



# Discrete Dark Matter and the reactor mixing angle

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Mexico



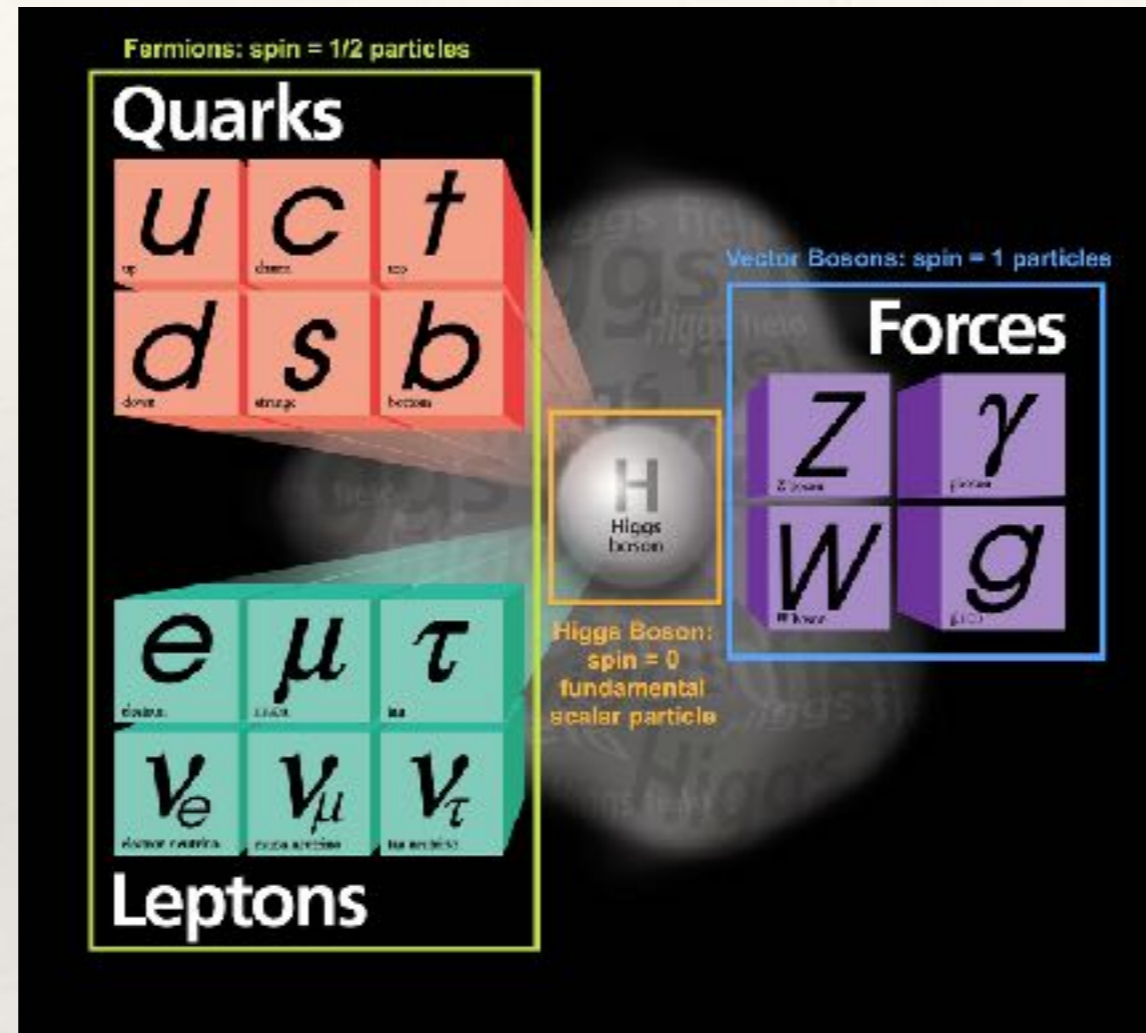
Flasy 2018, University of Basel

# Plan of the talk

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- ❖ Neutrino oscillation and masses
- ❖ Dark Matter Stability
  - DDM and texture zeros
- ❖ Summary and conclusions

# The Standard Model



EWSB  
mechanism

3 generations

neutrino oscillations  
(massive neutrinos)

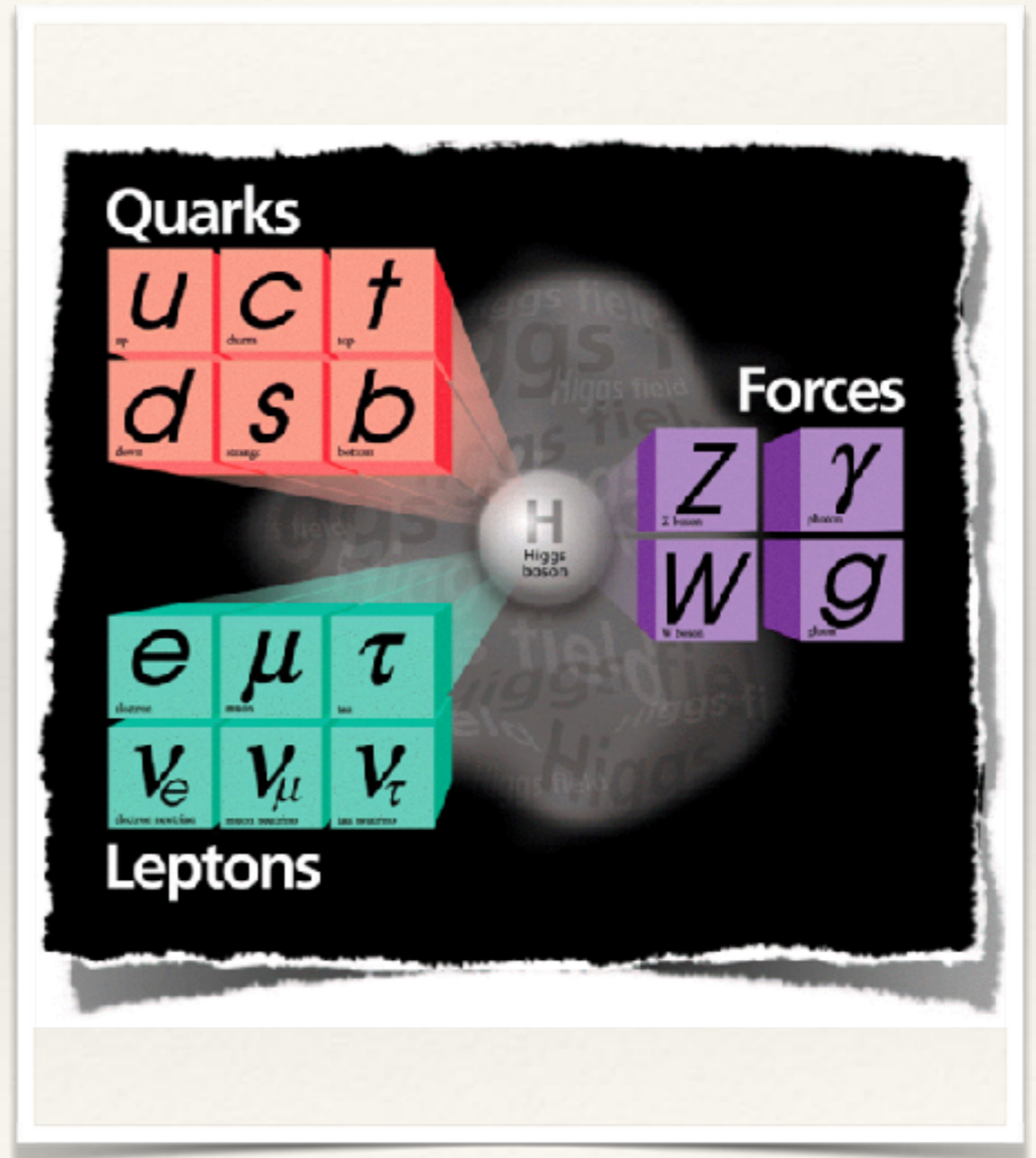
# The Standard Model

## BSM

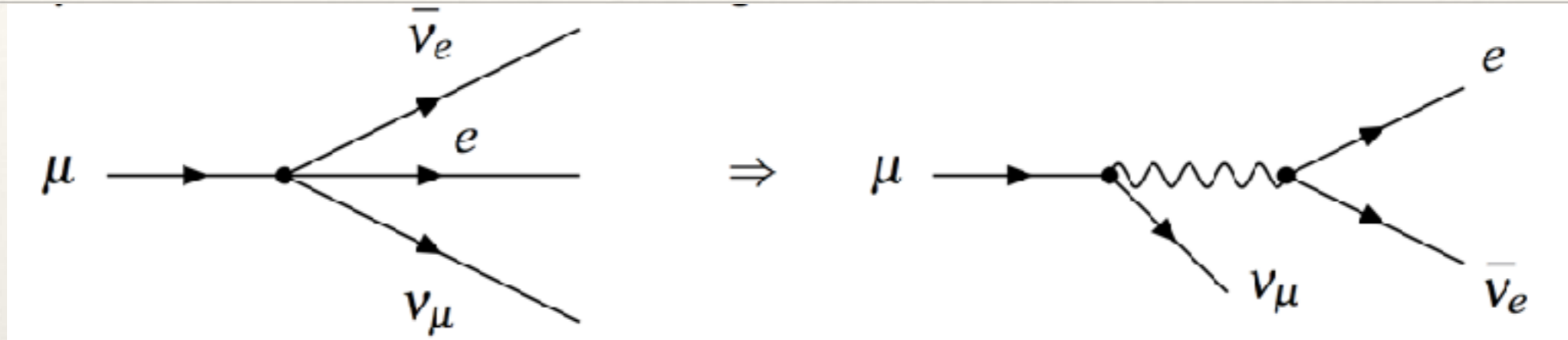
- ❖ Dark Matter
- ❖ Neutrino masses
- ❖ BAU
- ❖ Dark Energy

## \*Theoretical issues

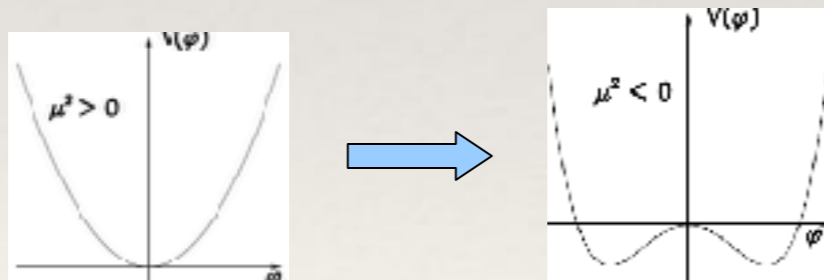
- ❖ Number of families
- ❖ Masses and mixings
- ❖ Hierarchy problem



