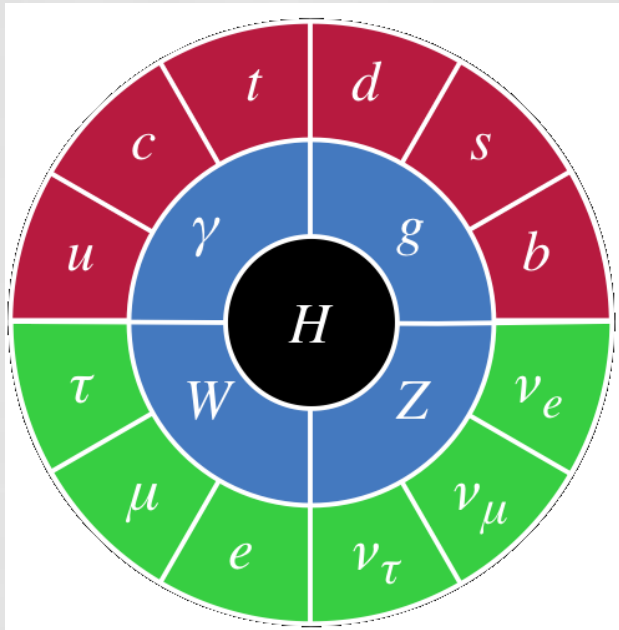


Muon $g-2$ in the 2HDM: maximum results and detailed phenomenology.

Adriano Cherchiglia, D. Stöckinger, H. Stöckinger-Kim

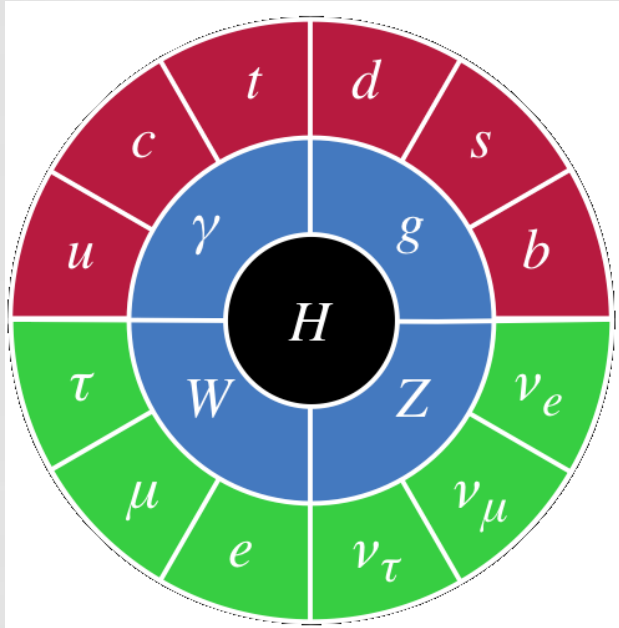


Standard Model

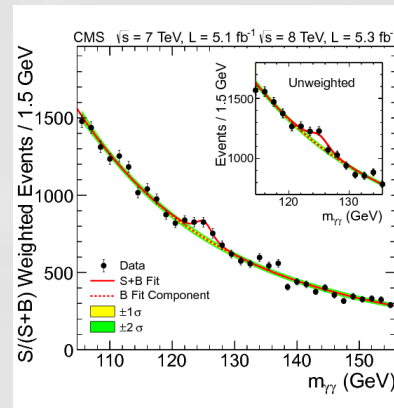


Particle Fever

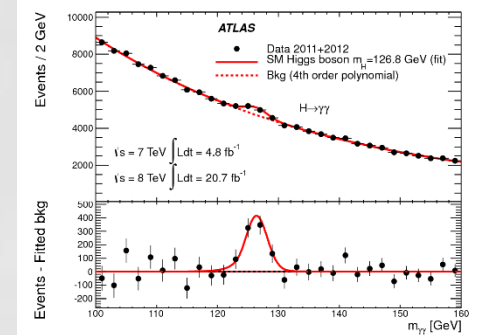
Standard Model



Particle Fever



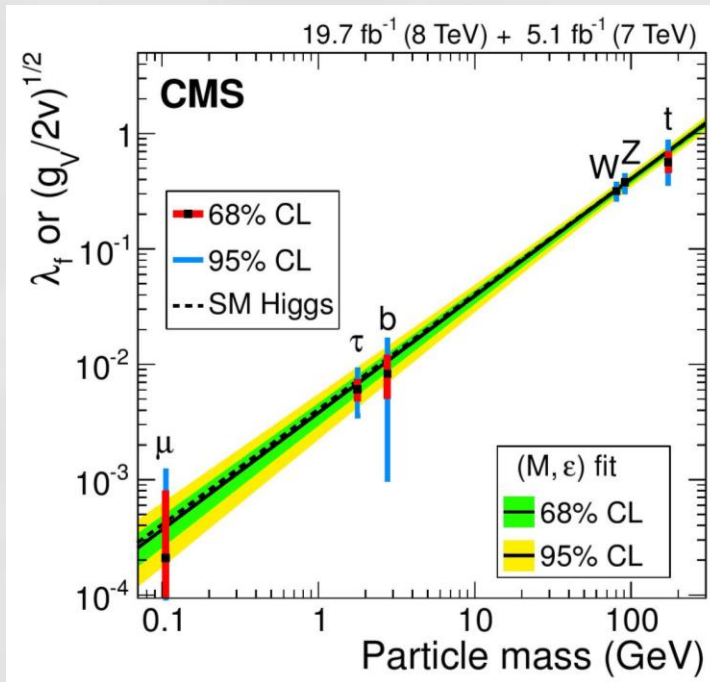
Phys.Lett. B716 (2012) 30-61



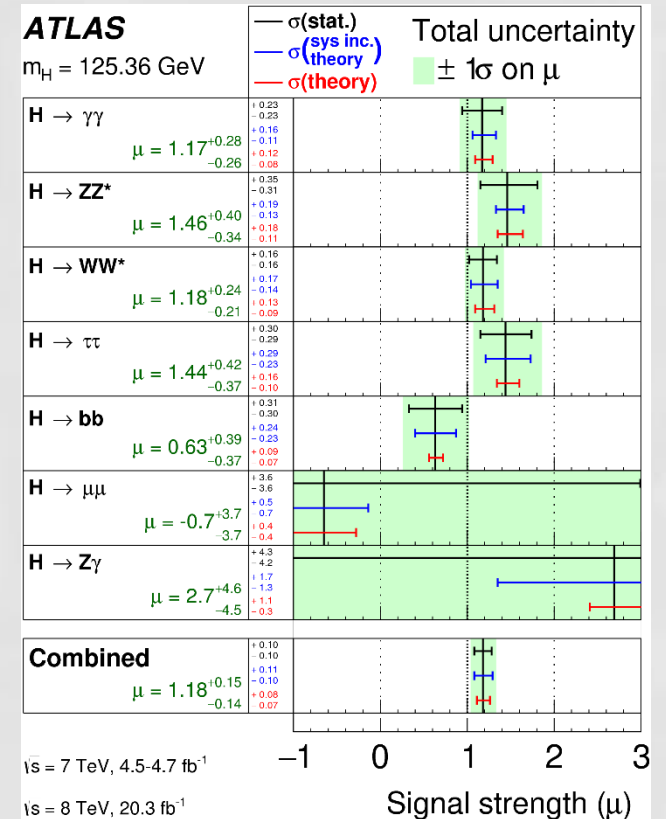
Phys.Lett. B716 (2012) 1-29

Standard Model

- Scalar sector scrutinized



Eur. Phys. J. C 75 (2015) 212



Eur. Phys. J. C76 (2016) 6

In the search for New Physics

- High Energy Physics (colliders)
 - Still no sign of New Physics.



- Low-energy observables
 - Muon magnetic moment.



<https://cds.cern.ch/record/1295244>



<http://muon-g-2.fnal.gov/>

$$(g - 2)_\mu$$

$$H_B = -\vec{\mu} \cdot \vec{B}$$

$$\vec{\mu}_s = g \left(\frac{q}{2m} \right) \vec{s}$$



<http://muon-g-2.fnal.gov/>

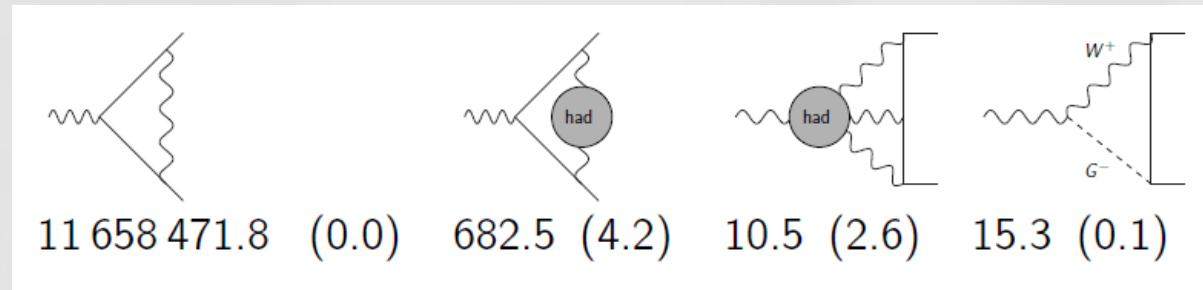
- Dirac: $g = 2$
- Quantum Field Theory: $g = 2 + \dots$



$$a_\mu = \frac{(g - 2)}{2}$$

$(g - 2)_\mu$ - Theory

- Standard Model



Thanks to D. Stöckinger

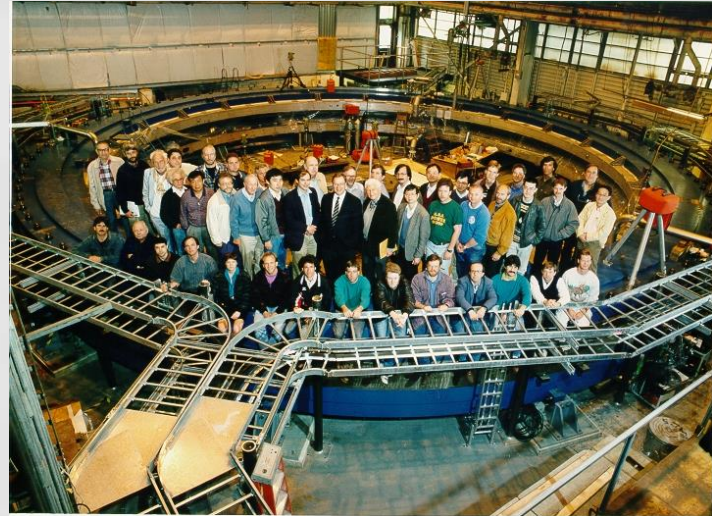
$$a_\mu^{th} = \begin{cases} (11\,659\,182.3 \pm 4.3) \times 10^{-10} \\ (11\,659\,182.04 \pm 3.56) \times 10^{-10} \end{cases}$$

