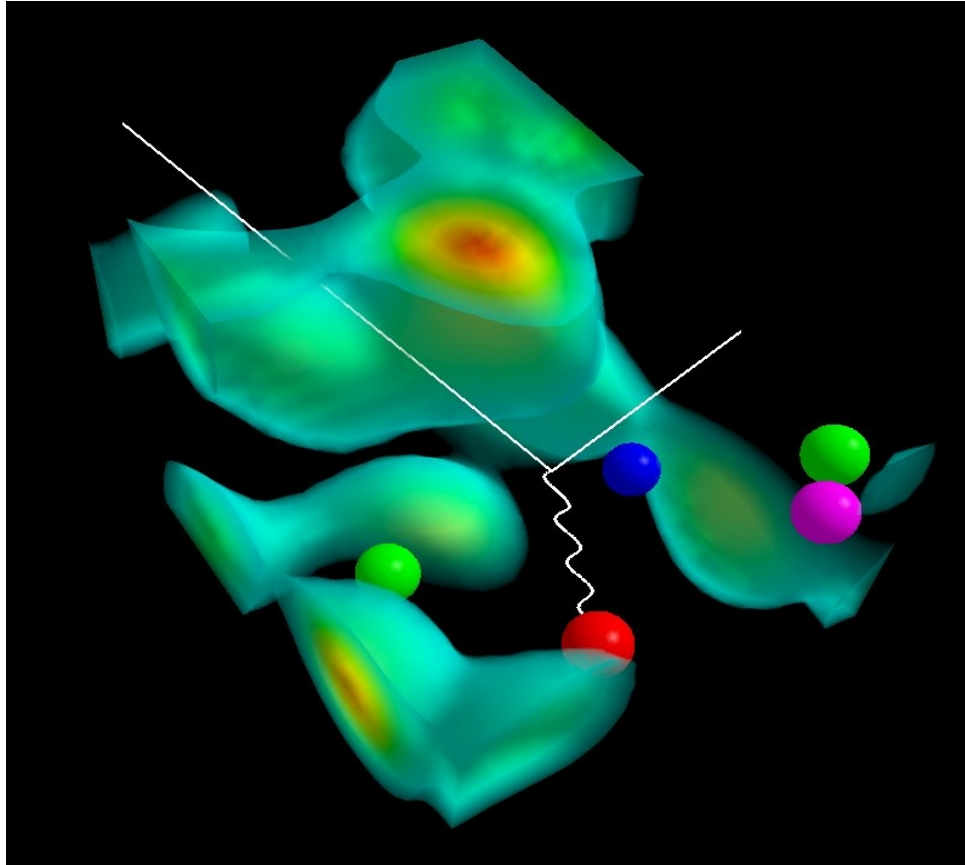


# Nuclei to Neutron Stars: Starting at the Quark Level



Australian Government  
Australian Research Council

**Anthony W. Thomas**

**Many Manifestations of Non-perturbative QCD**  
**Cambury, Brazil : 30<sup>th</sup> April 2018**



# Outline

## I. Nuclei from Quarks

- start from a QCD-inspired model of *hadron* structure
- develop a quantitative theory of nuclear structure

## II. Search for observable effects of the change in hadron structure in-medium

## III. Neutron Stars

## IV. Dark Matter:

- proposed explanation for neutron lifetime anomaly



# I. Insights into nuclear structure

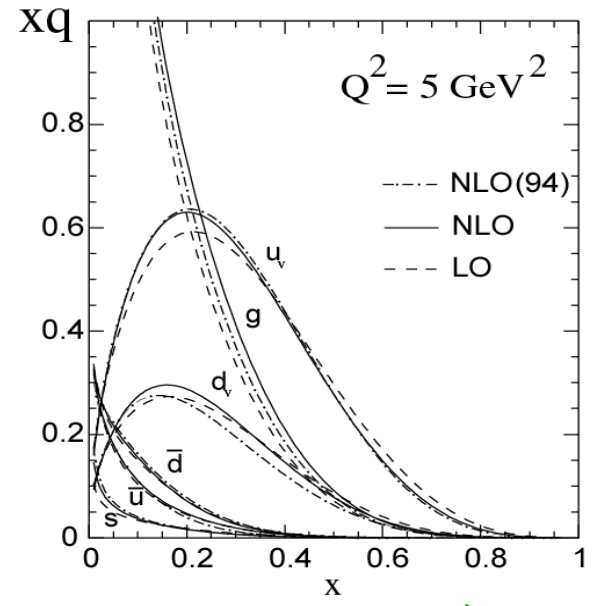
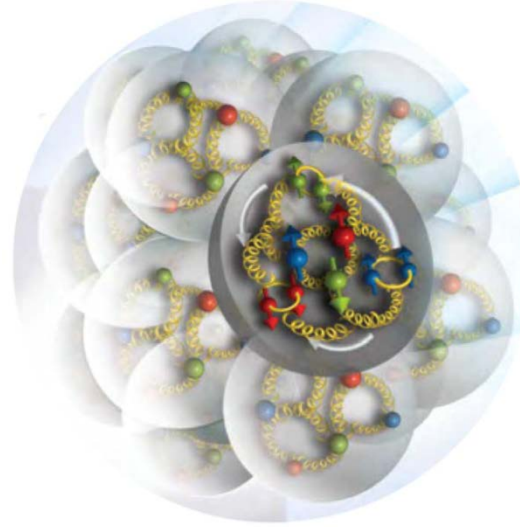
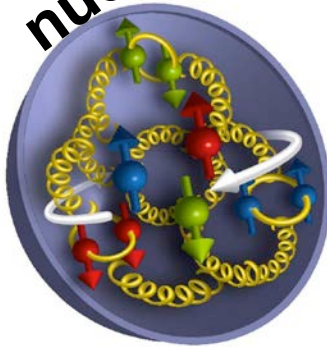
– what is the atomic nucleus?

**There are two very different extremes....**

# A. Nuclear Femtography

Science of mapping the position and motion of quarks and gluons in the nucleus.

**Artist's Conception  
of Quark and Gluons  
in a proton and  
nucleus**



← 12 GeV →

REQUIRES:

- High beam polarization
- High electron current
- High target polarization
- Large solid angle spectrometers

.. is just beginning

From Rolf Ent EINN2017

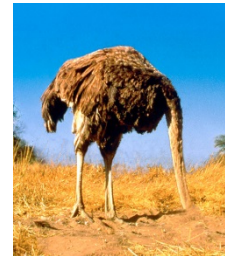
## B. Extreme Chiral Effective Field Theory

- “Considering quarks is in contrast to our **modern understanding of nuclear physics...** the basic degrees of freedom of QCD (quarks and gluons) have to be considered only at higher energies. The energies relevant for nuclear physics are only a few MeV”

- anonymous referee 2017

TRUE

OR



?

- Actually not so modern.....

## D. Alan Bromley (Yale) to Stan Brodsky in 1982

“Stan, you have to understand -- in nuclear physics we are only interested in how protons and neutrons make up a nucleus.

We are not interested in what is inside of a proton.”



Like this beautiful scene – very relaxing

## D. Alan Bromley (Yale) to Stan Brodsky in 1982

“Stan, you have to understand -- in nuclear physics we are only interested in how protons and neutrons make up a nucleus.

We are not interested in what is inside of a proton.”



**Moral: A comfortable picture is not necessarily the right one.....**



# What do we know?

- Since 1970s, intermediate range NN attraction is strong Lorentz scalar
- In relativistic treatments (RHF, RBHF, QHD...) this leads to mean scalar field  $\sim 300$  to  $500$  MeV!!
- This is not small – up to half the nucleon mass
  - death of “wrong energy scale” arguments
- Largely cancelled by large vector mean field BUT these have totally different dynamics:  $\omega^0$  just shifts energies,  $\sigma$  seriously modifies internal hadron dynamics



# Suggests a different approach : QMC Model

(Guichon, Saito, Tsushima et al., Rodionov et al.

- see Saito et al., Prog. Part. Nucl. Phys. 58 (2007) 1 and  
Prog. Part. Nucl. Phys. 100 (2018) 262-297 for reviews)

- Start with quark model (MIT bag/NJL...) for all hadrons

- Introduce a relativistic Lagrangian with  $\sigma$ ,  $\omega$  and  $\rho$  mesons coupling to non-strange quarks

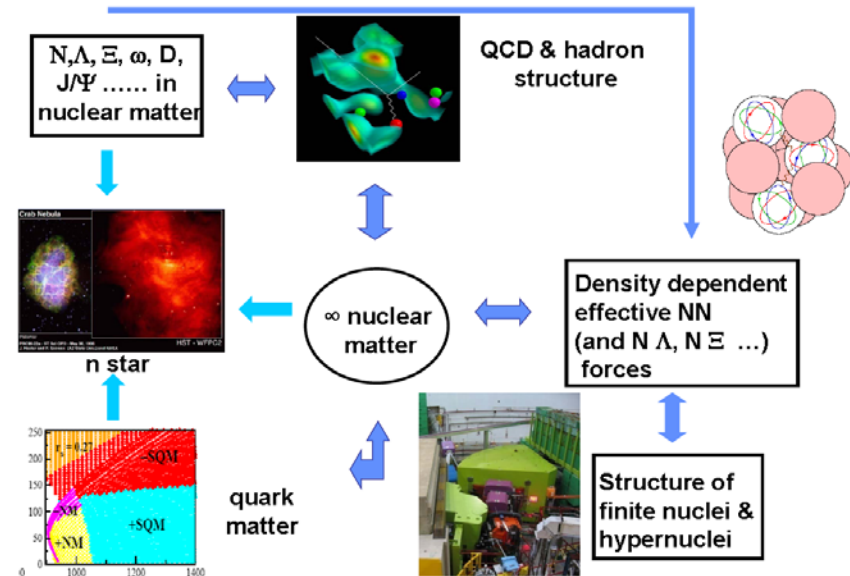
- Hence **only 3 parameters** (if  $\sigma$  mass fixed)

- determine by fitting to:

$\rho_0$ ,  $E/A$  and symmetry energy

- same in dense matter & finite nuclei

- Must solve self-consistently for the internal structure of baryons in-medium



# Self-consistent solution of nuclear matter

$$[i\gamma^\mu\partial_\mu - (m_q - g_\sigma q\bar{\sigma}) - \gamma^0 g_\omega q\bar{\omega}] \psi = 0$$

Source of  $\sigma$   
changes:

$$\int_{Bag} d\vec{r} \bar{\psi}(\vec{r}) \psi(\vec{r})$$

**SELF-CONSISTENCY**

and hence mean scalar field changes...

and hence quark wave function changes....

**THIS PROVIDES A NATURAL SATURATION MECHANISM  
(VERY EFFICIENT BECAUSE QUARKS ARE ALMOST MASSLESS)**

**source is suppressed as mean scalar field increases  
(i.e. as density increases)**

# Quark-Meson Coupling Model (QMC): Role of the Scalar Polarizability of the Nucleon

The response of the nucleon internal structure to the scalar field is of great interest... and importance

$$M^*(\mathbf{r}) = M - g_\sigma \sigma(\mathbf{r}) + \frac{d}{2} (g_\sigma \sigma(\mathbf{r}))^2$$

Non-linear dependence through the scalar polarizability  
 $d \sim 0.22 R$  in original QMC (MIT bag)

Indeed, in nuclear matter at mean-field level (e.g. QMC), this is the **ONLY** place the response of the internal structure of the nucleon enters.

