

Stable Sexaquark as Dark Matter



Glennys R. Farrar
New York University

Stable Sexaquark and other uds Dark Matter



*How could we have missed a
stable particle made of quarks?*

[Hints from Astrophysics]

[Primordial Nucleosynthesis]

Dark-Matter to Ordinary-Matter ratio

[Detecting S dark matter]

Discovering a stable sexaquark in the lab

Unique among multi-quark states:

Fermi statistics is compatible with a
totally symmetric spatial wave function AND

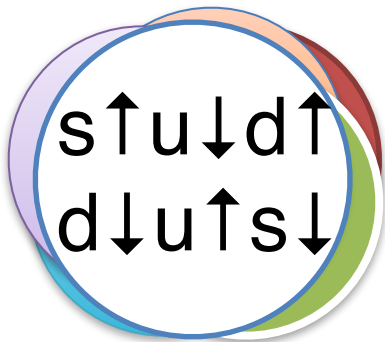
antisymmetric (singlet) in:

color

flavor

spin

totally symmetric in space



S

(Most-Attractive Channel)³ :

6-quark, $Q=0$, $B=2$

Spin-0, scalar

Flavor singlet

$m_S < 2 \text{ GeV}???$

Same quark content as H-dibaryon* (Jaffe 1977), but different physics: **not a loosely bound di- Λ !**

Why consider $m_S \sim 2 m_p^*$?

(*1.876 GeV)

- Light quarks almost massless, i.e. relativistic
 - $m_{u,d} \approx 0$, $m_s = 91 \text{ MeV}$
 - S has same QNs as ground state glueball
 - why not $m_S \approx m_{\text{glueball}} + 180 \text{ MeV} = (1.5-1.7) + 0.18 \text{ GeV} \approx 2 m_p$
 - 3 x di-quark mass = 1.2 - 2 GeV
 - $m_S < 2 (m_p + m_e)$: S is absolutely stable
 - $m_S > 2 (m_p - 8 \text{ MeV})$: nuclei are stable
- Interesting DM candidate
- triple-singlet (color, flavor, spin): MAC, lattice, almost all models $\Rightarrow m_S < 2 m_\Lambda$
 - *extensive experimental searches **exclude** weak-lifetime & $m > 2 \text{ GeV}$*
- bound state exists and mass $< 2 \text{ GeV}$ ($\tau > \tau_{\text{Univ}}$ or stable)

Stable Sexaquark Hypothesis

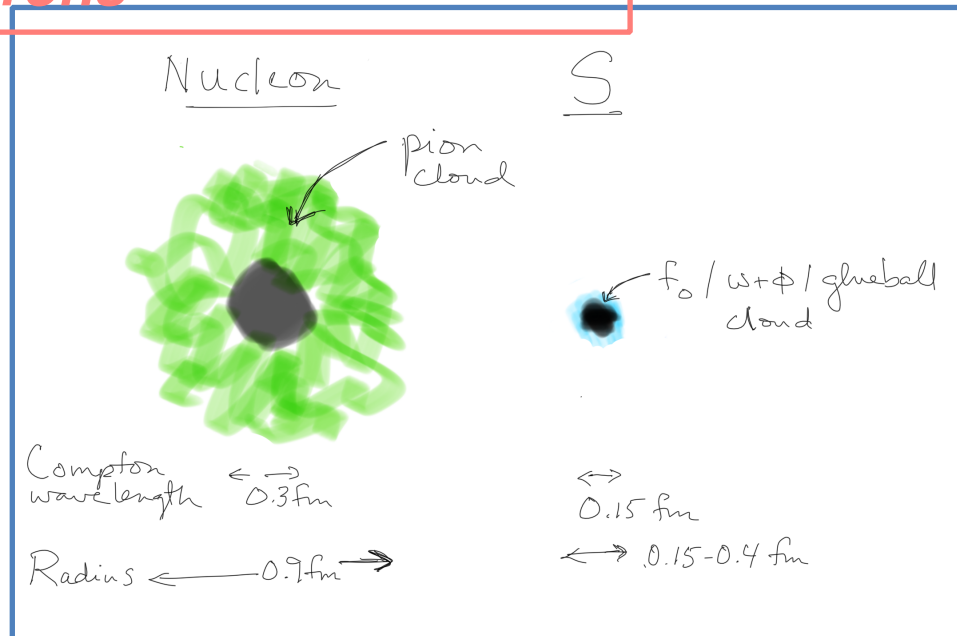
6	sexa- ^[19]	–	sen- ^[20]	sext- ^[21]	hex- ^[22]	hexakis- hexaplo- hexad- e.g. hexahedron	hect- ^[23] hectai-	shat-
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^{a b} Sometimes Greek *hexa-* is used in Latin compounds, such as *hexadecimal*, due to [taboo avoidance](#) with the English word *sex*.
https://en.wikipedia.org/wiki/Numeral_prefix