# Higgs mechanism



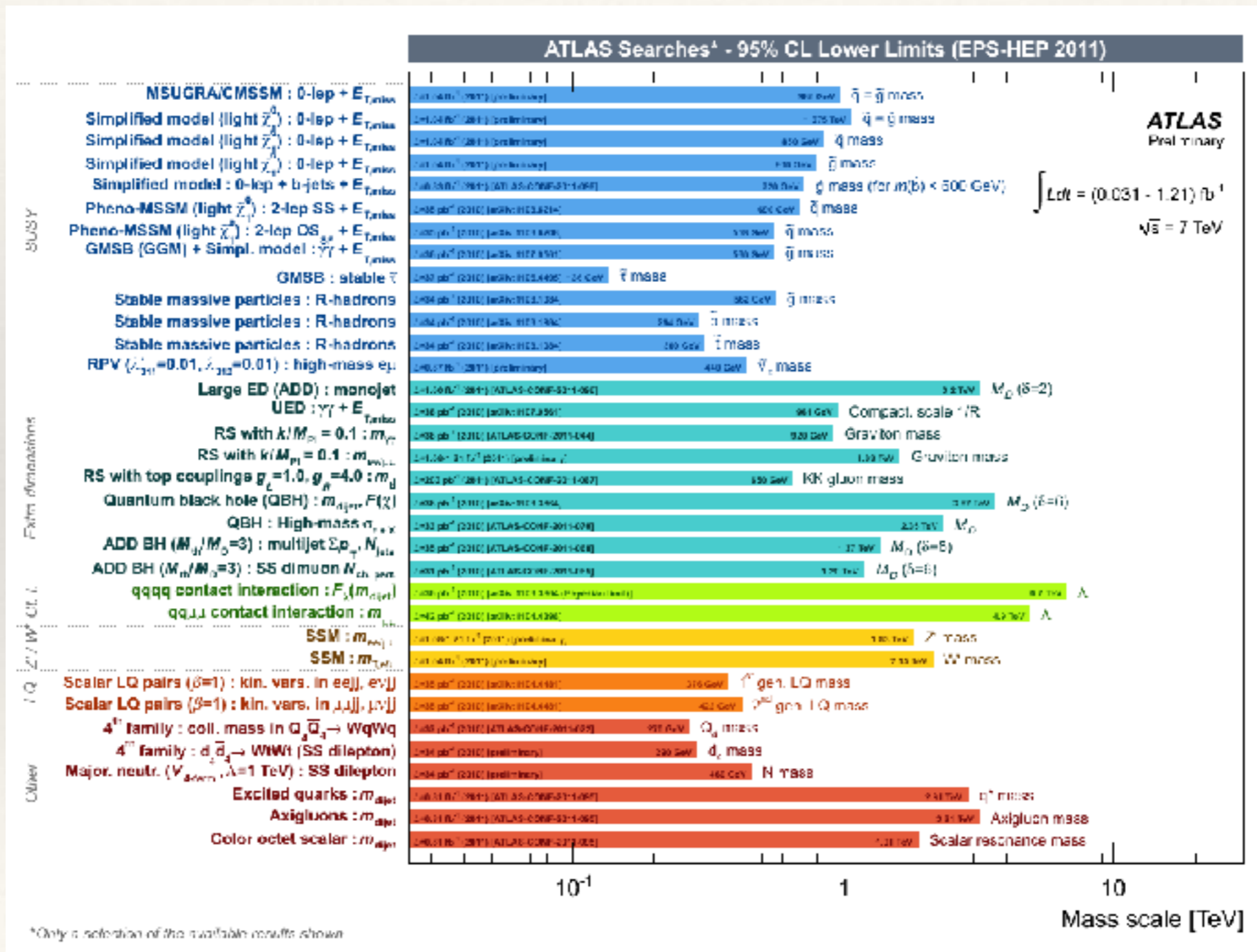
W's and Z boson masses



Brout-Englert-Higgs Mechanism

# BSM?

## Limits on some scenarios by LCH



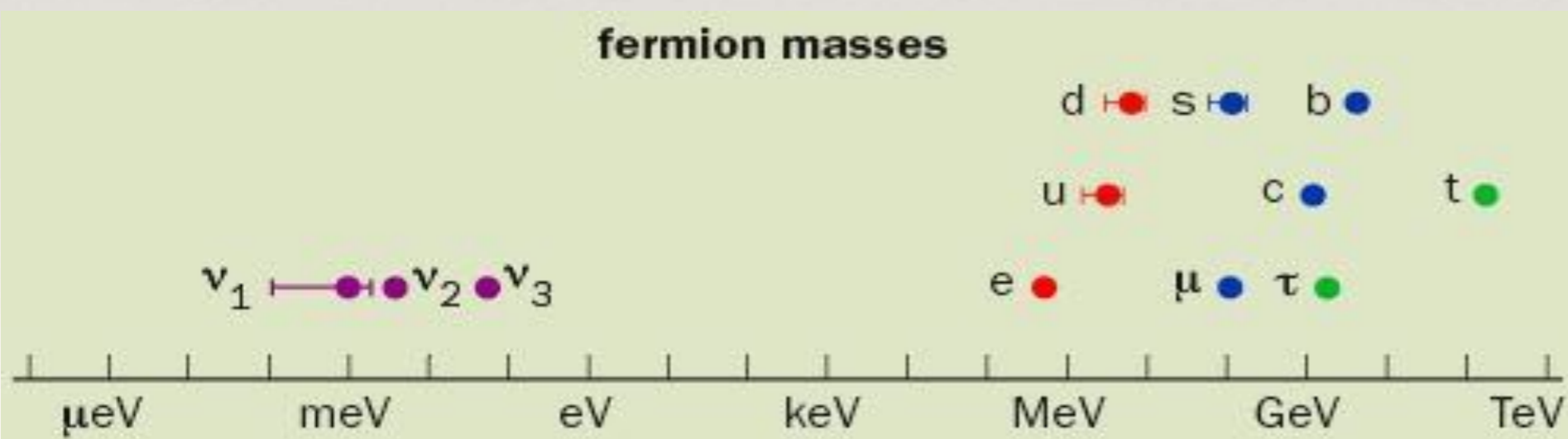
# Yukawas and masses

$$\begin{aligned}
 \mathcal{L} = & i\overline{L'_{\alpha L}}\not{D}L'_{\alpha L} + i\overline{Q'_{\alpha L}}\not{D}Q'_{\alpha L} + i\overline{l'_{\alpha R}}\not{D}l'_{\alpha R} \\
 & + i\overline{q'_{\alpha R}{}^D}\not{D}q'_{\alpha R}{}^D + i\overline{q'_{\alpha R}{}^U}\not{D}q'_{\alpha R}{}^U - \frac{1}{4}\vec{F}_{\mu\nu} \cdot \vec{F}^{\mu\nu} - \frac{1}{4}B_{\mu\nu}B^{\mu\nu} \\
 & + (D_\rho\Phi)^\dagger(D^\rho\Phi) + \mu^2\Phi^\dagger\Phi - \lambda(\Phi^\dagger\Phi)^2 \\
 & - (Y_{\alpha\beta}^N \overline{L'_{\alpha L}}\Phi l'_{\beta R} + Y_{\alpha\beta}^{N*} \overline{l'_{\beta R}}\Phi^\dagger L'_{\alpha L}) \\
 & - (Y_{\alpha\beta}^{D'} \overline{Q'_{\alpha L}}\Phi q'_{\beta R}{}^D + Y_{\alpha\beta}^{D'*} \overline{q'_{\beta R}{}^D}\Phi^\dagger Q'_{\alpha L}) \\
 & - (Y_{\alpha\beta}^{U'} \overline{Q'_{\alpha L}}(i\sigma_2\Phi^*)q'_{\beta R}{}^U + Y_{\alpha\beta}^{U'*} \overline{q'_{\beta R}{}^U}(-i\Phi^T\sigma_2)Q'_{\alpha L})
 \end{aligned}$$

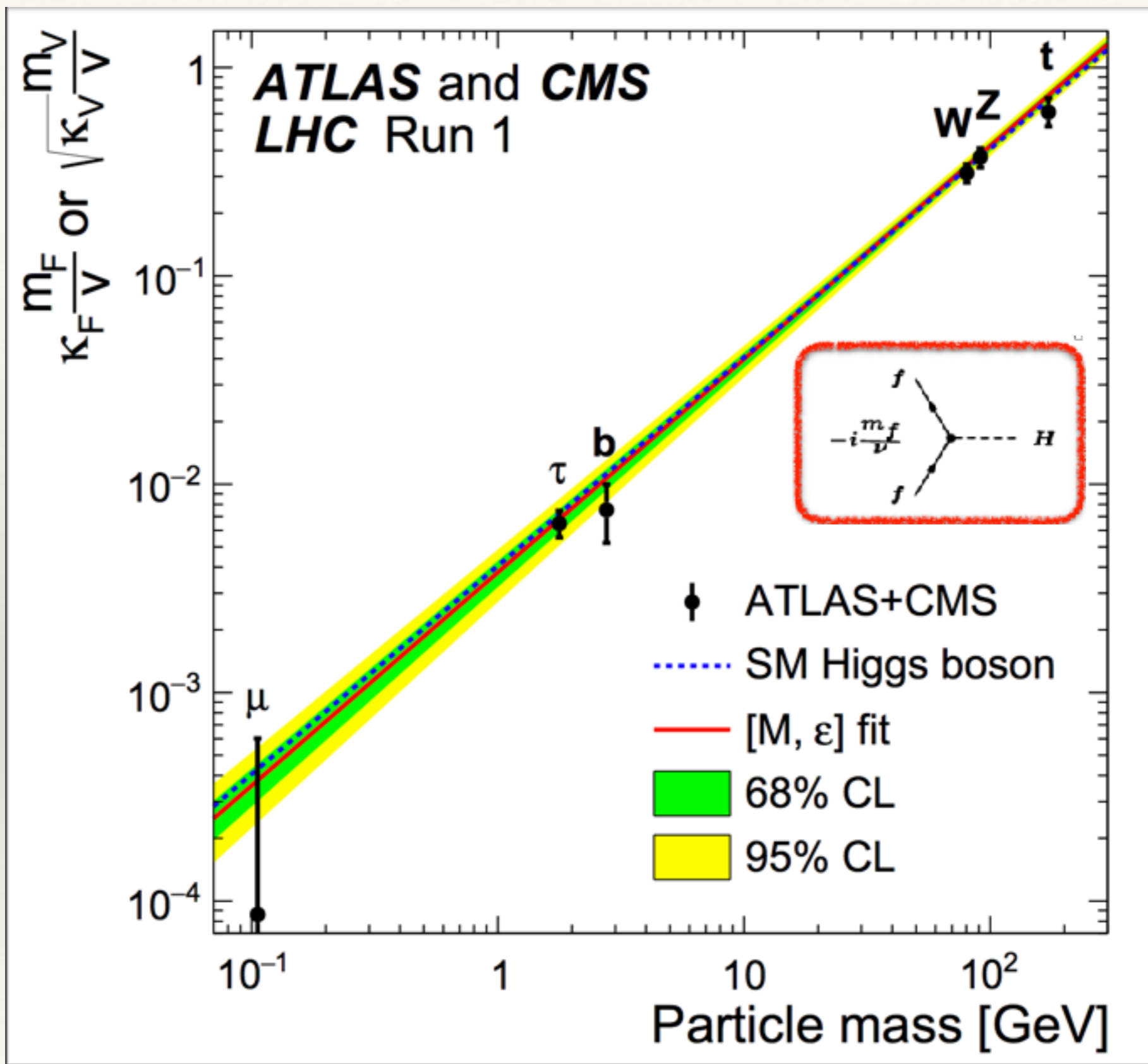
} Yukawa  
Lagrangiana

$$m_\nu \ll m_e \ll m_t$$

Very different Yukawa  
Couplings



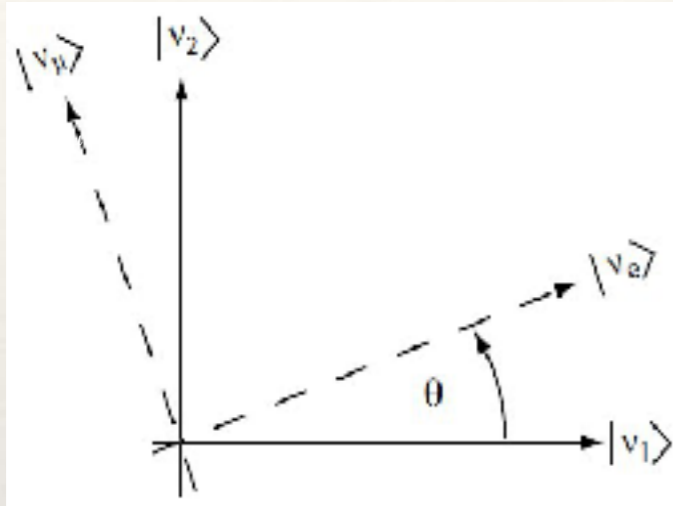
$$Y_{\nu_e} : Y_e : Y_t \\
 < 10^{-11} : 10^{-6} : 1$$





# Neutrino masses

# Neutrino oscillation



weak eigenstates

massive eigenstates

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$



$$P(\nu_\mu \rightarrow \nu_e) = |\langle \nu_e | \nu_\mu(t) \rangle|^2 = \sin^2 2\theta \sin^2 \left( \frac{\Delta m^2 L}{4 E_\nu} \right)$$

3 mixing angles and 2 squared mass differences

# Neutrino mixings

parameter	best fit $\pm 1\sigma$	$2\sigma$ range	$3\sigma$ range
$\Delta m_{21}^2 [10^{-5} \text{eV}^2]$	$7.55^{+0.20}_{-0.16}$	7.20–7.94	7.05–8.14
$ \Delta m_{31}^2  [10^{-3} \text{eV}^2]$ (NO)	$2.50 \pm 0.03$	2.44–2.57	2.41–2.60
$ \Delta m_{31}^2  [10^{-3} \text{eV}^2]$ (IO)	$2.42^{+0.03}_{-0.04}$	2.34–2.47	2.31–2.51
$\sin^2 \theta_{12}/10^{-1}$	$3.20^{+0.20}_{-0.16}$	2.89–3.59	2.73–3.79
$\theta_{12}/^\circ$	$34.5^{+1.2}_{-1.0}$	32.5–36.8	31.5–38.0
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.47^{+0.20}_{-0.30}$	4.67–5.83	4.45–5.99
$\theta_{23}/^\circ$	$47.7^{+1.2}_{-1.7}$	43.1–49.8	41.8–50.7
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.51^{+0.18}_{-0.30}$	4.91–5.84	4.53–5.98
$\theta_{23}/^\circ$	$47.9^{+1.0}_{-1.7}$	44.5–48.9	42.3–50.7
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.160^{+0.083}_{-0.069}$	2.03–2.34	1.96–2.41
$\theta_{13}/^\circ$	$8.45^{+0.18}_{-0.14}$	8.2–8.8	8.0–8.9
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.220^{+0.074}_{-0.076}$	2.07–2.36	1.99–2.44
$\theta_{13}/^\circ$	$8.53^{+0.14}_{-0.15}$	8.3–8.8	8.1–9.0
$\delta/\pi$ (NO)	$1.21^{+0.21}_{-0.15}$	1.01–1.75	0.87–1.94
$\delta/^\circ$	$218^{+38}_{-27}$	182–315	157–349
$\delta/\pi$ (IO)	$1.56^{+0.13}_{-0.15}$	1.27–1.82	1.12–1.94
$\delta/^\circ$	$281^{+23}_{-27}$	229–328	202–349



- ❖ 2 nearly maximal mixings
- ❖ One small  $\mathcal{O}(\lambda_c)$
- ❖ CP violation
- ❖ 2 squared mass differences

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PDG (2018)

$$V_{\text{CKM}} = \begin{pmatrix} 0.97446 \pm 0.00010 & 0.22452 \pm 0.00044 & 0.00365 \pm 0.00012 \\ 0.22438 \pm 0.00044 & 0.97359^{+0.00010}_{-0.00011} & 0.04214 \pm 0.00076 \\ 0.00896^{+0.00024}_{-0.00023} & 0.04133 \pm 0.00074 & 0.999105 \pm 0.000032 \end{pmatrix}$$

$$|U|_{3\sigma} = \begin{pmatrix} 0.799 \rightarrow 0.844 & 0.516 \rightarrow 0.582 & 0.141 \rightarrow 0.156 \\ 0.242 \rightarrow 0.494 & 0.467 \rightarrow 0.678 & 0.639 \rightarrow 0.774 \\ 0.284 \rightarrow 0.521 & 0.490 \rightarrow 0.695 & 0.615 \rightarrow 0.754 \end{pmatrix}$$

NuFIT 3.2 (2018)

# Fermion masses

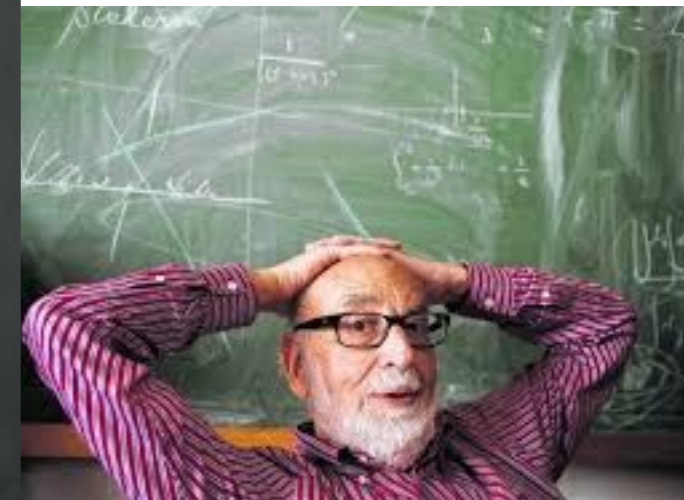
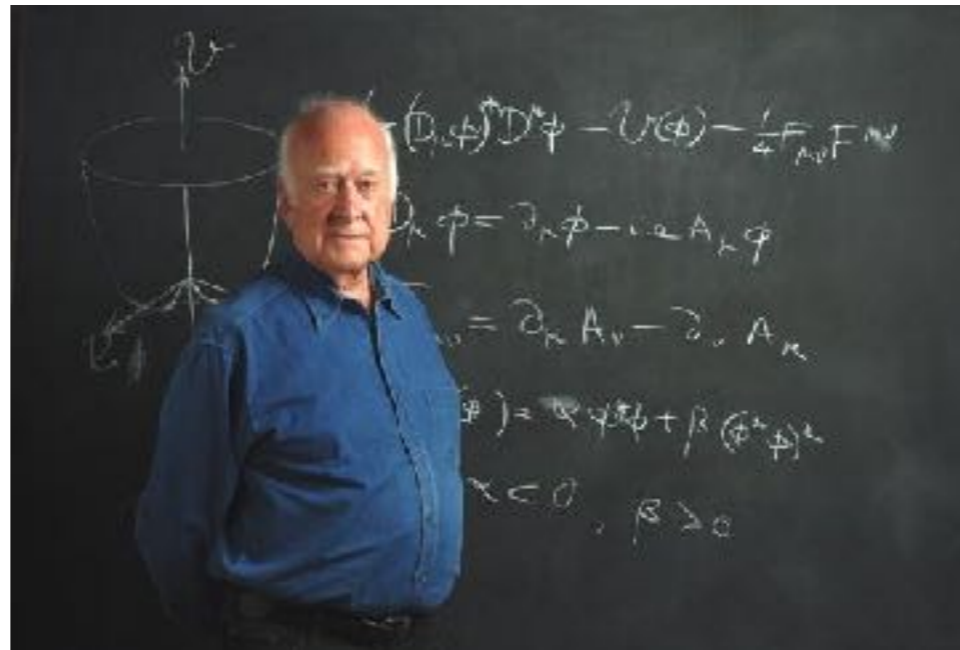
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 & + iq'_{\alpha R}{}^{D} \not{D} q'_{\alpha R}{}^{D} + iq'_{\alpha R}{}^{U} \not{D} q'_{\alpha R}{}^{U} - \frac{1}{4} \vec{F}_{\mu\nu} \cdot \vec{F}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} \\
 & + (D_{\rho} \Phi)^{\dagger} (D^{\rho} \Phi) + \mu^2 \Phi^{\dagger} \Phi - \lambda (\Phi^{\dagger} \Phi)^2 \\
 & - \left( Y'_{\alpha\beta}{}^l \overline{L}'_{\alpha L} \Phi l'_{\beta R} + Y'_{\alpha\beta}{}^{l*} \overline{l}'_{\beta R} \Phi^{\dagger} L'_{\alpha L} \right) \\
 & - \left( Y'_{\alpha\beta}{}^D \overline{Q}'_{\alpha L} \Phi q'_{\beta R}{}^D + Y'_{\alpha\beta}{}^{D*} \overline{q}'_{\beta R}{}^D \Phi^{\dagger} Q'_{\alpha L} \right) \\
 & - \left( Y'_{\alpha\beta}{}^U \overline{Q}'_{\alpha L} (i\sigma_2 \Phi^*) q'_{\beta R}{}^U + Y'_{\alpha\beta}{}^{U*} \overline{q}'_{\beta R}{}^U (-i\Phi^T \sigma_2) Q'_{\alpha L} \right)
 \end{aligned}$$