# Application to nuclear structure

# Derivation of Density Dependent Effective Force

Physical origin of density dependent forces of Skyrme type within the quark meson coupling model

P.A.M. Guichon <sup>a,\*</sup>, H.H. Matevosyan <sup>b,c</sup>, N. Sandulescu <sup>a,d,e</sup>,  
A.W. Thomas <sup>b</sup>

Nuclear Physics A 772 (2006) 1–19

- **Start with classical theory of MIT-bag nucleons with structure modified in medium to give  $M_{\text{eff}}(\sigma)$ .**
- **Quantise nucleon motion (non-relativistic), expand in powers of derivatives**
- **Derive equivalent, local energy functional:**

$$\langle H(\vec{r}) \rangle = \rho M + \frac{\tau}{2M} + \mathcal{H}_0 + \mathcal{H}_3 + \mathcal{H}_{\text{eff}} + \mathcal{H}_{\text{fin}} + \mathcal{H}_{\text{so}}$$

# Derivation of effective Force (cont.)

$$\mathcal{H}_0 + \mathcal{H}_3 = \rho^2 \left[ \frac{-3G_\rho}{32} + \frac{G_\sigma}{8(1 + d\rho G_\sigma)^3} - \frac{G_\sigma}{2(1 + d\rho G_\sigma)} + \frac{3G_\omega}{8} \right] \\ + (\rho_n - \rho_p)^2 \left[ \frac{5G_\rho}{32} + \frac{G_\sigma}{8(1 + d\rho G_\sigma)^3} - \frac{G_\omega}{8} \right],$$

$$\mathcal{H}_{\text{eff}} = \left[ \left( \frac{G_\rho}{8m_\rho^2} - \frac{G_\sigma}{2m_\sigma^2} + \frac{G_\omega}{2m_\omega^2} + \frac{G_\sigma}{4M_N^2} \right) \rho_n + \left( \frac{G_\rho}{4m_\rho^2} + \frac{G_\sigma}{2M_N^2} \right) \rho_p \right] \tau_n \\ + p \leftrightarrow n,$$

$$\mathcal{H}_{\text{fin}} = \left[ \left( \frac{3G_\rho}{32m_\rho^2} - \frac{3G_\sigma}{8m_\sigma^2} + \frac{3G_\omega}{8m_\omega^2} - \frac{G_\sigma}{8M_N^2} \right) \rho_n \right. \\ \left. + \left( \frac{-3G_\rho}{16m_\rho^2} - \frac{G_\sigma}{2m_\sigma^2} + \frac{G_\omega}{2m_\omega^2} - \frac{G_\sigma}{4M_N^2} \right) \rho_p \right] \nabla^2(\rho_n) + p \leftrightarrow n,$$

$$\mathcal{H}_{\text{so}} = \nabla \cdot J_n \left[ \left( \frac{-3G_\sigma}{8M_N^2} - \frac{3G_\omega(-1 + 2\mu_s)}{8M_N^2} - \frac{3G_\rho(-1 + 2\mu_v)}{32M_N^2} \right) \rho_n \right. \\ \left. + \left( \frac{-G_\sigma}{4M_N^2} + \frac{G_\omega(1 - 2\mu_s)}{4M_N^2} \right) \rho_p \right] + p \leftrightarrow n.$$

**Spin-orbit  
force  
predicted!**

**Note the totally new, subtle density dependence**

# Systematic approach to finite nuclei

J.R. Stone, P.A.M. Guichon, P. G. Reinhard & A.W. Thomas:  
( Phys Rev Lett, 116 (2016) 092501 )

- **Constrain 3 basic quark-meson couplings ( $g_\sigma^q, g_\omega^q, g_\rho^q$ ) so that nuclear matter properties are reproduced within errors**

$$-17 < E/A < -15 \text{ MeV}$$

$$0.14 < \rho_0 < 0.18 \text{ fm}^{-3}$$

$$28 < S_0 < 34 \text{ MeV}$$

$$L > 20 \text{ MeV}$$

$$250 < K_0 < 350 \text{ MeV}$$

- **Fix at overall best description of finite nuclei (+2 pairing pars)**
- **Benchmark comparison: SV-min 16 parameters (11+5 pairing)**



# Overview of 106 Nuclei Studied – Across Periodic Table

Element	Z	N	Element	Z	N
C	6	6 - 16	Pb	82	116 - 132
O	8	4 - 20	Pu	94	134 - 154
Ca	20	16 - 32	Fm	100	148 - 156
Ni	28	24 - 50	No	102	152 - 154
Sr	38	36 - 64	Rf	104	152 - 154
Zr	40	44 - 64	Sg	106	154 - 156
Sn	50	50 - 86	Hs	108	156 - 158
Sm	62	74 - 98	Ds	110	160
Gd	64	74 - 100			

Not  
fit

N	Z	N	Z
20	10 - 24	64	36 - 58
28	12 - 32	82	46 - 72
40	22 - 40	126	76 - 92
50	28 - 50		

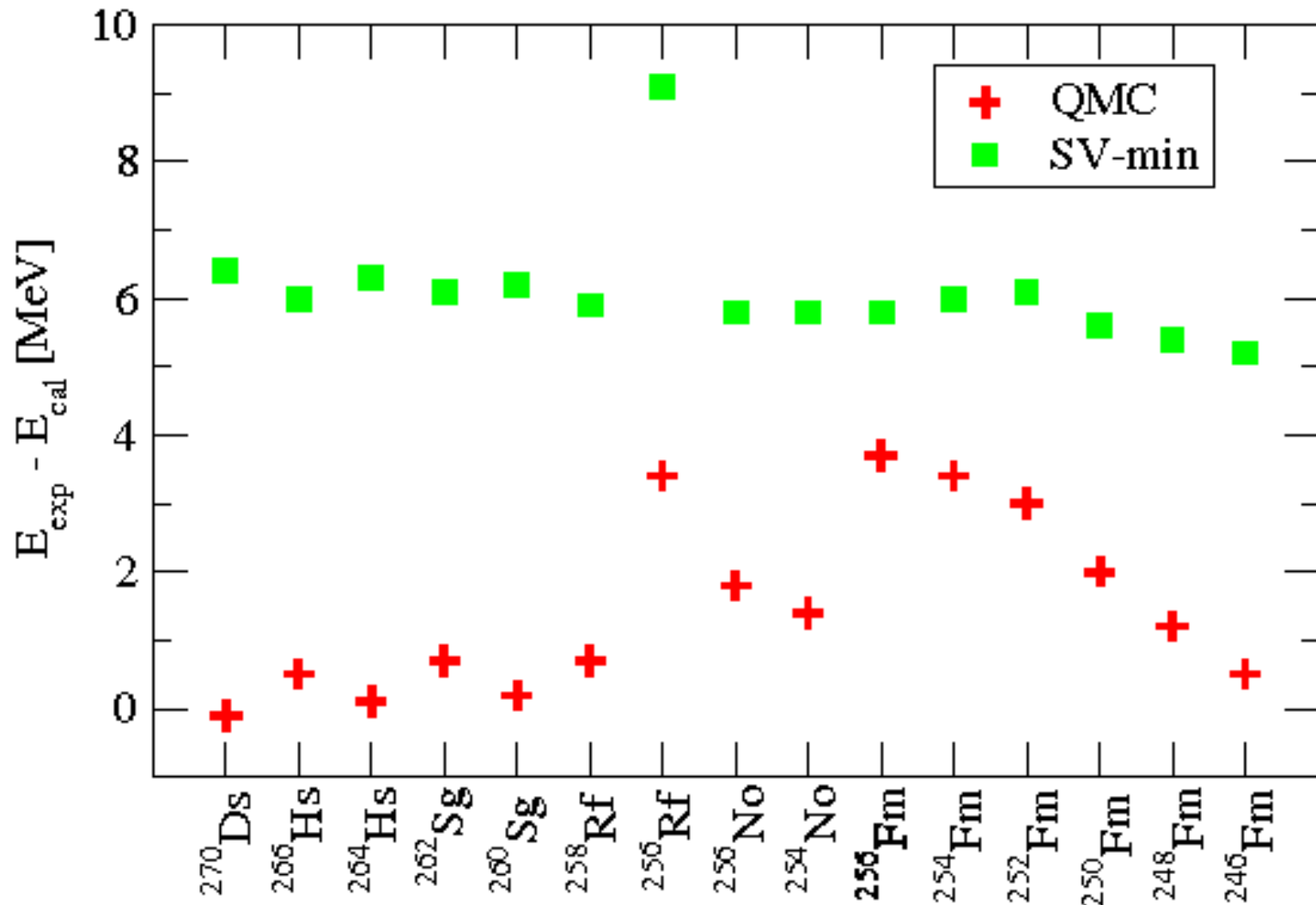
i.e. We look at most challenging cases of p- or n-rich nuclei

# Overview

data	rms error %	
	QMC	SV-min
fit nuclei:		
binding energies	<u>0.36</u>	0.24
diffraction radii	1.62	0.91
surface thickness	10.9	2.9
rms radii	0.71	0.52
pairing gap (n)	57.6	17.6
pairing gap (p)	25.3	15.5
1s splitting: proton	15.8	18.5
1s splitting: neutron	20.3	16.3
superheavy nuclei:		
	<u>0.1</u>	0.3
N=Z nuclei	1.17	0.75
mirror nuclei	1.50	1.00
other	0.35	0.26

