

# *Light Mediators in B Anomalies*

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July 2-5, 2018

*Flasy 2018*

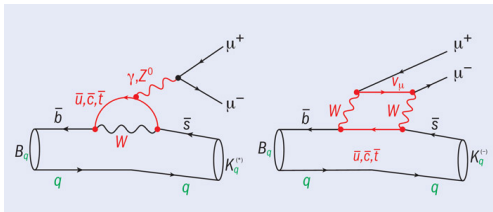
# Outline of Talk

- In recent times there have been some anomalies in  $B$  decays that indicate lepton non-universal new physics.
- These are in semileptonic  $b \rightarrow c\tau\bar{\nu}_\tau$  transitions:  $R_{D^{(*)}}$  puzzle.
- These are in semileptonic  $b \rightarrow s\ell^+\ell^-$  ( $\ell = \mu, e$ ) transitions:  $R_K, R_{K^{(*)}}$  puzzles. BR of  $b \rightarrow s\mu^+\mu^-$  modes are lower and also deviation in  $P'_5$  angular observable.
- These all indicate LUV New Physics.

# Plan of the Talk

- Focus on the neutral current anomalies:  $b \rightarrow s\mu^+\mu^-$  decays and  $R_K$  and  $R_{K^{(*)}}$  puzzles.
- NP explanation in terms of heavy mediators. Can light mediators explain the anomalies?
- Low  $q^2$  measurement of  $R_{K^{(*)}}$  difficult to understand with heavy new physics  $\sim$  TeV.
- Will consider light new physics with MeV scale mediators .

# $b \rightarrow s\mu^+\mu^-$ Anomaly



$$H_{\text{eff}}(b \rightarrow s\ell\bar{\ell}) = -\frac{\alpha G_F}{\sqrt{2}\pi} V_{tb} V_{ts}^* [C_9 (\bar{s}_L \gamma^\mu b_L) (\bar{\ell} \gamma_\mu \ell) + C_{10} (\bar{s}_L \gamma^\mu b_L) (\bar{\ell} \gamma_\mu \gamma^5 \ell)] ,$$

$$H_{\text{eff}}(b \rightarrow s\nu\bar{\nu}) = -\frac{\alpha G_F}{\sqrt{2}\pi} V_{tb} V_{ts}^* C_L (\bar{s}_L \gamma^\mu b_L) (\bar{\nu} \gamma_\mu (1 - \gamma^5) \nu) ,$$

$$H_{\text{eff}}(b \rightarrow s\gamma^*) = C_7 \frac{e}{16\pi^2} [\bar{s} \sigma_{\mu\nu} (m_s P_L + m_b P_R) b] F^{\mu\nu}$$

# $R_K$ puzzle, Ratios of $b \rightarrow s\mu^+\mu^-$ and $b \rightarrow se^+e^-$ . (Clean), 1708.02515

$$R_K \equiv \mathcal{B}(B^+ \rightarrow K^+\mu^+\mu^-)/\mathcal{B}(B^+ \rightarrow K^+e^+e^-)$$

$$R_K^{\text{expt}} = 0.745^{+0.090}_{-0.074} (\text{stat}) \pm 0.036 (\text{syst})$$

$$1 \leq q^2 \leq 6.0 \text{ GeV}^2$$

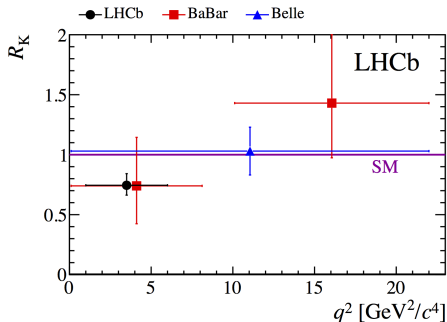
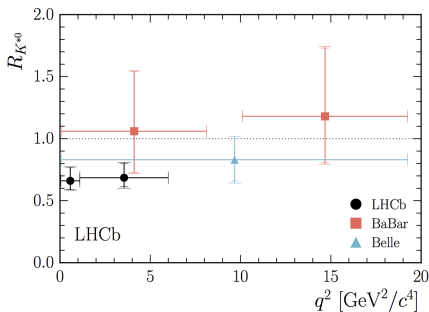
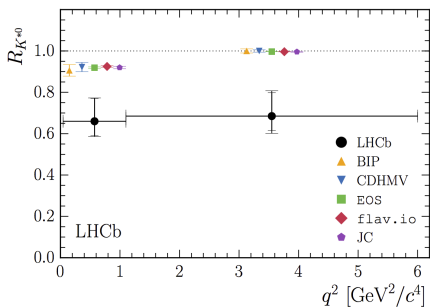


Figure: Comparison of the measurements of  $R_K$  from LHCb (black dots), BaBar (red squares) and Belle (blue triangles) with the SM expectation (purple line).



