

Cosmology of String Moduli and the Swampland

Fernando Quevedo

ICTP + Cambridge

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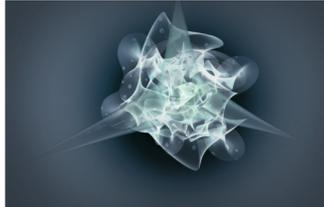
Lima, Peru, 2018

Based on Articles

- S. Antusch, F. Cefala, S. Krippendorf, F. Muia, S. Orani and FQ:
“Oscillons from String Moduli,”
JHEP {1801} (2018) 083, [arXiv:1708.08922].
- S. Krippendorf, F. Muia and FQ,
“Moduli Stars,”
JHEP {1808} (2018) 070, [arXiv:1806.04690].
- M Cicoli, S. de Alwis, A. Maharana, F. Muia and FQ
“de Sitter vs Quintessence in String Theory,”
[arXiv:1808.08967].
- J.P. Conlon and FQ
“Putting the Boot into the Swampland,”
[arXiv:1811.06276].

Strings and Moduli

- String theory predicts (6 or 7) extra dimensions
- Major problem: Fixing size and shape of extra dimensions (moduli)



- Progress to fix all moduli: only this century (GKP, KKLT, LVS,...)
- In some cases the 4D space = de Sitter space ($\Lambda > 0$)

Physics of Moduli

- Moduli: scalar particles in 4D: candidates for inflatons
- Gravitational strength couplings
- Mass of moduli \sim gravitino mass
- Each modulus equivalent to saxion+axion
- Number of moduli order 100-1000

Moduli Stabilisation in IIB

- Moduli S, T_i, U_a

$$V_F = e^K \left(K_{MN}^{-1} D_M W \bar{D}_{\bar{M}} \bar{W} - 3|W|^2 \right)$$

$$W_{\text{tree}} = W_{\text{flux}}(U, S) \quad K_{i\bar{j}}^{-1} K_i K_{\bar{j}} = 3 \quad \text{No-scale}$$

$$V_F = e^K \left(K_{a\bar{b}}^{-1} D_a W D_{\bar{b}} \bar{W} \right) \geq 0$$

Fix S, U but T arbitrary

- Quantum corrections

$$\delta V \propto W_0^2 \delta K + W_0 \delta W$$

- Three options: $W_0 \gg \delta W$ $\delta K \gg \delta W$ Runaway: Dine-Seiberg problem

$$\begin{aligned} W_0 &\sim \delta W = \tilde{W}_{\text{np}} \\ W_0 &\ll 1 \end{aligned}$$

Fix T-modulus: KKLT

$$\delta K \sim W_0 \delta W$$

$$\delta K \sim 1/\mathcal{V} \text{ and } \delta W \sim e^{-a\tau}$$

Fix T-moduli: LVS

String Cosmology

- Epochs: Pre-inflation, inflation, post-inflation (pre-BBN)
- Chiral spectrum implies $N=0,1$ in 4D (work with $N=1$)
- Strings relevant in postinflation? (yes: moduli).

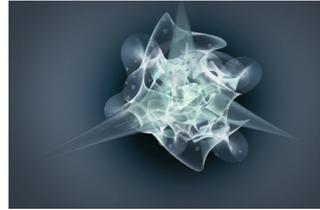
“Generically”: If EFT is suspersymmetric then the moduli survive at low energies until susy breaks:

$$\text{mass}_{\text{moduli}} \approx m_{\text{gravitino}}.$$

(but interesting exceptions!)

Kahler moduli

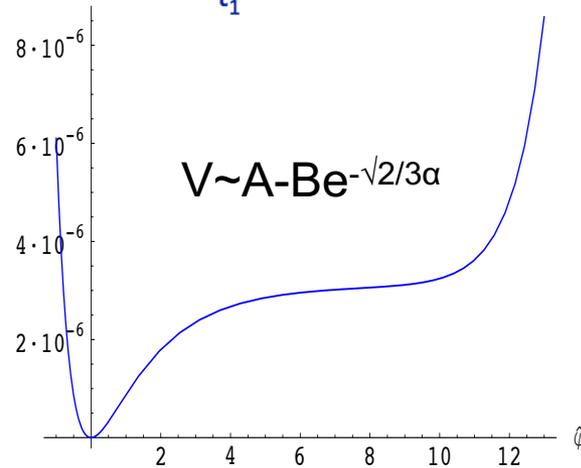
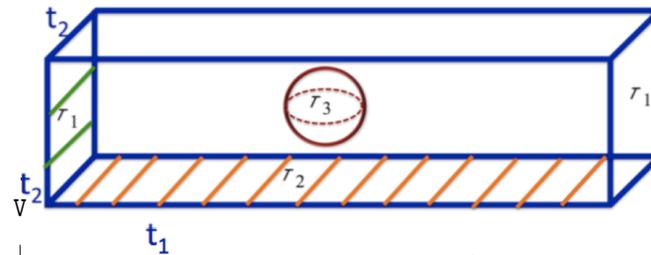
- Overall volume



- Blow-up

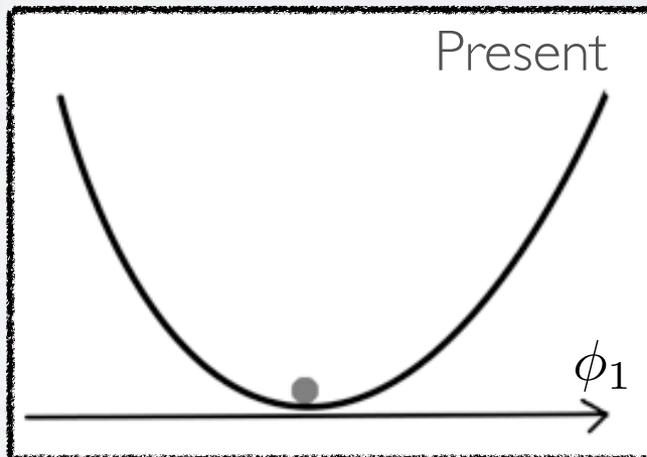
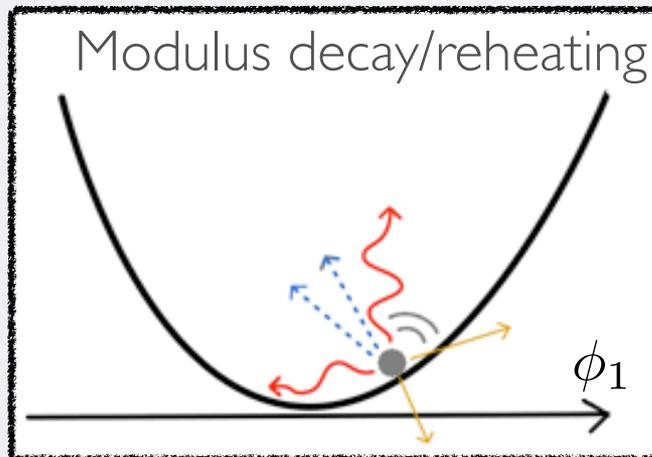
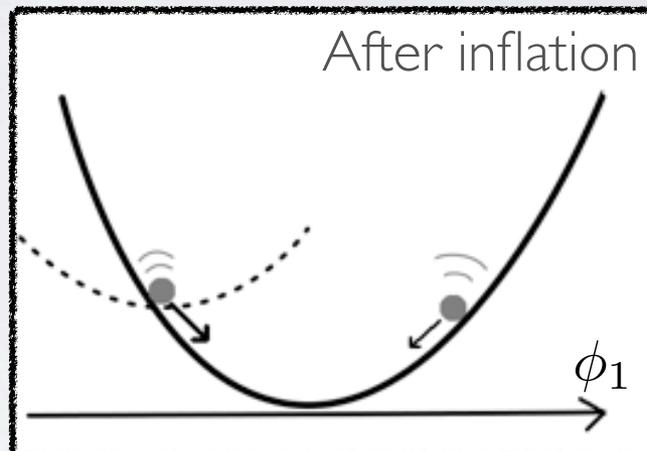
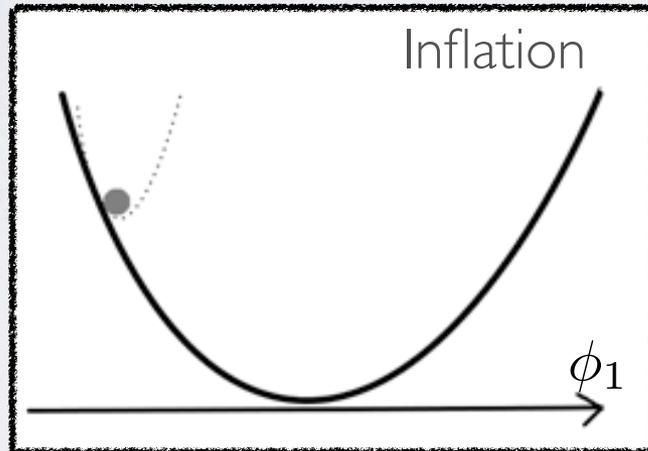


