

Global Recoil in Initial-Final Antennae

Rob Verheyen

In collaboration with Peter Skands & Ronald Kleiss

Work in progress



Radboud University



Introduction

Giele, Kosower, Skands:1102.2126

Gehrmann, Ritzmann, Skands:1108.6172

Parton shower: Vincia, plugin for Pythia based on antenna factorization

Backward evolution for initial state radiation
→ Recoil imparted on the entire final state

Most dipole-like showers: Global recoil in II and IF

- Sherpa [Höche, Schumann, Siebert: 0912.3501](#)
- Herwig [Platzer, Gieseke: 0909.5593](#)
- Dire [Höche, Prestel: 1506.05057](#)

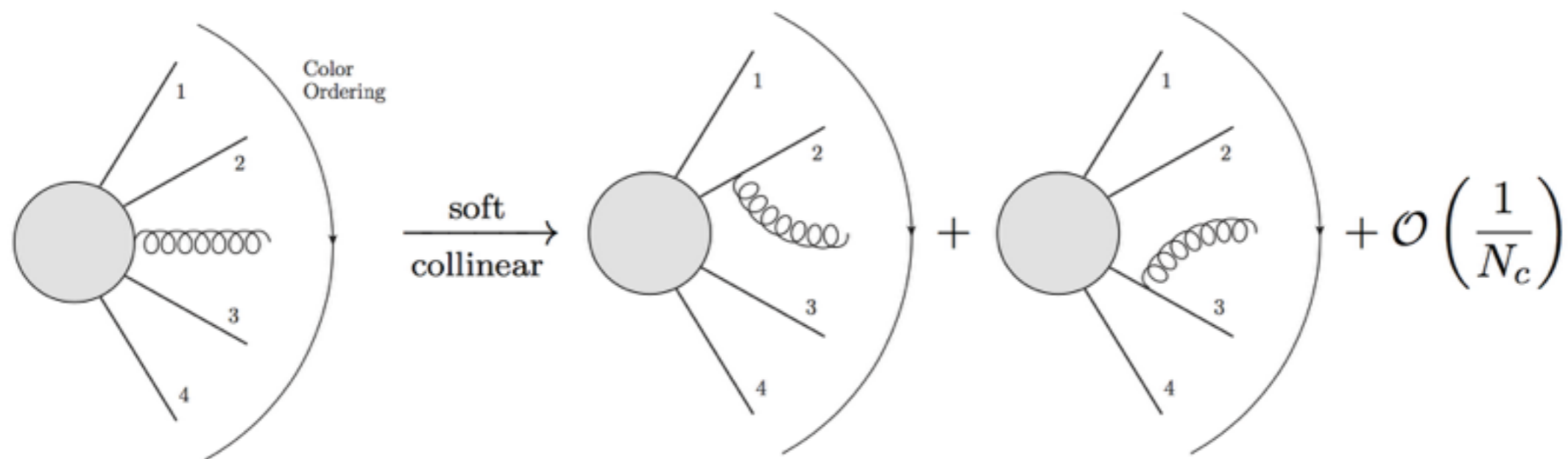
Vincia: only global recoil for II connections

Antenna Factorization

$$|M(\dots, p_a, k, \dots)|^2 \xrightarrow{p_a \parallel k} g^2 C \frac{P(z)}{p_a \cdot k} |M(\dots, p_a + k, \dots)|^2$$

$$|M(\dots, p_a, k, p_b, \dots)|^2 \xrightarrow{k \rightarrow 0} g^2 C \left[\frac{2p_a \cdot p_b}{(p_a \cdot k)(k \cdot p_b)} - \frac{m_a^2}{(p_a \cdot k)^2} - \frac{m_b^2}{(p_b \cdot k)^2} \right] |M(\dots, p_a, p_b, \dots)|^2$$

$$|M(\dots, p_a, k, p_b, \dots)|^2 \approx g^2 C a_e^{QCD}(p_a, k, p_b) |M(\dots, p'_a, p'_b, \dots)|^2$$



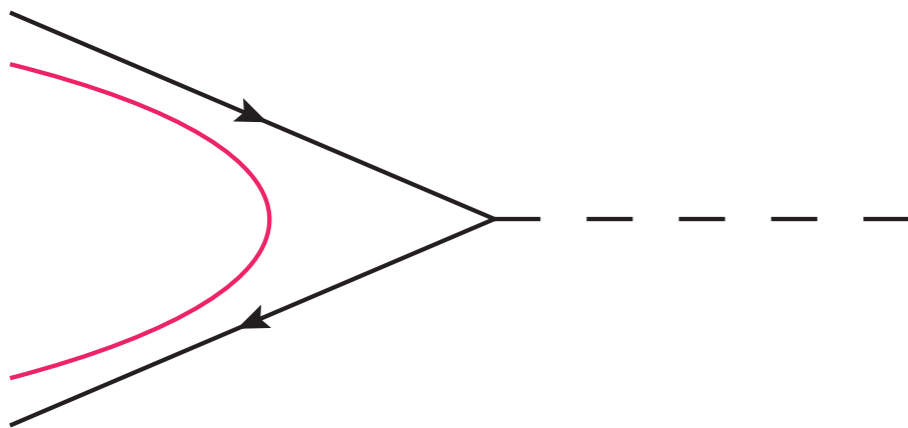
Phase Space Factorization

Exact factorization of phase space

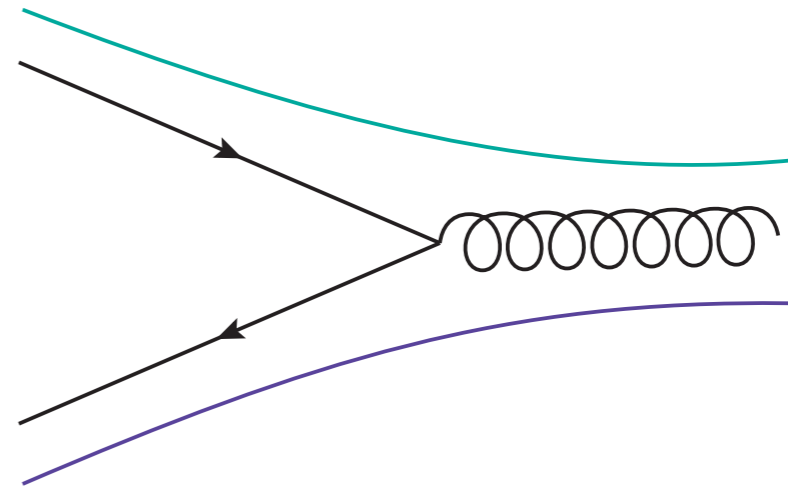
$$\frac{dx_a}{x_a} \frac{dx_b}{x_b} d\Phi_n = \frac{dx_A}{x_A} \frac{dx_B}{x_B} d\Phi_{n-1} d\Phi_{\text{ant}}$$

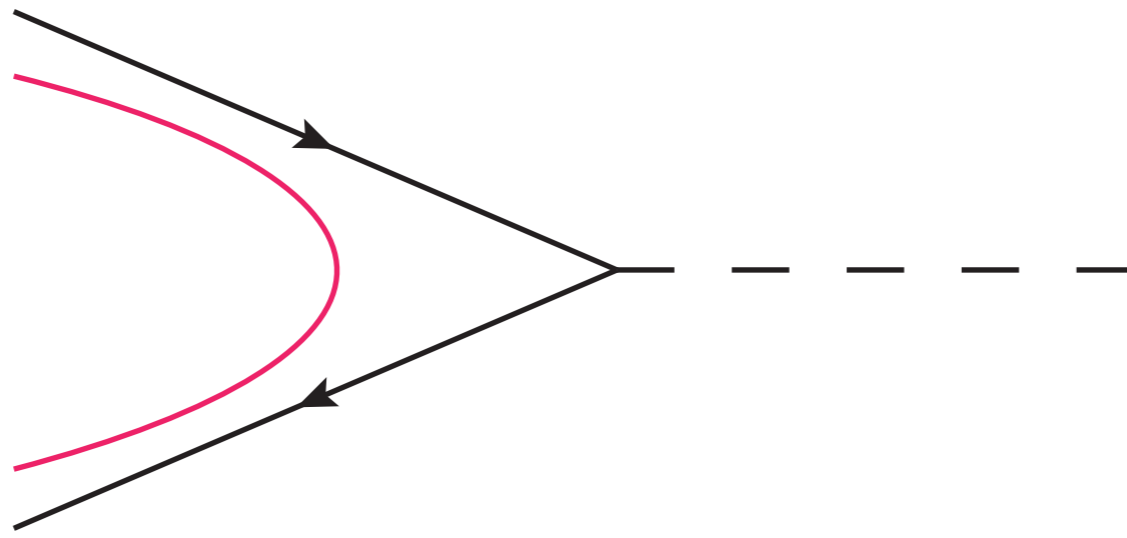
On-shell momenta with exact momentum conservation