**Figure:** Comparison of the measurements of  $R_{K^*}$  from LHCb with (left) SM predictions and (right) BaBar and Belle.

$$R_{K^*}^{\text{expt}} = \begin{cases} 0.660_{-0.070}^{+0.110} \text{ (stat)} \pm 0.024 \text{ (syst)} & 0.045 \leq q^2 \leq 1.1 \text{ GeV}^2, \\ 0.685_{-0.069}^{+0.113} \text{ (stat)} \pm 0.047 \text{ (syst)} & 1.1 \leq q^2 \leq 6.0 \text{ GeV}^2. \end{cases}$$

$R_K$  and  $R_{K^*}$  in the SM very close to 1 in the central bin and  
 $R_{K^*} \sim 0.92$  in the low bin.

## $R_{K^{(*)}}$ puzzle: Other Experiment

- Measurements from Belle finds difference in same  $q^2$  bin as LHCb

$$Q_5 = P'_5(\mu\mu) - P'_5(ee)$$

( 1612.05014). Large errors.

- Low  $q^2$   $R_{K^{(*)}}$  measurement dominated by photon pole which is not LUV. Hence measurement difficult to understand with heavy NP.

## Recent Fits after $R_{K^{(*)}}$

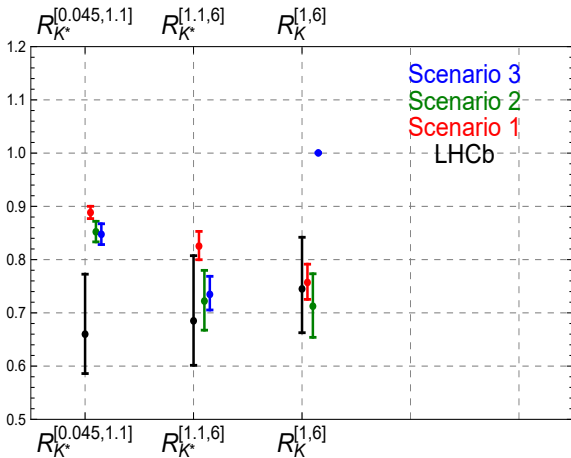
Fits by many authors( 1704.05435, 1704.05438, 1704.05444, 1705.05446, 1704.05447....) to all  $b \rightarrow s\ell\ell$  observables: arXiv:1704.07397 : Alok et.al.

Scenario	WC	pull
(I) $\Delta C_9^{\mu\mu}(\text{NP})$	$-1.25 \pm 0.19$	5.9
(II) $\Delta C_9^{\mu\mu}(\text{NP}) = -\Delta C_{10}^{\mu\mu}(\text{NP})$	$-0.68 \pm 0.12$	5.9
(III) $\Delta C_9^{\mu\mu}(\text{NP}) = -\Delta C_9^{\prime\mu\mu}(\text{NP})$	$-1.11 \pm 0.17$	5.6

Here NP effects only the muons.



# Motivating light $Z'$ - not the only motivation.



Question: Can we explain the  $R_K$  and  $R_{K^*}$  measurements in all bins with light mediators. I will focus on  $M < 200$  MeV mediators.

# Scope of the Model

Try to explain  $R_K$  and  $R_{K^{(*)}}$  in "all" bins.

( 1705.08423, 1704.07397, 1702.01099). Harder- very constraining.

Try to explain  $R_{K^{(*)}}$  in "only" the low  $q^2$  bin. "Easier" ( 1711.07494).

Possibilities: Dark photon, dark Higgs, ALP e.t.c.

## Light $Z'$ $R_K$ and $(g - 2)_\mu$ ( Datta, Marfatia, Liao)

Focus on high  $q^2$  bins only,  $q^2 > 1\text{GeV}^2$ .

