

Electroweak corrections in event generators

Marek Schönherr

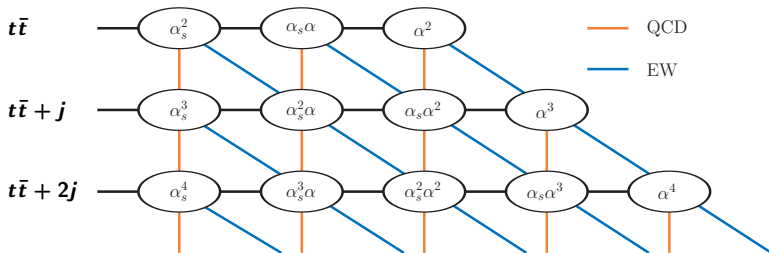
Parton Showers and Resummation Workshop – Lund, Sweden

06 Jun 2018



Anatomy of higher-order calculations – e.g. $t\bar{t} + \text{jets}$

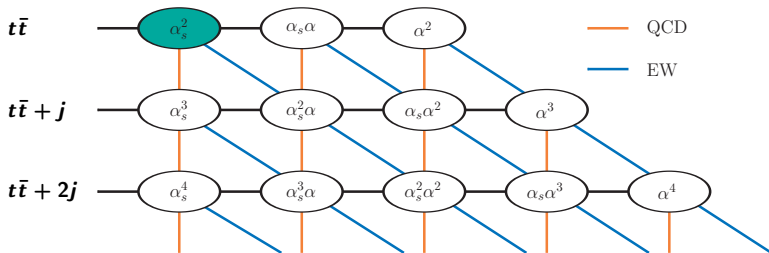
tree-level configuration



	$t\bar{t}$	$t\bar{t} + j$
LO	$\mathcal{O}(\alpha_s^2)$	$\mathcal{O}(\alpha_s^3)$
NLO QCD	$\mathcal{O}(\alpha_s^3)$	$\mathcal{O}(\alpha_s^4)$
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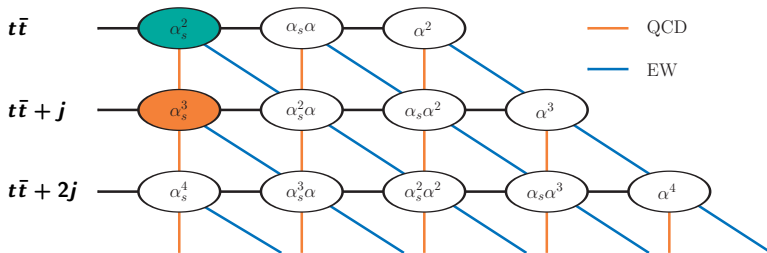
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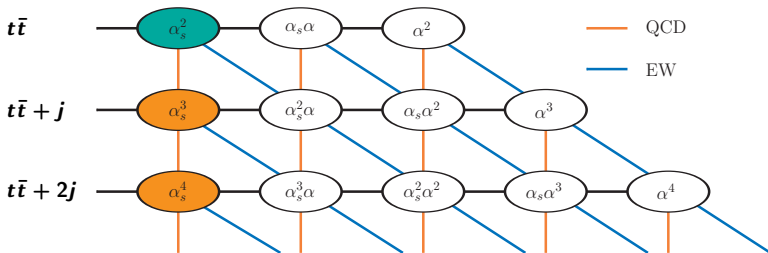
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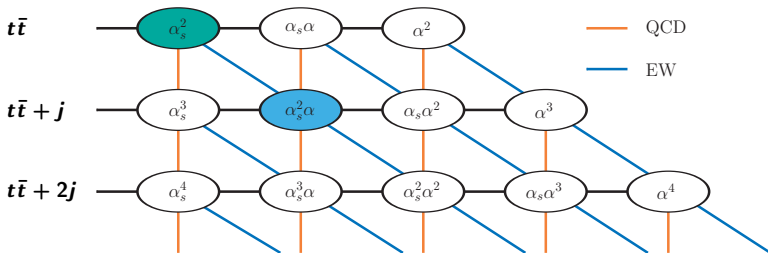
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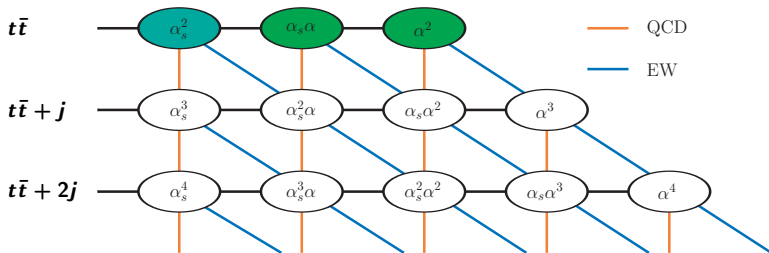
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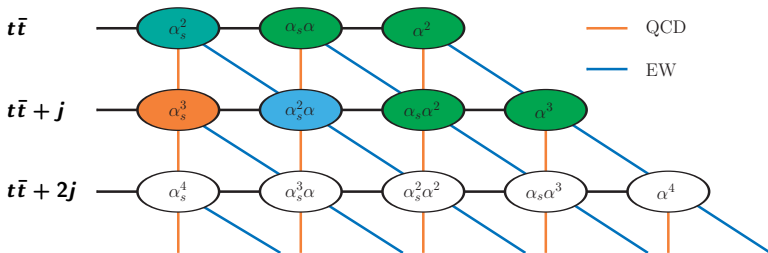
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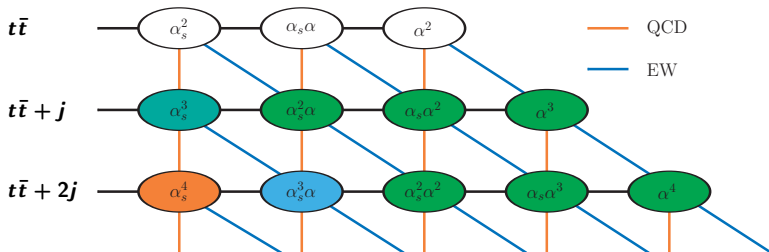
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Table of contents