Initial-initial



Initial-final





Initial-Initial

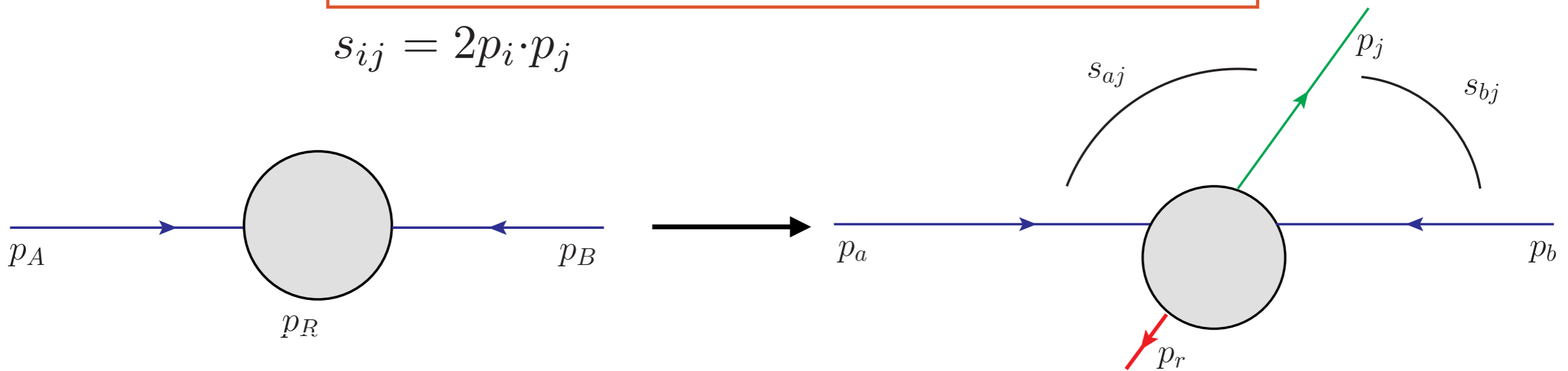
Phase Space Factorization - II

$$\frac{dx_a}{x_a} \frac{dx_b}{x_b} d\Phi_2(p_a + p_b \rightarrow p_j + p_r)$$

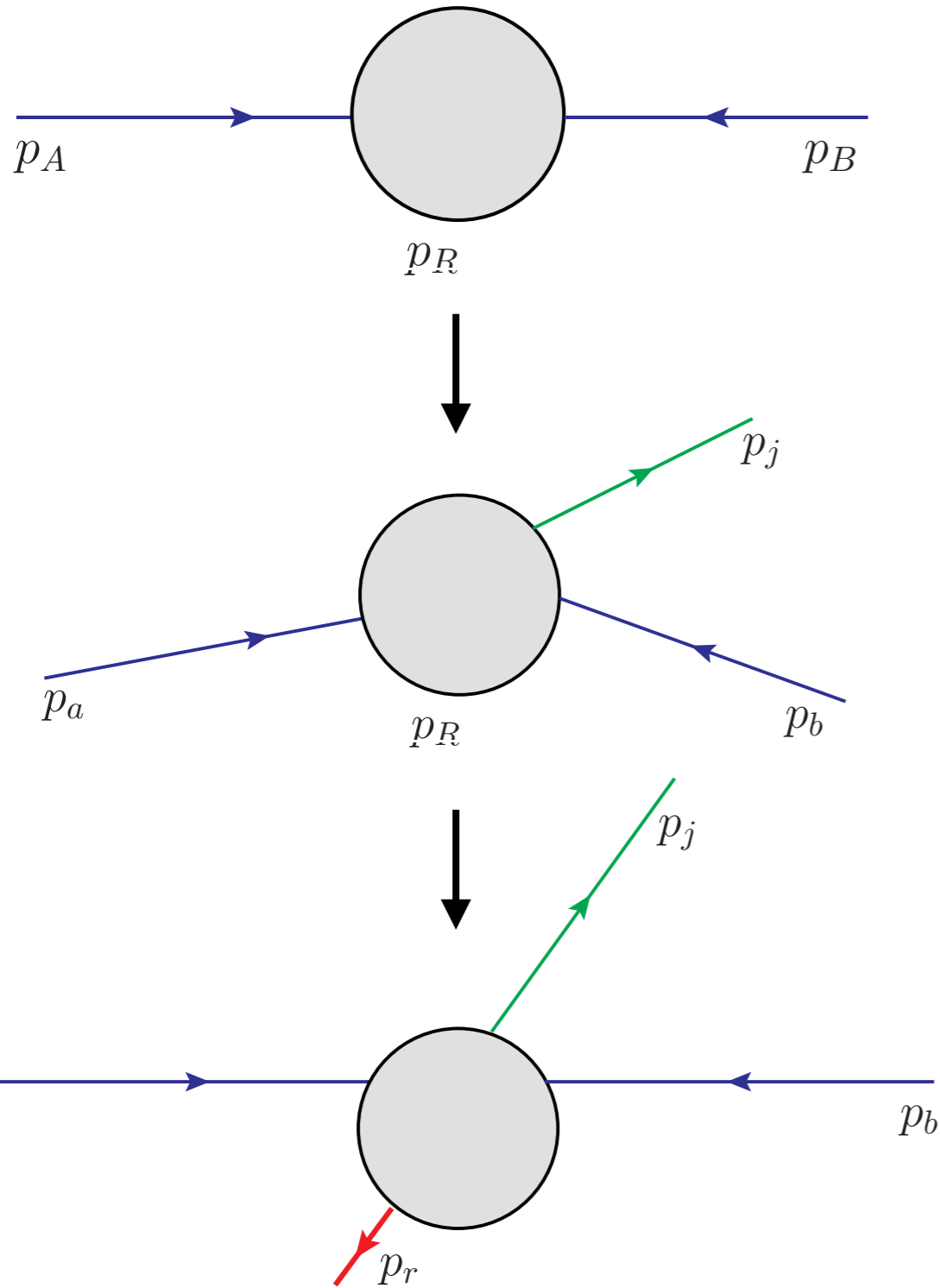
$$= \frac{dx_A}{x_A} \frac{dx_B}{x_B} d\Phi_1(p_A + p_B \rightarrow p_R) d\Phi_{\text{ant}}$$

$$d\Phi_{\text{ant}} = \frac{1}{16\pi^2} \frac{1}{s_{AB}} \left(\frac{x_A}{x_a} \frac{x_B}{x_b} \right)^2 ds_{aj} ds_{bj} \frac{d\varphi}{2\pi}$$

$$s_{ij} = 2p_i \cdot p_j$$



Phase Space Factorization - II

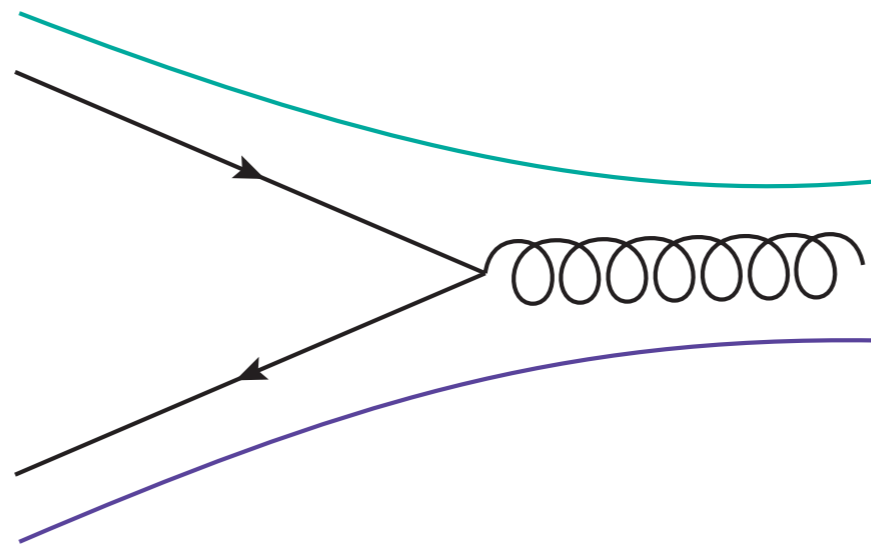


$$p_a = c_1 p_A$$

$$p_b = c_2 p_B$$

$$p_j = c_3 p_A + c_4 p_B + c_5 p_{\perp}(\varphi)$$

$$p_r = p_a + p_b - p_j$$



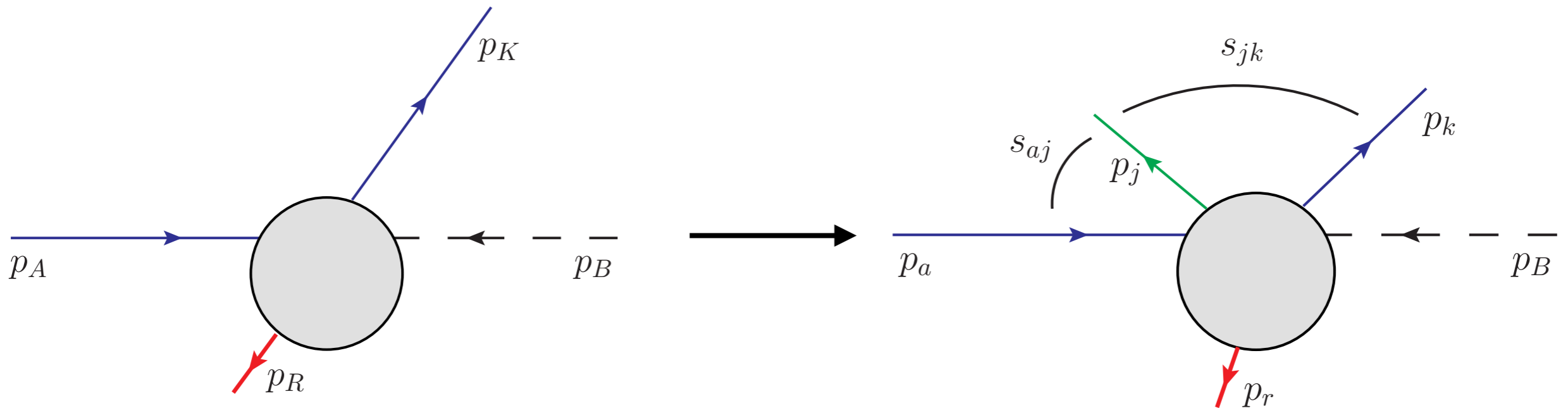
Initial-Final

Phase Space Factorization - IF

$$\frac{dx_a}{x_a} \frac{dx_B}{x_B} d\Phi_3(p_a + p_B \rightarrow p_j + p_k + p_r)$$

$$= \frac{dx_A}{x_A} \frac{dx_B}{x_B} d\Phi_2(p_A + p_B \rightarrow p_K + p_R) d\Phi_{\text{ant}}$$

$$d\Phi_{\text{ant}} = \frac{1}{16\pi^2} \frac{1}{s_{AK}} \frac{x_A^2}{x_a^2} ds_{aj} ds_{jk} \frac{d\varphi}{2\pi}$$