The most general form of the  $bsZ'$  vertex with vector type coupling is

$$H_{bsZ'} = F(q^2)\bar{s}\gamma^\mu P_L b Z'_\mu,$$

In case  $F(q^2) \neq 1$ , it can be expanded as expanded as

$$F(q^2) = a_{bs} + g_{bs} \frac{q^2}{m_B^2} + \dots,$$

when momentum transfer  $q^2 \ll m_B^2$ .

We assume  $Z'$  coupling to electrons is suppressed and  $m_{Z'} < 2m_\mu$ . There are negative searches bump in  $X \rightarrow \mu^+ \mu^-$  in  $B \rightarrow KX$  and then  $X \rightarrow \mu^+ \mu^-$ .

## $b \rightarrow sZ'$ Constant Form Factor $F(q^2) = 1$

- Only off-shell contribution :  $B \rightarrow KZ'^*(\rightarrow \mu^+\mu^-)$  . From  $R_K$

$$g_{bs}g_{\mu\mu} \sim 10^{-9}; \quad M_{Z'} \sim 100\text{MeV}..$$

- There is contribution to  $B_s$  mixing which strongly constrains

$$g_{bs} \sim 10^{-7} - 10^{-8}$$

$$D_{\mu\nu} \sim \left[ g_{\mu\nu} - \frac{q_\mu q_\nu}{m_X^2} \right].$$

- $SU(2)_L$  invariance  $\Rightarrow$  coupling to  $(\nu, \ell)_L$ . If  $Z'$  couples to neutrinos then

$$BR[B \rightarrow K\nu\bar{\nu}] = BR[B \rightarrow KZ'] \times BR[Z' \rightarrow \nu\bar{\nu}].$$

There is a longitudinal polarization enhancement  $\sim \frac{E_{Z'}}{m_{Z'}} \Rightarrow g_{bs} \sim 10^{-9}$ .

- $g_{\mu\mu} \sim 1 \Rightarrow$  problem with  $(g-2)_\mu$ .

$$F(q^2) \neq 1$$

This constraint rules out  $F(q^2) = 1$  and forces  $a_{bs} \sim 0$ , so that

$$H_{bsZ'} = g_{bs} \frac{q^2}{m_B^2} \bar{s} \gamma^\mu P_L b Z'_\mu \quad (H_{bsZ'} \sim \bar{s} \gamma^\mu b \partial^\nu Z'_{\mu\nu}),$$

for  $q^2 \ll m_B^2$ .

- $B_s$  mixing constrains  $F(q^2 = m_B^2)$ .
- $B \rightarrow K \nu \bar{\nu} \Rightarrow g_{bs} \sim 10^{-5} \Rightarrow g_{\mu\mu} \sim 10^{-4}$ .

$$\frac{q^2}{q^2 - m_{Z'}^2} \rightarrow 1,$$

where  $q^2 \gg m_{Z'}^2$ . So this low mass NP appears as  $\Delta C_9$  from heavy NP. So "all" observables,  $R_K$  and angular measurements are explained.

But  $R_{K^{(*)}}$  in low  $q^2$  bin cannot be explained.

# Origin of the Form Factor: Charm Loop effects: Ciuchini et.al. 1512.07157

$b \rightarrow s \mu^+ \mu^-$  can also receive corrections from non-leptonic operators

$$M = \langle K^* \mu^+ \mu^- | \bar{s} b \bar{q} q | B \rangle$$

$\bar{q} q \rightarrow \gamma^* \rightarrow \mu^+ \mu^-$ . There can also be resonant contributions

$\bar{q} q \rightarrow J/\psi \rightarrow \mu^+ \mu^-$ .

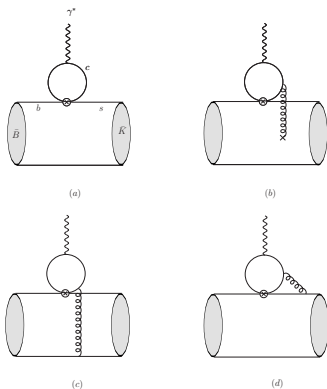
This long distance dominated contribution cannot be calculated from first principle. There are factorization theorem for small  $q^2$  in leading order in  $m_{heavy}$ . But sub-leading corrections are not known.

$$M = \bar{s} \gamma_\mu P_L b \left[ \frac{H(q^2)}{q^2} \right] \bar{\mu} \gamma^\mu \mu$$

$$H(q^2) = a + b \frac{q^2}{m_B^2} \dots$$

$H(q^2) \sim q^2$  and you reproduce  $\Delta C_9$  from pure SM hadronic effect.