- 1 NLO EW corrections
- 2 EW corrections in multijet merging
- 3 Soft-photon resummation
- 4 Conclusions

NLO EW corrections

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Setup

SHERPA+OPENLOOPS

- uses automated framework for general NLO calculations in SHERPA tree-level matrix elements, dipole subtraction, phase space integration, process management

MS arXiv:1712.07975

- virtual corrections from OPENLOOPS

Cascioli, Maierhöfer, Pozzorini arXiv:1111.5206

Parameters

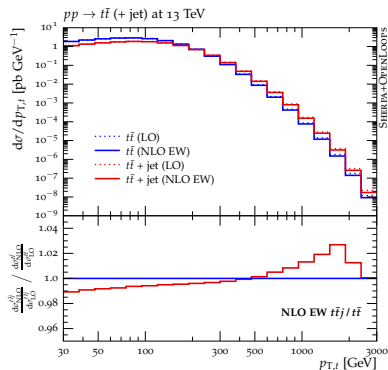
- $\mu_{R/F} = \frac{1}{2} (E_T^t + E_T^{\bar{t}})$ in fixed-order calculation
- CKKW scale with $\mu_{\text{core}} = \frac{1}{2} \left(\frac{1}{\hat{s}} + \frac{1}{m_t^2 - \hat{t}} + \frac{1}{m_t^2 - \hat{u}} \right)^{-\frac{1}{2}}$ in MEPS@NLO
- NNPDF3.0nnlo $\alpha_s = 0.118$, neglect γ -induced
- spin-correlated top decays, default tune for underlying event and hadronisation in data comparison