Initial - Final Mapping

Map 1: p_A retains its direction

$$p_a = \frac{s_{AK} + s_{jk}}{s_{jk}} p_A$$

$$p_j = \frac{s_{jk}s_{ak}}{s_{AK}(s_{AK} + s_{jk})} p_A + \frac{s_{aj}}{s_{AK} + s_{jk}} p_K + \frac{\sqrt{s_{jk}s_{aj}s_{ak}}}{s_{AK} + s_{jk}} p_{\perp}(\varphi)$$

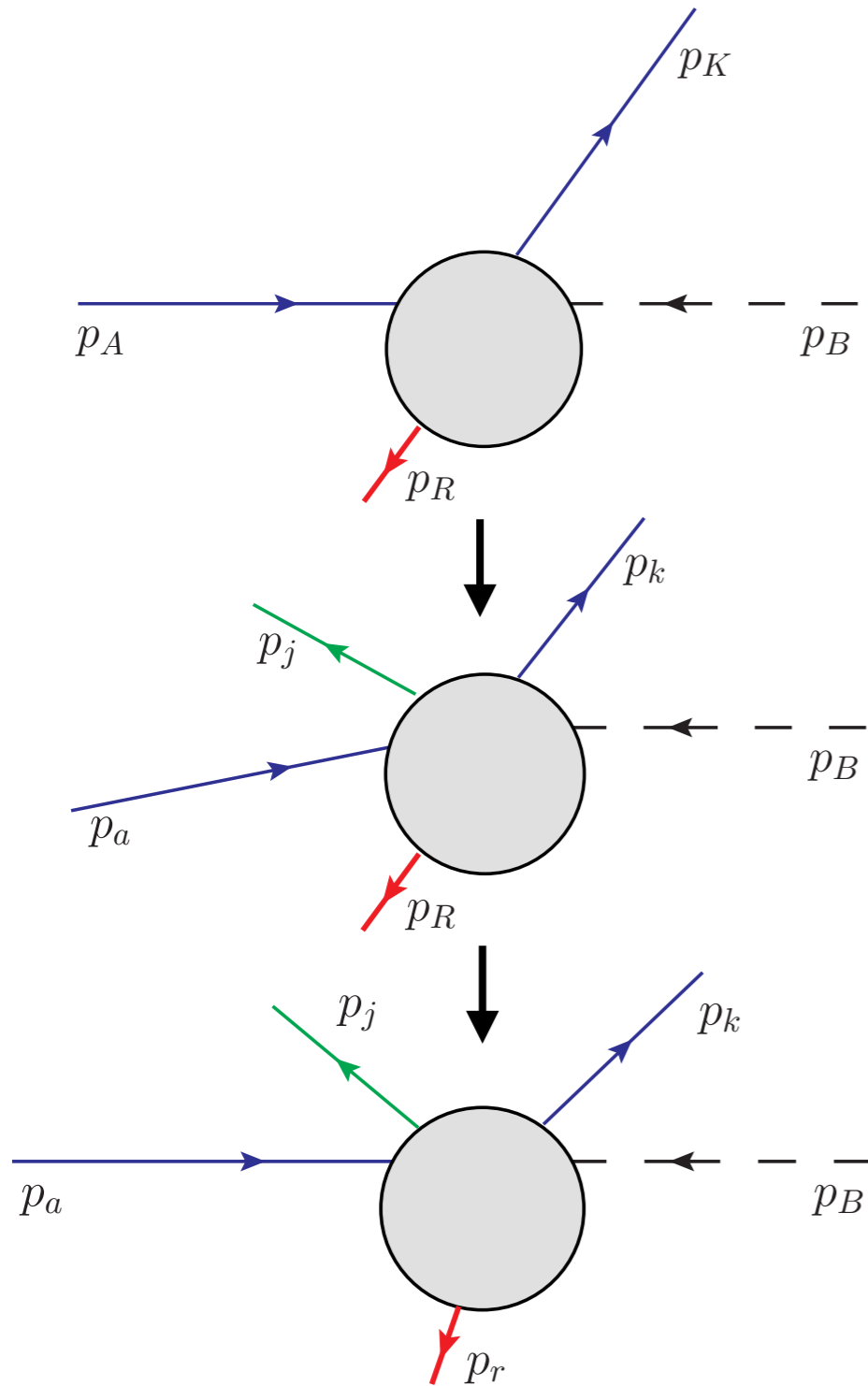
$$p_k = p_a - p_A + p_K - p_j$$

p_k emits p_j with p_a spectating

- No Lorentz boost required $\rightarrow p_R$ does not change
- Automatically $x_a > x_A$
- Correct collinear and soft behaviour
- Current default map in Vincia

$$d\Phi_{\text{ant}} = \frac{1}{16\pi^2} \frac{s_{AK}}{(s_{AK} + s_{jk})^2} ds_{aj} ds_{jk} \frac{d\varphi}{2\pi}$$

Initial - Final Mapping



Kinematics

$$p_a = c_1 p_A$$

$$p_j = c_2 p_A + c_3 p_K + c_4 p_R + c_5 p_{\perp}(\varphi)$$

$$p_k = c_6 p_A + c_7 p_K + c_8 p_R + c_9 p_{\perp}(\varphi)$$

$$p_r = p_a - p_A + p_K + p_R - p_j - p_k$$

Initial - Final Mapping

Map 2: p_K retains its direction

$$p_a = \frac{s_{ak}}{s_{AK} - s_{aj}} p_A + \frac{s_{aj} s_{sjk}}{s_{AK} (s_{AK} - s_{aj})} p_K + \frac{\sqrt{s_{jk} s_{aj} s_{ak}}}{s_{AK} - s_{aj}} p_{\perp}(\varphi)$$

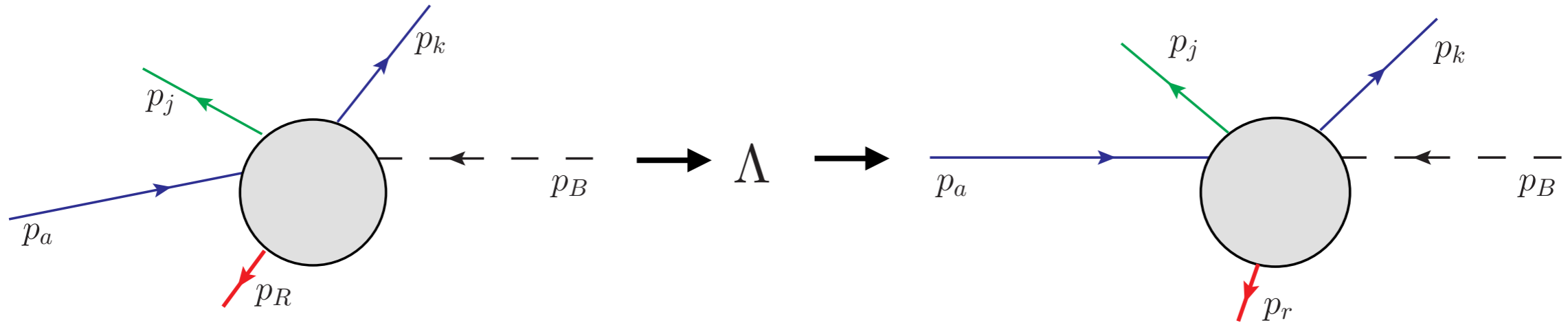
$$p_j = p_a - p_A + p_K - p_k$$

$$p_k = \frac{s_{AK} - s_{aj}}{s_{AK}} p_K$$

p_a emits p_j with p_k spectating

- Lorentz boost required to realign $p_a \rightarrow p_R$ changes
- Not necessarily $x_a > x_A$
- Correct collinear and soft behaviour

Lorentz boost



$$\Lambda^{\mu\nu} = g^{\mu\nu} + \frac{p_B^\mu p_a^\nu - p_a^\mu p_B^\nu}{p_a \cdot p_B} + \frac{p_A^\mu p_B^\nu - p_B^\mu p_A^\nu}{p_A \cdot p_B} + \frac{p_A \cdot p_a}{(p_A \cdot p_B)(p_a \cdot p_B)} p_B^\mu p_B^\nu$$

Properties:

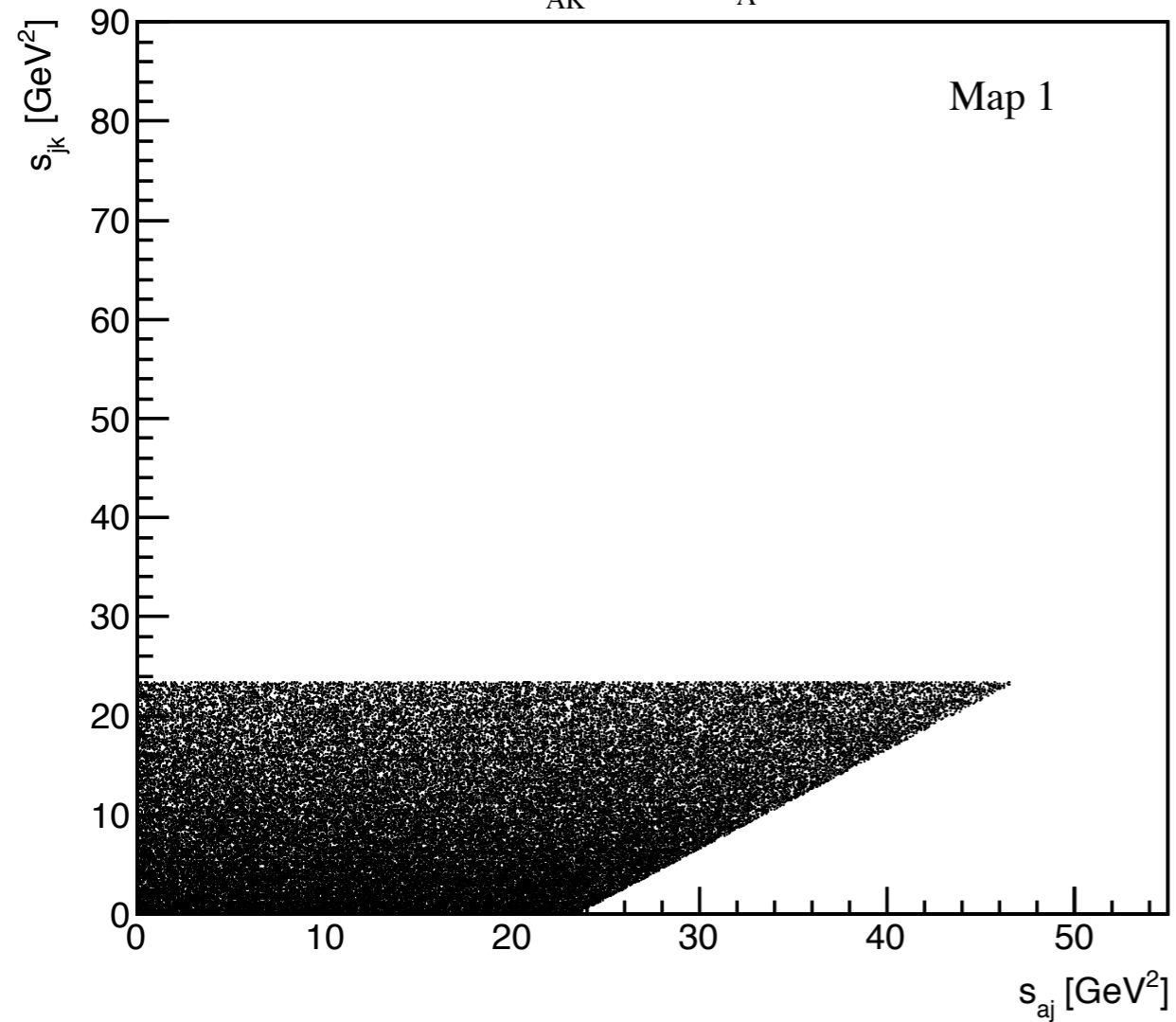
$$(\Lambda p_B) = p_B$$

$$(\Lambda p_a) = \frac{x_a}{x_A} p_A$$

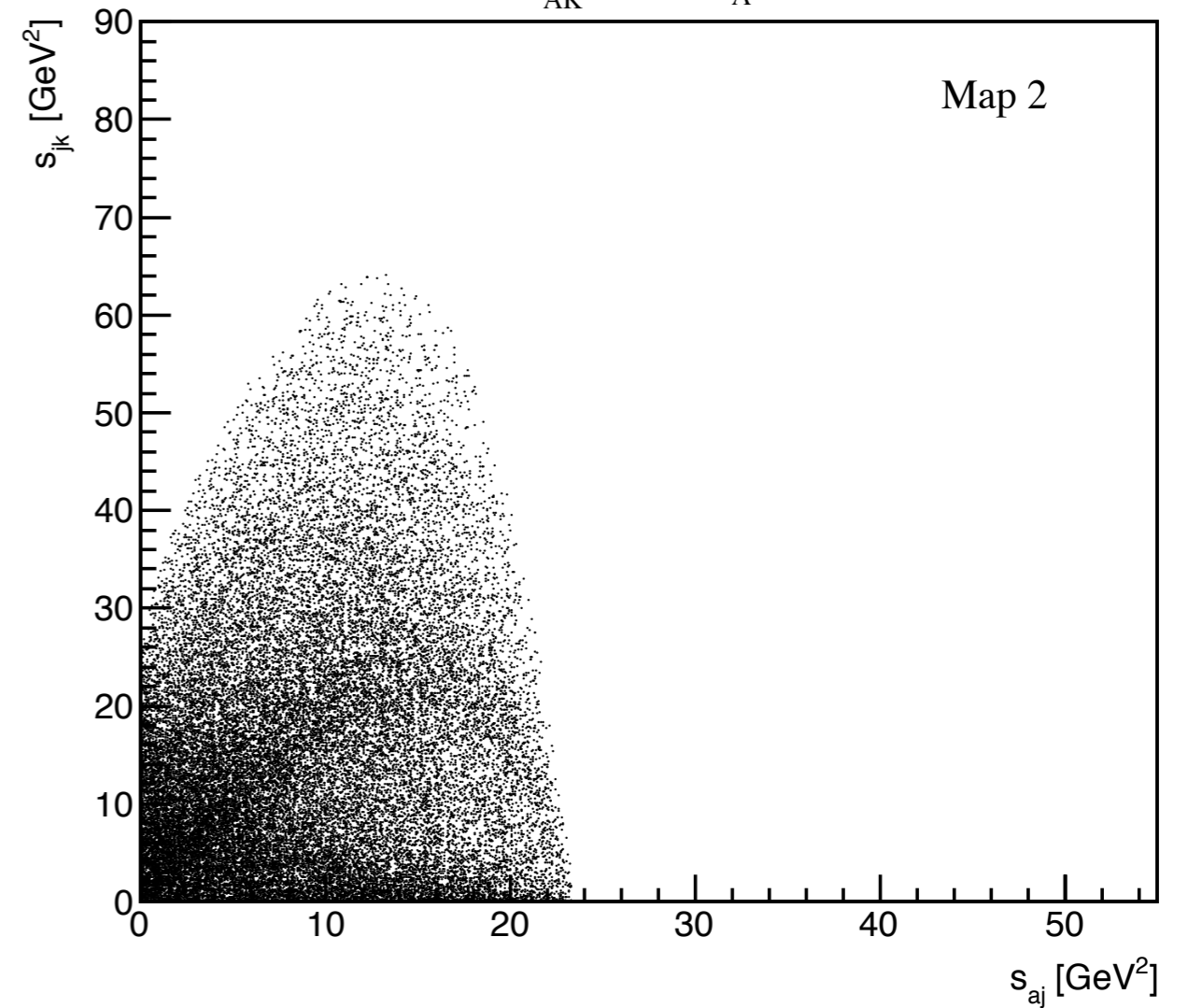
$$d\Phi_{\text{ant}} = \frac{1}{16\pi^2} \frac{1}{s_{AK}} \frac{s_{AB}^2}{s_{aB}^2} ds_{aj} ds_{jk} \frac{d\varphi}{2\pi}$$