Crucial fact:

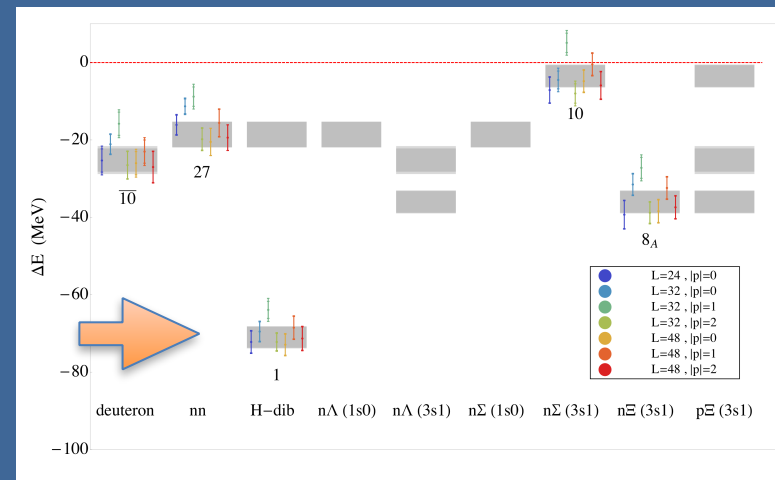
S does not couple to pions => much smaller than usual hadrons => hard to produce with hadrons

6-quark, $Q=0$, $B=2$
Spin-0, scalar
Flavor singlet
 $m \sim 1.7\text{-}2 \text{ GeV}$



Stable S?

- $\tau > \tau_{\text{Univ}}$
 - $M_S < 2 m_p + 2 m_e = 1877.6 \text{ MeV} \rightarrow \text{absolutely stable}$
 - $M_S > 2 m_p + 2 \text{ BE} = 1860 \text{ MeV} \rightarrow \text{nuclei absolutely stable}$
 - higher and lower mass may also work $\Gamma \sim G_F^4 \times (\text{wave function overlap})^2$
- **Lattice predicts binding (Beane+13)**
 - ($m_q = 850 \text{ MeV}$ so not realistic)
 - 80 MeV binding
- **Experiments exclude decaying S**
 \Rightarrow it must be **STABLE !** ;-)



Conditions on QCD Dark Matter

- ✓ $\tau_{\text{DM}} > \tau_{\text{Univ}}$, cold, neutral
- ✓ primordial nucleosynthesis
- ✓ Particle must not be already excluded
 - **accelerator searches**
 - exotic isotopes
 - DM searches
 - indirect impacts (heating planets, helioseismology,...)
 - stability of nuclei
 - equation of state of neutron stars (and their stability)
- ✓ **Correct relic density (for natural m_{DM} & $\sigma_{\text{f.o.}}$)**

Relic Abundance of *uds* Dark Matter

Quark-Gluon Plasma → Hadrons @~150 MeV

- Lattice QCD: crossover transition 160-140 MeV
 - $T > 160$ MeV: $u, \bar{u}, d, \bar{d}, s, \bar{s}$, gluons; NO vacuum condensates
 - $T < 140$ MeV: pions, kaons, p, \bar{p} , ...; $\langle q\bar{q} \rangle$ & $\langle GG \rangle$ condensates
 - Abundance relative to photons (for species in equilibrium):