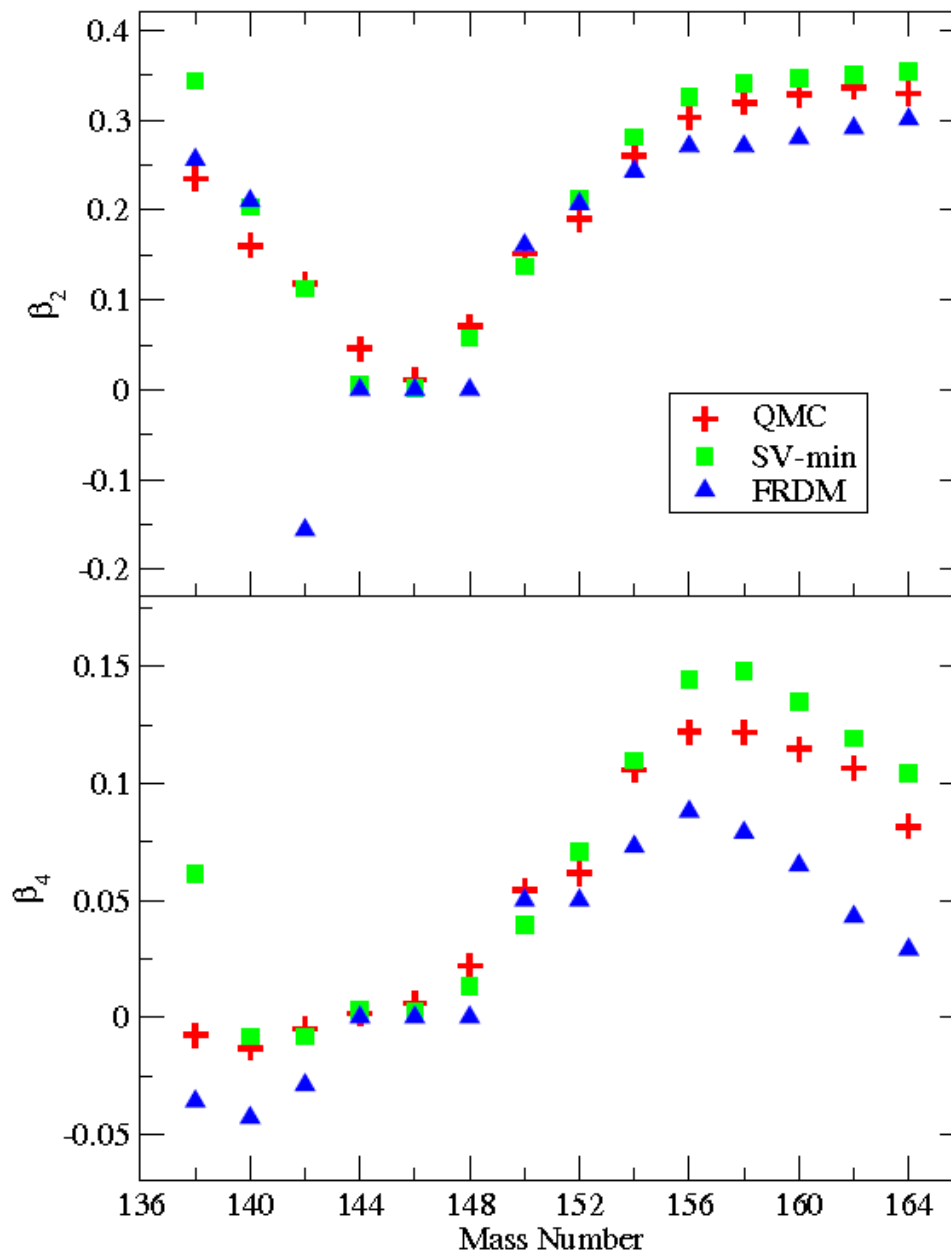
**Stone et al., PRL (2016)**

# Superheavy Binding : 0.1% accuracy

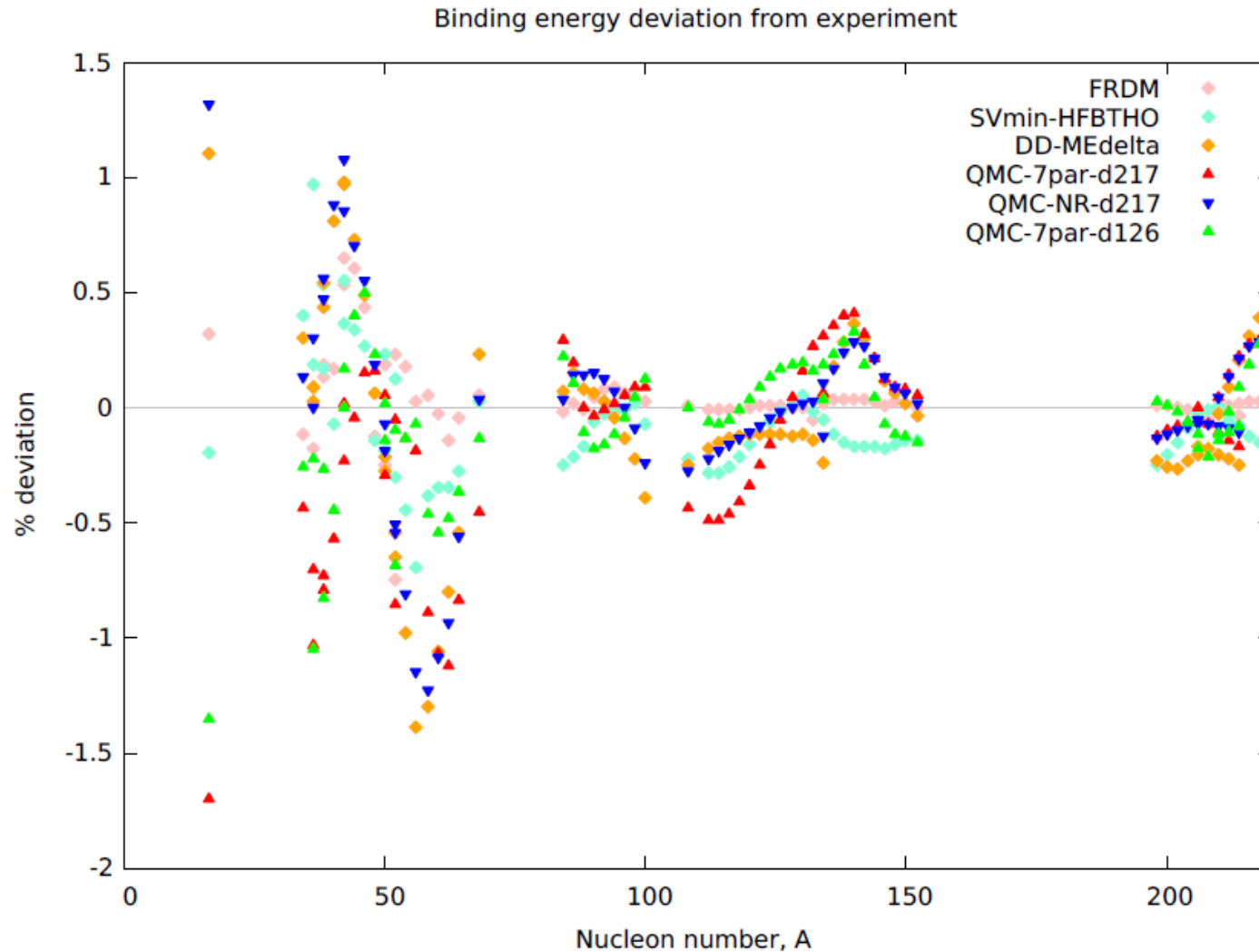


Stone et al., PRL 116 (2016) 092501

# Deformation in Gd (Z=64) Isotopes

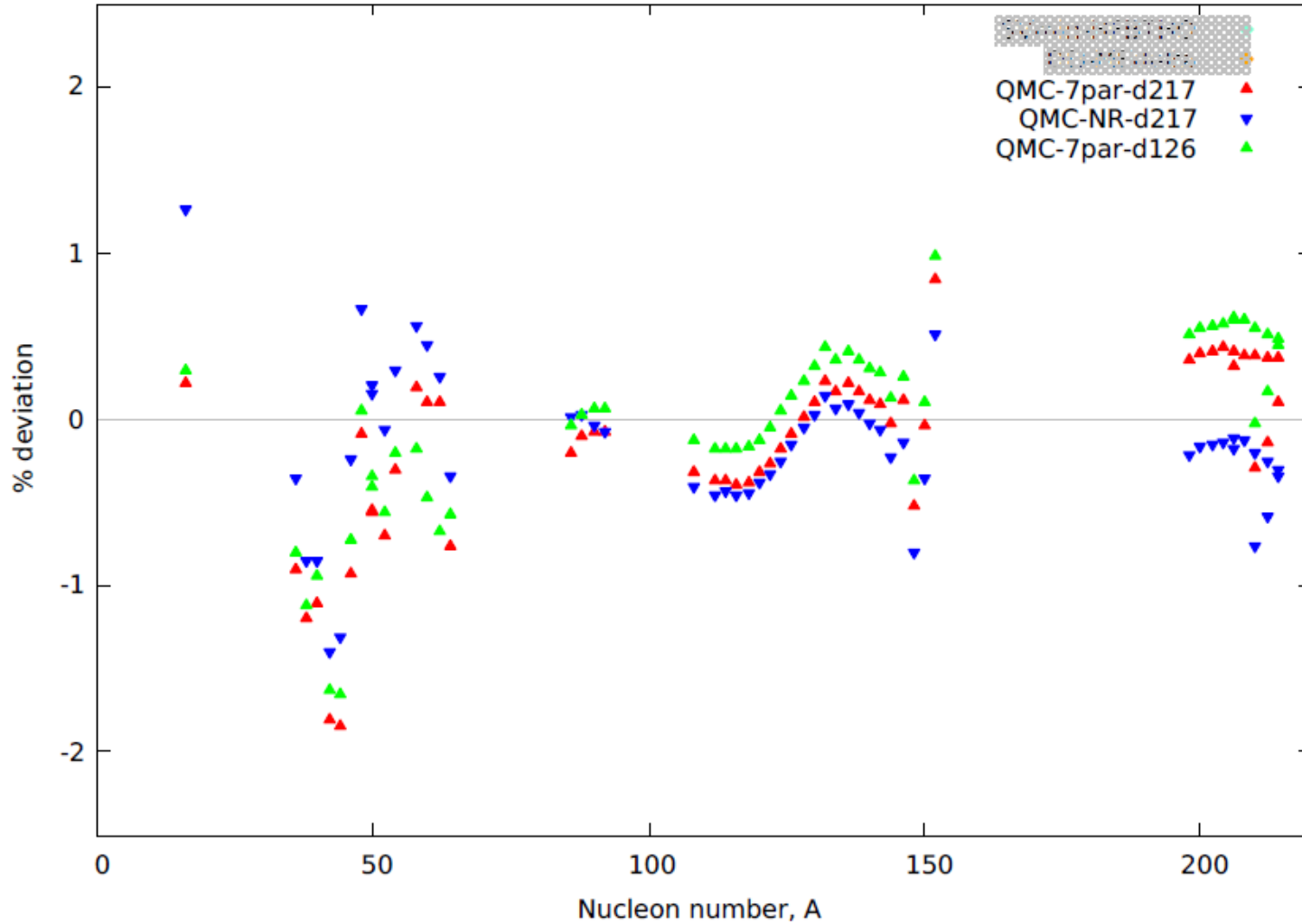


# Extended QMC – Martinez, Konieczka, Bąszyk et al. - implement QMC EFD in HFODD



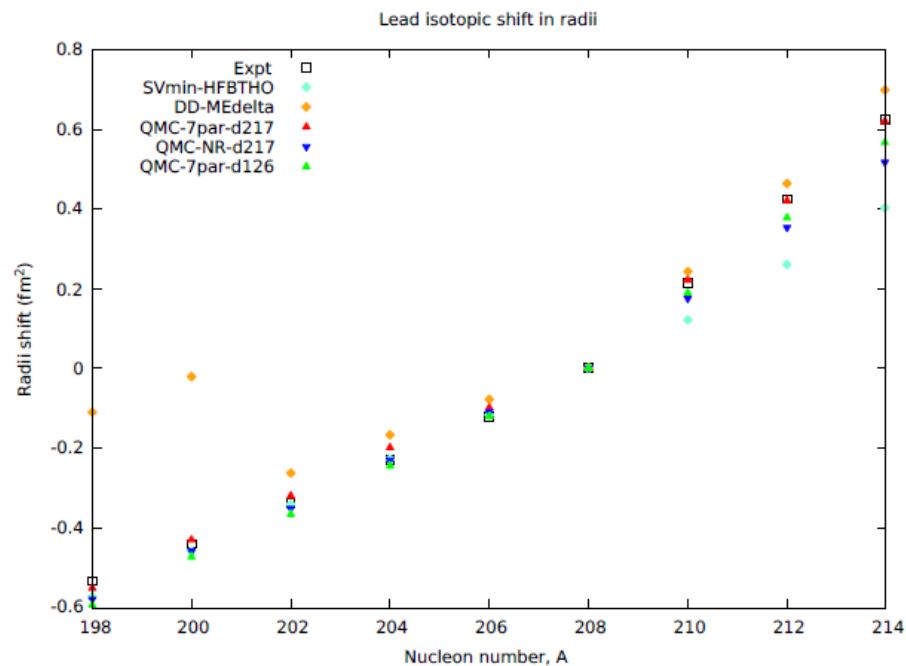
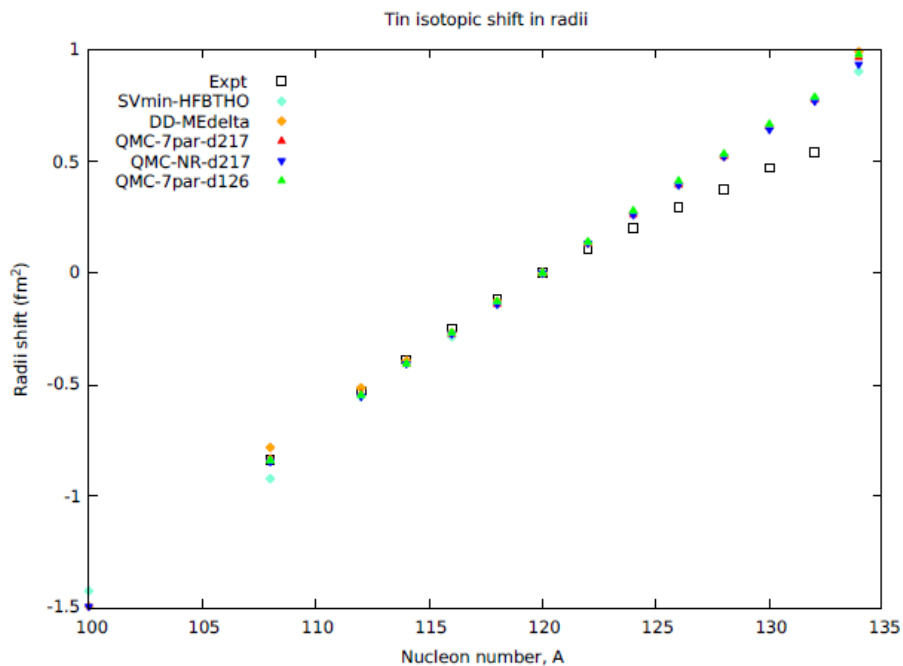
# Extended QMC – Martinez, Konieczka, Bąszyk *et al.*