Setup

- SHERPA+OPENLOOPS:
 - $pp \rightarrow V + 0, 1, 2(, 3)$ jets FCC report, arXiv:1607.01831
EW report arXiv:1606.02330
LH'15 arXiv:1605.04692
Kallweit,Lindert,Maierhöfer,Pozzorini,MS arXiv:1412.5157, arXiv:1511.08692
 - $pp \rightarrow Zj/pp \rightarrow \gamma j$ ratio LH'15 arXiv:1605.04692
Kallweit,Lindert,Maierhöfer,Pozzorini,MS arXiv:1505.05704
 - $pp \rightarrow \gamma/\ell\ell/\ell\nu/\nu\nu + j$ Lindert et.al arXiv:1705.04664
 - $pp \rightarrow Vh$ FCC report, arXiv:1607.01831
 - $pp \rightarrow 2\ell 2\nu$ Kallweit,Lindert,Pozzorini,MS, arXiv:1705.00598
 - $pp \rightarrow t\bar{t}/t\bar{t}j$ Gütschow, Lindert, MS arXiv:1803.00950
 - $pp \rightarrow t\bar{t}h$ LH'15 arXiv:1605.04692
- SHERPA+GOSAM
 - $pp \rightarrow \gamma\gamma + 0, 1, 2$ jets Chiesa et.al. arXiv:1706.09022
 - $pp \rightarrow \gamma\gamma\gamma / \gamma\gamma\ell\nu / \gamma\gamma\ell\ell$ Greiner, MS arXiv:1710.11514
 - $pp \rightarrow \gamma\gamma b\bar{b}$ Greiner, MS in prep.
- SHERPA+RECOLA
 - $pp \rightarrow V + 0, 1, 2 j, pp \rightarrow 4\ell, pp \rightarrow t\bar{t}h$ Biedermann et.al. arXiv:1704.05783
 - $pp \rightarrow 3\ell 3\nu$ MS arXiv:1806.00307

Top pair production in association with jets

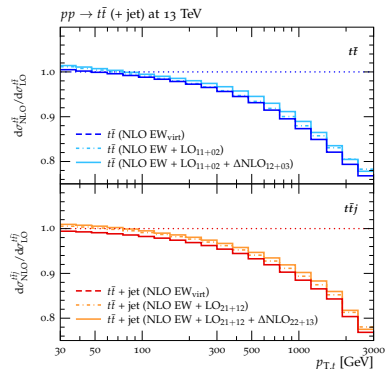
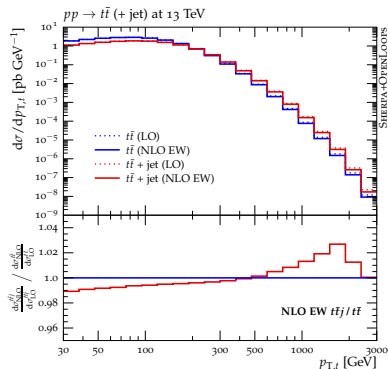
Gütschow, Lindert, MS arXiv:1803.00950



- $pp \rightarrow t\bar{t}$
 - LO: $\mathcal{O}(\alpha_s^2)$, $\mathcal{O}(\alpha_s\alpha)$, $\mathcal{O}(\alpha^2)$
 - include NLO corrections to subleading orders
- $pp \rightarrow t\bar{t}j$
 - LO: $\mathcal{O}(\alpha_s^3)$, $\mathcal{O}(\alpha_s^2\alpha)$, $\mathcal{O}(\alpha_s\alpha^2)$, $[\mathcal{O}(\alpha^3)]$
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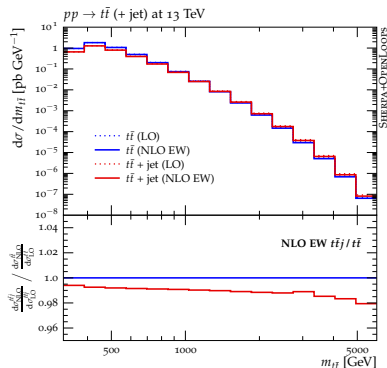
Gütschow, Lindert, MS arXiv:1803.00950



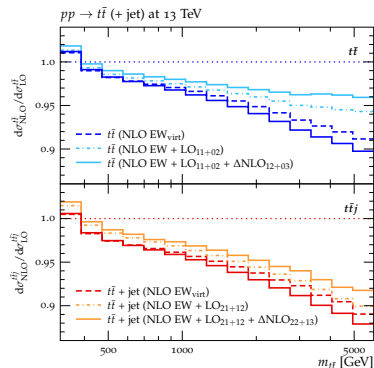
NLO EW factorises from additional jet activity