Baryogenesis ⇒

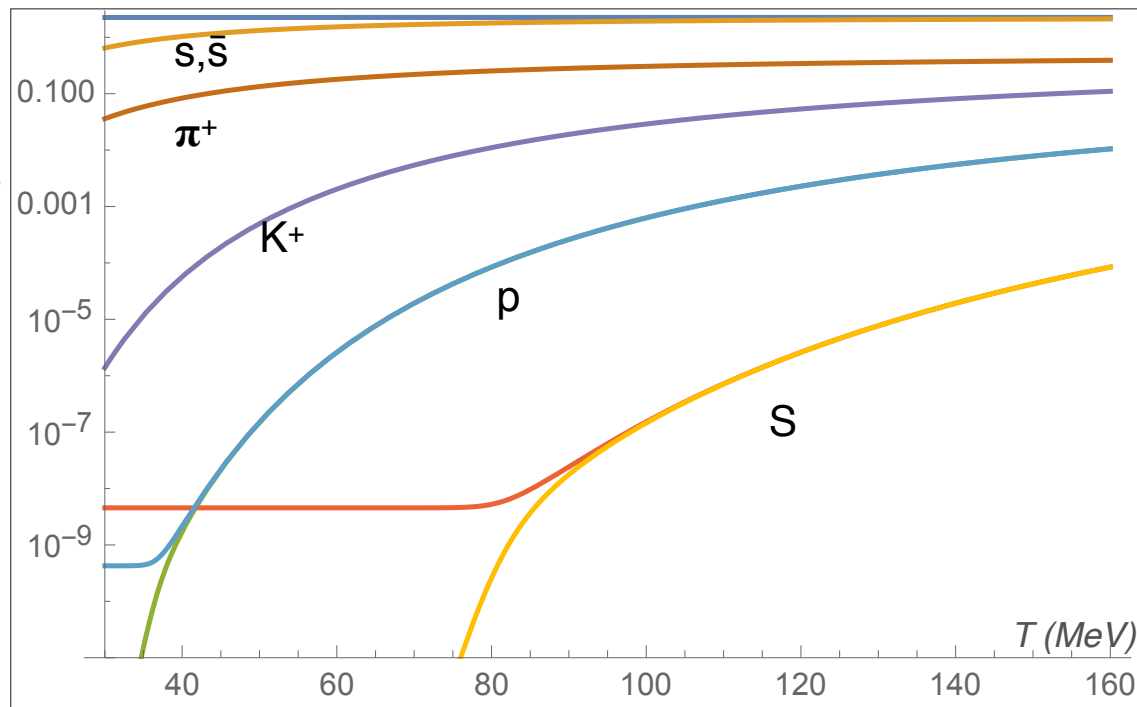
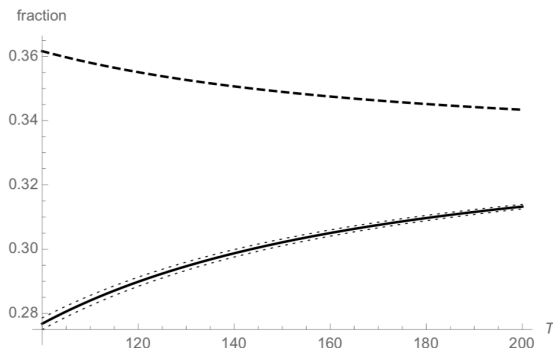
$$\eta_{\text{tot}} = \eta(1 + \Omega_{DM}/(y_b \Omega_b)) \approx 4.1 \times 10^{-9}$$

u,d,s ratio from q masses

$$m_u = 2.118(38) \text{ MeV}$$

$$m_d = 4.690(54) \text{ MeV}$$

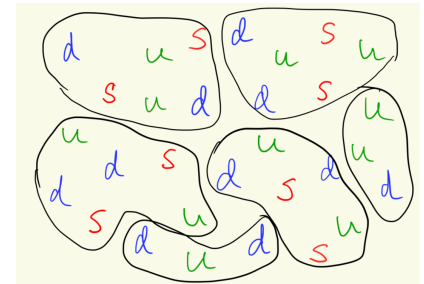
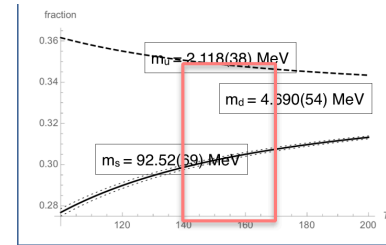
$$m_s = 92.52(69) \text{ MeV}$$



DM to (left-over) baryon ratio

- Hypothesis: DM has u,d,s in equal numbers
 - sexaquark DM, strange quark nuggets (Witten, 1984)*

$$\frac{\Omega_{DM}}{\Omega_b} = \frac{y_b \kappa_s 3f_s}{1 - \kappa_s 3f_s}$$



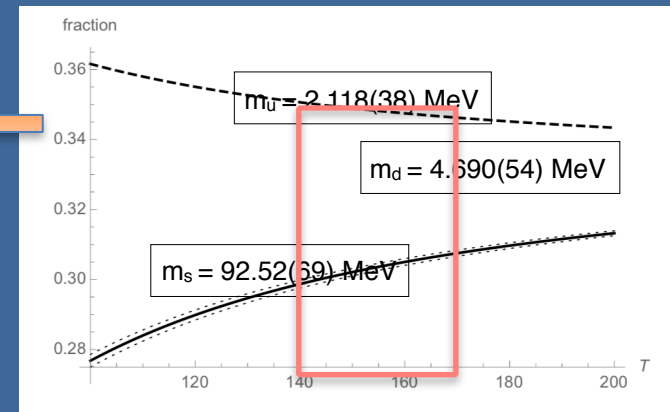
- $y_b = DM \text{ mass}/m_p$ (mass per unit baryon number)
- $f_s = \text{fraction of quarks that are } s$
- $3 f_s$ is number uds per unit baryon # — ranges from 0.964 to 0.948 as T decreases from 160 MeV to 140 MeV.
- κ_s is efficiency of uds \rightarrow DM (Boltzmann, from hyperon and S masses)

$$\kappa_s(m_S, T) = \frac{1}{1 + (r_{\Lambda, \Lambda} + r_{\Lambda, \Sigma} + 2r_{\Sigma, \Sigma} + 2r_{N, \Xi})} \quad r_{1,2} \equiv \exp[-(m_1 + m_2 - m_S)/T]$$

