw mechanism after EW symmetry breaking

# Phenomenology of

## TeV-scale minimal $U(1)_X$ model with RHN DM

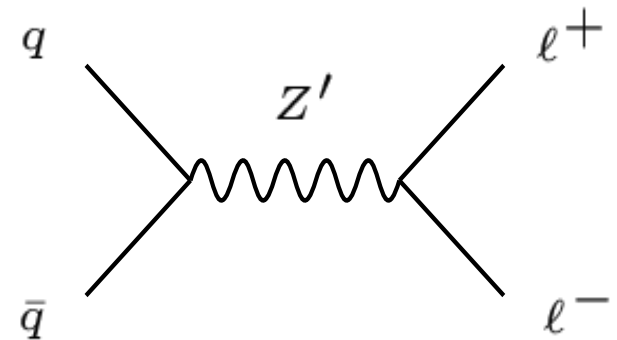
### (1) $Z'$ -portal RHN DM

RHN DM communicates with the SM particles through  $Z'$  boson mediated processes



### (2) $Z'$ boson search at the LHC Run-2

Search for a narrow resonance with the di-lepton final state at ATLAS and CMS with LHC Run-2



### (3) Complementarity

between DM physics and LHC physics

It turns out that both of DM physics and LHC physics are controlled by only 3 free parameters:

- U(1)<sub>X</sub> gauge coupling:  $\alpha_X = \frac{g_X^2}{4\pi}$
- Z' boson mass:  $m_{Z'}$
- SM Higgs U(1)<sub>X</sub> charge:  $x_H$