# Hadronic Uncertainties: Charm Loop effects: eprint: 1006.4945



Even away from the resonance region there are diagrams with the soft-gluon are suppressed by  $\frac{\Lambda_{QCD}^2}{(q^2 - (2m_c)^2)} \sim \frac{\Lambda_{QCD}^2}{(2m_c)^2}$  when  $q^2 \ll 4m_c^2$ . These are the unknown power corrections.

# Four quark operators, Datta, Duraisamy, Ghosh, 1310.1937

Some NP through new particle exchange generates the following operators

$$\mathcal{H}_{\text{eff}}^{\text{NP}} \sim \frac{\mathcal{A}_1}{\Lambda^2} \bar{b}' (1 + \gamma_5) b' \bar{b}' (1 - \gamma_5) b' + \frac{\mathcal{A}_1}{\Lambda^2} \bar{b}' (1 - \gamma_5) b' \bar{b}' (1 + \gamma_5) b' ,$$

Go from gauge to mass basis and

$$\begin{aligned} \mathcal{H}_{\text{eff}}^{\text{NP}} &= -\frac{\mathcal{G}_1}{\Lambda^2} [\bar{s}(1 - \gamma^5)b] [\bar{b}(1 + \gamma^5)b] \\ &\quad -\frac{\mathcal{G}_2}{\Lambda^2} [\bar{s}(1 + \gamma^5)b] [\bar{b}(1 - \gamma^5)b] + \text{h.c.} \end{aligned}$$



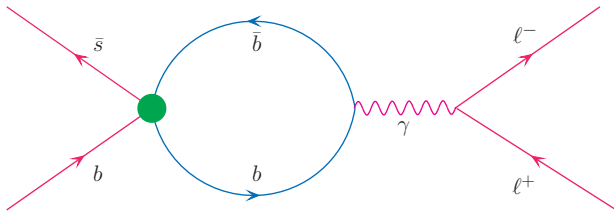
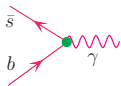


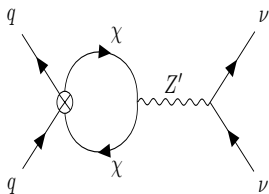
Figure:



$$= -\sqrt{4\pi\alpha_{em}}e_b F(q^2)\bar{s} [\mathcal{G}_1\mathcal{R}_1^\mu + \mathcal{G}_2\mathcal{R}_2^\mu] b A_\mu$$

where  $F(q^2) \sim \frac{q^2}{m_\lambda^2}$ . The  $q^2$  is cancelled by the photon propagator to give  $\Delta C_9$ .

- Since  $A_\mu$  couples to electron and muons equally. This predicts same NP in electron and muon decays for  $q^2 > 4m_\mu^2$ .
- To generate LUV we have to replace  $A_\mu$  with a different boson ( $Z'_\mu$ ) which has LUV interactions.



$$\mathcal{L} = \frac{g}{\Lambda^2} \bar{q}_{iL} Y_{ij} \gamma^\mu q_{jL} \bar{\chi}_L \gamma_\mu \chi + g_\chi \bar{\chi} \gamma_\rho \chi Z'^\rho + g_{\ell\bar{\ell}} [A_L \gamma_\rho (1 - \gamma_5) + A_R \gamma_\rho (1 + \gamma_5)] \ell Z'^\rho,$$

$\chi$  loop produces a  $\bar{q}_i q_j Z'$  coupling that goes a  $\frac{q^2}{\Lambda^2}$ . We take  $m_\chi \sim m_b$ .

## Summary: Explain $R_K$ , $R_{K(*)}$ in all bins

- Tree level  $bsZ'$  for MeV  $Z'$  ruled out.
- Form Factor FCNC coupling of  $Z'$  is allowed with  $FF \sim q^2$  for  $q^2 \ll m_B^2$ . But still need to explain low  $q^2$ ,  $R_{K(*)}$  measurement. Other observables can be explained.
- Scalar  $S$  coupling to muons does not work :  $R_K$  and  $R_{K(*)}$  increased from SM values. No interference with the SM.
- Scalar and vector coupling to electrons can work for all bins with  $FF \sim q^2$  for  $q^2 \ll m_B^2$  (1705.08423).

