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# Integral data assimilation of the MERCI-1 experiment for the nuclear data associated with the PWR decay heat computation

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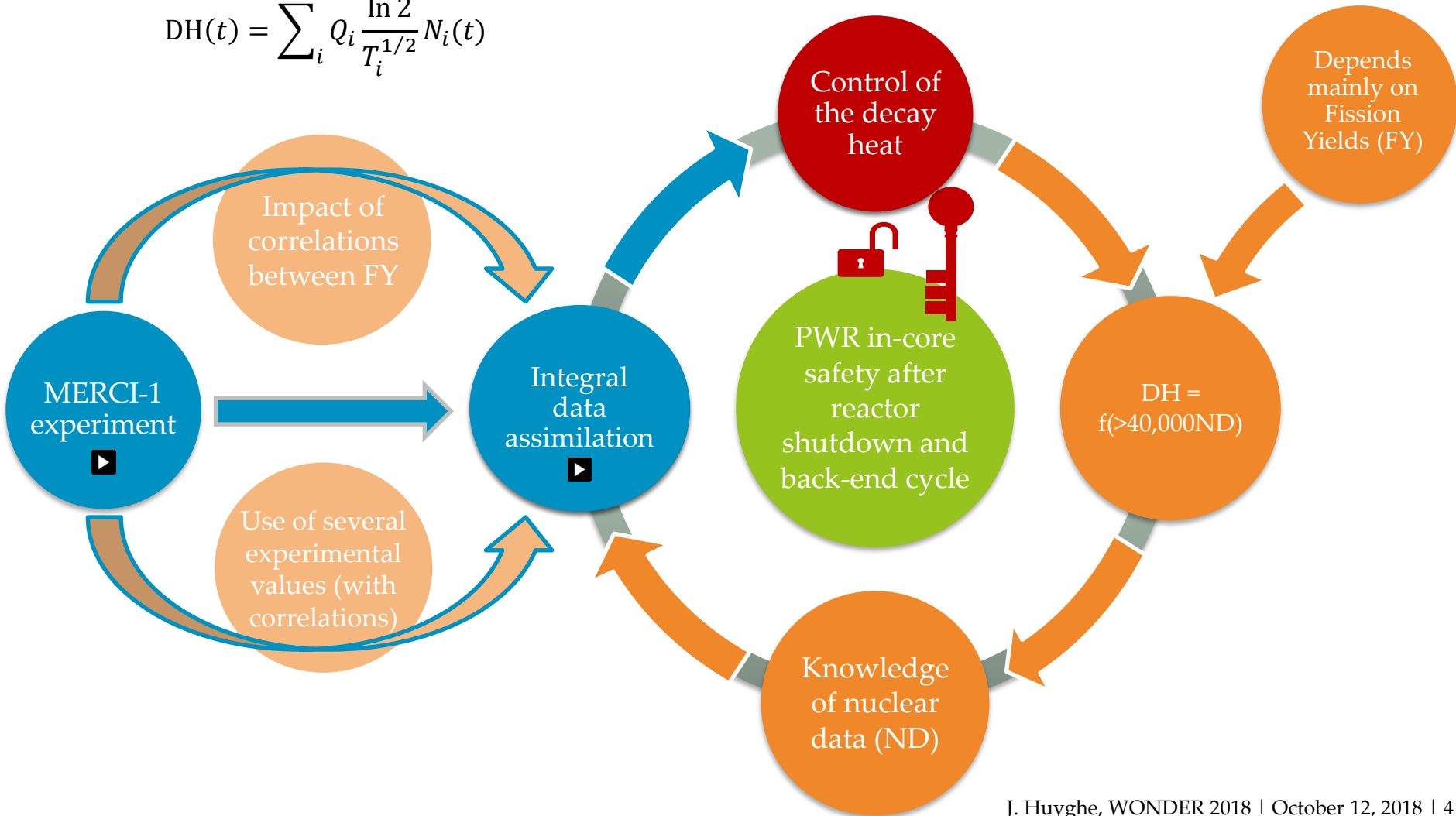


# Introduction

# Control of the decay heat for nuclear safety purposes

**Decay heat (DH)** = thermal power released by both radioactive decay of unstable fuel and material structure isotopes after reactor shutdown

$$DH(t) = \sum_i Q_i \frac{\ln 2}{T_i^{1/2}} N_i(t)$$



# MERCI-1 experiment overview

# MERCI-1 integral experiment (2008)<sup>1</sup>

- Irradiation of a **PWR UOX fuel rod sample** ( $e(^{235}\text{U}) = 3.7 \text{ wt.}\%$ ) in the OSIRIS reactor's reflector (CEA, Saclay, France) up to **3.6GWd/t<sub>HM</sub>**
- OSIRIS reactor core loaded with  $\text{U}_3\text{Si}_2\text{Al}$  plates ( $e(^{235}\text{U}) = 19.75 \text{ wt.}\%$ )
- Measurement of the decay heat released by the sample with the **MOSAIC calorimeter**<sup>2</sup> (measurements from 45 minutes to 42 days of cooling time) by an enthalpy balance on the secondary system of the calorimeter (heat pipe principle)<sup>2</sup>:

$$DH = Q_m C_p \Delta T \quad (1)$$

↙

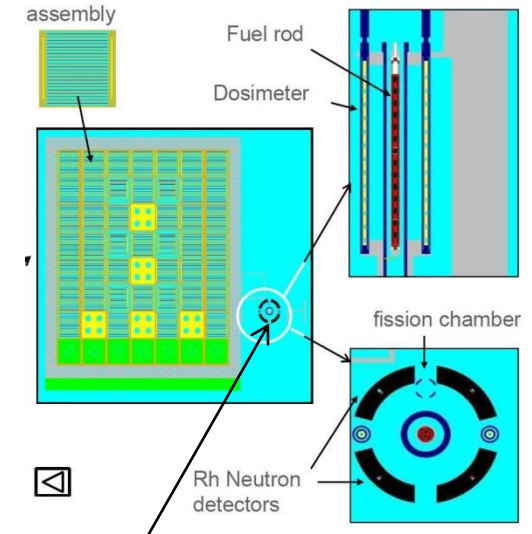
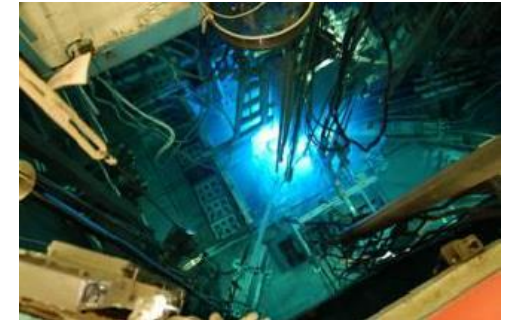
water mass flow

↓

heat capacity of water

↘

temperature difference between the inlet and the outlet of the condenser



MERCI device

1. J.C. Jaboulay, S. Bourganel, "Analysis of MERCI decay heat measurement for PWR UO<sub>2</sub> fuel rod", *Nuclear Technology*, Vol. 177, Jan. 2012

2. Ch. Blandin et al., "MERCI – MOSAIC: experimental tools for residual power measurement in the OSIRIS reactor", *IGORR 12*, 2009

# **Control of the uncertainties associated with the MERCI-1 experiment**

# MERCI-1 experimental uncertainty

$$DH = Q_m C_p \Delta T \quad (1)$$

Different sources of experimental uncertainties identified:  $Q_m$ ,  $C_p$ ,  $\Delta T$

- Assumed independent → global uncertainty on DH obtained by quadratic summation
  - no correlations between  $Q_m$  and  $C_p$
  - no correlations between  $Q_m$  and  $\Delta T$
  - correlations between  $C_p$  and  $\Delta T$  determined: negligible in the propagation calculation
- The different uncertainty values associated with  $Q_m$ ,  $C_p$  and  $\Delta T$  were found in internal documents and the literature<sup>3,4</sup>
- Uncertainties propagated to the DH → **0.5% at 1 std for cooling times ∈ [45 min ; 42 days]**  
 → **1.0% at 1 std for cooling times ∈ [16 ; 21 days] ∪ [23 ; 25 days]**

3. <https://webbook.nist.gov/chemistry/fluid/>

4. W. Wagner, A. Pruss, "The IAPWS formulation 1995 for the thermodynamic properties of ordinary water substance for general and scientific use", *J. Phys. Chem. Ref. Data*, 31, 2, 387-535, 2002



# MERCI-1 calculation uncertainty

Different sources of calculation uncertainties associated with the interpretation of the MERCI-1 experiment:

- **Adjustment of the burnup reached at the end of irradiation:**
  - ➔ adjustment performed by minimizing the calculation/experiment (C/E) discrepancies of the Nd concentrations ( $^{145,146,148,150}\text{Nd}$ ): depends on the cumulated FY uncertainties of  $^{235}\text{U}$  to  $^{1xx}\text{Nd}$
  - ➔ **resulting uncertainty on the DH: 1.1% at 1 std**
- **Irradiation conditions: fuel temperature, coolant temperature and  $^{235}\text{U}$  initial enrichment**
  - ➔ evaluated by (separate) direct perturbations in the transport calculation
  - ➔ **resulting uncertainty: between 0.1% at 45 min and 1.1% at 42 days of cooling (at 1 std)**

These different sources of calculation uncertainty + experimental uncertainty were propagated to the decay heat by quadratic summation (assuming they are all independent):