Ω_{DM} / Ω_b

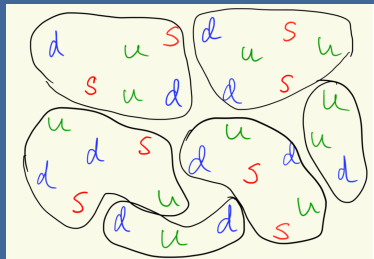
follows from **stat mech** , **quark masses** & temperature of **QGP-hadronization** transition

$$\frac{\Omega_{DM}}{\Omega_b} = \frac{m_S / (2m_p) y_b \kappa_s 3f_s}{1 - \kappa_s 3f_s}$$



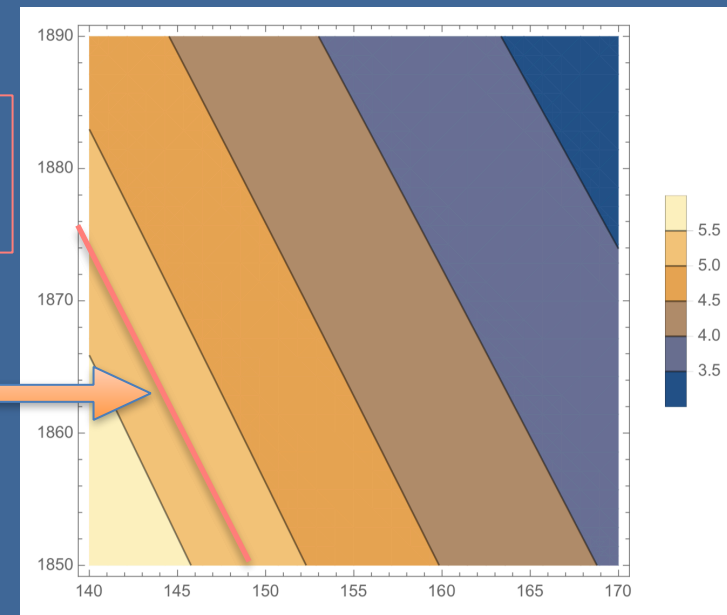
$$\kappa_s(m_S, T) = \frac{1}{1 + (r_{\Lambda, \Lambda} + r_{\Lambda, \Sigma} + 2r_{\Sigma, \Sigma} + 2r_{N, \Xi})}$$

$$r_{1,2} \equiv \exp[-(m_1 + m_2 - m_S)/T]$$



Prediction is both correct AND accurate to ~20% for entire range (uncertainties cancel)

$$\Omega_{DM} / \Omega_b = 5.3 \pm 0.1$$



Prediction also applies to strange quark nuggets...

S has not been discovered at accelerators because it is elusive

- **Many negative searches, but all are inapplicable.** They either:
 - looked for H-dibaryon through decays (but S is stable)
 - restricted to mass > 2 GeV (but $m_S < 2$ GeV)
 - required fast production in $S=-2$ hypernuclei (but small overlap with baryons)
- **Wavefunction overlap with baryons is very small.** Extremely rare fluctuation required for $S \leftrightarrow \Lambda\Lambda$; $S \leftrightarrow NN$ is G_F^4 smaller \Rightarrow
 - nuclei can be stable ($\tau > 10^{29}$ yr) even for $m_S > 2 m_p$
 - hard to produce in fixed target experiments
- **S is similar to** (much more copious) **neutrons**
- **Promising accelerator detection strategies**

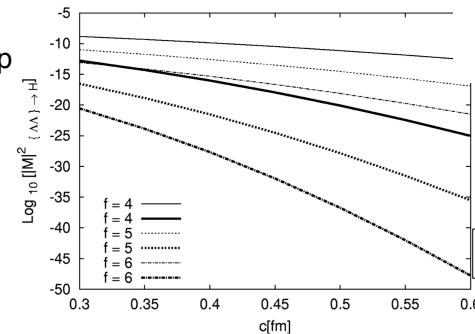
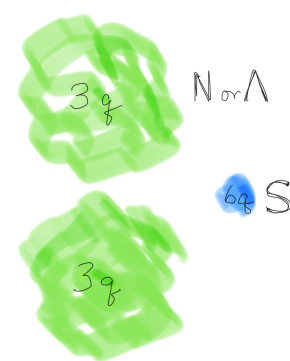


FIG. 1. Log_{10} of $|M|^2_{\Lambda\Lambda \rightarrow H}$ versus hard core radius in femtometers, for ratio $f=R_H/R_H$ and two values of the Isgur-Karl oscillator parameter: $\alpha_H=0.406$ GeV (thick lines) and $\alpha_H=0.221$ GeV (thin lines).