Davier et al (17)

Keshavarzi et al (18)

$(g - 2)_\mu$ - Experiment

- E821 BNL
- Final result in 2004



<http://www.g-2.bnl.gov/>

$$a_\mu^{exp} = (11\,659\,208.9 \pm 6.3) \times 10^{-10}$$

Phys. Rev. Lett. 92, 161802 (2004)

$(g - 2)_\mu$ - Experiment



<http://muon-g-2.fnal.gov/>

$$a_\mu^{exp} = \text{????}$$



<http://muon-g-2.fnal.gov/>

$(g - 2)_\mu$ - Experiment



<http://muon-g-2.fnal.gov/>

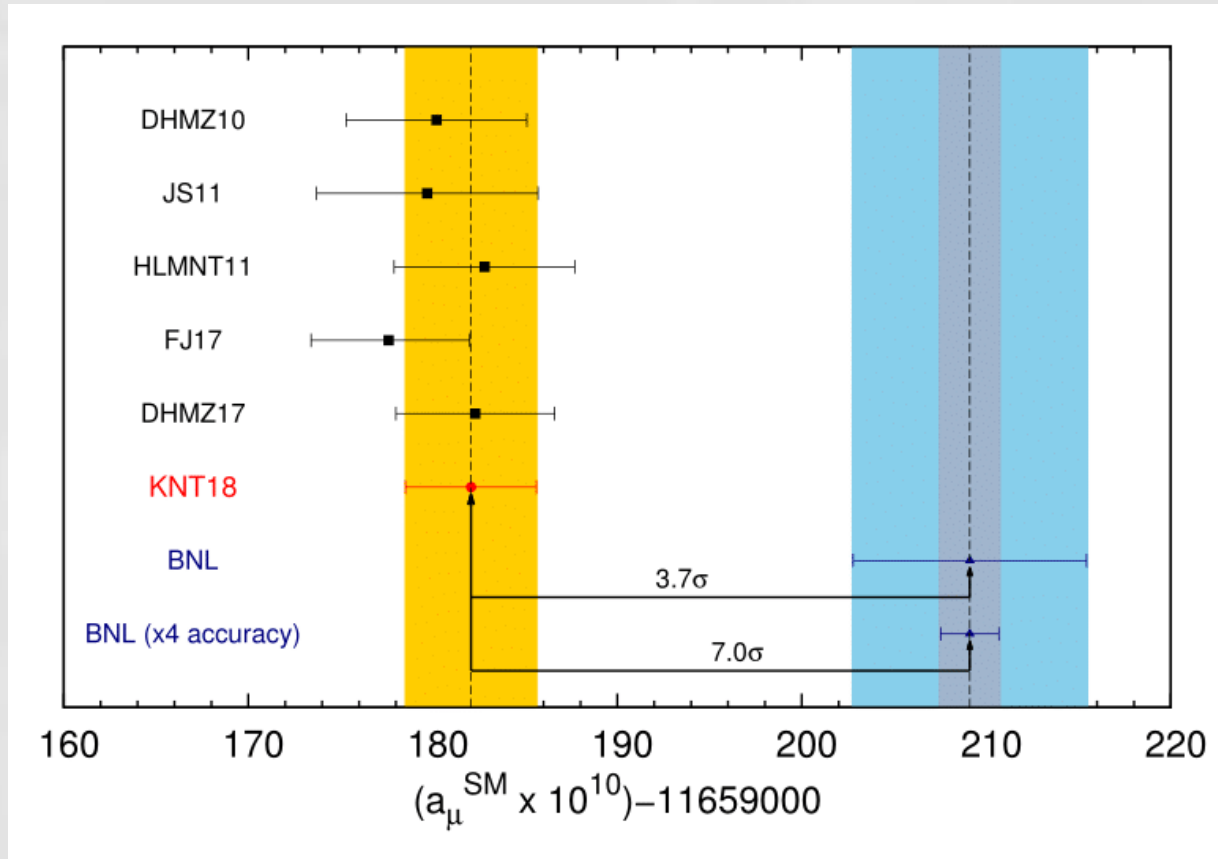
$$a_\mu^{exp} = \text{????}$$

First results by 2019!



<http://muon-g-2.fnal.gov/>

Theory Experiment

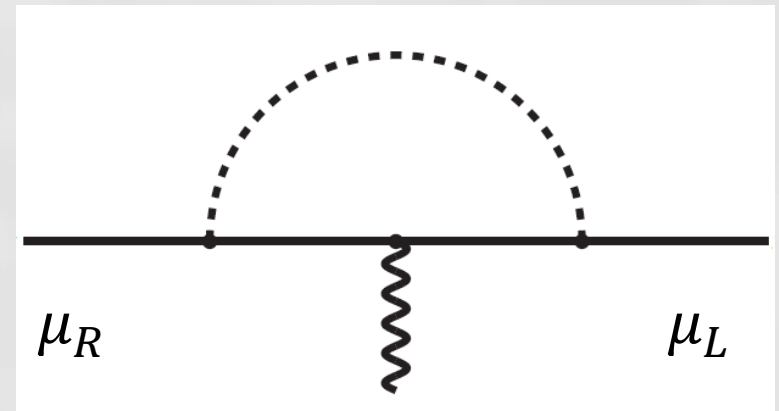


Keshavarzi et al (18)

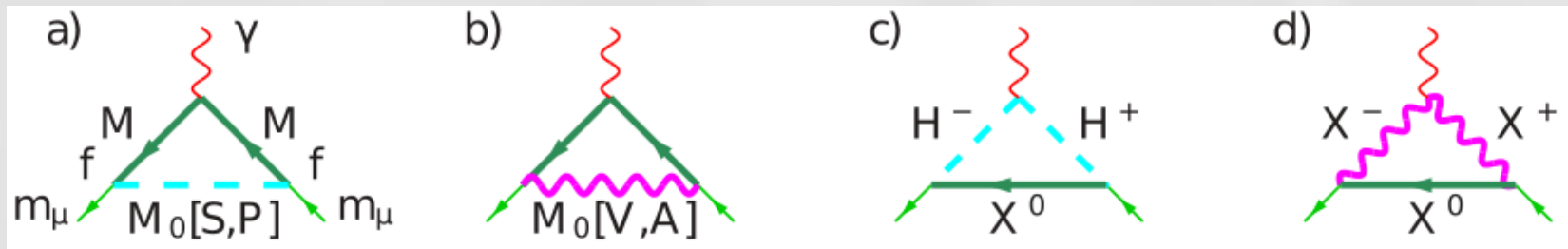
$(g - 2)_\mu$ - Beyond Standard Model

$$\mathcal{L}_5 \propto \frac{a_\mu}{m_\mu} \overline{\mu}_L \sigma^{\alpha\beta} F_{\alpha\beta} \mu_R$$

- Chirality flipping
- Loop induced

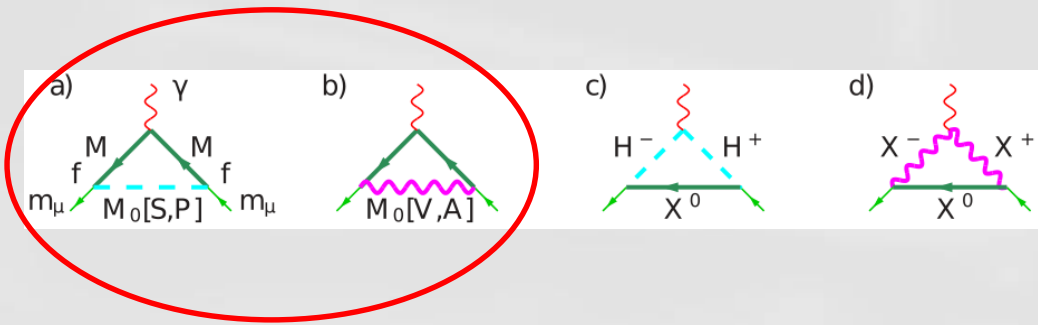


$(g - 2)_\mu$ - Beyond Standard Model



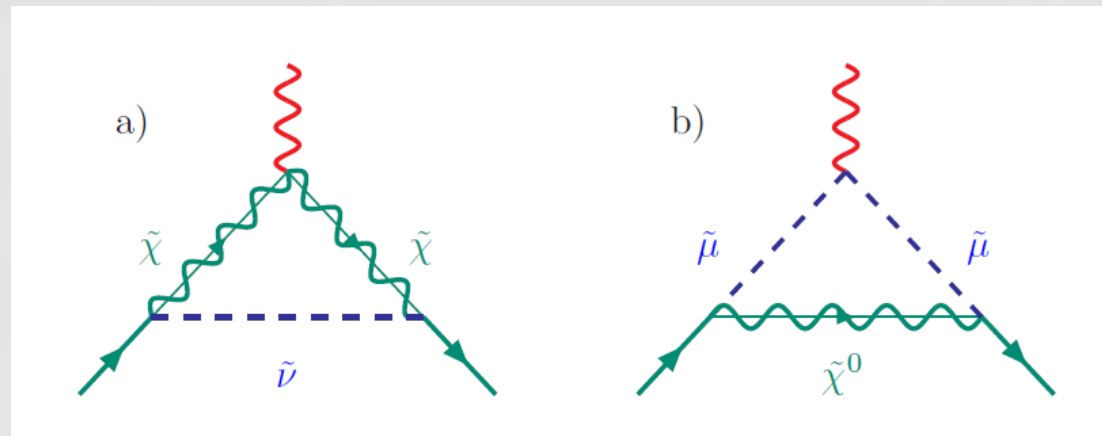
Jegerlehner, Nyffeler (09)