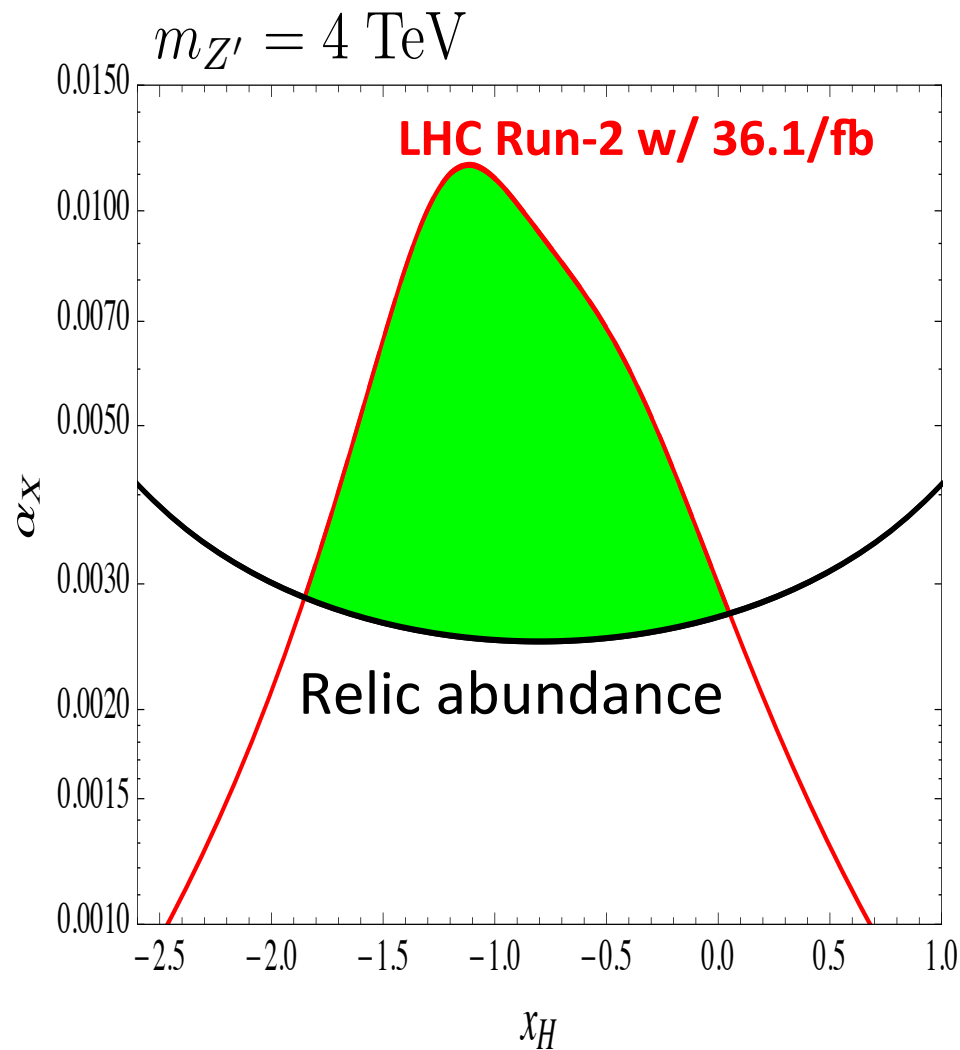
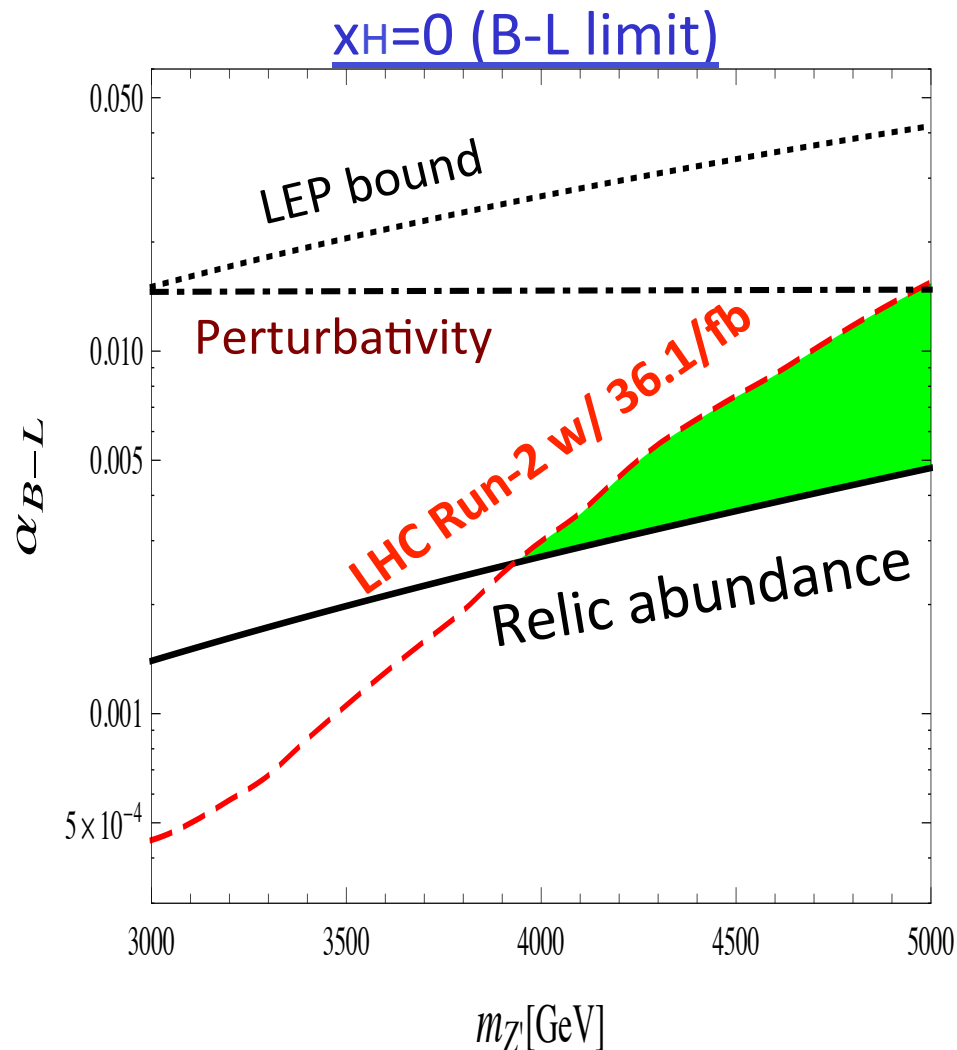
\* To reproduce the observed DM abundance,  $m_{\text{DM}} \simeq m_{Z'}/2$

\*\* For simplicity, 2 RHN mass =  $m_{Z'}$



# Complementarity

- DM relic abundance  $\rightarrow$  upper bound on  $\alpha_X$
- LHC bound from  $Z'$  boson search  $\rightarrow$  upper bound on  $\alpha_X$



We now propose

## Grand unified SU(5) x U(1)x model

into which the our U(1)x model is embedded.