- Fibre moduli



Post Inflation

Moduli Domination



$$\Gamma_\phi \sim \frac{1}{8\pi} \frac{m_\phi^3}{M_{\text{Pl}}^2}$$

$$T > O(1 \text{ MeV}), \text{ so } m_\phi \gtrsim 3 \cdot 10^4 \text{ GeV}$$

Coughlan et al 1983, Banks et al, de Carlos et al 1993

Oscillons* from String Moduli

Antusch, Cefalá, Krippendorf, Muia, Orani, FQ

[arXiv:1708.08922](https://arxiv.org/abs/1708.08922)

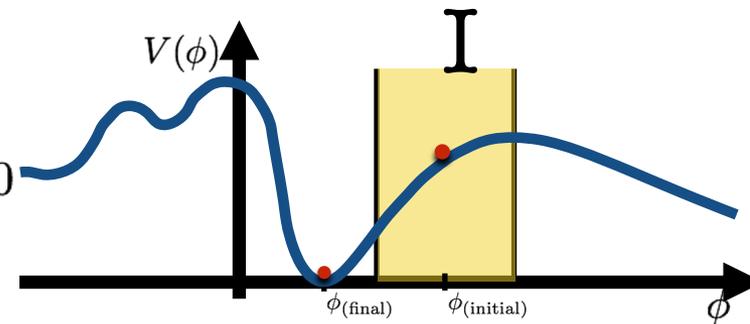
*localised, long-lived, non-linear excitations of the scalar fields.

Generalities

- Exponentially growing solutions:

$$\ddot{\phi}(t) + 3H\dot{\phi}(t) + V'(\phi(t)) = 0$$

$$\delta\ddot{\phi}_k + 3H\delta\dot{\phi}_k + \left(\frac{k^2}{a^2(t)} + V''(\phi(t)) \right) \delta\phi_k = 0$$



- Conditions for unstable solutions:

i. parametric resonance

ii. tachyonic preheating (modulus displaced in I)

$$k^2/a^2 + \partial^2 V/\partial\phi^2 < 0$$

iii. tachyonic oscillations (oscillations reach I)

$$k_p \sim \sqrt{\partial^2 V/\partial\phi^2|_{\min}} \equiv m$$

Necessary Conditions for Oscillons production

- Quantum fluctuations of the field grow as it oscillates around the minimum.
- The growth of fluctuations is sufficiently strong for non-linear interactions to become important.
- The potential is shallower than quadratic away from the minimum in some field space region relevant for the dynamics of the field.

$$V = \frac{m^2}{2}\phi^2 - \frac{\lambda}{4!}\phi^4 + \dots$$



Attractive 'force'
for $\lambda > 0$

Lattice simulations*

- LatticeEasy: to analyse strong growth of perturbations.

$$\ddot{\phi} + 3H\dot{\phi} - \frac{1}{a^2}\nabla^2\phi + \frac{\partial V}{\partial\phi} = 0 \quad H^2 = \frac{1}{3M_{\text{Pl}}^2} \left(V + \frac{1}{2}\dot{\phi}^2 + \frac{1}{2a^2}|\nabla\phi|^2 \right)$$

- Modified version to calculate also metric perturbations:

$$ds^2 = -dt^2 + a^2(t)(\delta_{ij} + h_{ij})dx^i dx^j$$
$$\ddot{h}_{ij} + 3H\dot{h}_{ij} - \frac{1}{a^2}\nabla^2 h_{ij} = \frac{2}{M_{\text{Pl}}^2}\Pi_{ij}^{\text{TT}} \quad \Pi_{ij}^{\text{TT}} = \frac{1}{a^2}[\partial_i\phi\partial_j\phi]^{\text{TT}}$$
$$\Omega_{\text{GW}}(k) = \frac{1}{\rho_c} k \frac{d\rho_{\text{GW}}}{dk} \quad \rho_{\text{GW}}(t) = \frac{M_{\text{Pl}}^2}{4} \left\langle \dot{h}_{ij}(\mathbf{x}, t)\dot{h}_{ij}(\mathbf{x}, t) \right\rangle_{\text{V}}$$

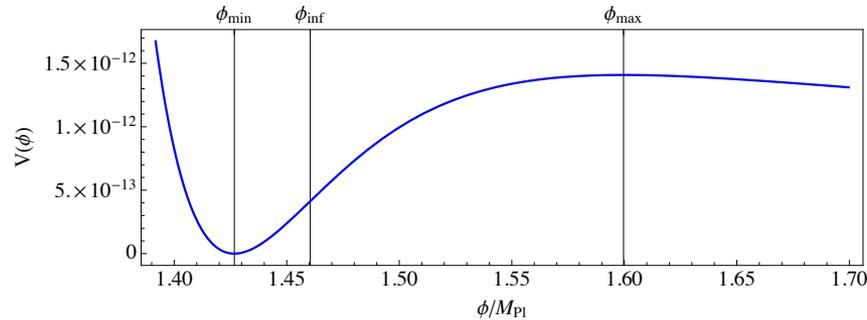
*Plus Floquet analysis

KKLT Oscillons

$$V/M_{\text{Pl}}^4 = \frac{e^{K_{\text{cs}}}}{6\tau^2} \left(aA^2(3 + a\tau)e^{-2a\tau} - 3aAe^{-a\tau}W_0 \right) .$$

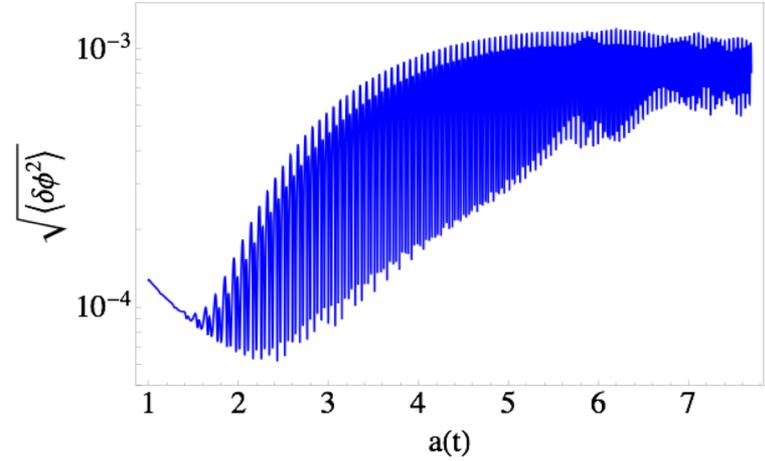
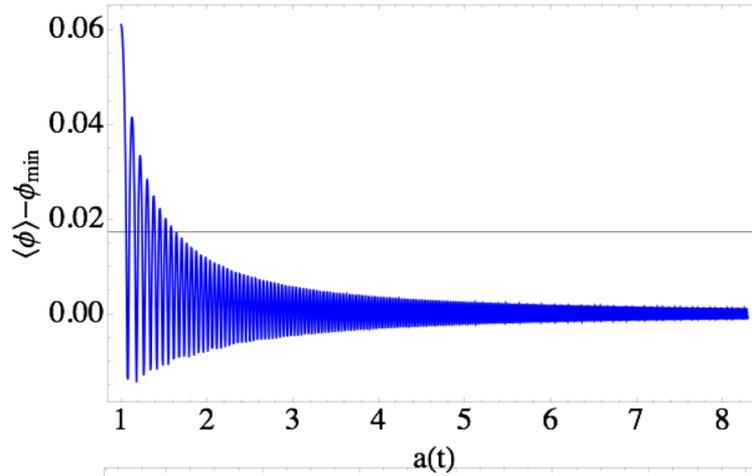
$$\phi/M_{\text{Pl}} = \frac{\sqrt{3}}{2} \log(T + \bar{T}) .$$

$$10^{-12} \leq W_0 \leq 10^{-5}, \quad 1 \leq A \leq 10, \quad 1 \leq a \leq 2\pi .$$

