

# **A detailed validation of 2 deterministic models of prompt emission: PbP and sequential emission**

**Residual temperature distributions and  
systematic behaviours of residual quantities  
following the sequential emission of  
prompt neutrons**

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# PbP and sequential emission modelings

## Similarities and differences

Both modelings work with the same fragmentation range constructed as following:

- the initial fragment mass range A is going from symmetric fragmentation up to a very asymmetric split (with a step of 1 mass unit)
- 3 or 5 charge numbers Z are considered for each A, as the nearest integer values above and below the most probable charge  $Z_p(A) = Z_{UCD}(A) + \Delta Z(A)$
- for each fragmentation (A, Z;  $A_0$ -A,  $Z_0$ -Z) the calculations are done at TKE values covering a large range, e.g. from 100 to 200 MeV, usually with a step size of 5 MeV. Step sizes of 2 MeV or 1 MeV are used, too.

Both models use the same TXE partition based on modeling at scission:

- calculation of the extra-deformation energy of fragments at scission compared to full acceleration  $\Delta E_{def} = E_{LDM}(\beta_{sciss}) - E_{LDM}(\beta_{full\ acc.})$
- partition of the available excitation energy at scission (obtained by subtracting  $\Delta E_{def}$  of the light and heavy fragments from TXE) between the nascent fragments under the assumptions :
  - statistical equilibrium at scission (equal nuclear temperatures of nascent frag.)
  - level densities of nascent fragments in the Fermi-gas regime

- PbP – the sequential emission is globally taken into account by a residual temperature distribution  $P(T)$

$$\phi(\varepsilon) = \int_0^{T_{\max}} P(T) \varphi(\varepsilon, T) dT$$

in the center-of-mass frame

$$\varphi(\varepsilon, T) = K(T) \varepsilon \sigma_c(\varepsilon) \exp(-\varepsilon/T) \quad K(T) = \left( \int_0^{\infty} \varepsilon \sigma_c(\varepsilon) \exp(-\varepsilon/T) d\varepsilon \right)^{-1}$$

with  $\sigma_c(\varepsilon)$ : optical model calc. with phenomenological potentials adequate for nuclei appearing as FF (B-G, K-D etc.) or analytical expressions or constant

[A.Tudora, F.-J.Hambsch, Eur. Phys.J A, 53 \(2017\) 159](#) and references therein

- Sequential emission treatment based on the successive equations of residual temperature

$$\overline{E}_r^{(k-1)} - S_n^{(k-1)} - \langle \varepsilon \rangle_k = a_k T_k^2$$

$\overline{E}_r^{(0)} = E^*$  of the initial fragment from the TXE partition

Solved for each emission sequence k corresponding to each initial fragment A, Z at each TKE value

All details: [A.Tudora, F.-J.Hambsch, V.Tobosaru, Eur. Phys.J A, 54\(5\) \(2018\) 87](#)

The equations of residual temperature are solved under the approximations:

- analytical expression of  $\sigma_c(\varepsilon)$   $\sigma_c(\varepsilon) = \sigma_0(1 + \alpha/\sqrt{\varepsilon})$
- non-energy dependent level density parameter of fragments  
(e.g. Egidy-Bucurescu systematic 2009 for BSFG, G-C systematic etc.)

Supported by :

- a deviation of  $\langle\varepsilon\rangle$  based on analytical  $\sigma_c(\varepsilon)$  from  $\langle\varepsilon\rangle$  based on  $\sigma_c(\varepsilon)$  from OM calculation is less than 4%
- non-energy dependent lev. dens. parameters of the EB-2009 systematic for BSFG which deviate less than 10% from the ones of the superfluid model of Ignatiuk over the entire A range, except around 130, especially at low residual excitation energies.

### Primary results of both modelings :

- **PbP** – the multi-parametric matrices of different quantities characterizing the fragments and the prompt emission  $q(A, Z, TKE)$   
(e.g.  $v(A, Z, TKE)$ ,  $E\gamma(A, Z, TKE)$ ,  $\langle\varepsilon\rangle(A, Z, TKE)$ ,  $a(A, Z, TKE)$  etc.)
- **Sequential emission** -  $q_k(A, Z, TKE)$  averaged over the number of sequences, i.e.

$$\bar{q}(A, Z, TKE) = \frac{1}{k_{\max}(A, Z, TKE)} \sum_{k=1}^{k_{\max}} q_k(A, Z, TKE)$$

## I. First validation, i.e. of the prompt emission model itself

It consists of the comparison of multi-parametric matrices  $q(A, TKE)$  with the existing experimental data (e.g.  $v(A, TKE)$ ,  $E\gamma(A, TKE)$  etc.)

In this case the  $Y(A, TKE)$  distributions **are not involved**.

## II. Second validation, i.e. of a prompt emission model together with the $Y(A, TKE)$ distribution

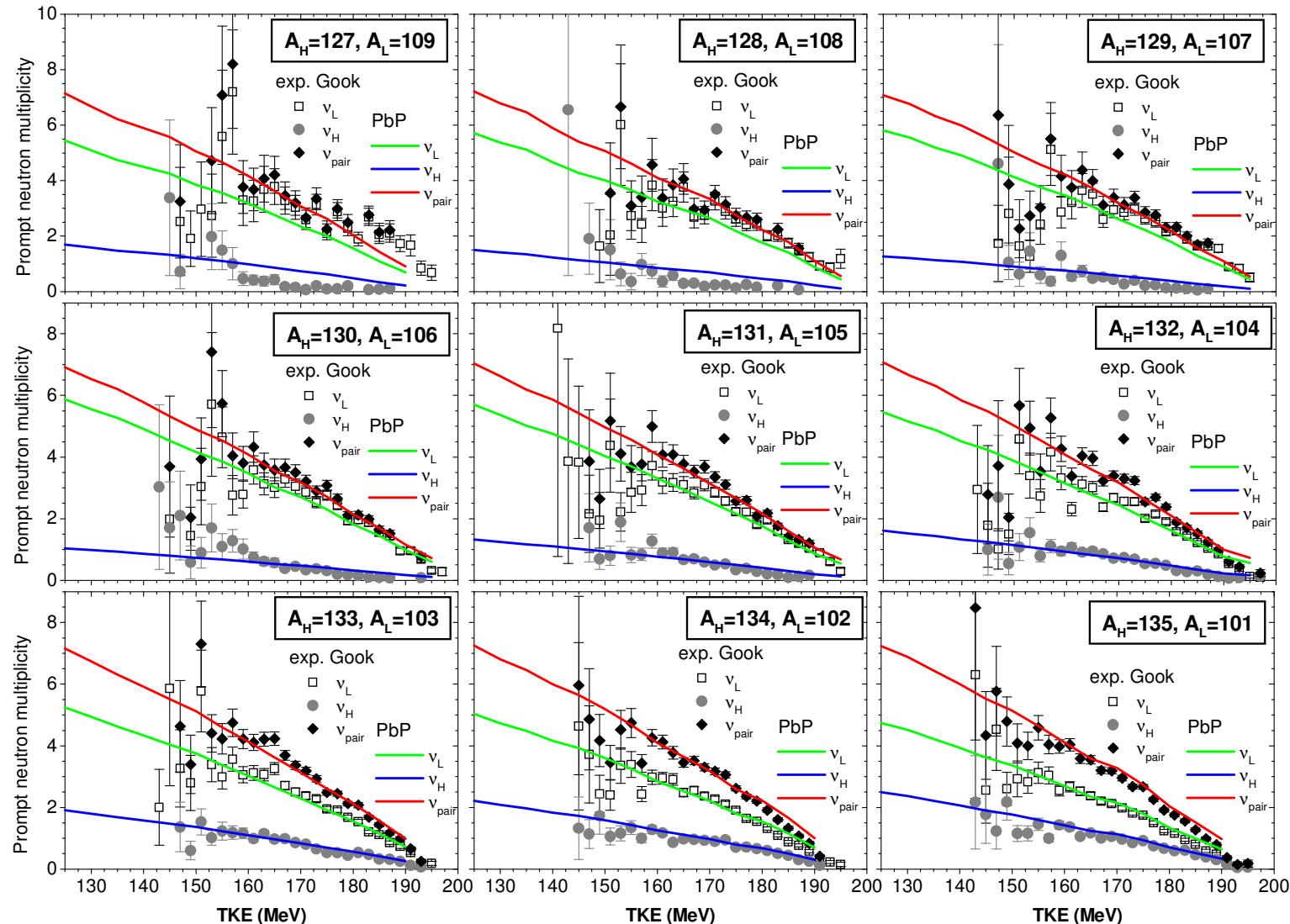
It consists of the comparison of different single distributions and total average values of prompt emission quantities with the available experimental data (e.g.  $v(A)$ ,  $\langle v \rangle(TKE)$ ,  $\langle E\gamma \rangle(A)$ ,  $\langle N\gamma \rangle(A)$ ,  $\langle \varepsilon \rangle(A)$ ,  $\langle \varepsilon \rangle(TKE)$ , PFNS,  $\langle v_p \rangle_{tot}$ ,  $\langle E\gamma \rangle_{tot}$  etc.)

Both PbP and sequential emission modelings were submitted to both validations mentioned above, being compared with the exp. data available in the last 10 years. The most recent refs are:

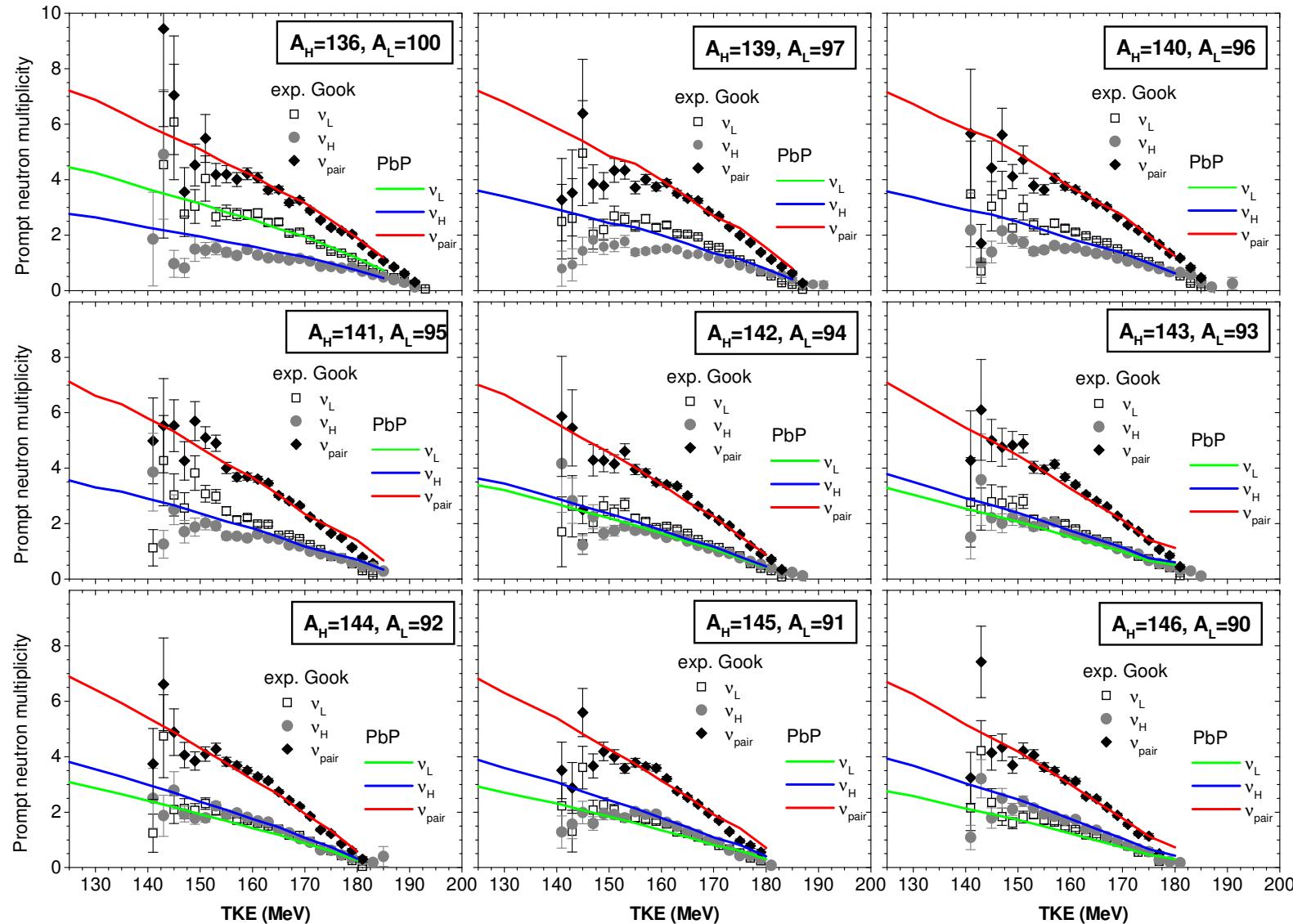
- “*Comprehensive overview of the Point-by-Point model of prompt emission in fission*”, A.Tudora, F.-J.Hambsch, *Eur.Phys.J A*, 53(8) (2017) 159
- “*Revisiting the residual temperature distribution in prompt neutron emission in fission*” A.Tudora, F.-J.Hambsch, V.Tobosaru, *Eur.Phys.J A*, 54(5) (2018) 87
- “*Prompt emission calculations for  $^{233}U(n_{th},f)$* ”, A.Tudora, A.Matei, *Roum.J.Phys.* 2018, in press

Here, only a supplementary validation based on the very recent exp. data for  $^{235}U(n,f)$  measured at JRC-Geel (Göök et al., *Phys.Rev.C* 2018)