$(g - 2)_\mu$ - Beyond Standard Model

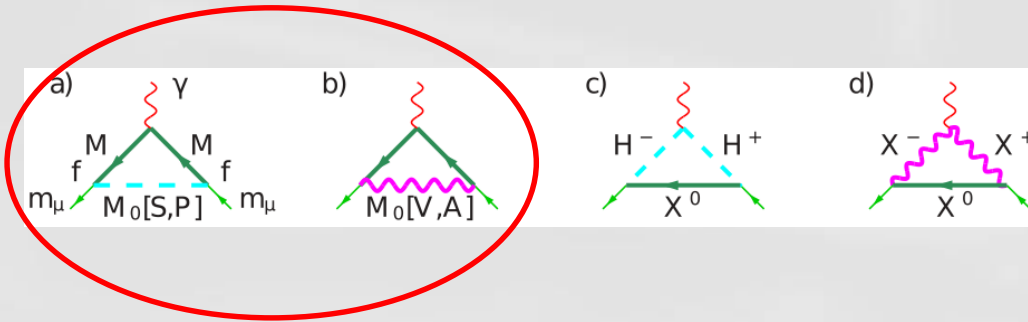


Jegerlehner, Nyffeler (09)

SUSY



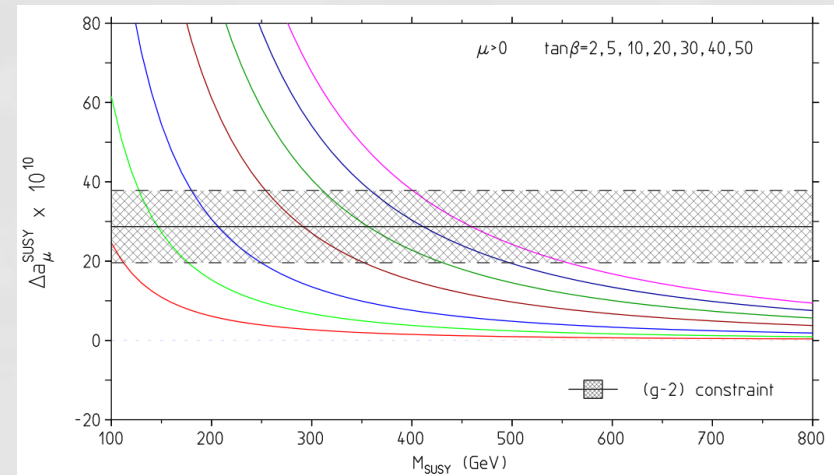
$(g - 2)_\mu$ - Beyond Standard Model



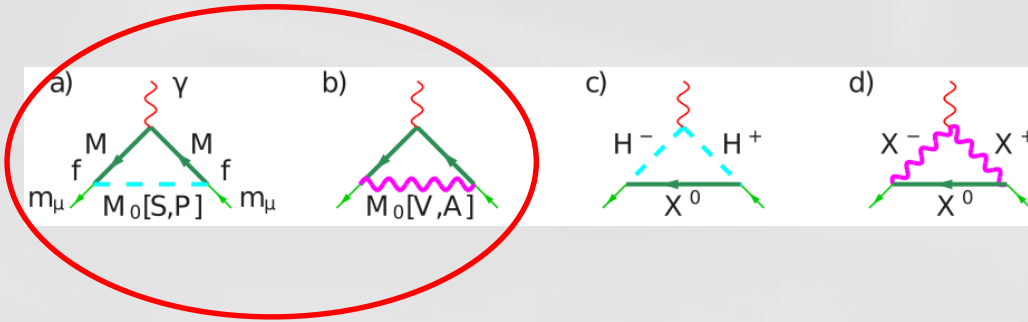
Jegerlehner, Nyffeler (09)

SUSY

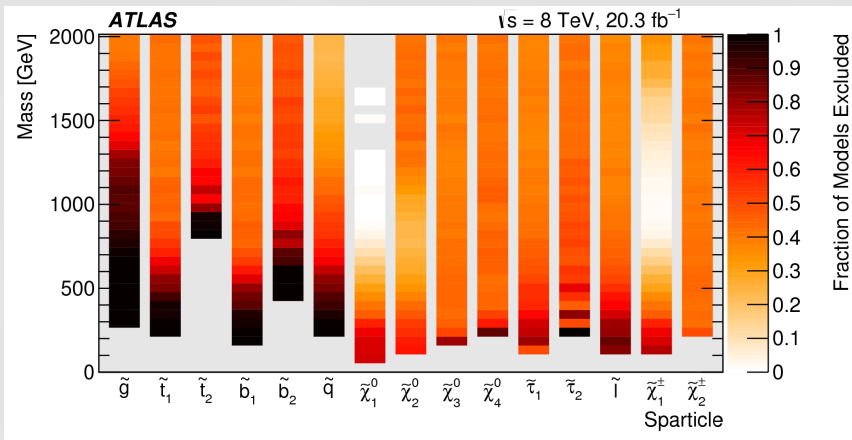
$$a_\mu(SUSY) \cong 123 \times 10^{-11} \left(\frac{100 \text{ GeV}}{M_{SUSY}} \right)^2 \tan \beta$$



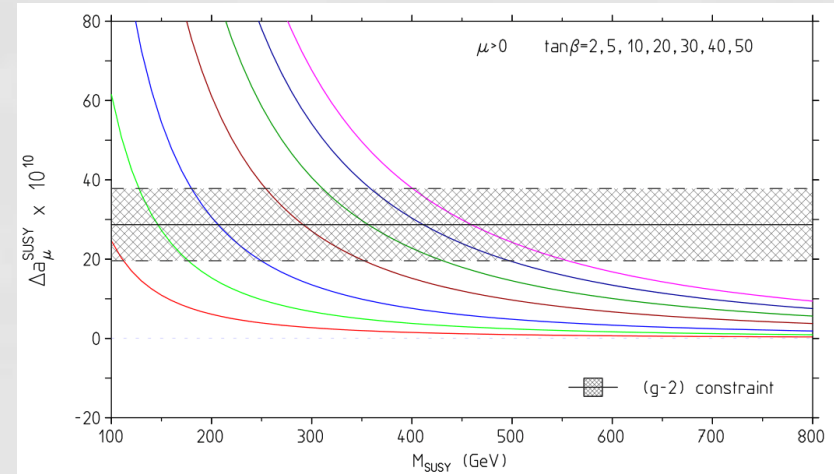
$(g - 2)_\mu$ - Beyond Standard Model



Jegerlehner, Nyffeler (09)



<https://atlas.web.cern.ch>



$(g - 2)_\mu$ - Beyond Standard Model

- Beyond Standard Model:

- SUSY



Other scenarios



Ex: extensions to the scalar sector

$$\mathcal{L}_S = (D_\mu \phi_1)^\dagger (D^\mu \phi_1) + (D_\mu \phi_2)^\dagger (D^\mu \phi_2) - V(\phi_1, \phi_2)$$

2HDM



Invariant under CP



Flavor Aligned 2HDM

$$\mathcal{L}_Y = -\bar{Q}'_L(\Gamma_1\phi_1 + \Gamma_2\phi_2)d'_R - \bar{Q}'_L(\Delta_1\tilde{\phi}_1 + \Delta_2\tilde{\phi}_2)u'_R \\ - \bar{L}'_L(\Pi_1\phi_1 + \Pi_2\phi_2)l'_R + \text{h.c.},$$

Pich, Túzón, 2009

$$\Gamma_2 = \xi_d e^{-i\theta} \Gamma_1, \quad \Delta_2 = \xi_u^* e^{i\theta} \Delta_1, \quad \Pi_2 = \xi_l e^{-i\theta} \Pi_1.$$