# Light Scalars and $Z'$ coupling to electrons and muons:

Datta, Marfatia, Jacky Kumar, Liao

- Still need to explain low  $q^2$ ,  $R_{K^{(*)}}$  measurement.
- $S$  coupling to muons does not work:  $R_K$  and  $R_{K^{(*)}}$  increased from SM values.
- $Z'$  couplings to muons do not work.
- We have to invoke NP coupling to electrons.  $S(Z') \rightarrow e^+e^-$ .
- We choose the mass of the new boson  $\sim 25$  MeV to avoid branching ratio constraints. ( All measurements have  $m_{ee}$  above 30 MeV.)

# Electron couplings are constrained

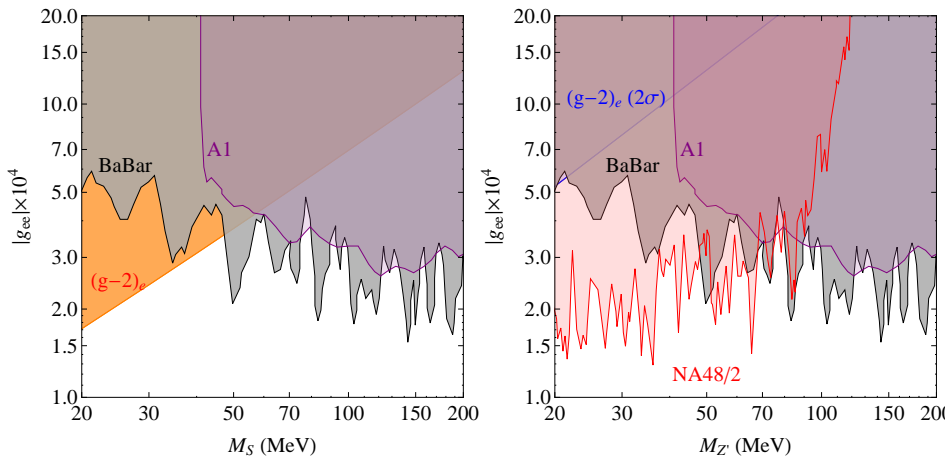


Figure:

## Two Body Problem.

- Main problem is from two body decays:  $B \rightarrow KX$  and  $X \rightarrow e^+ e^-$ .
- The  $B$  width is calculated with uncertainty of about 10%.
- Requiring  $\Gamma[B \rightarrow KX] \leq 1\% \Gamma_B$  forces  $g_{bs}$  to be  $10^{-8} - 10^{-9}$ .
- $g_{ee} \leq 10^{-3}$  and so  $g_{bs}g_{ee} \sim 10^{-11} - 10^{-12}$  and so too small for  $R_{K(*)}$ .
- Forced into  $sbX$  Form factor to go as  $F(q^2) \sim q^2$ .

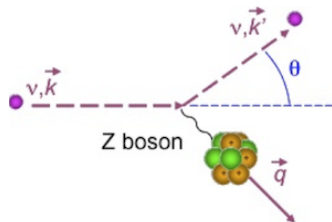
**Table:** The experimental results for various  $b \rightarrow se^+e^-$  observables, along with predictions for the SM and four new physics cases. The light mediator mass is 25 MeV,  $F(q^2) \neq 1$  and  $a_{bs} = 0$ .

	$R_{K[0.045-1.0]}$	$\mathcal{B}(B \rightarrow Ke^+e^-)_{[1.0-6.0]}$	$\mathcal{B}(B \rightarrow X_s e^+e^-)_{[1.0-6.0]}$	$\mathcal{B}(B^0 \rightarrow K^{*0}e^+e^-)_{[0.032-1]}$
Experimental results	-	$(1.56 \pm 0.18) \times 10^{-7}$	$(1.93 \pm 0.55) \times 10^{-6}$	$(3.1 \pm 0.9) \times 10^{-7}$
Standard model predictions	0.98	$1.69 \times 10^{-7}$	$1.74 \times 10^{-6}$	$2.6 \times 10^{-7}$
Light scalar $g_{bs}^S g_{ee}^S = 2.7 \times 10^{-8}$ , $g_{bs}'^S g_{ee}'^S = -15.5 \times 10^{-8}$	0.93	$2.5 \times 10^{-7}$	$2.3 \times 10^{-6}$	$2.6 \times 10^{-7}$
Light vector $g_{bs} g_{ee} = -3.9 \times 10^{-8}$ , $g_{bs}' g_{ee}' = 1.4 \times 10^{-8}$	0.73	$2.4 \times 10^{-7}$	$2.6 \times 10^{-6}$	$2.8 \times 10^{-7}$
Light vector, $g_{bs}' = 0$ $g_{bs} g_{ee} = -3.2 \times 10^{-8}$ , $g_{bs} g_{ee}' = 0.4 \times 10^{-8}$	0.66	$2.7 \times 10^{-7}$	$2.5 \times 10^{-6}$	$2.7 \times 10^{-7}$
Light vector, $g_{bs} = 0$ $g_{bs}' g_{ee} = 4.6 \times 10^{-8}$ , $g_{bs}' g_{ee}' = 2.0 \times 10^{-8}$	1.04	$2.4 \times 10^{-7}$	$2.5 \times 10^{-6}$	$2.8 \times 10^{-7}$

