Several Problems in Particle Physics and Cosmology Solved in One SMASH

Inflation, matter-anti-matter asymmetry, dark matter, neutrino oscillations, strong CP problem

Andreas Ringwald FLASY 2018 Basel, 2-5 July 2018

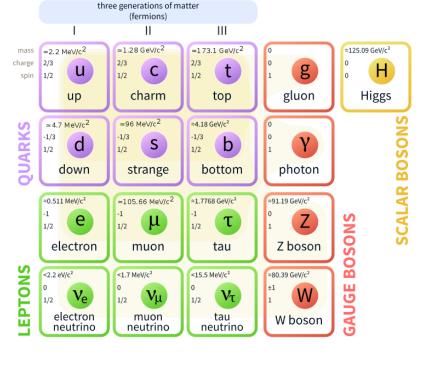




Introduction

Strong case for physics beyond the Standard Model

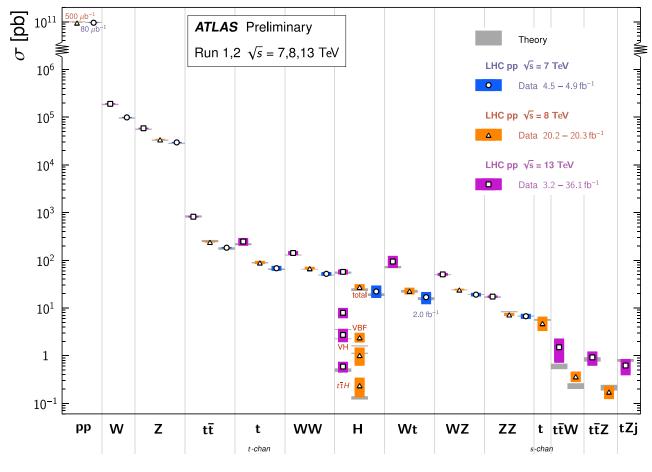
 Standard Model (SM) describes interactions of all known particles with remarkable accuracy



Standard Model of Elementary Particles

[Wikipedia]



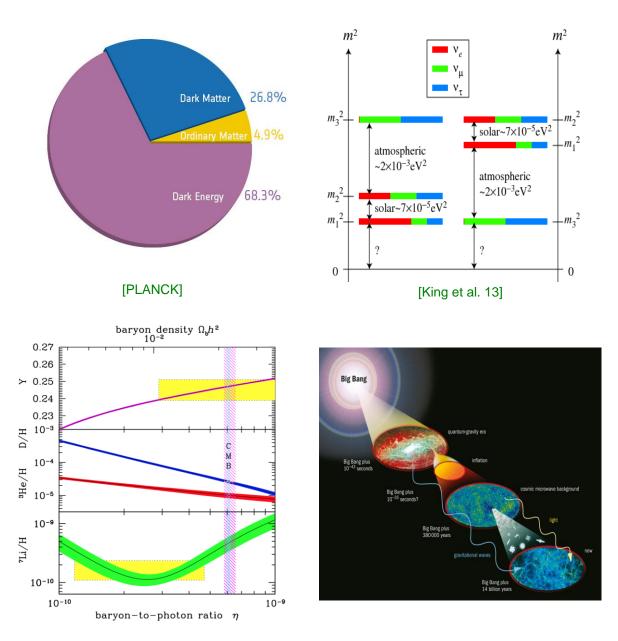


[twiki.cern.ch]

Introduction

Strong case for physics beyond the Standard Model

- Observations in particle physics, astrophysics and cosmology strongly suggest physics beyond the SM
 - Dark matter
 - Neutrino masses and mixing
 - Baryon asymmetry
 - Inflation
 - Strong CP problem



[Rev. Part. Phys. 18]

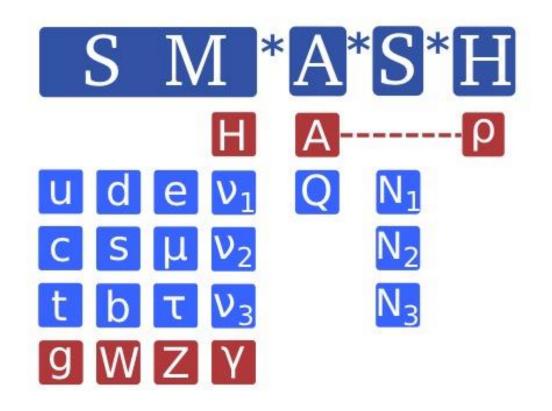
[physicsworld.com]

Introduction

Strong case for physics beyond the Standard Model

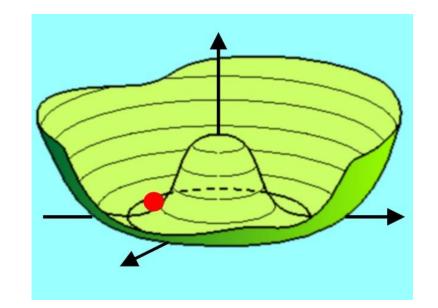
- Observations in particle physics, astrophysics and cosmology strongly suggest physics beyond the SM
 - Dark matter
 - Neutrino masses and mixing
 - Baryon asymmetry
 - Inflation
 - Strong CP problem
- These problems may be intertwined in a minimal way, with a solution pointing to a new physics scale between $10^{9-11} \, {\rm GeV}$

[Ballesteros, Redondo, AR, Tamarit, 1608.05414; 1610.01639]



UV completions yielding axion

- A singlet complex scalar field $\sigma,$ featuring a global $\,U(1)_{\rm PQ}\,$ symmetry, is added to SM
- Symmetry is broken by vev $\langle |\sigma|^2 \rangle = v_{PQ}^2/2$ $\sigma(x) = \frac{1}{\sqrt{2}} \left(v_{PQ} + \rho(x) \right) e^{iA(x)/v_{PQ}}$
 - Excitation of modulus: $m_{
 ho} \sim v_{
 m PQ}$
 - Excitation of phase: NGB $m_A = 0$

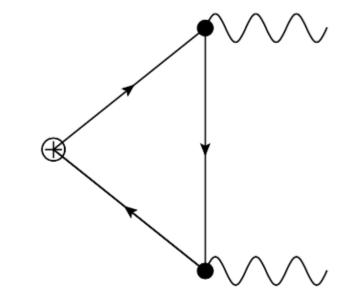


[Raffelt]

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- Colored fermions (SM or extra) carry PQ charges such that $U(1)_{PQ}$ is broken due to gluonic triangle anomaly:

$$\partial_{\mu} J^{\mu}_{U(1)_{\mathrm{PQ}}} \supset -\frac{\alpha_s}{8\pi} N \, G^b_{\mu\nu} \tilde{G}^{b,\mu\nu}$$