Ref: NO, S. Okada and D. Raut, PLB 780 (2018) 422-426

## Grand Unified Theory paradigm

- Unification of all the SM gauge interactions
- Electric charge quantization
- Mathematical beauty
- Prediction of proton decay

# 1. Embedding the U(1)<sub>X</sub> model into SU(5) x U(1)<sub>X</sub>


Left-handed fermion content:

	SU(3) <sub>C</sub>	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	U(1) <sub>X</sub>	Z <sub>2</sub>
$q_L^i$	<b>3</b>	<b>2</b>	1/6	$(1/6)x_H + 1/3$	+
$(u_R^i)^c$	<b>3*</b>	<b>1</b>	-2/3	$(-2/3)x_H - 1/3$	+
$(d_R^i)^c$	<b>3*</b>	<b>1</b>	+1/3	$(+1/3)x_H - 1/3$	+
$\ell_L^i$	<b>1</b>	<b>2</b>	-1/2	$(-1/2)x_H - 1$	+
$(e_R^i)^c$	<b>1</b>	<b>1</b>	-1	$(+1)x_H + 1$	+
<b>J=1,2</b> $(N_R^J)^c$	<b>1</b>	<b>1</b>	0	+1	+
$(N_R)^c$	<b>1</b>	<b>1</b>	0	+1	-

Left-handed fermion content with  $X_H = -4/5$

	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_X$	$Z_2$
$q_L^i$	<b>3</b>	<b>2</b>	1/6	1/5	+
$(u_R^i)^c$	<b>3*</b>	<b>1</b>	-2/3	1/5	+
$(d_R^i)^c$	<b>3*</b>	<b>1</b>	+1/3	-3/5	+
$\ell_L^i$	<b>1</b>	<b>2</b>	-1/2	-3/5	+
$(e_R^i)^c$	<b>1</b>	<b>1</b>	+1	1/5	+
$J=1,2$ $(N_R^j)^c$	<b>1</b>	<b>1</b>	0	+1	+
$(N_R)^c$	<b>1</b>	<b>1</b>	0	+1	-

  $\rightarrow$  **5\*** in  $SU(5)$

  $\rightarrow$  **1** in  $SU(5)$

  $\rightarrow$  **10** in  $SU(5)$

## Successful Unification of the matters into SU(5) x U(1)x

$$\overline{F}_5^i: (\mathbf{5}^*, -3/5) \supset (d_R^i)^c \oplus \ell_L^i$$

$$F_{10}^i: (\mathbf{10}, 1/5) \supset q_L^i \oplus (u_R^i)^c \oplus (e_R^i)^c$$

$$x_H = -4/5$$

➤ In the presence of 3 RHNs, this GUT model is free from all gauge and mixed-gravitational anomalies.

➤ Electric charge quantization as usual SU(5) GUT

➤  $x_H$  is also quantized by this unification

\* In terms of SO(10) unification, this is  $SO(10) \supset SU(5) \times U(1)$

The Standard SU(5) GUT by Georgi-Glashow is supplemented with the minimal seesaw for the neutrino mass matrix & Z'-portal RHN