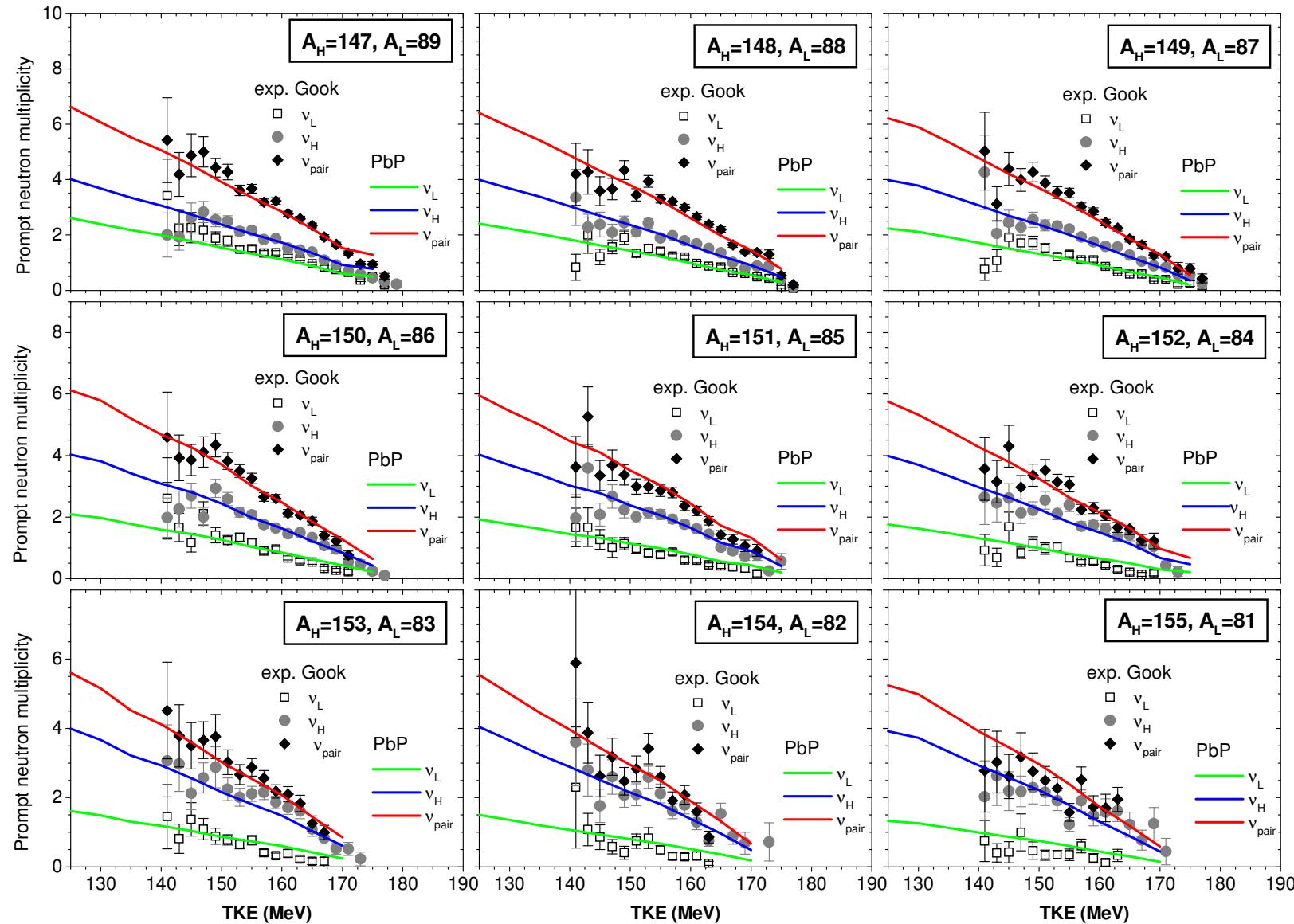
**PbP result of  $v(A, TKE)$  for  $^{235}\text{U}(n_{\text{th}}, f)$  compared with  
the recent data of Göök et al. (measured in the En range 0.26 eV – 45 keV)**



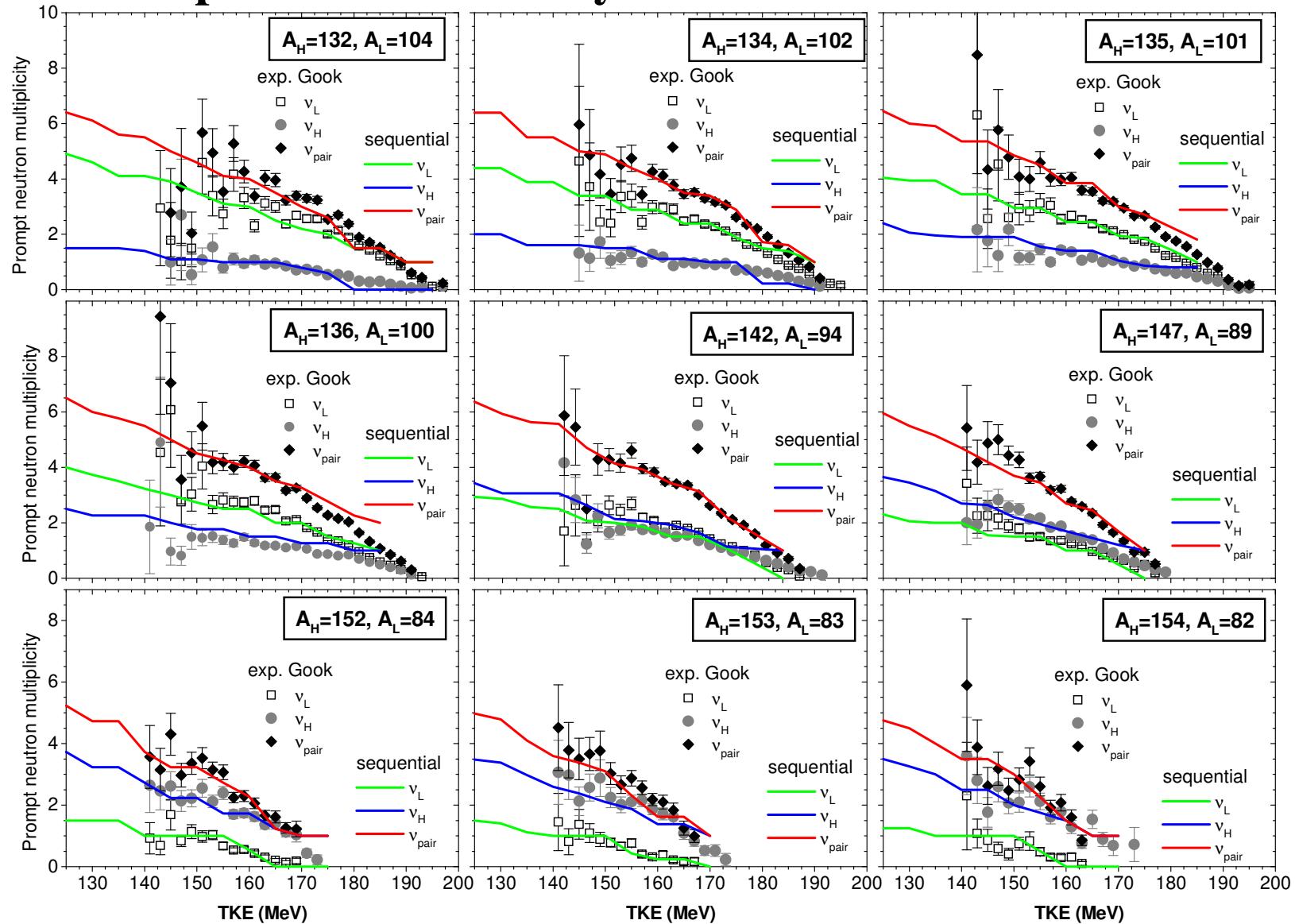
# PbP result of $v(A, TKE)$ for $^{235}\text{U}(n_{\text{th}}, f)$ compared with the very recent data of Göök et al.



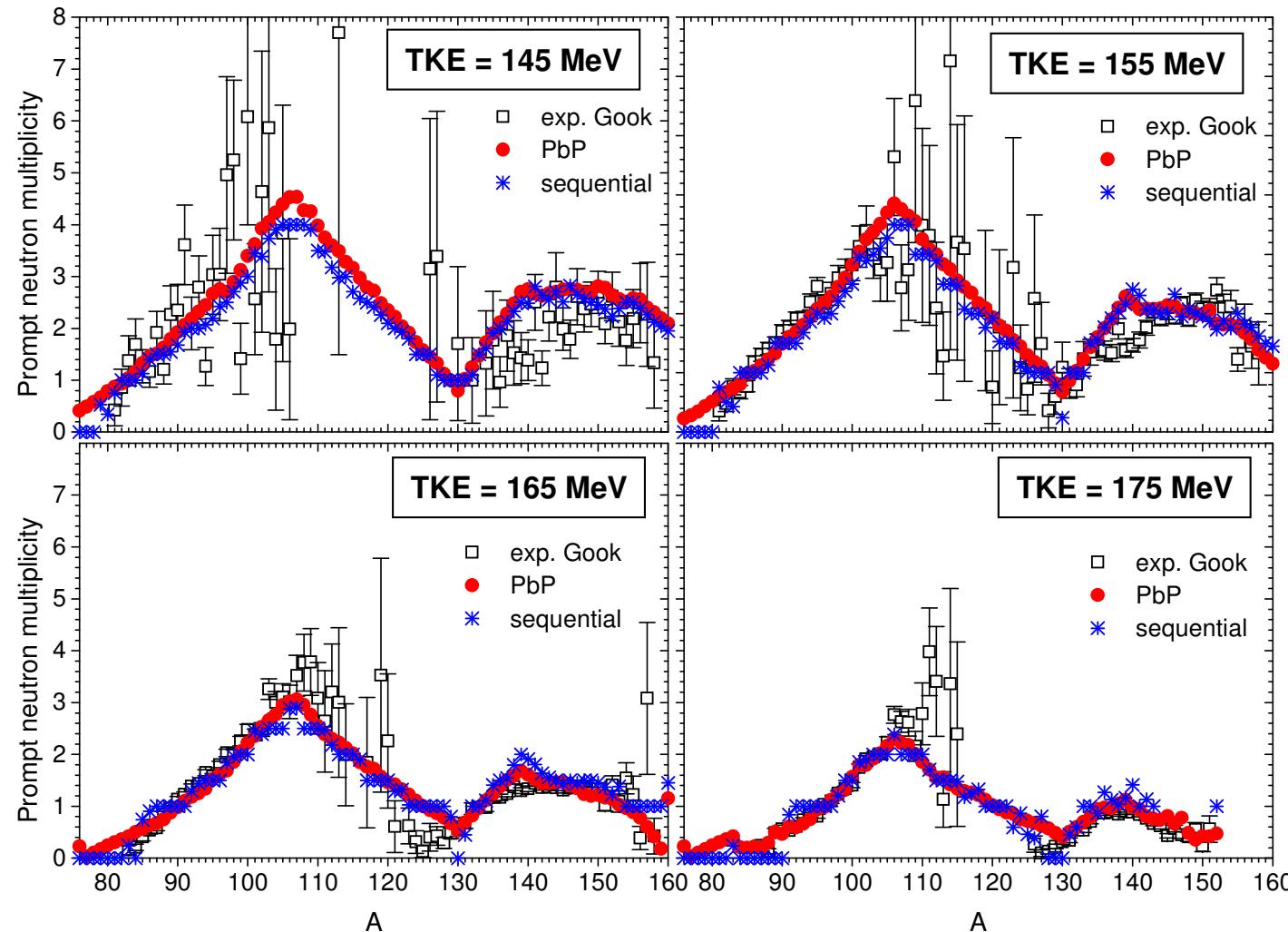
# PbP result of $v(A, TKE)$ for $^{235}\text{U}(n_{\text{th}}, f)$ compared with the very recent data of Göök et al.



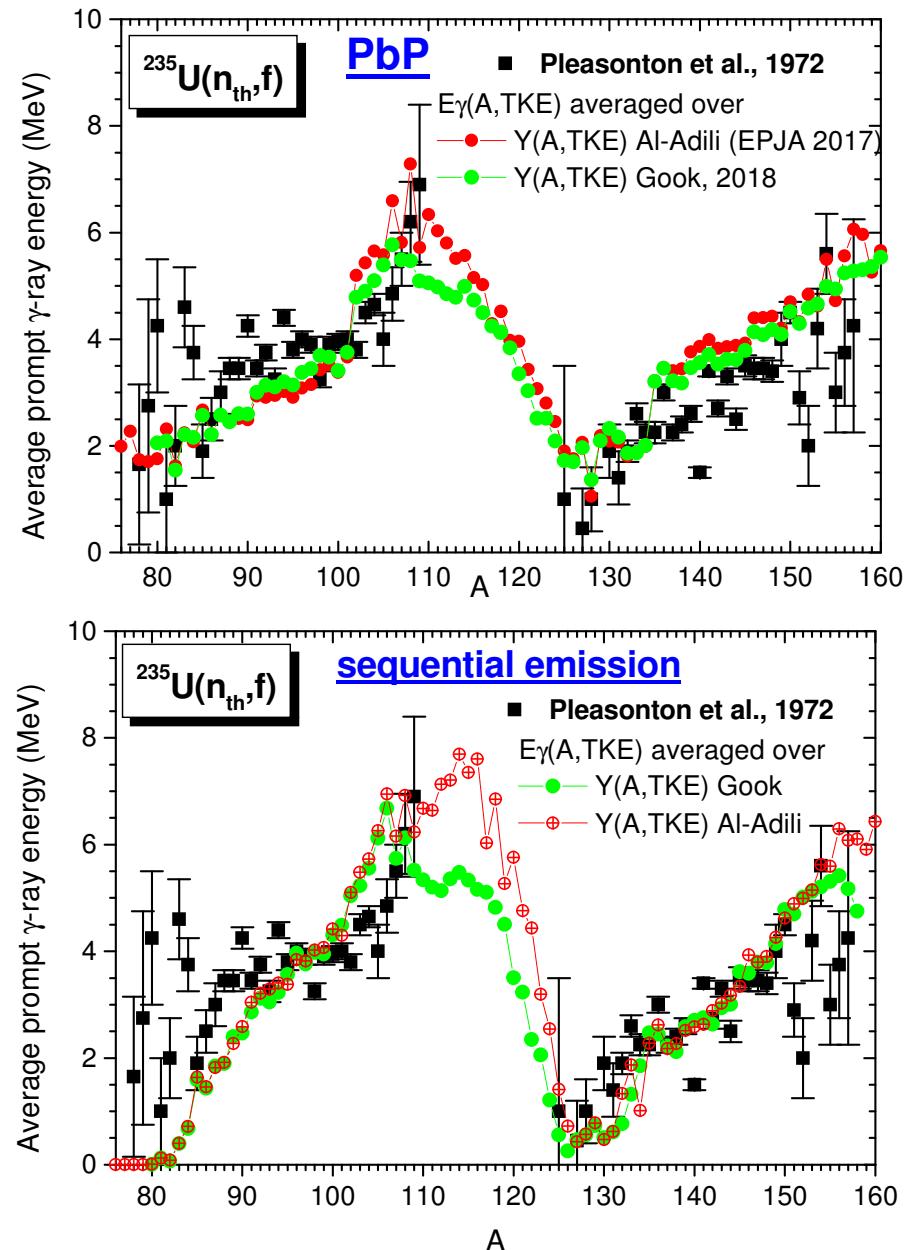
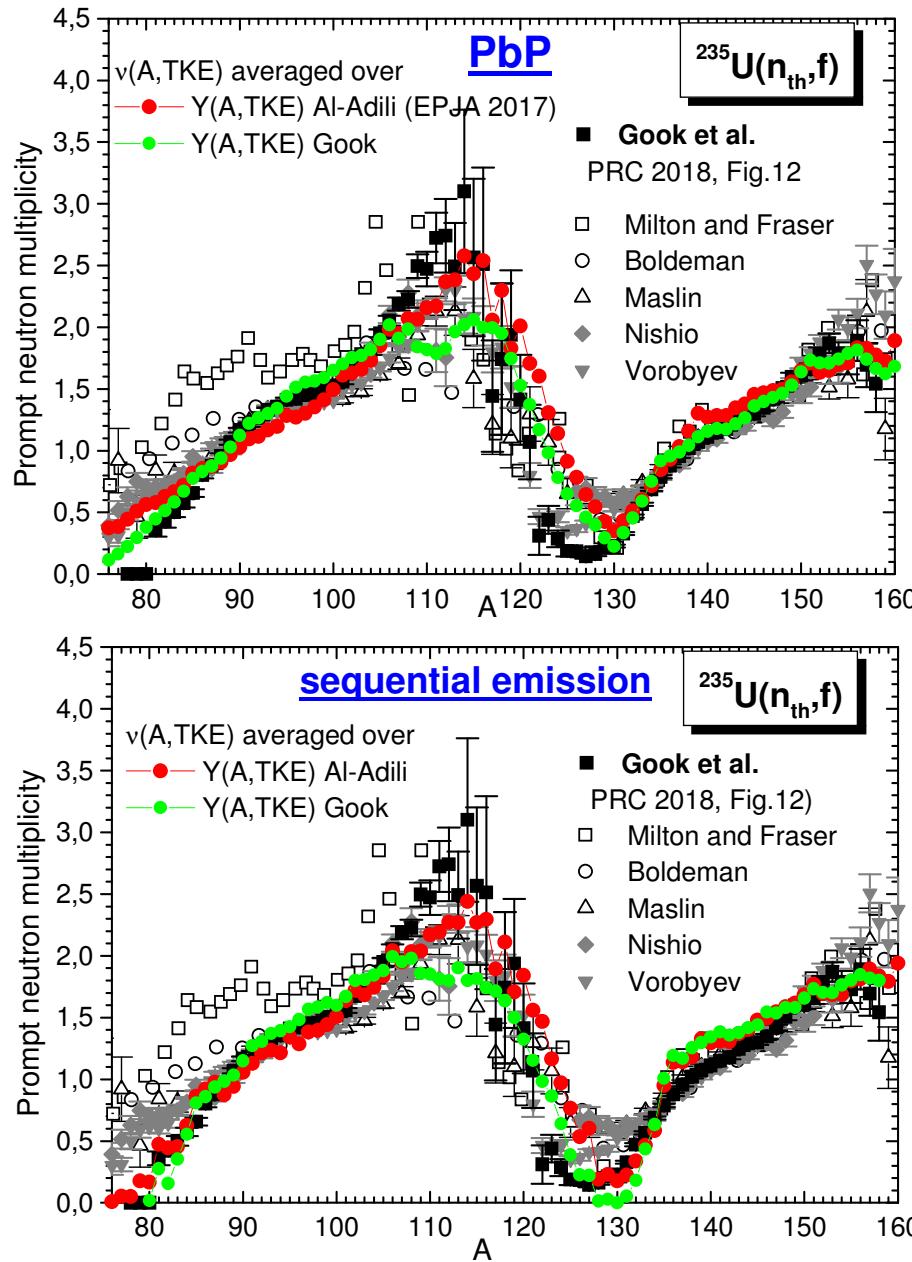
# Sequential emission result of $\nu(A, TKE)$ for $^{235}\text{U}(n_{\text{th}}, f)$ compared with the very recent data of Göök et al.

