

Photon associated top-quark pair production

A study at NLO QCD with off-shell effects

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LoopFest 2018

Michigan State University

17. July 2018

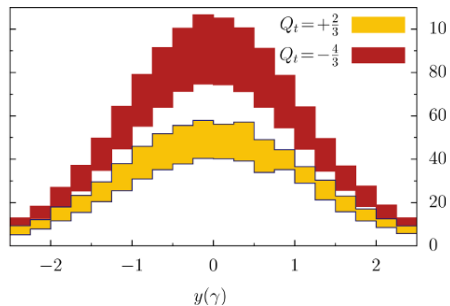
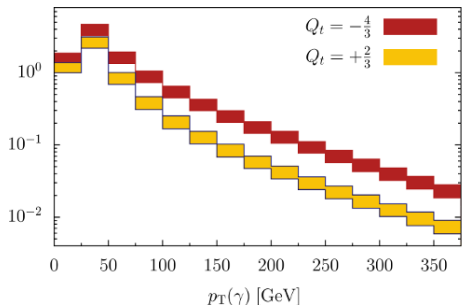


- Motivation
- Current status of $t\bar{t}\gamma$
- NWA vs. off-shell effects
- Results for $t\bar{t}\gamma$ in di-lepton channel
- Conclusions

Motivation for $t\bar{t}\gamma$

The study of (associated) $t\bar{t}$ production has a wide range of applications...

- SM benchmarks (e.g. $t\bar{t}$ cross section)
- precision measurements of SM parameters (e.g. m_t)
- probing Higgs-Yukawa sector (e.g. $t\bar{t}H$)
- constraining PDFs (especially gluon at large x)
- searches for BSM physics (e.g. heavy resonances decaying to tops)
- $t\bar{t}\gamma$ direct measurement of top charge $\sigma_{t\bar{t}\gamma} \sim Q_t^2$
- Indirect from $t\bar{t}$: $Q_t = Q_W - Q_{b\text{-jet}} = +\frac{2}{3}$



[Melnikov, Schulze, Scharf '11]

- Probe the structure of the $t\bar{t}\gamma$ vertex

$$\mathcal{L}_{t\bar{t}\gamma} = -eQ_t \bar{t}\gamma^\mu t A_\mu - e\bar{t} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (d_V^\gamma + id_A^\gamma \gamma_5) t A_\mu$$

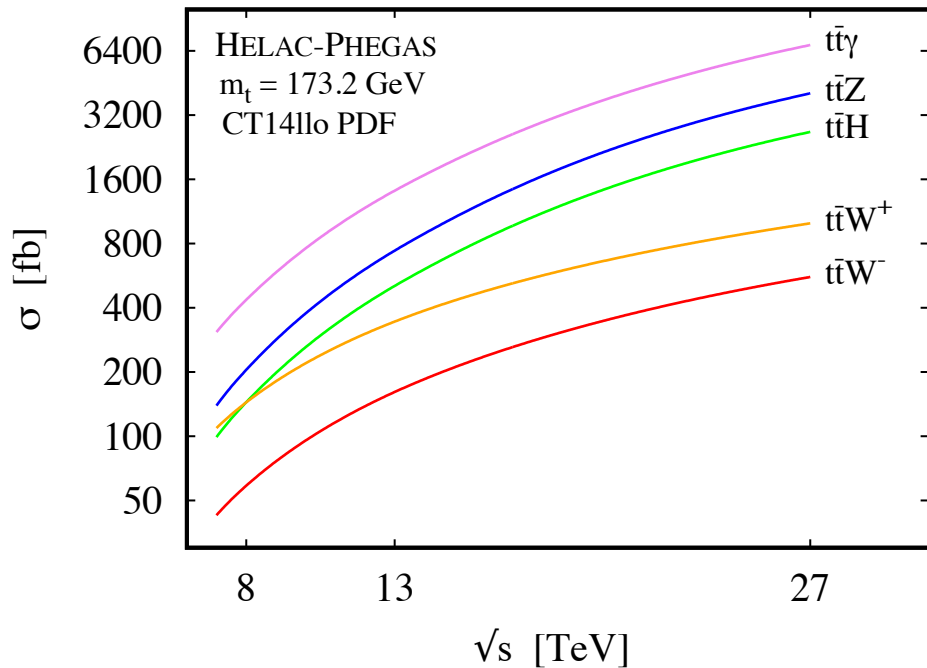
[Aguilar-Saavedra '09]