$R_K$  measurement in low  $q^2$  bin can help probe various low mass mediator models.

# Coherent Scattering( Datta, Dutta, Liao Marfatia, Strigari)

If light mediators couple to charged leptons then they couple to neutrinos also simply by  $SU(2)_L$  invariance. Can be probed in coherent scattering.

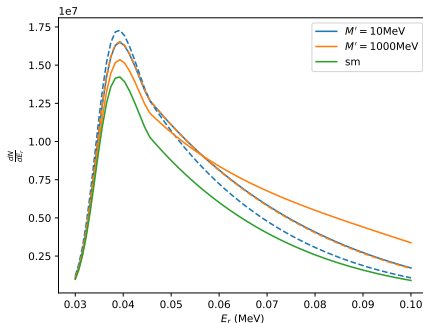


A  $q^2$  dependent form factor effect can be seen in the recoil spectrum.



# Coherent Scattering

If light mediators couple to charged leptons then they couple to neutrinos also simply by  $SU(2)_L$  invariance. Can be probed in coherent scattering.



A  $q^2$  dependent form factor effect can be seen in the recoil spectrum.

## Explaining only the low $q^2$ bin 1711.07494

In this case, assume a resonance near the low  $q^2$  bin and then

$$BR[B \rightarrow K^* ll] = BR[B \rightarrow K^* ll]_{SM} + BR[B \rightarrow K^* X] \times BR[X \rightarrow ll]$$

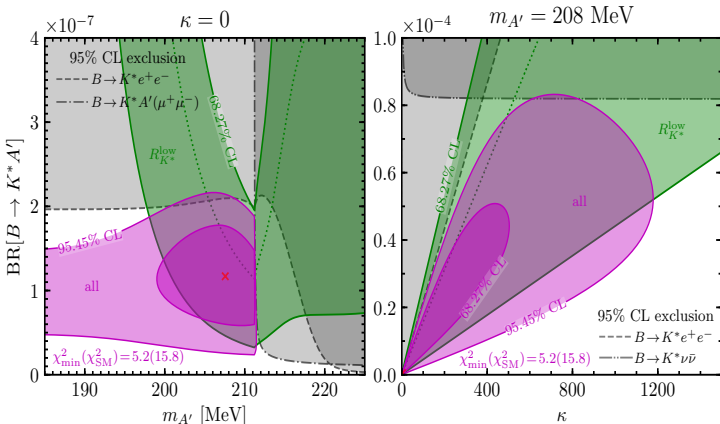
$X$  does not need to have LUV couplings. For instance if  $m_X < 2m_\mu$  then only  $B \rightarrow K^* e^+ e^-$  is affected. So in fact  $X$  can have lepton universal coupling and can be a dark photon for example.

A dark photon with mass just below the  $2m_\mu$  threshold can explain the low  $q^2$   $R_{K^{(*)}}$  measurement.

# Explaining only the low $q^2$ bin 1711.07494

Only interested in one bin. Dark photon with  $A'$  below the  $2\mu$  mass. LUV is just a kinematic effect in low  $q^2$   $R_{K^*}$ .