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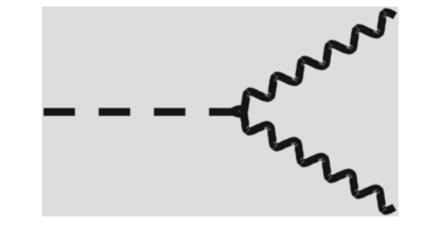
$$\partial_{\mu} J^{\mu}_{U(1)_{\mathrm{PQ}}} \supset -\frac{\alpha_s}{8\pi} N \, G^b_{\mu\nu} \tilde{G}^{b,\mu\nu}$$

• Low energy effective field theory at energies above $\Lambda_{\rm QCD}$ but below $v~(\ll v_{\rm PQ})$: [Peccei,Quinn 77; Weinberg 78; Wilczek 78]

$$\mathcal{L} \supset -\frac{\alpha_s}{8\pi} \,\theta(x) \, G^b_{\mu\nu} \tilde{G}^{b,\mu\nu} \,; \qquad \theta(x) = A(x)/f_A \,; \qquad f_A = v_{\rm PQ}/N$$

[Kim 79;Shifman,Vainshtein,Zakharov 80;Zhitnitsky 80;Dine,Fischler,Srednicki 81;...]

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Axion couplings to SM at energies below QCD scale

$$\mathcal{L} \supset \frac{1}{2} \partial_{\mu} A \partial^{\mu} A - \frac{1}{2} m_{A}^{2} A^{2} - \frac{\alpha}{8\pi} \frac{C_{A\gamma}}{f_{A}} A F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{C_{Af}}{f_{A}} \partial_{\mu} A \ \overline{\psi}_{f} \gamma^{\mu} \gamma_{5} \psi_{f}$$
Axion mass:
$$m_{A} = 57.0(7) \left(\frac{10^{11} \,\text{GeV}}{f_{A}}\right) \mu \text{eV}$$

[Grilli di Cortona et al. `16; Borsanyi et al. `16]

• Couplings of axion to SM suppressed by powers of

$$f_A = v_{\rm PQ}/N \gg v = 246 \,\mathrm{GeV}$$

rendering the axion "invisible"

- Photon coupling: $C_{A\gamma} = \frac{E}{N} 1.92(4)$
- Nucleon couplings:

[Kim 79;Shifman,Vainshtein,Zakharov 80;Zhitnitsky 80;Dine,Fischler,Srednicki 81;...]

[Kaplan 85;Srednicki `85]

[Grilli di Cortona et al. `16]

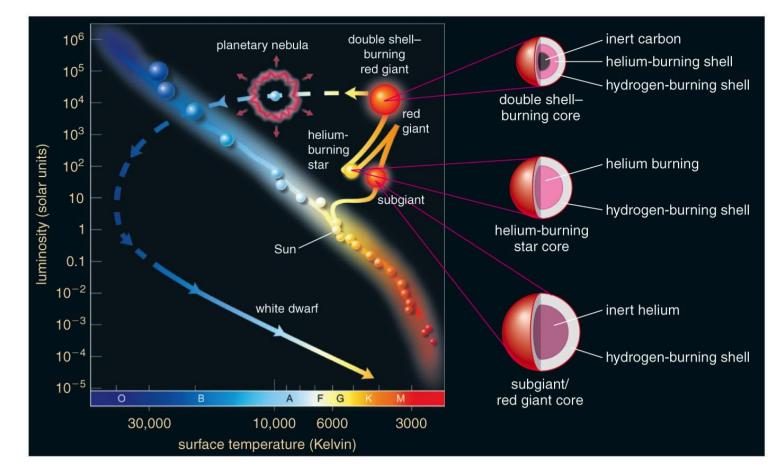
$$C_{Ap} = -0.47(3) + 0.88(3)C_{Au} - 0.39(2)C_{Ad} - 0.038(5)C_{As}$$
$$- 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At},$$
$$C_{An} = -0.02(3) + 0.88(3)C_{Ad} - 0.39(2)C_{Au} - 0.038(5)C_{As}$$
$$- 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At}$$

• Electron coupling very model-dependent

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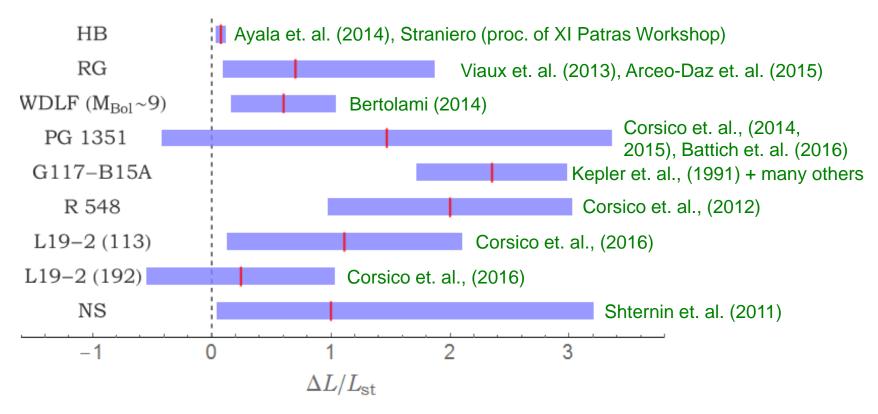
Excessive stellar energy losses

 Evolution of stars (Main Sequence – Red-Giant (RG) – Helium Burning (HB) – White Dwarf (WD)) sensitive to non-SM energy losses



Excessive stellar energy losses

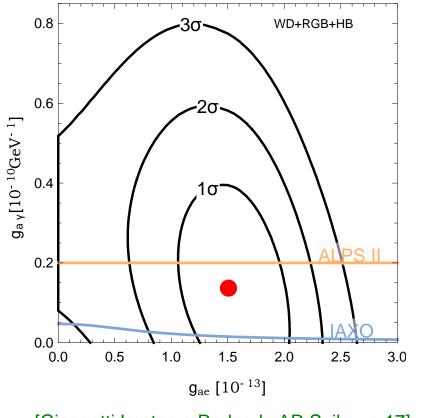
• Practically every stellar systems seems to be cooling faster than predicted by models:

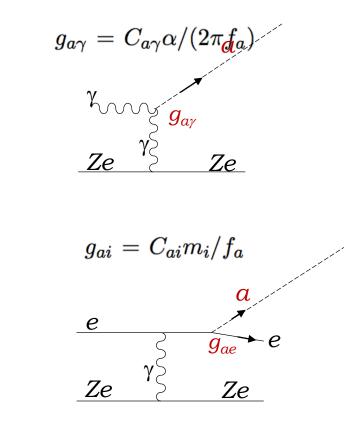


[Giannotti, Irastorza, Redondo, AR '15; Giannotti, Irastorza, Redondo, AR, Saikawa '17]

Excessive stellar energy losses

 Excessive energy losses of HBs, RG, WDs can be explained at one stroke by production of axion/ALP with coupling to photons and electrons:



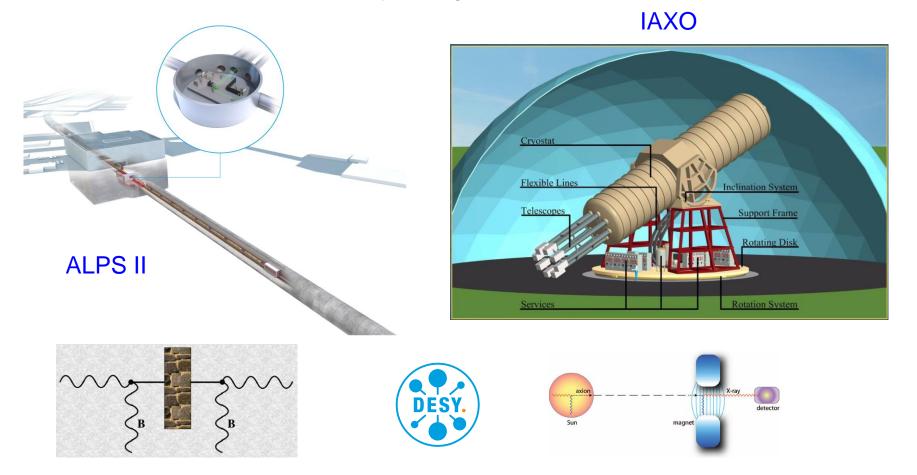


[Giannotti,Irastorza,Redondo,AR,Saikawa 17]

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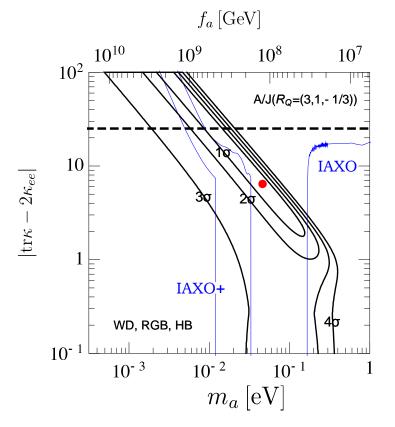
Excessive stellar energy losses

• Excessive energy losses of HBs, RG, WDs can be explained at one stroke by production of axion/ALP with coupling to photons and electrons and probed by next generation experiments:



Excessive stellar energy losses

• Excessive energy losses of HBs, RG, WDs can be explained at one stroke by production of axion/ALP with coupling to photons and electrons, e.g. KSVZ axion/majoron model [Shin `88]



$$C_{a\gamma} = \frac{2}{3} - 1.92(4)$$

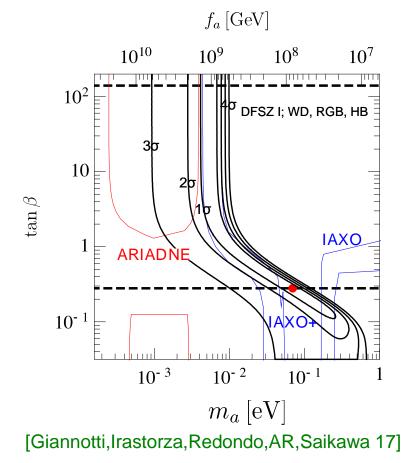
$$C_{ae}^{A/J} \simeq -\frac{1}{16\pi^2 N} \left(\mathrm{tr}\kappa - 2\kappa_{ee} \right)$$

$$\kappa \equiv \frac{m_D m_D^{\dagger}}{v^2}$$

[Giannotti,Irastorza,Redondo,AR,Saikawa 17]

Excessive stellar energy losses

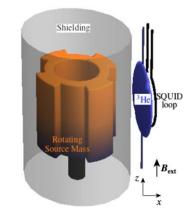
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$$f_a = \frac{v_{\mathrm{PQ}}}{6}, \quad \tan\beta = \frac{v_u}{v_d}$$

$$C_{a\gamma} = \frac{8}{3} - 1.92(4), \quad C_{ae} = \frac{1}{3}\sin^2\beta$$

ARIADNE



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Exploiting modulus of PQ field or mixture of it with Higgs modulus to solve horizon and flatness puzzle

• Take into account non-minimal coupling of Higgs and PQ field to gravity, $[Factor = 10^{-1}]$

$$S \supset -\int d^4x \sqrt{-g} \left[\frac{M^2}{2} + \xi_H H^{\dagger} H + \xi_\sigma \sigma^* \sigma \right] R; \quad M_P^2 = M^2 + \xi_H v^2 + \xi_\sigma v_\sigma^2$$

• Generated anyway radiatively even if set to zero at some scale

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- Non-minimal couplings stretch scalar potential in Einstein frame: makes it convex and asymptotically flat at large field values

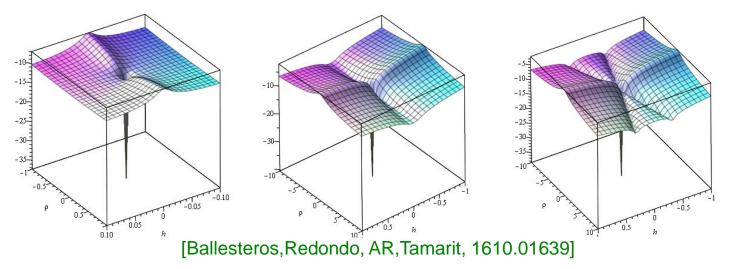
$$\tilde{V}(h,\rho) = \frac{1}{\Omega^4(h,\rho)} \left[\frac{\lambda_H}{4} \left(h^2 - v^2 \right)^2 + \frac{\lambda_\sigma}{4} \left(\rho^2 - v_\sigma^2 \right)^2 + \frac{\lambda_{H\sigma}}{2} \left(h^2 - v^2 \right) \left(\rho^2 - v_\sigma^2 \right) \right]$$
$$\tilde{g}_{\mu\nu} = \Omega^2(h,\rho) g_{\mu\nu} \qquad \qquad \Omega^2 = 1 + \frac{\xi_H(h^2 - v^2) + \xi_\sigma(\rho^2 - v_\sigma^2)}{M_P^2}$$

Exploiting modulus of PQ field or mixture of it with Higgs modulus to solve horizon and flatness puzzle

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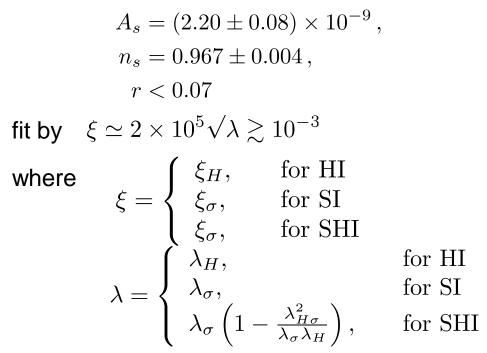
- Generated anyway radiatively even if set to zero at some scale
- Non-minimal couplings stretch scalar potential in Einstein frame; makes it convex and asymptotically flat at large field values
- Potential has valleys = attractors for Higgs Inflation (HI), Saxion Inflation (SI) or mixed Saxion/Higgs Inflation (SHI), depending on relative signs of $\kappa_H \equiv \lambda_{H\sigma}\xi_H \lambda_H\xi_\sigma$, $\kappa_\sigma \equiv \lambda_{H\sigma}\xi_\sigma \lambda_\sigma\xi_H$