Dark Matter: **Grand Unified SU(5) x U(1)x model**

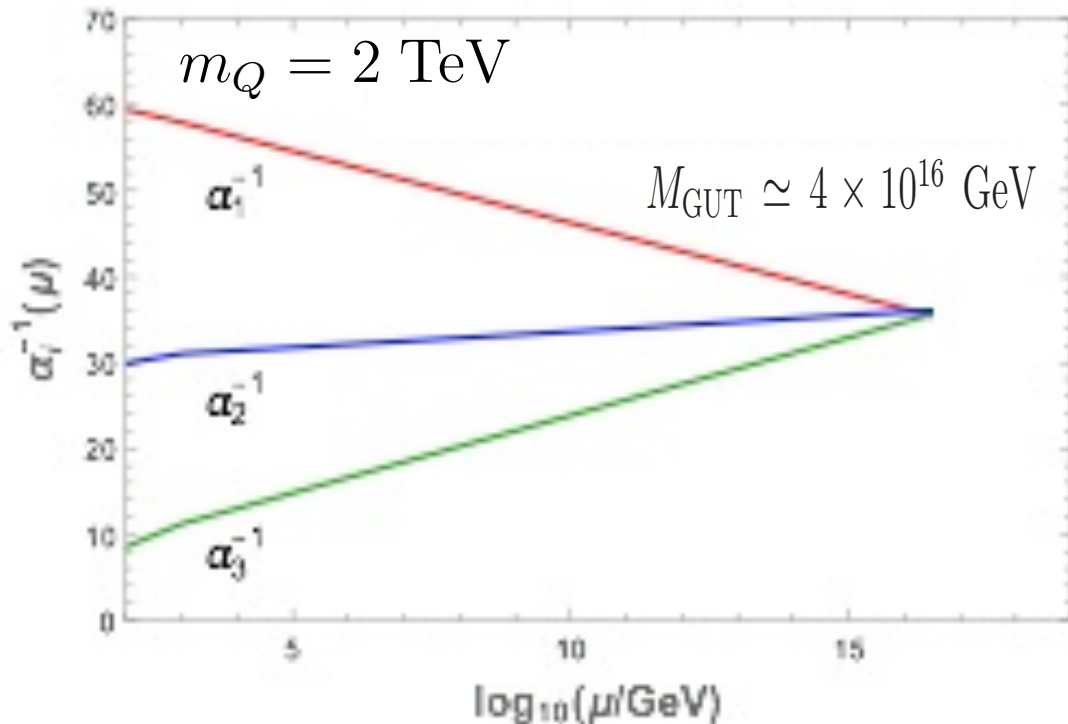
## 2. Phenomenological viability of $SU(5) \times U(1)$ Model

- Successful gauge coupling unification?
- Realizing the SM at low energies?
- Theoretical consistency & consistency with the current experimental results?
- Future prospects?

## 2-1. Gauge coupling unification with extra-quarks

It is known that in the presence of vector-like heavy quarks with mass at the TeV scale, the successful gauge coupling unification can be achieved.

**Amaldi et al., PLB 281 (1992) 374;**  
**Chkareuli et al., PLB 340 (1994) 63;**  
**Choudfury et al., PRD 65 (2002) 053002;**  
**Gogoladze et al., PLB 690 (2010) 495**



In the presence of vector-like quarks:

DL+DR: **(3, 1, 1/3)**

QL+QR: **(3, 2, -1/6)**

with mass of O(TeV)

$\tau_p(p \rightarrow \pi^0 e^+) \simeq 10^{38} \text{ years}$

## 2-2. Realizing the SM at low energies

- SU(5) symmetry breaking in the standard way with an SU(5) adjoint Higgs VEV at  $O(10^{16})$  GeV

$$\langle \Sigma \rangle = v_{\text{GUT}} \text{diag}(1, 1, 1, -3/2, -3/2)$$

- $SU(5) \times U(1)_X \rightarrow SM \times U(1)_X$   
 $U(1)_X$  is broken at the TeV scale

- Realizing the vector-like quarks at the TeV with a mass splitting at the GUT scale

$D_L + D_R^C$  and  $Q_L + Q_R^C$  are unified into  $F_5 + \overline{F}_5$  and  $F_{10} + \overline{F}_{10}$

We introducing Yukawa couplings and mass terms,

$$\mathcal{L}_Y = \overline{F}_5(Y_5 \Sigma - M_5)F_5 + \text{tr} [\overline{F}_{10}(Y_{10} \Sigma - M_{10})F_{10}]$$