Yukawa Lagrangiana

## Fermion masses:

$m_e$	.5 MeV
$m_d$	4.8 MeV
$m_u$	2.3 MeV
$m_{\mu}$	105 MeV
$m_s$	95 MeV
$m_c$	1.275 GeV
$m_{\tau}$	1.776 GeV
$m_b$	4.18 GeV
$m_t$	174 GeV



# Fermion masses

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 & - \left( Y_{\alpha\beta}^{\prime D} \overline{Q}'_{\alpha L} \Phi q'_{\beta R} + Y_{\alpha\beta}^{\prime D*} \overline{q}'_{\beta R} \Phi^\dagger Q'_{\alpha L} \right) \\
 & - \left( Y_{\alpha\beta}^{\prime U} \overline{Q}'_{\alpha L} (i\sigma_2 \Phi^*) q'_{\beta R} + Y_{\alpha\beta}^{\prime U*} \overline{q}'_{\beta R} (-i\Phi^T \sigma_2) Q'_{\alpha L} \right)
 \end{aligned}$$



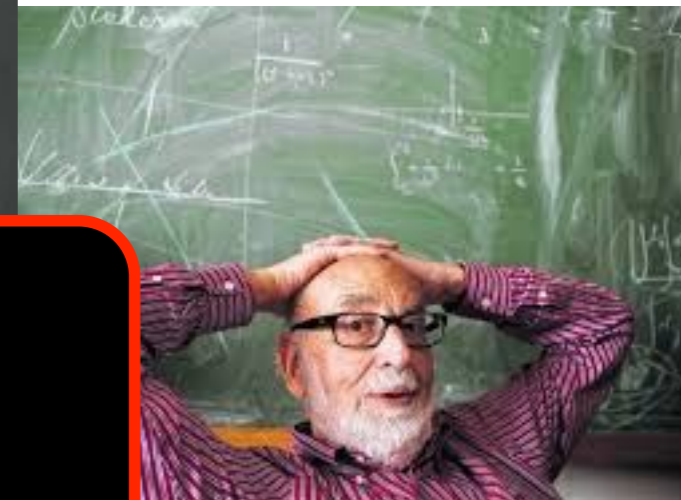
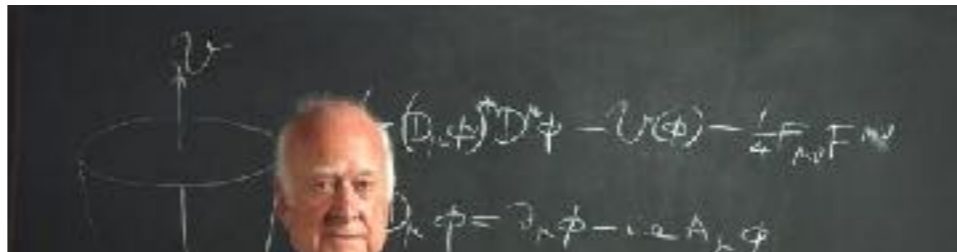
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## Neutrino mass scale:

Mainz current limit	$\Sigma m_\nu < 2 \text{ eV}$
Katrin future sensitivity	$\sim 0.2 \text{ eV}$
PLANK+BAO	$\Sigma m_\nu < 0.23 \text{ eV}$

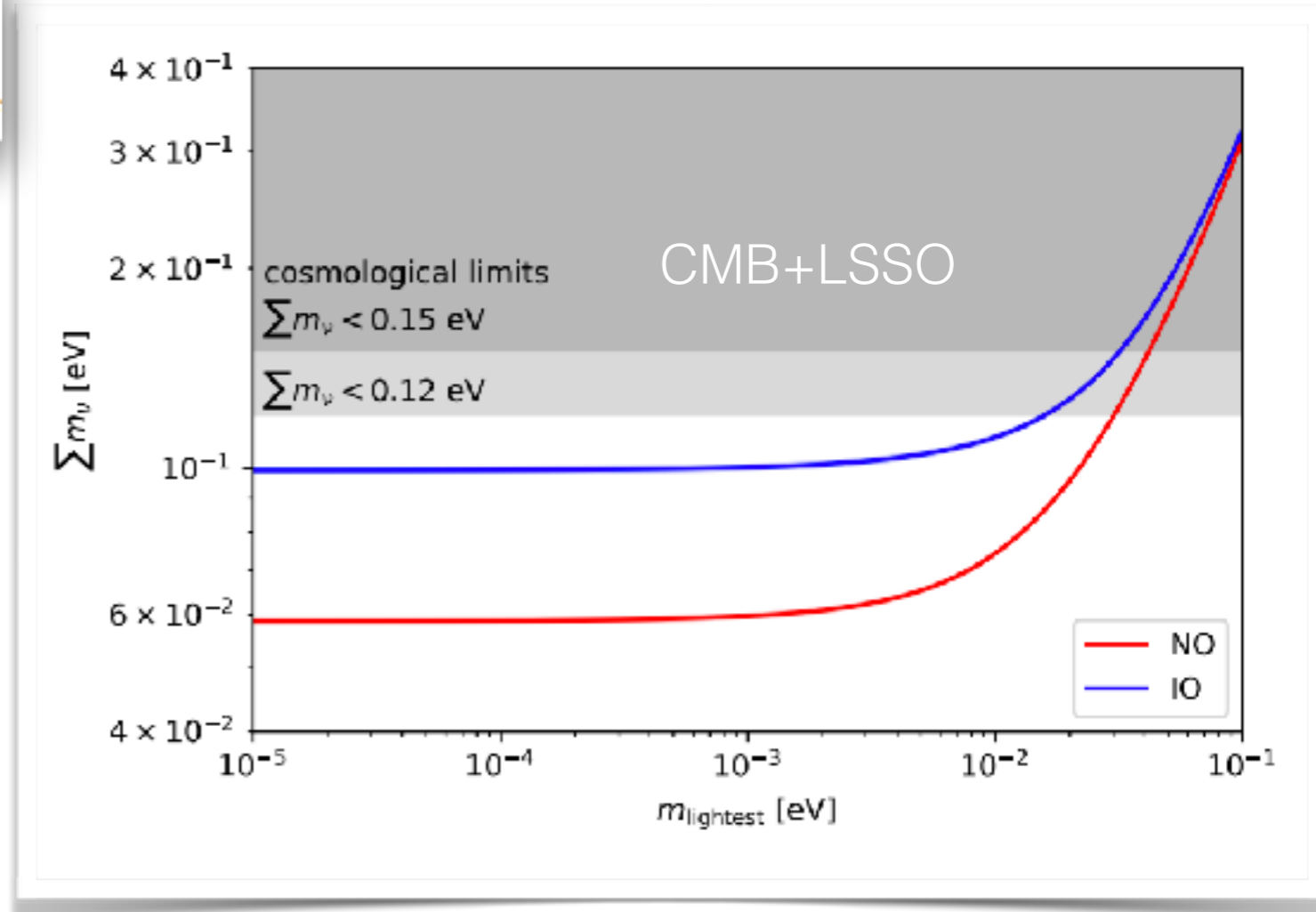
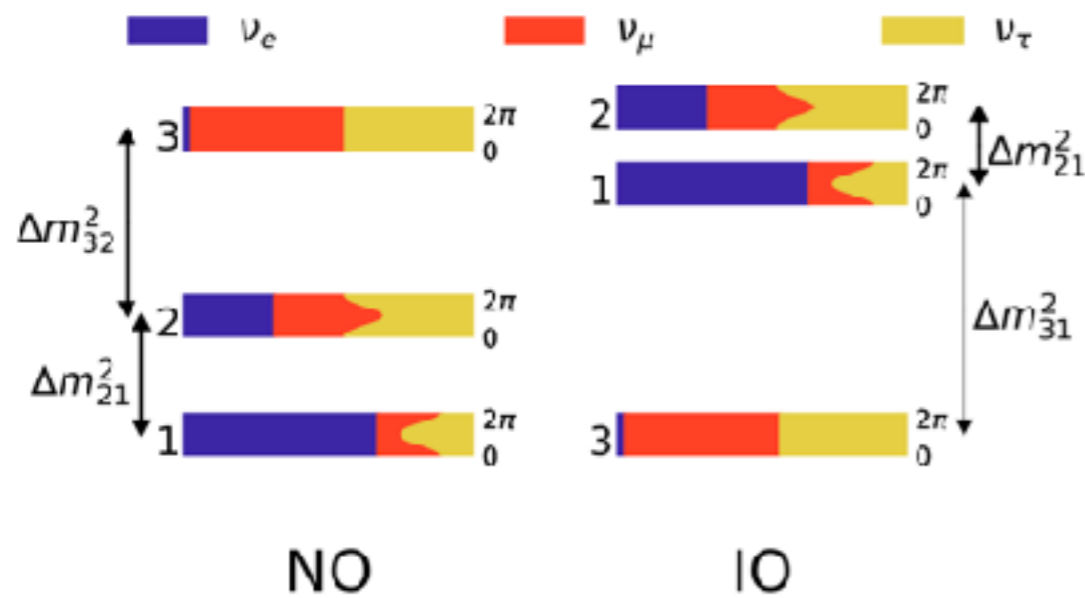


# Neutrino masses Cosmology

de Salas, Gariazzo, Mena, Ternes, Tortola (2018)

$$\sum m_\nu^{\text{NO}} = m_1 + \sqrt{m_1^2 + \Delta m_{21}^2} + \sqrt{m_1^2 + \Delta m_{31}^2},$$

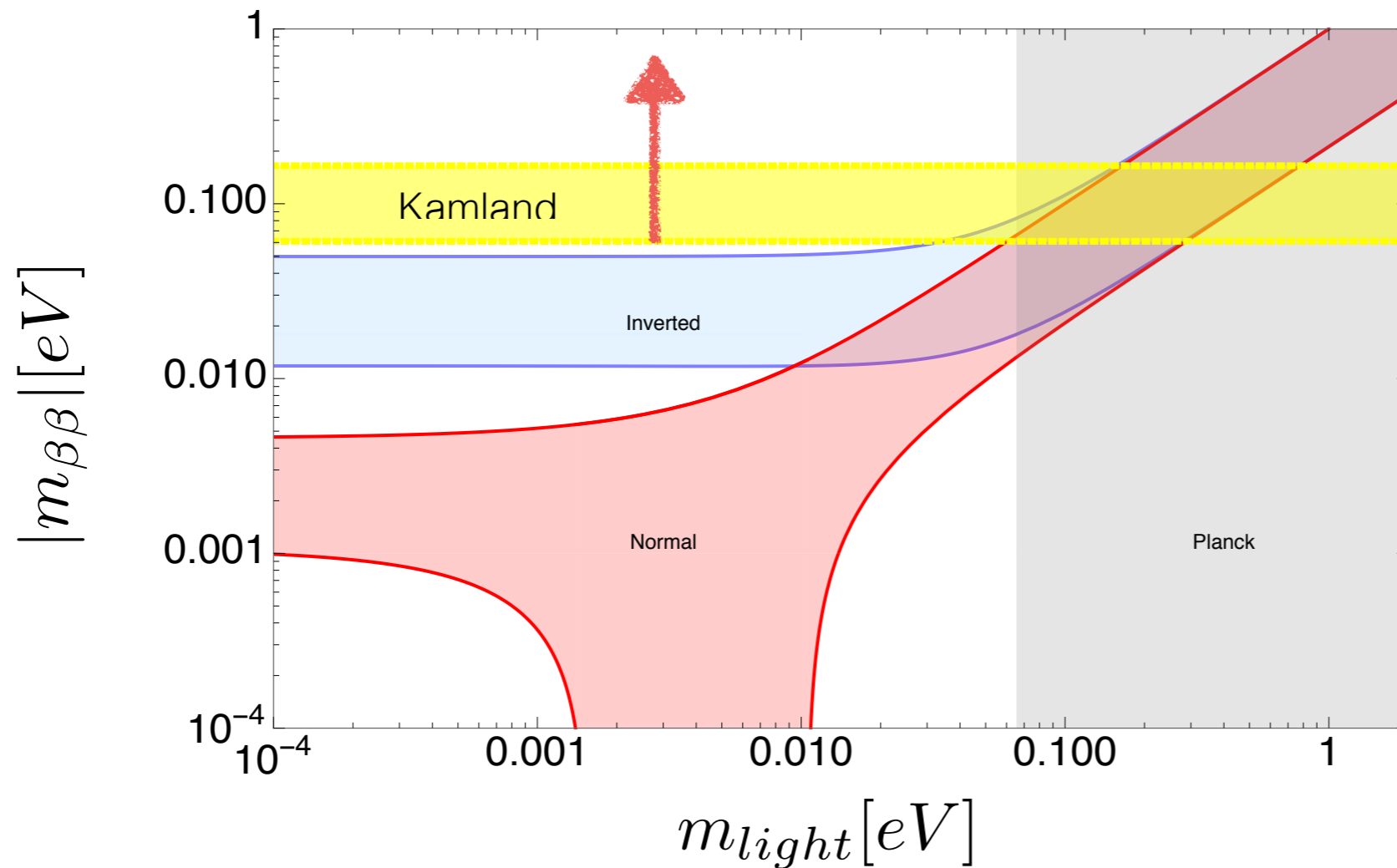
$$\sum m_\nu^{\text{IO}} = m_3 + \sqrt{m_3^2 + |\Delta m_{31}^2|} + \sqrt{m_3^2 + |\Delta m_{31}^2|} + \Delta m_{21}^2$$