Phase Space

Antenna Phase Space, $s_{AK} = 23.4$, $x_A = 0.5$

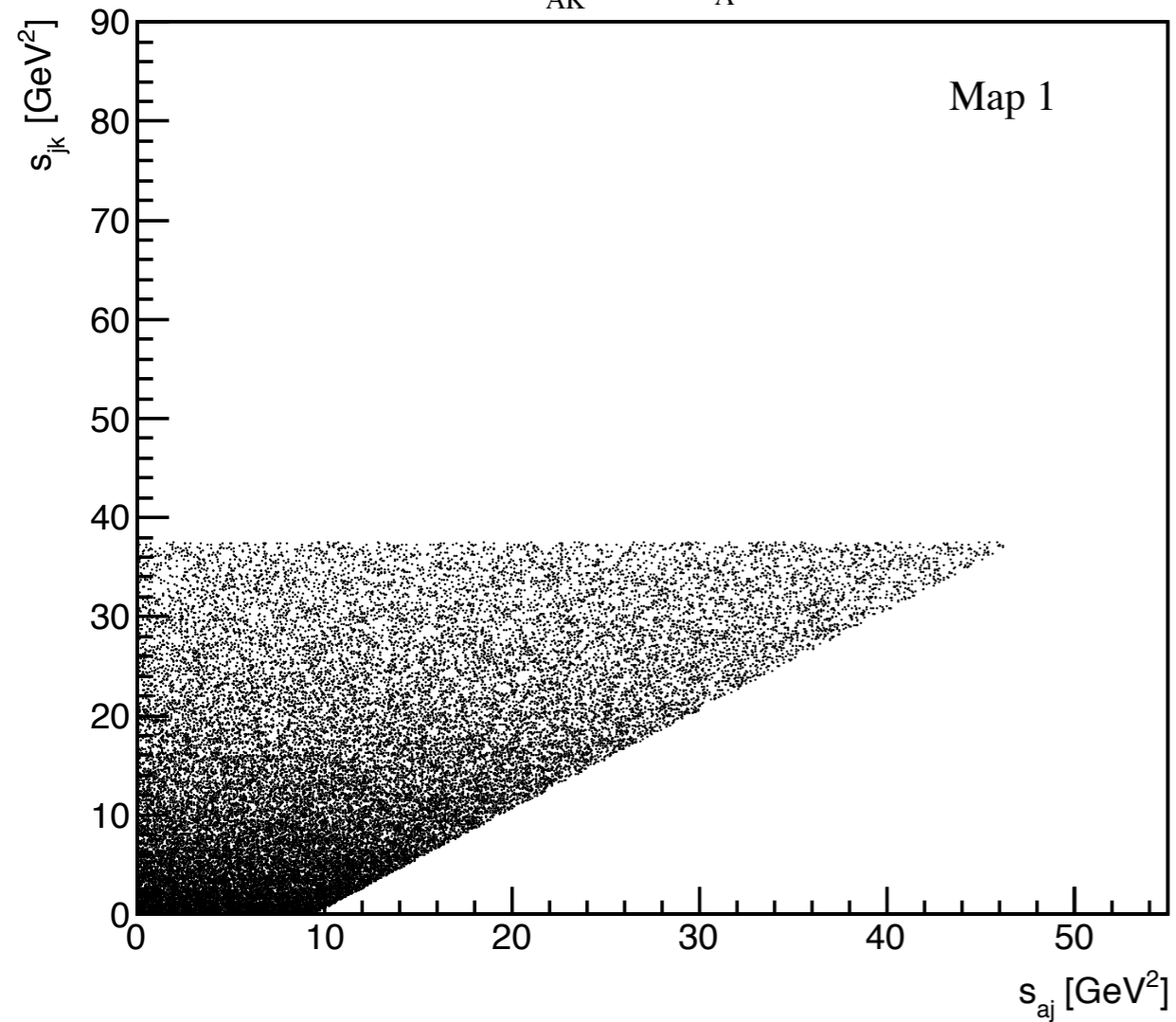


Antenna Phase Space, $s_{AK} = 23.4$, $x_A = 0.5$

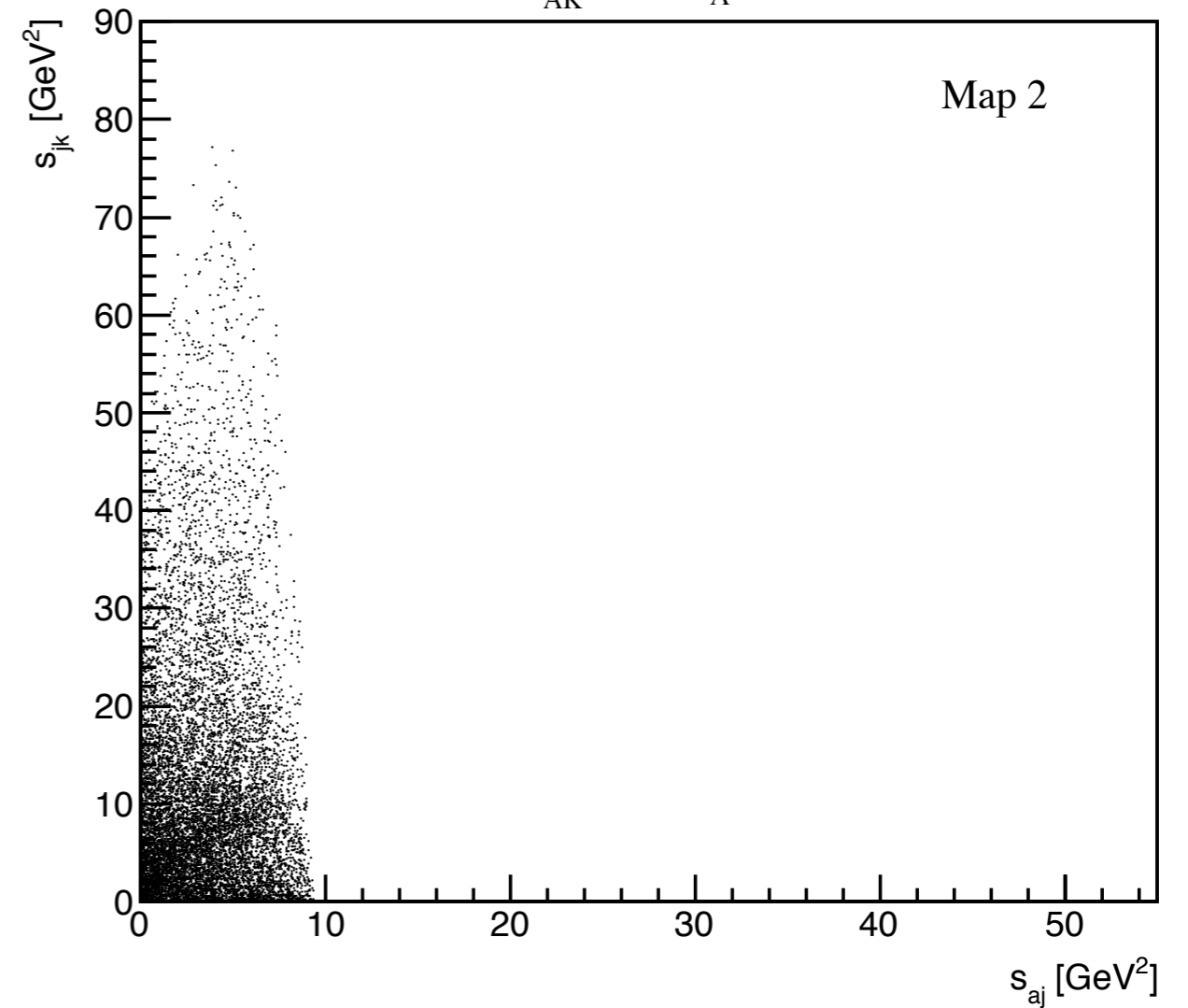


Phase Space

Antenna Phase Space, $s_{AK} = 9.4$, $x_A = 0.2$

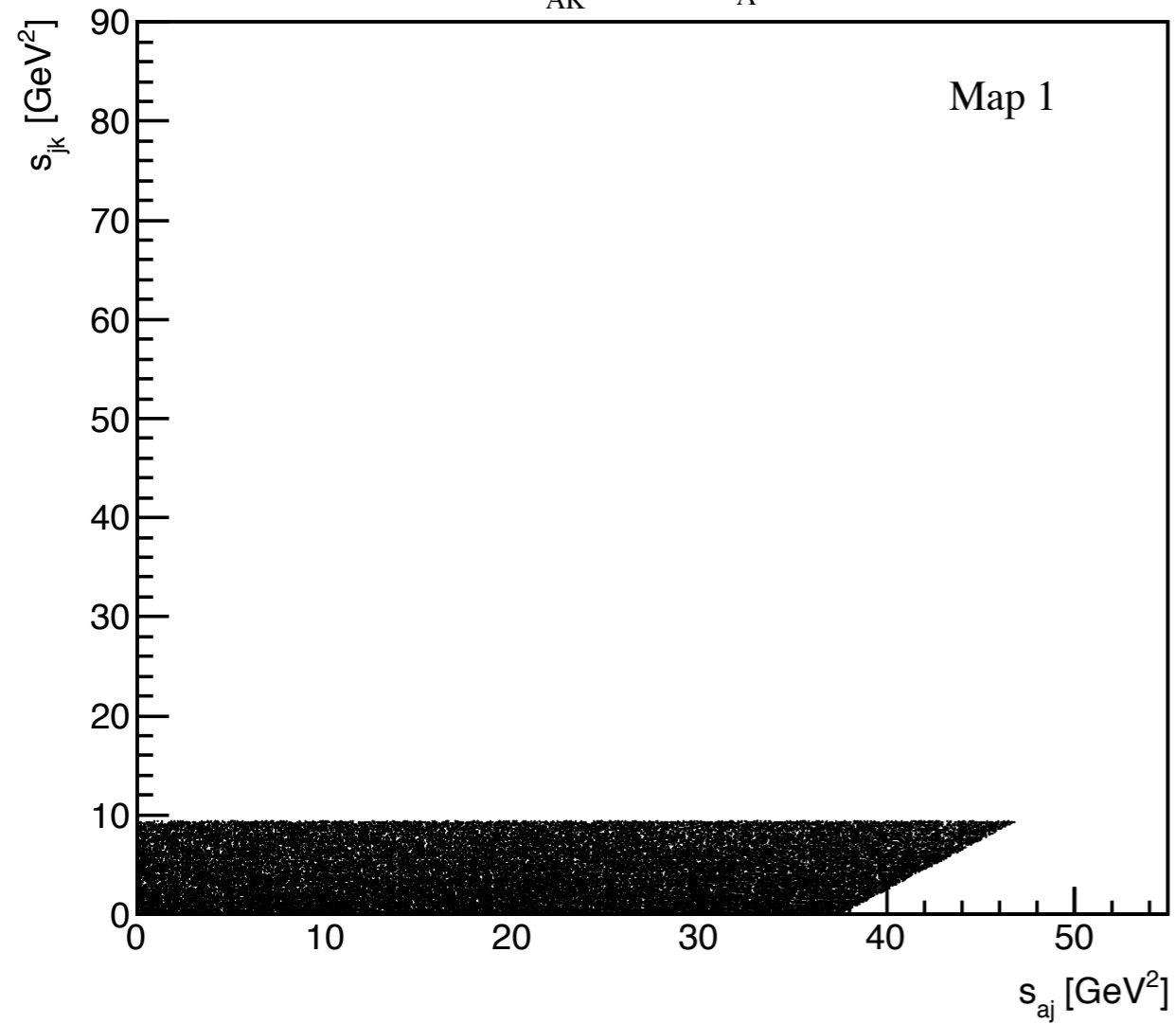


Antenna Phase Space, $s_{AK} = 9.4$, $x_A = 0.2$

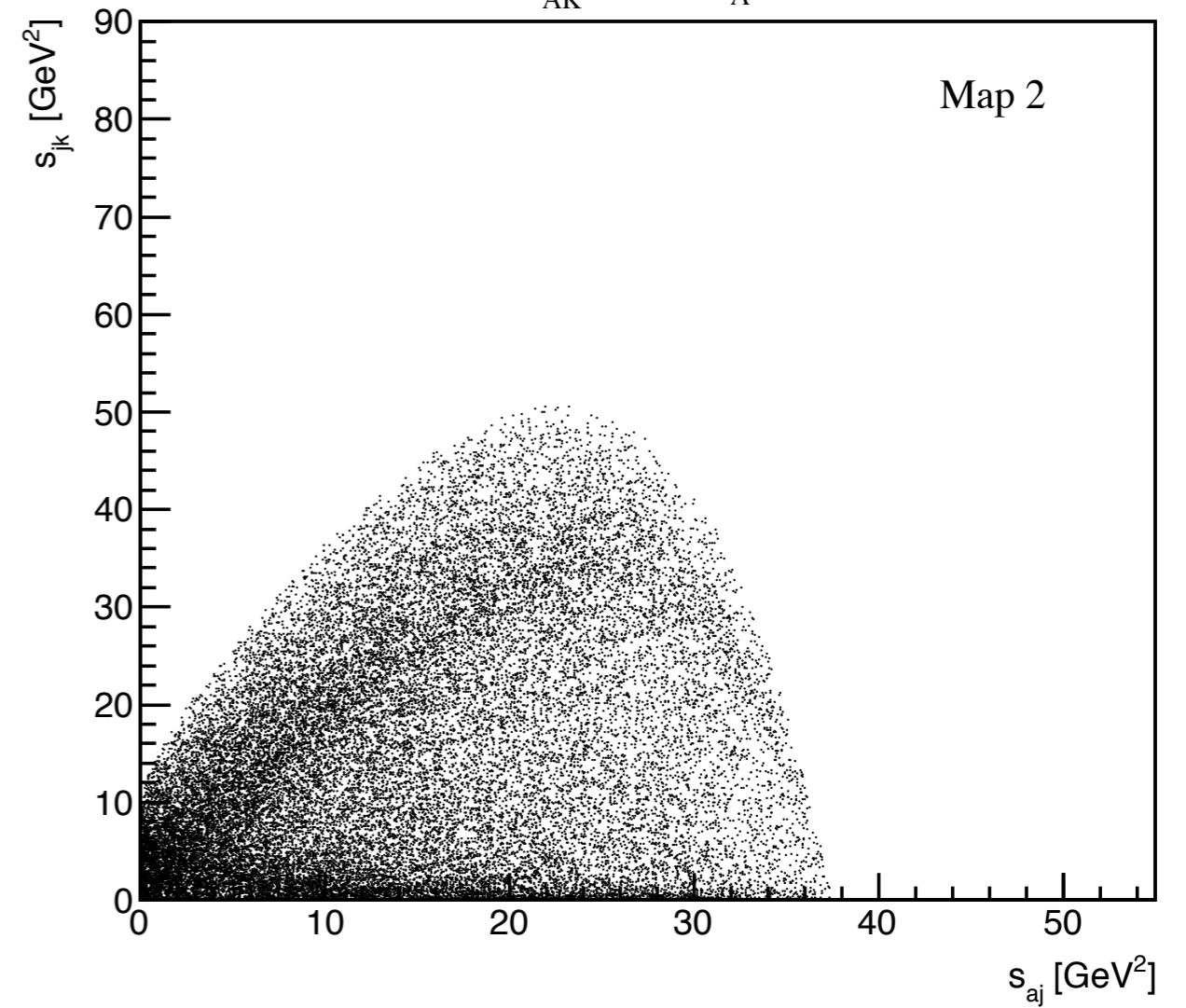


Phase Space

Antenna Phase Space, $s_{AK} = 37.5$, $x_A = 0.8$