and arrange the parameters to leave only D's and Q's light



## 2-3. Theoretical consistency and Consistency with the current experiments

### ➤ Perturbativity of U(1)<sub>X</sub> gauge coupling up to the GUT scale

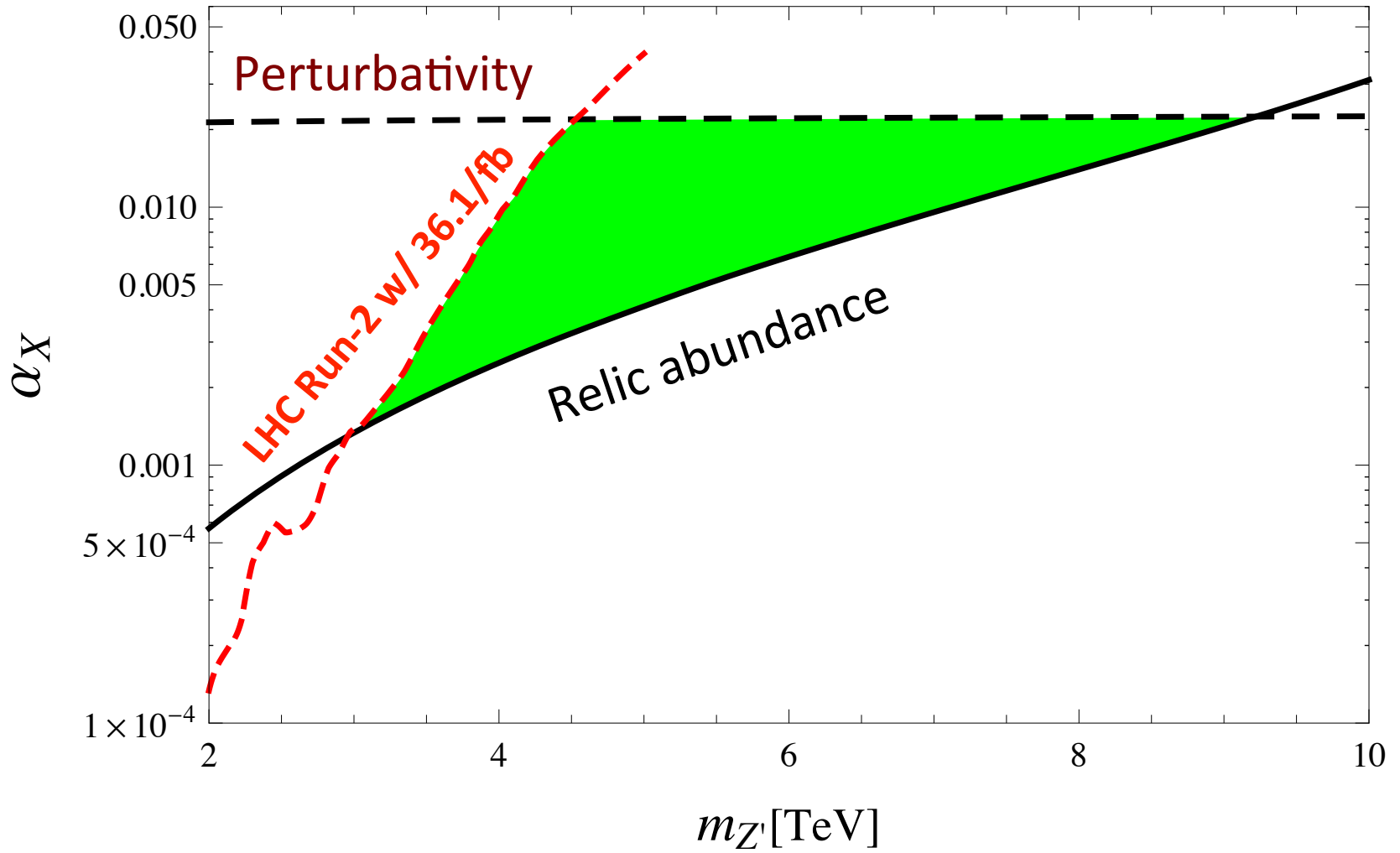
Solution to the Renormalization Group Equation for the U(1)<sub>X</sub> gauge coupling at 1-loop level:

$$\alpha_X(m_{Z'}) = \frac{\alpha_X(M_{\text{GUT}})}{1 + \alpha_X(M_{\text{GUT}}) \frac{b_X}{2\pi} \ln \left[ \frac{M_{\text{GUT}}}{m_{Z'}} \right]}$$