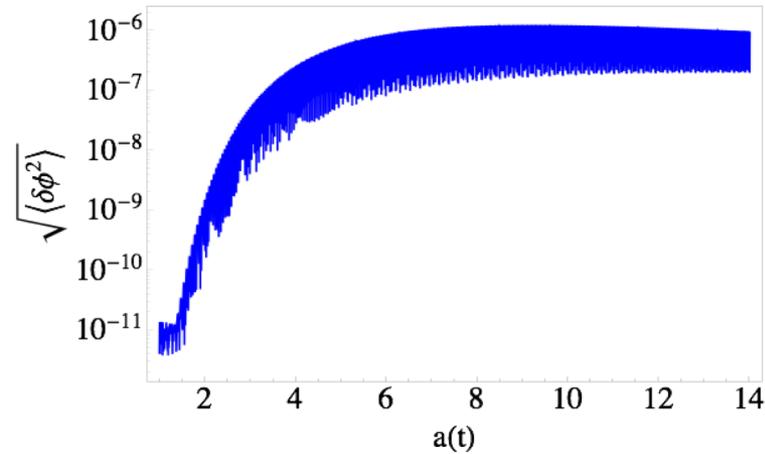
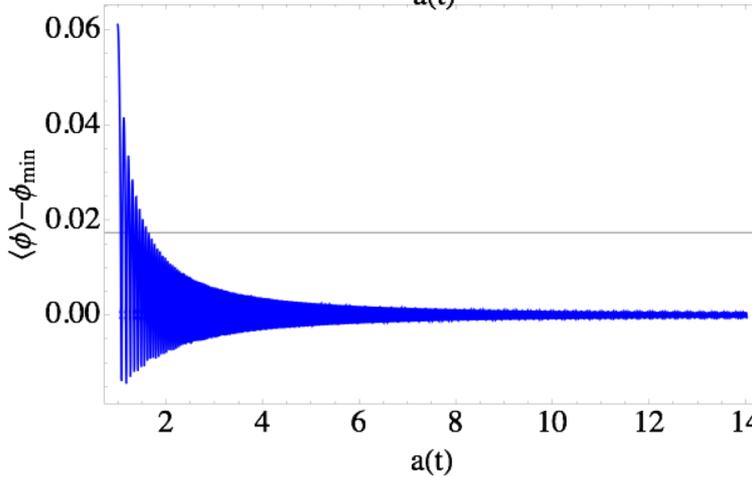


KKLT results

$W_0=10^{-12}$
(no oscillons)



$W_0=10^{-5}$
oscillons
generated

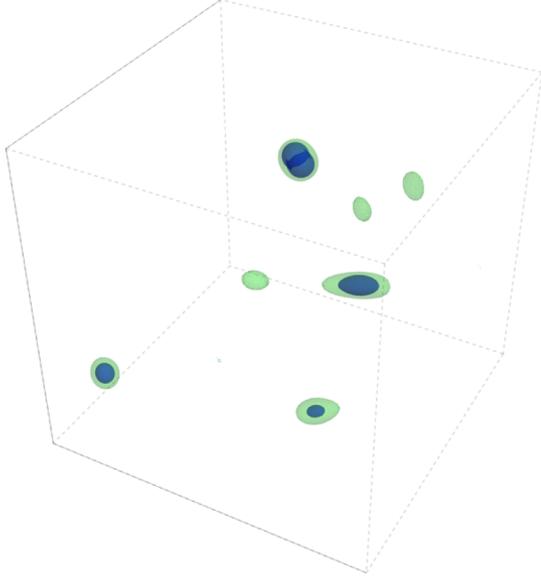


512^3 points

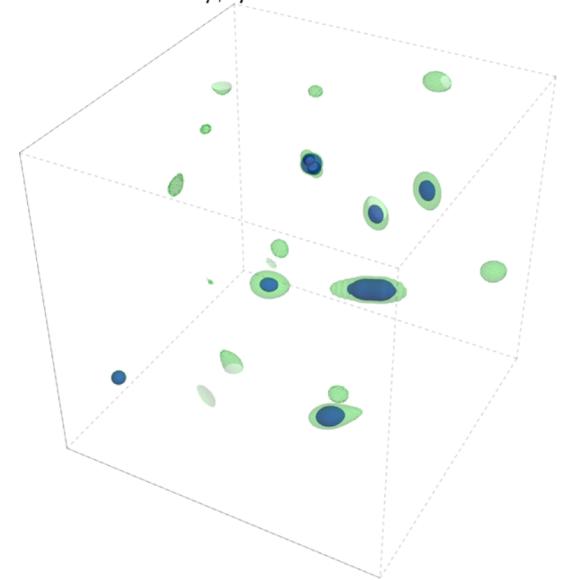
$$L^3 \simeq (0.7/H_{\text{initial}})^3$$