RMS charge radii deviation from experiment



# Extended QMC – Martinez, Konieczka, Bąszyk *et al.*

- Not bad for Tin, excellent for Pb isotopes





# Summary: Finite Nuclei

- The effective force was *derived* at the quark level *based upon changing structure of bound nucleon*
- Has many less parameters but reproduces nuclear properties at a level comparable with the best phenomenological Skyrme forces
- Looks like standard nuclear force
- BUT underlying theory also predicts modified internal structure and hence modified
  - DIS structure functions
  - elastic form factors.....

# Nuclear DIS Structure Functions : The EMC Effect

To address questions like this one **MUST** start with a theory that quantitatively describes nuclear structure and allows calculation of structure functions  
– very, very few examples.....

# Theoretical Understanding

- Still numerous proposals but few consistent theories
- Initial studies used MIT bag<sup>1</sup> to estimate effect of self-consistent change of structure in-medium – but better to use a covariant theory
- For that Bentz and Thomas<sup>2</sup> re-derived change of nucleon structure in-medium in the NJL model
- This set the framework for sophisticated studies by Bentz, Cloët and collaborators over the last decade

<sup>1</sup> Thomas, Michels, Schreiber and Guichon, Phys. Lett. B233 (1989) 43

<sup>2</sup> Bentz and Thomas, Nucl. Phys. A696 (2001) 138

# EMC Effect for Finite Nuclei

(There is also a spin dependent EMC effect - as large as unpolarized)

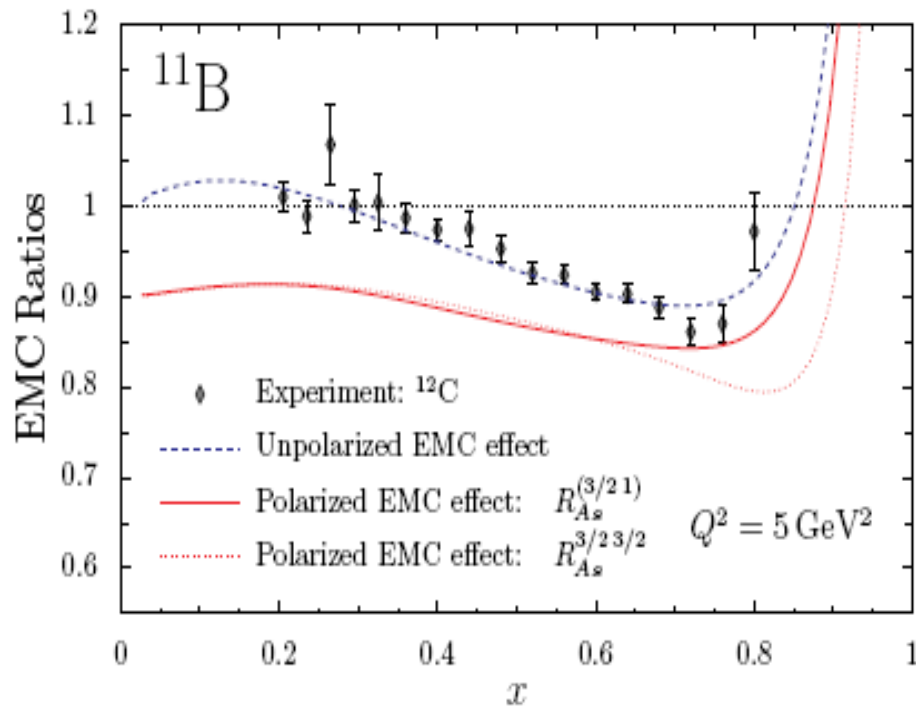


FIG. 7: The EMC and polarized EMC effect in  $^{11}\text{B}$ . The empirical data is from Ref. [31].

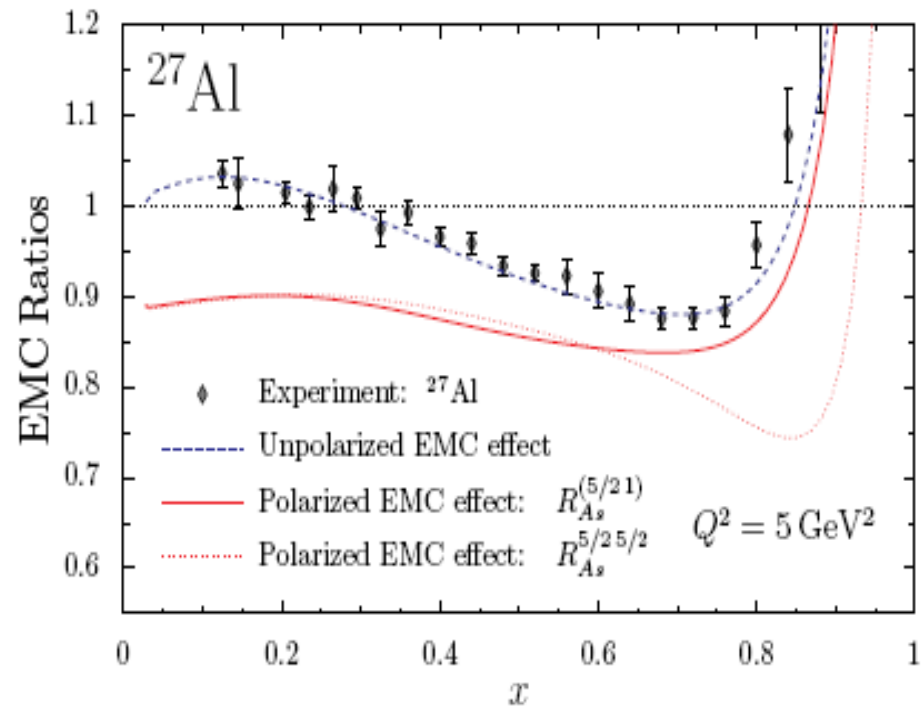
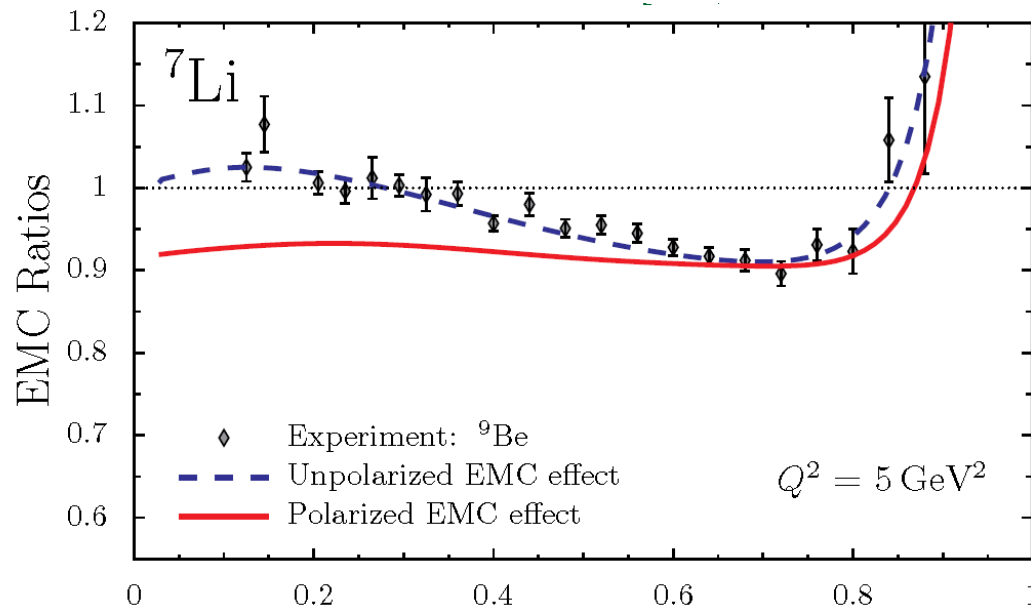


FIG. 9: The EMC and polarized EMC effect in  $^{27}\text{Al}$ . The empirical data is from Ref. [31].

Cloët, Bentz & Thomas, Phys. Lett. B642 (2006) 210  
(nucl-th/0605061)

# Approved JLab Experiment

- Effect in  ${}^7\text{Li}$  is slightly suppressed because it is a light nucleus and proton does not carry all the spin (simple WF:  $P_p = 13/15$  &  $P_n = 2/15$ )
- Experiment now approved at JLab [E12-14-001] to measure spin structure functions of  ${}^7\text{Li}$  (GFMC:  $P_p = 0.86$  &  $P_n = 0.04$ )
- *Everyone with their favourite explanation for the EMC effect should make a prediction for the polarized EMC effect in  ${}^7\text{Li}$*



Other tests (e.g. Isovector EMC effect)