where  $b_X = \frac{48}{5}$ , including the vector-like quarks

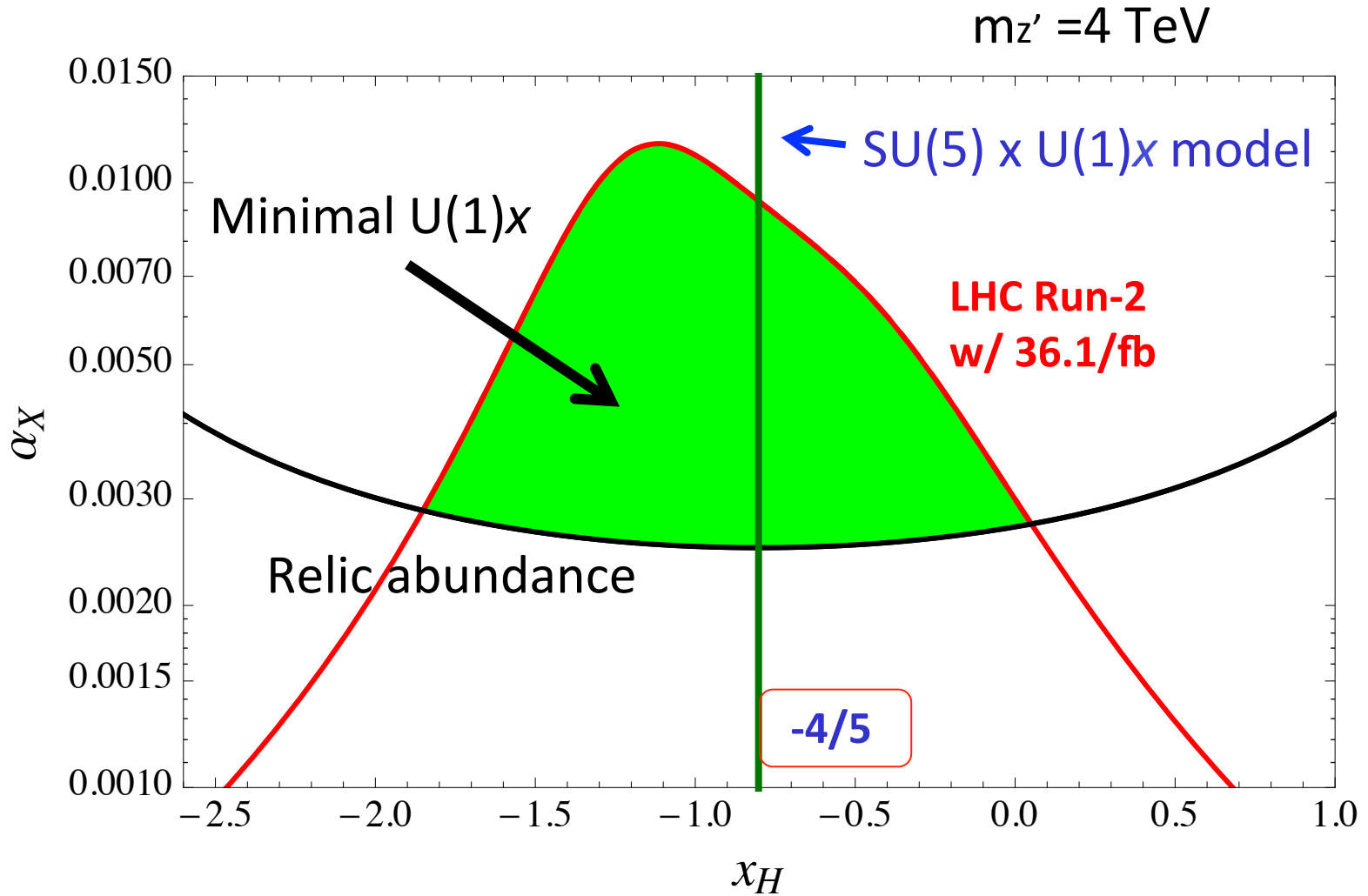
For a requirement,  $\alpha_X(M_{\text{GUT}}) \leq 4\pi$  we find  $\alpha_X(m_{Z'}) \leq 0.022$  for  $m_{Z'} \leq 10 \text{ TeV}$