Top pair production in association with jets

Gütschow, Lindert, MS arXiv:1803.00950

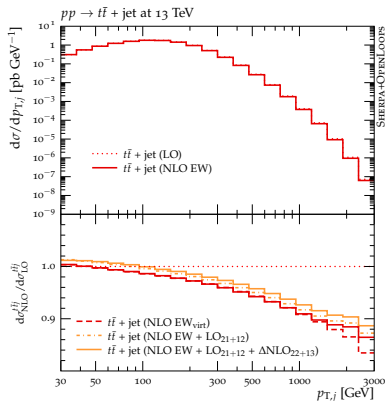


subleading orders important

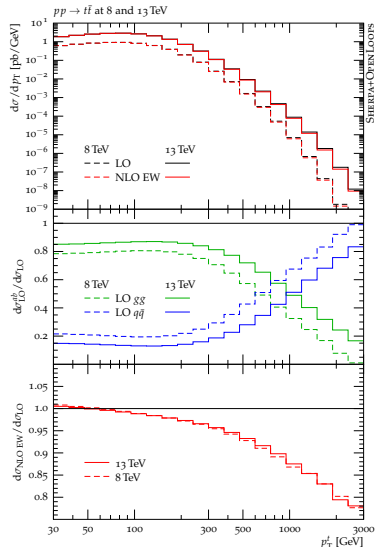


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NLO EW corrections to $t\bar{t}$ at 8 and 13 TeV

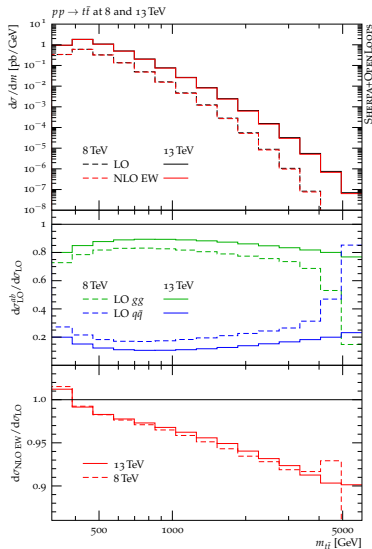
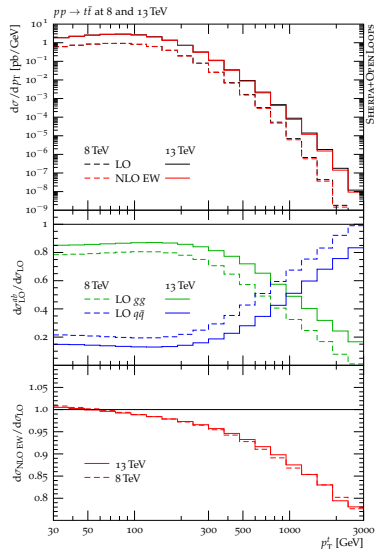


- gg channel receives smaller EW corrections in Sudakov limit than $q\bar{q}$ channel, at 1 TeV:

$$\delta_{EW,sud}^{q\bar{q}} \approx 1.5 \delta_{EW,sud}^{gg}$$

- composition of total from gg vs $q\bar{q}$ channels changes
 - NLO EW correction changes
 - effect still small

NLO EW corrections to $t\bar{t}$ at 8 and 13 TeV

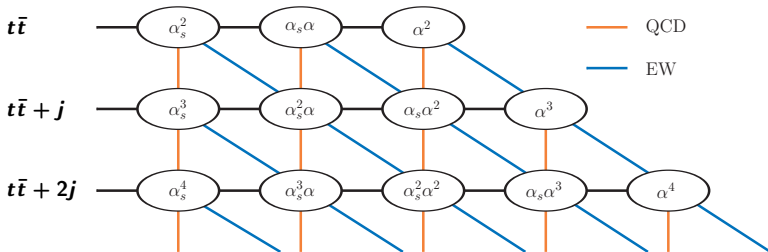


EW corrections in multijet merging

- 1 NLO EW corrections
- 2 EW corrections in multijet merging**
- 3 Soft-photon resummation
- 4 Conclusions