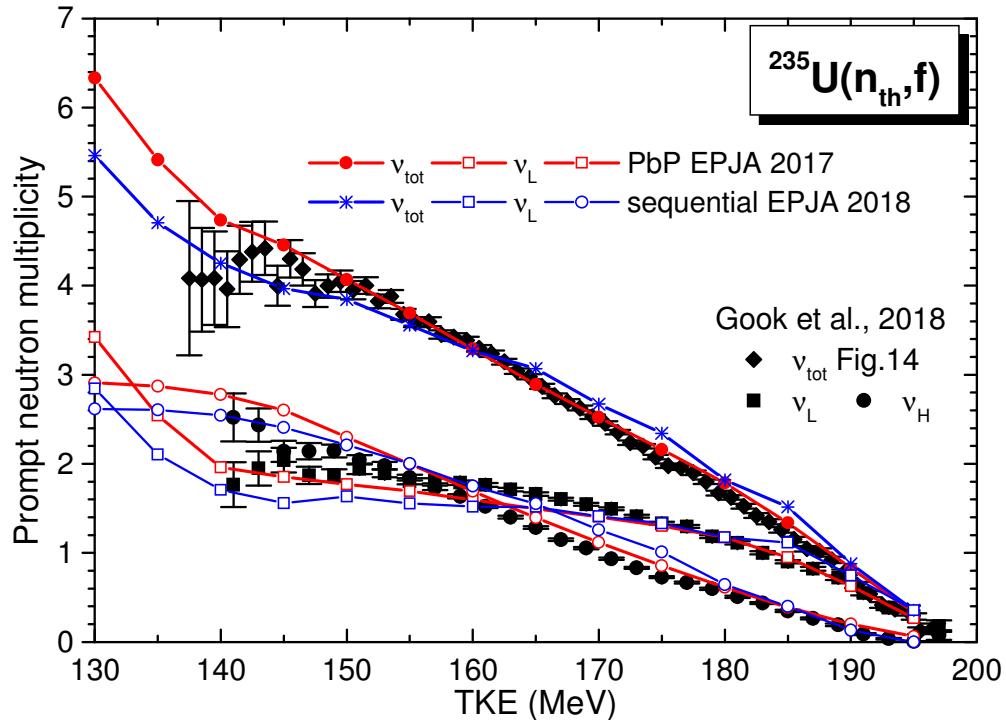


# $\nu(A, TKE)$ results of PbP and sequential emission for $^{235}\text{U}(n_{\text{th}}, f)$ compared with very recent data of Göök et al.

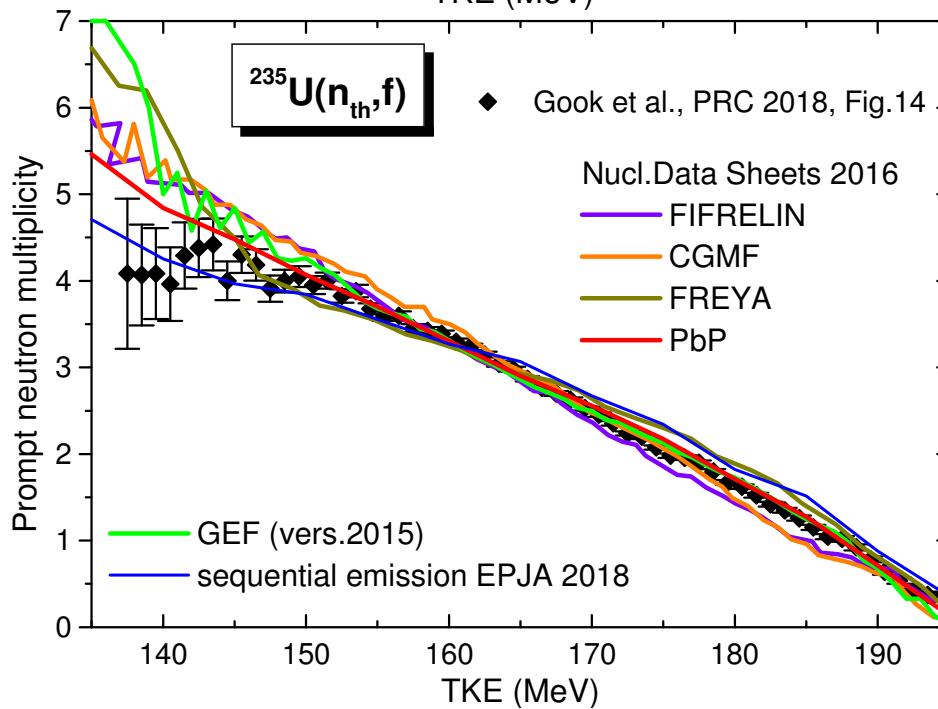


# Average quantities, single distributions – influence of Y(A,TKE)





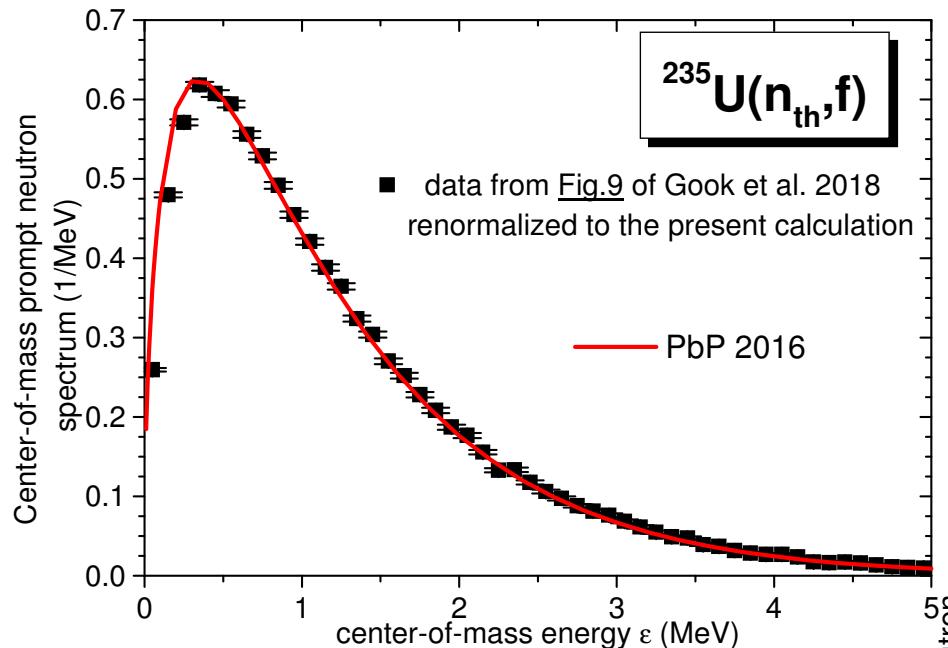
$\langle v \rangle(\text{TKE})$  obtained by averaging  $v(A, \text{TKE})$  over  $Y(A, \text{TKE})$  of Göök et al. and of Al-Adili et al. do not differ significantly from each other because the difference between their  $Y(\text{TKE})$  projections are very low, almost insignificant. Consequently here only the PbP and sequential emission results based on  $Y(A, \text{TKE})$  of Al-Adili are given.



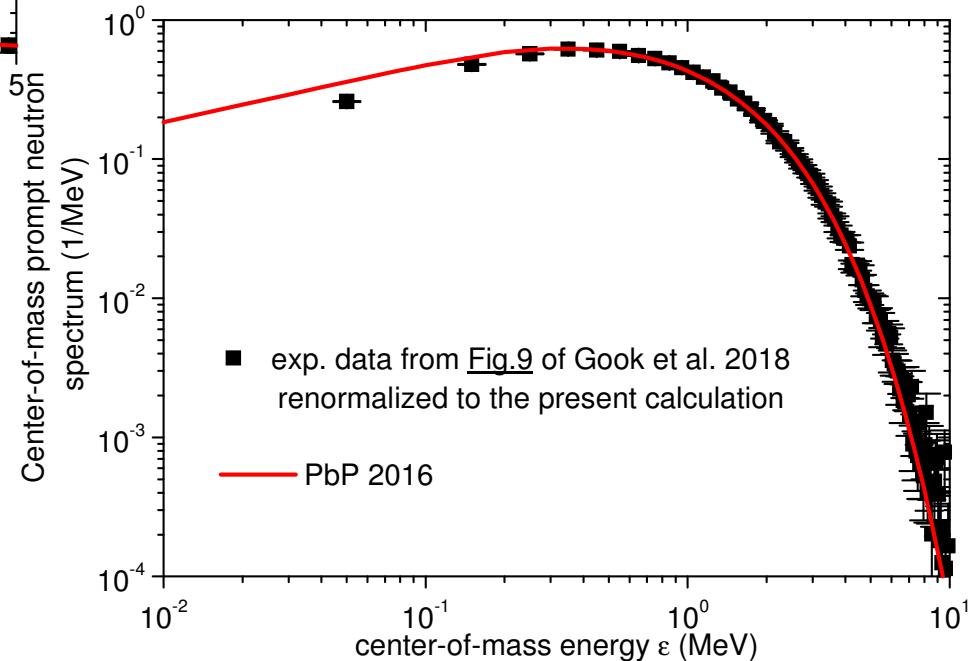
The  $\langle v \rangle(\text{TKE})$  predictions of FIFRELIN, CGMF, FREYA and PbP reported in 2016, of GEF (vers. 2015) and of the sequential emission treatment (EPJA 2018) are confirmed by the recent data of Göök et al.

The best description of these exp.data is given by the results of PbP and GEF.

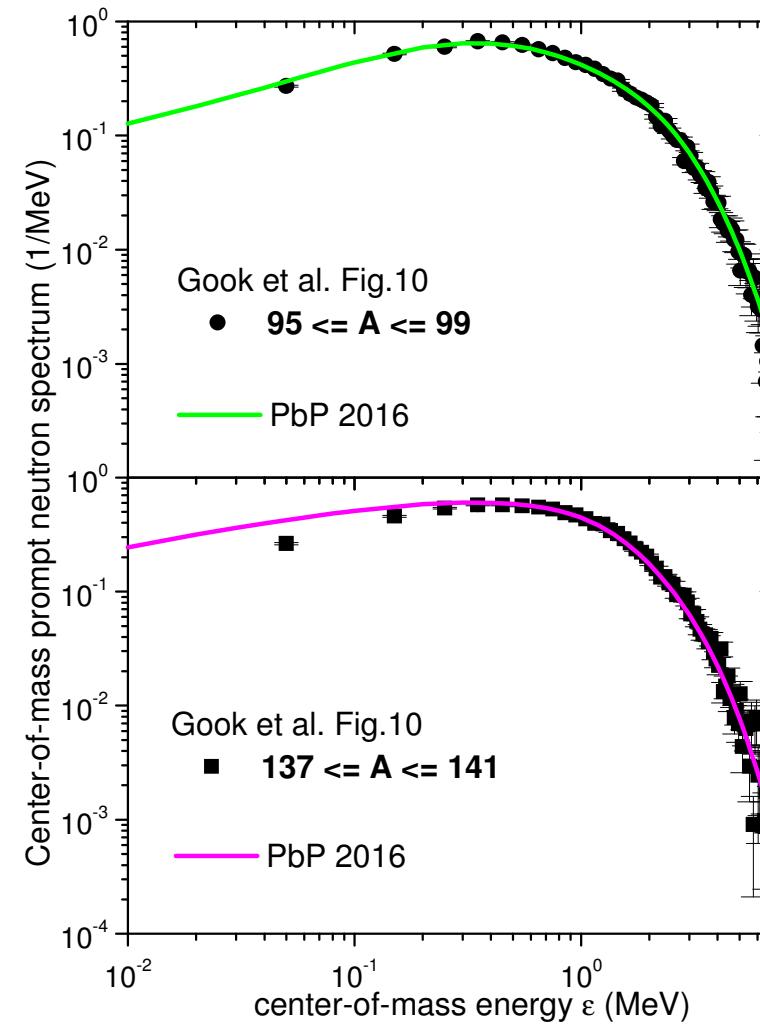
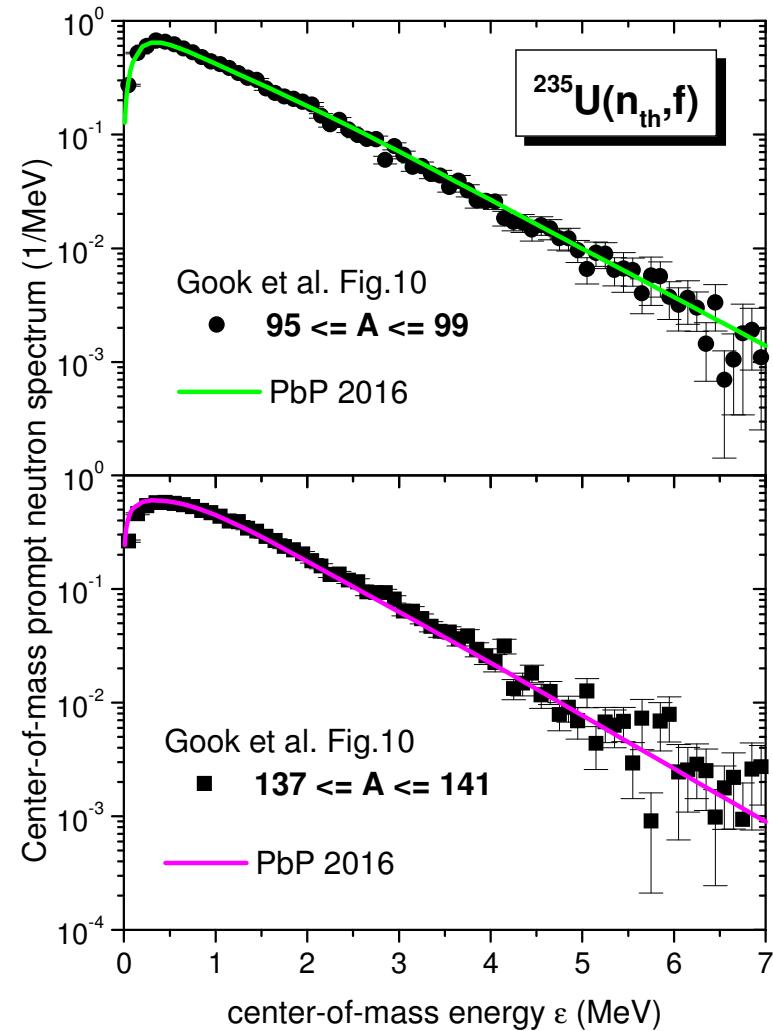
# PbP result of the prompt neutron spectrum in the center-of-mass frame compared with the data of Göök et al.