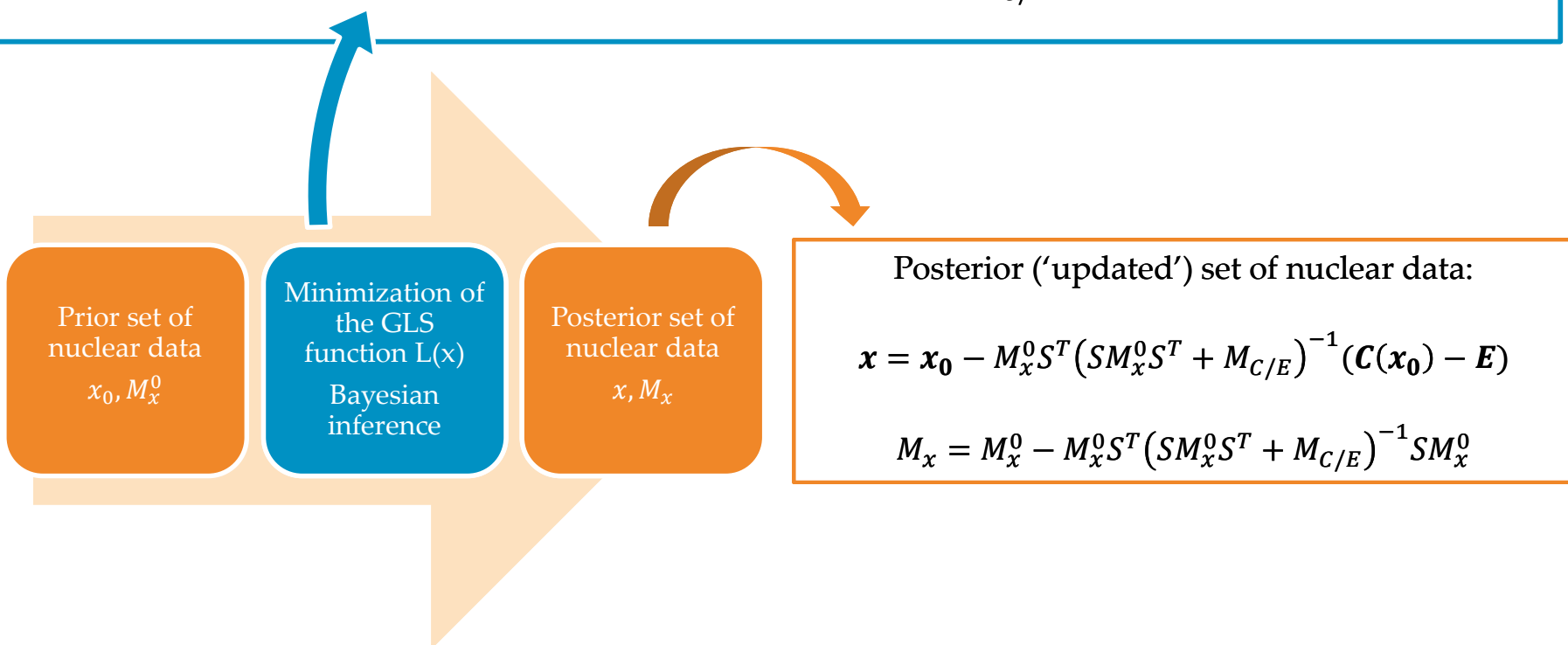
- ➔ result in a **global C/E decay heat uncertainty between 1.2 and 1.6% at 1 std** according to the cooling time considered

# **Integral Data Assimilation of the MERCI-1 experiment**

Integral data assimilation performed with the CONRAD code<sup>5</sup>: **CO**de for Nuclear **R**eaction **A**nalysis and **D**ata assimilation (developed at CEA, Cadarache)

→ assimilation of integral experiments (**C/E discrepancies + uncertainties** ( $\mathbf{M}_{C/E}$ )) to provide feedback on nuclear data of interest for the decay heat

$$L(\mathbf{x}) = (\mathbf{x} - \mathbf{x}_0)^T \mathbf{M}_x^0 (\mathbf{x} - \mathbf{x}_0) + (\mathbf{C}(\mathbf{x}) - \mathbf{E})^T \mathbf{M}_{C/E}^{-1} (\mathbf{C}(\mathbf{x}) - \mathbf{E})$$



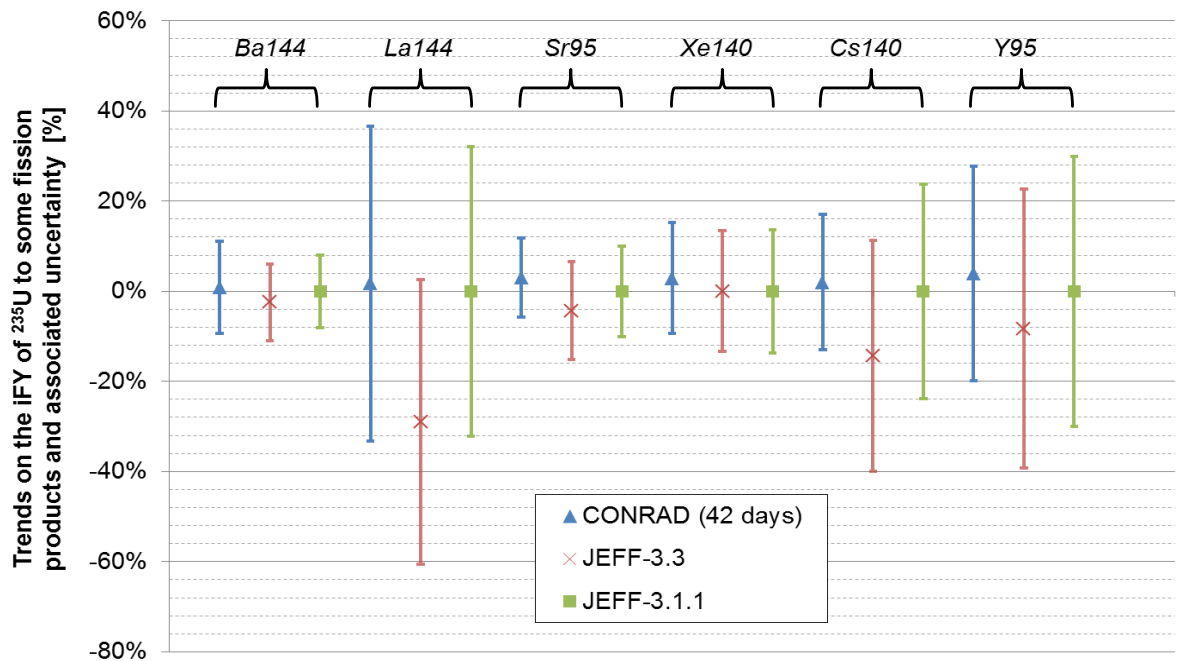
# 1. Assimilation of a particular MERCI-1 exp. value

Example case: standard PWR UOX fuel / BU = 15GWd/t<sub>HM</sub> / 1 year of cooling (e.g. fuel transport issues)

→ Assimilation of the last DH measurement of MERCI-1, *i.e.* at 42 days of cooling (C/E - 1 = -0.83% ± 1.6%)

→ DH = mainly sensitive to **independent FY (iFY) of <sup>235</sup>U to <sup>140</sup>Xe, <sup>140</sup>Cs, <sup>95</sup>Sr, <sup>95</sup>Y, <sup>144</sup>La, <sup>144</sup>Ba (42 days / 1 year)**

→ parameters fitted with CONRAD



- **Consistent trends** (posterior mean value + uncertainty) **with JEFF-3.3** at 1 std
- **No significant change in terms of uncertainty** except for iFY of <sup>235</sup>U to <sup>140</sup>Cs and <sup>95</sup>Y (reduced)

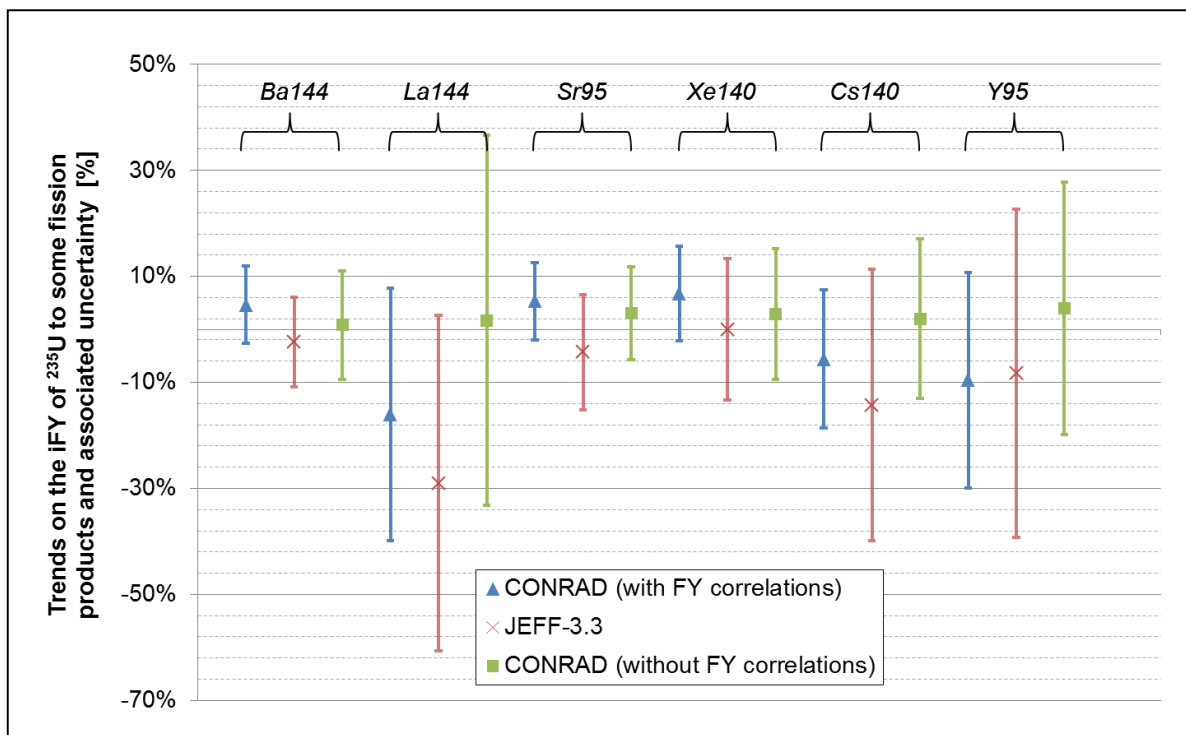
Feedbacks on JEFF-3.1.1 independent fission yield (iFY) data after assimilation of the MERCI-1 experimental at 42 days of cooling with CONRAD and comparison to JEFF-3.3 trends

## 2. Impact of correlations between iFY data

DH mainly sensitive to iFY // JEFF-3.1.1 does not provide covariance matrices for iFY

→ covariance matrices for both fissile systems of  $^{235}\text{U}$  and  $^{239}\text{Pu}$  produced at the CEA<sup>6</sup> associated with JEFF-3.1.1 iFY data, stored in the COMAC covariance matrix database<sup>7</sup>

→ Same integral data used for the assimilation (*i.e.* MERCI-1, 42 days) → impact of correlations between iFY



- **More consistent trends** (posterior mean value + uncertainty) **with JEFF-3.3** at 1 std (in particular for  $^{144}\text{La}$ ,  $^{140}\text{Cs}$ ,  $^{95}\text{Y}$ )

- **Reduced associated uncertainties**  
→ 15 to 30% uncertainty reduction compared to the 'without iFY correlations' case

→ **The iFY correlations will be taken into account from now on for this study**

6. N. Terranova, "Covariance evaluation for nuclear data of interest to the reactivity loss estimation of the Jules Horowitz Material Testing Reactor", PhD thesis, 2016

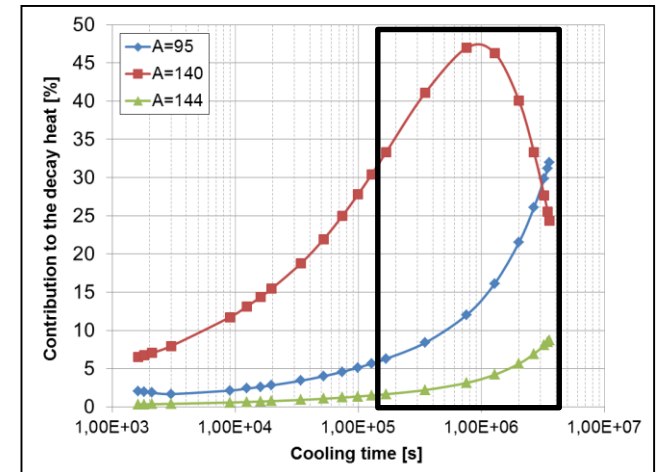
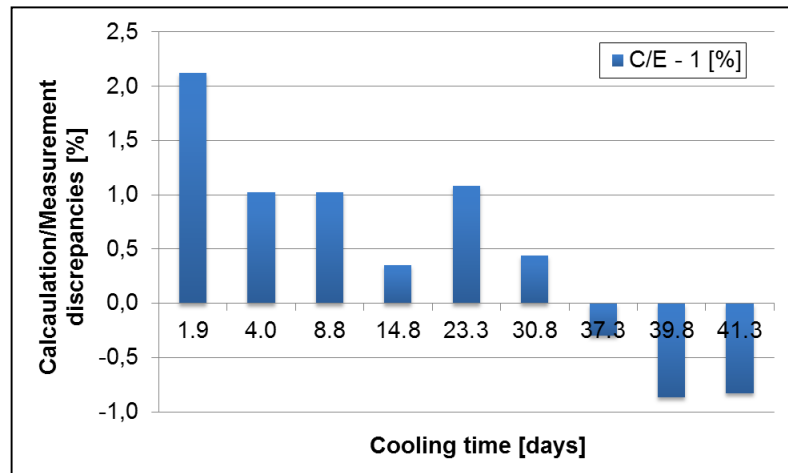
7. P. Archier et al., "COMAC: Nuclear data covariance matrices library for reactor applications", Proc. Int. Conf. PHYSOR, 2014

### 3. Assimilation of several experimental values – Which experimental data?

Improve the data assimilation process → **several experimental data used simultaneously**, *i.e.* MERCI-1 measurements at different cooling times → which experimental data?

→ Choice: based on the relative contribution of the fission products of interest to the DH (main masses A=95, 140 and, marginally, 144)

→ **9 experimental values considered** (example)



→ The simultaneous use of several experimental values coming from the same experiment raises issues of **experimental correlations** to consider for the data assimilation → determination?

### 3. Assimilation of several experimental values – Experimental correlations?

Determination of the **experimental covariances**?

$$DH = Q_m C_p \Delta T \quad (1)$$



$$\text{cov}(DH_a, DH_b) = \text{cov}(Q_{m_a} C_{p_a} \Delta T_a, Q_{m_b} C_{p_b} \Delta T_b)$$

The calculation decomposition involves several terms of covariance:

- $\alpha \times \text{cov}(C_{p_a}, C_{p_b})$
- $\beta \times \text{cov}(T_a, T_b)$
- $\gamma \times \text{cov}(Q_{m_a}, Q_{m_b})$

→  $\alpha \times \text{cov}(C_{p_a}, C_{p_b})$  determined by performing a polynomial regression (3<sup>rd</sup> order in good accordance with experimental data of  $C_p$ ) of  $C_p$  vs.  $T$ :

$$C_p(T) = aT^3 + bT^2 + cT + d$$

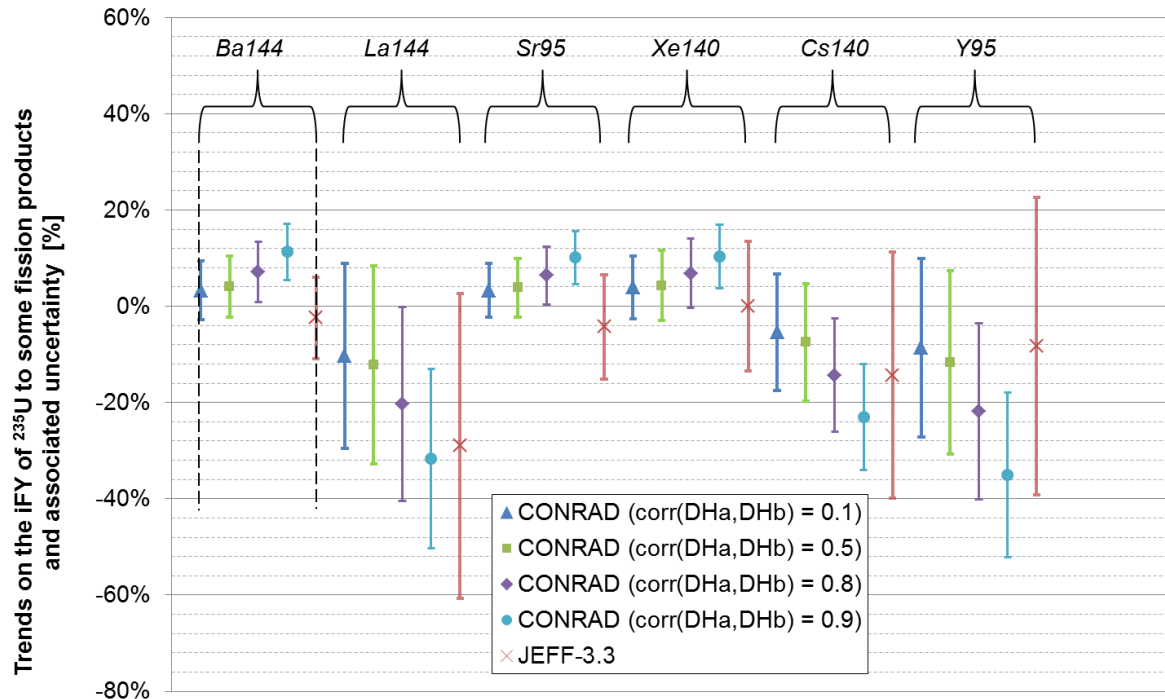
a, b, c and d determined with associated variances and covariances → propagation to  $\alpha \times \text{cov}(C_{p_a}, C_{p_b})$   
 → numerical applications for the nine experimental values taken: **negligible term** (given the values of  $\alpha, \beta, \gamma$ )

→  $\text{cov}(T_a, T_b), \text{cov}(Q_{m_a}, Q_{m_b})$  could not be assessed → lack of information thereon in the experimental process  
 → other methods?

→ **Different tests were performed** (with different experimental correlation values) to **measure the sensitivity of the assimilation results due to the experimental correlations considered**

### 3. Assimilation of several experimental values – Results

→ Different tests performed with experimental correlations of 0.1, 0.5, 0.8, 0.9



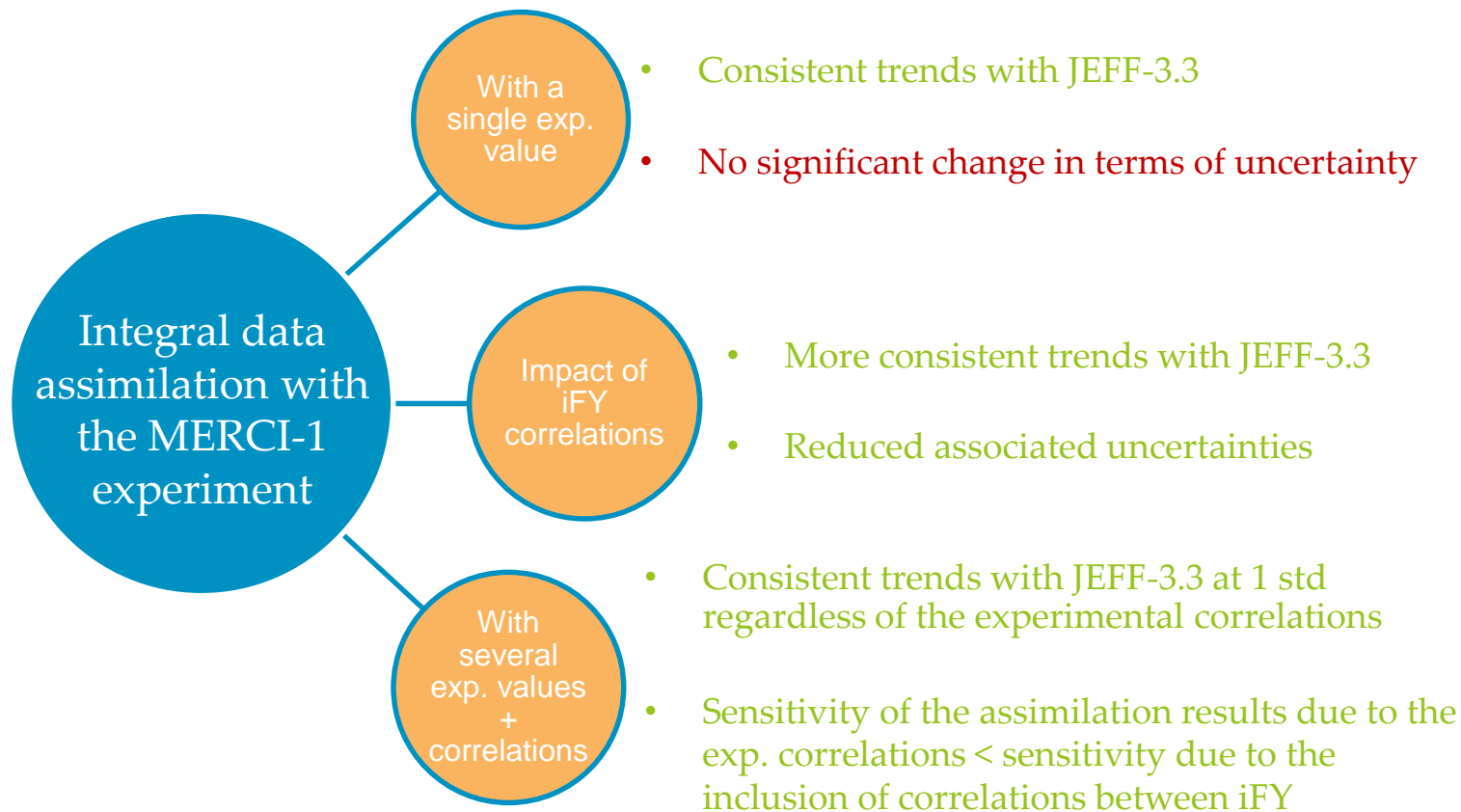
- Depending on the iFY studied, the trends get closer to JEFF-3.3
  - with lower exp. correlations for  $^{144}\text{Ba}$ ,  $^{140}\text{Xe}$ ,  $^{95}\text{Sr}$  and  $^{95}\text{Y}$
  - with higher exp. correlations for  $^{144}\text{La}$  and  $^{140}\text{Cs}$

- Consistent trends with JEFF-3.3 at 1 std regardless of the experimental correlations considered between each couple of DH values
- The sensitivity of the assimilation results due to the experimental correlations considered is lower than the sensitivity due to the inclusion of correlations between iFY
- The lower the exp. correlation, the more independent each experiment is with each other, and the more restrained the trends on each iFY are → cf. C/E discrepancies



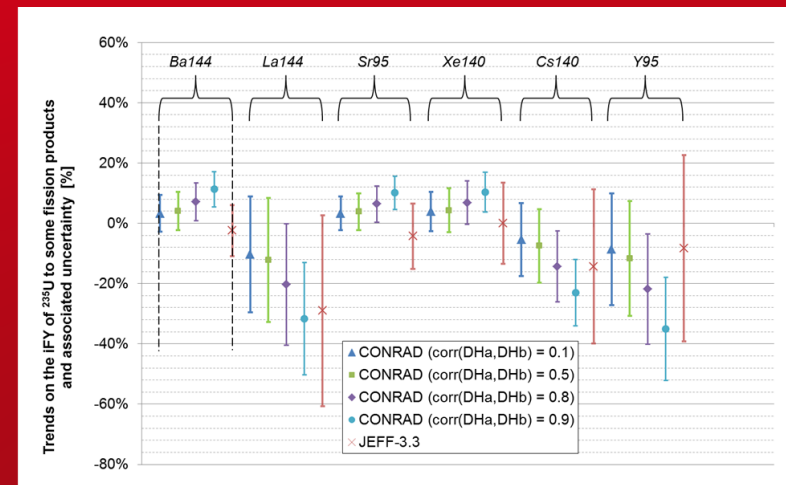
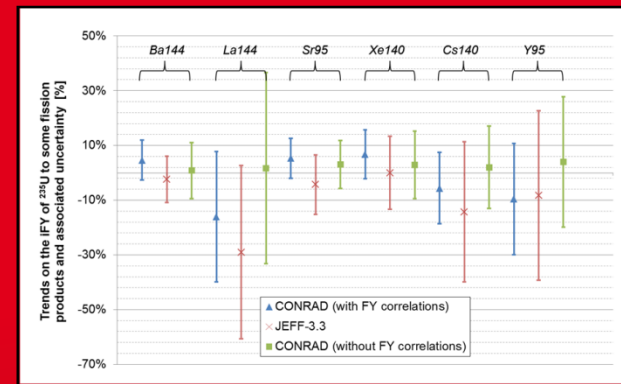
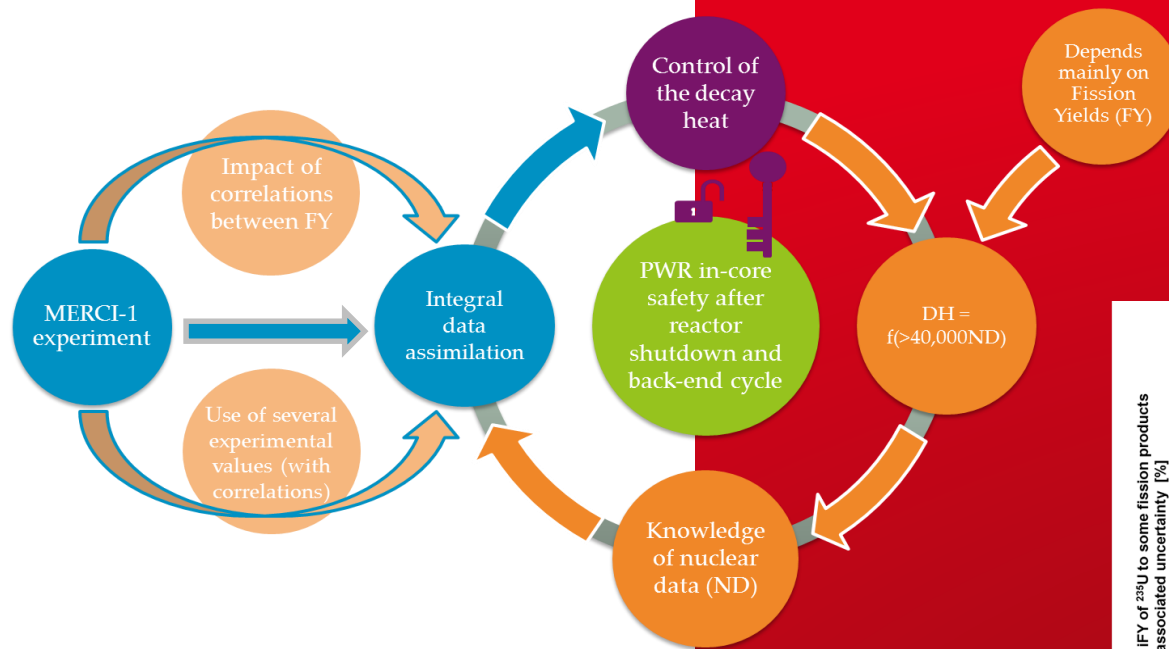
# Conclusions and perspectives

# Conclusions and perspectives



- ➔ Assimilating several correlated MERCI-1 experimental values and adding covariance information on iFY result in trends in better accordance with JEFF-3.3
- ➔ Need to accurately assess the experimental correlations since it has a direct impact on the assimilation results

# Thank you for your attention



$$L(\mathbf{x}) = (\mathbf{x} - \mathbf{x}_0)^T M_{\mathbf{x}}^{0^{-1}} (\mathbf{x} - \mathbf{x}_0) + (\mathbf{C}(\mathbf{x}) - \mathbf{E})^T M_{\mathbf{C}/\mathbf{E}}^{-1} (\mathbf{C}(\mathbf{x}) - \mathbf{E})$$

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