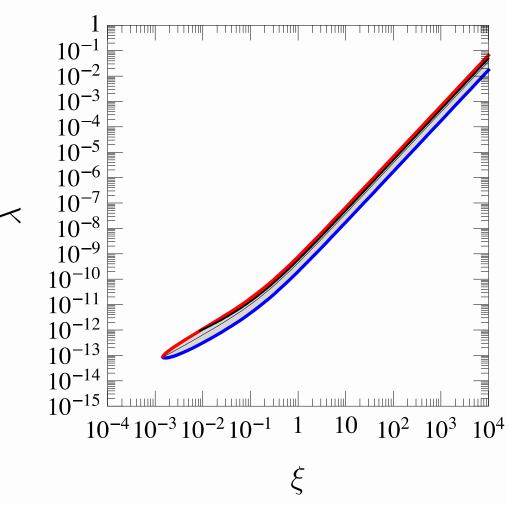
$\operatorname{sign}(\kappa_H)$	$\operatorname{sign}(\kappa_{\sigma})$	Inflation
+	_	HI
—	+	SI
	_	SHI

Exploiting modulus of PQ field or mixture of it with Higgs modulus to solve horizon and flatness puzzle

Characteristics of primordial density fluctuations
 inferred from CMB fluctuations



- HI has unitarity problem
- SI and SHI have no unitarity problem if $\lambda_{\sigma}, \tilde{\lambda}_{\sigma} \lesssim 10^{-10}$



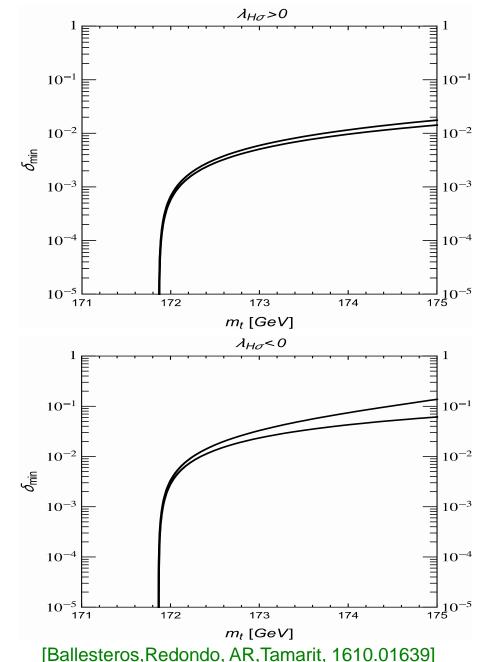
[Ballesteros, Redondo, AR, Tamarit, 1610.01639]

Modulus of PQ field or mixture with Higgs modulus as inflaton

- Stability up to Planck scale?
 - SM-singlet scalar $\sigma\,$ helps to stabilize scalar potential in Higgs direction through threshold effect associated with Higgs portal
 - When ρ integrated out, Higgs portal gives negative contribution to Higgs quartic,

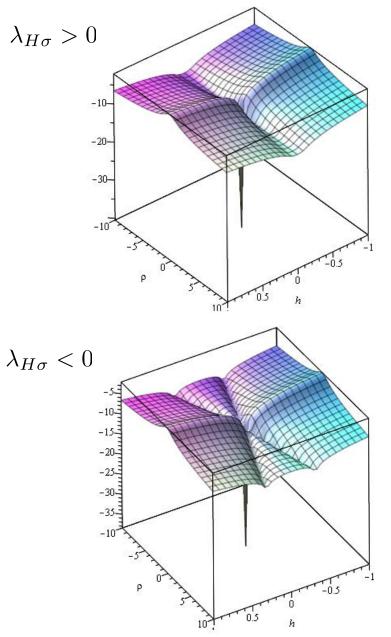
$$\overline{\lambda}_H(m_h) = \lambda_H - \lambda_{H\sigma}^2 / \lambda_\sigma \big|_{\mu=m_h}$$

- At energies above $m_{\rho},$ true (and larger!) value of λ_{H} is revealed by integrating $\rho~$ in
- Stability up to Planck scale ensured if $\delta = \lambda_{H\sigma}^2 / \lambda_\sigma |_{\mu=m_h}$ exceeds a minimum value dependent on top mass



Modulus of PQ field or mixture with Higgs modulus as inflaton

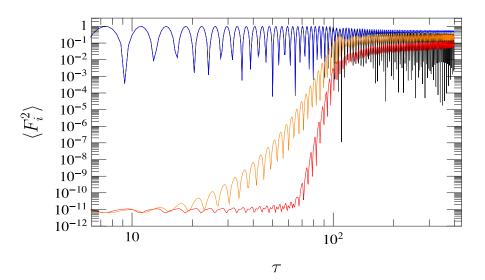
- Both in SI and SHI with $\xi_{\sigma} \lesssim 1$, slow-roll inflation ends at a value of $\rho \sim \mathcal{O}(M_P)$
- Inflaton starts to undergo Hubble-damped oscillations in a quasi-quartic potential, with Universe expanding as in a radiation-dominated era

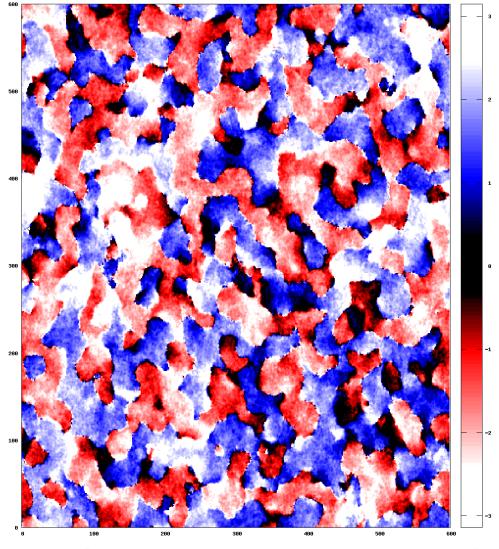


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- For $f_A \lesssim 10^{16} \, {
 m GeV}$, PQ symmetry restored after few oscillations and then broken again