The recent data of Göök et al. from Fig.9 (PRC 2018) are very well described by the previous PbP result.  
(calculated in 2016 and published in EPJA 2017)

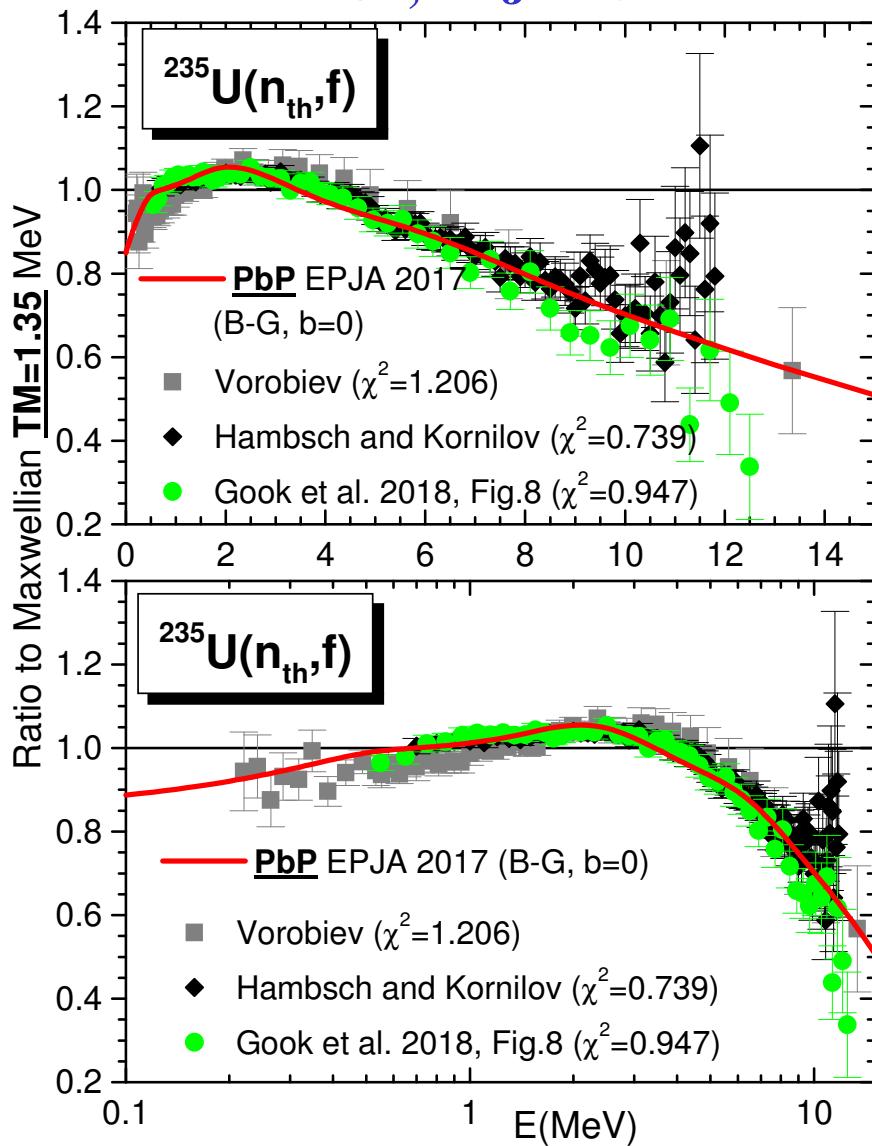


The data of Göök et al. (Fig.10 of PRC 2018) regarding the prompt neutron spectrum in the **center-of-mass frame** for selected fragment mass ranges around the most probable fragmentation (LF upper part, HF lower part) are **very well described by the PbP results** (representing the spectrum obtained by averaging over the light and heavy fragment groups, respectively).

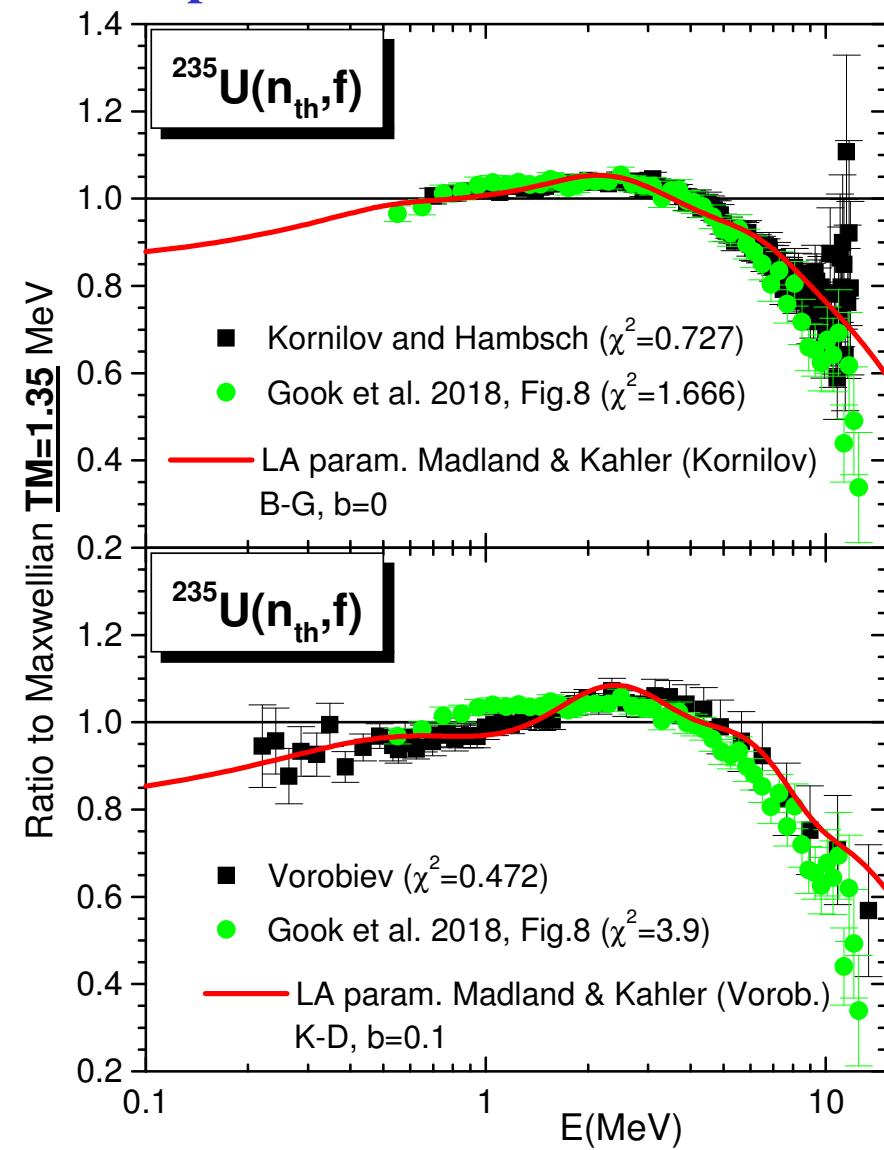


PFNS in the **laboartory frame** - previous results of PbP and LA (EPJA 2017) compared with the data of Göök et al. (PRC 2018, Fig.8)

PbP, EPJA 2017



LA param. Madland & Kahler 2017



**Residual temperature distributions and  
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*- preliminary results -*

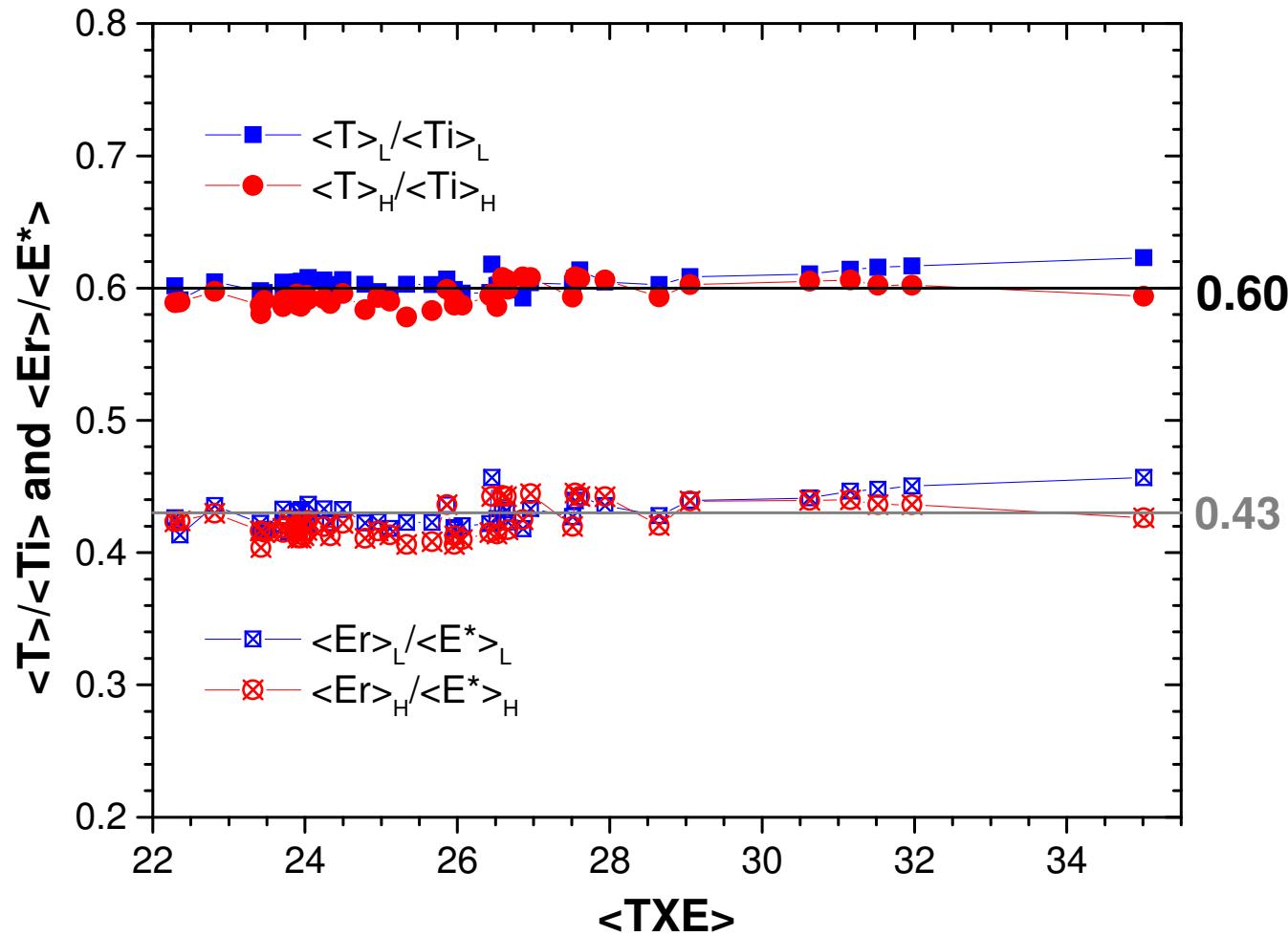
The development of a sequential emission modeling (with a deterministic treatment) has had as initial goal the determination of a general form for P(T) to be used in prompt emission models with a global treatment of the sequential emission, like PbP and LA.

For this reason the sequential emission modeling was applied to many fissioning systems benefiting of experimental Y(A,TKE) data, as follows :

- SF:  $^{252}\text{Cf(SF)}$ ,  $^{236,238,240,242,244}\text{Pu(SF)}$
- $(n_{th},f)$ :  $^{235}\text{U}(n_{th},f)$ ,  $^{239}\text{Pu}(n_{th},f)$  and  $^{233}\text{U}(n_{th},f)$
- $(n,f)$  below the threshold of the second chance fission:
  - $^{237}\text{Np}(n,f)$  at 12 En going from 0.3 and 5.5 MeV
  - $^{238}\text{U}(n,f)$  at 14 En going up to 5.5 MeV
  - $^{234}\text{U}(n,f)$  at 14 En ranging from 0.2 to 5 MeV

i.e. a total number of 49 fission cases covering a large range of nuclei and TXE values. These allowed to determine interesting systematics.