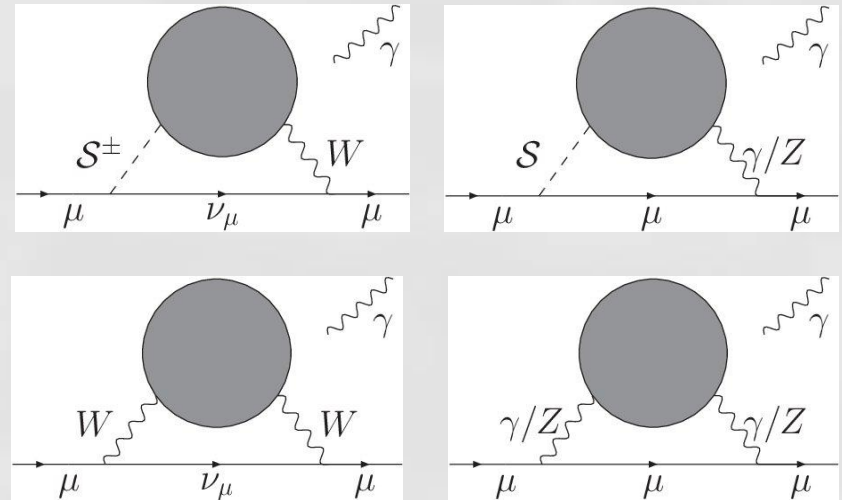
Model	S_d	S_u	S_l
Type I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type II	$-\tan \beta$	$\cot \beta$	$-\tan \beta$
Type X	$\cot \beta$	$\cot \beta$	$-\tan \beta$
Type Y	$-\tan \beta$	$\cot \beta$	$\cot \beta$
Inert	0	0	0

$$\zeta_f \equiv \frac{\xi_f - \tan \beta}{1 + \xi_f \tan \beta}.$$

$(g - 2)_\mu$ - Flavor Aligned 2HDM

AC, Kneschke, Stöckinger, Stöckinger-Kim (17)

Complete two-loop prediction

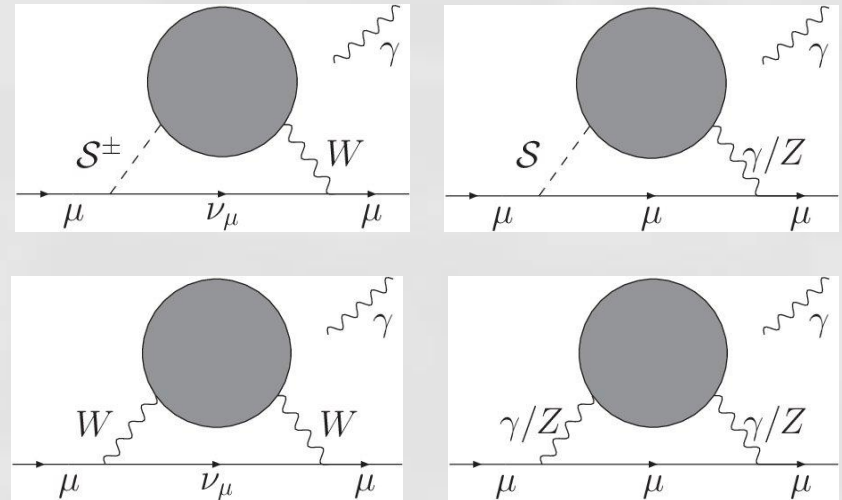


Theoretical uncertainty under control (below new $(g - 2)_\mu$ experiment)

$(g - 2)_\mu$ - Flavor Aligned 2HDM

AC, Kneschke, Stöckinger, Stöckinger-Kim (17)

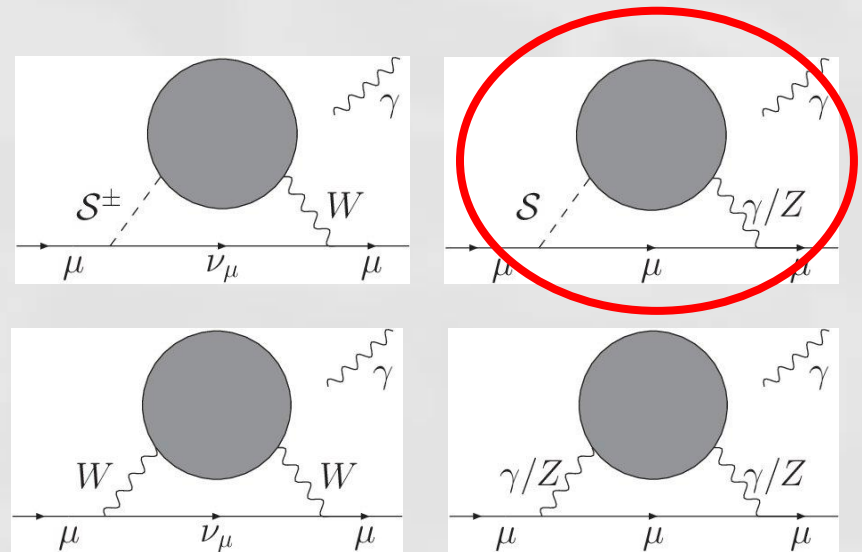
Given phenomenological constraints,
what are the maximum values for a_μ ?



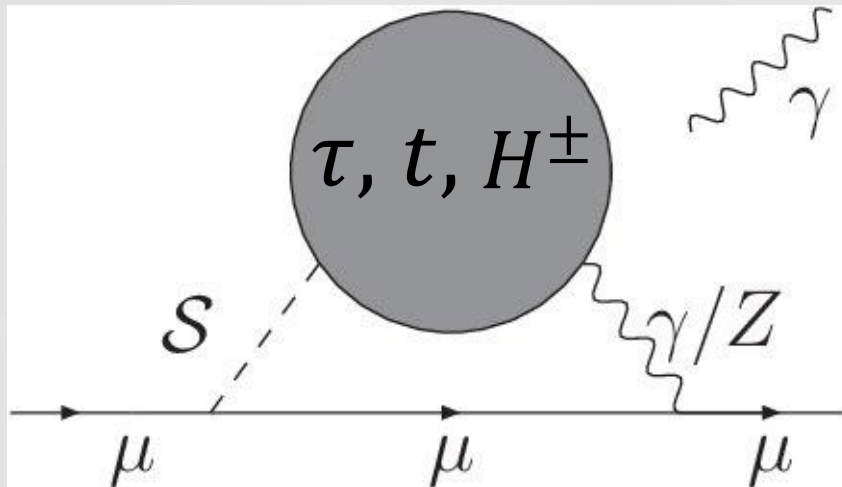
$(g - 2)_\mu$ - Flavor Aligned 2HDM

AC, Kneschke, Stöckinger, Stöckinger-Kim (17)

Given phenomenological constraints,
what are the maximum values for a_μ ?



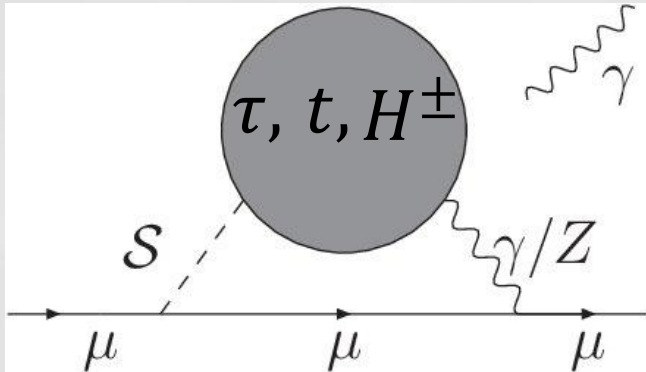
Maximum allowed $(g - 2)_\mu$



Constraints

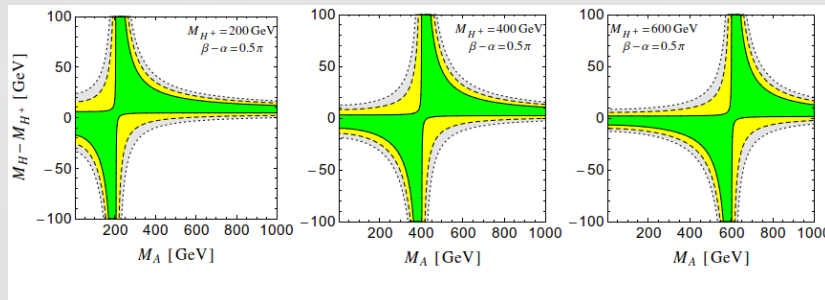
- B-physics;
- Tau decay;
- $Z \rightarrow \tau\tau$;
- Collider;
- Theoretical;
- EW parameters.

Maximum allowed $(g - 2)_\mu$



Constraints

- B-physics;
- Tau decay;
- $Z \rightarrow \tau\tau$;
- Collider;
- Theoretical;
- EW parameters.

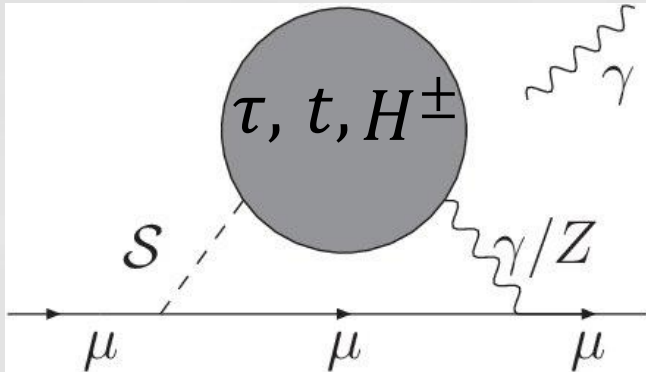


Broggio et al (14)



Control splitting between scalar masses.