EW corrections in multijet merging – e.g. $t\bar{t}$

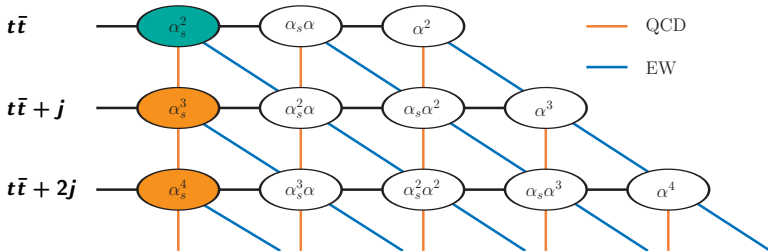
tree-level configuration



- extend NLO QCD multijet merging
- include approximate NLO EW corrections
- also include subleading tree-level corrections

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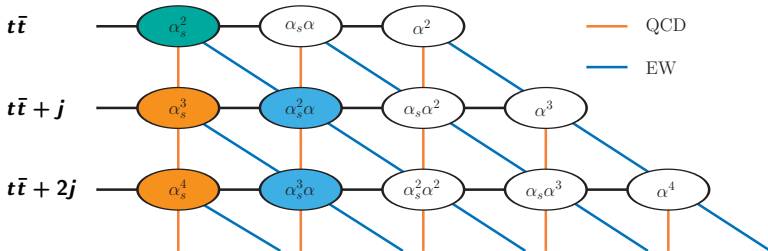
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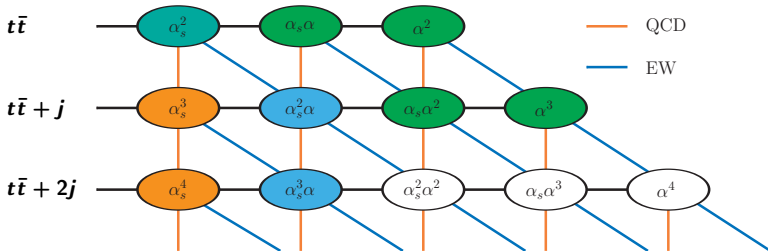
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EW corrections in multijet merging

- straight forward in Sudakov limit
→ modify weight of LO kinematics

Denner, Pozzorini [hep-ph/0010201](#), [hep-ph/0104127](#)

- $\text{LO} \times \text{EW}_{\text{sud}}$ in ALPGEN and HERWIG for selected processes

Chiesa et.al. [arXiv:1305.6837](#)

Gieseke, Kasprzik, Kühn [arXiv:1401.3964](#)

- at NLO, both additive and multiplicative combination possible
 $\text{NLO QCD} + \text{EW}_{\text{sud}}$ vs. $\text{NLO QCD} \times \text{EW}_{\text{sud}}$

- typically done on the histogram/observable level
→ not straight forward on event-by-event basis
- choose additive approach for now

Kallweit, Lindert, Maierhöfer, Pozzorini, MS [arXiv:1511.08692](#)

EW corrections in multijet merging

- incorporate approximate electroweak corrections in SHERPA's NLO QCD multijet merging (MEPS@NLO)
- modify MC@NLO \bar{B} -function to include NLO EW virtual corrections and integrated approx. real corrections

$$\bar{B}_{n,\text{QCD}+\text{EW}_{\text{virt}}}(\Phi_n) = \bar{B}_{n,\text{QCD}}(\Phi_n) + V_{n,\text{EW}}(\Phi_n) + I_{n,\text{EW}}(\Phi_n) + B_{n,\text{mix}}(\Phi_n)$$

- real QED radiation can be recovered through standard tools (parton shower, YFS resummation)
- simple stand-in for proper QCD+EW matching and merging
→ validated at fixed order, found to be reliable,
diff. $\lesssim 5\%$ for observables not driven by real radiation