The first finding, related to the initial aim → a general relation between the average residual temperature  $\langle T \rangle$  and the average temperature of initial fragments  $\langle T_i \rangle$  (*A.Tudora et al. Eur.Phys.J A, 54 (2018) 87*)

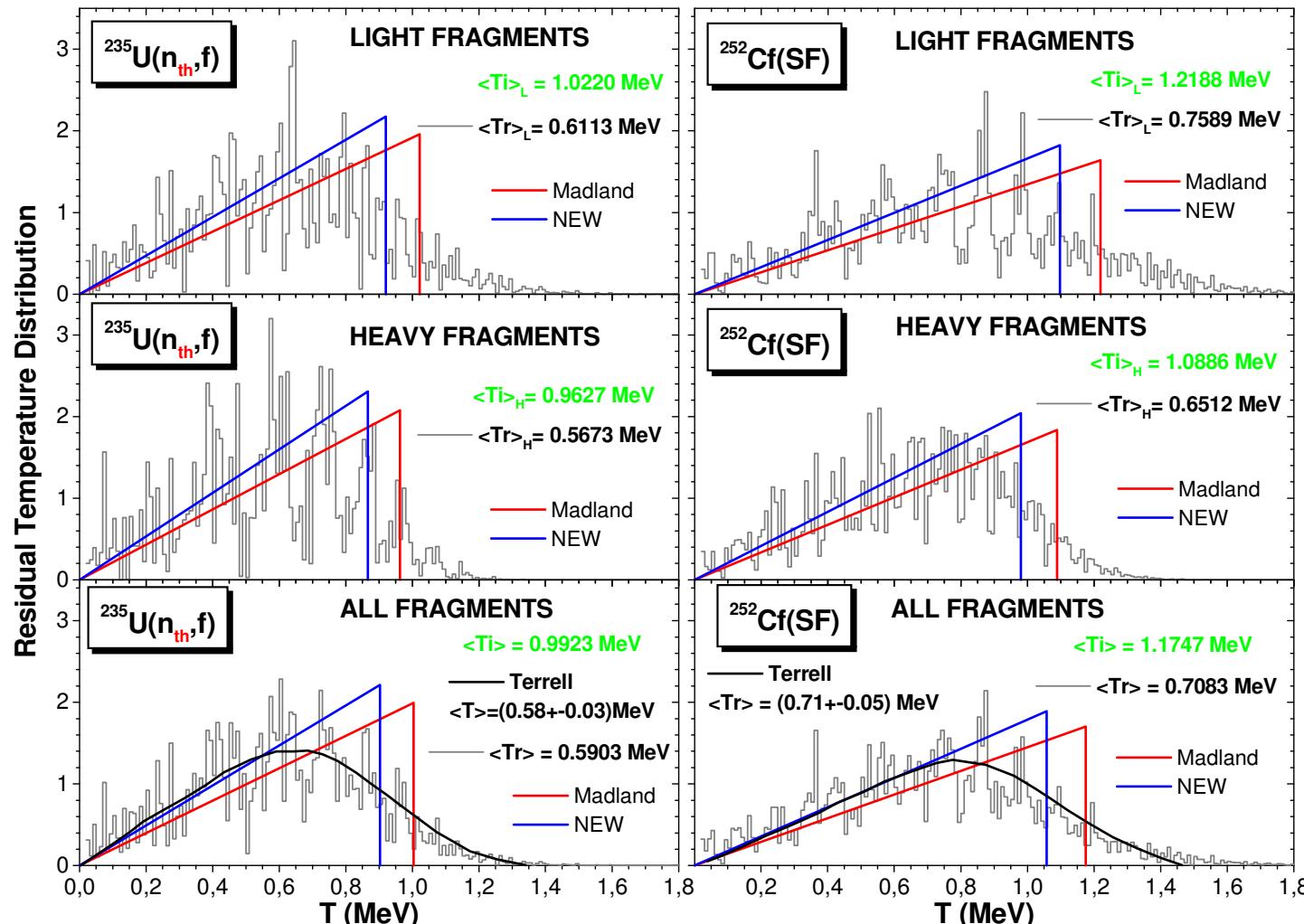


$$\langle T \rangle_L \approx 0.6 \langle Ti \rangle_L$$

$$\langle T \rangle_H \approx 0.6 \langle Ti \rangle_H$$

$$\langle T \rangle \approx 0.6 \langle Ti \rangle$$

Irrespective of the prescriptions used for  $\sigma_c(\varepsilon)$  and the level density parameters of initial and residual fragments



Replacement of the triangular  $P(T)$  with a moderately broad cut-off at high  $T$  by a distribution with a sharp cut-off.

This is justified by the use of a Weisskopf evaporation spectrum which overestimates somewhat the spectra at high energies. This overestimation can be compensated by a triangular  $P(T)$  with a sharp cut-off, which eliminates the residual temp. higher than  $T_{\text{max}} = (3/2)\langle T \rangle$

$$P(T) = \begin{cases} 2T/T_{\text{max}}^2 & T \leq T_{\text{max}} \\ 0 & T > T_{\text{max}} \end{cases}$$

$$T_{\text{max}} = \frac{3}{2} 0.6 \langle Ti \rangle = 0.9 \langle Ti \rangle$$

*Tudora et al.,  
Eur.Phys.J.A 54 (2018) 87*

$$\langle T \rangle = \frac{2}{3} T_{\text{max}}$$

$$T_{\text{max}} = \langle Ti \rangle$$

$$\langle T \rangle = \frac{2}{3} \langle Ti \rangle$$

*Madland and Nix*

By solving  $\overline{E_r}^{(k-1)} - S_n^{(k-1)} - \langle \epsilon \rangle_k = a_k T_k^2$  for each A, Z, TKE

different quantities for each emission sequence “k” →  $q_k(A, Z, TKE)$  are obtained, e.g.  $T_k(A, Z, TKE)$ ,  $E_r(A, Z, TKE)$ ,  $\langle \epsilon \rangle_k(A, Z, TKE)$ , the average energy carried away per each neutron  $\eta_k(A, Z, TKE) = \langle \epsilon \rangle_k(A, Z, TKE) + S_{n-1}(A, Z, TKE)$  etc.

They appear with the probability expressed by the  $Y(A, Z, TKE)$  distribution.

### Average values corresponding to each emission sequence:

$$\langle q_k \rangle = \sum_{A, Z, TKE} q_k(A, Z, TKE) Y(A, Z, TKE) / \sum_{A, Z, TKE} Y(A, Z, TKE)$$

by summing separately for the light and heavy groups or over all fragments

A total average quantity corresponding to the sum of the distributions following the emission of each neutron is obtained by averaging  $\langle q_k \rangle$  over the probability for emission of each neutron (or the probability for apparition of each residual fragment)  $Pn_k$ :

$$\langle q \rangle = \sum_{k=1}^n \langle q_k \rangle Pn_k / \sum_{k=1}^n Pn_k$$

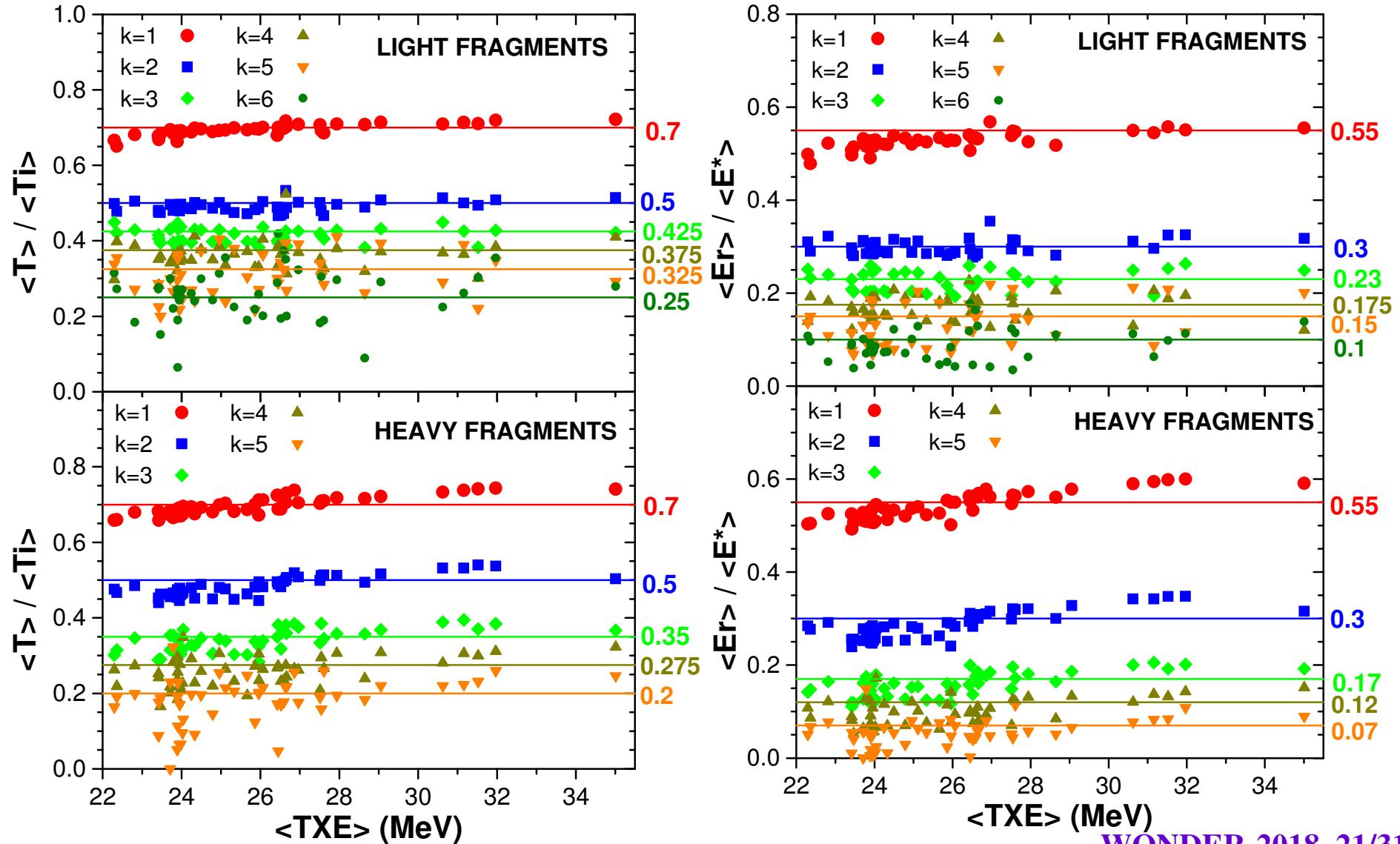
Note:

$Pn_k$  = the probability for emission of the 1-st, second, ... k-th neutron  
to be not confounded with

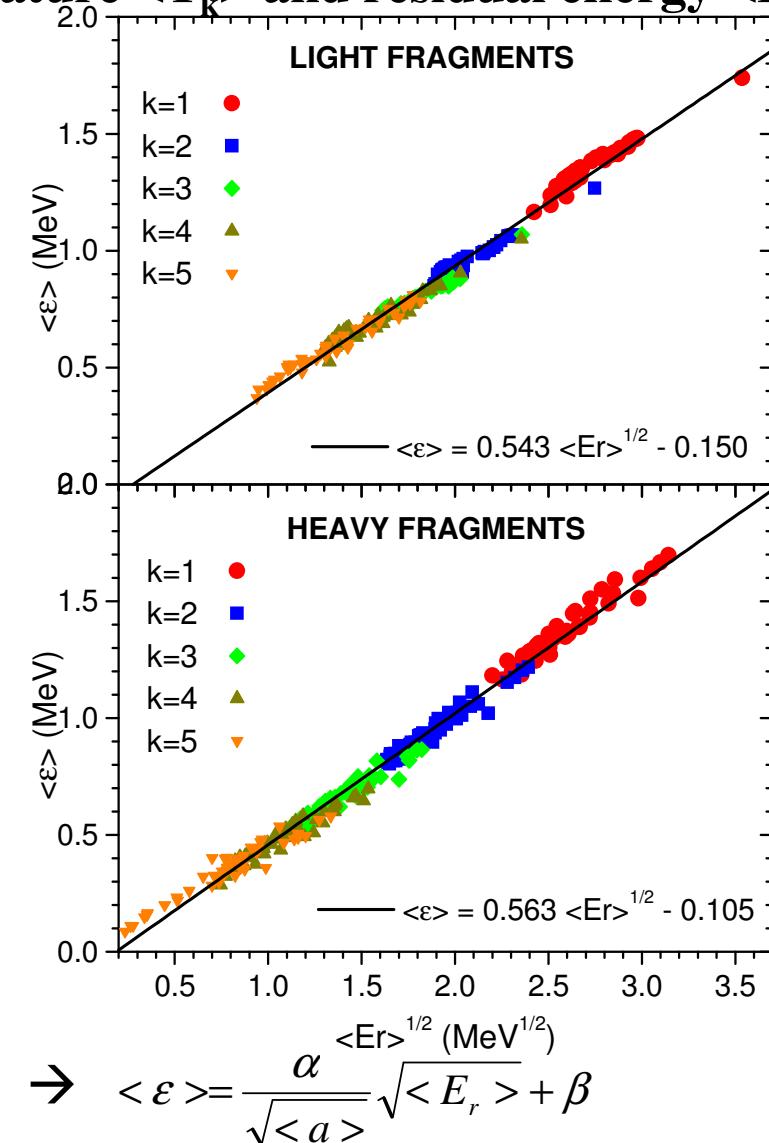
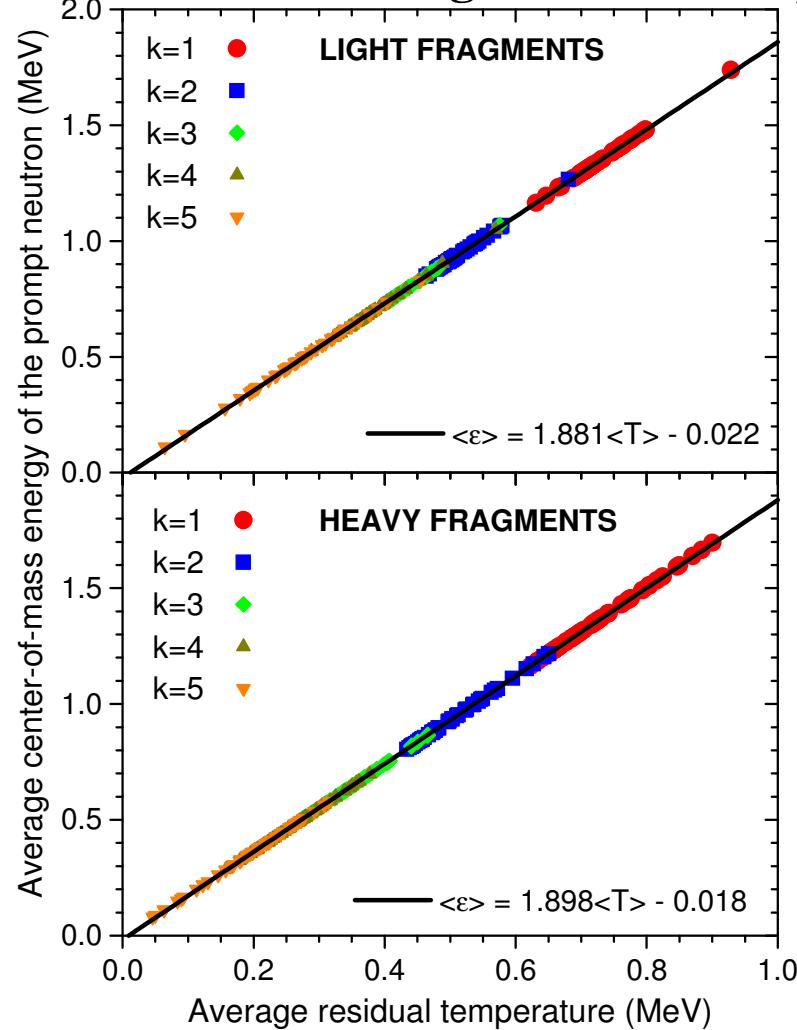
$P(v)$  = the probability for emission of one, two, three... neutrons