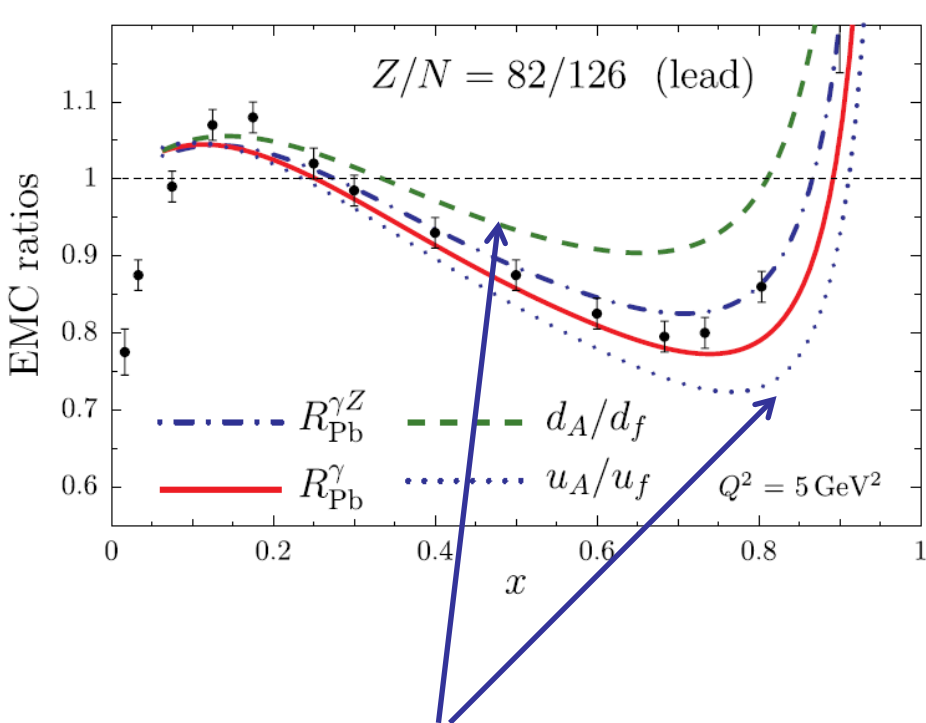
# Isovector EMC Effect

- New realization concerning EMC effect in this approach:
  - isovector force in nucleus (like Fe) with  $N \neq Z$  effects ALL u and d quarks in the nucleus
  - subtracting structure functions of extra neutrons is not enough
  - *there is a shift of momentum from all u to all d quarks*
- Sign and magnitude of this effect exhibits little model dependence

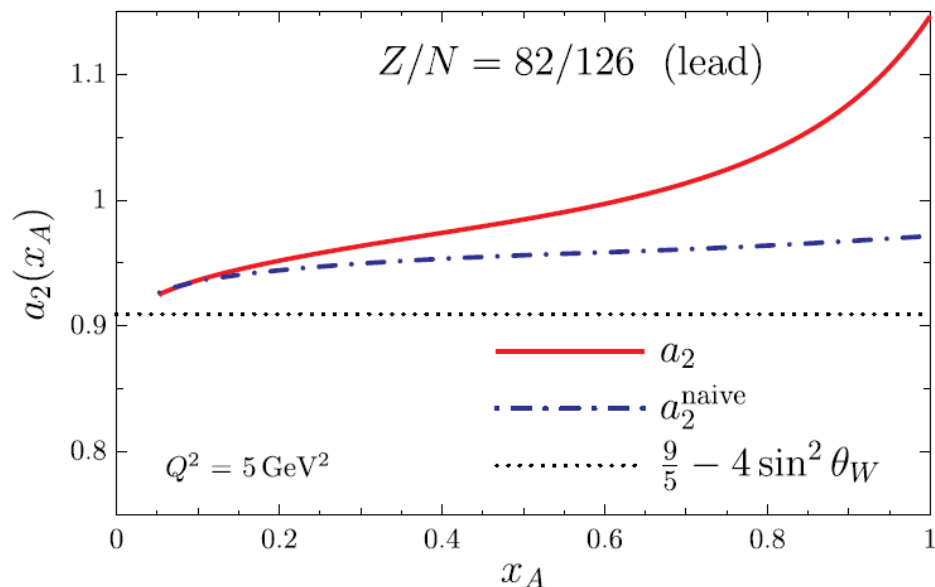
Cloet *et al.*, Phys.Rev.Lett.102:252301,2009  
Londergan et al., Phys Rev D67 (2003) 111901

# Parity-Violating Deep Inelastic Scattering and the Flavor Dependence of the EMC Effect

I. C. Cloët,<sup>1</sup> W. Bentz,<sup>2</sup> and A. W. Thomas<sup>1</sup>



$$A_{\text{PV}} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha_{\text{em}}} \left[ a_2(x_A) + \frac{1 - (1 - y)^2}{1 + (1 - y)^2} a_3(x_A) \right]$$



**Ideally tested at EIC with CC reactions**

**Parity violating EMC will test this at JLab 12 GeV**



# Comment on EMC explanation in terms of SRC

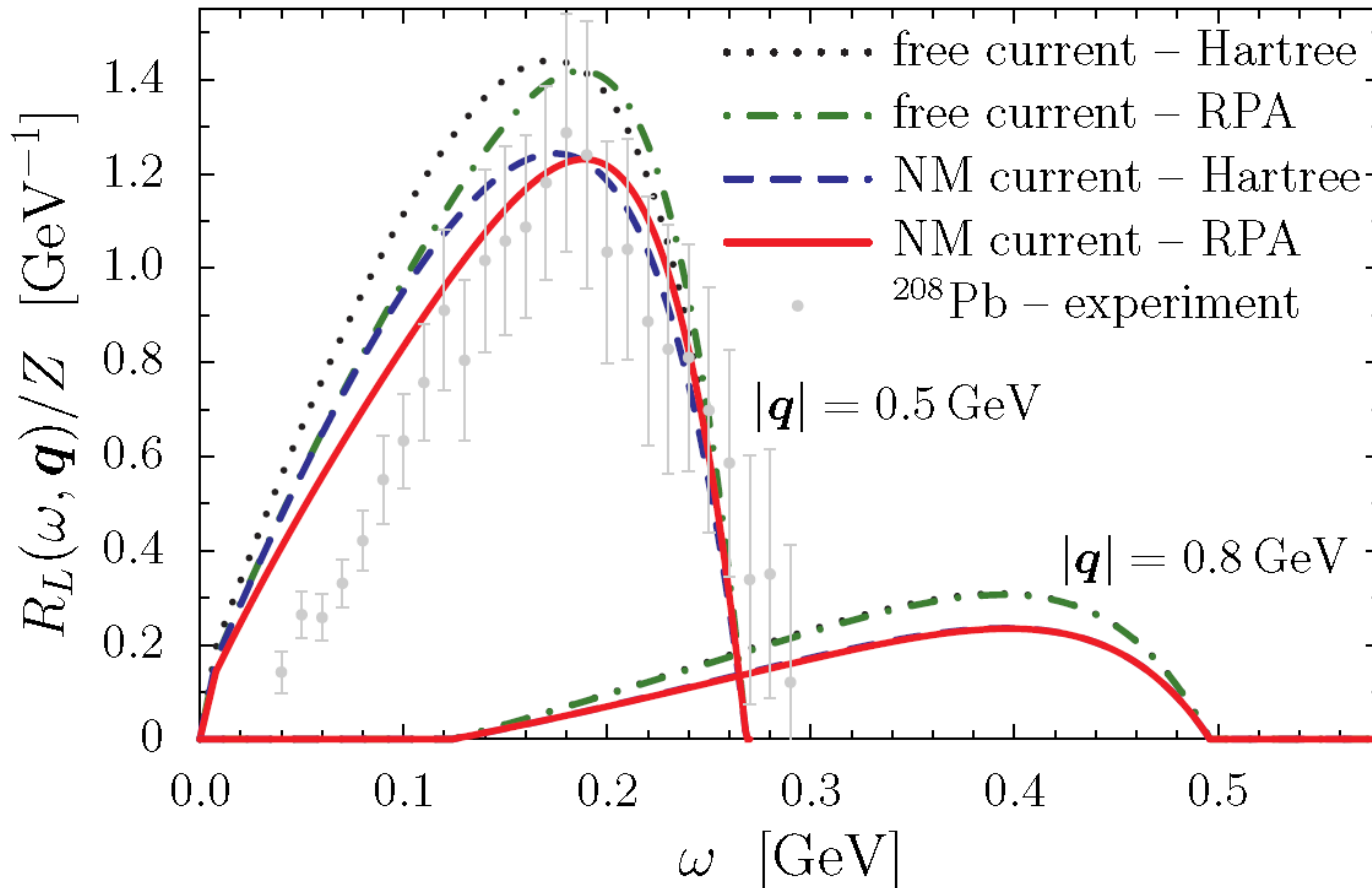
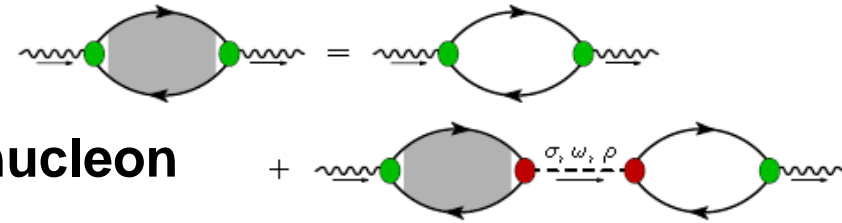
- It is crucial to have experimental signatures which might distinguish the mean field modification from an effect arising solely from SRC
- Isovector EMC effect: difference between effect on  $u$  and  $d$  quarks is much smaller in SRC approach
- Spin EMC effect is essentially absent in SRC approach

# Modified Electromagnetic Form Factors In-Medium

# Response Function

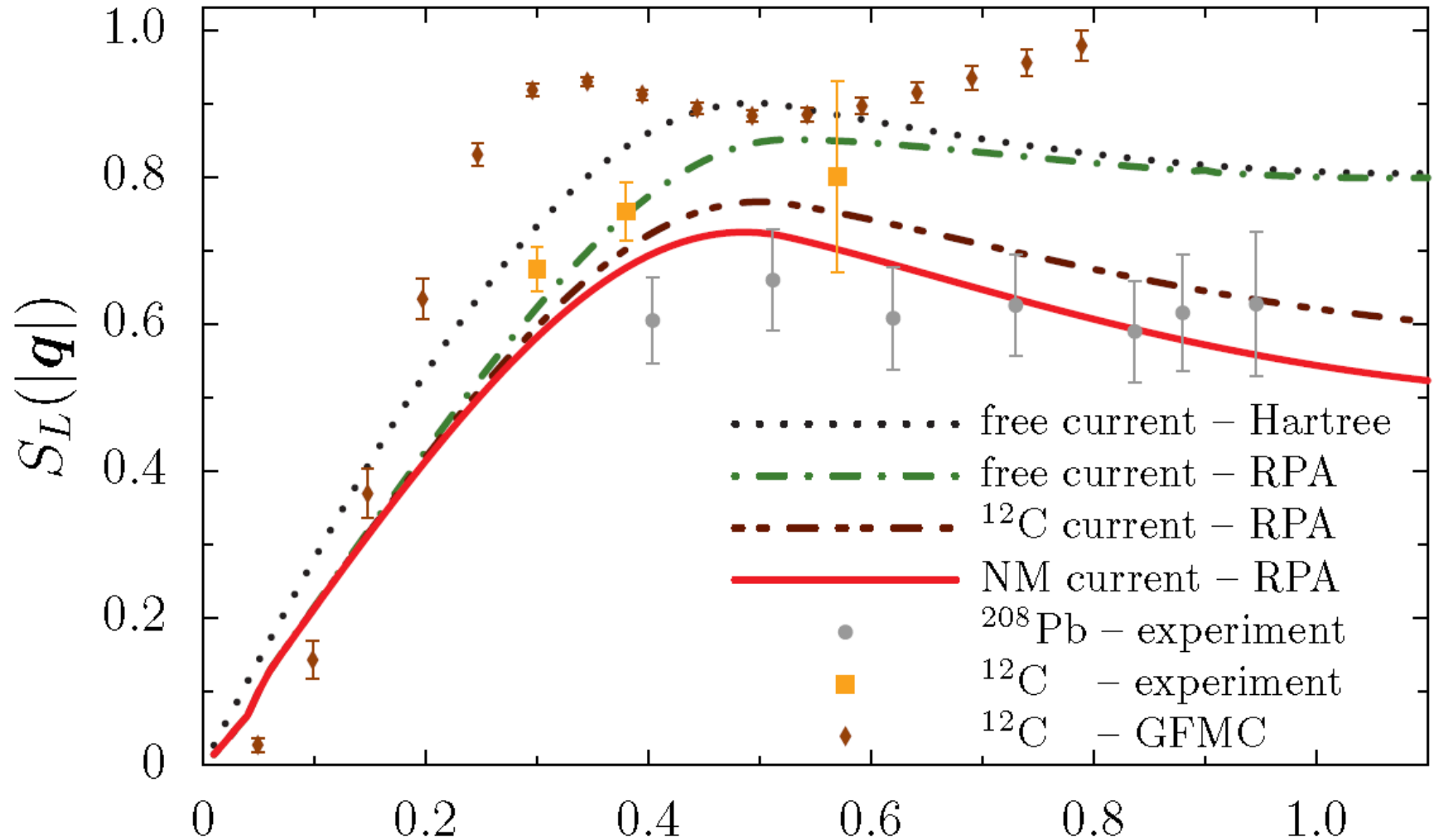
$$\frac{d^2\sigma}{d\Omega d\omega} = \sigma_{\text{Mott}} \left[ \frac{q^4}{|\mathbf{q}|^4} R_L(\omega, |\mathbf{q}|) + \left( \frac{q^2}{2|\mathbf{q}|^2} + \tan^2 \frac{\theta}{2} \right) R_T(\omega, |\mathbf{q}|) \right]$$