Dark photon



# Explaining only the low $q^2$ bin Feng, Datta, Kamali

Familon model/ ALP:

$$\mathcal{L}_{Q'Q'} = \frac{g_Q}{F_Q} \bar{Q}'_\alpha \gamma^\mu P_L T_{\alpha\beta}^a Q'_\beta \partial_\mu f^a ,$$

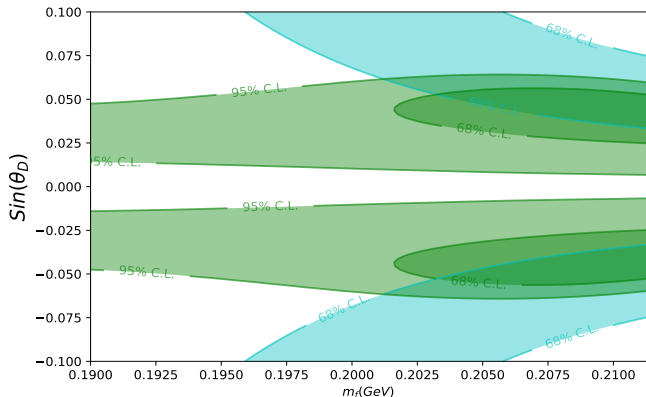
where  $Q'_L = (u_L, d_L)^T$  are the left-handed quark doublets. The quarks are in the gauge basis and are indicated by primes. For the lepton couplings we write,

$$\mathcal{L}_{L'L'} = \frac{g_L}{F_L} \bar{L}'_\alpha \gamma^\mu P_L S_{\alpha\beta}^a L'_\beta \partial_\mu f^a ,$$

where  $L'_L = (\nu_L, \ell_L)^T$  are the left-handed lepton doublets. The leptons are in the gauge basis and are indicated by primes. Note we do not assume  $F_L$  and  $F_Q$  are the same.

# Familon

$U(1)$  Family Symmetry. Coupling  $\sim$  mass. Fit prefers  $F_Q \gg F_L$ .



## $(g - 2)_\mu$ problem

- LHCb signal requires The  $K^{*0}$  meson and  $\ell^+\ell^-$  pair are required to originate from a common vertex in order to form a  $B$  candidate.
- This gives a lower bound on the width of the particle which gives  $\frac{g}{F_L}$ .

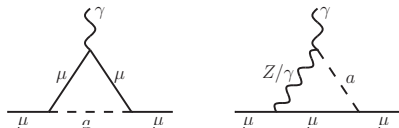
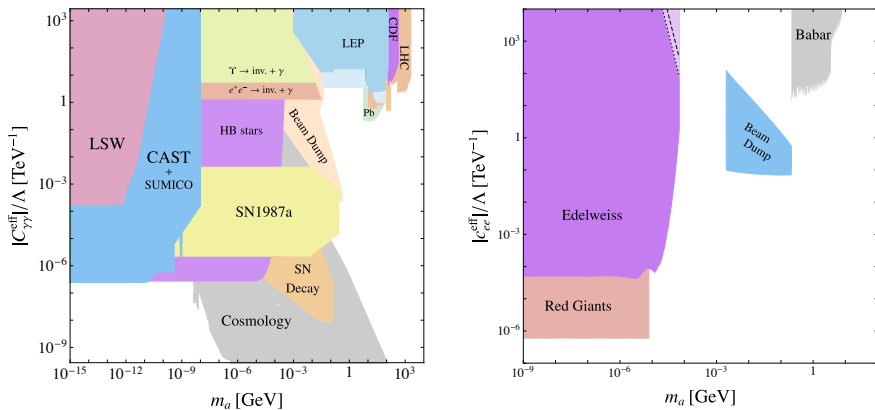


Figure: One-loop diagrams contributing to the anomalous magnetic moment of the muon.

- Constraint on  $\frac{g}{F_L} \Rightarrow$  too large ( and opposite sign) contribution to  $(g - 2)_\mu$ .
- This suggest other modes to  $\gamma\gamma$  or invisible have to be opened up.



**Figure:** Existing constraints on the ALP–photon (left) and ALP–electron coupling (right) derived from a variety of particle physics, astro-particle physics and cosmological observations. Several of these bounds are model dependent. The BaBar constraint in the right-hand plot assumes  $c_{\mu\mu} \approx c_{ee}$ .

# Conclusions

- Several anomalies in  $B$  decays indicating lepton non-universal interactions.
- Not all measurements can be understood with heavy new physics.
- We considered solution of the puzzles with light new physics.
- Light NP is highly constrained but some scenarios are viable. There may be some signal in low  $q^2$   $R_K$  measurement or in neutrino scattering.