Snapshots

$\rho / \langle \rho \rangle$ at $a = 6.41$

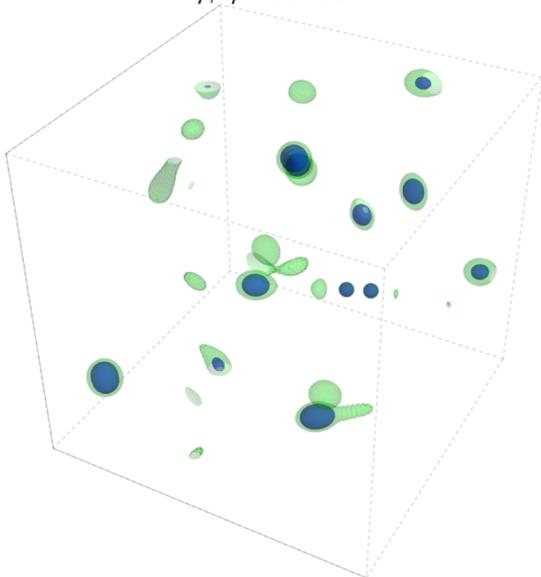


$\rho / \langle \rho \rangle$ at $a = 7.07$

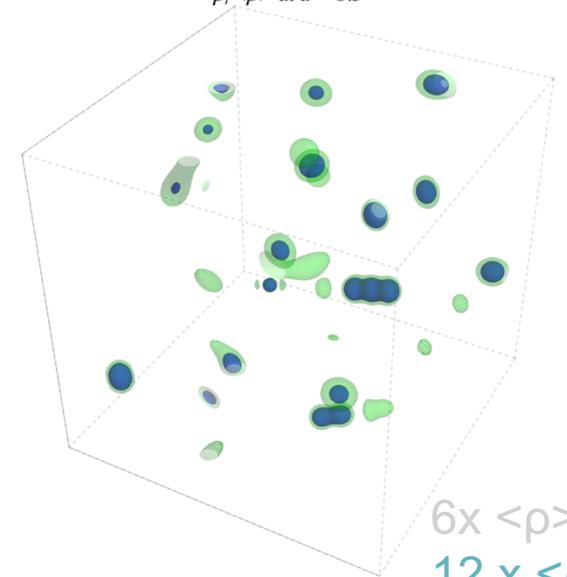


$W_0 = 10^{-5}$
 $A = 10$
 $a = 2\pi$

$\rho / \langle \rho \rangle$ at $a = 7.7$

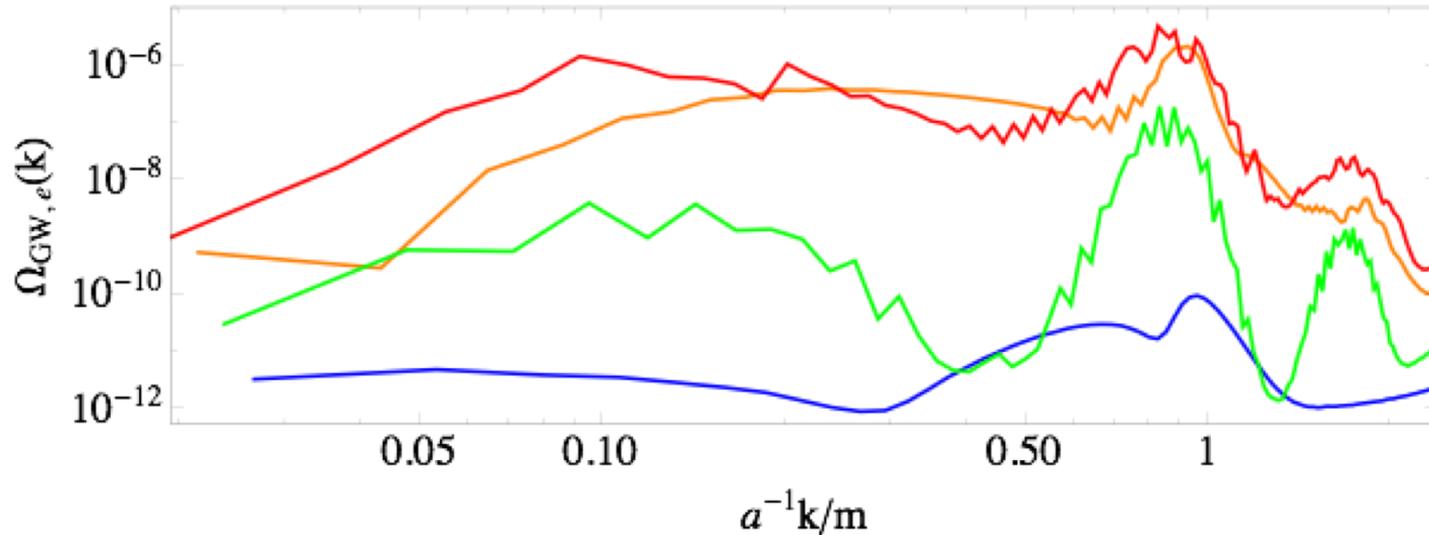


$\rho / \langle \rho \rangle$ at $a = 8.3$



$6x \langle \rho \rangle$
 $12x \langle \rho \rangle$

GW spectrum: KKL T



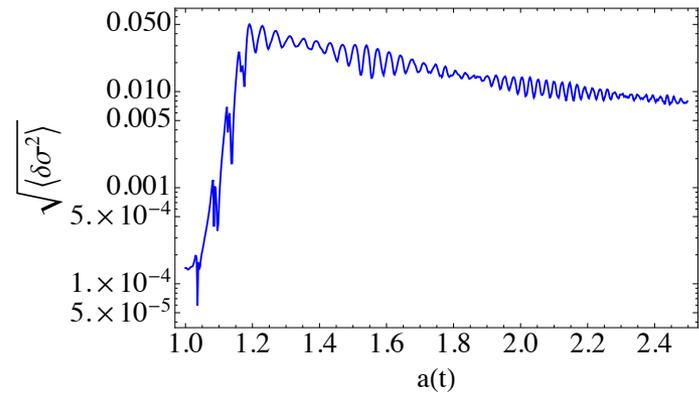
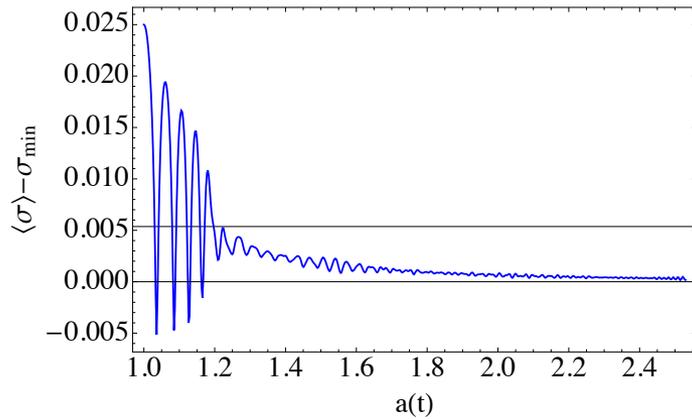
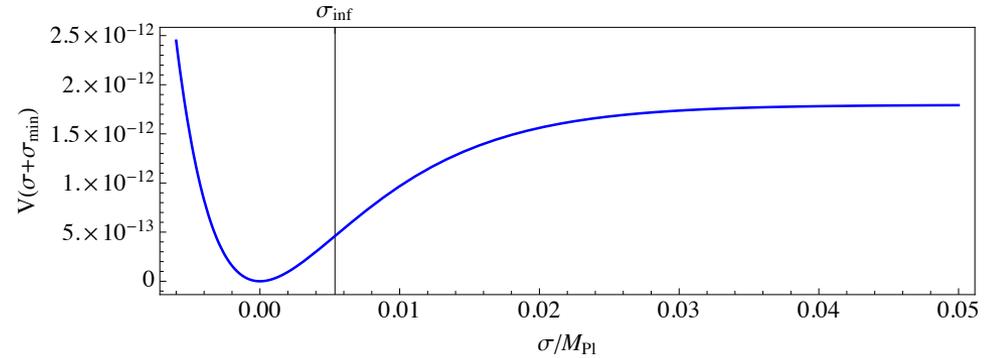
$$f_{0,\text{peak}} \sim 10^9 \text{ Hz}$$