RPA correlations repulsive  
 Significant reduction in Response  
 Function from modification of bound-nucleon



Cloët, Bentz & Thomas ( PRL 116 (2016) 032701)

# Comparison with Unmodified Nucleon & Data

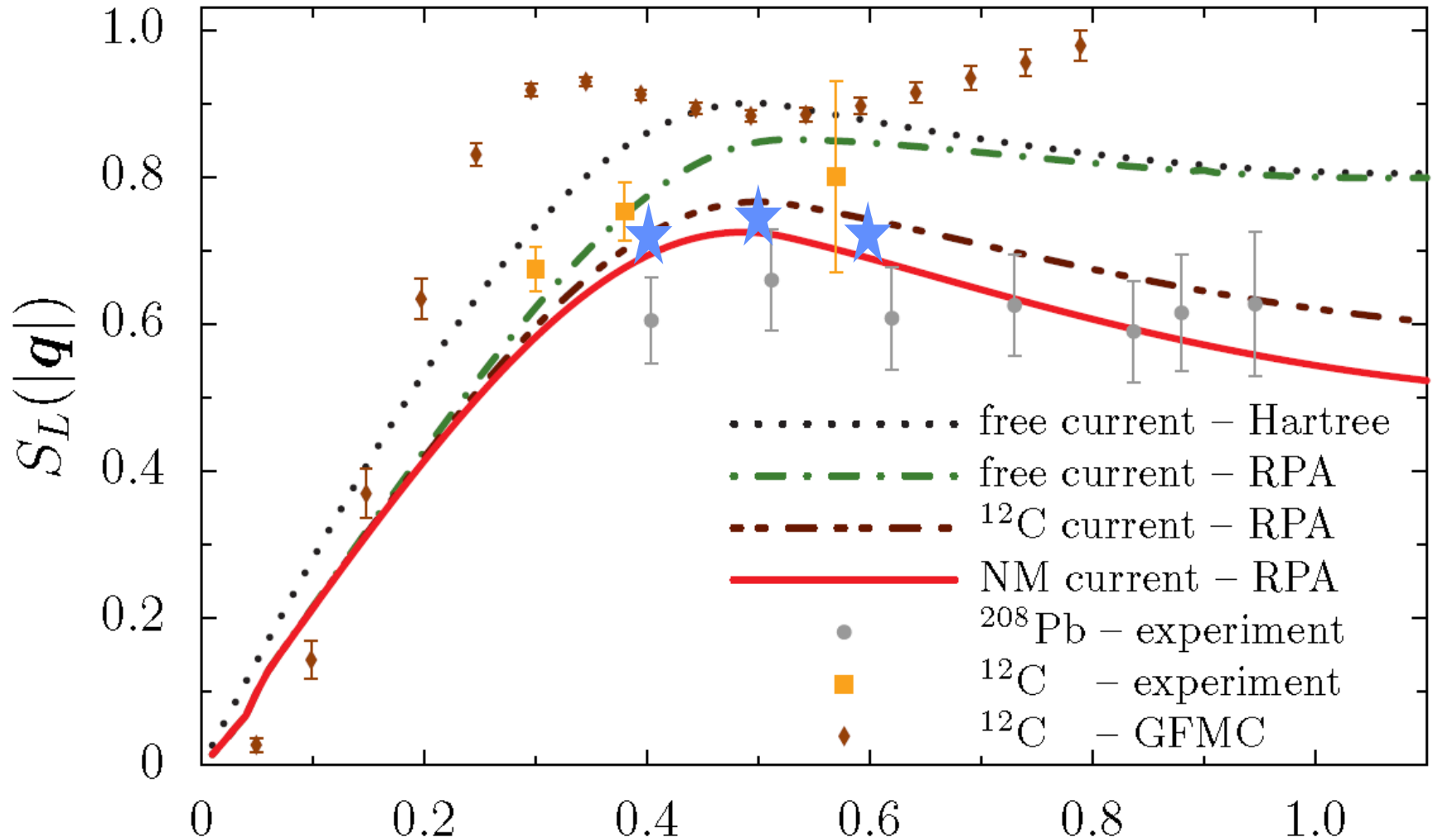


$$S_L(|\mathbf{q}|) = \int_{\omega_+}^{|\mathbf{q}|} d\omega \frac{R_L(\omega, |\mathbf{q}|)}{Z G_{Ep}^2(Q^2) + N G_{En}^2(Q^2)} |\mathbf{q}| \text{ [GeV]}$$

**Data: Morgenstern & Meziani**

**Calculations: Cloët, Bentz & Thomas (PRL 116 (2016) 032701)**

# and these predictions are stable!



$$S_L(|\mathbf{q}|) = \int_{\omega_+}^{|\mathbf{q}|} d\omega \frac{R_L(\omega, |\mathbf{q}|)}{Z G_{Ep}^2(Q^2) + N G_{En}^2(Q^2)} |\mathbf{q}| \text{ [GeV]}$$

★ Saito et al., QMC 1999  
(op cit)

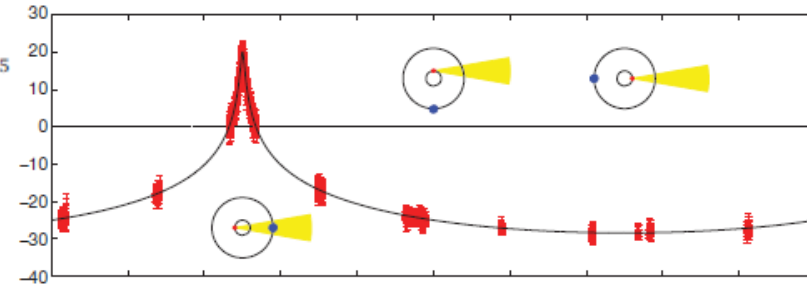
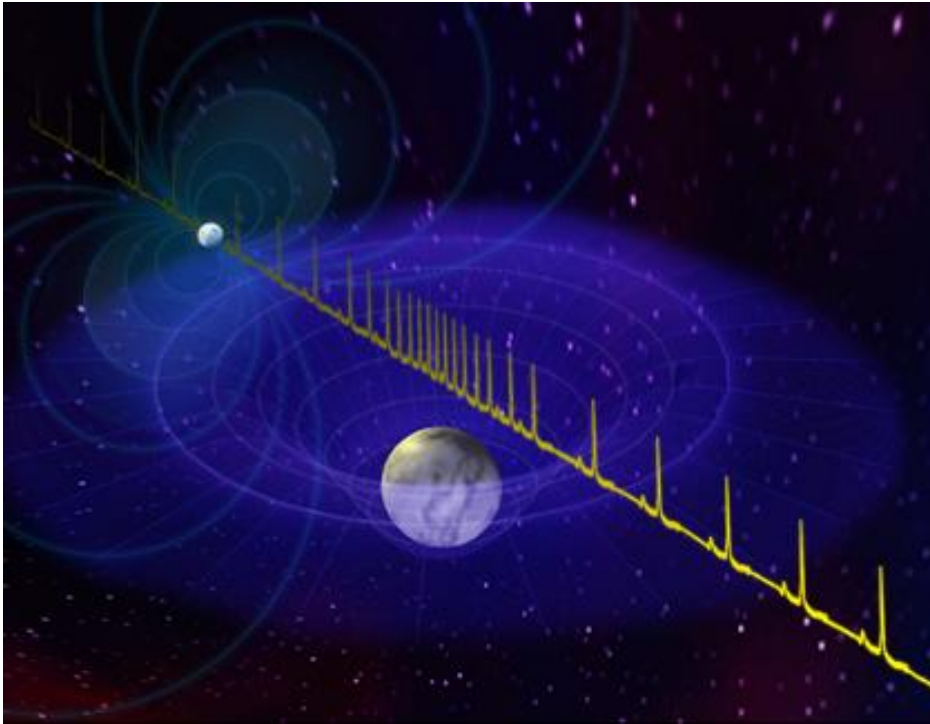
Data: Morgenstern & Meziani

Calculations: Cloët, Bentz & Thomas (PRL 116 arXiv:1506.05875)

# Neutron Stars

# A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest<sup>1</sup>, T. Pennucci<sup>2</sup>, S. M. Ransom<sup>1</sup>, M. S. E. Roberts<sup>3</sup> & J. W. T. Hessels<sup>4,5</sup>



Reports a very accurate pulsar mass much larger than seen before :  $1.97 \pm 0.04$  solar mass

Claim: it rules out hyperon occurrence

- ignored our *published* work three years before!