# Neutrinoless double beta decay

$$m_{\beta\beta} = \sum_{k=1}^N e^{i\alpha_k} |U_{ek}|^2 m_k$$

 If neutrinos are Majorana particles

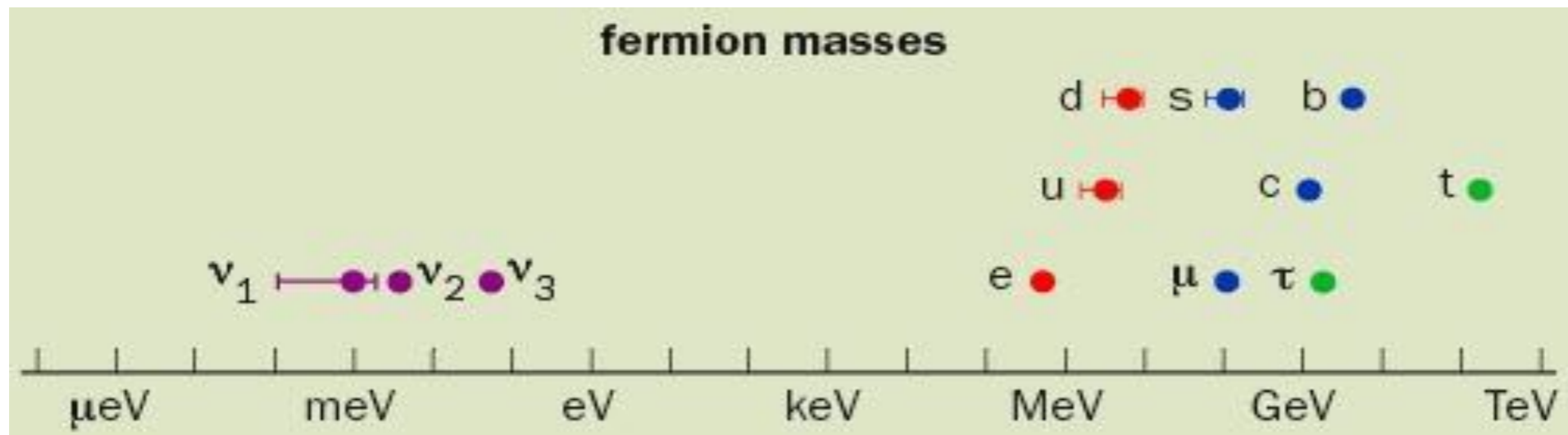


11 neutrino mass matrix  $m_{ee}$



# Dirac neutrino masses

- If we impose Lepton number then the neutrinos are Dirac particles just like quarks and charged leptons



- many orders of magnitude

$m_\nu$	$< 1 \text{ eV}$
$m_e$	$.5 \text{ MeV}$
$m_t$	$174 \text{ GeV}$

$$m_\nu \ll m_e \ll m_t$$

The Yukawa couplings  
are very different

$$Y_{\nu_e} : Y_e : Y_t$$

$$< 10^{-11} : 10^{-6} : 1$$

# Neutrino masses

---

## How can we give mass to the neutrinos?

- Neutrinos are neutral particles
- If we add a Right-Handed neutrino (singlet of SM) then we have the Yukawa coupling with the Higgs (like quarks and leptons)

$$\lambda_{\alpha i} \bar{L}_{\alpha} \epsilon H^* N_i$$

- But there is no symmetry that forbids also this term

$$M_i \bar{N}_i N_i$$

# Neutrino masses

## How can we give mass to the neutrinos?

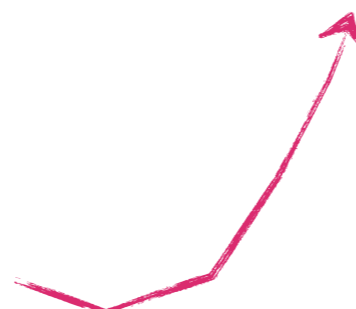
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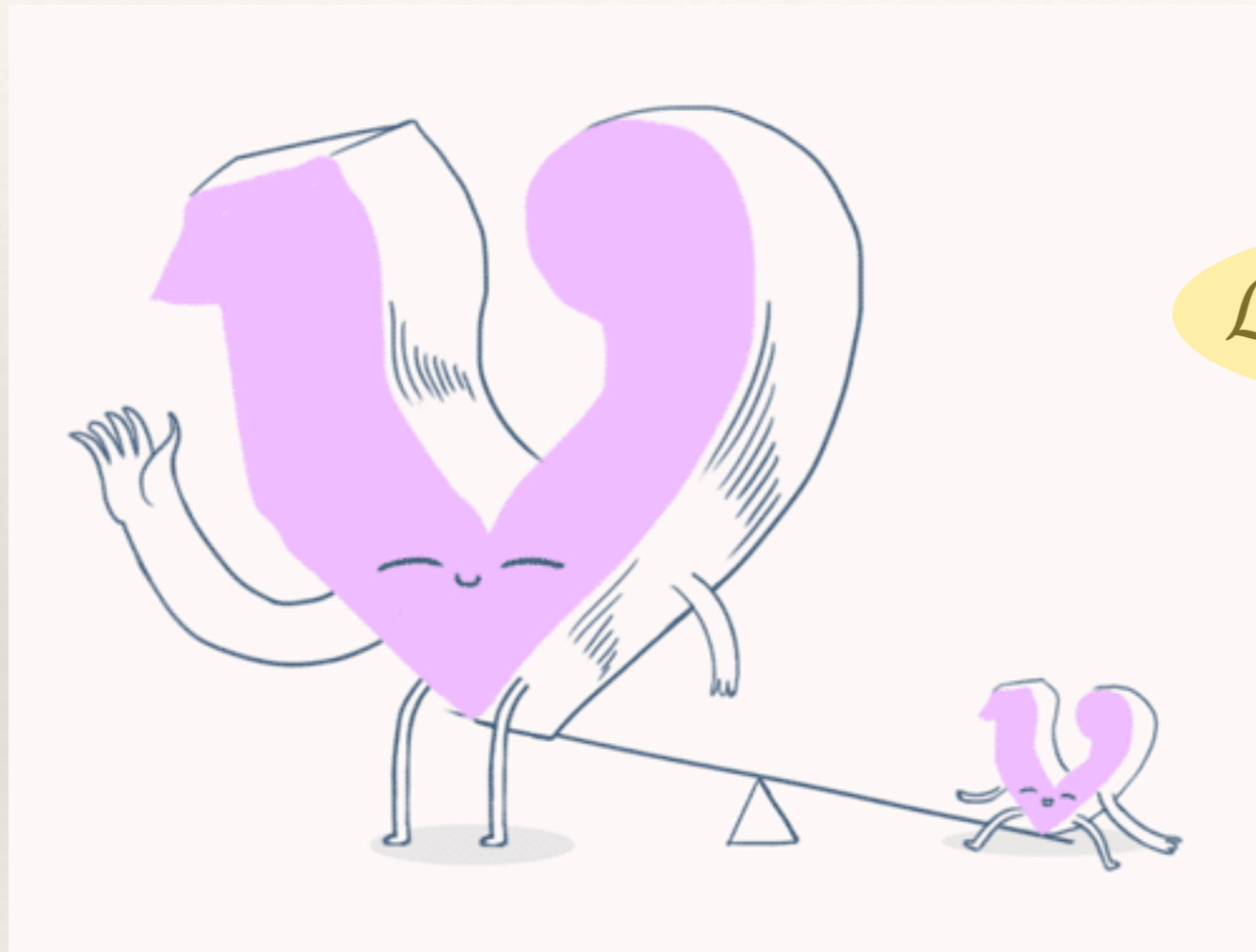
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Vs.



# See-Saw

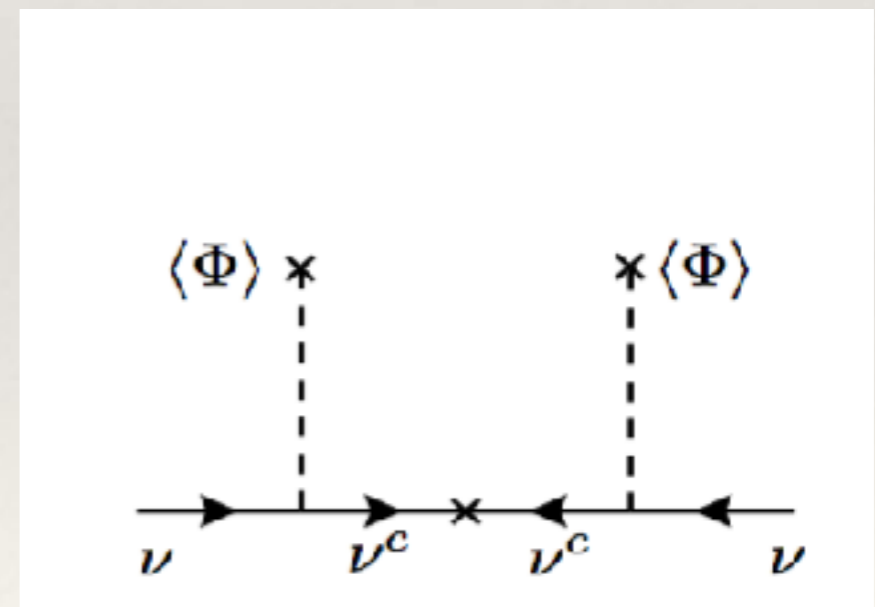


Symmetry magazine

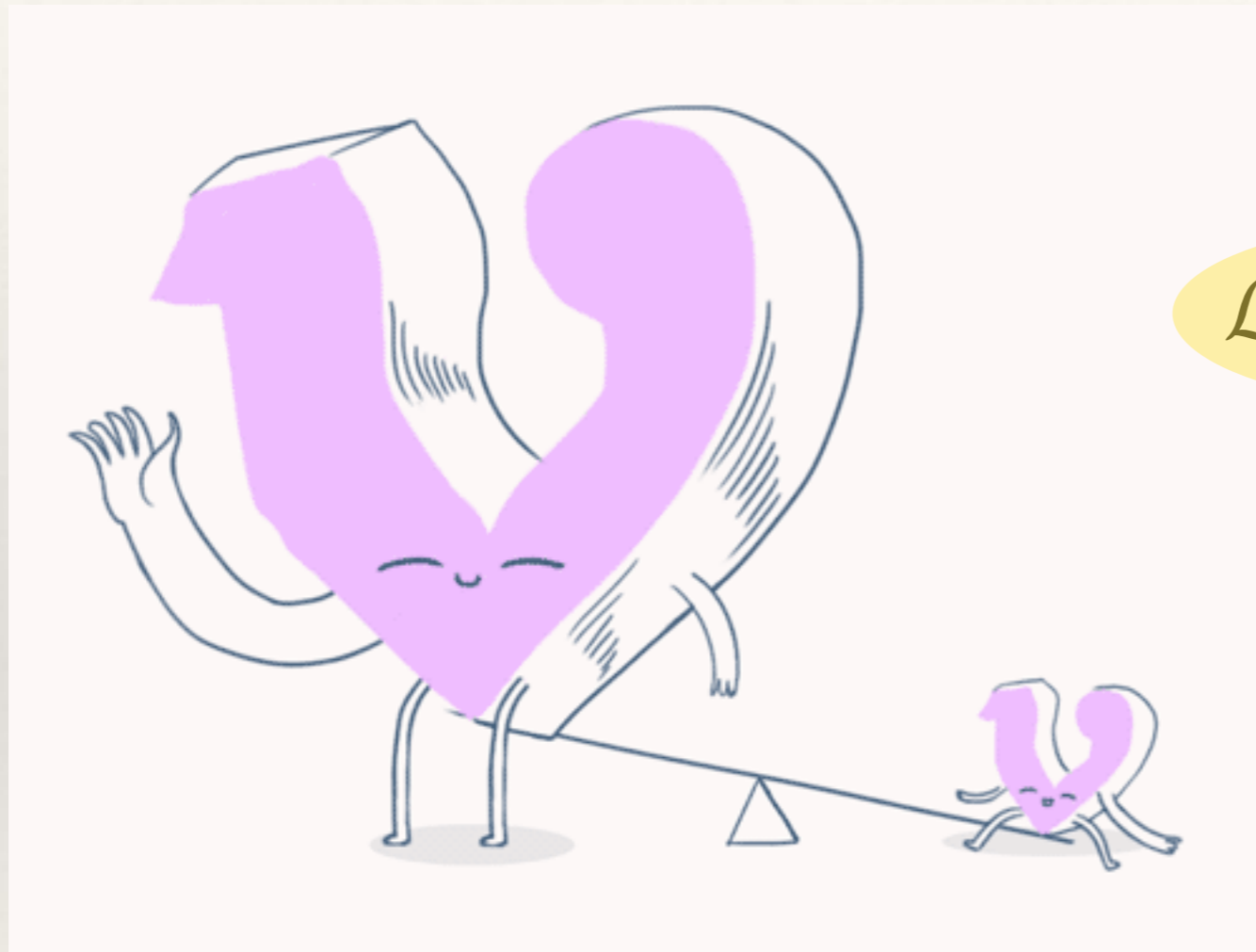
$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda} \mathcal{L}_5$$

$$\mathcal{L}_5 = LL\Phi\Phi$$

$$\Delta L = 2$$



# See-Saw

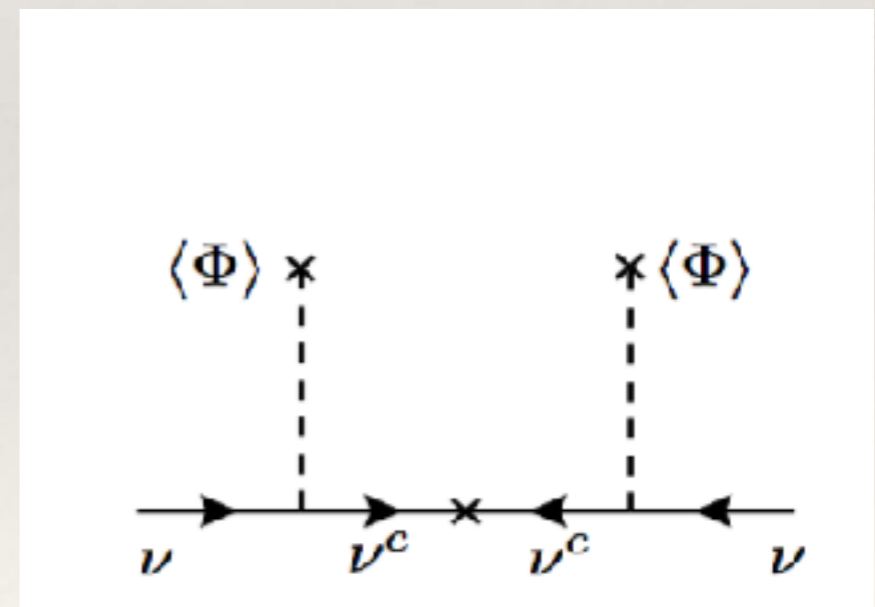


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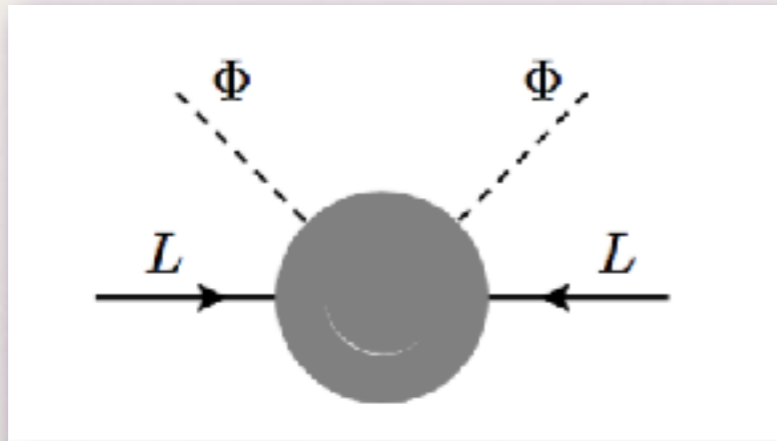
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# See-Saw

- The simplest effective source of Majorana neutrino masses dim 5 Weinberg operator



Weinberg, S. (1980)