$$\Omega_{\text{GW},0}(f_{0,\text{peak}}) \sim 3 \times 10^{-11}$$

*Overall scaling can lower frequency but also lower the amplitude

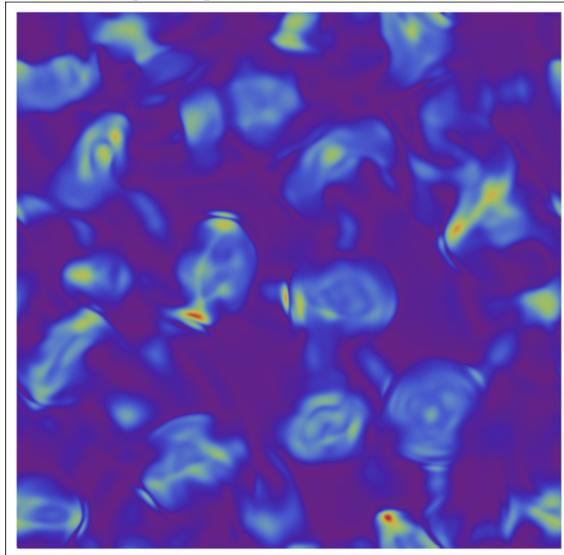
Blow-up Potential in LVS

$$V \sim V_0 \left(1 - \kappa(\sigma) e^{-\alpha \sigma^{4/3}} \right)^2 ,$$

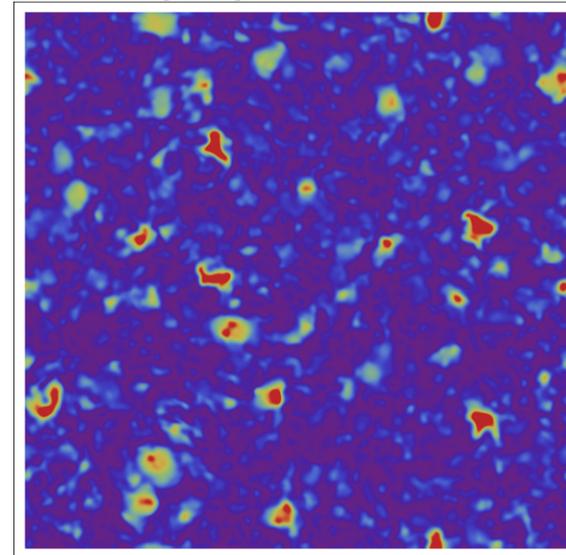


Oscillons from Blow-up mode

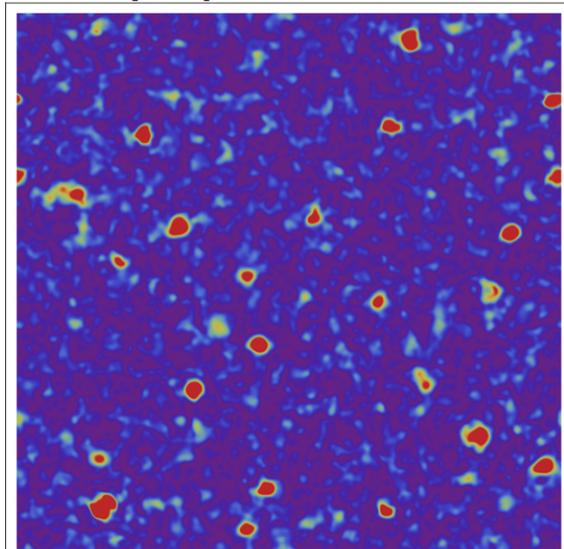
$\rho/\langle\rho\rangle$ at $a=1.26$



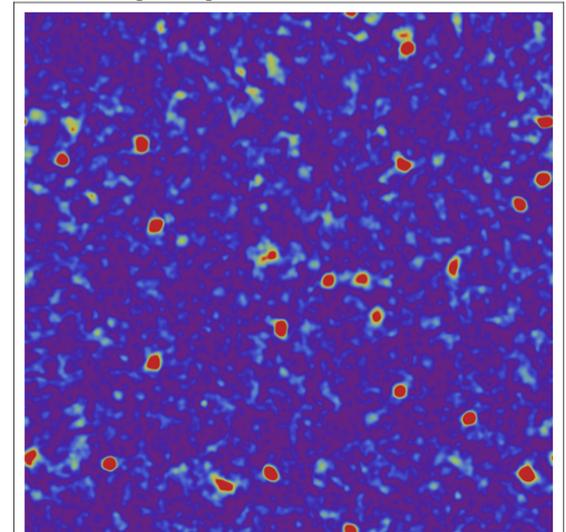
$\rho/\langle\rho\rangle$ at $a=2.$



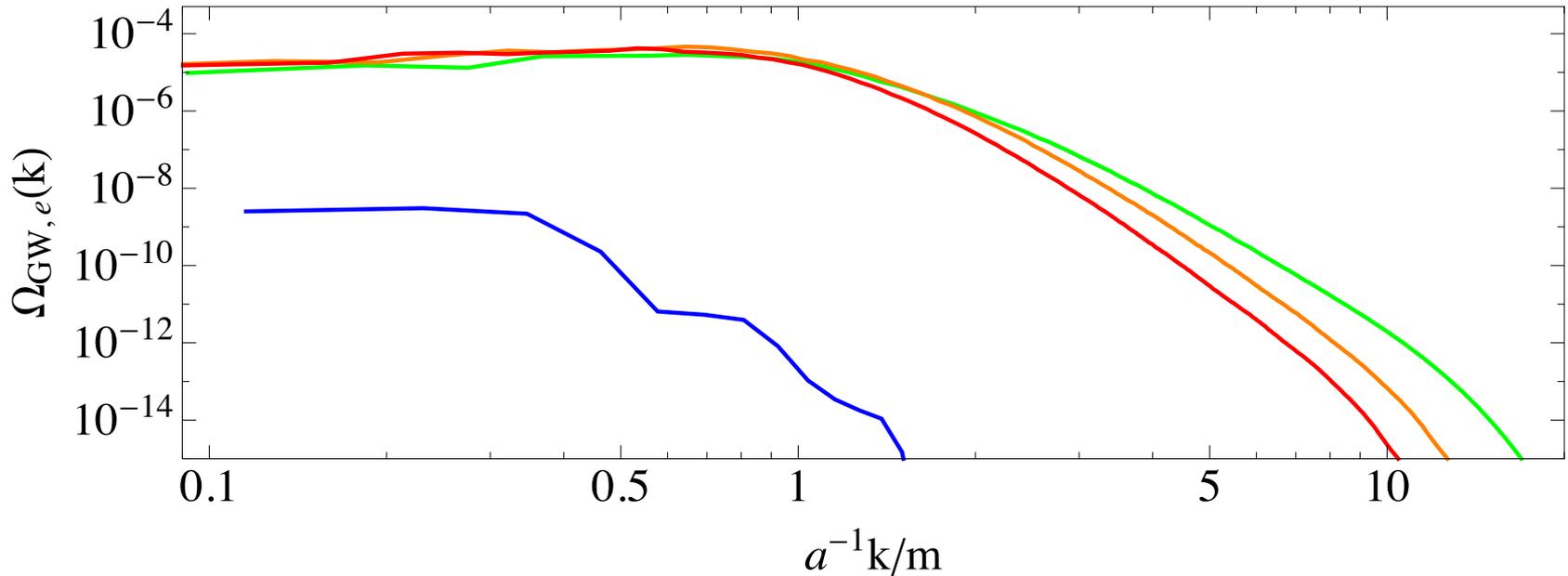
$\rho/\langle\rho\rangle$ at $a=3.02$



$\rho/\langle\rho\rangle$ at $a=4.02$



Gravitational Waves



$$f_0 \sim 10^8 \text{ Hz} - 10^9 \text{ Hz}, \quad \text{with} \quad \Omega_{\text{GW},0} \sim 10^{-10} - 5 \times 10^{-10}.$$

*No oscillons for volume nor fibre moduli but also no overshooting!

Moduli Stars

Boson and Fermion Stars

- Fermion stars: Gravity vs fermion pressure

$$GM^2/R \sim N^{4/3}/R, \quad N = M/m$$

$$M_{\max} \sim \frac{M_{\text{P}}^3}{m_f^2} \quad R_{\min} \sim \frac{M_{\text{P}}}{m_f^2}.$$

(e.g. $M \sim M_{\odot}$ for $m \sim 1$ GeV neutron star)

- Boson stars: Gravitational BEC

Heisenberg $R > 1/m$
Schwarzschild $R \sim 2GM$

$$R_{\min} \sim \frac{1}{m} \quad M_{\max} \sim \frac{M_{\text{P}}^2}{m}.$$

But adding interactions

$$M_c \sim M_{\text{p}}^3/m^2$$

Bosonic Compact Objects

- Q-balls
 - Oscillons
- } Repulsive pressure vs attractive interaction

Gravity vs Repulsive pressure

- Boson stars
- Mini-boson stars
- Oscillatons (e.g. axion stars)
(+ axion miniclusters)

Are there stringy boson/fermion stars?

Candidates:

Long-lived (stable) gravitationally coupled fields:

- hidden sector fermions/bosons,
- moduli,
- modulini,
- gravitini

Stringy Fermion Stars

Gravitino and modulini:

$$M_{\max} \sim \frac{M_{\text{P}}^3}{m_f^2} \quad m_f = m_{3/2} = \frac{W_0}{\mathcal{V}}$$

Validity of EFT and Cosmological moduli problem: $10^3 \leq \mathcal{V} \leq 10^9$

$$1 \text{ g} \lesssim M \lesssim 10^{15} \text{ g}, \quad 10^{-27} \text{ cm} \lesssim R \lesssim 10^{-15} \text{ cm}$$

Recall: $M_{\odot} \simeq 2 \times 10^{33} \text{ g} \simeq 10^{57} \text{ GeV}$. $1 \text{ GeV} \simeq 1.8 \times 10^{-24} \text{ g}$

Volume modulus stars

$$S = \int d^4x \sqrt{-g} \left[-\frac{g^{\mu\nu}}{2} \partial_\mu \varphi \partial_\nu \varphi - V(\varphi) \right]$$

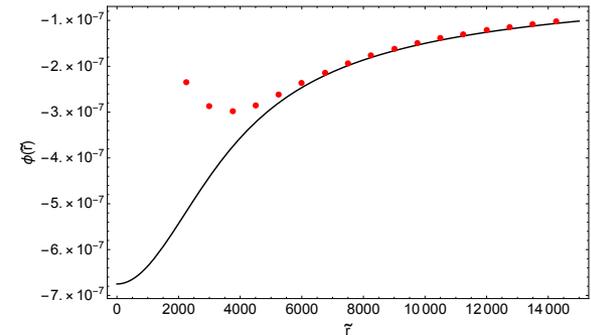
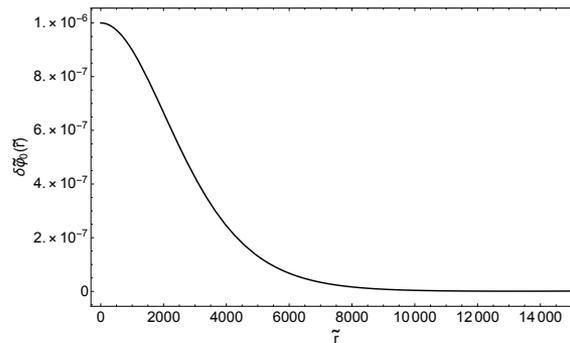
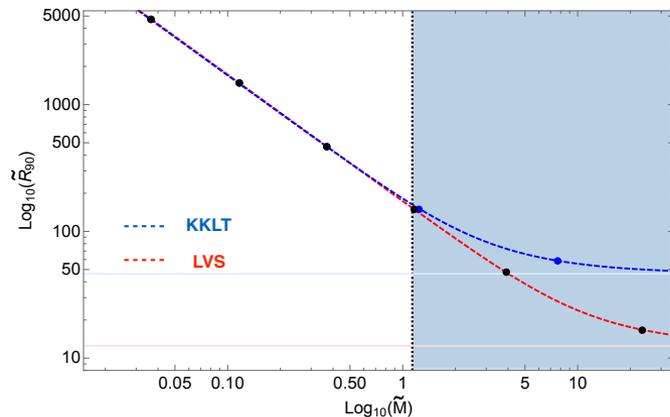
$$\varphi(r, t) = \varphi_0(r) \cos(\omega t),$$

$$ds^2 = -(1 + 2\phi) dt^2 + (1 - 2\phi) dr^2 + r^2 d\Omega^2,$$

$$\tilde{\varphi}_0''(\tilde{r}) + \frac{2}{\tilde{r}} \tilde{\varphi}_0'(\tilde{r}) = 2(\phi(\tilde{r}) - \epsilon) \tilde{\varphi}_0(\tilde{r}),$$

$$\phi''(\tilde{r}) + \frac{2}{\tilde{r}} \phi'(\tilde{r}) = \frac{\tilde{\varphi}_0^2(\tilde{r})}{4},$$

$$M(r) = \left(\frac{\Lambda^2}{m} \right) \tilde{M}(\tilde{r}), \quad \tilde{M}(\tilde{r}) = 4\pi \int_0^{\tilde{r}} d\tilde{r}' \tilde{r}'^2 \tilde{\rho}(\tilde{r}').$$



Q-Balls*

...Coleman (1985)...