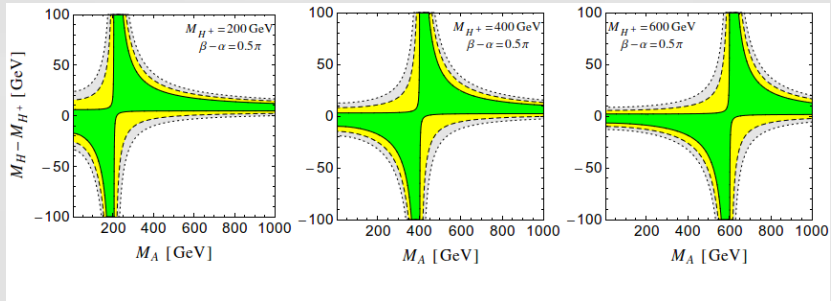
Maximum allowed $(g - 2)_\mu$



$$M_A \text{ free}$$

$$M_H \approx M_{H^\pm}$$

- Constraints**
- B-physics;
 - Tau decay;
 - $Z \rightarrow \tau\tau$;
 - Collider;
 - Theoretical;
 - **EW parameters.**

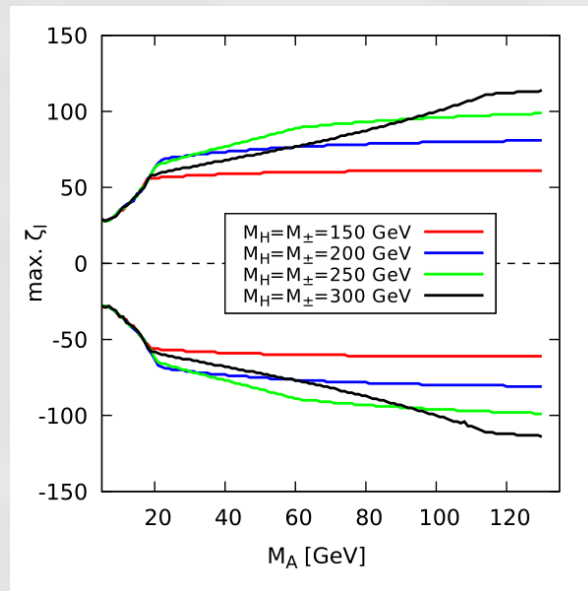
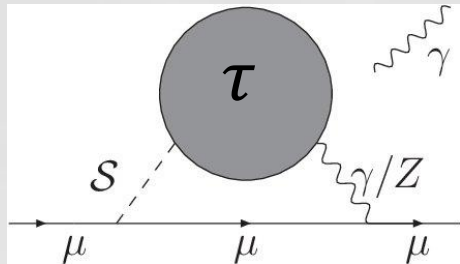


Broggio et al (14)



Control splitting between scalar masses.

Maximum allowed $(g - 2)_\mu$



Constraints

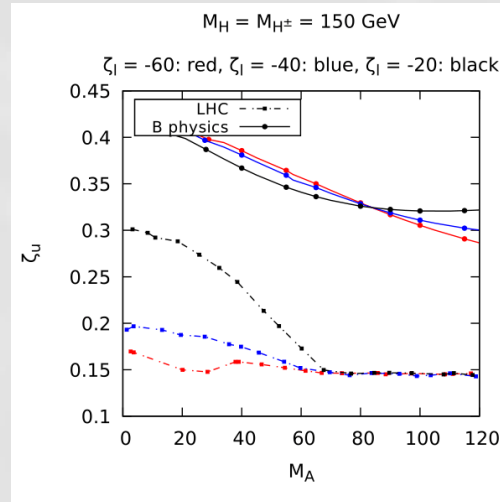
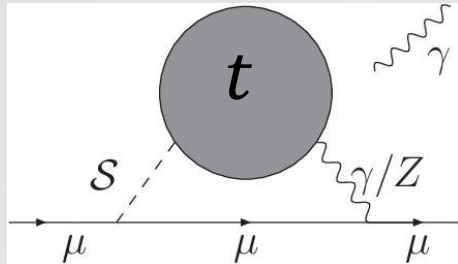
- B-physics;
- **Tau decay;**
- **$Z \rightarrow \tau\tau$;**
- **Collider;**
- Theoretical;
- EW parameters.

S: h, H, A, H^\pm

Flavour-aligned: $\zeta_l, \zeta_u, \zeta_d$

Only contribution in a lepton-specific scenario

Maximum allowed $(g - 2)_\mu$

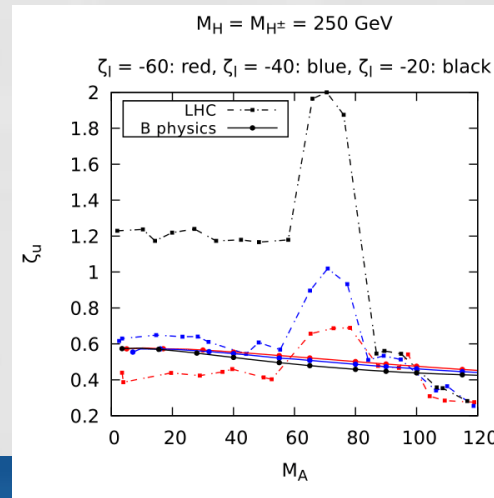


Constraints

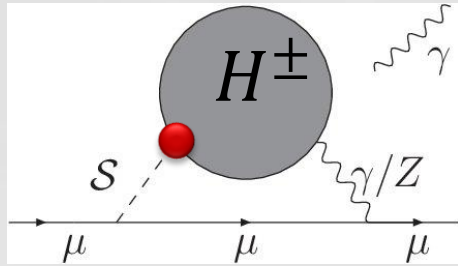
- B-physics;
- Tau decay;
- $Z \rightarrow \tau\tau$;
- Collider;
- Theoretical;
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Flavour-aligned: $\zeta_l, \zeta_u, \zeta_d$



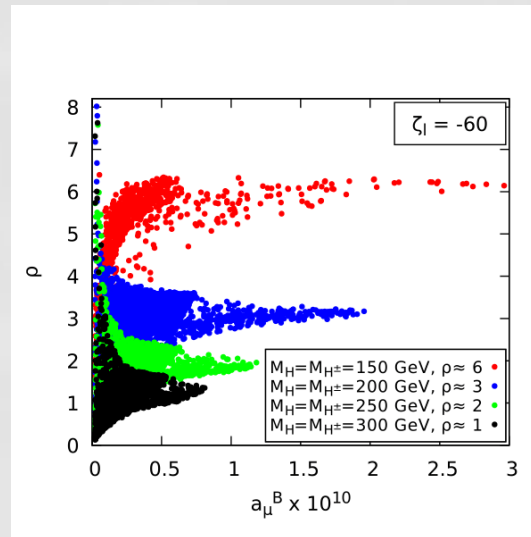
Maximum allowed $(g - 2)_\mu$



$$|a_\mu^B| \approx \rho \left| \frac{C_{HH^+H^-}}{\text{GeV}} \right| |\zeta_l| \times 10^{-15}$$

Constraints

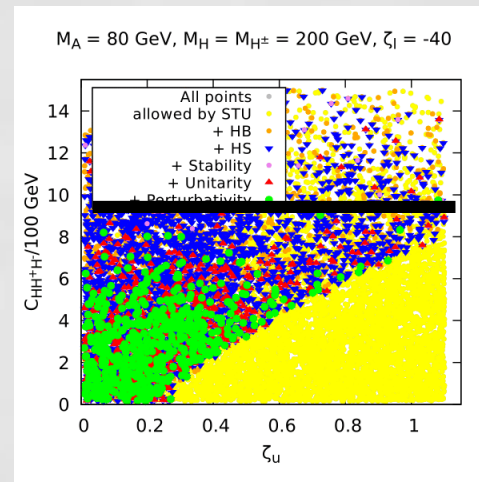
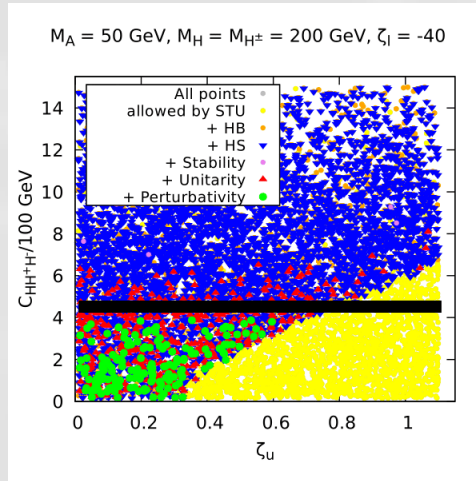
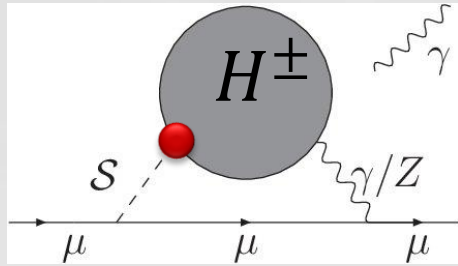
- B-physics;
- Tau decay;
- $Z \rightarrow \tau\tau$;
- Collider;
- Theoretical;
- EW parameters.