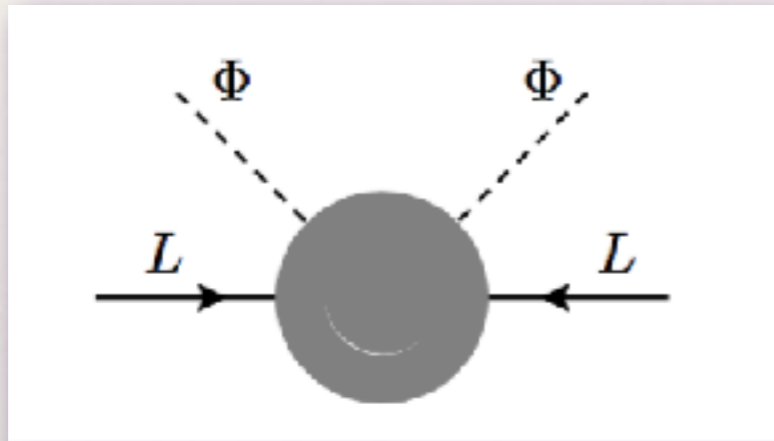
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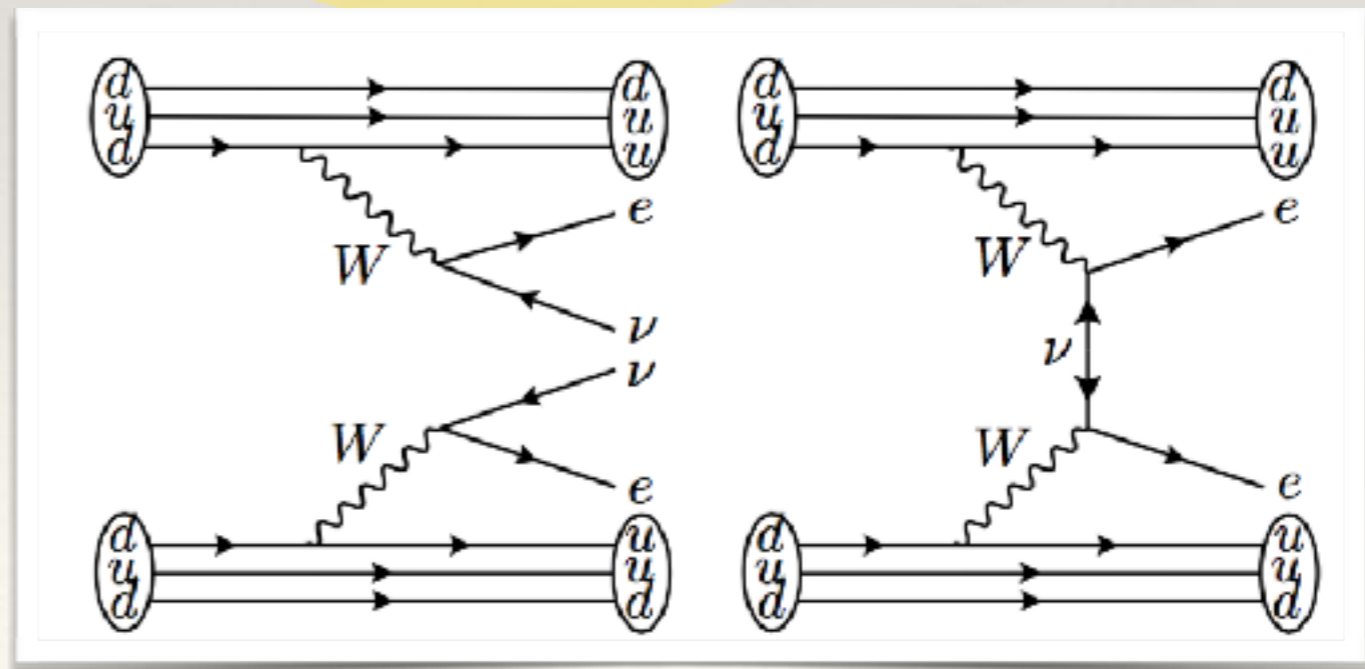
$$\mathcal{L}_5 = LL\Phi\Phi$$

$$\Delta L = 2$$



- Implications?

$0\nu\beta\beta$





# UV-completion dim 5 operator

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## seesaw

 We have several possibilities SU(2) doublets L

$$2 \otimes 2 = 1 + 3$$

type I seesaw

$$LHN \quad 2 \otimes 2 \otimes 1$$

type II seesaw

$$L\Delta L \quad 2 \otimes 3 \otimes 2$$

type III seesaw

$$LH\Sigma \quad 2 \otimes 3 \otimes 2$$

# UV-completion dim 5 operator

## seesaw

We have several possibilities SU(2) doublets L

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type I seesaw

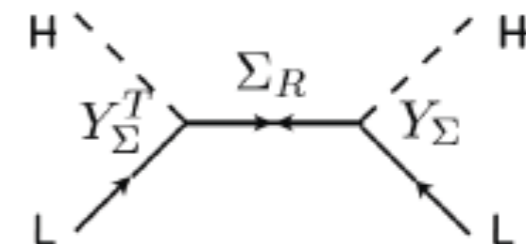
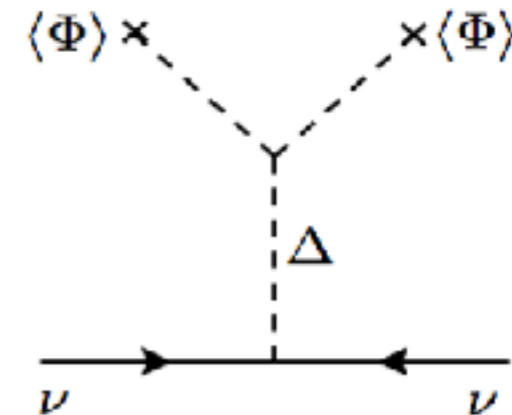
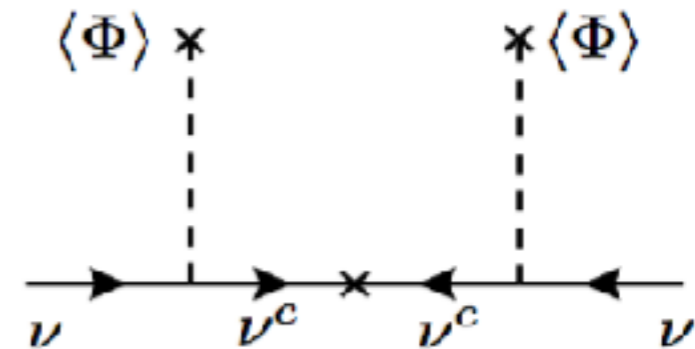
$$LHN \quad 2 \otimes 2 \otimes 1$$

type II seesaw

$$L\Delta L \quad 2 \otimes 3 \otimes 2$$

type III seesaw

$$LH\Sigma \quad 2 \otimes 3 \otimes 2$$



Type III

# UV-completion dim 5 operator

seesaw

We have several possibilities SU(2) doublets L

$$2 \otimes 2 = 1 + 3$$

type I

type I

type II

$$\mathcal{M}_\nu = \begin{bmatrix} M_1 & M_D \\ M_D^T & M_2 \end{bmatrix}$$

$LH\Sigma$

$$2 \otimes 3 \otimes 2$$

$\langle \Phi \rangle \times$

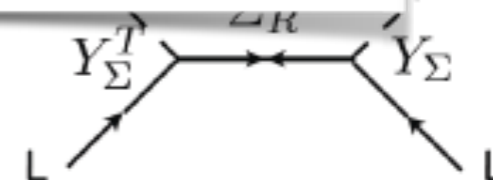
$\times \langle \Phi \rangle$

$\nu$

$\times \langle \Phi \rangle$

$\nu$

H



Type III

# Flavour symmetries

---

FS has been used to reduce  
# of Yukawa couplings

Correlations among observables  
masses, mixings and CP phases

Sometimes predictions  
such as TBM mixing

# Flavour symmetries

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Correlations among observables  
masses, mixings and CP phases

Sometimes predictions  
such as TBM mixing

Texture Zeros to obtain  
Correlations

$$A_1: \begin{pmatrix} 0 & 0 & X \\ 0 & X & X \\ X & X & X \end{pmatrix}, \quad A_2: \begin{pmatrix} 0 & X & 0 \\ X & X & X \\ 0 & X & X \end{pmatrix}$$

$$B_1: \begin{pmatrix} X & X & 0 \\ X & 0 & X \\ 0 & X & X \end{pmatrix}, \quad B_2: \begin{pmatrix} X & 0 & X \\ 0 & X & X \\ X & X & 0 \end{pmatrix},$$

$$B_3: \begin{pmatrix} X & 0 & X \\ 0 & 0 & X \\ X & X & X \end{pmatrix}, \quad B_4: \begin{pmatrix} X & X & 0 \\ X & X & X \\ 0 & X & 0 \end{pmatrix},$$

$$C: \begin{pmatrix} X & X & X \\ X & 0 & X \\ X & X & 0 \end{pmatrix},$$

# Flavour symmetries

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Correlations

$$A_1: \begin{pmatrix} 0 & 0 & X \\ 0 & X & X \\ X & X & X \end{pmatrix}, \quad A_2: \begin{pmatrix} 0 & X & 0 \\ X & X & X \\ 0 & X & X \end{pmatrix}$$

$$B_1: \begin{pmatrix} X & X & 0 \\ X & 0 & X \\ 0 & X & X \end{pmatrix}, \quad B_2: \begin{pmatrix} X & 0 & X \\ 0 & X & X \\ X & X & 0 \end{pmatrix},$$

$$B_3: \begin{pmatrix} X & 0 & X \\ 0 & 0 & X \\ X & X & X \end{pmatrix}, \quad B_4: \begin{pmatrix} X & X & 0 \\ X & X & X \\ 0 & X & 0 \end{pmatrix},$$