Complex scalar, U(1) global symmetry

$$\mathcal{L} = \int d^3x \left(\frac{1}{2} \partial^\mu \Phi \partial_\mu \Phi^* - U(|\Phi|) \right)$$

U minimum at $\Phi=0$

Noether current and conserved charge

$$J_\mu = \frac{1}{2i} (\Phi^* \partial_\mu \Phi - \Phi \partial_\mu \Phi^*); \quad Q = \int d^3x J^0 = \frac{1}{2i} \int d^3x (\Phi^* \dot{\Phi} - h.c.)$$

Extrema of energy

$$\begin{aligned} E_\omega &= \int d^3x \left(\frac{1}{2} |\dot{\Phi}|^2 + \frac{1}{2} |\nabla \Phi|^2 + U(|\Phi|) \right) + \omega \left(Q - \frac{1}{2i} \int d^3x (\Phi^* \dot{\Phi} - h.c.) \right) \\ &= \int d^3x \left(\frac{1}{2} |\dot{\Phi} - i\omega \Phi|^2 + \frac{1}{2} |\nabla \Phi|^2 + \hat{U}(|\Phi|) \right) + \omega Q \end{aligned} \quad \hat{U}_\omega(|\Phi|) = U(|\Phi|) - \frac{1}{2} \omega^2 |\Phi|^2.$$

$$\Phi(x, t) = \varphi(x) e^{i\omega t}$$

Thin wall approximation (large Q)

$$E = Q \sqrt{\frac{2U(\varphi_0)}{\varphi_0^2}}$$

Q-balls in string theory?*

Global symmetries?

1. From (non) anomalous U(1)
2. From Peccei-Quinn symmetries

***Open strings:**

$$U_D = g^2 \left(\xi - \sum_i q_i |\Phi_i|^2 \right)^2$$
$$U_{\text{soft}} = \sum_i m_i^2 |\Phi_i|^2 + \left(\sum_{ijk} A_{ijk} \Phi_i \Phi_j \Phi_k + \sum_{ij} B_{ij} \Phi_i \Phi_j + h.c. \right)$$
$$E^2 = \frac{2U}{\sum_i q_i |\Phi_i|^2} = \frac{2(U_D + U_{\text{soft}})}{\sum_i q_i |\Phi_i|^2}$$

Minimum for nonvanishing: $\rho^2 = \sum_i q_i \rho_i^2 = \sum_i q_i |\Phi_i|^2$

e.g. Kusenko (1997) for
MSSM

Closed string sector*

- Massive moduli + axion
(generalised axion stars, $m > 1$ TeV)

- Axion much lighter
(Ultra-light axion)

$$V_\psi = \frac{g_s}{2\pi} a_b A_b \frac{e^{-a_b \tau_b}}{\tau_b^2} [1 + \cos(a_b \psi_b)] ,$$

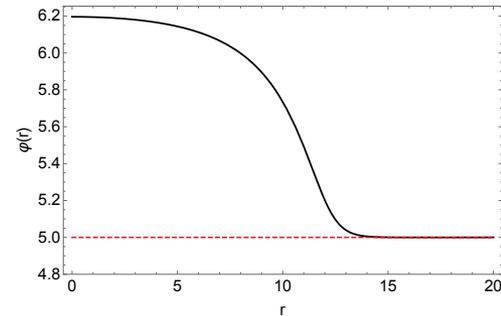
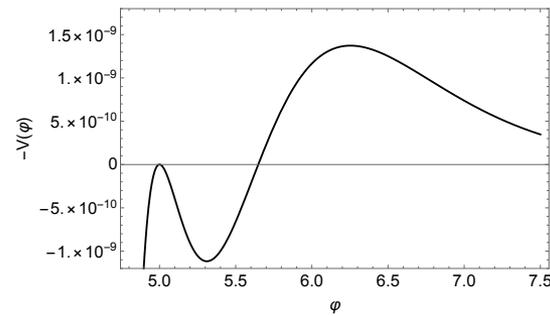
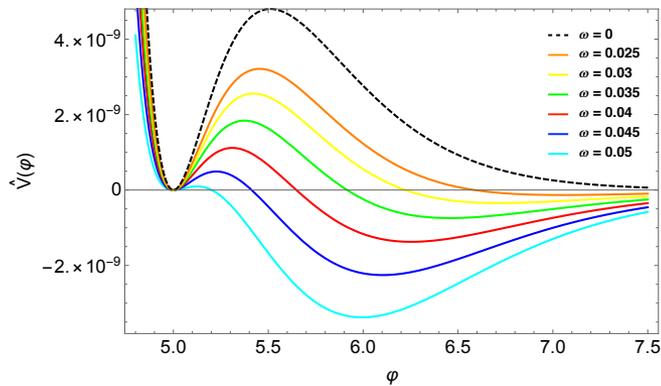
- PQ symmetry almost exact (PQ-balls?)

PQ Balls?*

$$S = \int d^4x \mathcal{L} = \int d^4x [-f(\tau) [\partial_\mu \tau \partial^\mu \tau + \partial_\mu \theta \partial^\mu \theta] - V(\tau)]$$

$$\dot{\theta} = \omega, \quad \nabla \theta = 0. \quad \hat{V}(\tau) = V(\tau) - \omega^2 f(\tau)$$

$$Q = \omega \int d^3x f(\tau) \propto \int 4\pi r^2 dr \frac{\omega}{r^2} \rightarrow \infty.$$



Spinning Axions?*

$$\mathcal{S} = \int d^4x \sqrt{-g} [-g^{\mu\nu} (\partial_\mu \varphi \partial_\nu \varphi + f(\varphi) \partial_\mu \theta \partial_\nu \theta) - V]$$

$$f = \alpha / \tau^2 = \alpha e^{-\sqrt{2/\alpha} \varphi}.$$

$$\ddot{\varphi} + 3H\dot{\varphi} + \partial_\varphi V = \frac{q^2 \partial_\varphi f}{4a^6 f^2}.$$

$$V = V_0 e^{-\kappa_1 \varphi}, \quad f = \alpha e^{-\kappa_2 \varphi},$$

$$\varphi(t) = B \ln t - C, \quad a(t) = t^{\frac{\kappa_1 + \kappa_2}{3\kappa_1}}, \quad w(\varphi) = \frac{\kappa_1 - \kappa_2}{\kappa_1 + \kappa_2}.$$

Similar to
spintessence

Formation Mechanisms?

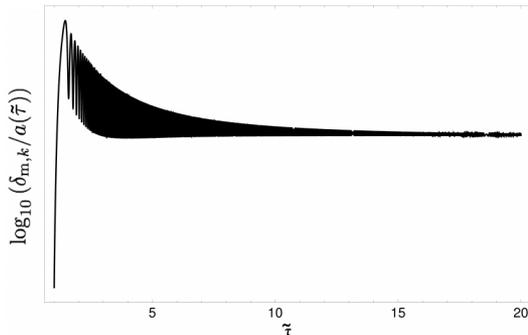
I) There is some initial localized overdensity;

II) The initial overdensity collapses due to the effect of attractive interactions.

$$\delta_{m,k} \equiv \frac{\delta\rho_{m,k}}{\langle\rho\rangle} \propto a(t) \sim t^{2/3}, \quad k \gg aH.$$

$$\Psi = \frac{\delta_{m,k}(t_{\text{dec}})}{\delta_{m,k}(t_{\text{mat}})} \approx \left(\frac{t_{\text{dec}}}{t_{\text{mat}}}\right)^{2/3} \approx \left(\frac{H_{\text{mat}}}{H_{\text{dec}}}\right)^{2/3} \approx \left(\frac{m}{\Gamma}\right)^{2/3} \approx \left(\frac{M_{\text{P}}}{m}\right)^{4/3},$$