S : h, H, A, H^\pm

Flavour-aligned: $\zeta_l, \zeta_u, \zeta_d$

Maximum allowed $(g - 2)_\mu$



Constraints

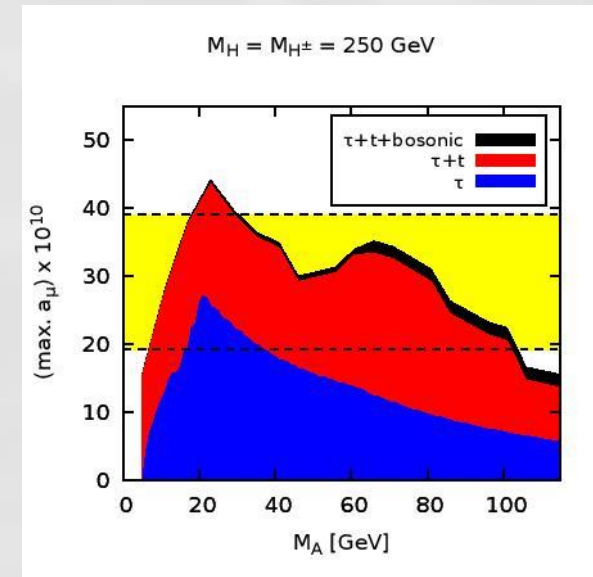
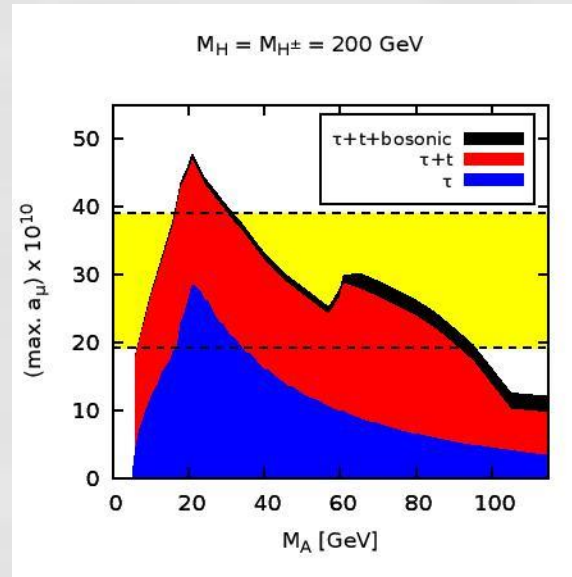
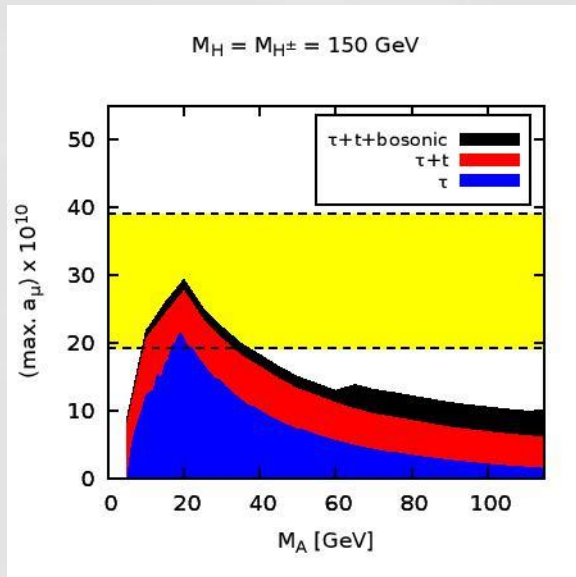
- B-physics;
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$$|a_\mu^B| \approx \rho \left| \frac{C_{HH^+H^-}}{\text{GeV}} \right| |\zeta_l| \times 10^{-15}$$

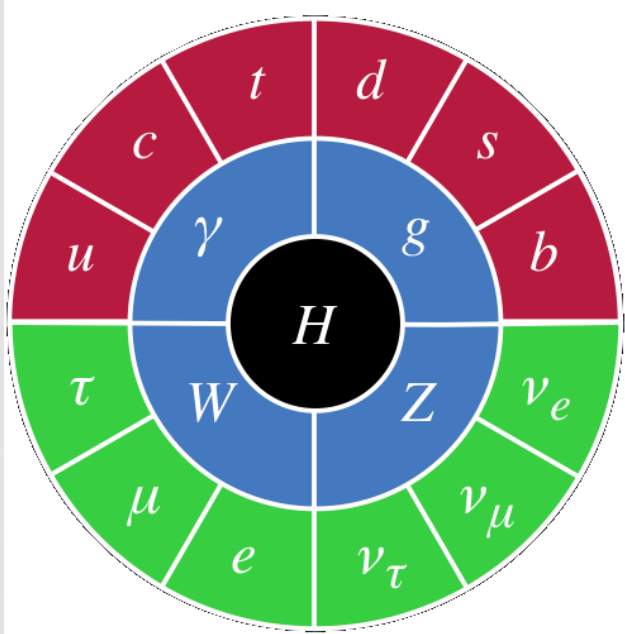
S : h, H, A, H^\pm

Flavour-aligned: $\zeta_l, \zeta_u, \zeta_d$

Maximum allowed $(g - 2)_\mu$



Conclusions



THEORY

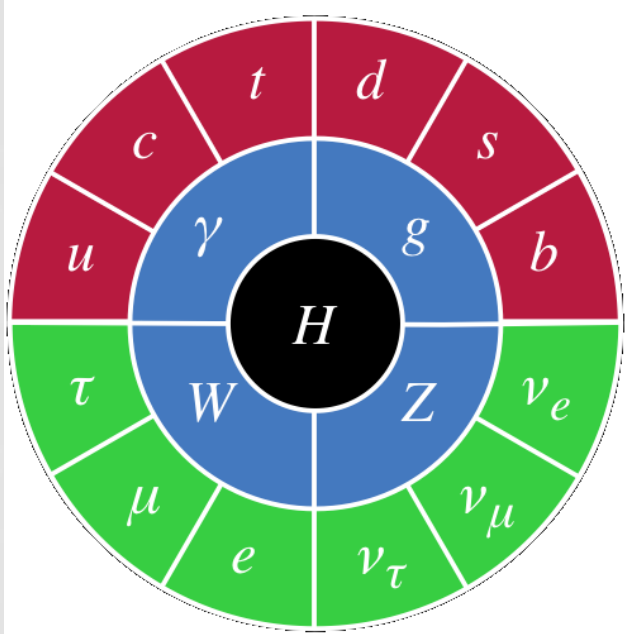


<https://cds.cern.ch/record/1295244>

Small deviations

EXPERIMENT

Conclusions



THEORY

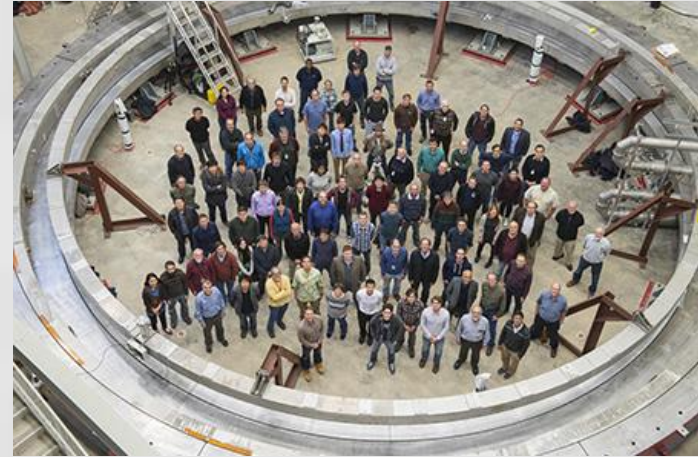
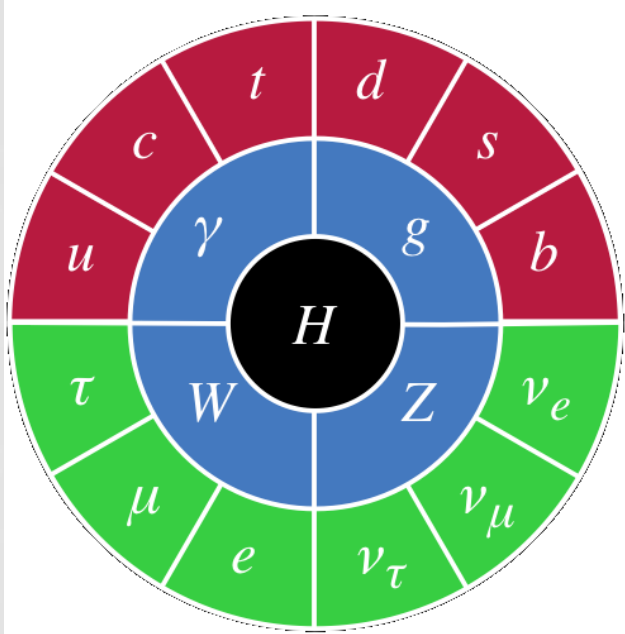


<http://muon-g-2.fnal.gov/>

3.7σ deviation

EXPERIMENT

Conclusions



<http://muon-g-2.fnal.gov/>



3.7σ deviation

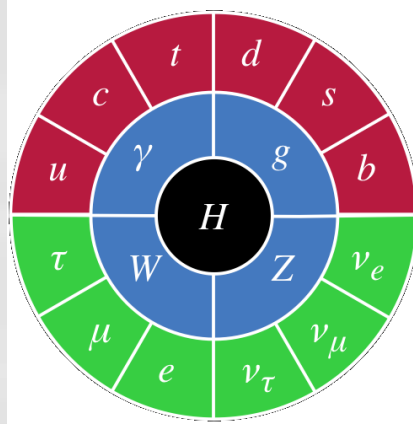
EXPERIMENT

THEORY



Conclusions

2HDM =

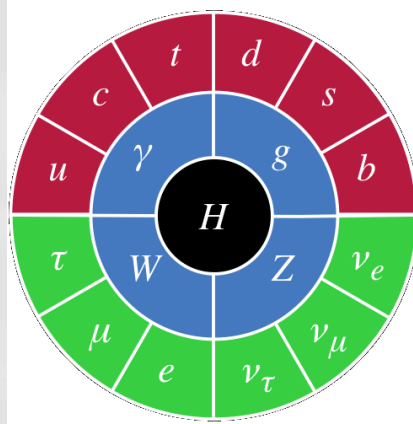


+ 4 scalars

$(g - 2)_\mu$
Phenomenology

Conclusions

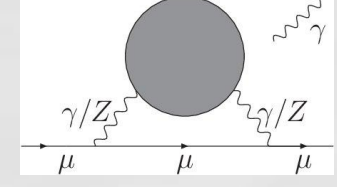
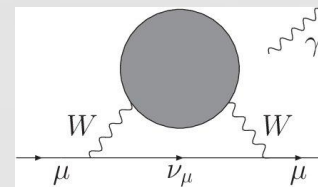
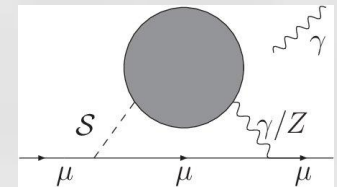
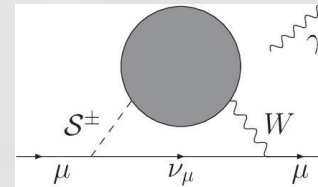
2HDM =