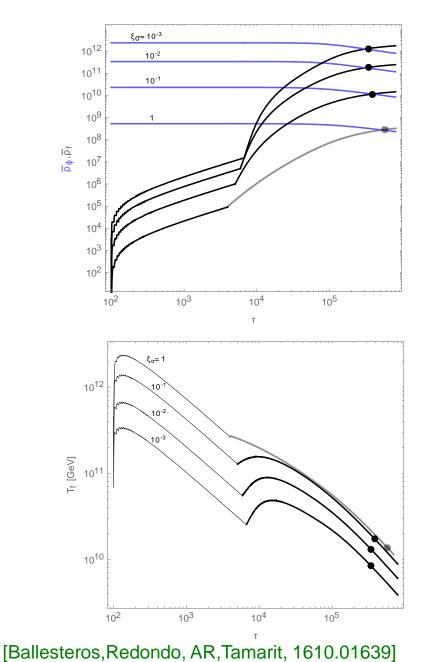




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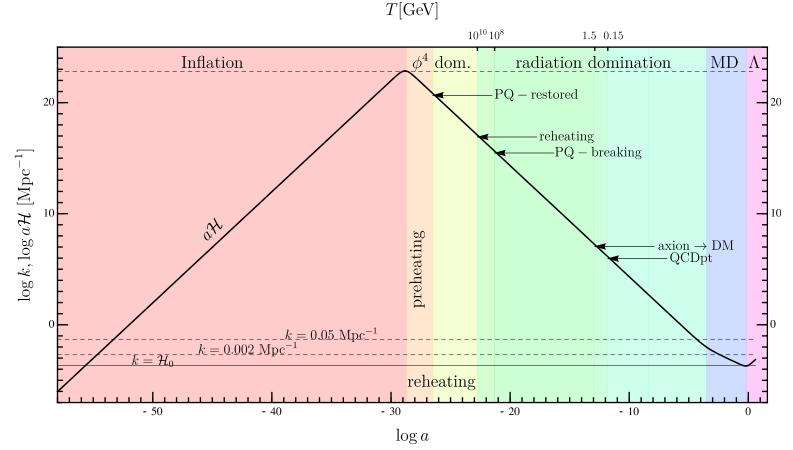
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- For $f_A \lesssim 10^{16} \, {
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- SI: Large induced particle masses quench inflaton decays or annihilations into SM particles $T_R \sim 10^7 \,\text{GeV} v_{11} \lambda_{10}^{3/8} \delta_3^{-1/8} \ \Delta N_{\nu}^{\text{eff}} \sim (\delta_3 v_{11}/\lambda_{10})^{-1/6}$
- SHI: Higgs component of inflaton allows for production of SM gauge bosons $T_R \sim 10^{10} \,\mathrm{GeV}$ $\Delta N_{\nu}^{\mathrm{eff}} \simeq 0.0268 \,\left(rac{427/4}{g_{*s}(T_A^{\mathrm{dec}})}
 ight)^{4/3}$



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Modulus of PQ field or mixture with Higgs modulus as inflaton

• Expansion and thermal history of universe predicted

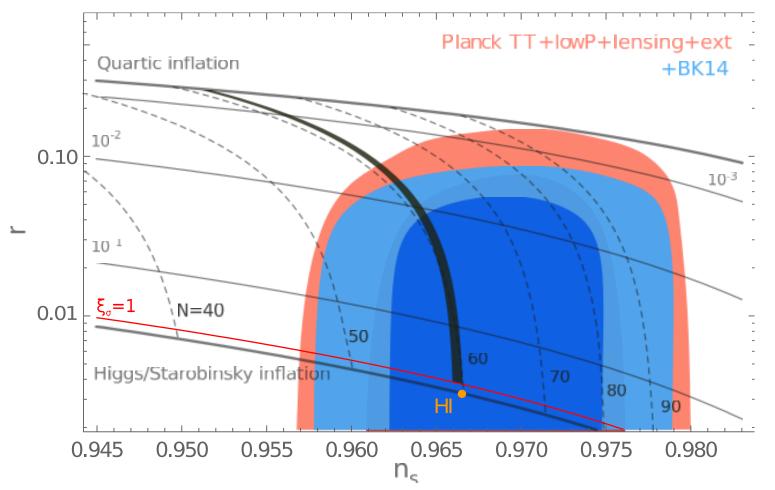


• Number of e-folds N(k) from the time a given comoving scale k leaves horizon until end of inflation predicted

[Ballesteros, Redondo, AR, Tamarit, 1610.01639]

Modulus of PQ field or mixture with Higgs modulus as inflaton

• Sharp prediction of r vs n_s :

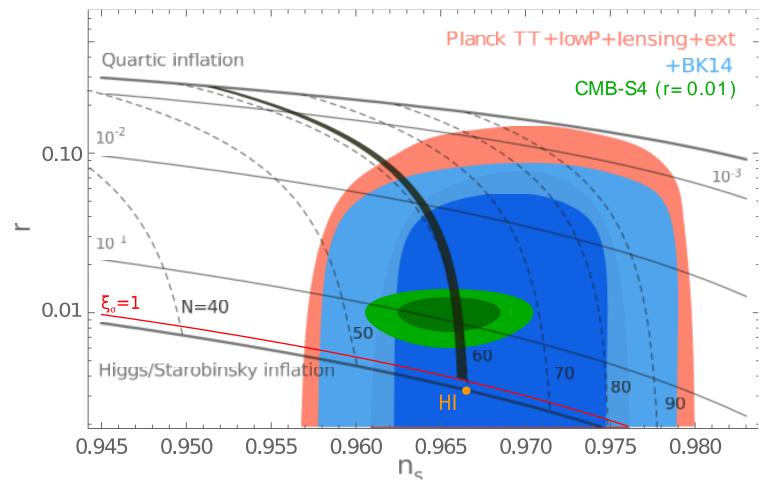


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Modulus of PQ field or mixture with Higgs modulus as inflaton

• Sharp prediction of r vs n_s can be probed by upcoming CMB experiments (e.g. CMB-S4):



[Ballesteros, Redondo, AR, Tamarit, 1610.01639]

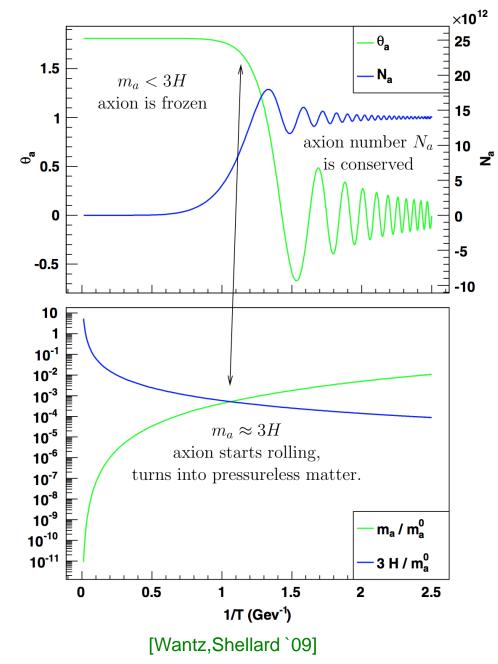
Predictions of post-inflationary PQ SB scenario

• PQ phase transition takes place at

 $T \lesssim T_c^{\rm PQ} \sim v_{\rm PQ} = N f_A$

- Axion takes random initial values in causally connected domains
- Later when $H(T) \sim m_A(T)$, axion field starts to oscillate around minimum of potential; behaves like cold dark matter: $w_A = p_A/\rho_A \simeq 0$

[Preskill,Wise,Wilczek 83; Abbott,Sikivie 83; Dine,Fischler 83,....]