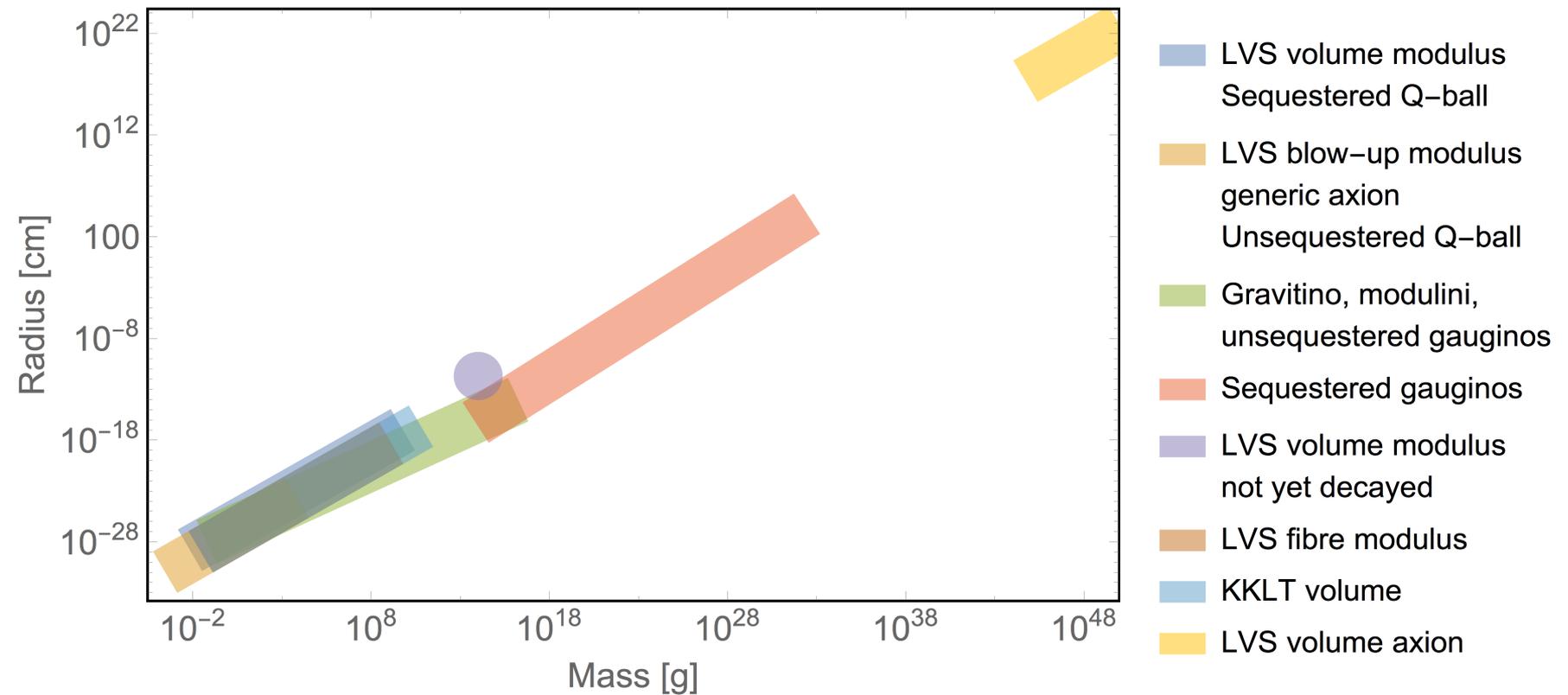
$$\Psi = \frac{\delta_{m,k}(\tau_{\text{dec}})}{\delta_{m,k}(\tau_{\text{mat}})} \Big|_{\nu} \approx \left(\frac{M_{\text{P}}}{M_{\text{P}}/\nu^{3/2}}\right)^{4/3} = \nu^2, \quad \text{Enhancement factor!}$$



Properties of Moduli Stars

Particle	State mass	Star mass	Star radius	Enhancement
LVS volume modulus	$M_{\text{P}}/\mathcal{V}^{3/2}$	$M_{\text{P}}\mathcal{V}^{3/2}$	$l_{\text{P}}\mathcal{V}^{3/2}$	\mathcal{V}^2
LVS blow-up modulus Generic axion	M_{P}/\mathcal{V}	$M_{\text{P}}\mathcal{V}$	$l_{\text{P}}\mathcal{V}^{5/3}$	$\mathcal{V}^{4/3}$
LVS fibre moduli	$M_{\text{P}}/\mathcal{V}^{5/3}$	$M_{\text{P}}\mathcal{V}^{5/3}$	$l_{\text{P}}\mathcal{V}^{5/3}$	$\mathcal{V}^{20/9}$
LVS volume axion	$M_{\text{P}}e^{-\alpha\mathcal{V}^{2/3}}$	$M_{\text{P}}e^{\alpha\mathcal{V}^{2/3}}$	$l_{\text{P}}e^{\alpha\mathcal{V}^{2/3}}$	$e^{4/3\alpha\mathcal{V}^{2/3}}$
KKLT volume modulus	$M_{\text{P}} W_0 /\mathcal{V}$	$M_{\text{P}} W_0 ^{-1}\mathcal{V}$	$l_{\text{P}} W_0 ^{-1}\mathcal{V}$	$(W_0 ^{-1}\mathcal{V})^{4/3}$
Gravitino, modulini, unsequestered gauginos	$M_{\text{P}} W_0 /\mathcal{V}$	$M_{\text{P}}\mathcal{V}^2/ W_0 ^2$	$l_{\text{P}}\mathcal{V}^2/ W_0 ^2$	$\mathcal{V}^{4/3}/ W_0 ^{4/3}$
Sequestered gauginos	$M_{\text{P}}/\mathcal{V}^2$	$M_{\text{P}}\mathcal{V}^4$	$l_{\text{P}}\mathcal{V}^4$	$\mathcal{V}^{8/3}$
Unsequestered Q-balls	M_{P}/\mathcal{V}	$M_{\text{P}}\mathcal{V}$	$l_{\text{P}}\mathcal{V}$	$\mathcal{V}^{4/3}$
Sequestered Q-balls	$M_{\text{P}}/\mathcal{V}^{3/2}$	$M_{\text{P}}\mathcal{V}^{3/2}$	$l_{\text{P}}\mathcal{V}^{3/2}$	\mathcal{V}^2

Size and Mass of Moduli Stars



de Sitter vs Quintessence

de Sitter Challenges

- Define S-matrix (resonance?)
- Classical no-go theorems (atoms are unstable classically!)
- No dS solution of string theory under full calculational control* (KKLT, LVS,...?)

* de Sitter solutions so far EFT “not under full control” \neq “no control at all”!

Swampland conjectures

- Swampland: Quantum gravity vs EFT ! Vafa et al.
- Weak gravity conjecture
- Distance conjecture
- New (non) de Sitter conjecture: $M_p \frac{|\nabla V|}{V} \gtrsim c,$

(It would imply quintessence and no de Sitter Obied et al
and difficult to have inflation!).

Challenges for the new conjecture

- Higgs potential with quintessence field? (at the $\langle H \rangle = 0$ point. Denef et al.
- If V asymptotes to infinite from above even supersymmetric AdS forbidden. Conlon
- Both addressed if modify conjecture (allow saddle points for $V > 0$). see e.g. Andriot
Ooguri et al

Quintessence from Strings?

- Need stabilise all moduli except for quintessence field:
as difficult as getting de Sitter
- Or have many fields rolling but slower than
quintessence. Difficult.
- Fifth force and varying couplings constraints (e.g.
volume modulus or dilaton problematic)

Quintessence Candidates

- Modulus (fibre, blow-up) that does not couple directly to SM. It also would require a very small string scale (e.g. $M_s \sim \text{TeV}$)

Cicoli, et al

- Axions

$$\mathcal{L} = -\frac{1}{2}\partial^\mu\theta\partial_\mu\theta - \mu^4 \left(1 - \cos\left(\frac{\theta}{f}\right)\right),$$

K. Choi
Panda et al
Kaloper et al.

Axion Quintessence 1

$$m_a \simeq \sqrt{\frac{g_s}{8\pi}} \frac{M_p}{\mathcal{V}^{2/3}} e^{-\frac{\pi}{N} \mathcal{V}^{2/3}} M_p, \quad \text{Naturally very small!}$$

$$V = \Lambda^4 - \sum_{i=1}^{N_{\text{ULA}}} \Lambda_i^4 \cos\left(\frac{a_i}{f_i}\right) + \dots, \quad \text{Minimum not necessarily at zero}$$

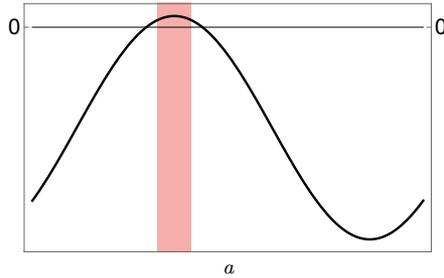
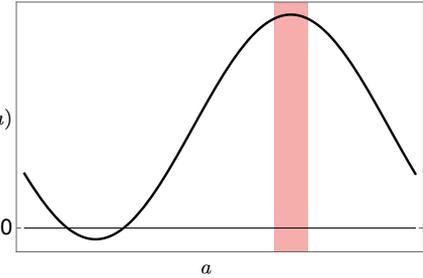
$$\epsilon = \frac{1}{2} \left[\left(\frac{\Lambda_\ell}{\Lambda}\right)^4 \frac{M_p}{f_\ell} \right]^2 \frac{\sin^2(a_\ell/f_\ell)}{\left(1 - (\Lambda_\ell/\Lambda)^4 \cos(a_\ell/f_\ell)\right)^2} < 1. \quad \text{Slow-roll}$$