+ 4 scalars

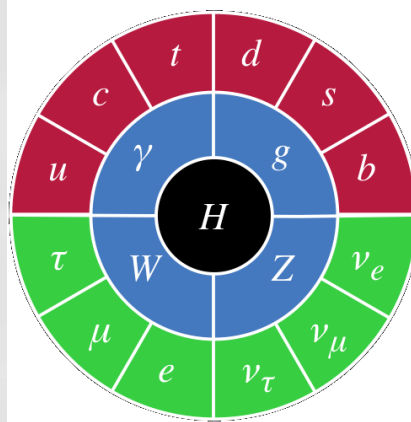
$(g - 2)_\mu$
Phenomenology

AC, Kneschke, Stöckinger, Stöckinger-Kim (17)



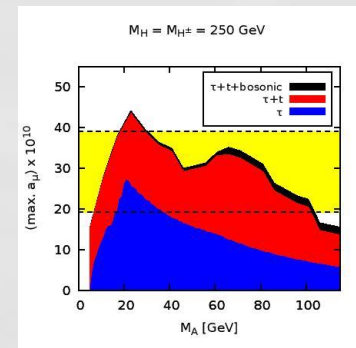
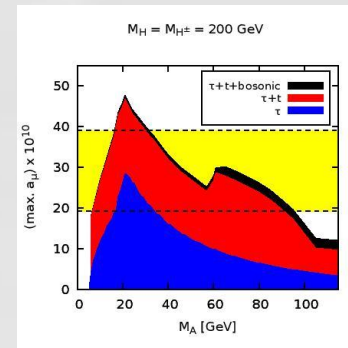
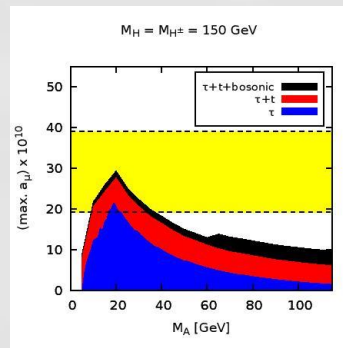
Conclusions

2HDM =



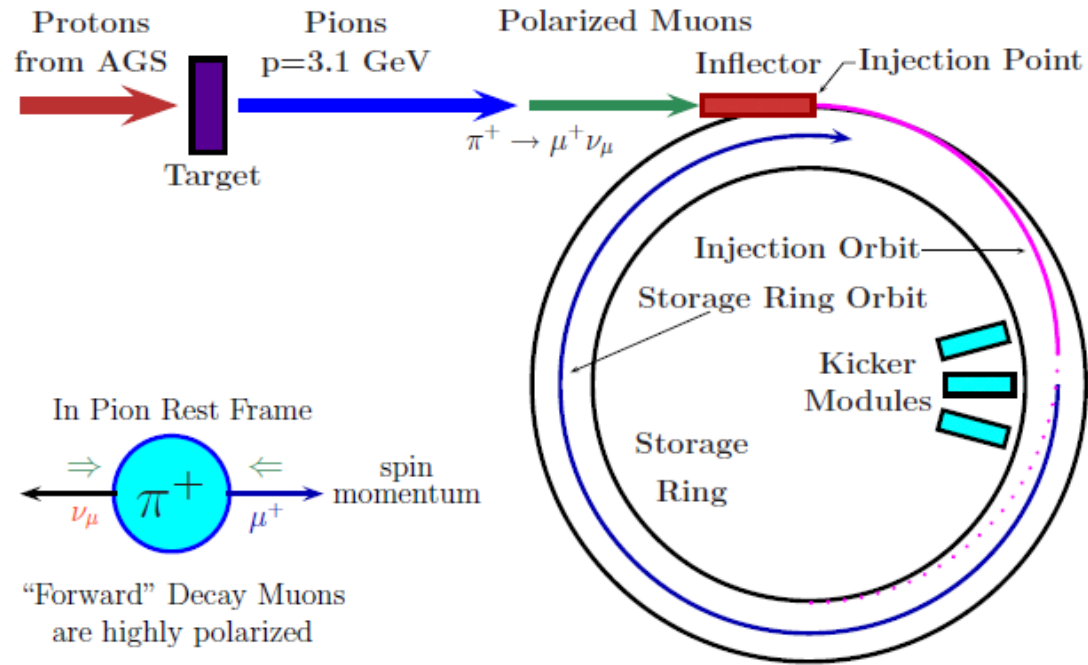
+ 4 scalars

$(g - 2)_\mu$
Phenomenology

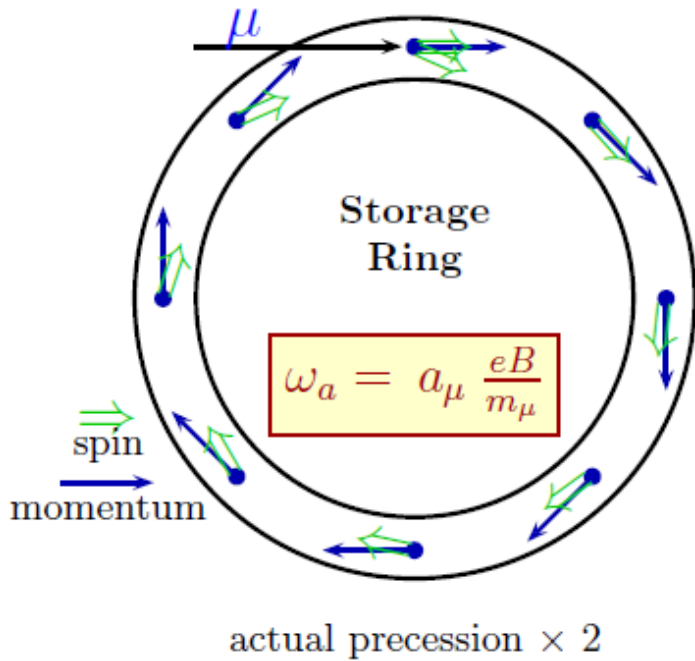


Thanks!

Backup



Jegerlehner, Nyffeler
(09)



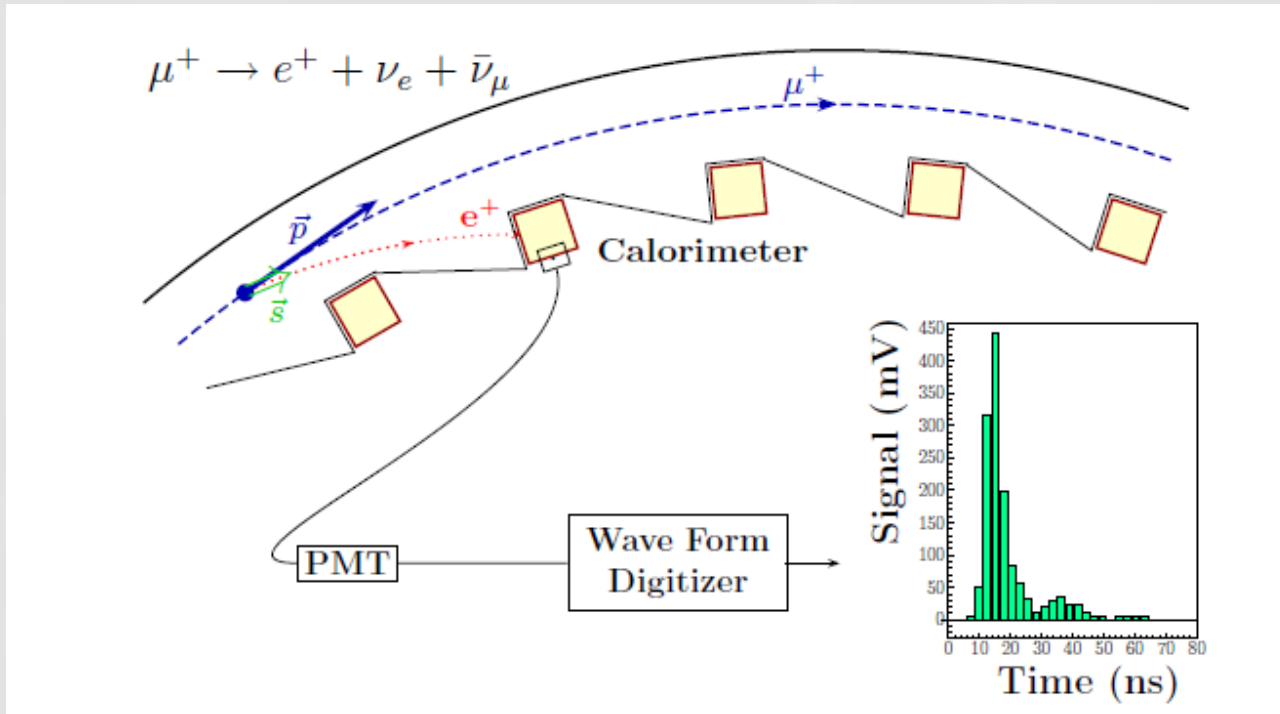
$$\omega_a = \omega_s - \omega_c.$$

$$\omega_c = \frac{eB}{m_\mu \gamma}, \quad \omega_s = \frac{eB}{m_\mu \gamma} + a_\mu \frac{eB}{m_\mu}, \quad \omega_a = a_\mu \frac{eB}{m_\mu},$$