$$C: \begin{pmatrix} X & X & X \\ X & 0 & X \\ X & X & 0 \end{pmatrix},$$

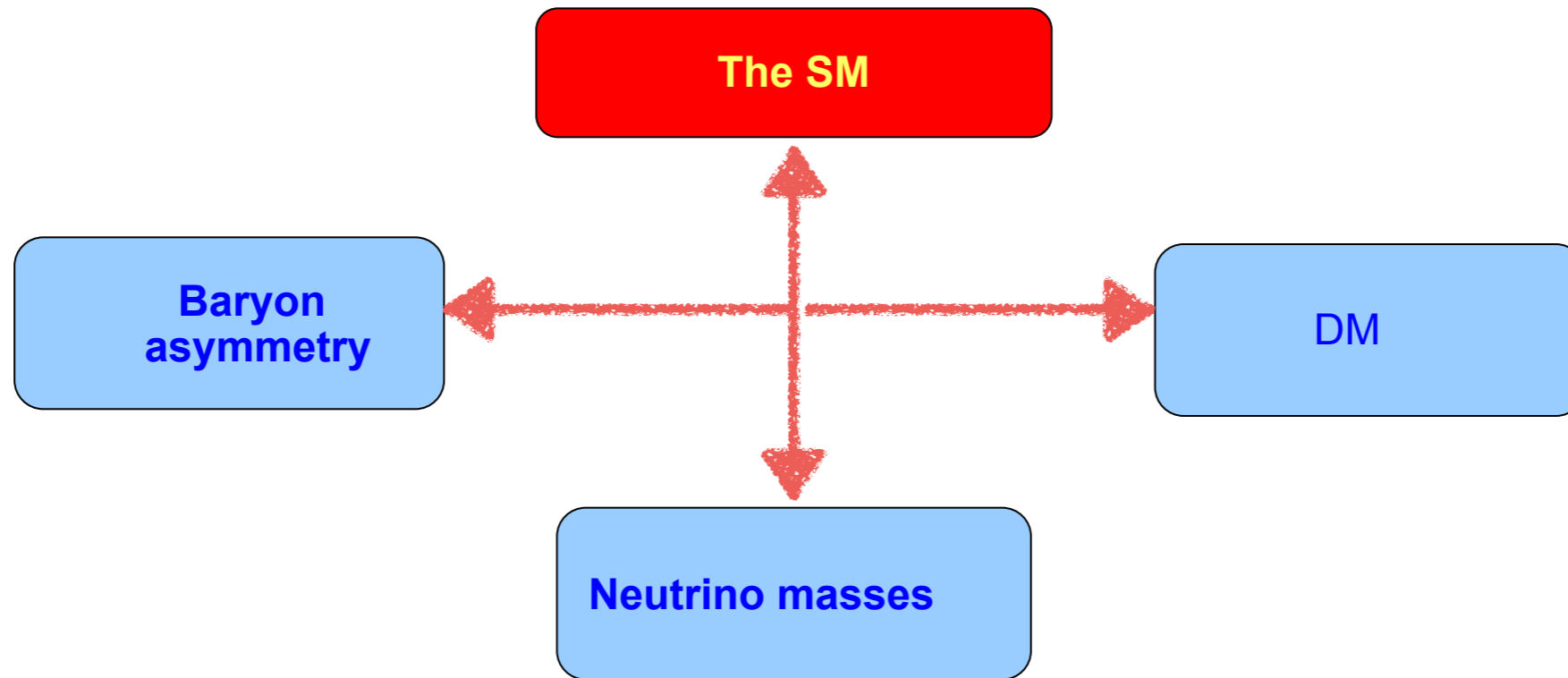
# Connection of neutrinos with DM

---

The SM

# Connection of neutrinos with DM

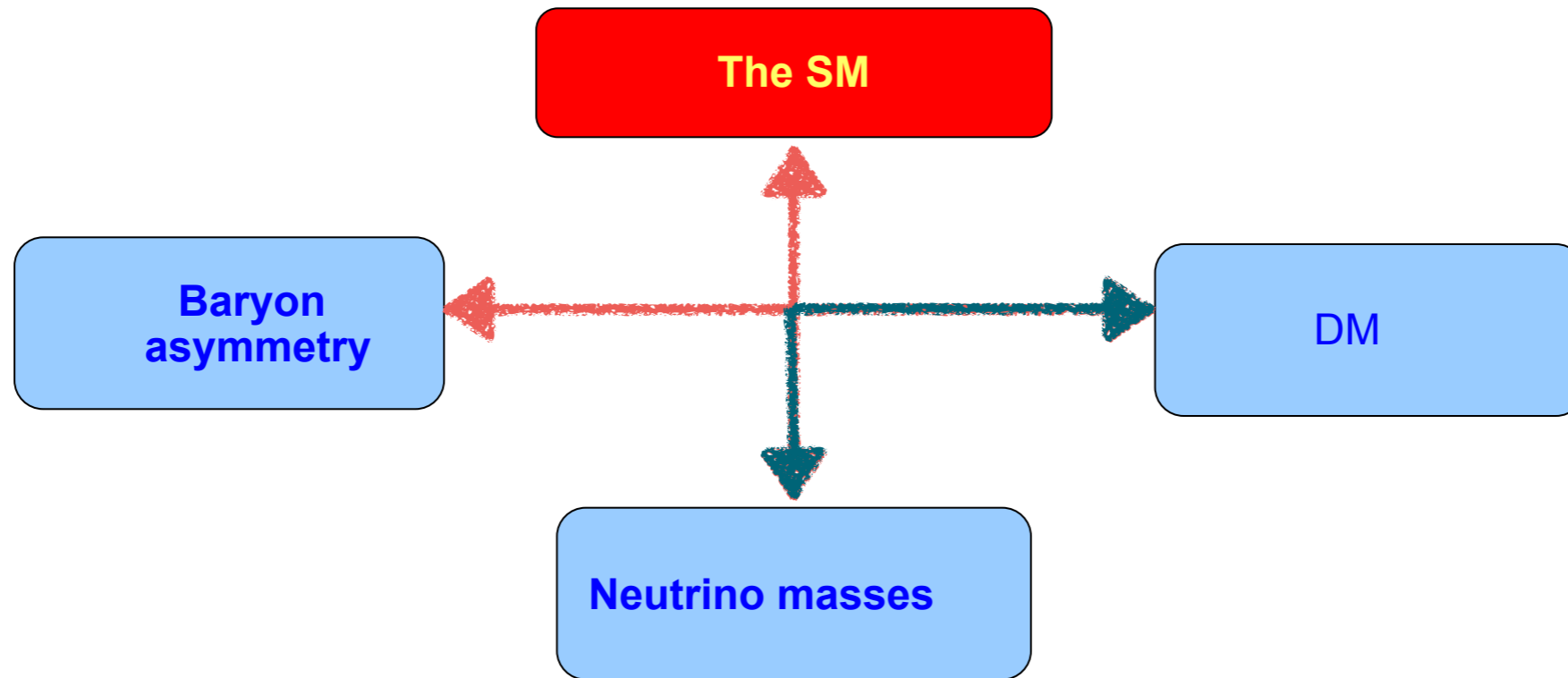
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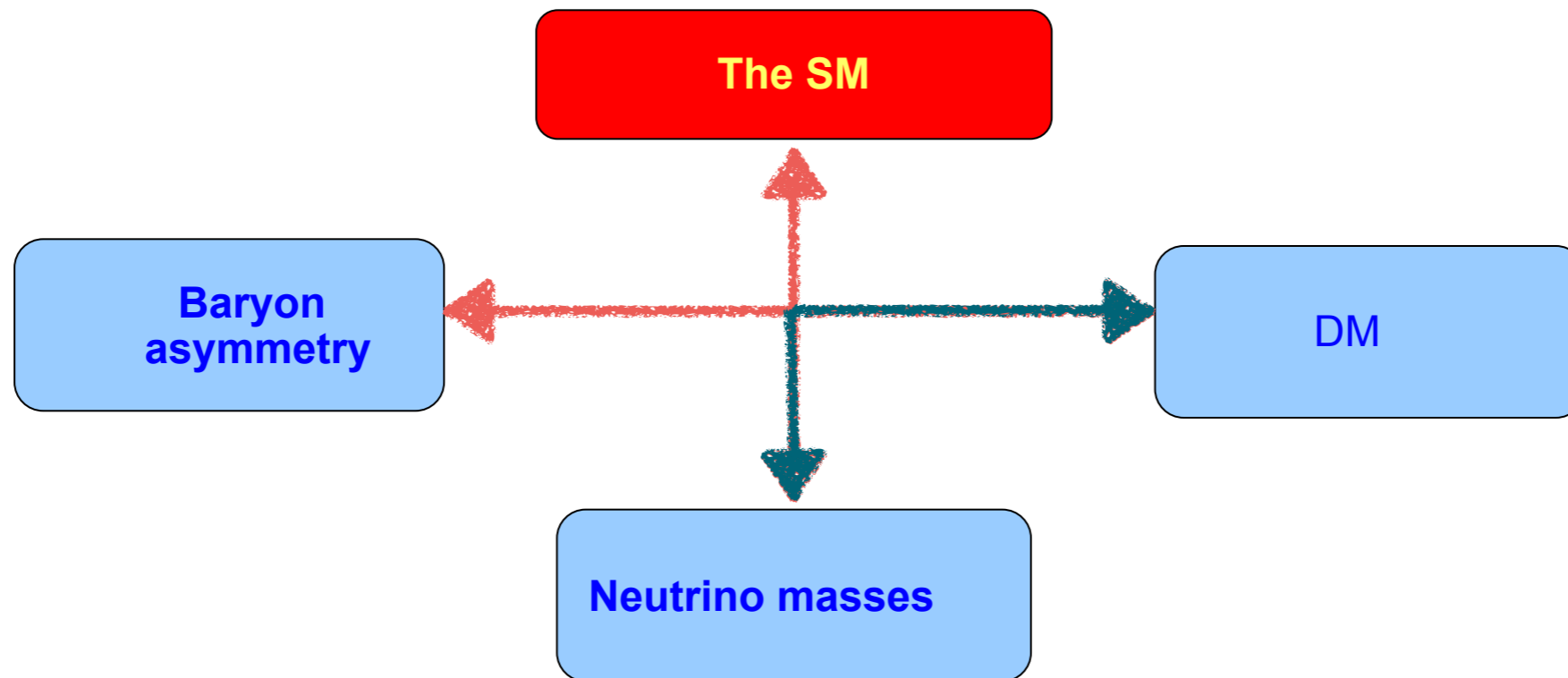


# Connection of neutrinos with DM

---



# Connection of neutrinos with DM



Majoron  
Inert+Loops  
DDM

Loops with higher Higgs representations  
KeV sterile neutrinos  
etc...

# Stability

---



Symmetry

SM +  $\chi$

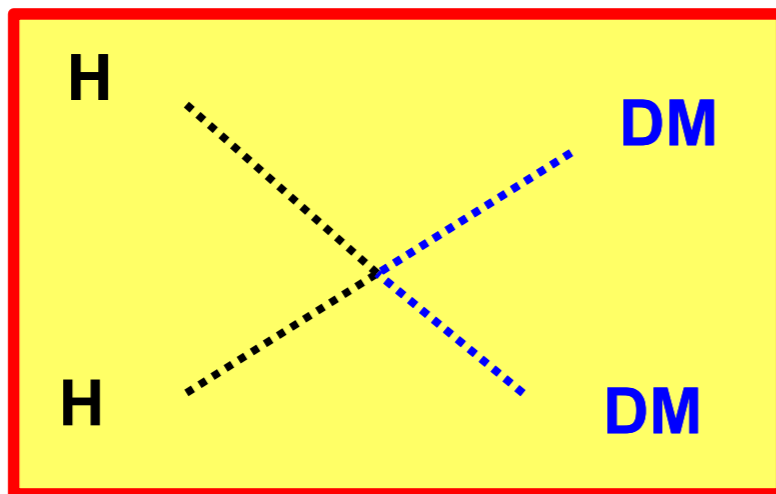
$Z_2$  +1 -1

# Stability

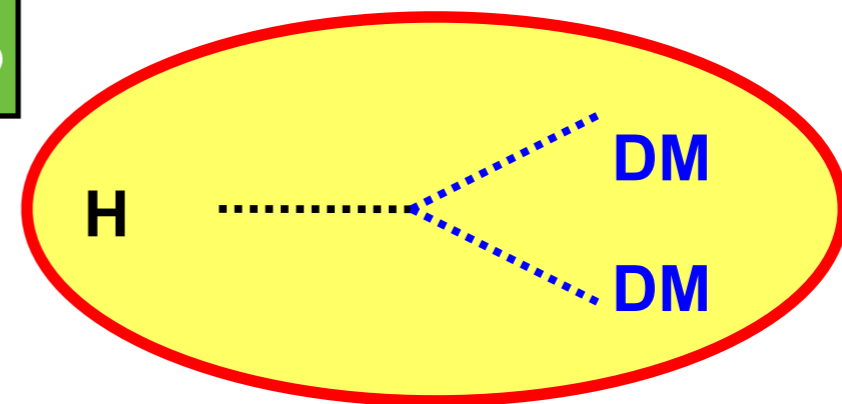


## Symmetry

$$Z_2 \quad \begin{array}{cc} \text{SM} & + \\ +1 & \chi \\ & -1 \end{array}$$



EWWSB



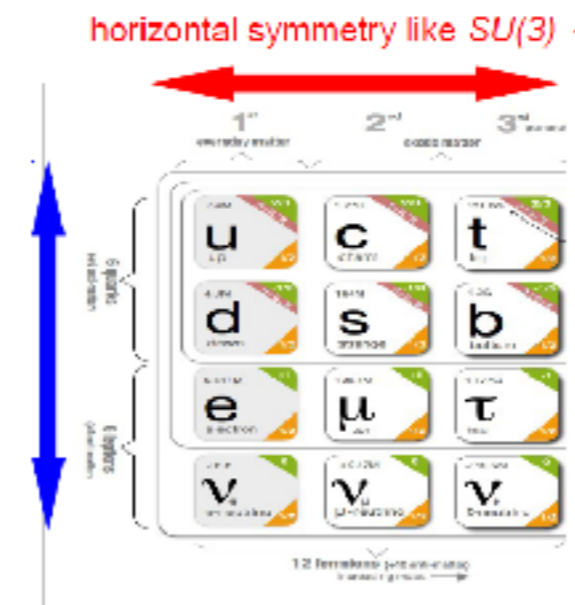
Higgs portal

# Flavor symmetries

Frampton and Kephart, PRD64 (01)

order	groups
6	$S_3 \equiv D_3$
8	$D_4, Q = Q_4$
10	$D_5$
<u>12</u>	$D_6, Q_6, T \equiv A_4$
14	$D_7$
16	$D_8, Q_8, Z_2 \times D_4, Z_2 \times Q$
18	$D_9, Z_3 \times D_3$
20	$D_{10}, Q_{10}$
22	$D_{11}$
24	$D_{12}, Q_{12}, Z_2 \times D_6, Z_2 \times Q_6, Z_2 \times T, Z_3 \times D_4, Z_3 \times Q, Z_4 \times D_3, S_4$
26	$D_{13}$
28	$D_{14}, Q_{14}$
30	$D_{15}, D_5 \times Z_3, D_3 \times Z_5$

vertical gauge symmetry



horizontal symmetry like  $SU(3)$  - triplets

Abelian, non abelian  
continuous, discrete,  
global, local

$Z_N$  already in these symmetries

# A4

Ma and Rajasekaran 2001  
Babu, Ma, Valle 2003  
Altarelli, Feruglio 2005

...

The generators are :

$S$  and  $T$

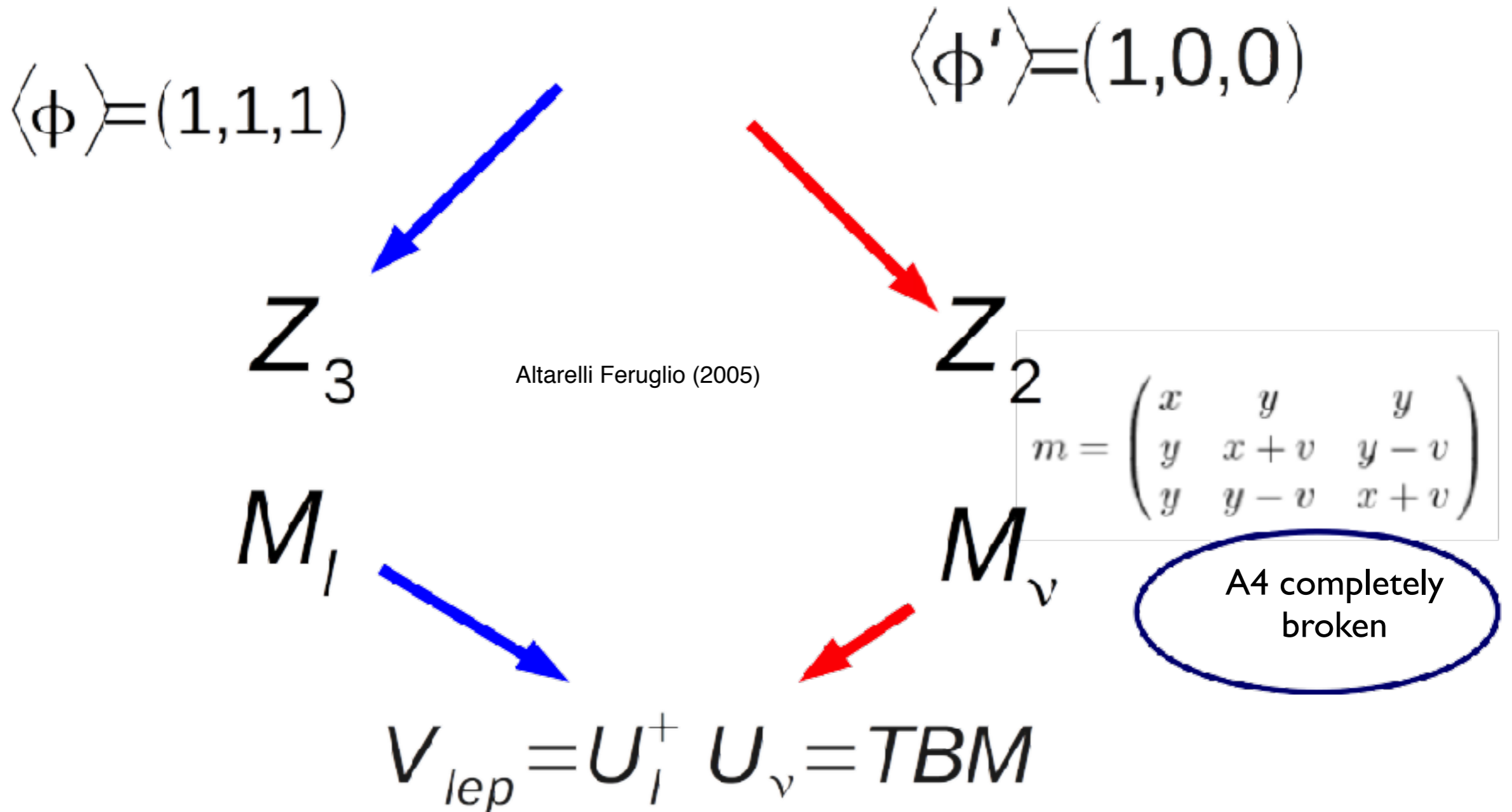
$$S^2 = T^3 = (ST)^3 = \mathcal{I}.$$

1, 1', 1'' and 3

1	$S = 1$	$T = 1$
1'	$S = 1$	$T = e^{i4\pi/3} \equiv \omega^2$
1''	$S = 1$	$T = e^{i2\pi/3} \equiv \omega$

$$S = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \quad T = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$$

# A4 and TBM



**Large neutrino mixing**



$\phi \neq \phi'$   
**Misalignment**

# How to use it to stabilise DM

---

Instead of **breaking A4** in two different directions

$$\langle \phi \rangle = (1, 0, 0)$$

Preserves “S” ( $Z_2$ )

~~$$\langle \phi \rangle = (1, 1, 1)$$~~

~~Preserves “T” ( $Z_3$ )~~



# How to use it to stabilise DM

---

Instead of **breaking A4** in two different directions

$$\langle \phi \rangle = (1, 0, 0)$$

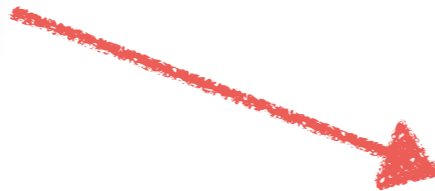
Preserves "S" ( $Z_2$ )

~~$$\langle \phi \rangle = (1, 1, 1)$$~~

~~Preserves "T" ( $Z_3$ )~~

No TBM, but  $Z_2$

DM Stability



# The Discrete Dark Matter

---

- We need a non-abelian flavor group
- Scalar fields in a non-trivial irrep
- This scalar only couples with leptons
- not connected with quarks
- The vev of the scalar breaks the flavor into a  $Z_N$  subgroup of the FS
- This breaking dictates the Neutrino pheno

# The model

SM + 3 Higgs SU(2) doublets , 4 right handed neutrinos

Hirsch, Morisi, Peinado and Valle  
Phys. Rev. D 82, 116003 (2010)