Antenna Phase Space, $s_{AK} = 37.5$, $x_A = 0.8$



Implementation

Idea: Select maps probabilistically

$$P_1 = \frac{s_{aj}}{s_{aj} + s_{jk}}$$

$$P_1 = \frac{s_{jk}}{s_{aj} + s_{jk}}$$

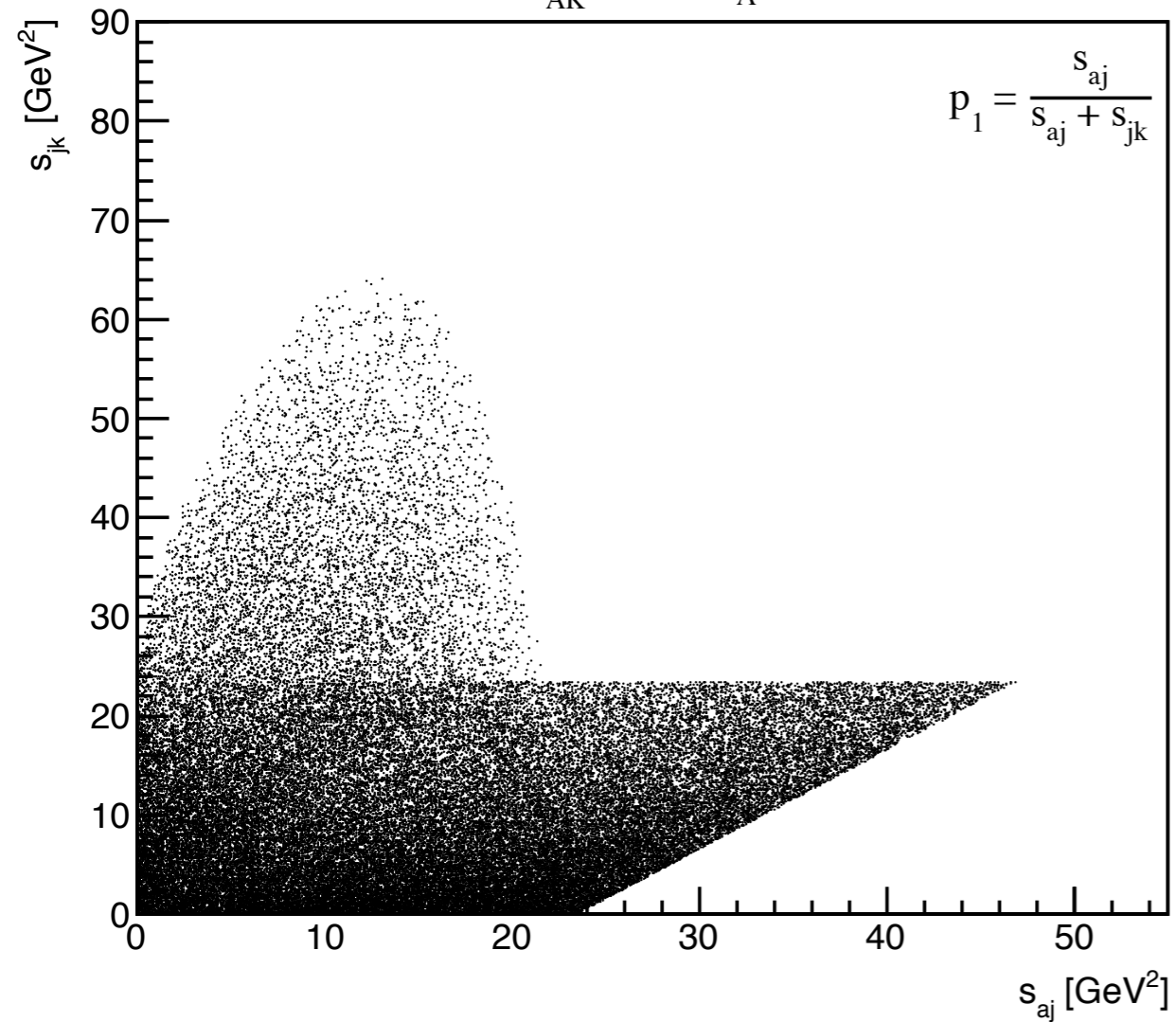
Similar to dipole approach

Correct Jacobian by veto with a factor

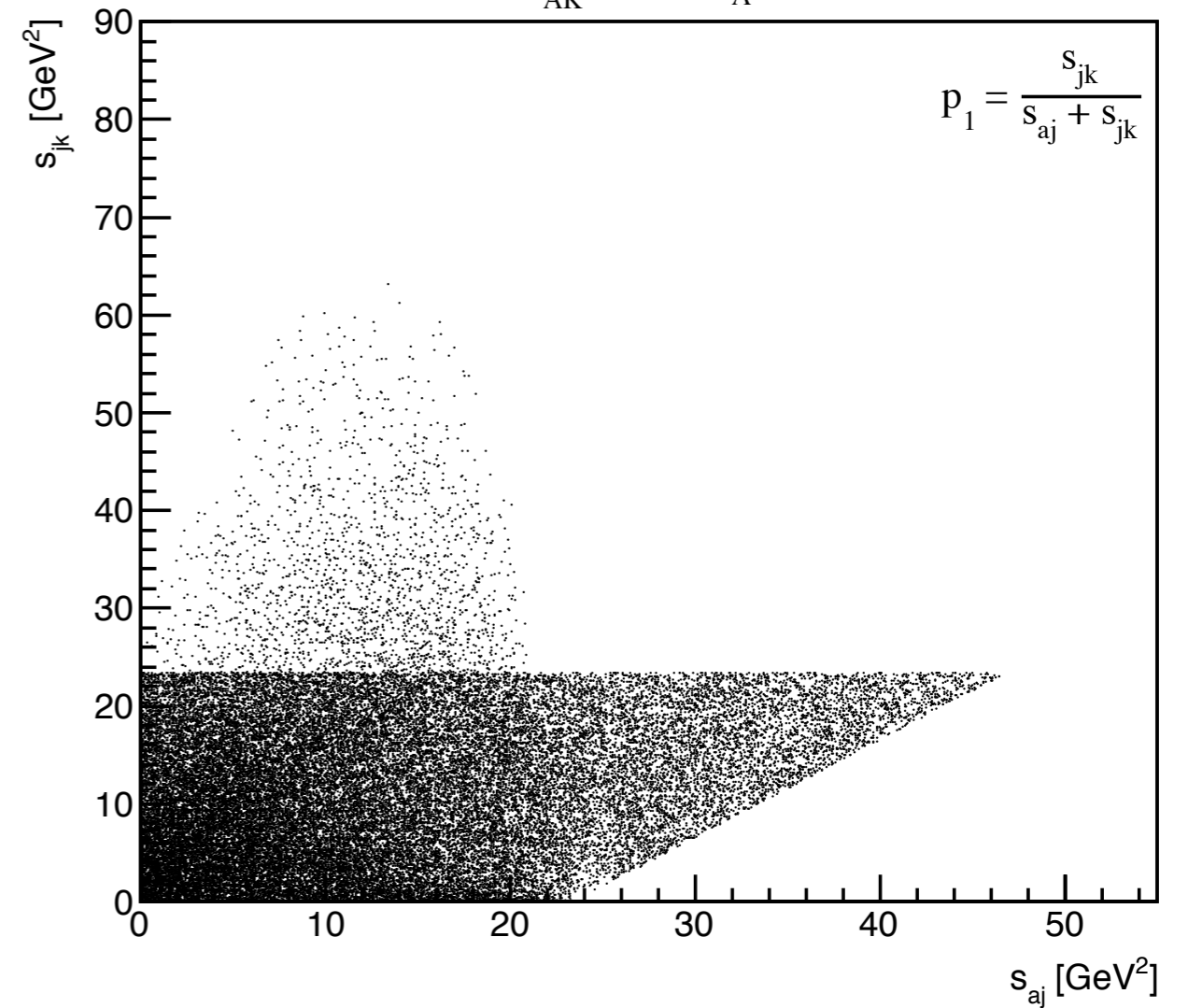
$$P_J = \frac{P_1 \left(\frac{x_{A1}}{x_{a1}} \right)^2 + (1 - P_1) \left(\frac{x_{A2}}{x_{a2}} \right)^2}{\left(\frac{x_{A1}}{x_{a1}} \right)^2}$$