GRF+G.Zaharijas 2004

• Apparent lack of baryon number and strangeness conservation:

- $\Delta B = \pm 2$ with $\Delta S = \mp 2$

• Reconstruct missing mass, e.g.:

- $\Upsilon \rightarrow \Lambda \Lambda \bar{S}$ (+ pions) $M_S^2 = (p_Y - p_{\Lambda 1} - p_{\Lambda 2} - \sum p_{\pi_i})^2$

Experimental searches so far

Looking for Jaffe's H-dibaryon (same QN but assumed to be unstable and $r \sim 1$ fm)

- Require $M > 2$ GeV:
 - Gustafson+ FNAL 1976 : Beam-dump + tof *Limit on production of neutral stable strongly interacting particle with mass > 2 GeV.*
 - Carroll+ BNL 1978: No narrow missing mass peak above 2 GeV in $pp \rightarrow K K X$
- Require H-dibaryon decay:
 - Badier+ NA3 1986
 - Bernstein+ FNAL 1988: Limit on production of neutral with $10^{-8} < \tau < 2 \times 10^{-6}$ s
 - Belz+ BNL 1996: $H \rightarrow \Lambda n$ or Σn [c.f., issue raised by L. Littenberg]
 - Kim+ Belle 2013: no narrow resonance in $\Upsilon \rightarrow \Lambda p K$
- Limits from production in doubly-strange hypernuclei:
 - Ahn+ BNL 2001
 - Takahashi+ KEK 2001

Search for Six-Quark States

A. S. Carroll, I-H. Chiang, R. A. Johnson, T. F. Kycia, K. K. Ki,
L. S. Littenberg, and M. D. Marx
Brookhaven National Laboratory, Upton, New York 11973

and

R. Cester, R. C. Webb, and M. S. Witherell
Princeton University, Princeton, New Jersey 08540

(Received 26 July 1978)

We have searched the missing-mass spectrum of the reaction $pp \rightarrow K^+ K^+ X$ for a narrow six-quark resonance in the mass range $2.0\text{--}2.5$ GeV/ c^2 . No narrow structure was observed. Upper limits for the production cross section of such a state depend upon mass and vary from 30 to 130 nb.

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PHYSICAL REVIEW LETTERS

29 APRIL 1996

Search for the Weak Decay of an H Dibaryon

J. K. Ahn,^{1,2} R. D. Cousins,³ M. V. Diwan,^{5,1} M. Eckhauser,⁸ K. M. Ecklund,⁵ A. D. Hancock,³ V. L. Highland,^{5,4} C. Hoff,³ G. W. Hoffmann,⁷ G. M. Irwin,² J. R. Kane,² S. H. Kettell,^{5,1} J. R. Klein,^{4,4} Y. Kuang,² K. Lang,⁷ R. Martin,² M. May,² J. McDonough,⁷ W. R. Molzon,² P. J. Riley,⁷ J. L. Ritchie,⁷ A. J. Schwartz,² A. Trandafir,⁶ B. Ware,⁷ R. E. Welsh,⁸ S. N. White,¹ M. T. Witkowski,^{5,1} S. G. Wojcicki,¹ and S. Worn⁷

¹Brookhaven National Laboratory, Upton, New York 11973

²University of California, Irvine, California 92717

³University of California, Los Angeles, California 90024

⁴Princeton University, Princeton, New Jersey 08544

⁵Stanford University, Stanford, California 94309

⁶Temple University, Philadelphia, Pennsylvania 19122

⁷University of Texas at Austin, Austin, Texas 78712

⁸College of William and Mary, Williamsburg, Virginia 23187

(Received 8 December 1995)

We have searched for a neutral H dibaryon decaying via $H \rightarrow \Lambda n$ and $H \rightarrow \Sigma^0 n$. Our search has yielded two candidate events from which we set an upper limit on the H production cross section. Normalizing to the inclusive Λ production cross section, we find $(d\sigma_H/d\Omega)/(d\sigma_\Lambda/d\Omega) < 6.3 \times 10^{-6}$ at 90% C.L., for an H of mass ≈ 2.15 GeV/ c^2 . [S0031-9007(96)00050-6]