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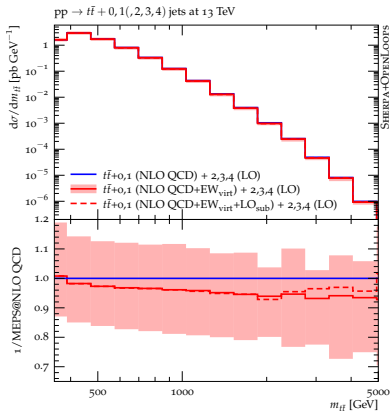
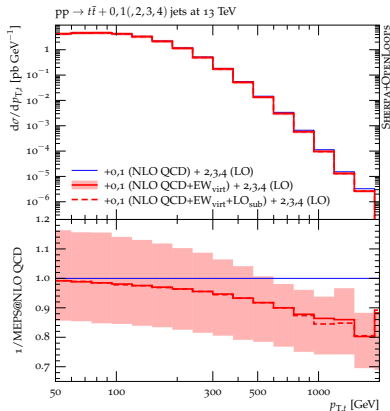
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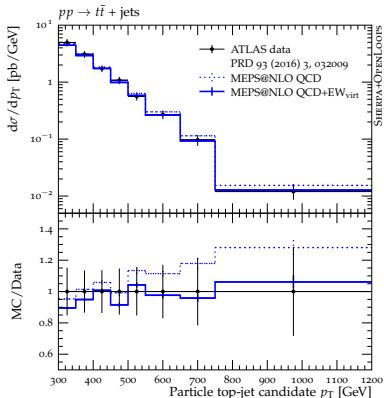
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Results: $t\bar{t} + \text{jets}$



reproduces well the corrections seen at fixed-order

Results: $t\bar{t} + \text{jets}$ at high p_T



Gütschow, Lindert, MS arXiv:1803.00950

- $pp \rightarrow t\bar{t} + 0, 1j@NLO$
+ 2, 3, 4j@LO
- additional LO multiplicities inherit electroweak corrections through MENLOPS differential K -factor

Höche, Krauss, MS, Siegert
arXiv:1009.1127

- improved description of data

Soft-photon resummation

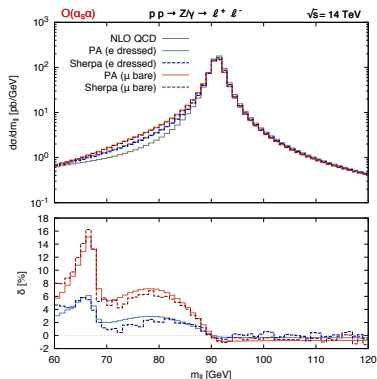
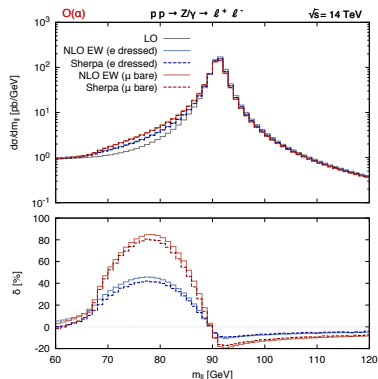
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Soft-photon resummation

- YFS soft-photon resummation default for higher-order QED corrections in SHERPA [Yennie, Frautschi, Suura Annals Phys.13\(1961\)379-452](#)
[MS, Krauss JHEP12\(2008\)018](#)
- coherent radiation off multipoles
- universal soft eikonal supplemented with universal hard collinear corrections
- process specific corrections can be easily incorporated where known
 - NLO QED accuracy in $W \rightarrow \ell\nu$ and $Z \rightarrow \ell\ell$
and other important resonant decay channels
 - generic resonance identification in multibody final states
invariant masses are preserved
important in e.g. VV etc.

Accuracy in $pp \rightarrow \ell\ell$

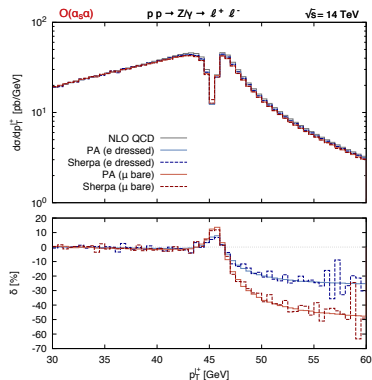
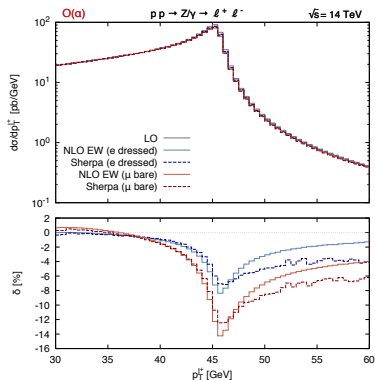
Huss, MS for LH'15