Phase Space

Antenna Phase Space, $s_{AK} = 23.4, x_A = 0.5$

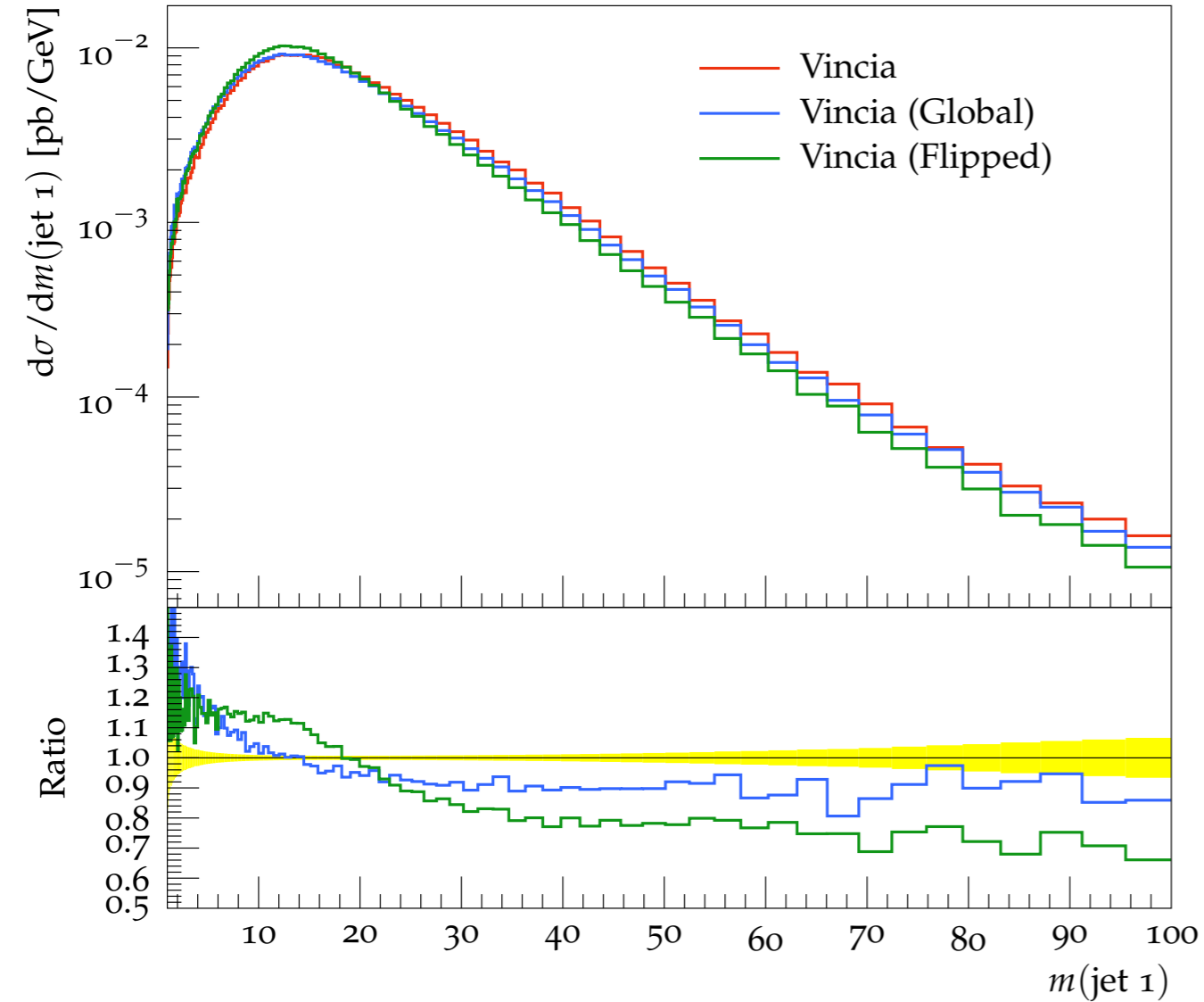


Antenna Phase Space, $s_{AK} = 23.4, x_A = 0.5$

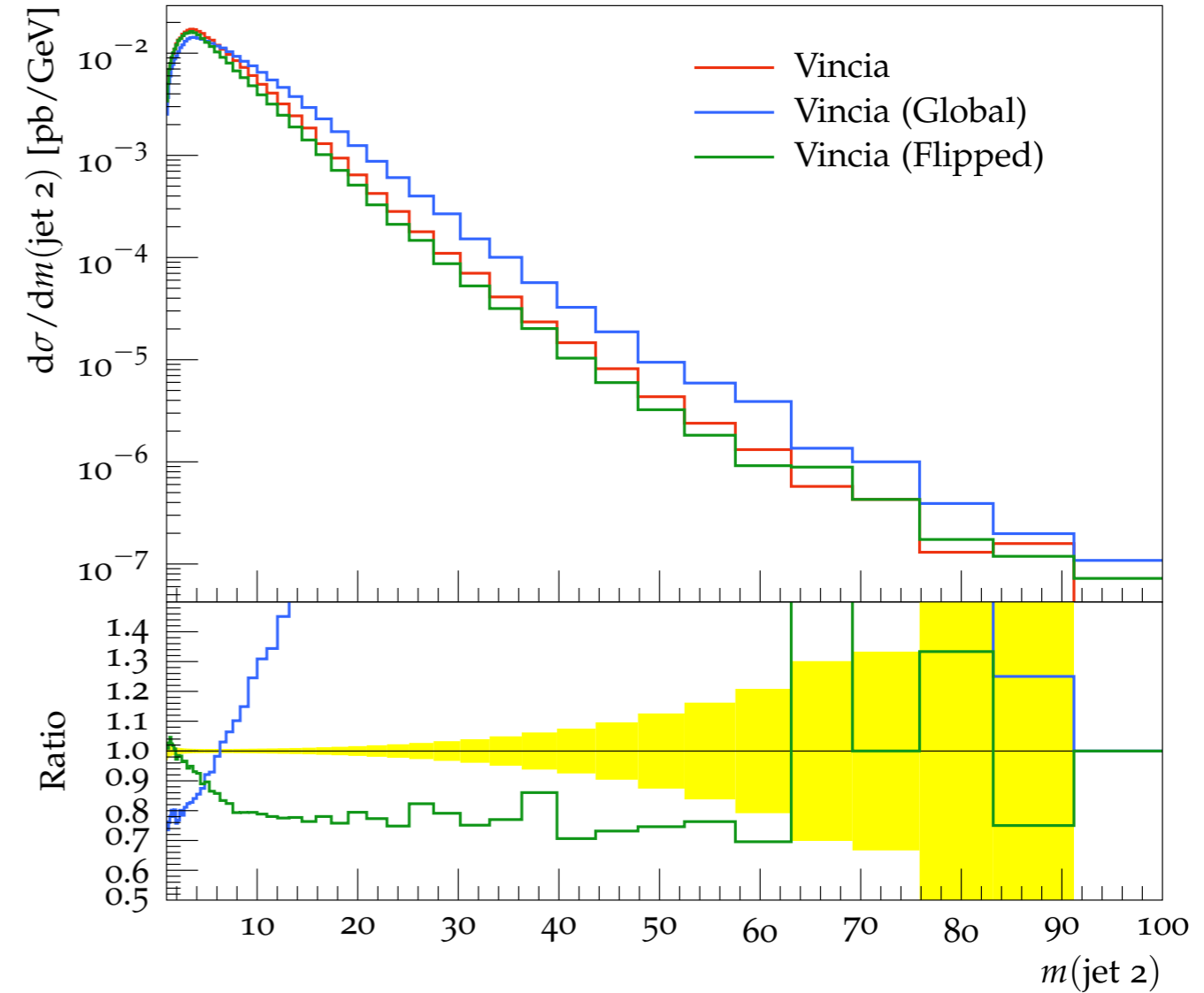


$$q + \bar{q} \rightarrow \gamma^*/Z + g$$

Mass of first jet



Mass of second jet



Conclusion

Goal: Incorporate global recoil for initial-final antennae in Vincia

Linear combination of dipole-like maps

- Agnostic about emitter/spectator roles