► Cosmological & LHC Run-2 constraints & perturbativity



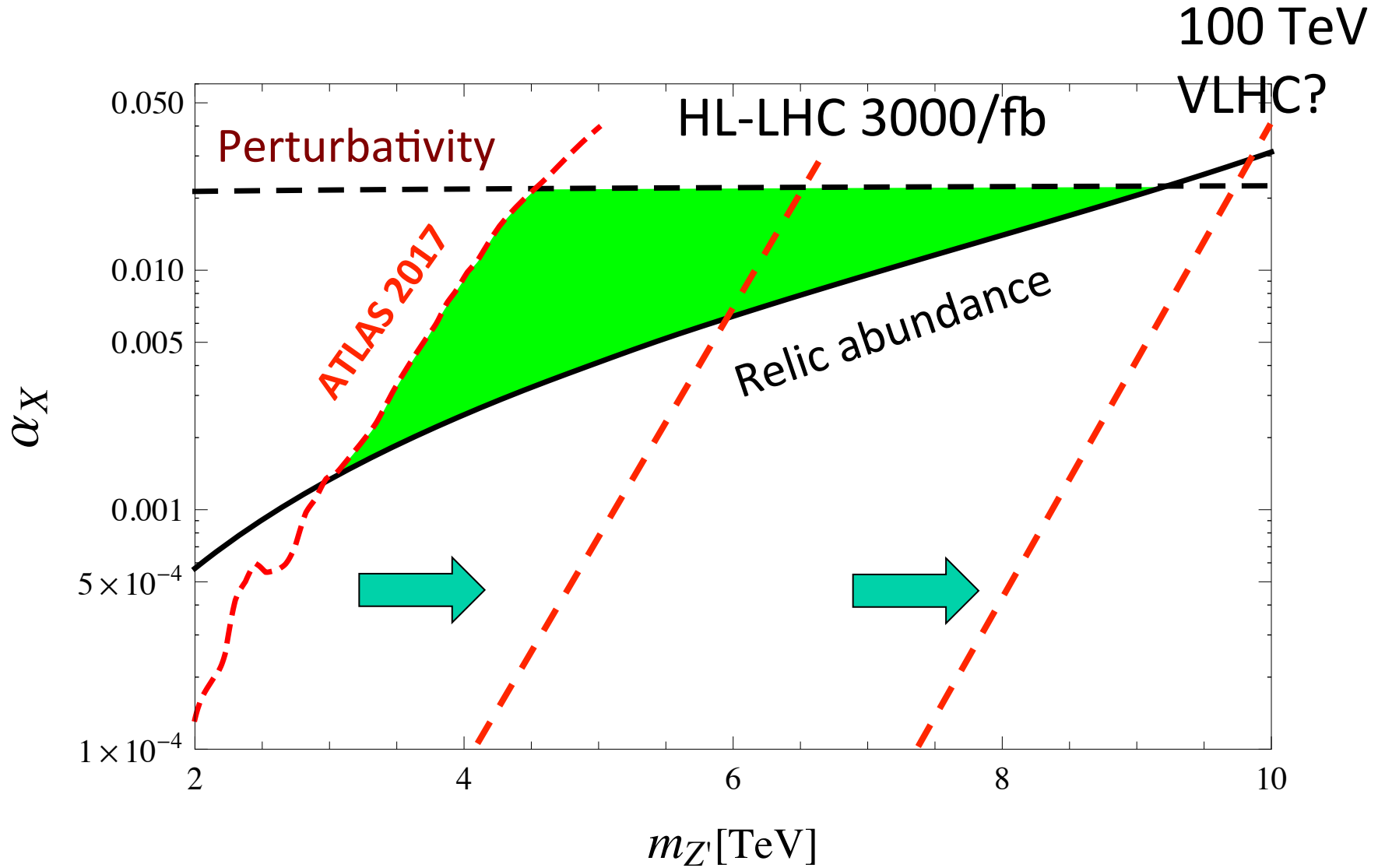
$$3.0 \leq m_{Z'} [\text{TeV}] \leq 9.2$$

# Is $x_H = -4/5$ special?



Interestingly,  $x_H = -4/5$  is almost an ideal choice to survive the severe experimental constraints

## 2-4. Future prospects



$$3.0 \leq m_{Z'} [\text{TeV}] \leq 9.2$$

# Summary

- We have proposed a grand unified  $SU(5) \times U(1)_X$  model, where the standard grand unified  $SU(5)$  model is supplemented by minimal seesaw and  $Z'$ -portal dark matter.
- The  $SU(5)$  symmetry is broken at  $10^{16}$  GeV, while  $U(1)_X$  symmetry is broken at the TeV scale.
- Phenomenological viabilities if this scenario has been investigated.
- The constraints from (i) the DM relic abundance (ii) the LHC search results for  $Z'$  boson and (iii) gauge coupling perturbativity are complementary to narrow down the  $Z'$  boson mass to the range of **3 TeV – 9.2 TeV**, which will be explored in the near future.