# Ratios of residual temperatures and energies to the ones of initial fragments for the 49 studied fission cases

Prescriptions: analytical expression of  $\sigma_c(\epsilon)$  and level density parameters provided  
by the Egidy-Bucurescu systematic (2009) for BSFG



# Average center-of-mass energy of prompt neutrons $\langle \varepsilon \rangle_k$ as a function of average residual temperature $\langle T_k \rangle$ and residual energy $\langle E_{r_k} \rangle^{1/2}$

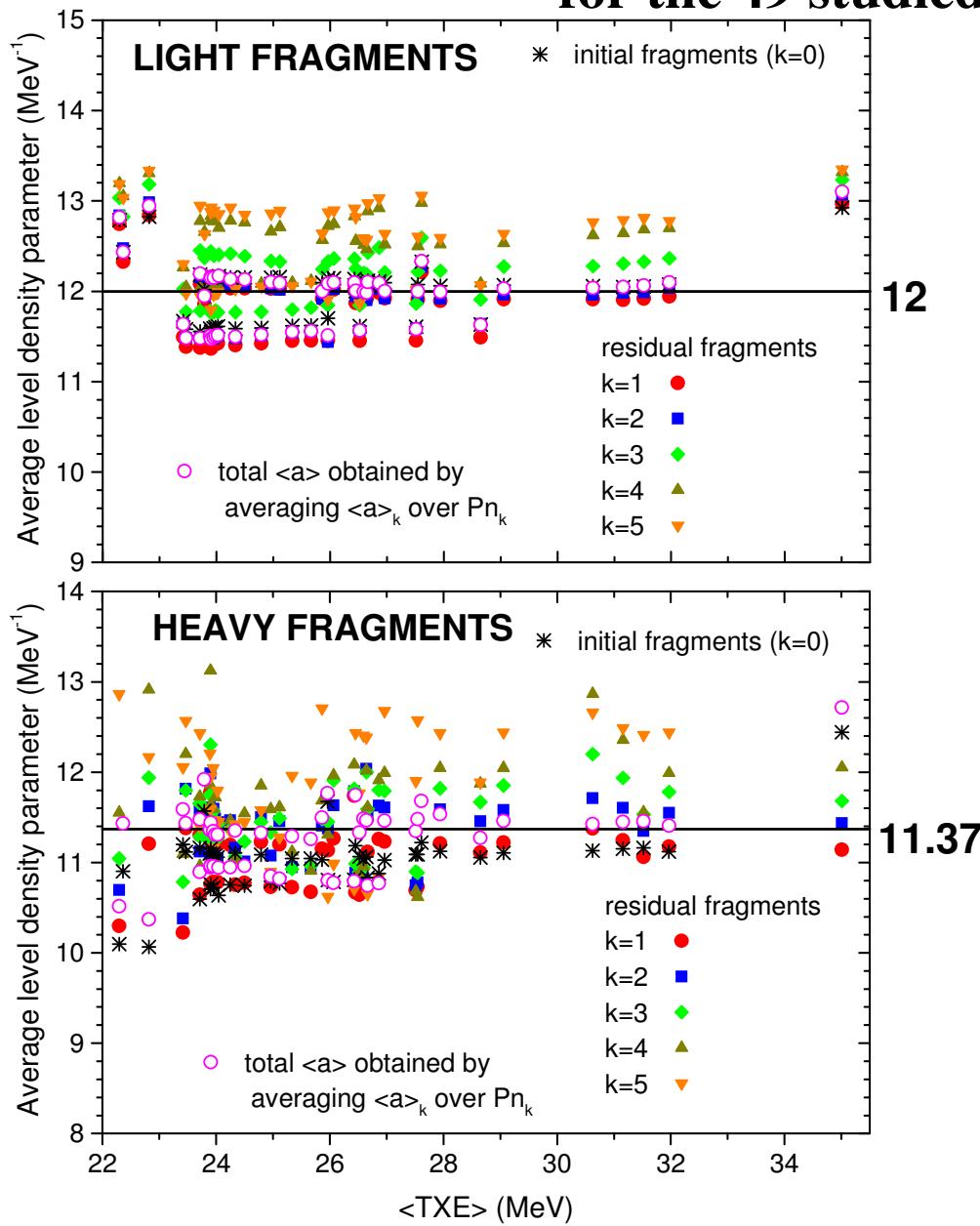


$$\text{from } \langle \varepsilon \rangle = \alpha \langle T \rangle + \beta \quad \text{and} \quad \langle E_r \rangle = \langle a \rangle \langle T \rangle^2$$

$$\rightarrow \langle \varepsilon \rangle = \frac{\alpha}{\sqrt{\langle a \rangle}} \sqrt{\langle E_r \rangle} + \beta$$

Using the slopes from these figures → global values of the average level density param. of the light and heavy fragm. groups:  $\langle a \rangle_L = 12 \text{ MeV}^{-1}$ ,  $\langle a \rangle_H = 11.37 \text{ MeV}^{-1}$

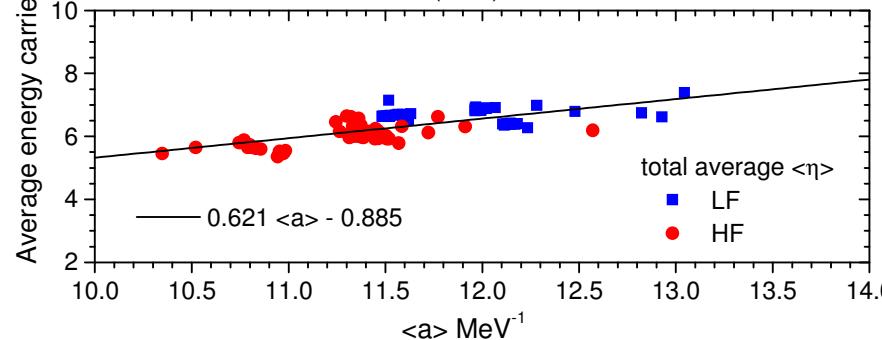
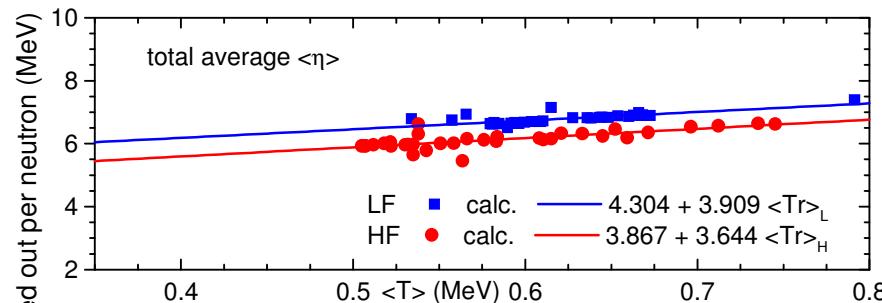
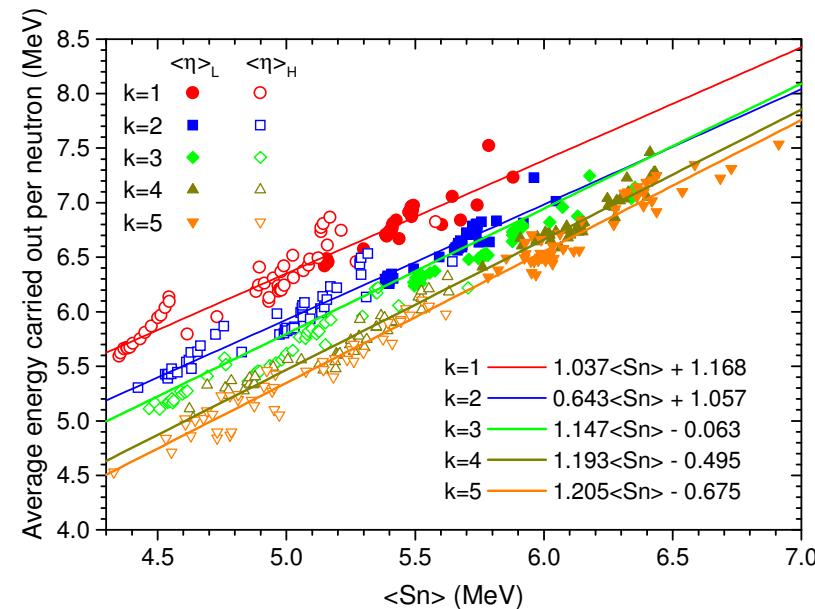
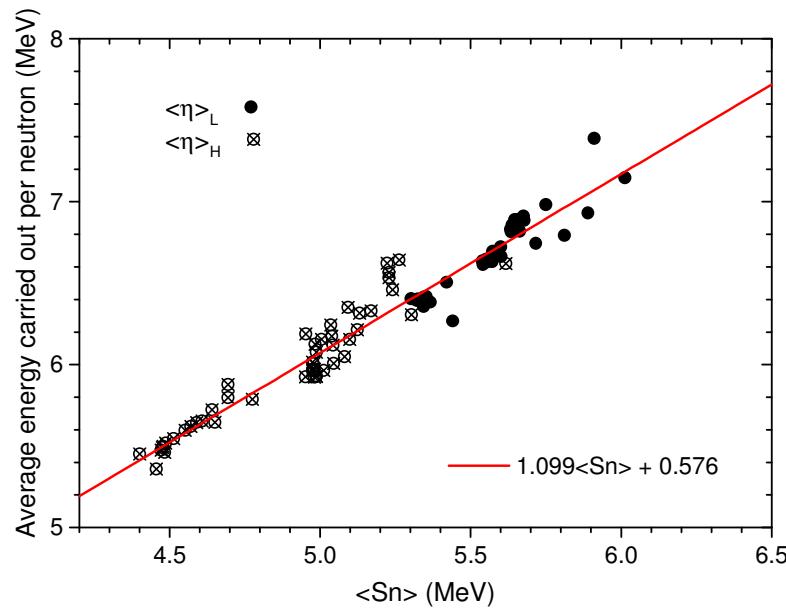
# Average level density parameters of the initial and residual fragments for the 49 studied fission cases.



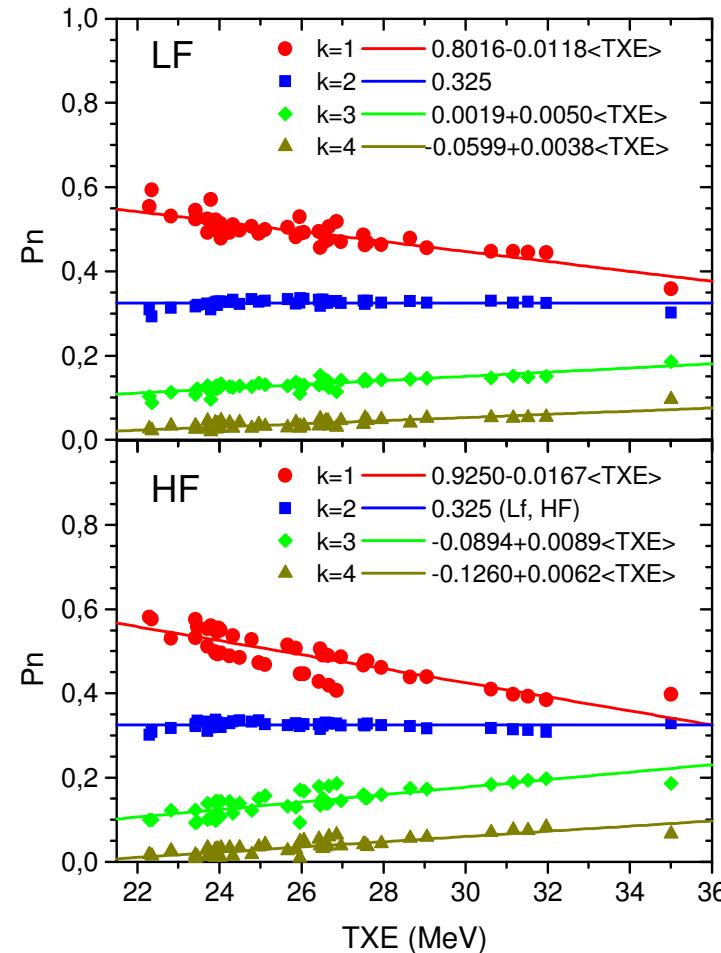
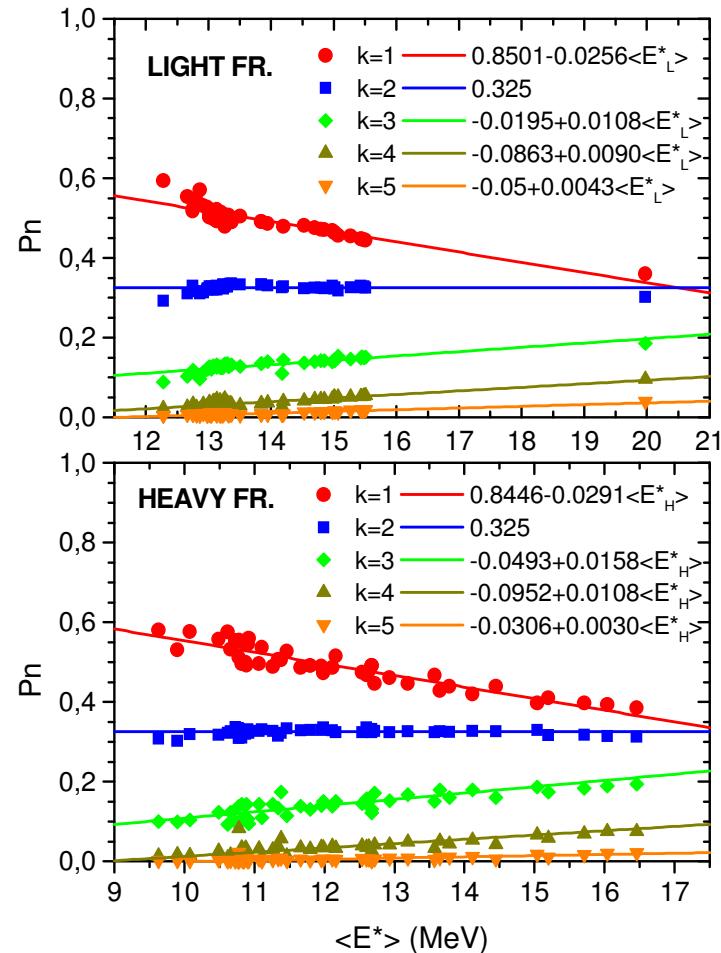
The global values of  $\langle a \rangle$  (horizontal lines) resulting from the systematic behaviour of  $\langle \varepsilon \rangle_k$  as a func. of  $\langle T \rangle_k$  and  $\langle E_r \rangle_k^{1/2}$  are in agreement with the total average  $\langle a \rangle$  ( magenta open circles).