# Hyperons

- Derive  $\Lambda N, \Sigma N, \Lambda \Lambda \dots$  effective forces in-medium with **no** additional free parameters
- Attractive and repulsive forces ( $\sigma$  and  $\omega$  mean fields) both decrease as # light quarks decreases
- Predict: NO  $\Sigma$  hypernuclei are bound! **Agrees expt**
- $\Lambda$  bound by  $\sim 30$  MeV in nuclear matter ( $\sim \text{Pb}$ ): **Agrees expt**
- Nothing (was) known about  $\Xi$  hypernuclei  
– JPARC **Progress**



# $\Lambda$ - and $\Xi$ -Hypernuclei in QMC

	$^{89}_{\Lambda}\text{Yb}$ (Expt.)	$^{91}_{\Lambda}\text{Zr}$	$^{91}_{\Xi^0}\text{Zr}$	$^{208}_{\Lambda}\text{Pb}$ (Expt.)	$^{209}_{\Lambda}\text{Pb}$	$^{209}_{\Xi^0}\text{Pb}$
$1s_{1/2}$	-22.5	-24.0	-9.9	-27.0	-26.9	-15.0
$1p_{3/2}$		-19.4	-7.0		-24.0	-12.6
$1p_{1/2}$	-16.0 (1p)	-19.4	-7.2	-22.0 (1p)	-24.0	-12.7
$1d_{5/2}$		-13.4	-3.1	—	-20.1	-9.6
$2s_{1/2}$		-9.1	—	—	-17.1	-8.2
$1d_{3/2}$	-9.0 (1d)	-13.4	-3.4	-17.0 (1d)	-20.1	-9.8
$1f_{7/2}$		-6.5	—	—	-15.4	-6.2
$2p_{3/2}$		-1.7	—	—	-11.4	-4.2
$1f_{5/2}$	-2.0 (1f)	-6.4	—	-12.0 (1f)	-15.4	-6.5
$2p_{1/2}$		-1.6	—	—	-11.4	-4.3

Predicts  $\Xi$  – hypernuclei bound by 10-15 MeV – to be tested at J-PARC

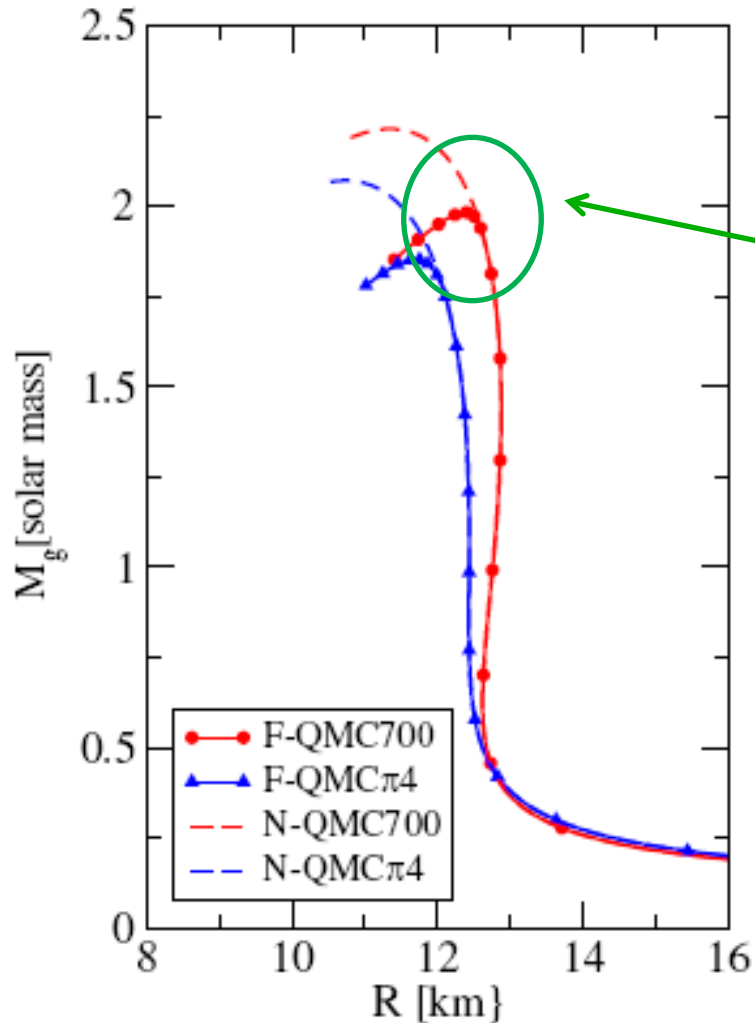
“The first evidence of a bound state of  $\Xi^{-14}\text{N}$  system”,

K. Nakazawa et al.,

Prog. Theor. Exp. Phys. (2015)

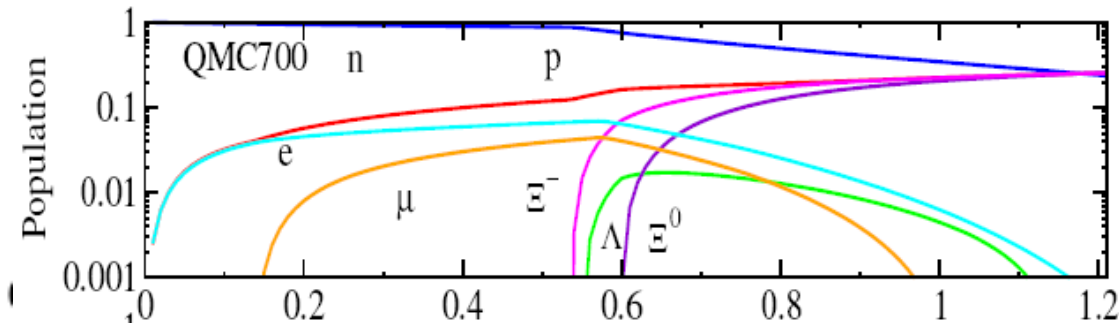
Guichon *et al.*, Nucl.Phys. A814 (2008) 66; see also 1998

# Consequences of QMC for Neutron Star



Rikovska-Stone *et al.*, NP A792 (2007) 341

2 Solar mass stars predicted with hyperons present:



Predicted HNN forces crucial!

Later work: Saito *et al.*, Whittenbury *et al.*.....

**Just for fun....**

# Light Dark Matter

Recently there was a very interesting proposal from Fornal and Grinstein (1801.01124).

Originated in long-standing puzzle concerning free neutron lifetime:

- Measurement for trapped n's:  $879.6 \pm 0.6$  sec
- Measurement in beam decay :  $888.0 \pm 2.0$  sec

This  $3.5\sigma$  discrepancy solved by existence of new decay mode, which would not be seen in the beam decay experiment

$n \longrightarrow \text{Dark Matter } (\chi) + \text{something}$

“Something” not a photon : Tang *et al.*, Los Alamos 1802.01595

# Also stimulating in view of a recent Nature article

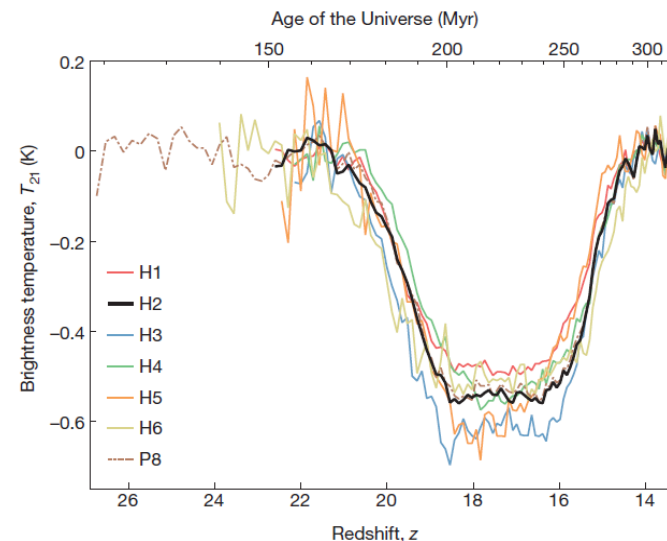
- Bowman *et al.* (Nature 555, 67-70 March 1<sup>st</sup> 2018) look at effect of star formation in the early Universe

Astronomers detect signal from the dawn of the universe, using simple antenna in WA outback



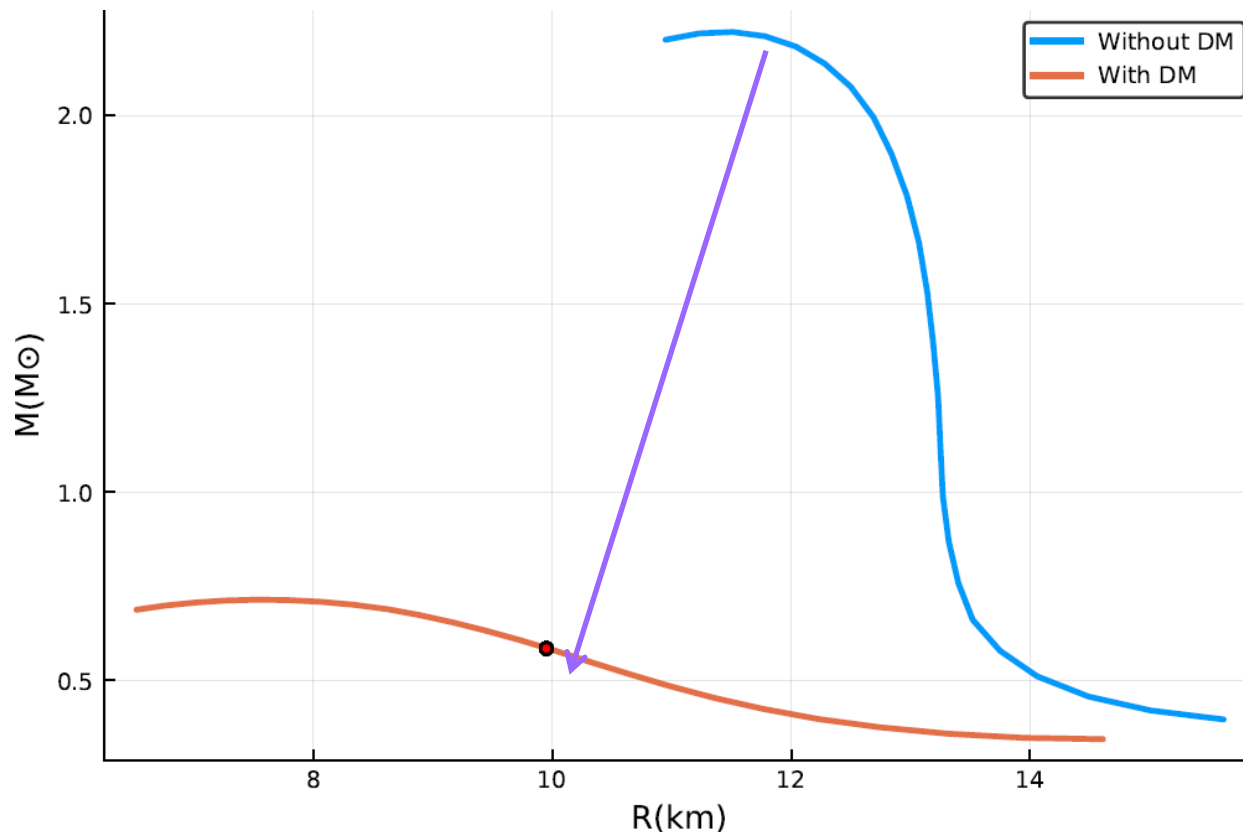
- Dark matter can explain the absorption at the hydrogen 21cm line IF it has