- “Free parameter” selection probability

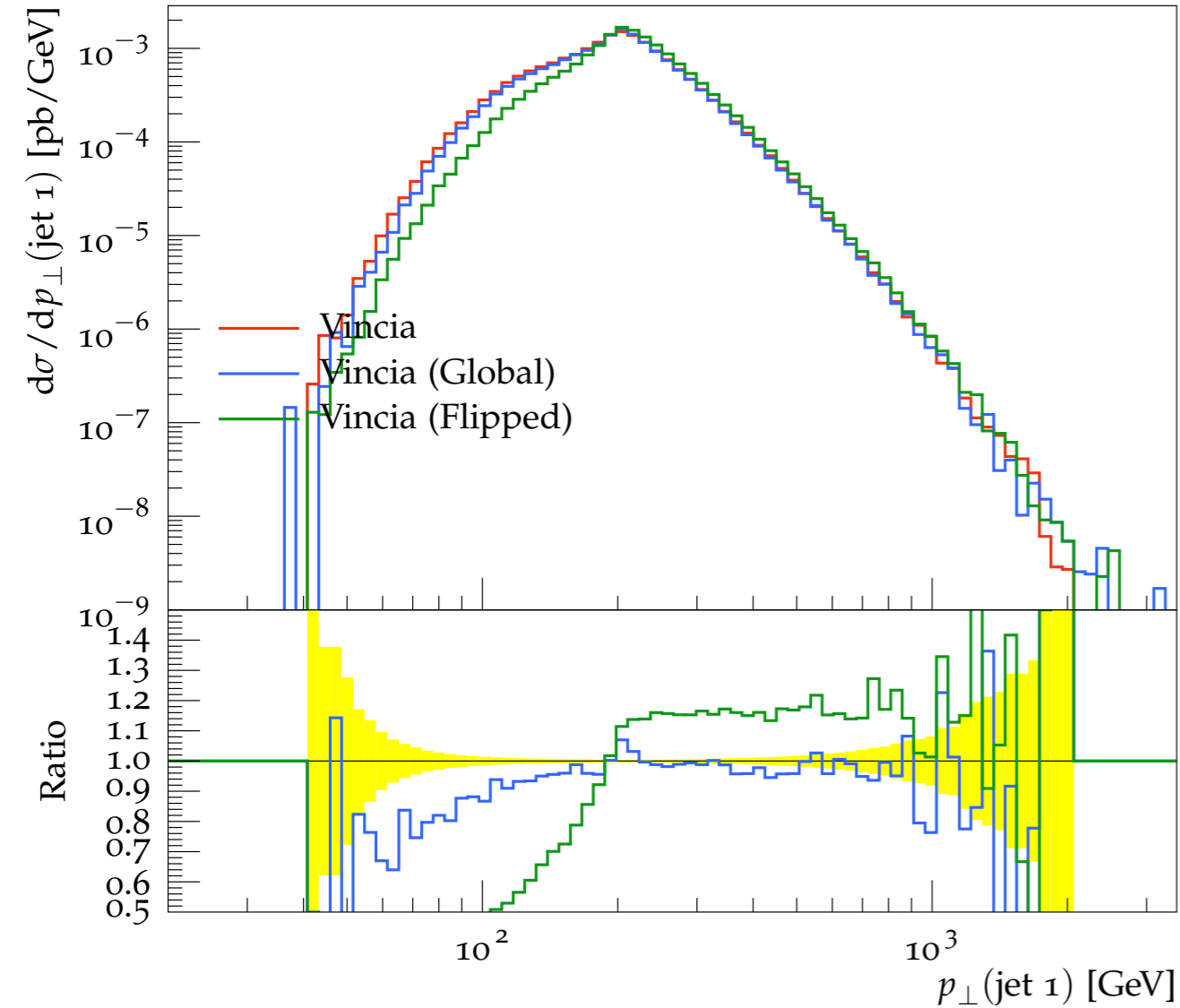
Outlook

- More efficient implementation
- Investigate influence of the selection probability

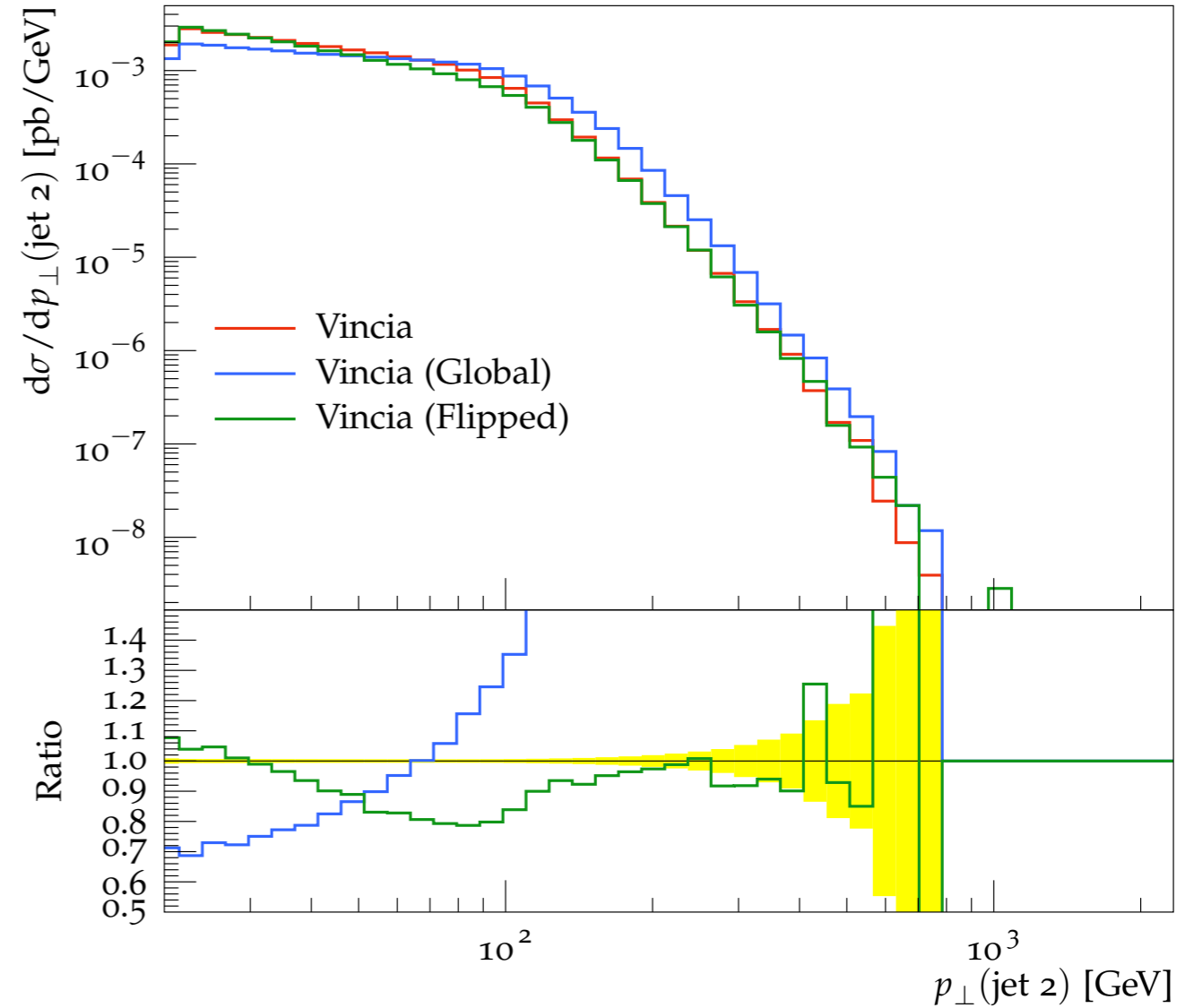
Phase Space

$$q + \bar{q} \rightarrow \gamma^*/Z + g$$

Transverse momentum of leading jet



Transverse momentum of second jet



Phase Space

$$q + \bar{q} \rightarrow \gamma^*/Z + g$$