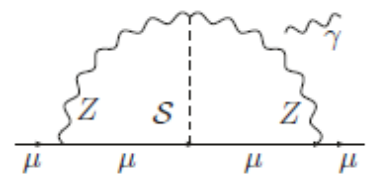
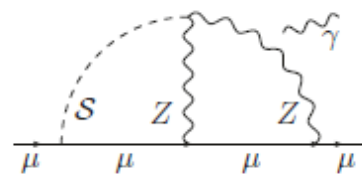
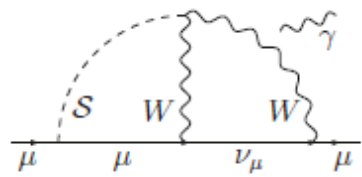
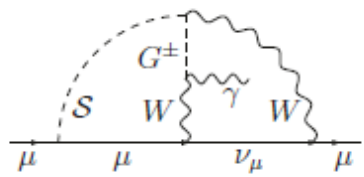
ciclotron

spin

Jegerlehner, Nyffeler
(09)



Jegerlehner, Nyffeler
(09)



$$Y_f^h = s_{\beta\alpha} + c_{\beta\alpha}\zeta_f,$$

$$Y_f^H = c_{\beta\alpha} - s_{\beta\alpha}\zeta_f,$$

$$Y_{d,l}^A = i\zeta_{d,l},$$

$$Y_u^A = -i\zeta_u.$$

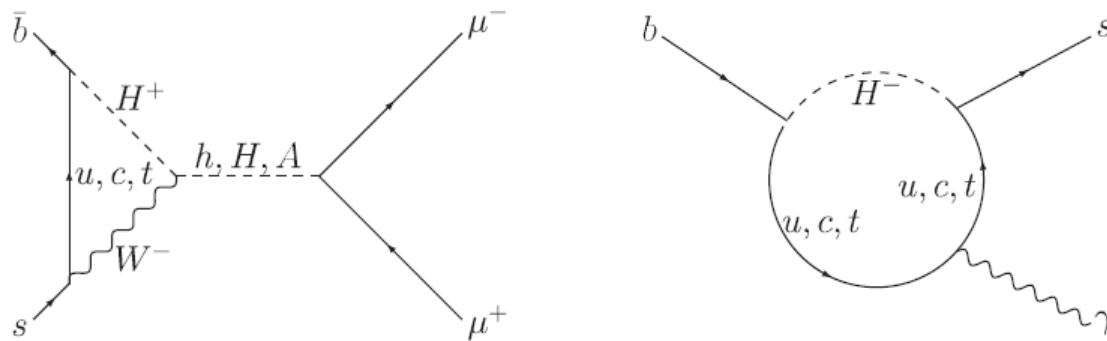
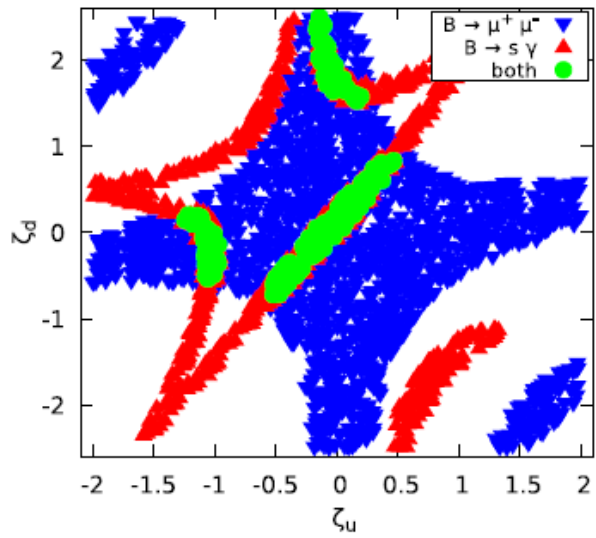
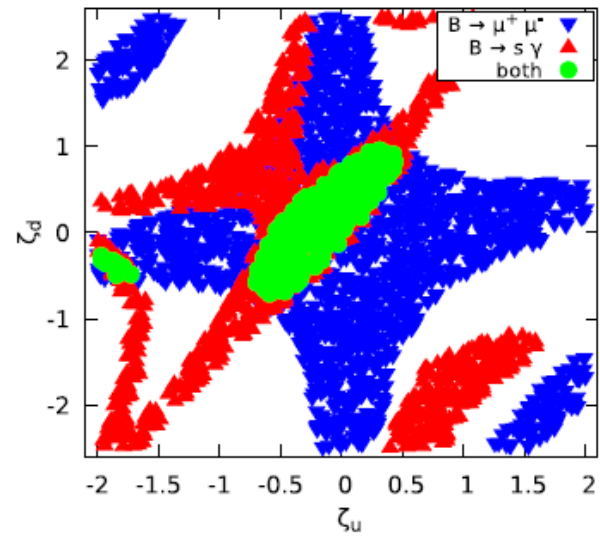


FIG. 2. Sample Feynman diagrams for the processes $B_s \rightarrow \mu^+ \mu^-$ and $b \rightarrow s \gamma$, which depend on the Yukawa couplings of up- and down-type quarks and leptons.

$M_A=40 \text{ GeV}, M_H=M_{H^\pm}=200 \text{ GeV}, \zeta_I=-60$



$M_A=50 \text{ GeV}, M_H=M_{H^\pm}=200 \text{ GeV}, \zeta_I=-40$



Maximum allowed $(g - 2)_\mu$

AC, Stöckinger, Stöckinger-Kim (18)

$$a_\mu^{1L} \approx \left(\frac{\zeta_l}{100}\right)^2 \left\{ \frac{-3 - 0.5 \ln(\hat{x}_A)}{\hat{x}_A^2} \right\} \times 10^{-10}$$

$$\hat{x}_S^2 = \frac{m_S^2}{100 \text{ GeV}}$$

$$a_\mu^{F,\tau} \approx \left(\frac{\zeta_l}{100}\right)^2 \left\{ \frac{8 + 4\hat{x}_A^2 + 2 \ln(\hat{x}_A)}{\hat{x}_A^2} \right\} \times 10^{-10}$$

$$a_\mu^{F,t} \approx \left(\frac{-\zeta_l \zeta_u}{100}\right) \{22 - 14 \ln(\hat{x}_A) + 32 - 15 \ln(\hat{x}_H)\} \times 10^{-10}$$

$$|a_\mu^B| \approx \rho \left| \frac{C_{HH^+H^-}}{\text{GeV}} \right| |\zeta_l| \times 10^{-15}$$

$$(g - 2)_\mu$$

- Beyond Standard Model:
 - Radiative corrections



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- Complementary information to direct searches (LHC)

Standard Model

- High Energy Physics (colliders)
 - Small deviations

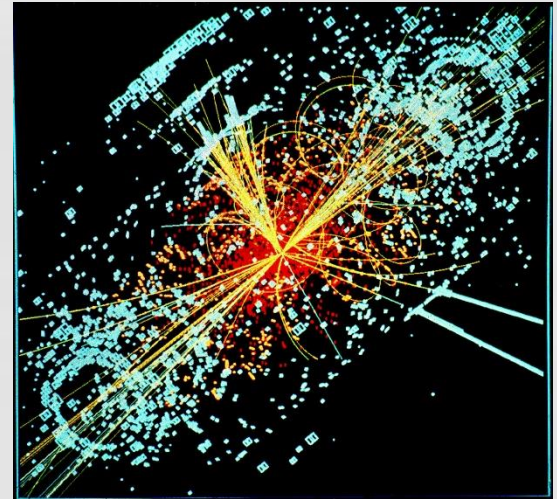


BSM predictions

Increase precision



- Open questions:
 - No gravitational interactions included;
 - No candidates for Dark Matter;
 - Matter-antimatter asymmetry;
 -



<http://cds.cern.ch/record/628469>

Beyond Standard Model

- Two-Higgs-Doublet-Model (2HDM)

- Minimal extension to scalar sector
- Four more scalars

Some variants (inert model) have dark matter candidate

- Supersymmetry (SUSY)

- Correlates bosons and fermions;
- Has a non-minimal scalar sector (2HDM);
- Predicts a partner to each particle of SM.



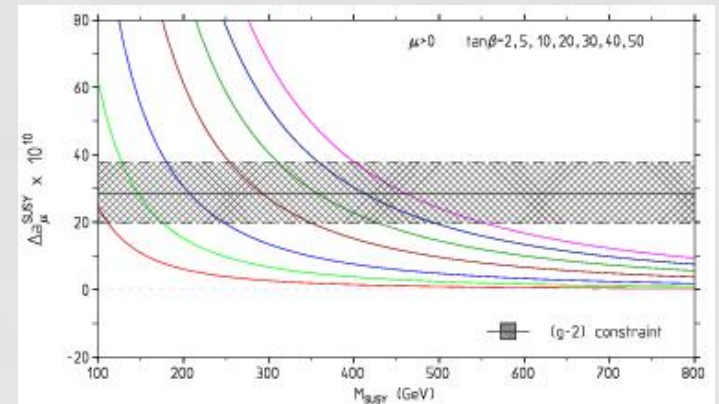
- Dark matter candidate;
- Solves naturalness problem.

$(g - 2)_\mu$

- Beyond Standard Model:
 - SUSY



$$a_\mu(SUSY) \cong 123 \times 10^{-11} \left(\frac{100 \text{ GeV}}{M_{SUSY}} \right)^2 \tan \beta$$



$$(g - 2)_\mu$$

- Beyond Standard Model:
 - SUSY