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PHYSICAL REVIEW LETTERS

24 SEPTEMBER 2001

Production of $\Lambda\Lambda^4\text{H}$ Hypernuclei

J. K. Ahn,^{1,2} S. Ajimura,¹⁰ H. Aikawa,⁷ B. Bassalleck,⁹ A. Berdoz,² D. Carman,² R. E. Chrien,¹ C. A. Davis,^{8,14} P. Eugenio,² H. Fischer,³ G. B. Franklin,² J. Franz,² T. Fukuda,¹² L. Gan,² H. Hotchi,¹² A. Ichikawa,⁷ K. Imai,⁷ S. H. Kahana,¹ P. Khavutov,² T. Kishimoto,¹⁰ P. Koran,² H. Kohri,¹⁰ A. Kourepin,⁵ K. Kubota,¹² M. Landry,⁸ M. May,¹ C. Meyer,² Z. Meziani,¹¹ S. Minami,¹⁰ T. Miyachi,¹² T. Nagae,² J. Nakano,¹² H. Oota,⁵ K. Paschke,² P. Pile,¹ M. Prokhabatlov,⁶ B. P. Quinn,² V. Rasin,⁶ A. Rusek,¹ H. Schmitt,³ R. A. Schumacher,² M. Sekimoto,² K. Shileev,⁶ Y. Shimizu,¹⁰ R. Sutter,¹ T. Tamagawa,¹² L. Tang,⁴ K. Tanida,¹² K. Yamamoto,² and L. Yuan⁴

¹Brookhaven National Laboratory, Upton, New York 11973

²Department of Physics, Carnegie Mellon University, Pittsburgh, Pennsylvania 15213

³Department of Physics, University of Freiburg, D-79104 Freiburg, Germany

⁴Department of Physics, Hampton University, Hampton, Virginia 23668

⁵High Energy Accelerator Research Organization (KEK), Tsukuba, Ibaraki 305-0801, Japan

⁶Institute for Nuclear Research (INR), Moscow 117312, Russia

⁷Department of Physics, Kyoto University, Sakyo-Ku, Kyoto 606-8502, Japan

⁸Department of Physics and Astronomy, University of Manitoba, Winnipeg, MB, Canada R3T 2N2

⁹Department of Physics and Astronomy, University of New Mexico, Albuquerque, New Mexico 87131

¹⁰Department of Physics, Osaka University, Toyonaka, Osaka 560-0043, Japan

¹¹Department of Physics, Temple University, Philadelphia, Pennsylvania 19122

¹²Department of Physics, University of Tokyo, Tokyo 113-0033, Japan

¹³Department of Physics, Pusan National University, Pusan 609-735, Korea

¹⁴TRIUMF, 4004 Wesbrook Mall, Vancouver, BC, Canada V6T 2A3

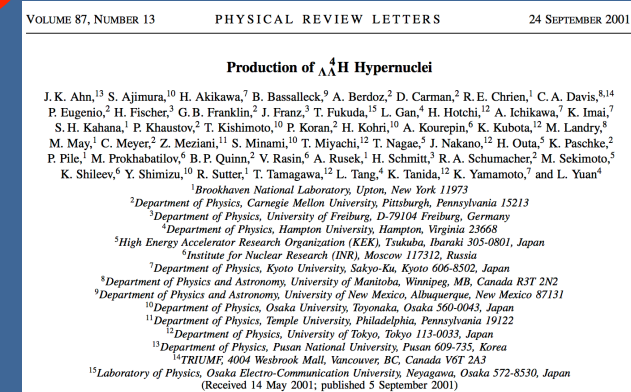
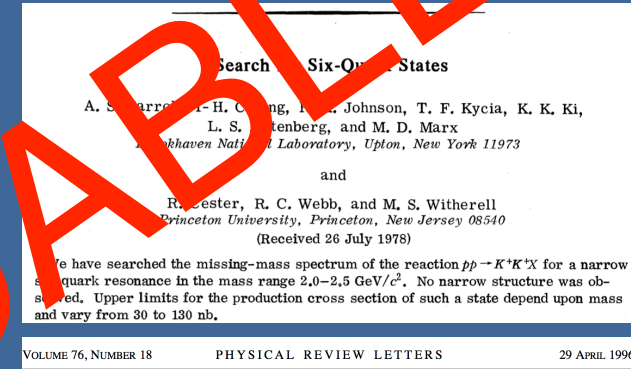
¹⁵Laboratory of Physics, Osaka Electro-Communication University, Neyagawa, Osaka 572-8530, Japan