The fact that  $\langle a \rangle$  for  $k=1$  (red) and  $k=2$  (blue) are close to the total  $\langle a \rangle$  (magenta open circles) is not surprising because the first two emission sequences take place for almost all fragments at the majority of TKE values.

# Energy carried away per neutron $\eta_k = \langle \mathcal{E} \rangle_k + S_n^{(k-1)}$ precursor

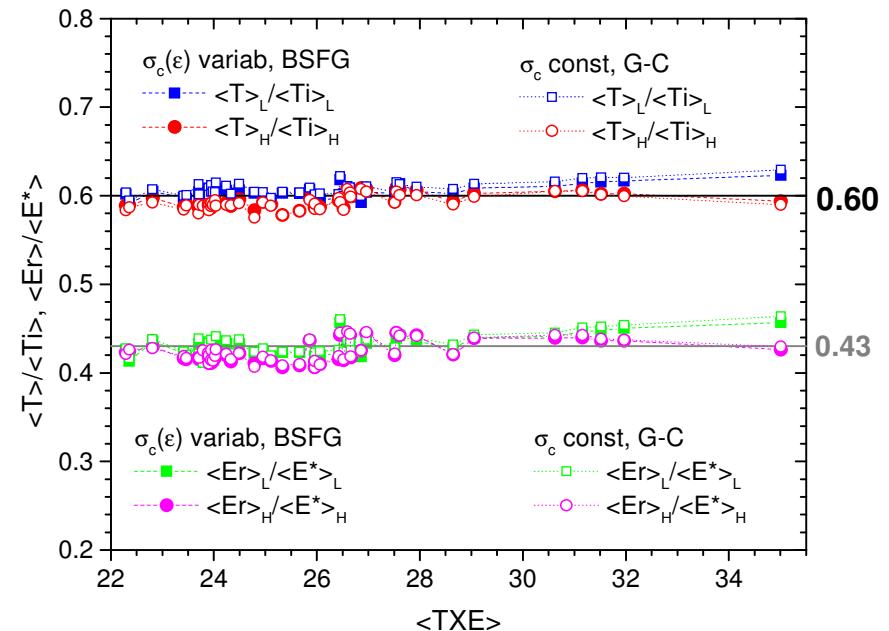
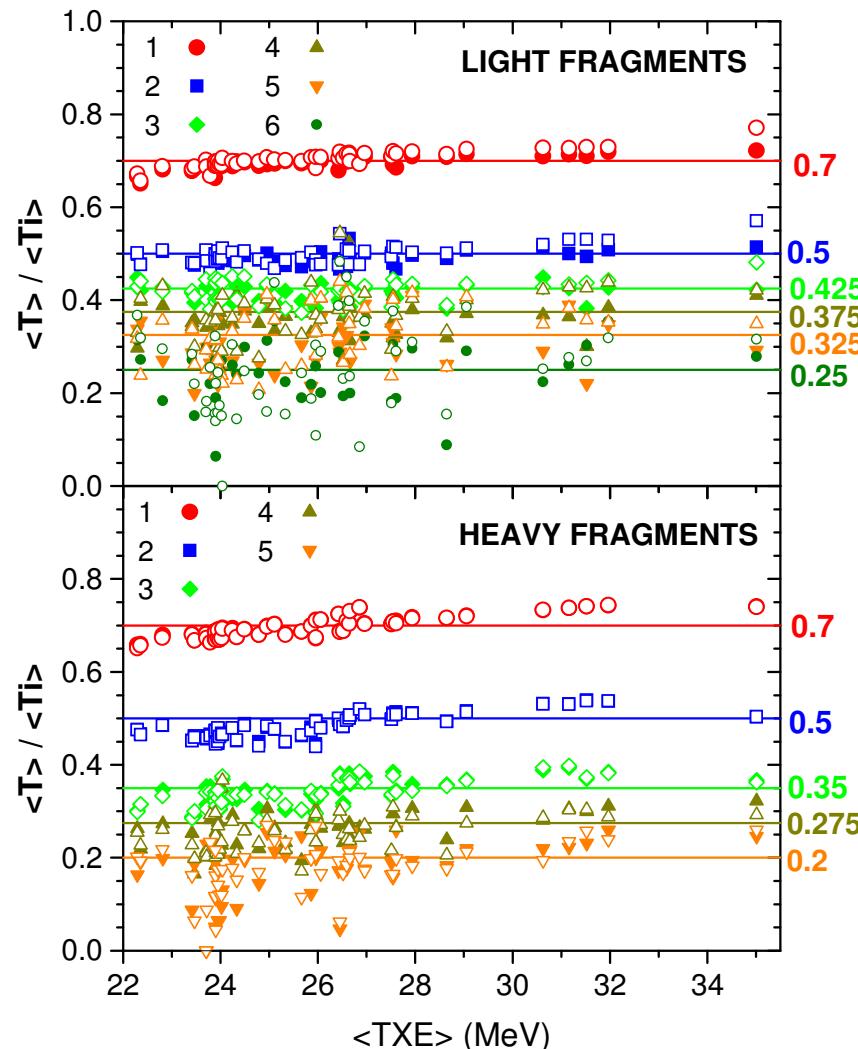


**Probability for emission of the k-th prompt neutron from the light and heavy fragment groups as a function of the average excitation energy of the initial light and heavy fragments and as a function of  $\langle TXE \rangle$  for the 49 studied fission cases.**



## The use of other prescriptions does not change the results.

Here examples for the prescriptions  $\sigma_c(\varepsilon)=\text{constant}$  and level dens. parameters of the Gilbert-Cameron systematic for spherical nuclei, which are very different from the prescriptions previously employed (i.e. analytical expression of  $\sigma_c(\varepsilon)$ , lev.dens.param. provided by the systm. E-B 2009 for BSFG)



Full symbols: analytical expression  $\sigma_c(\varepsilon)$  and  
E-B 2009 systm. for BSFG  
Open symbols: constant  $\sigma_c(\varepsilon)$  and  
G-C systematic

# APPLICATION of the systematic behaviour $\langle T \rangle_k / \langle T_i \rangle = r_k$

## Inclusion of the sequential emission into the Los Alamos model

Up to now in the LA model → Tmax of P(T) was taken equal to  $\langle T_i \rangle$

$$\langle T_i \rangle = \sqrt{\langle TXE \rangle / \langle a_L + a_H \rangle}$$

*Madland and Nix (NSE 1982) the same P(T)*

$$\langle T_i \rangle_{L,H} = \sqrt{\langle E^* \rangle_{L,H} / \langle a \rangle_{L,H}}$$

*Madlald and Kahler (NPA 2017)*

**non-equal Tmax for LF and HF** (as in PbP)

Now:

The consideration of a triangular  
P<sub>k</sub>(T) for each emission sequence “k”  
with:

$$T_{\max}^{(k)} = \frac{3}{2} r_k \langle T_i \rangle$$

$$P_k(T) = \begin{cases} 2T/T_{\max}^{(k)2} & T \leq T_{\max}^{(k)} \\ 0 & T > T_{\max}^{(k)} \end{cases}$$

r<sub>k</sub> given by the systematic,  
e.g. r<sub>1</sub>=0.7, r<sub>2</sub>=0.5 etc.

c.m.s.

$$\Phi_k(\varepsilon) = \int_0^{T_{\max}^{(k)}} \varphi(\varepsilon, T) P_k(T) dT = \varepsilon \sigma_c^{(k)}(\varepsilon) \int_0^{T_{\max}^{(k)}} K_k(T) P_k(T) \exp(-\varepsilon/T) dT$$

$$K_k(T) = \left( \int_0^{\infty} \varepsilon \sigma_c^{(k)}(\varepsilon) \exp(-\varepsilon/T) d\varepsilon \right)^{-1}$$

## Inclusion of the sequential emission into the Los Alamos model

For the input parameters of the LA model (as average values), different prescriptions can be used regarding:

- a)  $\sigma_c(\varepsilon)$ : constant or an analytical expression (depending on the mass number and the s-wave neutron strength function of the nucleus {Z, A-k+1} or provided by optical model calc. with phenomenological potentials adequate for nuclei appearing as FF
- b) **TXE partition**: e.g. by modeling at scission (PbP), the procedure proposed by Madland and Kahler, the method of FREYA (adjustable param. "x") of FIFRELIN (implying the nucl.temp.ratio RT)) etc.
- c) **level density parameters** of fragments: either energy-dependent (super-fluid with different shell corrections and parameterizations of the dumping and asymptotic lev. dens.) or non-energy dependent (e.g. systematics of EB-2009 for BSFG, G-C etc.)

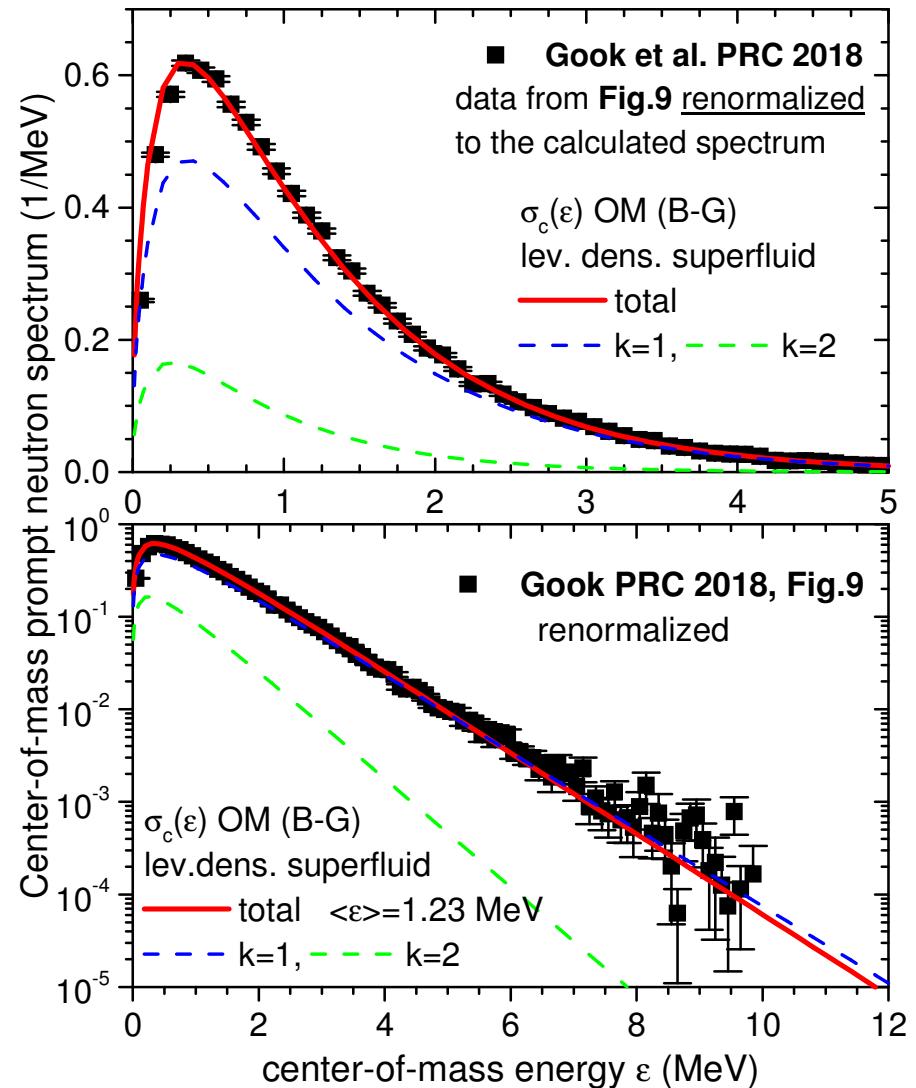
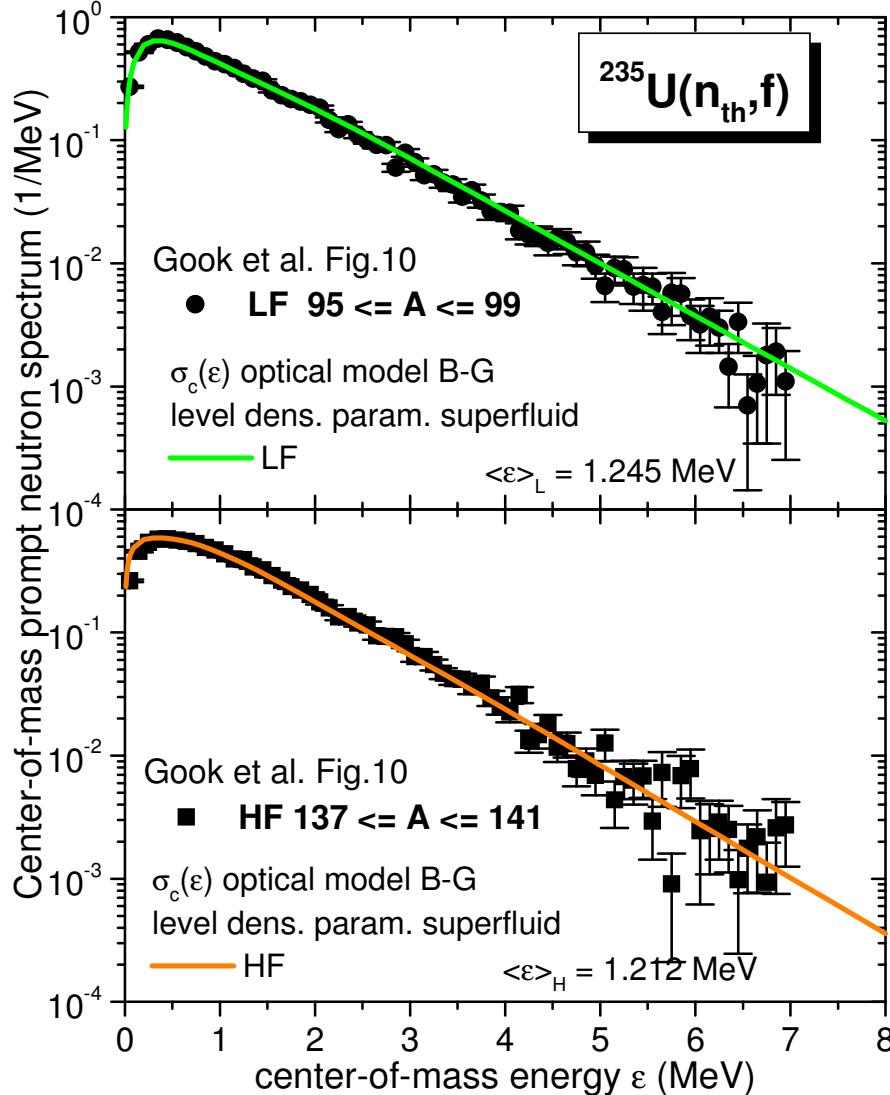
**Example:**  $\langle \varepsilon \rangle_k = \int_0^{\infty} \varepsilon \Phi_k(\varepsilon) d\varepsilon$        $\langle \varepsilon \rangle = \sum_{k=1}^n Pn_k \langle \varepsilon \rangle_k / \sum_{k=1}^n Pn_k$

$^{252}\text{Cf(SF)}$	$\langle \varepsilon \rangle_L$	$\langle \varepsilon \rangle_H$	$\langle \varepsilon \rangle$	exp (Göök)
i) $\sigma_c(\varepsilon)$ const, EB-2009 BSFG	<b>1.432</b>	<b>1.254</b>	<b>1.356</b>	<b>~1.45</b> (6%)
ii) $\sigma_c(\varepsilon)$ OM (B-G), super-fluid average number of sequences n=3	<b>1.517</b>	<b>1.309</b>	<b>1.428</b>	(1.5%)

$$\text{Example: } \Phi_{L,H}(\varepsilon) = \sum_{k=1}^n Pn_k \Phi_k^{(L,H)}(\varepsilon) \left/ \sum_{k=1}^n Pn_k \right.$$

sequential emission into the Los Alamos model

Prescriptions:  $\sigma_c(\varepsilon)$  optical model B-G, TXE partition by modeling at scission and level density parameters of the super-fluid model



**The systematic behaviours presented above can be also used in order to obtain indicative values of different average prompt emission quantities in the absence of any prompt emission model.**

If the average temperatures of initial fragments are known for a given fissioning nucleus (i.e. the equivalent  $\langle Ti \rangle$  or  $\langle Ti \rangle_L$  and  $\langle Ti \rangle_H$  )

then  $\langle \varepsilon \rangle$  can be obtained from the linear behaviour presented above i.e.  $\langle \varepsilon \rangle_L = 1.881 \langle T \rangle - 0.022$  and  $\langle \varepsilon \rangle_H = 1.898 \langle T \rangle - 0.018$  by using the ratio  $\langle T \rangle / \langle Ti \rangle \sim 0.6$ .

Examples for  $^{252}\text{Cf(SF)}$  for which

$$\langle TXE \rangle = 35.01 \text{ MeV}, \quad \langle E^* \rangle_L = 19.973 \text{ MeV} \text{ and } \langle E^* \rangle_H = 15.037 \text{ MeV}$$

i) using the equivalent  $\langle Ti \rangle$  based on  $\langle a \rangle = A_0 / 11 \text{ MeV}^{-1} \rightarrow \langle \varepsilon \rangle = 1.382 \text{ MeV}$

ii) considering  $\langle Ti \rangle_{L,H}$  based on level dens.param. of the superfluid model

$$\langle a \rangle_L = 13.545 \text{ MeV}^{-1}, \quad \langle a \rangle_H = 12.759 \text{ MeV}^{-1}$$

$$\rightarrow \langle \varepsilon \rangle_L = 1.430 \text{ MeV}, \quad \langle \varepsilon \rangle_H = 1.273 \text{ MeV}, \quad \langle \varepsilon \rangle = 1.363 \text{ MeV}$$

which deviate with 0.7% from the result of Madland and Kahler (NPA 2017)

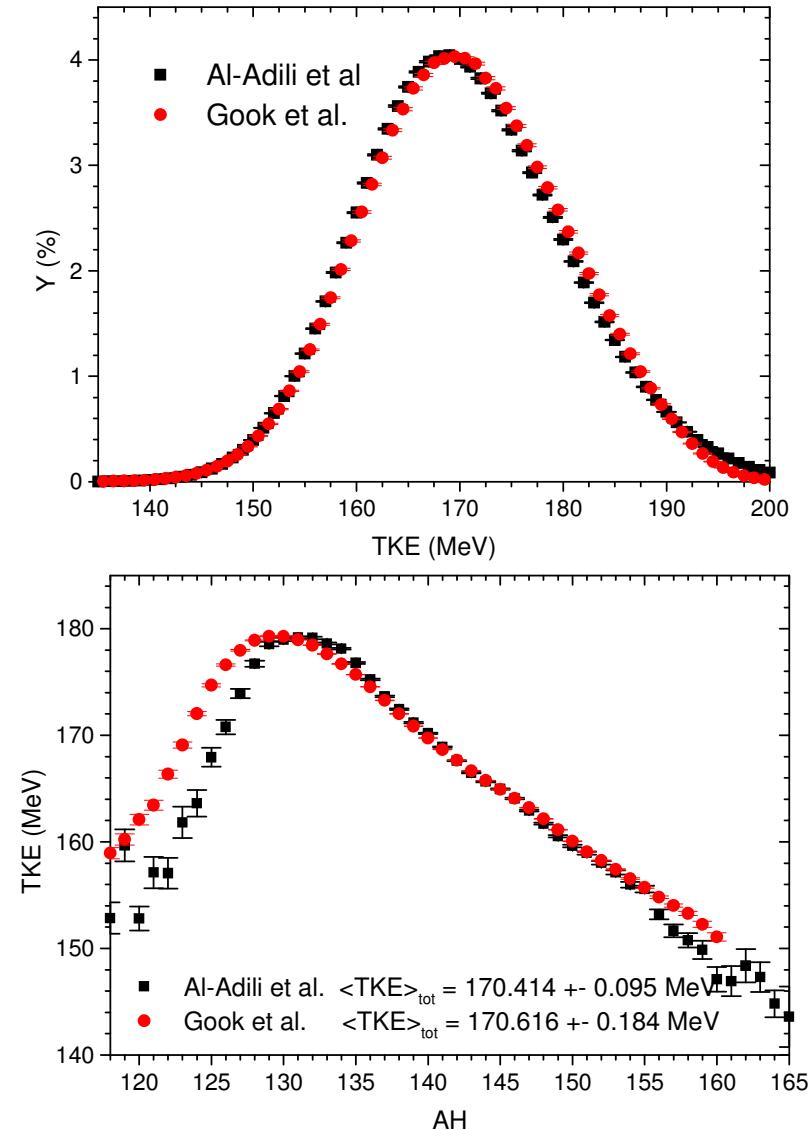
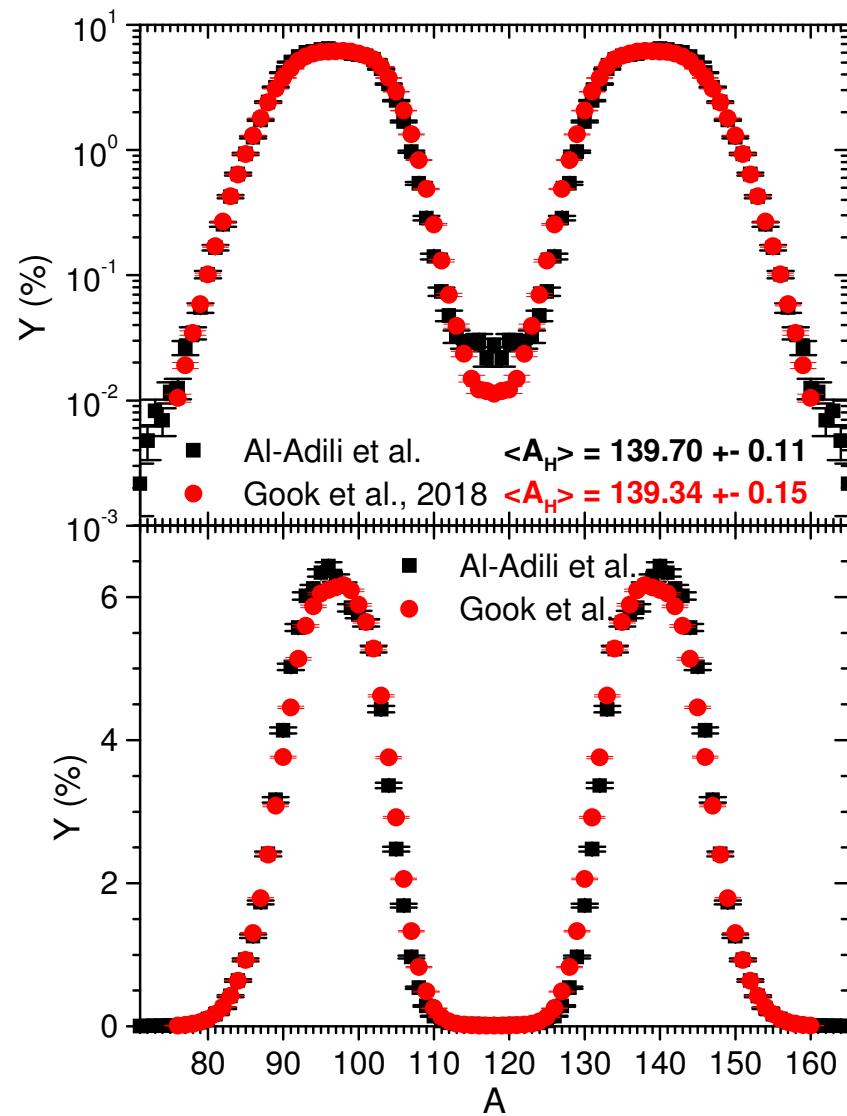
# CONCLUSIONS

The deterministic treatment of sequential emission applied to 49 fission cases allowed to obtain systematic behaviours and correlations between different average quantities characterizing the initial and residual fragments and the prompt neutron emission

1. The ratios  $\langle T \rangle / \langle Ti \rangle$  of LF, HF groups and of all fragments are of about 0.6 irrespective of the prescriptions used for  $\sigma_c(\epsilon)$  and the lev.dens.parameters, leading to a triangular  $P(T)$  with  $T_{\max} = 0.9 \langle Ti \rangle$  (*A.Tudora et al. EPJA 54 (2018)*)
  - $\langle T_k \rangle / \langle Ti \rangle = r_k$  (e.g.  $r_1=0.7$ ,  $r_2=0.5$  for LF, HF,  $r_3=0.425$  (LF), 0.35 (HF) etc.) allow to define  $P_k(T)$  for each emission sequence with  $T_{\max}^{(k)} = (3/2)r_k \langle Ti \rangle$  and the inclusion of sequential emission into the Los Alamos model.
2. The constant ratios  $\langle T \rangle / \langle Ti \rangle \sim 0.6$  and the linear behaviour of  $\langle \epsilon \rangle_{L,H}$  as a function of  $\langle T \rangle_{L,H}$  allow to obtain indicative values of different average prompt emission quantities in the absence of any prompt emission model.
3.  $\langle Er \rangle / \langle E^* \rangle$  of LF, HF groups and of all FF are of about 0.43 irrespective of the prescriptions mentioned above and also  $\langle Er_k \rangle / \langle E^* \rangle = r'_k$  ( $r'_1=0.55$ ,  $r'_2=0.3$  etc.)
4. The linear dependences of  $\langle \epsilon \rangle_k$  on  $\langle T \rangle_k$  and on  $(\langle Er \rangle_k)^{1/2}$  are the same for all emission sequences. Almost linear dependences of  $\langle \eta \rangle_k$  on  $\langle Sn \rangle_{k-1}$ ,  $\langle T \rangle_k$  and  $\langle a \rangle_k$  are established, too.

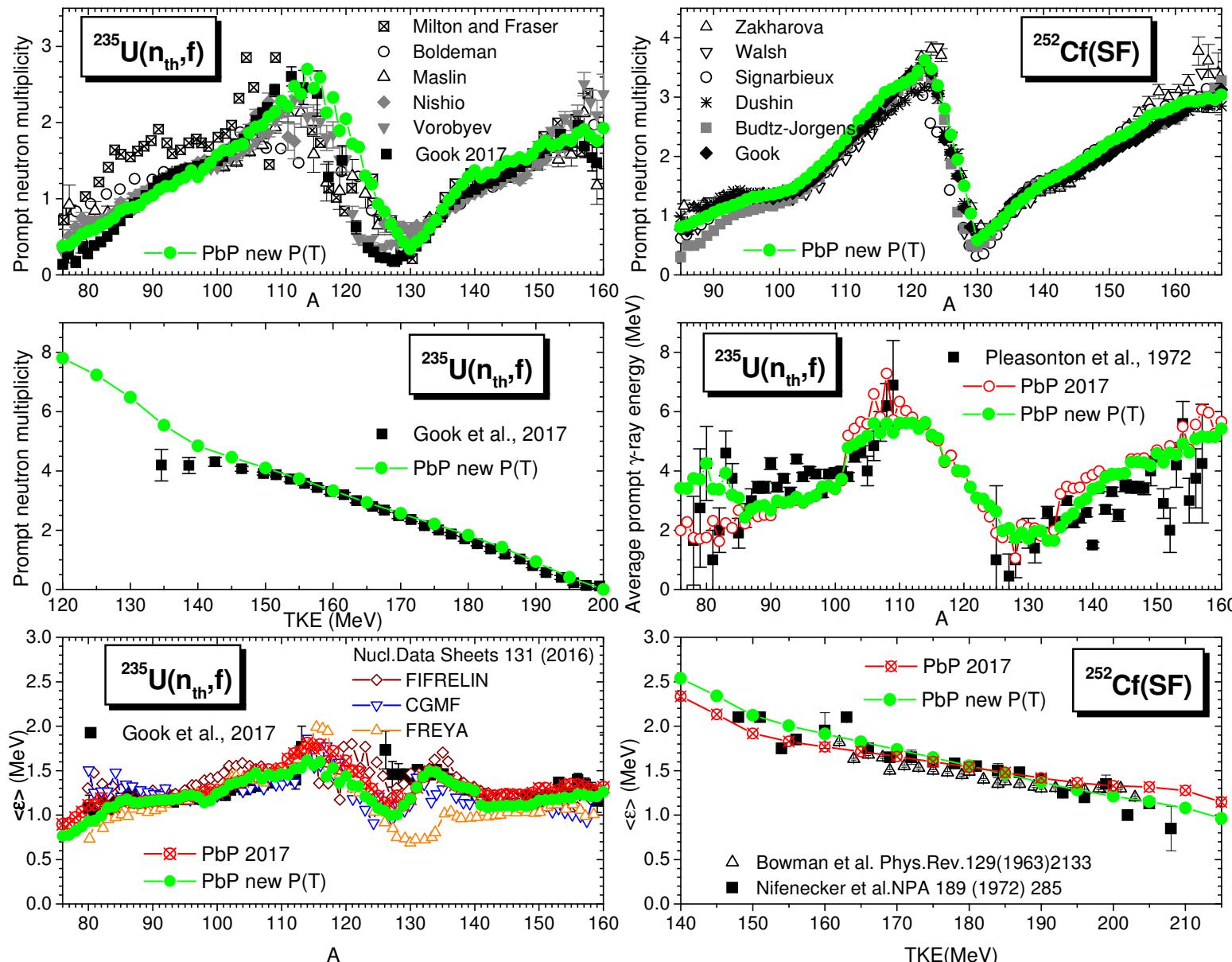
**Many thanks for your attention**

Fission fragment distributions of  $^{235}\text{U}(\text{n},\text{f})$  measured at JRC-Geel  
of Al-Adili et al. (black symbols) and of Göök et al. (red symbols)



# Examples of PbP results obtained with the new triangular form of P(T)

Fig.27 from A.Tudora et al. Eur.Phys.J A, 54 (2018) 87



# Examples of the linear correlation between the prompt $\gamma$ -ray energy and the prompt neutron multiplicity