	$L_e$	$L_\mu$	$L_\tau$	$l_e^c$	$l_\mu^c$	$l_\tau^c$	$N_T$	$N_4$	$H$	$\eta$
$SU(2)$	2	2	2	1	1	1	1	1	2	2
$\Lambda_4$	1	1'	1''	1	1''	1'	3	1	1	3

$$\langle \eta_{2,3}^0 \rangle = 0$$

$$\langle \eta \rangle \sim (1, 0, 0)$$

$$\langle \eta_1^0 \rangle = v_\eta$$

$$\langle H^0 \rangle = v_h$$

$$m_D = \begin{pmatrix} x_1 & 0 & 0 & y_1 \\ x_2 & 0 & 0 & 0 \\ x_3 & 0 & 0 & 0 \end{pmatrix}$$

$$M_R = \text{diag}(M_1, M_1, M_1, M_2)$$

inert part

Rank 2 matrix

# Neutrino Pheno

Scaling matrix,  
Rodejohan and Mohapatra

$$\begin{pmatrix} y^2 & ab & ac \\ ab & b^2 & bc \\ ac & bc & c^2 \end{pmatrix}$$



$$m_3 = 0$$

$$\begin{pmatrix} 0 \\ -c/b \\ 1 \end{pmatrix}$$

**Inverse mass Hierarchy**

$$\left\{ m_{ee} \sim 0.03 - 0.05 \text{ eV} \right\}$$

# Neutrino Pheno

Scaling matrix,  
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$$m_3 = 0$$

$$\begin{pmatrix} 0 \\ -c/b \\ 1 \end{pmatrix}$$

$\sin^2 \theta_{13}/10^{-2}$  (NH)

$2.34 \pm 0.20$

1.95–2.74

1.77–2.94

$\theta_{13}/^\circ$

$8.8 \pm 0.4$

8.0–9.5

7.7–9.9

**Inverse mass Hierarchy**

$$\left\{ m_{ee} \sim 0.03 - 0.05 \text{ eV} \right\}$$

# The path to $\theta_{13}$

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---

Lets couple a scalar field with RH neutrinos

# The path to $\theta_{13}$

---

Lets couple a scalar field with RH neutrinos



This scalar field breaks the FS at the see-saw scale



# The path to $\theta_{13}$

---

Lets couple a scalar field with RH neutrinos



This scalar field breaks the FS at the see-saw scale



At EW we have a  $Z_2$  (like in the inert case)

# The model(s)

M. Lamprea and E. Peinado (2016)

	$L_e$	$L_\mu$	$L_\tau$	$l_e^c$	$l_\mu^c$	$l_\tau^c$	$N_T$	$N_4$	$N_5$	$H$	$\eta$	$\phi$
SU(2)	2	2	2	1	1	1	1	1	1	2	2	1
$A_4$	1	1'	1''	1	1''	1'	3	1	1'	1	3	3

$$\langle \phi \rangle = (1, 0, 0)$$

$$A_4 \longrightarrow Z_2$$

In order to preserve the  $Z_2$ , only  $\eta_1$  acquire vev

$$\begin{aligned} \mathcal{L}_Y^{(A)} = & y_e L_e l_e^c H + y_\mu L_\mu l_\mu^c H + y_\tau L_\tau l_\tau^c H \\ & + y_1^\nu L_e [N_T \eta]_1 + y_2^\nu L_\mu [N_T \eta]_{1''} + y_3^\nu L_\tau [N_T \eta]_{1'} + y_4^\nu L_e N_4 H + y_5^\nu L_\tau N_5 H \\ & + M_1 N_T N_T + M_2 N_4 N_4 + y_1^N [N_T \phi]_{3_i} N_T + y_2^N [N_T \phi]_1 N_4 + y_3^N [N_T \phi]_{1''} N_5 \end{aligned}$$

# Neutrino masses

M. Lamprea and E. Peinado (2016)

$$m_D^{(A)} = \begin{pmatrix} y_1^\nu v_\eta & 0 & 0 & y_4^\nu v_h & 0 \\ y_2^\nu v_\eta & 0 & 0 & 0 & 0 \\ y_3^\nu v_\eta & 0 & 0 & 0 & y_5^\nu v_h \end{pmatrix}$$

$$M_R = \begin{pmatrix} M_1 & 0 & 0 & y_2^N v_\phi & y_3^N v_\phi \\ 0 & M_1 & y_1^N v_\phi & 0 & 0 \\ 0 & y_1^N v_\phi & M_1 & 0 & 0 \\ y_2^N v_\phi & 0 & 0 & M_2 & 0 \\ y_3^N v_\phi & 0 & 0 & 0 & 0 \end{pmatrix}$$

# Neutrino masses

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Effectively only 3 RHN participate in the see-saw

# Neutrino masses

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Effectively only 3 RHN participate in the see-saw

Two zero-texture B3

$$m_\nu^{(A)} \equiv \begin{pmatrix} a & 0 & b \\ 0 & 0 & c \\ b & c & d \end{pmatrix}$$

Frampton, Glashow, Marfatia  
 Merle, Rodejohan  
 Xing, Fritsch  
 Ludl, Morisi, Peinado  
 Meroni, Meloni, Peinado  
 ...

# Neutrino masses

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$$m_D^{(A)} = \begin{pmatrix} y_1^\nu v_\eta & 0 & 0 & y_4^\nu v_h & 0 \\ y_2^\nu v_\eta & 0 & 0 & 0 & 0 \\ y_3^\nu v_\eta & 0 & 0 & 0 & y_5^\nu v_h \end{pmatrix} \quad M_R = \begin{pmatrix} M_1 & 0 & 0 & y_2^N v_\phi & y_3^N v_\phi \\ 0 & M_1 & y_1^N v_\phi & 0 & 0 \\ 0 & y_1^N v_\phi & M_1 & 0 & 0 \\ y_2^N v_\phi & 0 & 0 & M_2 & 0 \\ y_3^N v_\phi & 0 & 0 & 0 & 0 \end{pmatrix}$$

Effectively only 3 RHN participate in the see-saw

$$m_\nu^{(A)} \equiv \begin{pmatrix} a & 0 & b \\ 0 & 0 & c \\ b & c & d \end{pmatrix}$$

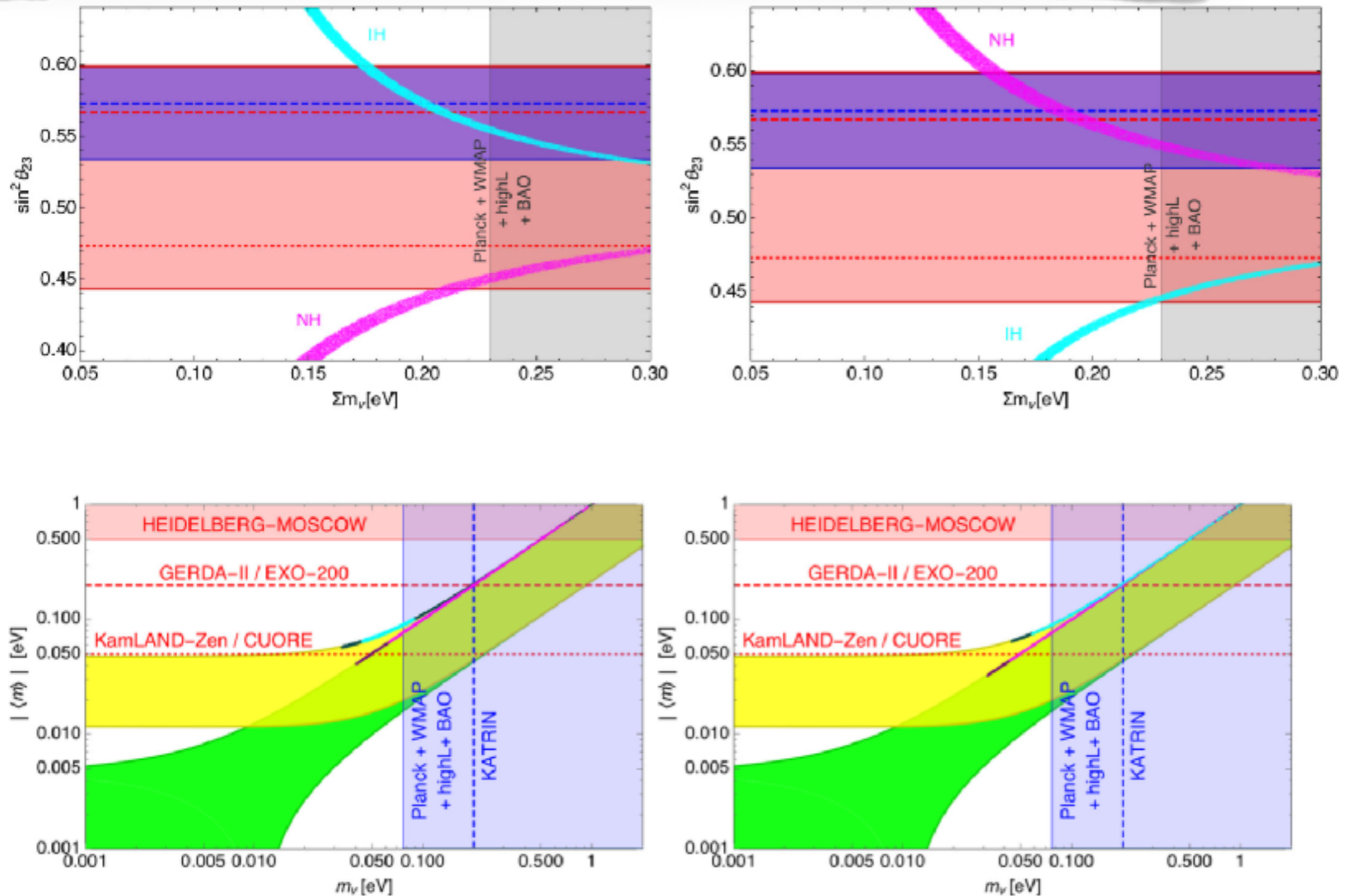
If N5 is 1"

$$m_\nu^{(B)} \equiv \begin{pmatrix} a & b & 0 \\ b & d & c \\ 0 & c & 0 \end{pmatrix}$$

Ludl, Morisi, Peinado  
Meroni, Meloni, Peinado  
...

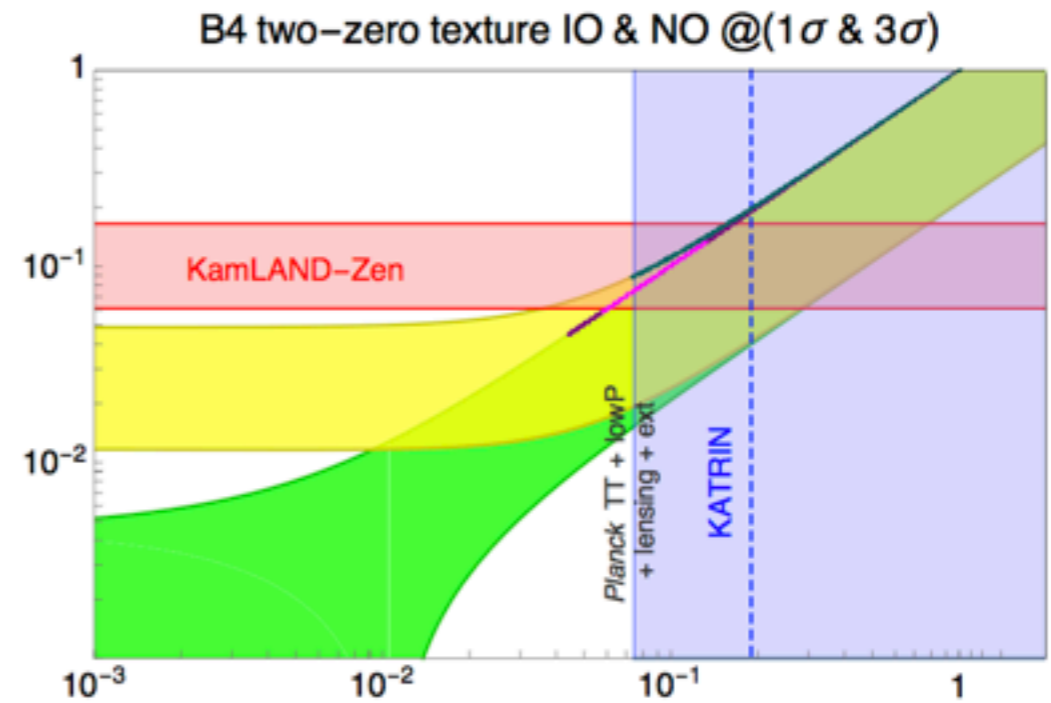
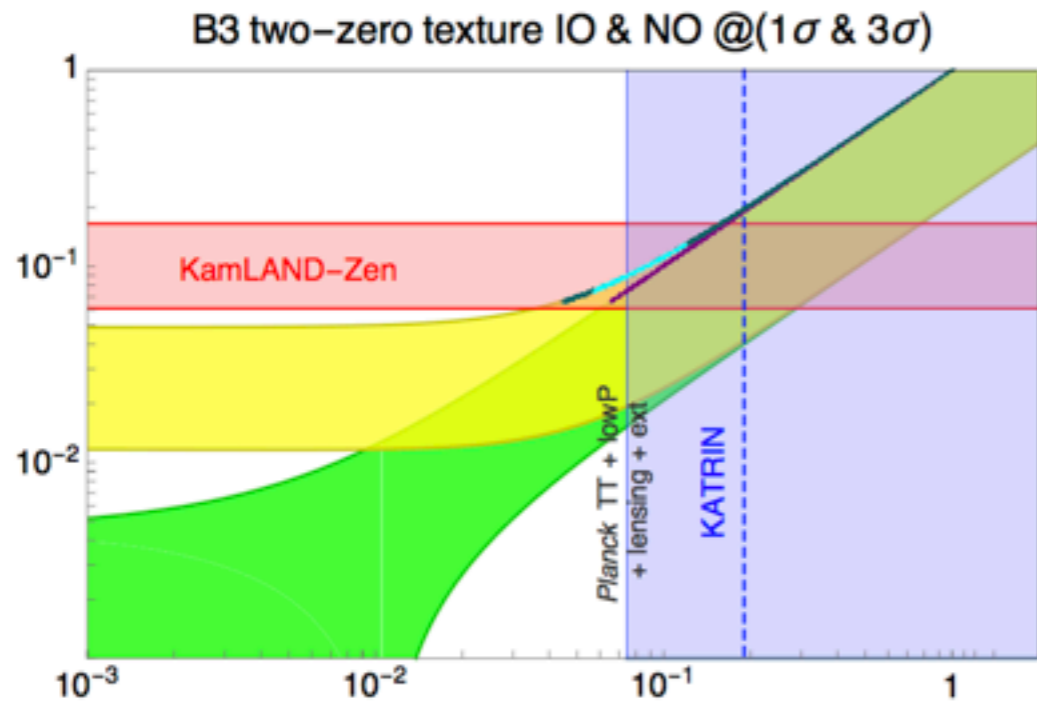
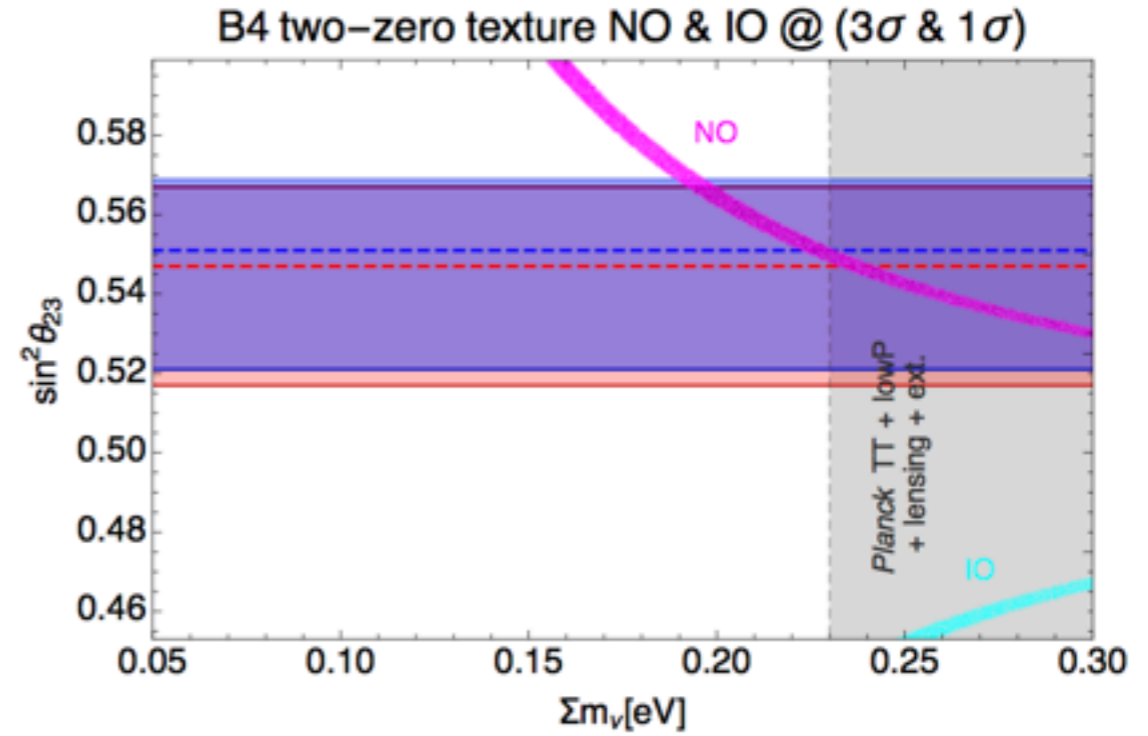
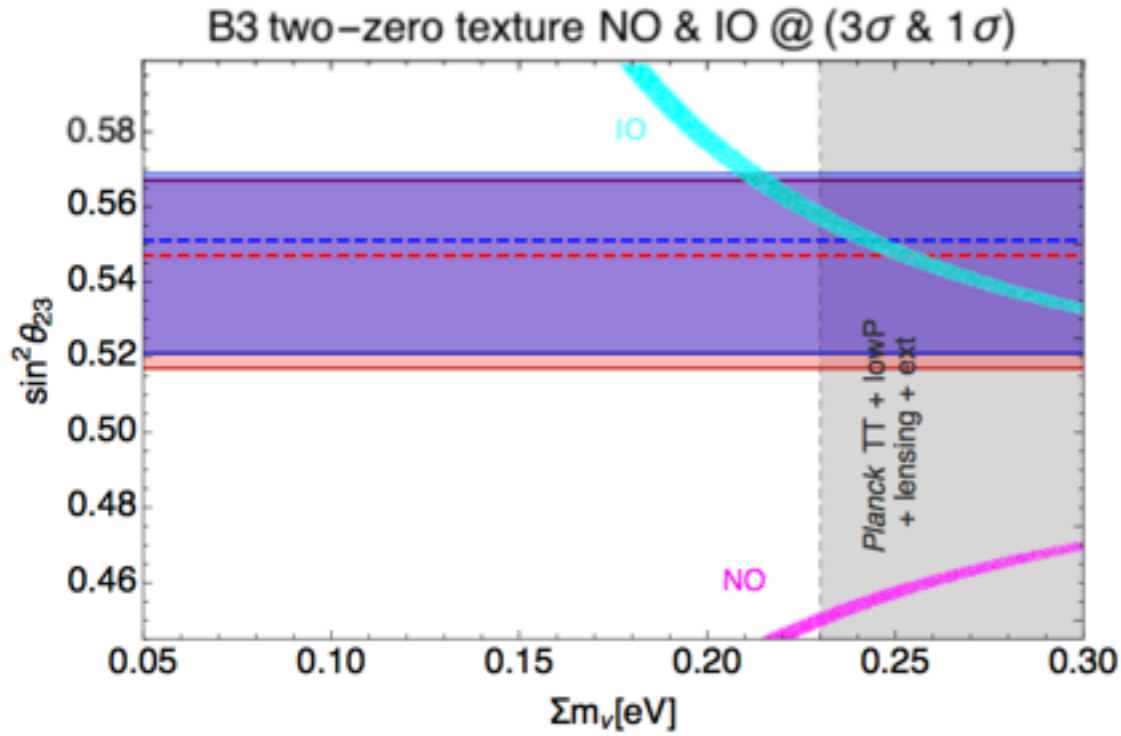
# Neutrino Phenomenology