(Received 14 May 2001; published 5 September 2001)

An experiment demonstrating the production of double- Λ hypernuclei in (K^-, K^+) reactions on ^9Be was carried out at the D6 line in the JBNL alternating-gradient synchrotron. The technique was the observation of pions produced in sequential mesonic weak decay, each pion associated with one unit of strangeness change. The results indicate the production of a significant number of the double hypernucleus $\Lambda\Lambda^4\text{H}$ and the twin hypernuclei $\Lambda^4\text{H}$ and $\Lambda^3\text{H}$. The relevant decay chains are discussed and a simple model of the production mechanism is presented. An implication of this experiment is that the existence of an $S = -2$ dibaryon more than a few MeV below the $\Lambda\Lambda$ mass is unlikely.

Experimental Searches

- Require $M > 2 \text{ GeV}$:
 - Gufstafson+ FNAL1976 : Beam-dump + tof *Limit on production of neutral stable strongly interacting particle with mass $> 2 \text{ GeV}$.*
 - Carroll+ BNL 1978: No narrow missing mass peak above 2 GeV in $pp \rightarrow K K X$
- Require H-dibaryon decay:
 - Badier+ NA3 1986
 - Bernstein+ FNAL 1988: Limit on production of neutral with $10^{-8} < \tau < 2 \times 10^{-6} \text{ s}$
 - Belz+ BNL 1996: $H \rightarrow \Lambda \bar{\Lambda}$ or $\Sigma \bar{\Sigma}$ [c.f., issue raised by L. Littenberg]
 - Kim+ Belle 2013: no narrow resonance in $\Upsilon \rightarrow \Lambda \bar{\Lambda} K$
- Limits from production in doubly-strange hypernuclei:
 - Ahn+ BNL 2001
 - Takanashi+ KEK 2001



Cosmology & structure formation

- **DM-baryon interaction: momentum transfer => *slight drag on DM during structure formation***
 - Dvorkin, Blum, Kamionkowski (2014), Gluscevic+Boddy (2017), Xu+18
 - **Ly-alpha forest: $\sigma < \sim 10$ mb if v-indept — no problem for S**
 - Buen-Abad, Marques-Tavares, Schmalz (2015):
 - **momentum transfer helps reconcile H_0 & σ_8**
 - Boring or an opportunity? To be determined...
- **S-S self interactions + S-baryon interactions:**
 - could have similar benefits as Self Interacting DM
 - core-cusp, “too-big-to-fail” & missing sub-halos problems.

Galaxies & Clusters

DM-gas scattering provides a source of heating, useful for

- Milky Way's extended hot gas halo — 2×10^6 K
- Quenching star formation
- Avoiding “cooling flow catastrophe” in X-ray clusters

Key points to take home

- **There may a tightly bound 6-quark state $S = uuddss$**
 - Unique, symmetric structure \Rightarrow other hadrons don't provide guidance
 - mass is not driven by chiral symmetry breaking (unlike baryons)
 - constituent quark model probably completely misleading
 - **If $M_S < 2 m_p + 2 m_e$, S is absolutely stable**
- **If S is stable, its an excellent Dark Matter candidate**
 - Relic abundance is natural. **EXPLAINS 7Li Discrepancy in BBN and Dark Matter to baryon ratio**
 - Usual WIMP detection strategy isn't applicable.
 - May reconcile tension in H_0 & σ_8 and explain astrophysics puzzles ("quenching", core-cusp, DM rotation curves...)
- ***S may be waiting to be discovered in existing Υ -decays or LHC experiments... mass can be accurately measured in Υ -decay exclusive final states.***
- ***SDM will be challenging to detect, but not impossible. Astrophysical and cosmological effects may allow it to be constrained, excluded or confirmed.***

Backup Slides

Sexaquark Discovery Strategy

- Apparent lack of B and S conservation:

- $\Delta B = \pm 2 \quad + \quad \Delta S = \mp 2$

- Reconstruct missing mass, e.g.:

- $\Upsilon \rightarrow \Lambda \Lambda \bar{S}$ (+ pions) $M_S^2 = (p_\Upsilon - p_{\Lambda 1} - p_{\Lambda 2} - \sum p_{\pi i})^2$

- LHC: $\bar{S} + N \rightarrow \bar{\Lambda} K^+$ $M_S^2 = (p_{\bar{\Lambda}} + p_K - p_N)^2$

- Snolab nuclei: $pn \rightarrow S e^+ \nu$ $G_F^4 \quad \tau > 10^{+29} \text{ yr}$

$$\Upsilon \rightarrow \Lambda \Lambda \bar{S} \text{ \& } \bar{\Lambda} \bar{\Lambda} S$$