$$f_\ell \gtrsim M_p. \quad \text{Not necessarily}$$

Axion Quintessence 2

- Hilltop Quintessence

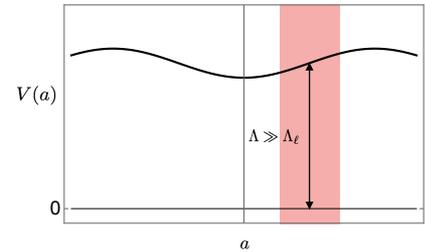
$$\Lambda^4 + \Lambda_i^4 > 0$$



- Quasi-natural quintessence

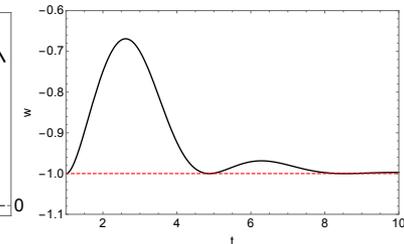
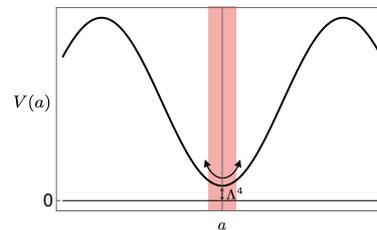
$$f_\ell \gtrsim \left(\frac{\Lambda_\ell}{\Lambda}\right)^4 M_p$$

$$f_\ell < M_p \quad \Lambda \gg \Lambda_\ell.$$



$$w = \frac{p}{\rho} = \frac{\frac{\dot{a}^2}{2} - V}{\frac{\dot{a}^2}{2} + V} \sim -\frac{1 - \frac{1}{3}\epsilon}{1 + \frac{1}{3}\epsilon} \sim -1 + \frac{2}{3}\epsilon.$$

- Oscillating quintessence



AdS/CFT and Bootland Conjectures

Bootland Conjecture

- LVS/CFT correspondence?

$$\Delta = \frac{3(1 + \sqrt{19})}{2} \left(1 - \sqrt{\frac{2}{27}} \frac{1}{\langle \Phi \rangle} + \mathcal{O} \left(\frac{1}{\langle \Phi \rangle} \right)^2 \right). \quad \text{For Volume mode}$$

$$\Delta_a = 3. \quad \text{For volume axion mode}$$

- n-point functions

$$\mathcal{L}_{(\delta\Phi)^n} = (-1)^{n-1} \lambda^n (n-1) \left(-3 \frac{M_P^2}{R_{AdS}^2} \right) \frac{1}{n!} \left(\frac{\delta\Phi}{M_P} \right)^n \left(1 + \mathcal{O} \left(\frac{1}{\lambda \langle \Phi \rangle} \right) \right),$$
$$\mathcal{L}_{(\delta\Phi)^{n-2} aa} = \left(-\sqrt{\frac{8}{3}} \right)^{(n-2)} \frac{1}{2(n-2)!} \left(\frac{\delta\Phi}{M_P} \right)^{n-2} \partial_\mu a \partial^\mu a,$$

- Bootland: bootstrap constraints in CFT side=Swampland constraints on AdS side.

Conclusions

- Rich spectrum of compact objects (stringy oscillons, gravitino, modulini, moduli, oscillatons, axion stars)
Gravitational waves spectrum ('hear the shape of the extra dimensions?')
- de Sitter vs Quintessence: Many achievements, challenges, open questions (*experiments??)

The report of my death was an exaggeration.

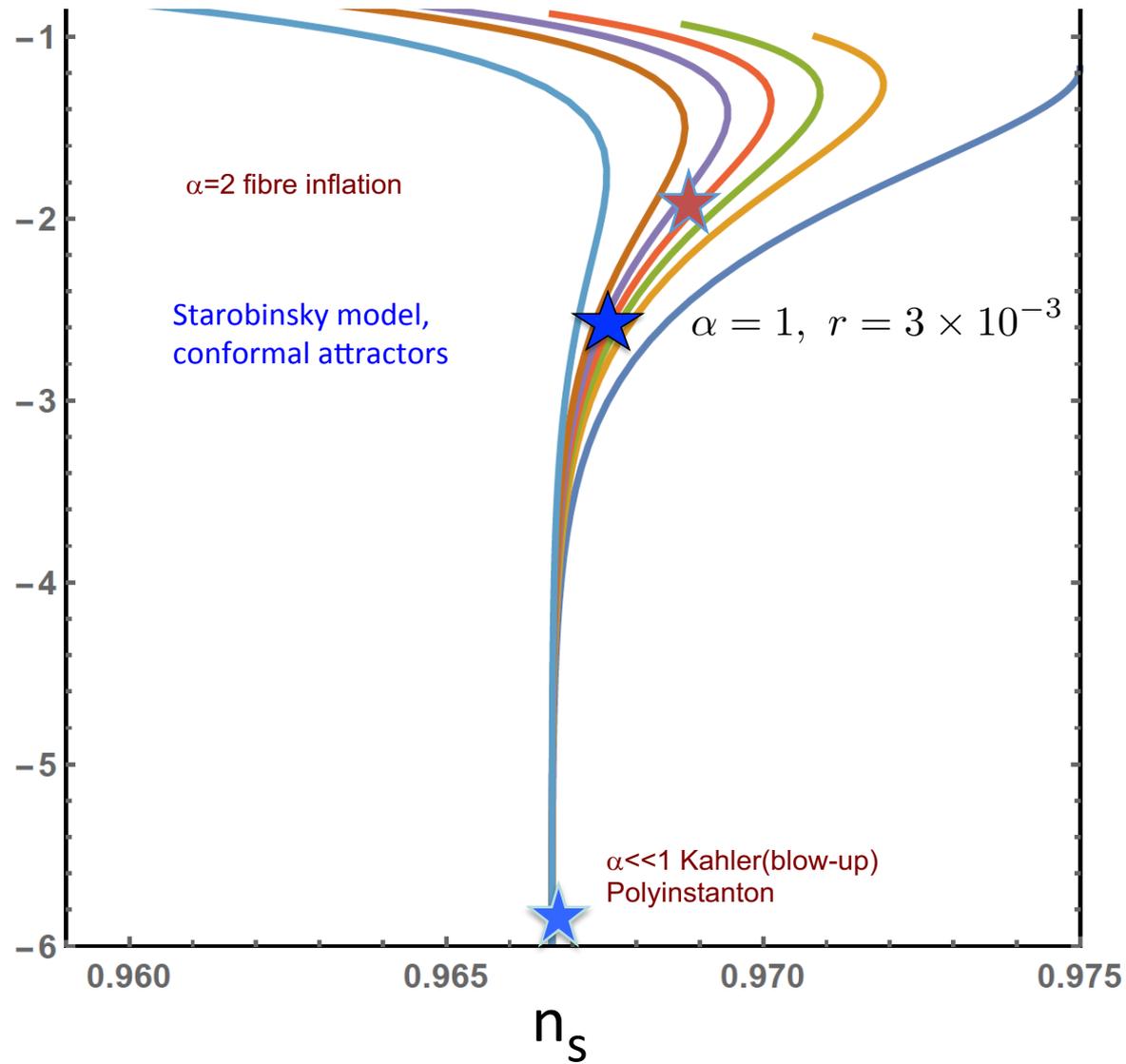
Mark Twain

- Swampland conjectures: interesting new perspective, e.g. "bootland" and LVS/CFT, KKLT/CFT
- More? "Standard Model Swampland Conjecture"??..

de Sitter Achievements

- Remarkable: well defined prescription exists that includes all stringy ingredients: branes, orientifolds, warping, anti (T)-branes, perturbative, non-perturbative effects, etc.
- IIB with fluxes ~ Calabi-Yau (moduli space understood).
- $W_0 \ll 1$ is plausible (not achieved yet) due to the large number of fluxes.
- Perturbative effects in LVS in better control as the volume is exponentially large. All computed so far harmless.
- Antibrane: nonlinearly realised SUSY (nilpotent superfield)
- Hierarchies:
$$E \ll M_{\text{KK}} = \frac{M_s}{\mathcal{V}^{1/6}} \ll M_s \equiv \frac{1}{\ell_s} \equiv \frac{1}{2\pi\sqrt{\alpha'}} = g_s^{1/4} \frac{M_p}{\sqrt{4\pi\mathcal{V}}}.$$

Inflation: Fibre+Blow-up



Adapted from
Kallosh, Linde
 α -attractors

Conclusions 2

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Challenges to KKLT, LVS,...

- Fluxes under full control only in SUSY 10D Sethi
- All SUSY breaking part is 4D EFT (with string inputs).
Trust EFT?
- Tuning $W_0 \ll 1$? in KKLT
- Higher correction in LVS?
- Antibranes (by hand, non susy, singularity?)
- T-branes in a control region? Bena et al.
- Antibranes and non-perturbative effects? Moritz et al.

String Cosmology

- Some inflationary EFTs describe CMB + other data very well.
- Inflation needs an UV completion.
- Some EFTs of string compactification can describe inflation
- Challenges: Moduli stabilisation and

$$M_{\text{planck}} > M_{\text{string}} > M_{\text{kk}} > M_{\text{inf}} \cdot$$