mass  $<$  few GeV  
and  $\sigma > 10^{-21}$  cm<sup>2</sup>



# Solve Tolman-Oppenheimer-Volkoff Equations

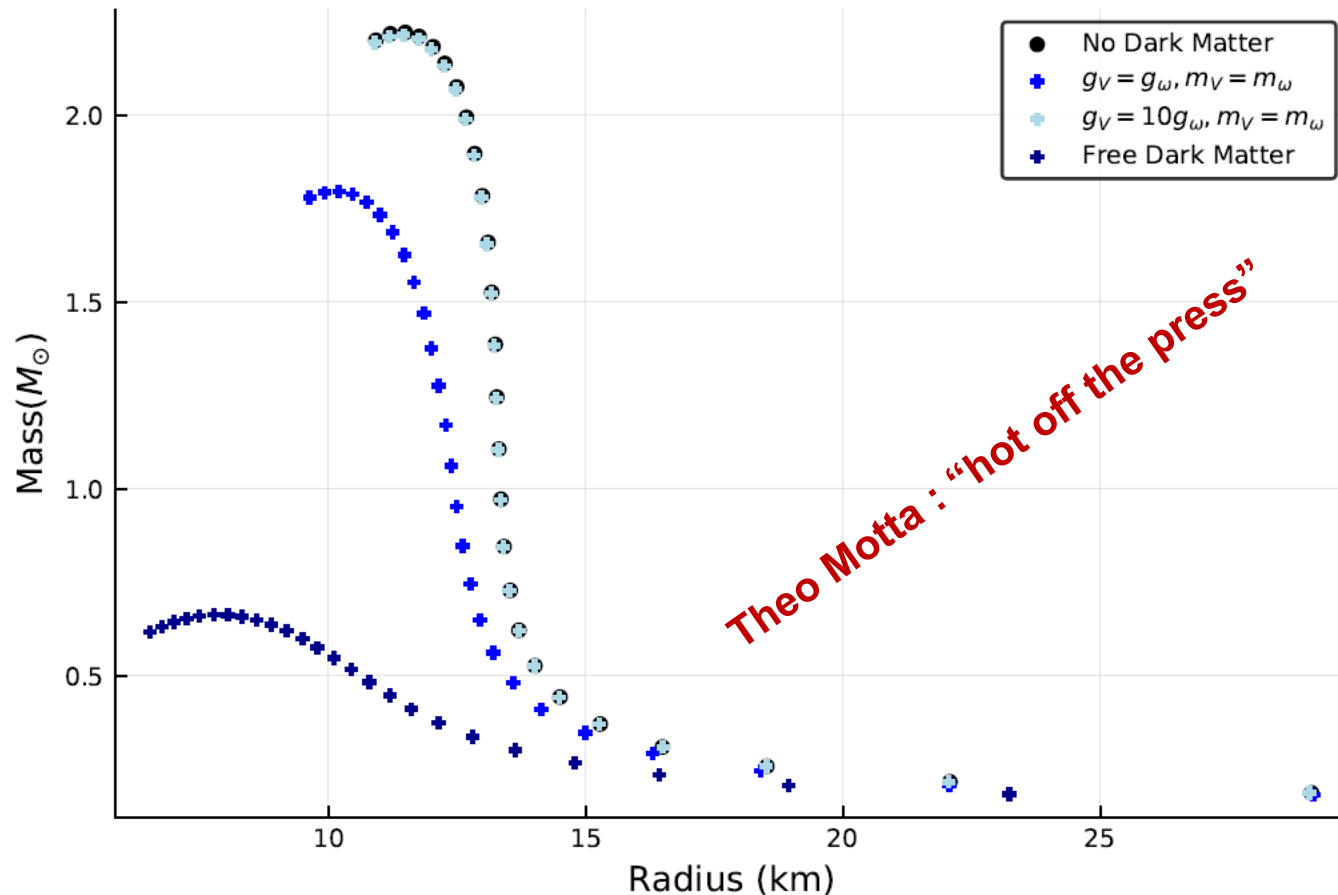
- Maximum allowed mass for stable neutron star drops from  $2.21 M_{\odot}$  to  $0.7 M_{\odot}$
- But cannot even get that as maximum stable star goes to just  $0.58 M_{\odot}$



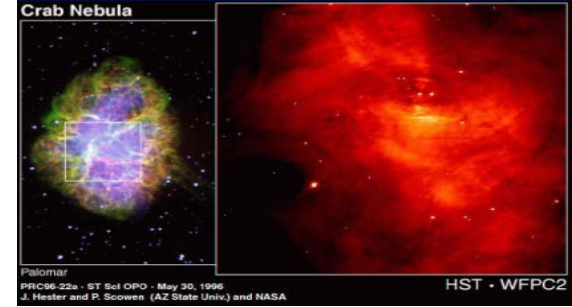
Motta et al., J.Phys. G45 (2018) no.5, 05LT01

# Is there a way out?

- If the dark matter has a strong repulsive interaction with other dark matter we can lift the pressure and hence the maximum neutron star mass



# I. Summary



- Intermediate range NN attraction is **STRONG Lorentz scalar**
- This modifies the intrinsic structure of the bound nucleon
  - profound change in shell model :  
what occupies shell model states are **NOT** free nucleons
- Scalar polarizability is a natural source of three-body forces (NNN, HNN, HHN...)
  - clear physical interpretation
- Naturally generates effective HN and HNN forces with no new parameters and predicts heavy neutron stars



# II. Summary

- Initial systematic study of finite nuclei very promising
  - Binding energies typically within 0.3% across periodic table
  - Super-heavies ( $Z > 100$ ) especially good
- Need empirical confirmation:
  - Response Functions & Coulomb sum rule (soon?)
  - Isovector EMC effect; spin EMC (not too long?)
- Yields neutron stars at  $2M_{\odot}$  *with hyperons*
- Unfortunately existence of neutron stars means that the nice idea to resolve  $\tau_n$  anomaly in terms of decay to dark matter is incorrect

# Special Mentions.....



**Guichon**



**Tsushima**



**Saito**



**Stone**



**Krein**



**Bentz**



**Matevosyan**



**Cloët**



**Whittenbury**



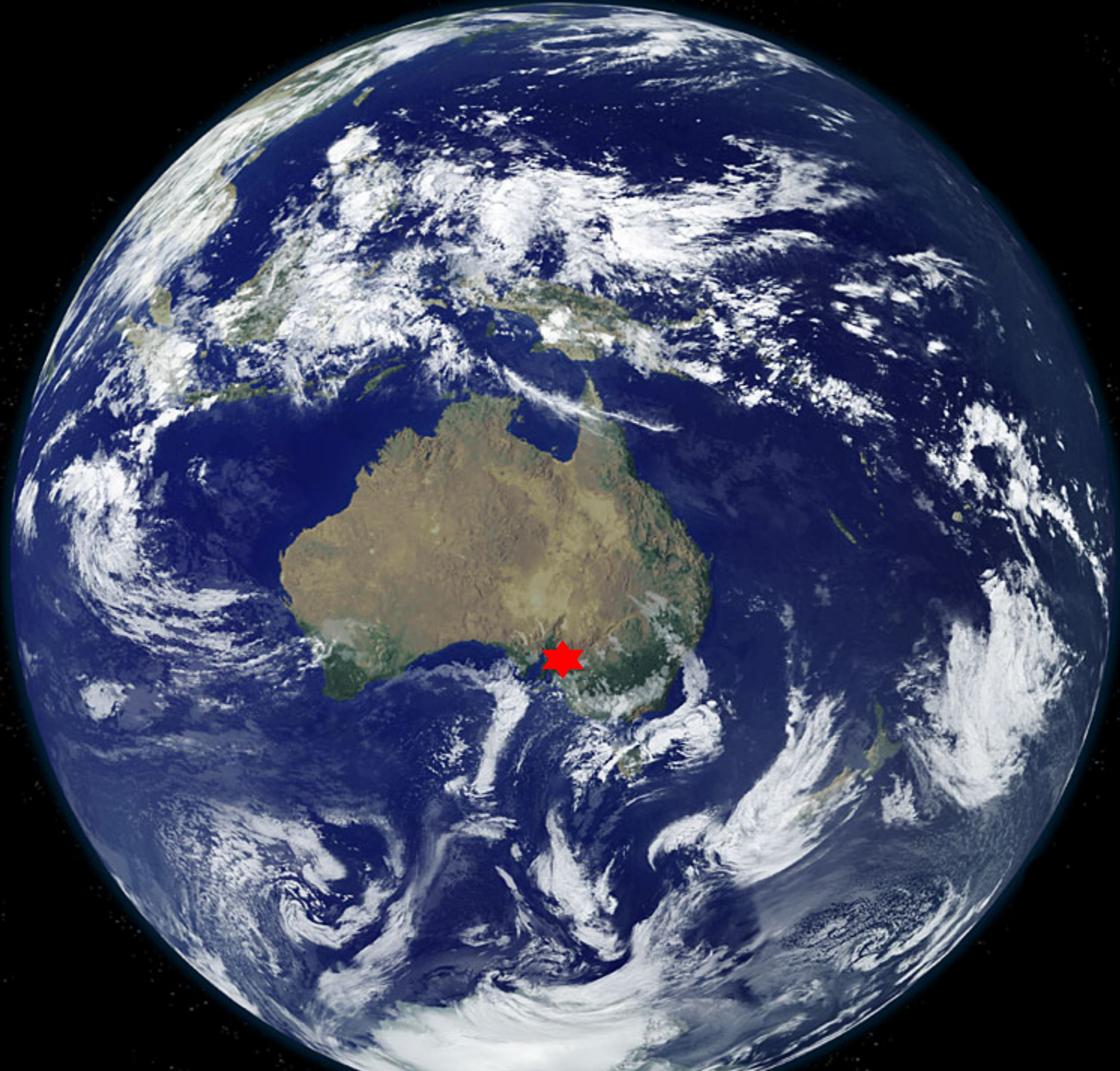
**Simenel**

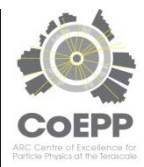


**Martinez**



**Motta**







# Effect of scalar field on quark spinor

- MIT bag model: quark spinor modified in bound nucleon

$$\psi = \frac{\mathcal{N}}{4\pi} \begin{pmatrix} j_0(xu'/R_B) \\ i\beta_q \vec{\sigma} \cdot \hat{u}' j_1(xu'/R_B) \end{pmatrix} \chi_m$$

- Lower component enhanced by attractive scalar field

$$\beta_q = \sqrt{\frac{\Omega_0 - m_q^* R_B}{\Omega_0 + m_q^* R_B}}$$

- This leads to a *very small* ( $\sim 1\%$  at  $\rho_0$ ) *increase in bag radius*
- It also *suppresses the scalar coupling to the nucleon as the scalar field increases*

$$\frac{\Omega_0/2 + m_q^* R_B (\Omega_0 - 1)}{\Omega_0 (\Omega_0 - 1) + m_q^* R_B / 2} = \int \bar{\psi} \psi \, dV$$

- This is the “**scalar polarizability**”: a new saturation mechanism for nuclear matter

# Key papers on QMC

- **Two major, recent papers:**
  1. Guichon, Matevosyan, Sandulescu, Thomas, Nucl. Phys. A772 (2006) 1.
  2. Guichon and Thomas, Phys. Rev. Lett. 93 (2004) 132502
- **Built on earlier work on QMC: e.g.**
  3. Guichon, Phys. Lett. B200 (1988) 235
  4. Guichon, Saito, Rodionov, Thomas, Nucl. Phys. A601 (1996) 349
- **Major review of applications of QMC to many nuclear systems:**
  5. Saito, Tsushima, Thomas, Prog. Part. Nucl. Phys. 58 (2007) 1-167 (hep-ph/0506314)

# References to: Covariant Version of QMC

- **Basic Model: (Covariant, chiral, confining version of NJL)**
- **Bentz & Thomas, Nucl. Phys. A696 (2001) 138**
- **Bentz, Horikawa, Ishii, Thomas, Nucl. Phys. A720 (2003) 95**
- **Applications to DIS:**
- **Cloet, Bentz, Thomas, Phys. Rev. Lett. 95 (2005) 052302**
- **Cloet, Bentz, Thomas, Phys. Lett. B642 (2006) 210**
- **Applications to neutron stars – including SQM:**
- **Lawley, Bentz, Thomas, Phys. Lett. B632 (2006) 495**
- **Lawley, Bentz, Thomas, J. Phys. G32 (2006) 667**

# Can we Measure Scalar Polarizability in Lattice QCD ?

- IF we can, then in a real sense we would be linking nuclear structure to QCD itself, because scalar polarizability is sufficient in simplest, relativistic mean field theory to produce saturation
- Initial ideas on this published :  
the trick is to apply a chiral invariant scalar field  
– do indeed find polarizability opposing applied  $\sigma$  field

**18<sup>th</sup> Nishinomiya Symposium: nucl-th/0411014**

**– published in Prog. Theor. Phys.**