- $\mathcal{O}(\alpha)$ and $\mathcal{O}(\alpha_s\alpha)$ electroweak corrections well reproduced
- residual difference due to multi-photon emissions
- genuine weak corrections very small

Accuracy in $pp \rightarrow \ell\ell$

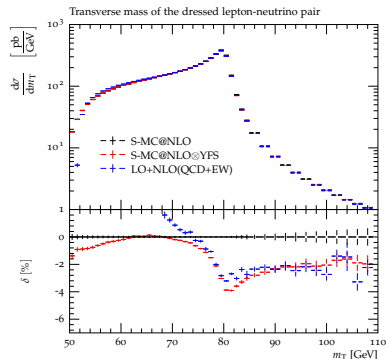
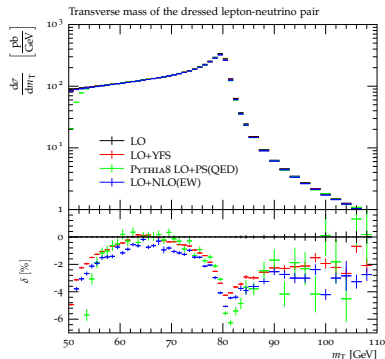
Huss, MS for LH'15



- $\mathcal{O}(\alpha)$ and $\mathcal{O}(\alpha_s\alpha)$ electroweak corrections well reproduced
- for $p_{\perp}^{\ell} > \frac{1}{2}m_Z$ driven by ISR (not in YFS), but \ll QCD ISR
- genuine weak corrections sizeable only at large p_{\perp}^{ℓ}

Accuracy in $pp \rightarrow \ell\nu$

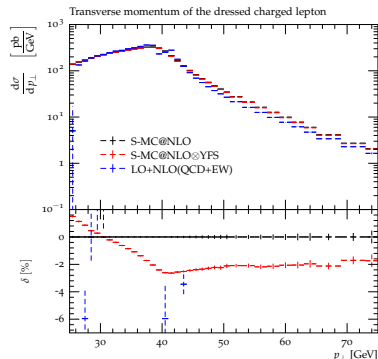
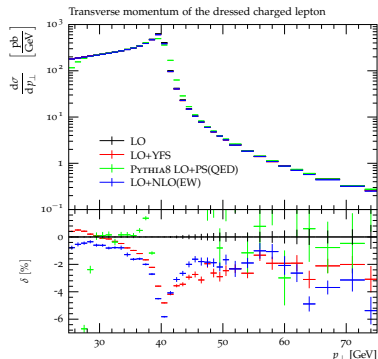
Höche, Prestel, MS for EW report



- $\mathcal{O}(\alpha)$ electroweak corrections well reproduced
- residual difference due to multi-photon emissions
- genuine weak corrections small

Accuracy in $pp \rightarrow \ell\nu$

Höche, Prestel, MS for EW report



- $\mathcal{O}(\alpha)$ electroweak corrections well reproduced
- for $p_{\perp}^{\ell} > \frac{1}{2}m_W$ driven by ISR (not in YFS), but \ll QCD ISR
- genuine weak corrections sizeable only at large p_{\perp}^{ℓ}

Conclusions

- EW corrections in the Sudakov limit can easily be incorporated in LO and NLO QCD Monte-Carlo event generators
 - real photon emission effects can be recovered through DGLAP or soft-photon resummation (if matched to NLO QED better than fixed order description at NLO EW)
 - small finite corrections for inclusive distributions not exact to NLO EW
- inclusion of approximate EW corrections in MEPS@NLO available including important contributions from subleading orders
- improves data description at large transverse momenta
- publically available in SHERPA-2.2.5

Thank you for your attention!