(+ pions)

- Υ is **localized** source of ggg

\Rightarrow production of S is (relatively) enhanced

- Many $\times 10^8$ events collected (CLEO, Babar, Belle)

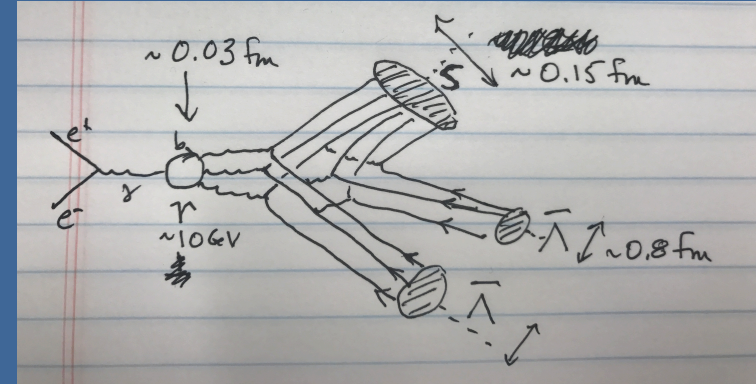
- detectors pretty hermetic, have good mass resolution, $O(10 \text{ MeV})$
- Λ decays quickly to $p\pi$ so easy to ID. $c\tau = 8 \text{ cm}$

- Can MEASURE m_S via missing mass

- **Very clean**

- Main bkg is $K_S K_S K_L K_L$ (+ pions)
 - K_S 's mis-ID'd as Λ 's and K_L 's escaping before decay : *negligible for Belle*
 - rare and can model accurately
 - $K_S K_S K_L K_L$ (+ pions) *is measurable*, from $K^+ K^+ K^- K^-$ (+ pions)
- “Conspiracy” of missed particles producing $\Delta B = \pm 2$, $\Delta S = \mp 2$ very hard

Background does not have narrow peak in missing mass!



LHC

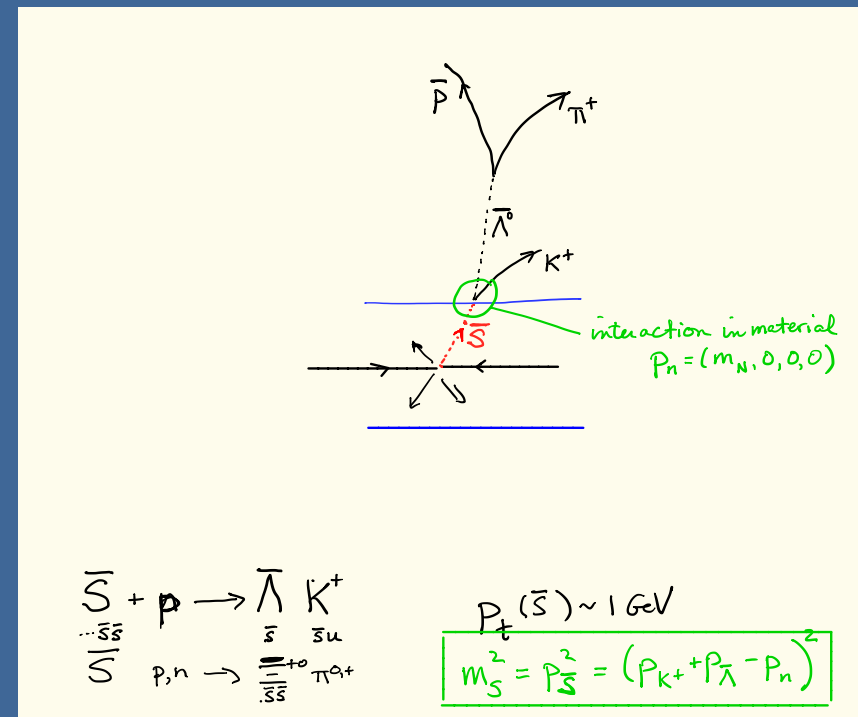
- Hadronic collisions: low production rate due to small wfn overlap
- Find a needle in a haystack (10^{11} recorded events; potential for trigger >>> more)
- Statistical examination of correlation between

$$\Delta B = \pm 2, \Delta S = \mp 2$$

- **\bar{S} annihilation in tracker, tag by**

$$\bar{E}^{+,0} \rightarrow \bar{\Lambda} \pi^{+,0} \quad (c\tau = 5\gamma \text{ cm}) \quad \bar{\Lambda} \rightarrow \bar{p} \pi^+$$

$$\text{or } \bar{\Lambda} K^+$$



- 2nd exponential in scattering-length distribution of n-like interactions, due to S