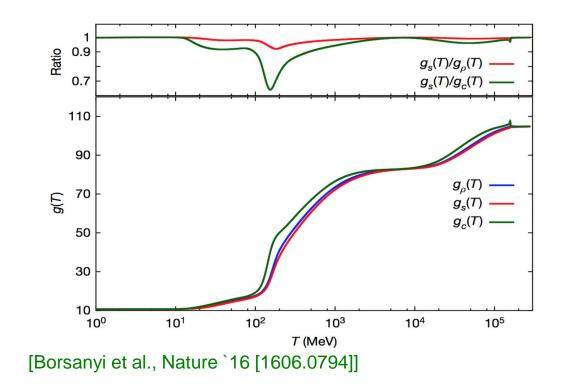


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- QCD input from lattice:
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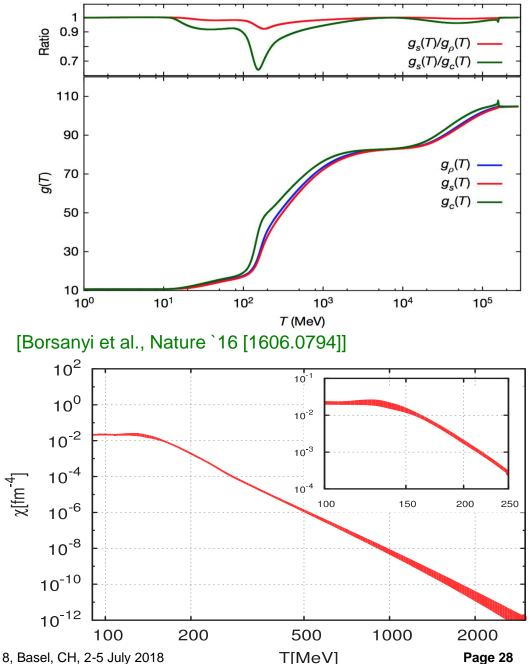


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 - Topological susceptibility $\Rightarrow m_A(T) = \frac{\sqrt{\chi(T)}}{f_A}$



Predictions of post-inflationary PQ SB scenario

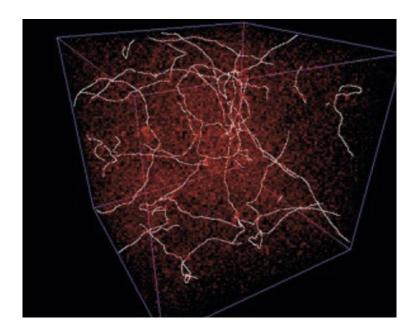
• Averaging over random initial axion field values

$$\Omega_A^{(\mathrm{VR})} h^2 = (3.8 \pm 0.6) \times 10^{-3} \left(\frac{f_A}{10^{10} \,\mathrm{GeV}}\right)^{1.165}$$

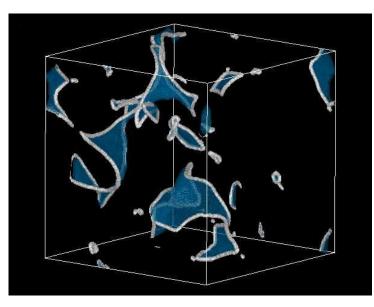
• Does not exceed observed CDM abundance for

 $m_A > 28(2)\,\mu\text{eV}$

- Axions also produced by collapse of network of topological defects strings and domain-walls
 - Need field theoretic simulations to determine their contribution to dark matter



[Hiramatsu et al.]



Predictions of post-inflationary PQ SB scenario

• For N = 1, exploiting results from field theoretic lattice simulations, updated to latest determination of topological susceptibility, find CDM explained for [Hiramatsu et al. 11,12]

 $f_A \approx (3.8 - 9.9) \times 10^{10} \,\text{GeV} \quad \Leftrightarrow \quad m_A \approx (58 - 150) \,\mu\text{eV}$

- [Hiramatsu et al. 11,12,13; Kawasaki,Saikawa,Segikuchi 15; Borsanyi et al. 16; Ballesteros et al. 16]
- Still large unknown theoretical error because simulations can be done only at unrealistic values of the string tension

[Gorghetto,,Hardy,Villadoro.18]

• Result from new simulation technique designed to work directly at high string tension:

 $m_A = (26.2 \pm 3.4) \,\mu \mathrm{eV}$ [K]

[Klaer,Moore `17]

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m eV}$ [Klaer,Moore `17]

• For N > 1, domain wall problem can be avoided if PQ symmetry explicitly broken, e.g. by Planck suppressed operators, $\mathcal{L} \supset gM_{\rm P}^4 (\sigma/M_{\rm P})^{\mathcal{N}} + \text{h.c.}$, for $\mathcal{N} = 9, 10$,

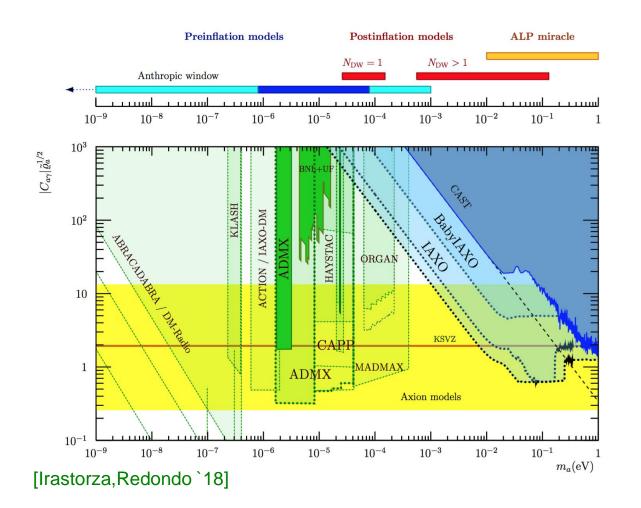
 $4.4 \times 10^7 (1.3 \times 10^9) \,\text{GeV} < f_A < 1 \times 10^{10} \,\text{GeV} \iff 0.56 \,\text{meV} < m_A < 130 \,(4.5) \,\text{meV}$ [Kawasaki,Saikawa,Sekiguchi `15;

AR,Saikawa `16]

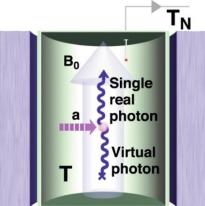
- May postulate discrete symmetry to forbid lower dimensional operators e.g. [Dias et al. `14]
- Axion n this mass range may explain excessive stellar energy losses [Giannotti,Irastorza,Redondo,AR,Saikawa`17]

Predictions of post-inflationary PQ SB scenario

• Mass range will be probed in near future:



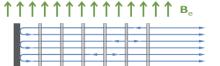




MADMAX

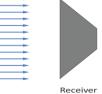


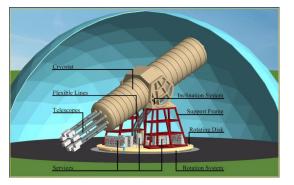
IAXO



Dielectric Disks

Mirror





DESY. Several Problems in Particle Physics and Cosmology Solved in One SMASH | Andreas Ringwald, FLASY 2018, Basel, CH, 2-5 July 2018

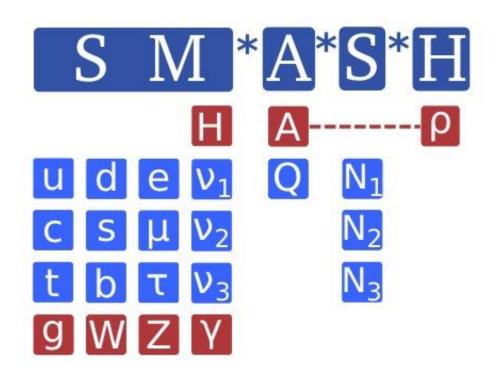
Unifying Inflation, Dark Matter, and Seesaw with PQ Field

One SM*A*S*H to rule them all ...

- Extension of SM to PQSM plus three SM singlet neutrinos, getting their Majorana masses also through PQ vev $v_{\sigma} = N f_A$
 - no strong CP problem
 - dark matter
 - inflation
 - neutrino masses and mixing
 - baryogenesis via leptogenesis

[Shin `88; Dias et al. `14; Ballesteros et al. `16]

SM*Axion*Seesaw*Higgs Portal Inflation



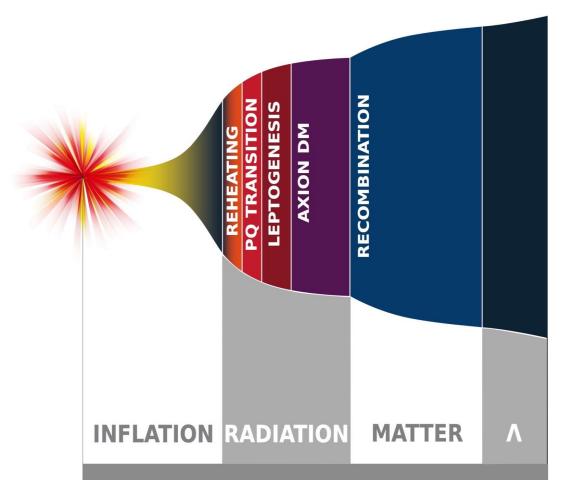
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[Shin `88; Dias et al. `14; Ballesteros et al. `16]

• Complete and consistent history of the universe from inflation to now



[desy.de]

Summary

- PQ extensions of SM very attractive:
 - Axion solves strong CP puzzle
 - Axion is dark matter candidate (for $f_A \gtrsim 10^8 \,\mathrm{GeV} \, \Leftrightarrow m_A \lesssim 60 \,\mathrm{meV}$)
 - Saxion/Higgs is inflaton candidate (for $1\gtrsim\xi_\sigma\simeq 2 imes 10^5\sqrt{\lambda_\sigma}\gtrsim 10^{-3}$)
- PQSM with saxion/Higgs inflation very predictive and thus experimentally testable in near future:
 - CMB observatories: $r\gtrsim 0.004;~~\Delta N_{
 m eff}^{
 u}\gtrsim 0.03$
 - Axion dark matter experiments: $m_A \gtrsim 30 \,\mu {\rm eV}$

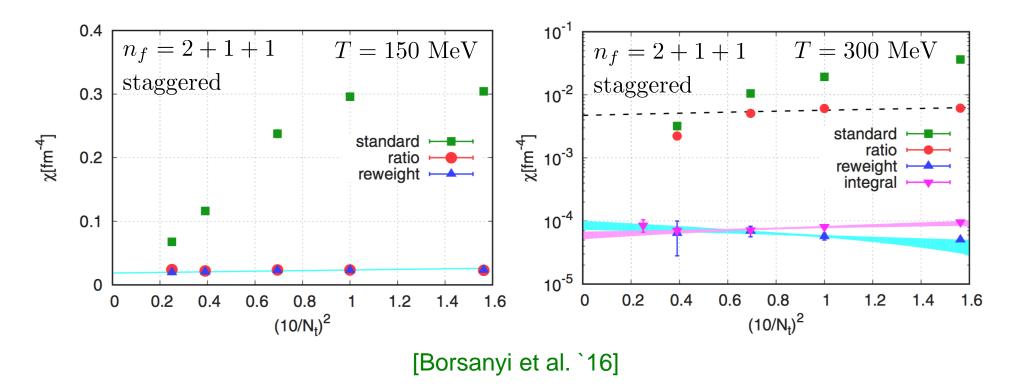
STAY TUNED!

- Topological susceptibility notoriously difficult to calculate on lattice
 - 1. Large cutoff effects when exploiting action with non-chiral quarks to calculate topo-logical observables
 - 2. Tiny topological susceptibility needs extremely long simulation threads to observe enough changes of topological sectors
- Solutions of these problems:

[Borsanyi et al. `16]

- 1. Eigenvalue reweighting technique: Substitute topology related eigenvalues of non-chiral quark Dirac operator with its corresponding eigenvalues in continuum
- 2. Fixed sector integral technique: Measure logarithmic differential of topological sus-ceptibility which is related to quantities to be measured in fixed topological sectors. Then integrate.

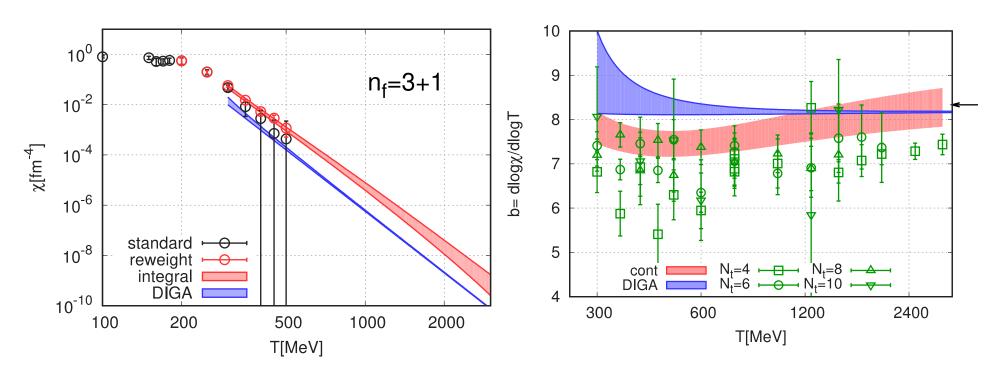
• Comparison of lattice spacing dependence of topological susceptibility determined via different methods:



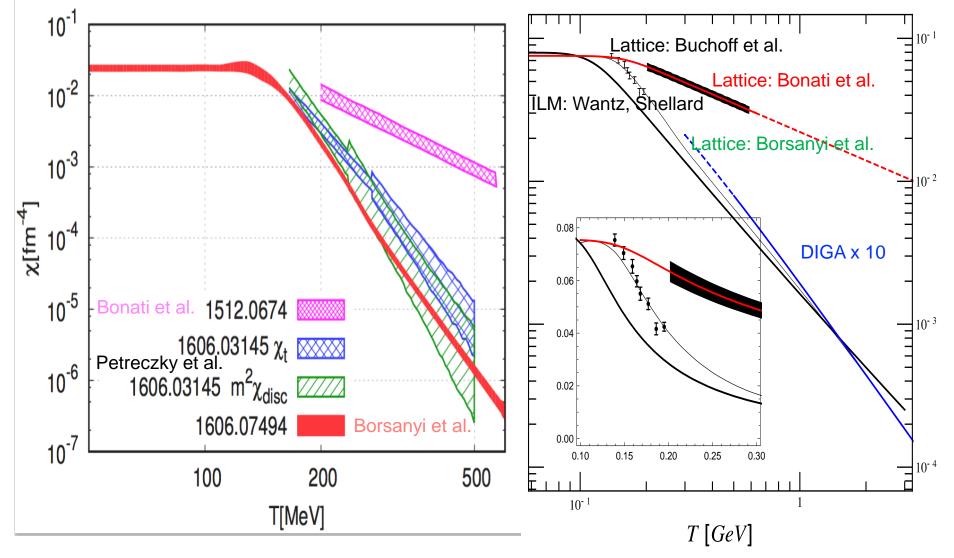
• At high temperatures, brute force ("standard") method and ratio method suffer from strong cutoff effects

• Result:

[Borsanyi et al. `16]



- Temperature slope close to dilute instanton gas approximation (DIGA)
- DIGA underestimates topological susceptibility by overall normalization "K factor" of order ten (should be improved in two-loop DIGA)



Back-Up: DM Axion Mass in Post-Inflationary PQ SB Scenario

- For $\kappa \gg 1$, string's interactions with the long range PQ field ($\propto f_A^2$) become less important relative to string evolution under tension ($\propto f_A^2 R$)
- For $\kappa \gg 1$ string behavior should approximately $\kappa \gg 1$ infinitely thin, i.e. local Nambu-Goto strin
- New method: exploit UV extension of PC theory, with additional comp-lex scalar a additional local U(1) symmetry, [Klae

$$T_{\rm str} = \pi f_A^2 \kappa$$
$$\kappa = \ln(\sqrt{2\lambda_\sigma} f_A/H)$$

For
$$\kappa \gg 1$$
 string behavior should approach that of infinitely thin, i.e. local Nambu-Goto strings
New method: exploit UV extension of PQ field theory, with additional comp-lex scalar and additional local U(1) symmetry, [Klaer,Moore `17]

$$\mathcal{L} = \mathcal{L}_{NG} + \mathcal{L}_{GS} + \mathcal{L}_{KR},$$

$$\mathcal{L}_{NG} = \bar{\kappa}\pi f_A^2 \int d\sigma \sqrt{y'^2(\sigma)(1-\dot{y}^2(\sigma))},$$

$$\mathcal{L}_{GS} = f_A^2 \int d^3x \, \partial_\mu \partial^\mu \theta,$$

$$\mathcal{L}_{KR} = \int d^3x \, A_{\mu\nu} j^{\mu\nu},$$

$$H_{\mu\nu\alpha} = f_A \epsilon_{\mu\nu\alpha\beta} \partial^\beta \theta = \partial_\mu A_{\nu\alpha} + \text{cyclic},$$

$$j^{\mu\nu} = -2\pi f_A \int d\sigma \left(v^{\mu} y'^{\nu} - v^{\nu} y'^{\mu}\right) \delta^3(x - y(\sigma))$$

$$-\mathcal{L}(\varphi_1, \varphi_2, A_{\mu}) = \frac{1}{4e^2} F_{\mu\nu} F^{\mu\nu} + \left| (\partial_{\mu} - iq_1 A_{\mu}) \varphi_1 \right|^2 + \left| (\partial_{\mu} - iq_2 A_{\mu}) \varphi_2 \right|^2$$

$$+ \frac{m_1^2}{8v_1^2} \left(2\varphi_1^* \varphi_1 - v_1^2 \right)^2 + \frac{m_2^2}{8v_2^2} \left(2\varphi_2^* \varphi_2 - v_2^2 \right)^2 + \frac{\lambda_{12}}{2} \left(2\varphi_1^* \varphi_1 - v_1^2 \right) \left(2\varphi_2^* \varphi_2 - v_2^2 \right)$$

Back-Up: DM Axion Mass in Post-Inflationary PQ SB Scenario

• Exploiting lattice results on topological susceptibility of [Borsanyi et al. `16]:

 $m_A = 26.2 \pm 3.4\,\mu\mathrm{eV}$ [Klaer,Moore `17]

 Axion production efficiency smaller than angle-average of ``realignment'' mechanism

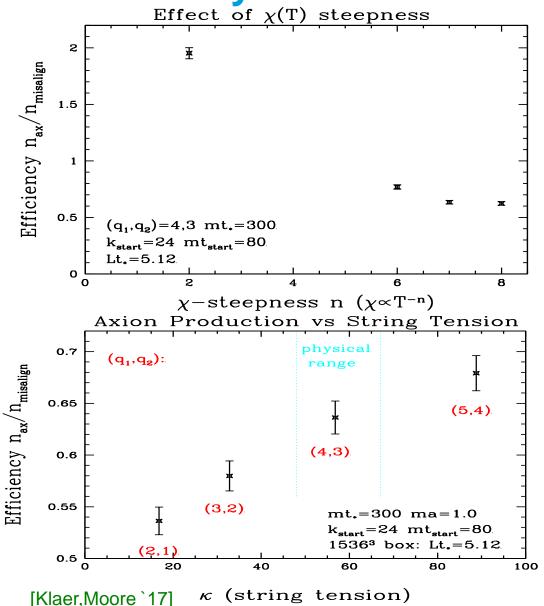
$$\Omega_A^{\rm vr} h^2 = 0.12 \, \left(\frac{29.7 \,\,\mu {\rm eV}}{m_A}\right)^{1.165}$$

• Simple sum

 $\Omega_A^{\rm tot} = \Omega_A^{\rm vr} + \Omega_A^{\rm string+wall}$

double counts

- Energy in domain walls is the energy of field misalignment, from values $\theta \sim \pi$



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[Dias et al. `14; Ballesteros et al. `16]

• SO(10) GUT SMASH?

[Ernst,AR,Tamarit `18 and in prep.]

- Minimal scalar sector predicts GUT-scale decay constant
- Need to extend scalar sector in order to accommodate smaller decay constant

Minimal $SO(10) \times U(1)_{PQ}$ models:

