

# 4321

(or on how to make sense of the vector  
leptoquark solution of the B-anomalies)

High-energy implications of flavor anomalies  
CERN - 23.10.2018

Luca Di Luzio



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[Based on:

LDL, Greljo, Nardecchia - 1708.08450

LDL, Fuentes-Martin, Greljo, Nardecchia, Renner - 1808.00942]

# Outline

1. The EFT case for  $U \sim (3,1,2/3)$
2. 432 I: A renormalizable UV completion of  $U \sim (3,1,2/3)$ 
  - model building challenges
  - gauge & flavour structure
  - pheno (low-energy + high-pT)

# EFT [combined explanations]

- $SU(2)_L$  triplet operator as a natural starting point for explaining  $R(D) + R(K)^*$

$$-\frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell \left[ C_T (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) \right]$$

[Bhattacharya et al 1412.7164  
Alonso, Grinstein, Camalich 1505.05164,  
Greljo, Isidori, Marzocca 1506.01705,  
Calibbi, Crivellin, Ota 1506.02661, ... ]

$$Q_L^i = \begin{pmatrix} (V_{CKM}^\dagger u_L)^i \\ d_L^i \end{pmatrix}$$

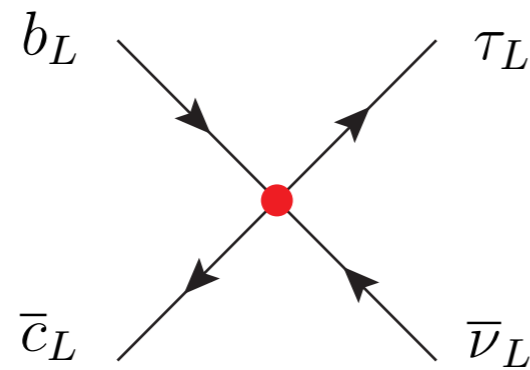
$$L_L^\alpha = \begin{pmatrix} \nu_L^\alpha \\ e_L^\alpha \end{pmatrix}$$

[\*see talks by O. Sumensari and D. Shih for alternative approaches]

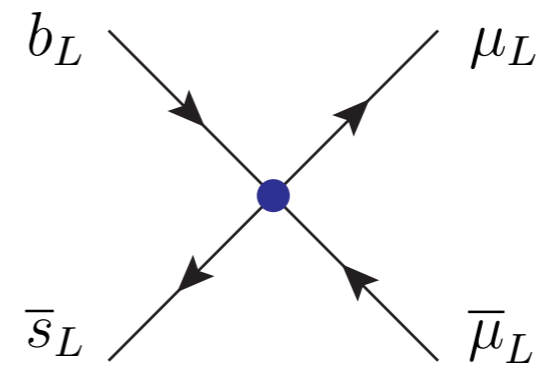
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$$\Lambda_{RD} = 3.4 \text{ TeV}$$



$$\Lambda_{RK} = 31 \text{ TeV}$$

$\ll$

- Perturbative unitarity bound from  $2 \rightarrow 2$  fermion scatterings (**worse case scenario**)

$$\sqrt{s_{RD}} < 9.2 \text{ TeV}$$

$$\sqrt{s_{RK}} < 84 \text{ TeV}$$



no-loose theorem for HL/HE-LHC ?

[LDL, Nardecchia 1706.01868]

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- Flavour structure:

1. large couplings in taus [*SM tree level*]

2. sizable couplings in muons [*SM one loop*]

3. negligible couplings in electrons [*well tested, not much room*]

$$\lambda_{ij}^{q,\ell} = \delta_{i3} \delta_{j3} + \text{corrections} \quad U(2)_q \times U(2)_\ell \quad \text{approx flavor symmetry}$$

[Barbieri et al | 105.2296, 1512.01560]



link to SM Yukawa pattern? [see talk by R. Ziegler]

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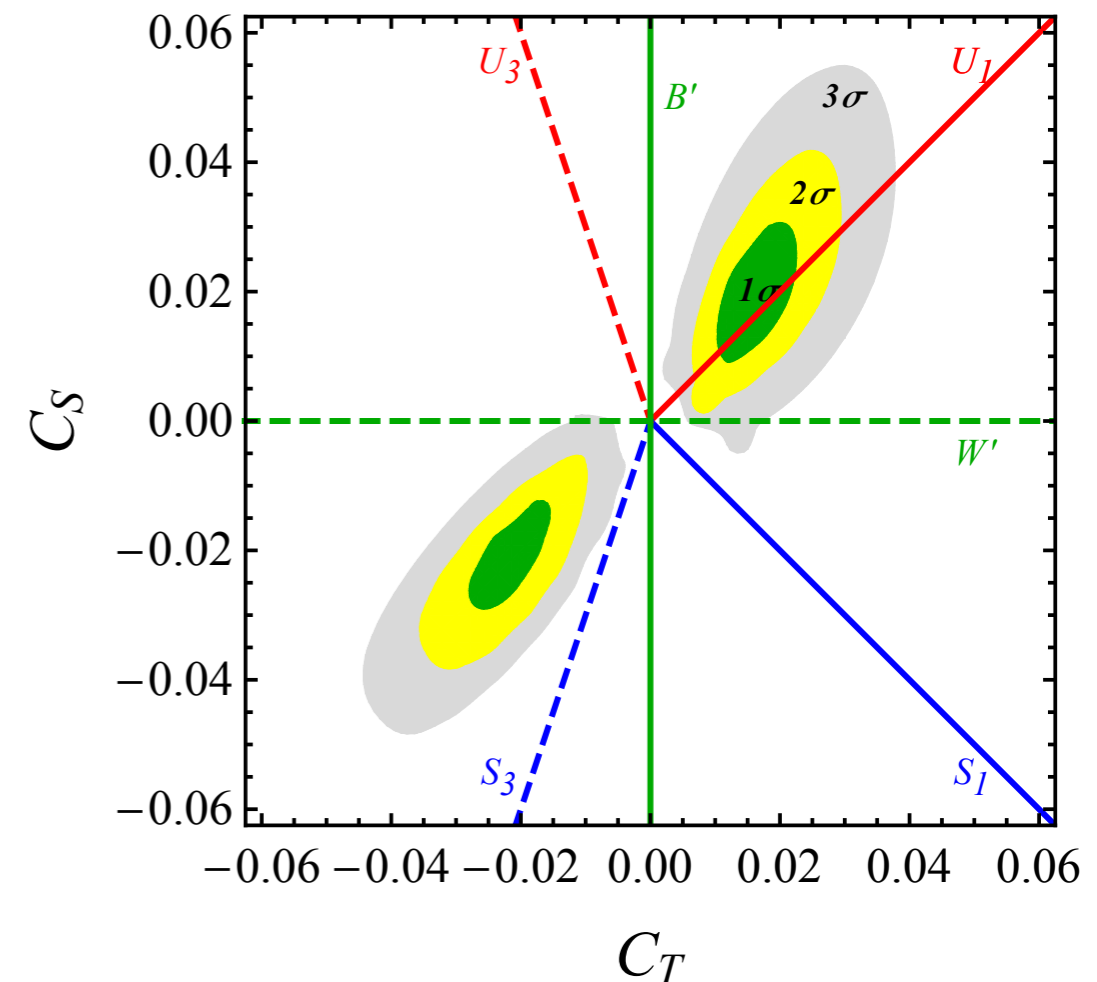
- Finite list of tree-level mediators

[Zürich's guide for combined explanations, 1706.07808]

| Simplified Model | Spin | SM irrep              | $C_S/C_T$ | $R_{D(*)}$ | $R_{K(*)}$ |
|------------------|------|-----------------------|-----------|------------|------------|
| $Z'$             | 1    | (1, 1, 0)             | $\infty$  | ×          | ✓          |
| $V'$             | 1    | (1, 3, 0)             | 0         | ✓          | ✓          |
| $S_1$            | 0    | ( $\bar{3}$ , 1, 1/3) | -1        | ✓          | ×          |
| $S_3$            | 0    | ( $\bar{3}$ , 3, 1/3) | 3         | ✓          | ✓          |
| $U_1$            | 1    | (3, 1, 2/3)           | 1         | ✓          | ✓          |
| $U_3$            | 1    | (3, 3, 2/3)           | -3        | ✓          | ✓          |



$U_1$  emerges as an exceptional single mediator consistent with various flavour/EW constraints



# UV completion: $U_1 \sim (3, 1, 2/3)$

- Massive vectors point to UV dynamics at the TeV scale

composite resonance of  
a new strong dynamics

gauge boson of an  
extended gauge sector

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$$\frac{G}{H} = \frac{SU(4) \times SO(5) \times U(1)_X}{SU(4) \times SO(4) \times U(1)_X}$$

[Barbieri, Isidori, Pattori, Senia | 502.01560  
Barbieri, Murphy, Senia | 611.0493  
Buttazzo, Greljo, Isidori, Marzocca | 706.07808  
Barbieri, Tesi | 712.06844]

- pNGB Higgs +  $U_1$  as composite state of  $G$ 
  - 😊 conceptual link with the naturalness issue of EW scale
  - 😞 light LQ lowers the whole resonances' spectrum (direct searches + EWPTs)
  - 😞 intrinsically non-calculable (e.g. Bs-mixing quadratically divergent)

[see also talks by B. Gripaios and D. Marzocca]



# UV completion: $U_1 \sim (3, 1, 2/3)$

- Pati-Salam (well-motivated, 44 years old)

$$G_{PS} = SU(4)_{PS} \times SU(2)_L \times SU(2)_R$$

$$G_{PS}/G_{SM} = U_1 + Z' + W_R$$

gauge boson of an  
extended gauge sector

😊 hinted by SM chiral structure and neutrino masses + one step from SO(10)

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- 😞  $M_{U_1} \gtrsim 100$  TeV from  $K_L^0, B^0, B_s \rightarrow \ell \ell'$  [ $L \times R$  couplings both present by unitarity]
- 😞  $Z'$  direct searches [ $M_{U_1} \sim M_{Z'} \sim$  TeV +  $O(g_s)$   $Z'$  couplings to valence quarks]
- 😞 neutrino masses also suggest  $M_{U_1} \gg$  TeV [ $y_{\text{top}} \sim y_{\nu_3\text{-Dirac}}$ ]

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➔ LQ of minimal PS cannot explain B-anomalies

[Non-minimal PS options lack the beauty and simplicity of the minimal construction: Calibbi, Crivellin, Li 1709.00692, Bordone, Cornella, Fuentes-Martin, Isidori 1712.01368 + 1805.09328, Blanke, Crivellin 1801.07256, Heeck, Teresi 1808.07492 ... ]

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➔ step 0: does a gauge UV completion of  $U_1$  addressing these three phenomenological issues (in order to be a viable solution of B-anomalies) exist?

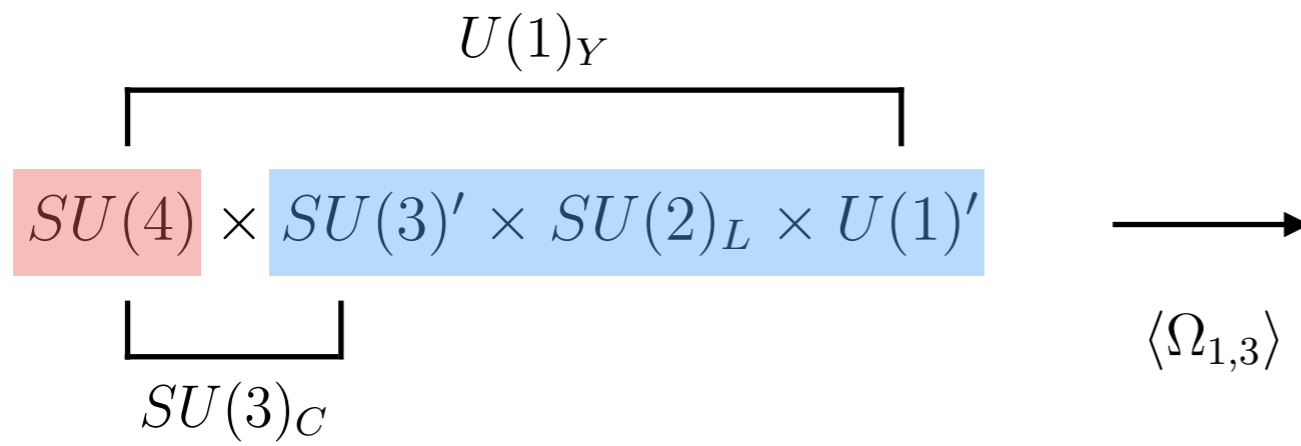
# The '4321' model

[LDL, Greljo, Nardecchia | 708.08450,  
See also Diaz, Schmaltz, Zhong | 706.05033]

$$SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$$

# The '4321' model

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$$G_{\text{SM}} = SU(3)_C \times SU(2)_L \times U(1)_Y$$

SM embedding:

$$SU(3)_C = (SU(3)_4 \times SU(3)')_{diag}$$

$$U(1)_Y = (U(1)_4 \times U(1)')_{diag}$$

$$g_4 \gg g_3 \gg g_1$$



$$g_s = \frac{g_4 g_3}{\sqrt{g_4^2 + g_3^2}} \simeq g_3$$

$$g_Y = \frac{g_4 g_1}{\sqrt{g_4^2 + \frac{2}{3} g_1^2}} \simeq g_1$$

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$$\begin{array}{ccc}
 & \overbrace{\hspace{10em}}^{U(1)_Y} & \\
 & \boxed{SU(4) \times SU(3)' \times SU(2)_L \times U(1)'} & \longrightarrow \\
 & \underbrace{\hspace{3em}}_{SU(3)_C} & \langle \Omega_{1,3} \rangle \\
 & & G_{\text{SM}} = SU(3)_C \times SU(2)_L \times U(1)_Y
 \end{array}$$


SM embedding:

Massive gauge bosons:

$$G/G_{\text{SM}} = U + Z' + g'$$

$$M_{g'} \simeq \sqrt{2} M_U \quad M_{Z'} \simeq \frac{1}{\sqrt{2}} M_U$$

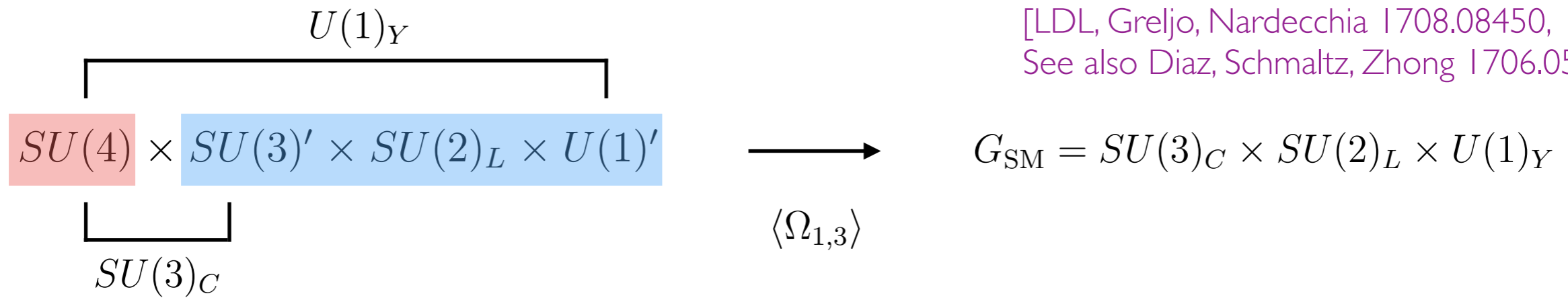
$$\begin{pmatrix}
 (g'_a)_\beta^\alpha \vdots U_\mu^\alpha \\
 \dots \vdots \dots \\
 (U_\mu^\beta)^\dagger \vdots Z'_\mu
 \end{pmatrix}$$

 cannot decouple  $g'$  and  $Z'$  from LQ mass scale !

[a theorem (?) that in whatever UV construction  $U$  always comes with a  $Z'$  - while the coloron is a specific consequence of the 4321 model]

# The '4321' model

[LDL, Greljo, Nardecchia | 708.08450,  
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Matter content:

| Field      | $SU(4)$   | $SU(3)'$ | $SU(2)_L$ | $U(1)'$ |
|------------|-----------|----------|-----------|---------|
| $q_L^i$    | 1         | 3        | 2         | 1/6     |
| $u_R^i$    | 1         | 3        | 1         | 2/3     |
| $d_R^i$    | 1         | 3        | 1         | -1/3    |
| $\ell_L^i$ | 1         | 1        | 2         | -1/2    |
| $e_R^i$    | 1         | 1        | 1         | -1      |
| $\Psi_L^i$ | 4         | 1        | 2         | 0       |
| $\Psi_R^i$ | 4         | 1        | 2         | 0       |
| $H$        | 1         | 1        | 2         | 1/2     |
| $\Omega_3$ | $\bar{4}$ | 3        | 1         | 1/6     |
| $\Omega_1$ | $\bar{4}$ | 1        | 1         | -1/2    |

Would-be SM fields

Vector-like fermions ( $Q'+L'$ )

SSB

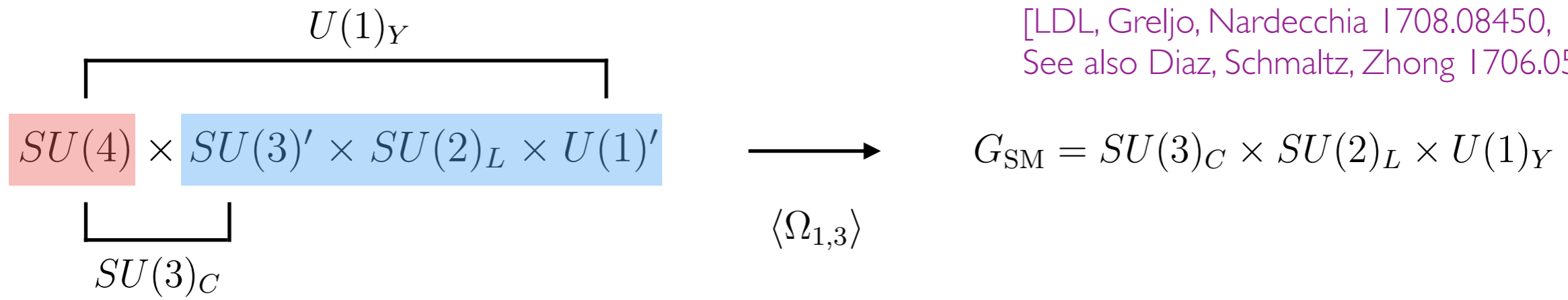


mix after SSB



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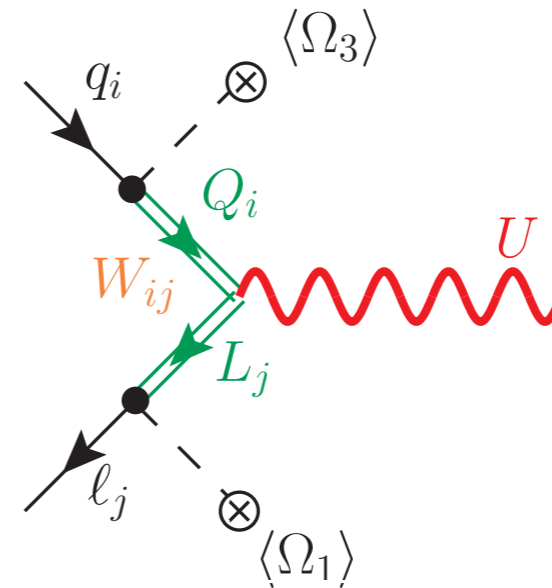


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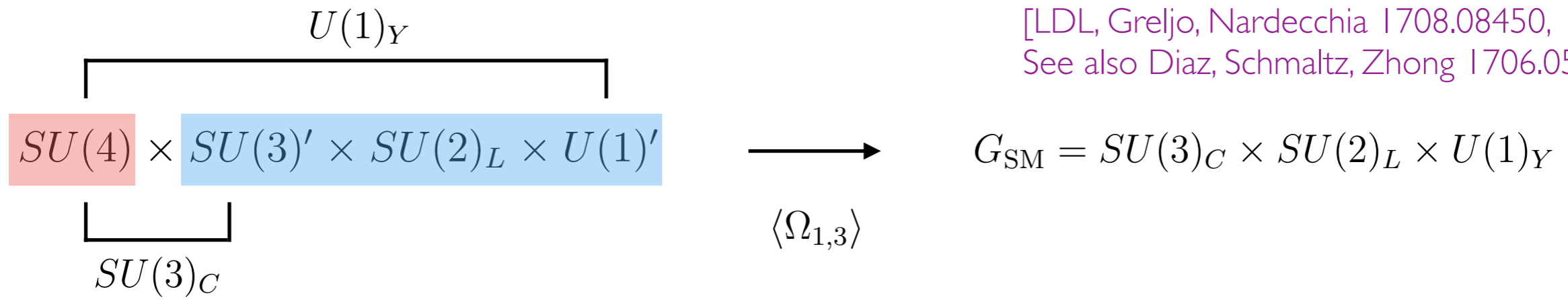
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LQ dominantly couples to 3rd generation LH fields:  
[matches in first approx. EFT analysis for B-anomalies +  
relaxes flavour bounds from chirality enhanced meson decays]



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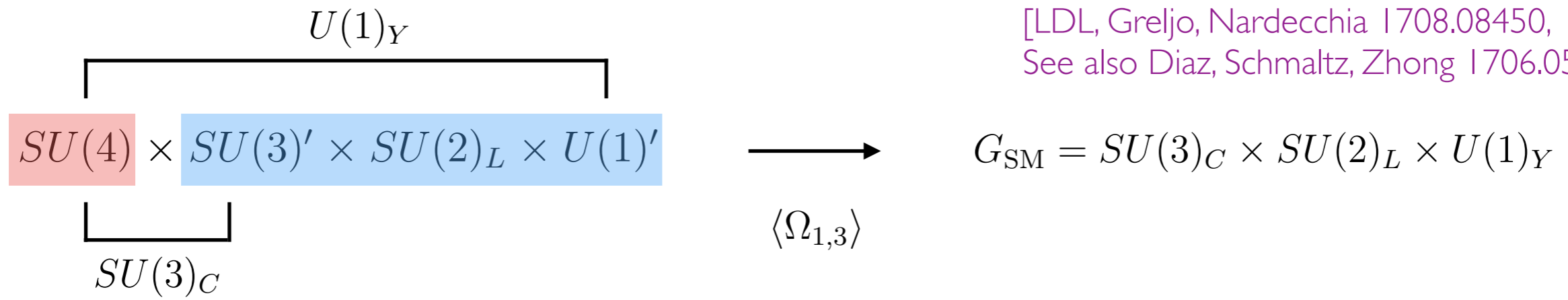


Suppressed  $Z'$  and  $g'$  couplings to light generations  
[requires phenomenological limit  $g_4 \gg g_3 \simeq g_s \gg g_1 \simeq g_Y$ ]

$$\begin{aligned} \mathcal{L}_L = & \frac{g_4}{\sqrt{2}} \bar{Q}'_L \gamma^\mu L'_L U_\mu + \text{h.c.} \\ & + g_s \left( \frac{g_4}{g_3} \bar{Q}'_L \gamma^\mu T^a Q'_L - \frac{g_3}{g_4} \bar{q}'_L \gamma^\mu T^a q'_L \right) g'_\mu{}^a \\ & + \frac{1}{6} \sqrt{\frac{3}{2}} g_Y \left( \frac{g_4}{g_1} \bar{Q}'_L \gamma^\mu Q'_L - \frac{2}{3} \frac{g_1}{g_4} \bar{q}'_L \gamma^\mu q'_L \right) Z'_\mu \\ & - \frac{1}{2} \sqrt{\frac{3}{2}} g_Y \left( \frac{g_4}{g_1} \bar{L}'_L \gamma^\mu L'_L - \frac{2}{3} \frac{g_1}{g_4} \bar{\ell}'_L \gamma^\mu \ell'_L \right) Z'_\mu \end{aligned}$$

# The '4321' model

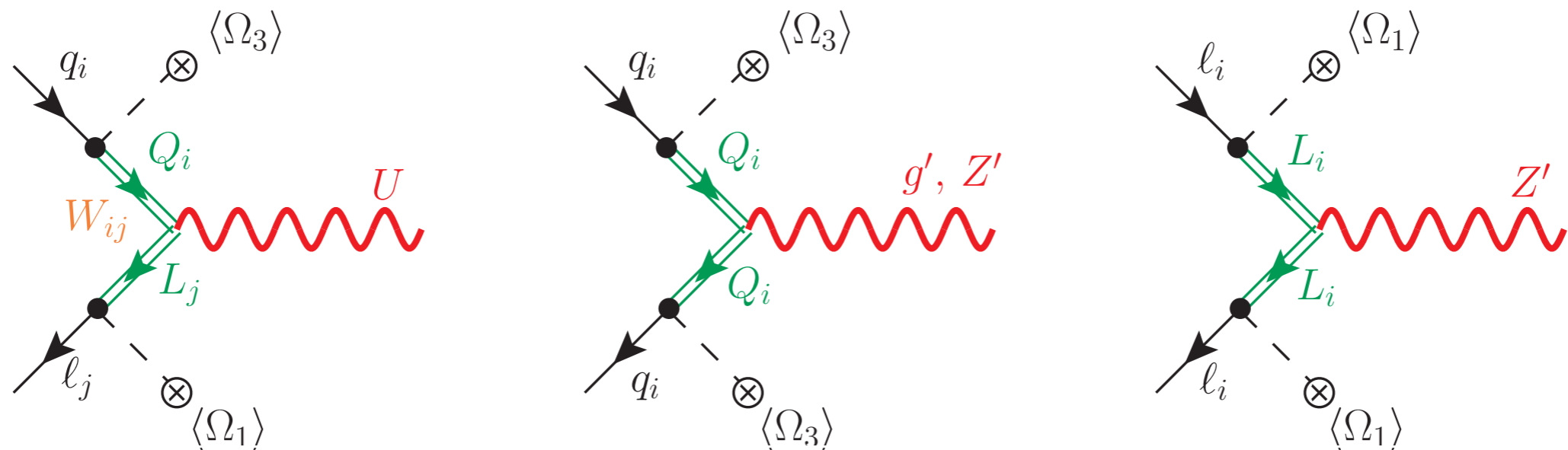
[LDL, Greljo, Nardecchia | 708.08450,  
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*[matches in first approx. EFT analysis for B-anomalies + relaxes flavour bounds from chirality enhanced meson decays]*
- Suppressed  $Z'$  and  $g'$  couplings to light generations  
*[requires phenomenological limit  $g_4 \gg g_3 \simeq g_s \gg g_1 \simeq g_Y$ ]*
- B and L accidental global symmetries  
*[neutrino massless as in the SM]*

# Key phenomenological features

1. Large quark-lepton transitions in 3-2 sector
2. Tree-level FCNC involving down quarks and leptons are absent
3. Tree-level FCNC involving up quarks are U(2) protected

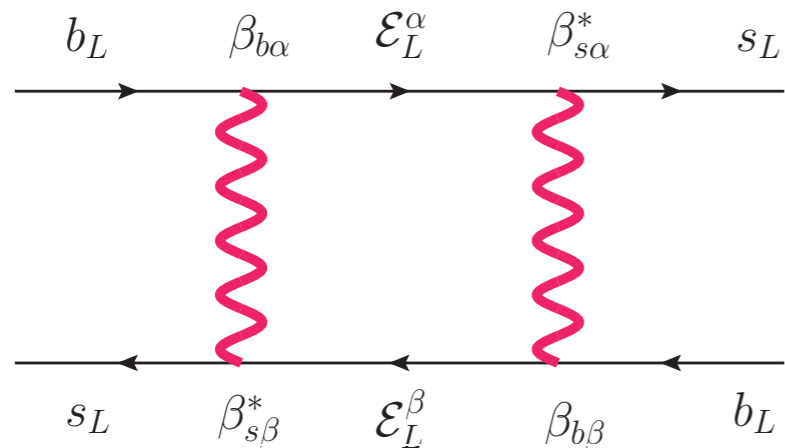


[see backup slides for the discussion of the flavour structure]

[LDL, Fuentes-Martin, Greljo, Nardecchia, Renner | 808.00942]

# Key phenomenological features

1. Large quark-lepton transitions in 3-2 sector
2. Tree-level FCNC involving down quarks and leptons are absent
3. Tree-level FCNC involving up quarks are U(2) protected
4. FCNC @ 1-loop under control



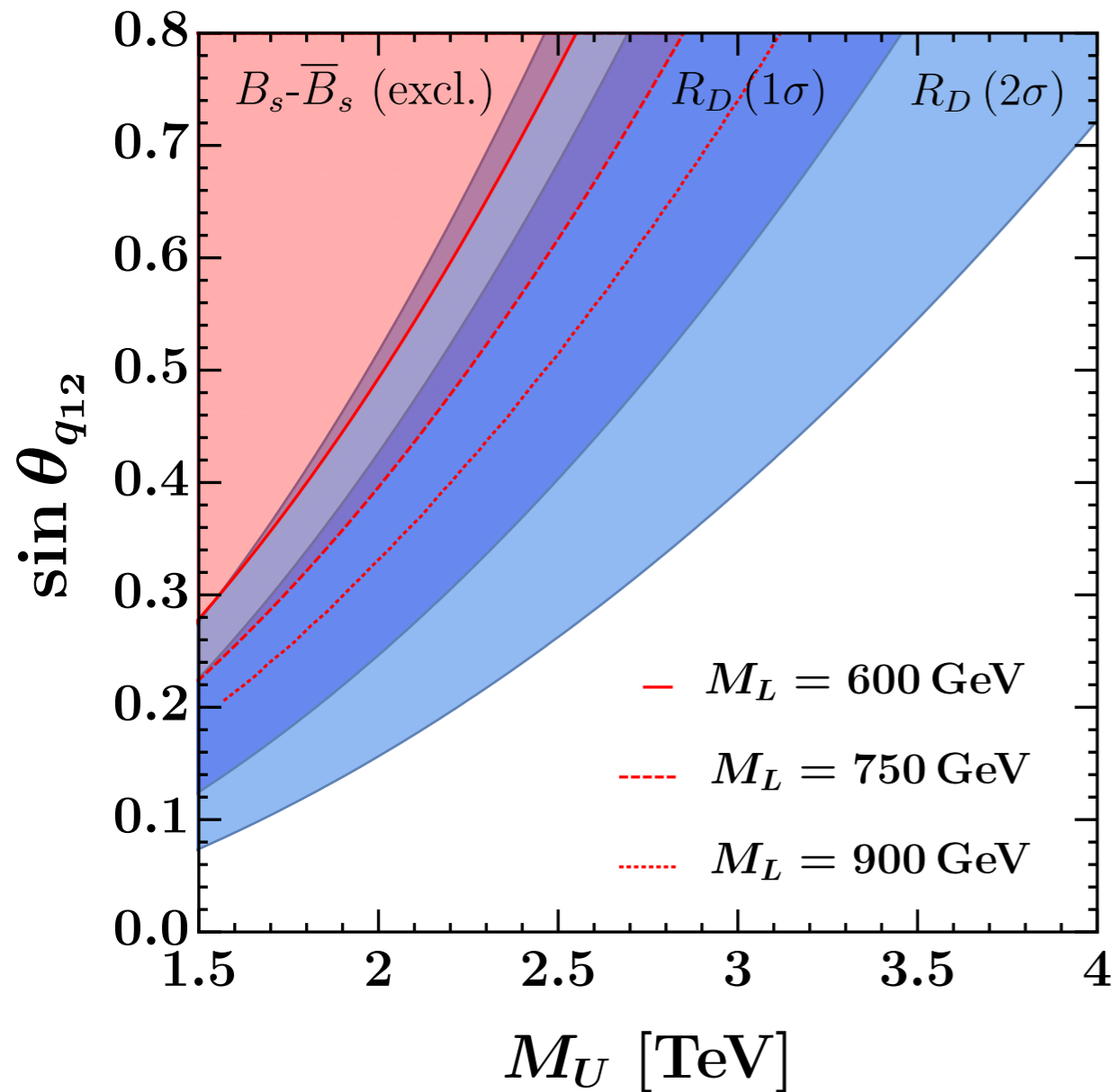
$$\mathcal{H}_{\text{eff}}^{\text{NP}} = -\frac{g_4^4}{128\pi^2 m_U^2} (\bar{b}_L \gamma^\mu s_L) (\bar{b}_L \gamma_\mu s_L) \sum_{\alpha, \beta} \lambda_\alpha \lambda_\beta F(x_\alpha, x_\beta)$$

$$\lambda_\alpha = \beta_{b\alpha} \beta_{s\alpha}^* \quad x_\alpha = m_\alpha^2 / M_U^2 \quad \alpha = (1, \dots, 6)$$

$$\sum_{\alpha} \lambda_\alpha = 0 \quad [\text{ensures cancellation of quadratic divergences}]$$

$$F(x_\alpha, x_\beta) \simeq \cancel{1} + x_\alpha + x_\beta + \dots \quad \longrightarrow \quad \text{dynamical suppression from light lepton partners}$$

# Low-energy / high-pT interplay

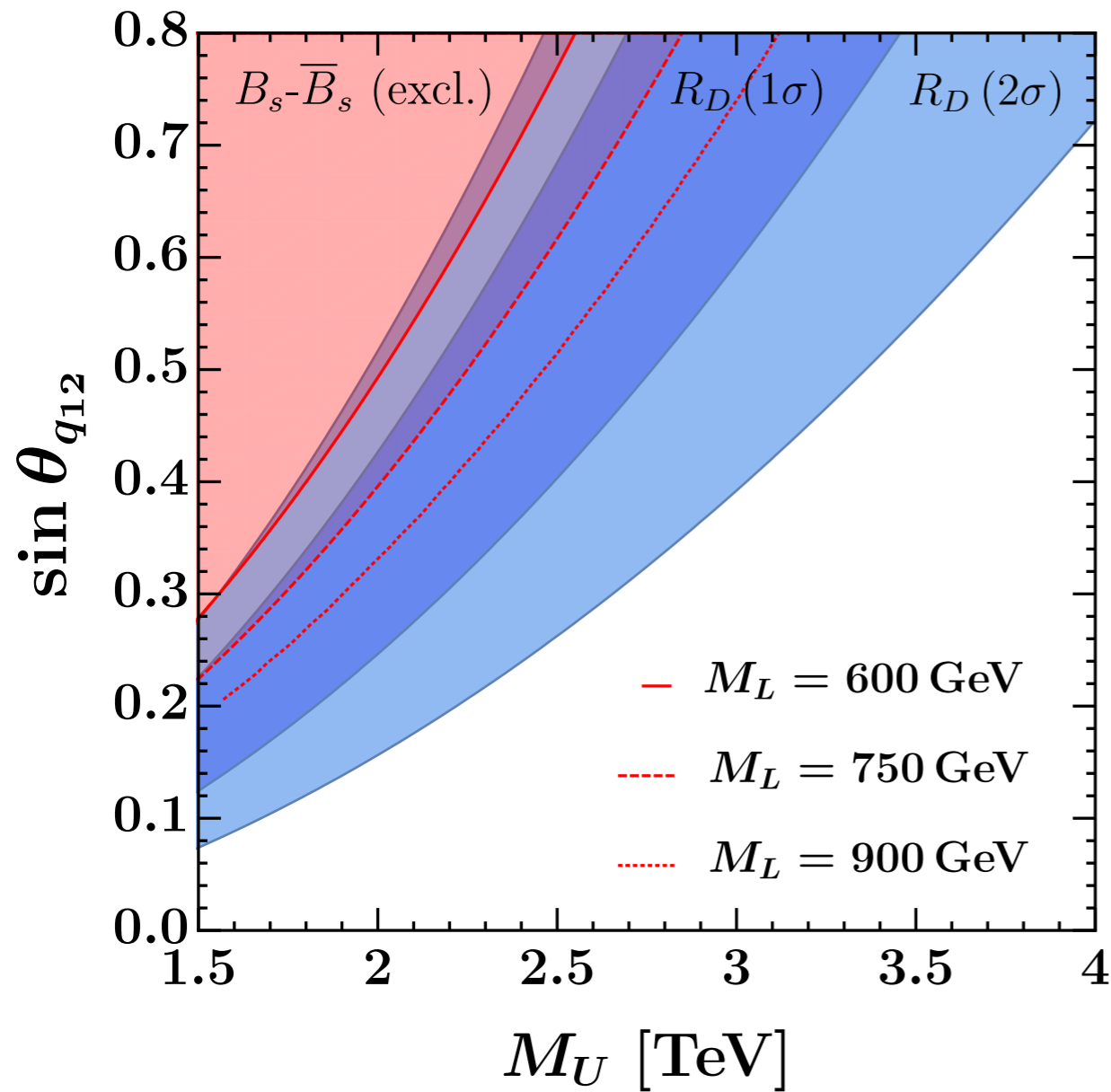


$$C_{bs}^{LL} \sim \Delta R_{D(*)}^2 M_L^2$$



vector-like leptons are predicted to be the lightest new states !

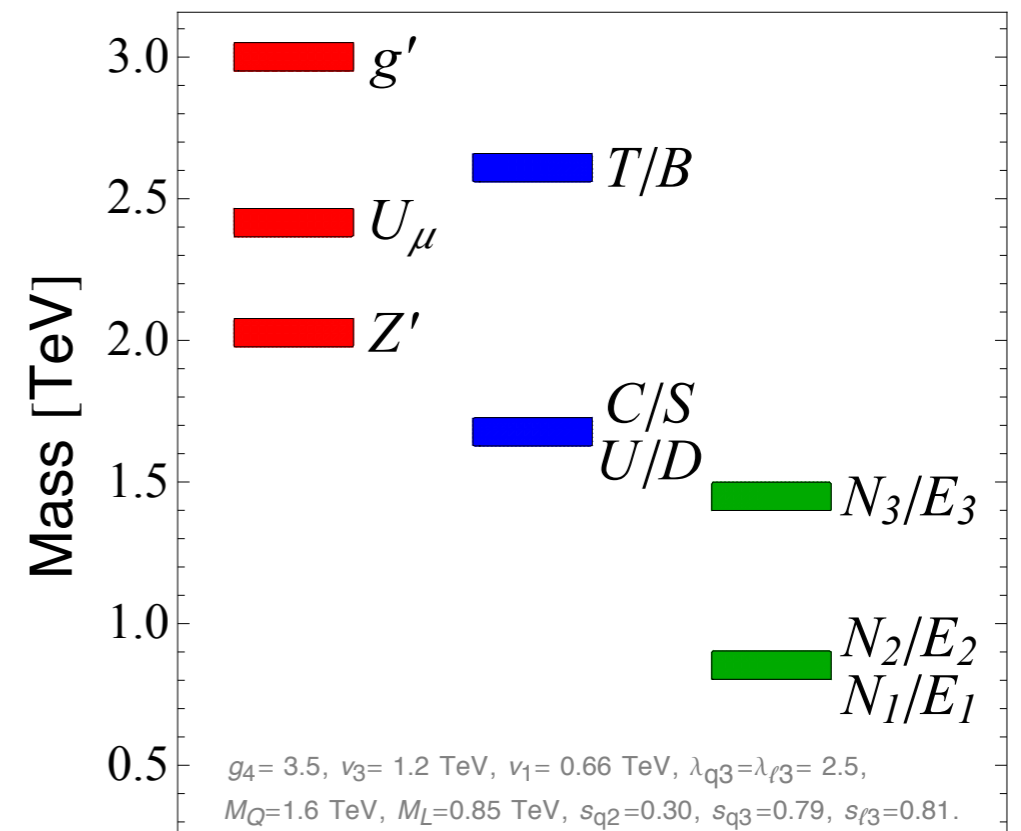
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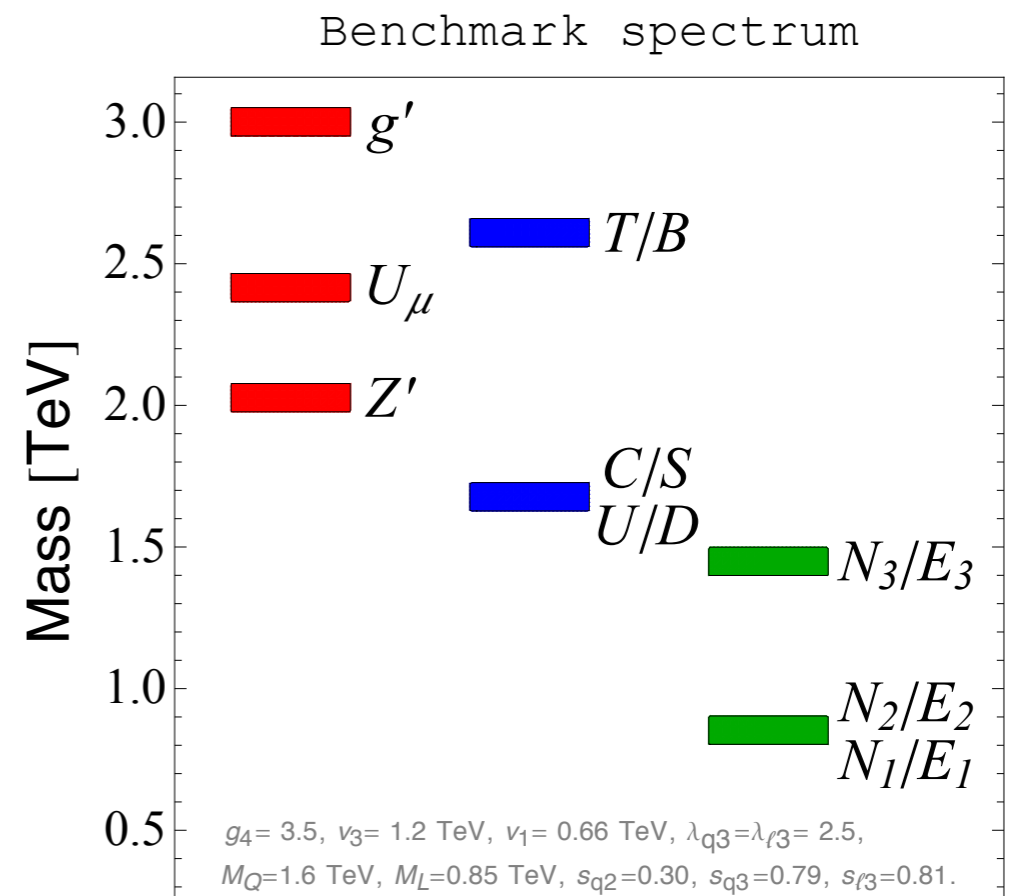
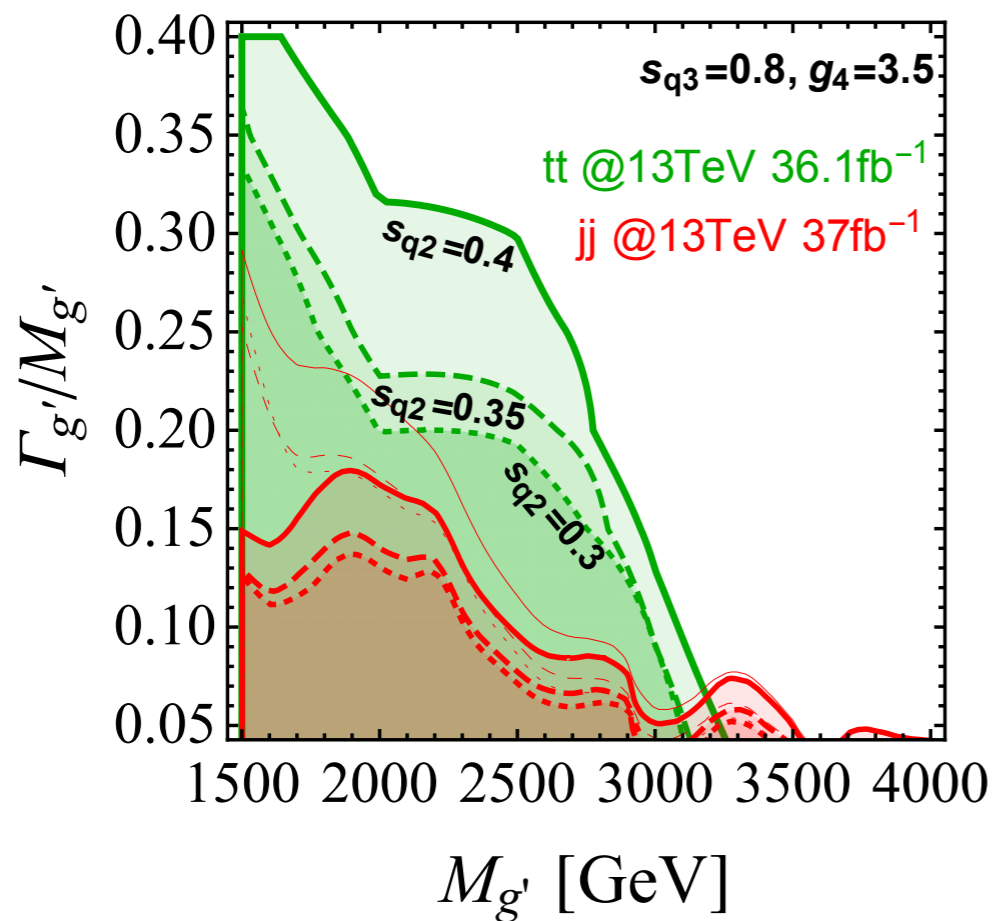
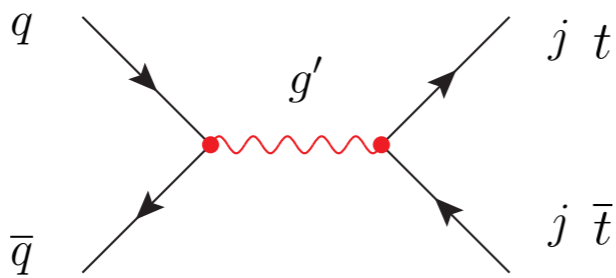


Benchmark spectrum



# High- $p_T$ highlights

- Coloron searches push the whole spectrum up

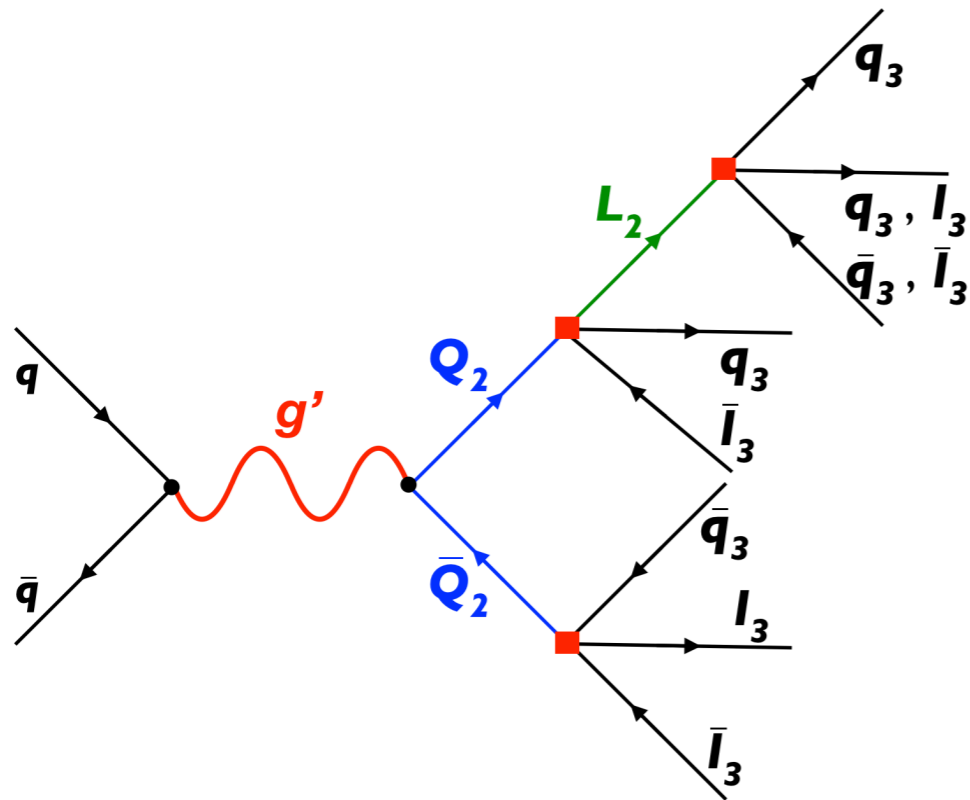
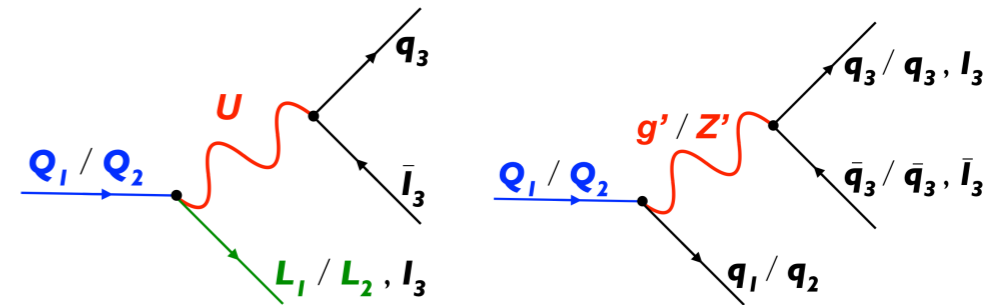




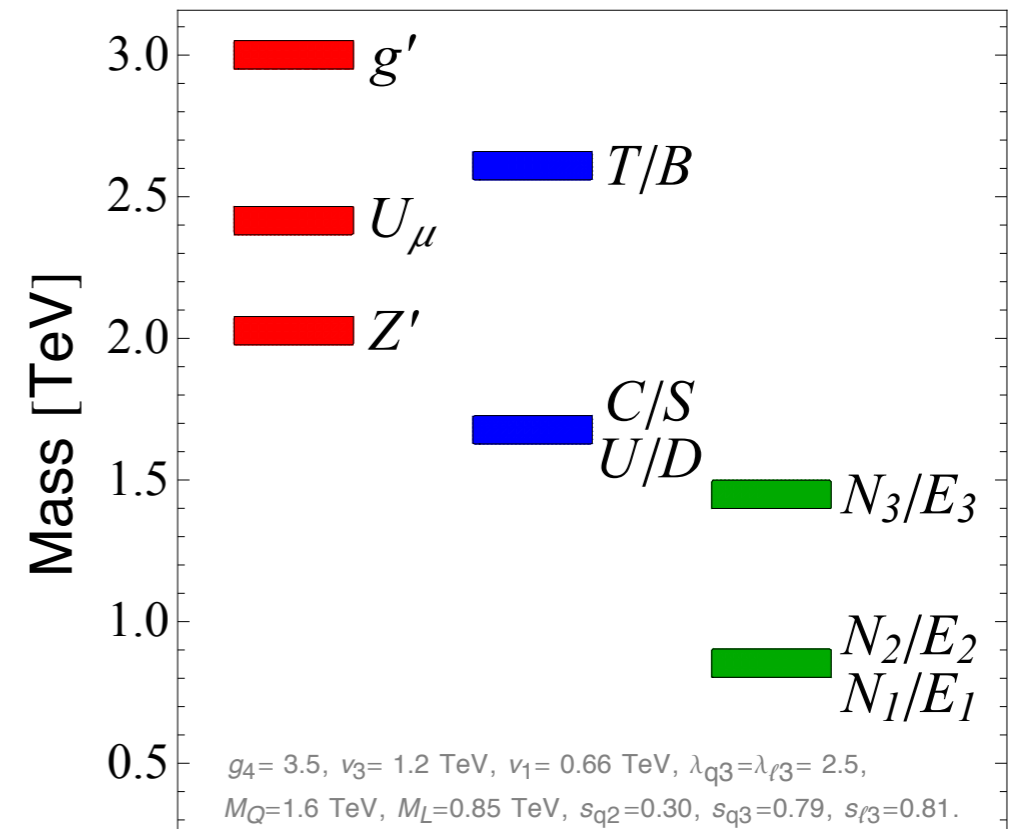
# High- $p_T$ highlights

- Coloron searches push the whole spectrum up
- Exotic multi-lepton & multi-jet signatures

[Dominant decays of new fermions are  $1 \rightarrow 3$ ]



Benchmark spectrum

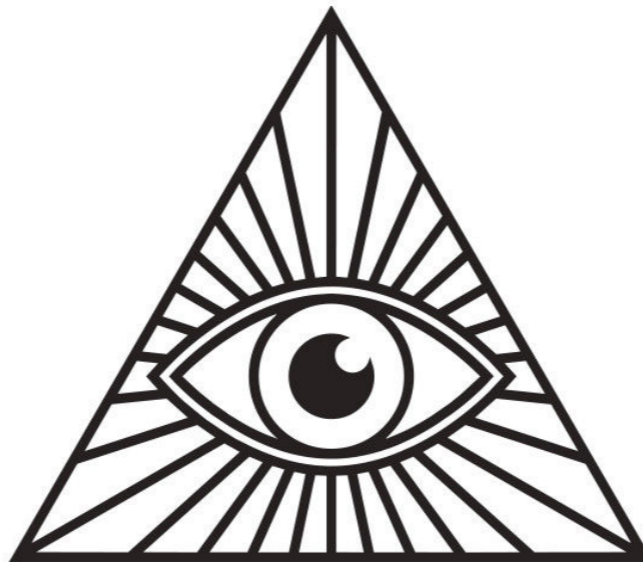
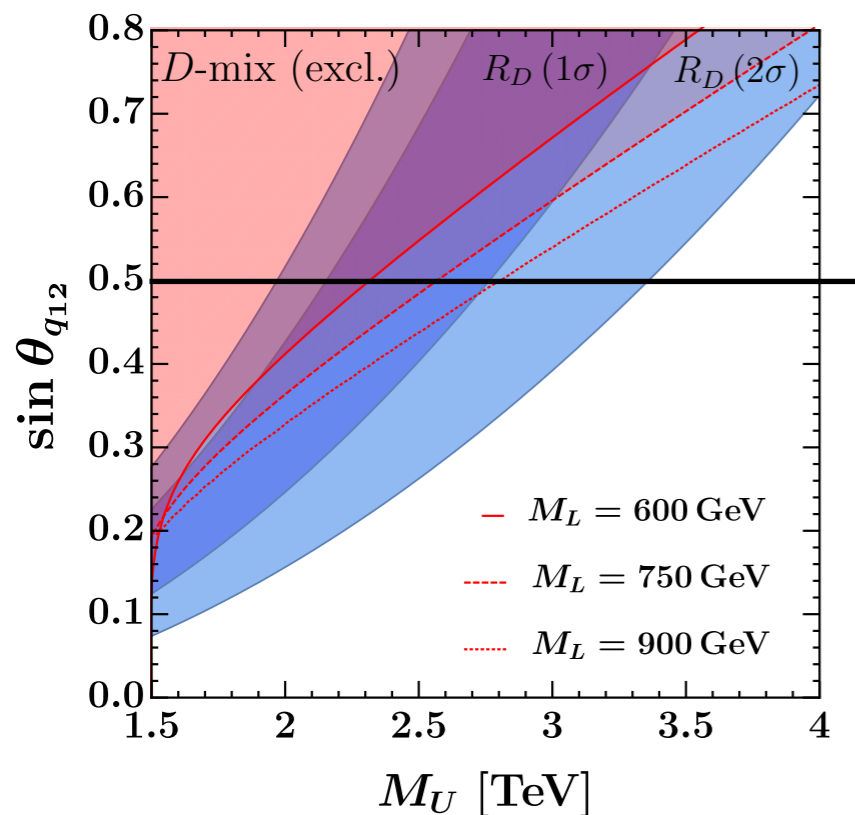


# B-anomalies paradox

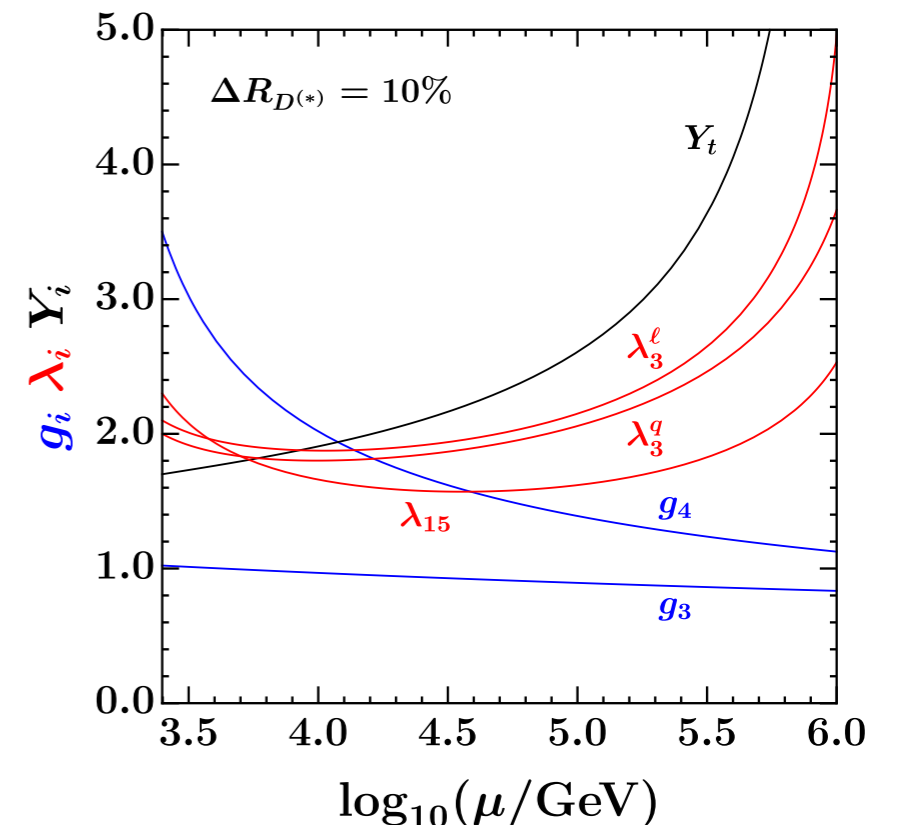
- NP expected to be seen yesterday ?

$$\Delta R_{D^{(*)}} \approx 0.2 \left( \frac{2 \text{ TeV}}{M_U} \right)^2 \left( \frac{g_4}{3.5} \right)^2 \sin(2\theta_{LQ}) \left( \frac{s_{l_3}}{0.8} \right)^2 \left( \frac{s_{q_3}}{0.8} \right) \left( \frac{s_{q_2}}{0.3} \right)$$

$\Delta F = 2$  + direct searches



Perturbativity



# Conclusions

1. Early speculations point to TeV-scale vector leptoquark ( $R(D)+R(K)$  explanation)

- who ordered that ?

- connection to EW naturalness and SM flavour ?

2. In the meanwhile, lesson from 432I [UV complete / calculable model]

 unexpected experimental signatures (coloron, vector-like leptons, ...)  
+ playground to compute correlations

3. Situation is tough, but not impossible [e.g. if deviation in  $R(D^{(*)})$  gets reduced]

# Backup slides

# Flavour structure

- Pick-up a basis exploiting  $U(3)^7$  symmetry of kinetic term

$$\mathcal{L}_{\text{SM-like}} = -\bar{q}'_L \hat{Y}_d d'_R H - \bar{q}'_L V^\dagger \hat{Y}_u u'_R \tilde{H} - \bar{\ell}'_L \hat{Y}_e e'_R H$$

$$\mathcal{L}_{\text{mix}} = -\bar{q}'_L \lambda_q \Psi_R \Omega_3 - \bar{\ell}'_L \lambda_\ell \Psi_R \Omega_1 - \bar{\Psi}_L \hat{M} \Psi_R$$

\*hat denotes a diagonal matrix

| Field      | $SU(4)$   | $SU(3)'$ | $SU(2)_L$ | $U(1)'$ |
|------------|-----------|----------|-----------|---------|
| $q_L^i$    | 1         | 3        | 2         | 1/6     |
| $u_R^i$    | 1         | 3        | 1         | 2/3     |
| $d_R^i$    | 1         | 3        | 1         | -1/3    |
| $\ell_L^i$ | 1         | 1        | 2         | -1/2    |
| $e_R^i$    | 1         | 1        | 1         | -1      |
| $\Psi_L^i$ | 4         | 1        | 2         | 0       |
| $\Psi_R^i$ | 4         | 1        | 2         | 0       |
| $H$        | 1         | 1        | 2         | 1/2     |
| $\Omega_3$ | $\bar{4}$ | 3        | 1         | 1/6     |
| $\Omega_1$ | $\bar{4}$ | 1        | 1         | -1/2    |

$$\Psi = \begin{pmatrix} Q' \\ L' \end{pmatrix}$$

# Flavour structure

- $\mathcal{L}_{\text{mix}} \rightarrow 0$

$$\mathcal{L}_{\text{SM-like}} = -\bar{q}'_L \hat{Y}_d d'_R H - \bar{q}'_L V^\dagger \hat{Y}_u u'_R \tilde{H} - \bar{\ell}'_L \hat{Y}_e e'_R H$$

- A well-known story:

- $Y_u \rightarrow 0$ :  $U(1)_d \times U(1)_s \times U(1)_b$
- $Y_d \rightarrow 0$ :  $U(1)_u \times U(1)_c \times U(1)_t$

# Flavour structure

- $\mathcal{L}_{\text{mix}} \rightarrow 0$

$$\mathcal{L}_{\text{SM-like}} = -\bar{q}'_L \hat{Y}_d d'_R H - \bar{q}'_L V^\dagger \hat{Y}_u u'_R \tilde{H} - \bar{\ell}'_L \hat{Y}_e e'_R H$$

- A well-known story:

$$\begin{array}{l} - Y_u \rightarrow 0: U(1)_d \times U(1)_s \times U(1)_b \\ - Y_d \rightarrow 0: U(1)_u \times U(1)_c \times U(1)_t \end{array} \left. \vphantom{\begin{array}{l} - Y_u \rightarrow 0: U(1)_d \times U(1)_s \times U(1)_b \\ - Y_d \rightarrow 0: U(1)_u \times U(1)_c \times U(1)_t \end{array}} \right] \xrightarrow{SU(2)_L} U(1)_{d+u} \times U(1)_{s+c} \times U(1)_{b+t} \xrightarrow{V} U(1)_B$$

- **Collective breaking** in the SM ensures:

1. No FCNC in either up or down sector [forbidden by the two  $U(1)^3$  in isolation]
2. FCCC from up/down misalignment [due to CKM  $\neq I$ ]

# Flavour structure

- Let us assume:

$$\mathcal{L}_{\text{mix}} = -\bar{q}'_L \lambda_q \Psi_R \Omega_3 - \bar{\ell}'_L \lambda_\ell \Psi_R \Omega_1 - \bar{\Psi}_L \hat{M} \Psi_R$$

$$\mathcal{L}_{\text{SM-like}} = -\bar{q}'_L \hat{Y}_d d'_R H - \bar{q}'_L V^\dagger \hat{Y}_u u'_R \tilde{H} - \bar{\ell}'_L \hat{Y}_e e'_R H$$

$$\lambda_q = \text{diag}(\lambda_{12}^q, \lambda_{12}^q, \lambda_3^q)$$

$$\lambda_\ell = \text{diag}(\lambda_1^\ell, \lambda_2^\ell, \lambda_3^\ell) W \quad W = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{LQ} & \sin \theta_{LQ} \\ 0 & -\sin \theta_{LQ} & \cos \theta_{LQ} \end{pmatrix} \quad \hat{M} \propto \mathbb{1}$$



# Flavour structure

- Let us assume:

$$\mathcal{L}_{\text{mix}} = -\bar{q}'_L \lambda_q \Psi_R \Omega_3 - \bar{\ell}'_L \lambda_\ell \Psi_R \Omega_1 - \bar{\Psi}_L \hat{M} \Psi_R$$

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- $\lambda_\ell \rightarrow 0$

$$\mathcal{G}_Q = U(2)_{q'+\Psi} \times U(1)_{q'_3+\Psi_3} \quad [\text{promoting approximate } U(2)_{q'} \text{ of SM to NP}]$$

- No tree-level FCNC in the down sector ( $\lambda_q$  and  $Y_d$  diagonal in the same basis)
- CKM-induced tree-level FCNC in the up sector (D-mixing) protected by  $U(2)_{q'}$

$$C_1^D \propto (V_{cb} V_{ub}^*)^2 \sim 10^{-8}$$

# Flavour structure

- Let us assume:

$$\mathcal{L}_{\text{mix}} = -\bar{q}'_L \lambda_q \Psi_R \Omega_3 - \bar{\ell}'_L \lambda_\ell \Psi_R \Omega_1 - \bar{\Psi}_L \hat{M} \Psi_R$$

$$\mathcal{L}_{\text{SM-like}} = -\bar{q}'_L \hat{Y}_d d'_R H - \bar{q}'_L V^\dagger \hat{Y}_u u'_R \tilde{H} - \bar{\ell}'_L \hat{Y}_e e'_R H$$

$$\lambda_q = \text{diag}(\lambda_{12}^q, \lambda_{12}^q, \lambda_3^q)$$

$$\lambda_\ell = \text{diag}(\lambda_1^\ell, \lambda_2^\ell, \lambda_3^\ell) W \quad W = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{LQ} & \sin \theta_{LQ} \\ 0 & -\sin \theta_{LQ} & \cos \theta_{LQ} \end{pmatrix} \quad \hat{M} \propto \mathbb{1}$$

- $\lambda_q \rightarrow 0$

$$\mathcal{G}_L = U(1)_{\ell'_1 + \tilde{\Psi}_1} \times U(1)_{\ell'_2 + \tilde{\Psi}_2} \times U(1)_{\ell'_3 + \tilde{\Psi}_3} \quad [\tilde{\Psi} = W \Psi]$$

1. No tree-level FCNC in the lepton sector ( $\lambda_\ell$  and  $Y_e$  diagonal in the same basis)

2.  $W$  is unphysical

# Flavour structure

- Let us assume:

$$\mathcal{L}_{\text{mix}} = -\bar{q}'_L \lambda_q \Psi_R \Omega_3 - \bar{\ell}'_L \lambda_\ell \Psi_R \Omega_1 - \bar{\Psi}_L \hat{M} \Psi_R$$

$$\mathcal{L}_{\text{SM-like}} = -\bar{q}'_L \hat{Y}_d d'_R H - \bar{q}'_L V^\dagger \hat{Y}_u u'_R \tilde{H} - \bar{\ell}'_L \hat{Y}_e e'_R H$$

$$\lambda_q = \text{diag}(\lambda_{12}^q, \lambda_{12}^q, \lambda_3^q)$$

$$\lambda_\ell = \text{diag}(\lambda_1^\ell, \lambda_2^\ell, \lambda_3^\ell) W \quad W = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{LQ} & \sin \theta_{LQ} \\ 0 & -\sin \theta_{LQ} & \cos \theta_{LQ} \end{pmatrix} \quad \hat{M} \propto \mathbb{1}$$

- Collective breaking** (Q and L locked by SU(4) gauge symmetry)

$$\mathcal{G}_Q \cap \mathcal{G}_L \xrightarrow{SU(4)+W} U(1)_{q'_1+\ell'_1+\Psi_1} \times U(1)_{q'+\ell'+\Psi}$$

1. no FV involving down and electrons

2. only LQ feels W matrix

$$\Psi_L = (Q'_L, L'_L)^T = (Q_L, W L_L)^T \quad \longrightarrow \quad i\bar{\Psi}_L \gamma^\mu D_\mu \Psi_L \supset \frac{g_4}{\sqrt{2}} U_\mu \bar{Q}_L \gamma^\mu W L_L$$

# A suggestive analogy\*

| 321  | 4321  |
|--|---|
| $\theta_C$   | $\theta_{LQ}$   |
| $V$  | $W$   |
| $W^\mu$  | $U^\mu$   |
| $q_L = \begin{pmatrix} u_L \\ V d_L \end{pmatrix}$ | $\Psi_L = \begin{pmatrix} Q_L \\ W L_L \end{pmatrix}$   |
| $Y_u, Y_d$   | $\lambda_q, \lambda_\ell$   |
| $SU(2)_L$  | $SU(4)$   |
| $U(1)_u \times U(1)_c \times U(1)_t$               | $U(2)_{q'+\Psi} \times U(1)_{q'_3+\Psi_3}$  |
| $U(1)_d \times U(1)_s \times U(1)_b$               | $U(1)_{\ell'_1+\tilde{\Psi}_1} \times U(1)_{\ell'_2+\tilde{\Psi}_2} \times U(1)_{\ell'_3+\tilde{\Psi}_3}$ |
| $U(1)_B$   | $U(1)_{q'_1+\ell'_1+\Psi_1} \times U(1)_{q'+\ell'+\Psi}$  |
| $u \rightarrow d$ tree level                       | $Q \rightarrow L$ tree level  |
| $u_i \rightarrow u_j$ loop level                   | $Q_i \rightarrow Q_j$ loop level  |
| $d_i \rightarrow d_j$ loop level                   | $L_i \rightarrow L_j$ loop level  |

\* symmetries in 321 accidental, in 4321 imposed (still, helpful for understanding pheno)

# Fermion mass basis

$$\mathcal{M}_u = \begin{pmatrix} V^\dagger \hat{Y}_u \frac{v}{\sqrt{2}} & \hat{\lambda}_q \frac{v_3}{\sqrt{2}} \\ 0 & \hat{M}_Q \end{pmatrix}, \quad \mathcal{M}_d = \begin{pmatrix} \hat{Y}_d \frac{v}{\sqrt{2}} & \hat{\lambda}_q \frac{v_3}{\sqrt{2}} \\ 0 & \hat{M}_Q \end{pmatrix},$$

$$\mathcal{M}_N = \begin{pmatrix} 0 & \hat{\lambda}_\ell \frac{v_1}{\sqrt{2}} \\ 0 & \hat{M}_L \end{pmatrix}, \quad \mathcal{M}_e = \begin{pmatrix} \hat{Y}_e \frac{v}{\sqrt{2}} & \hat{\lambda}_\ell W^\dagger \frac{v_1}{\sqrt{2}} \\ 0 & \hat{M}_L \end{pmatrix},$$

$$M_{L_i} = \sqrt{\frac{|\lambda_i^\ell|^2 v_1^2}{2} + \hat{M}_L^2}, \quad M_{Q_i} = \sqrt{\frac{|\lambda_i^q|^2 v_3^2}{2} + \hat{M}_Q^2},$$

$$m_{f_i} \approx |\hat{Y}_f^i| \cos \theta_{f_i} \frac{v}{\sqrt{2}} \quad (f = u, d, e).$$

$$\sin \theta_{q_i} = \frac{\lambda_i^q v_3}{\sqrt{|\lambda_i^q|^2 v_3^2 + 2 \hat{M}_Q^2}},$$

$$\sin \theta_{\ell_i} = \frac{\lambda_i^\ell v_1}{\sqrt{|\lambda_i^\ell|^2 v_1^2 + 2 \hat{M}_L^2}},$$


# LQ interactions

I. Large quark-lepton transitions in 3-2 sector

$$\mathcal{L}_U \supset \frac{g_4}{\sqrt{2}} \beta_{ij} \bar{q}_L^i \gamma^\mu \ell_L^j U_\mu$$

$$\beta = \text{diag}(s_{q_{12}}, s_{q_{12}}, s_{q_3}) W \text{diag}(0, s_{l_2}, s_{l_3}) = \begin{pmatrix} 0 & 0 & 0 \\ 0 & c_{\theta_{LQ}} s_{q_{12}} s_{l_2} & s_{\theta_{LQ}} s_{q_{12}} s_{l_3} \\ 0 & -s_{\theta_{LQ}} s_{q_3} s_{l_2} & c_{\theta_{LQ}} s_{q_3} s_{l_3} \end{pmatrix}$$

$$\Delta R_{D^{(*)}} = \frac{g_4^2 v^2}{2 M_U^2} \beta_{b\tau} \left( \beta_{b\tau} - \beta_{s\tau} \frac{V_{tb}^*}{V_{ts}^*} \right)$$

$\beta_{s\tau} > V_{ts} \sim 0.04$   allows to raise the LQ mass scale

we need:  $\theta_{LQ} \sim \pi/4$   $\theta_{l_3} \sim \pi/2$   $\theta_{q_3} \sim \pi/2$   $\theta_{q_{12}} \sim \mathcal{O}(1)$

# Z' / g' interactions

$$\mathcal{L}_{g'} \supset g_s \frac{g_4}{g_3} g_\mu^{Ia} \left[ \kappa_q^{ij} \bar{q}^i \gamma^\mu T^a q^j + \kappa_u^{ij} \bar{u}_R^i \gamma^\mu T^a u_R^j + \kappa_d^{ij} \bar{d}_R^i \gamma^\mu T^a d_R^j \right]$$

$$\mathcal{L}_{Z'} \supset \frac{g_Y}{2\sqrt{6}} \frac{g_4}{g_1} Z'_\mu \left[ \xi_q^{ij} \bar{q}^i \gamma^\mu q^j + \xi_u^{ij} \bar{u}_R^i \gamma^\mu u_R^j + \xi_d^{ij} \bar{d}_R^i \gamma^\mu d_R^j - 3 \xi_\ell^{ij} \bar{\ell}^i \gamma^\mu \ell^j - 3 \xi_e^{ij} \bar{e}_R^i \gamma^\mu e_R^j \right]$$

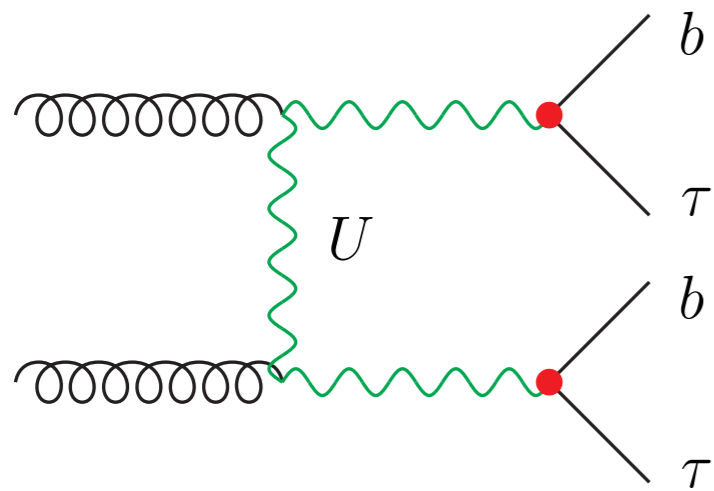
$$\kappa_q \approx \begin{pmatrix} s_{q1}^2 & 0 & 0 \\ 0 & s_{q2}^2 & 0 \\ 0 & 0 & s_{q3}^2 \end{pmatrix} - \frac{g_3^2}{g_4^2} \mathbb{1}, \quad \kappa_u \approx \kappa_d \approx -\frac{g_3^2}{g_4^2} \mathbb{1},$$

$$\xi_q \approx \begin{pmatrix} s_{q1}^2 & 0 & 0 \\ 0 & s_{q2}^2 & 0 \\ 0 & 0 & s_{q3}^2 \end{pmatrix} - \frac{2g_1^2}{3g_4^2} \mathbb{1}, \quad \xi_u \approx \xi_d \approx -\frac{2g_1^2}{3g_4^2} \mathbb{1},$$

$$\xi_\ell \approx \begin{pmatrix} s_{\ell1}^2 & 0 & 0 \\ 0 & s_{\ell2}^2 & 0 \\ 0 & 0 & s_{\ell3}^2 \end{pmatrix} - \frac{2g_1^2}{3g_4^2} \mathbb{1}, \quad \xi_e \approx -\frac{2g_1^2}{3g_4^2} \mathbb{1}.$$

# High- $p_T$ searches

- LQ pair production via QCD
  - 3rd generation final states (fixed by anomaly and  $SU(2)_L$  invariance)



$$\begin{cases} U \rightarrow b\tau^+, & \text{BR} = 50 \% \\ U \rightarrow t\bar{\nu}, & \text{BR} = 50 \% \end{cases}$$

[CMS search for spin-0, 1703.03995  
recast for spin-1 1706.01868 (see also 1706.05033) + Moriond EW update]

$$m_U \gtrsim 1.5 \text{ TeV}$$



LQ mass sets the overall scale:  $M_{g'} \simeq \sqrt{2} M_U$   $M_{Z'} \simeq \frac{1}{\sqrt{2}} M_U$



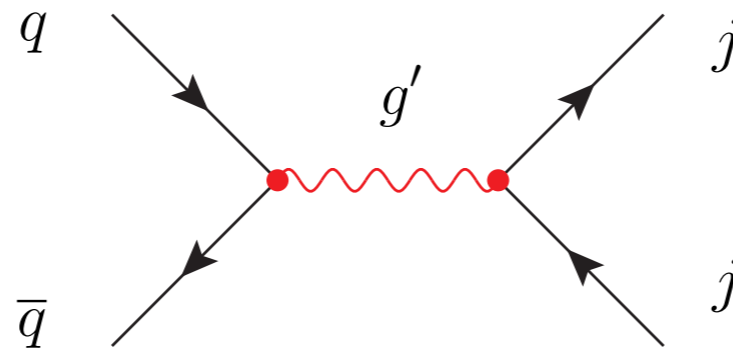
# High- $p_T$ searches

- LQ pair production via QCD
- $Z'$  Drell-Yan production naturally suppressed

$$\sin \theta_{Z'} = \sqrt{\frac{3}{2}} \frac{g_Y}{g_4} \simeq 0.09 \quad \longrightarrow \quad \text{requires } g_4 \gtrsim 3$$

- $g'$  resonant di-jet searches [ATLAS, 1703.09127]

$$\sin \theta_{g'} = \frac{g_s}{g_4} \simeq 0.3 \quad \longrightarrow \quad 2 \text{ TeV coloron naively excluded}$$



# Coloron