Data from D.V.Forero, M.Tortola and J.W.F.Valle, Phys.Rev.D90(2014)9,093006



# Updated

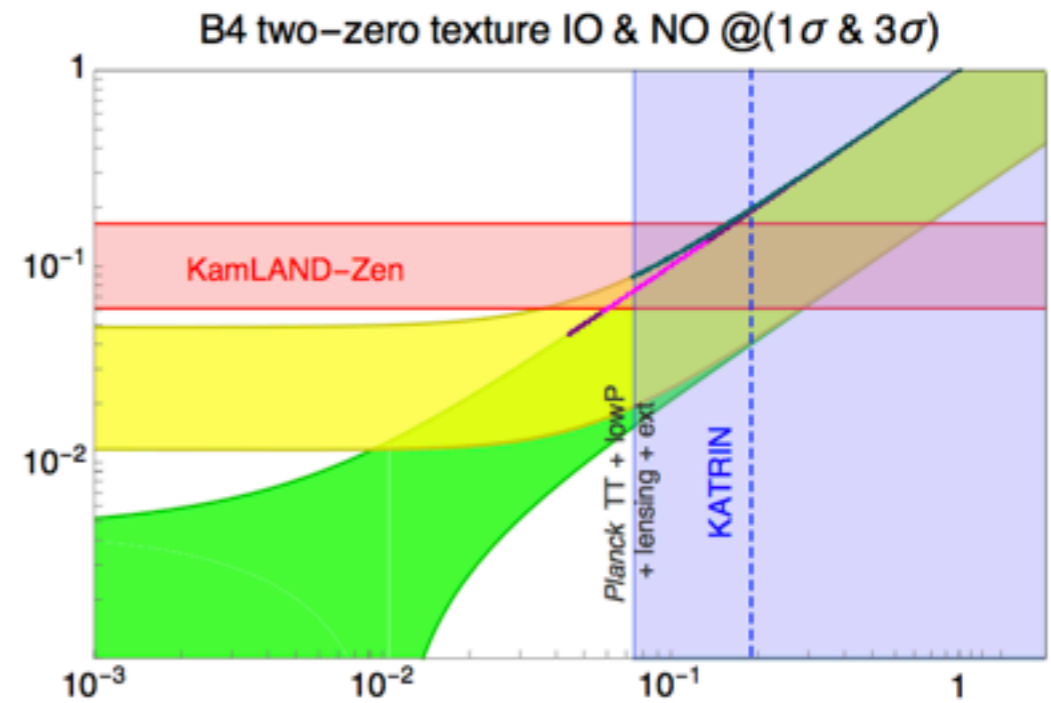
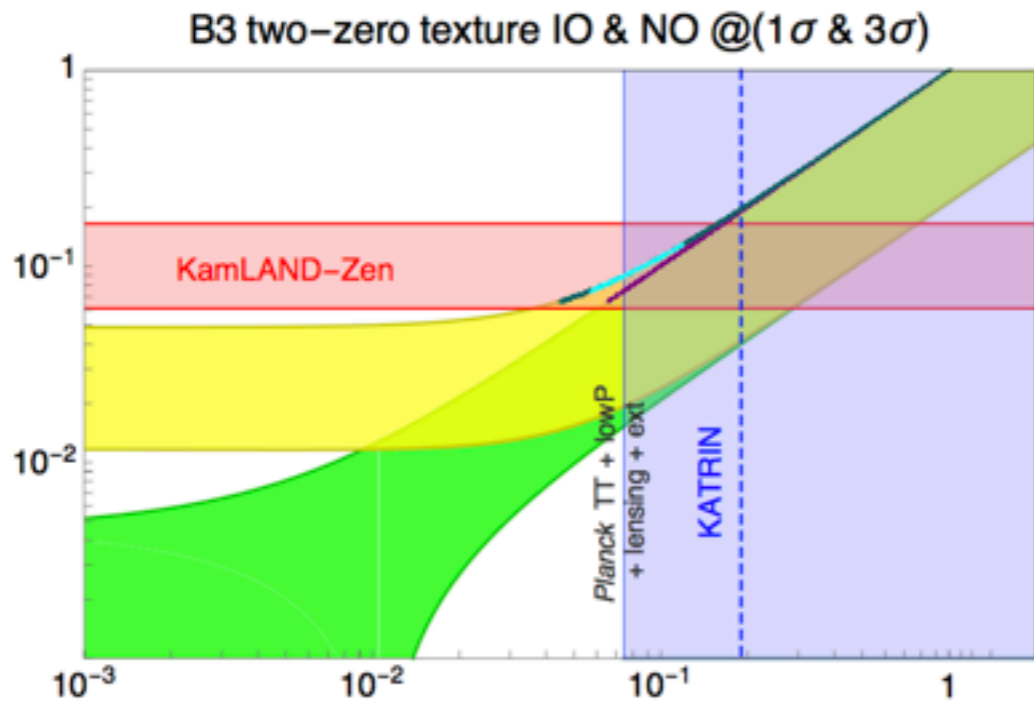
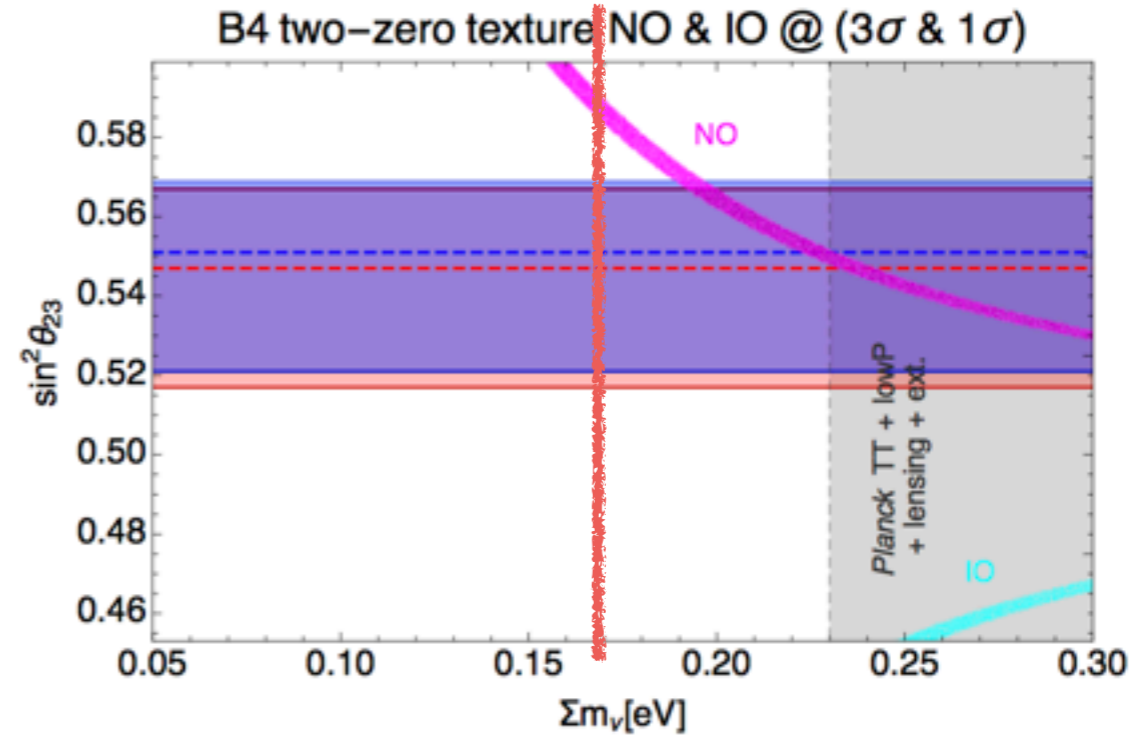
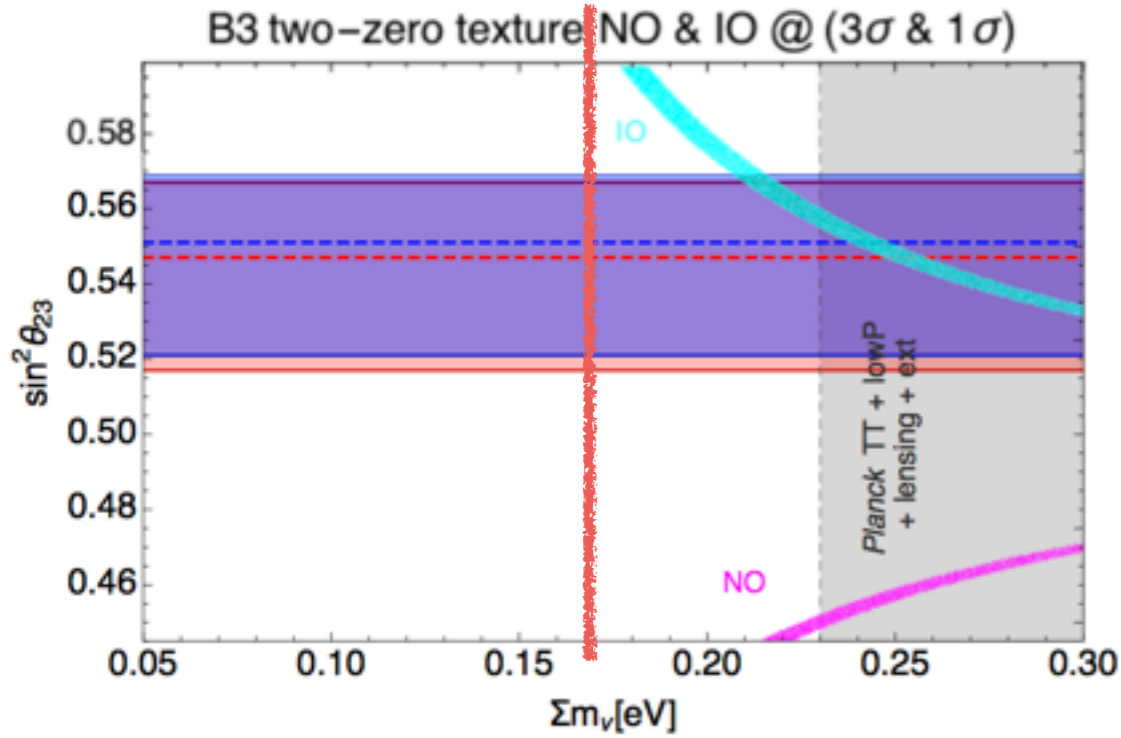
de Salas, Forero, Ternes, Tortola, Valle (2018)





# Updated

de Salas, Forero, Ternes, Tortola, Valle (2018)



# Summary

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- ❑ Neutrino pheno “compatible” with DDM
- ❑ The atmospheric mixing angle correlates with neutrino masses
- ❑ Neutrinoless double beta decay lower bound also for NH
- ❑ Barion assymetry?

**Thank you and  
Let's the game begin!!!!!!**