- Constraints on anomalous couplings
- Measure cross section ratio

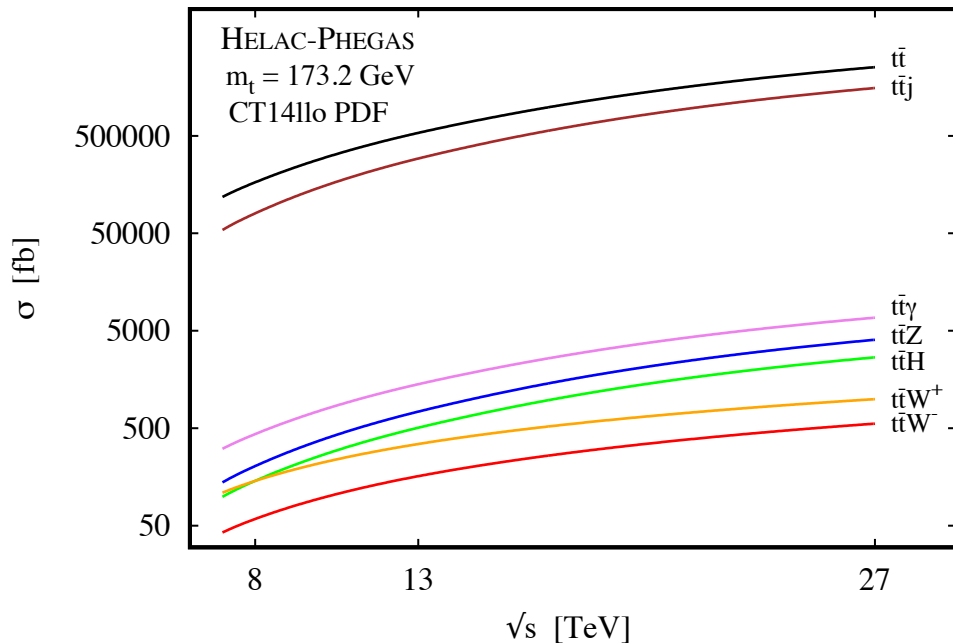
$$\mathcal{R} = \frac{\sigma_{pp \rightarrow t\bar{t}\gamma}}{\sigma_{pp \rightarrow t\bar{t}}} , \quad \frac{d\mathcal{R}}{dX} = \frac{d\sigma_{pp \rightarrow t\bar{t}\gamma}/dX}{d\sigma_{pp \rightarrow t\bar{t}}/dX}$$

- Various uncertainties cancel in ratio
- More stable with respect to radiative corrections
- Can probe new physics at the LHC

Motivation for $t\bar{t}\gamma$



Motivation for $t\bar{t}\gamma$



Experimental:

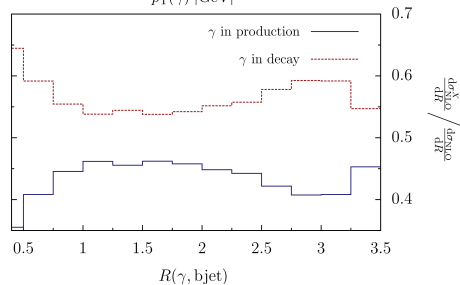
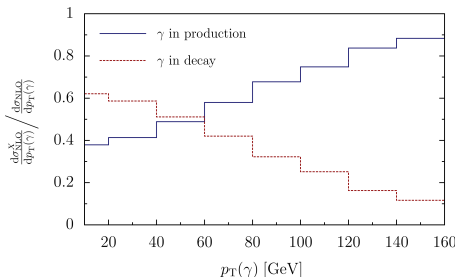
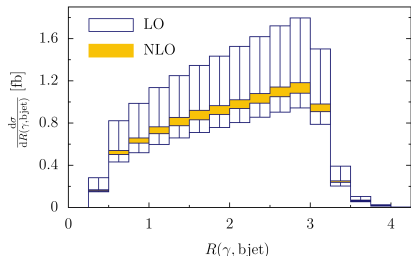
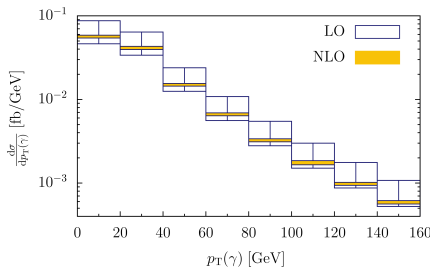
- First evidence: CDF @ TeVatron [CDF Collaboration '11]
- Observation: ATLAS @ LHC 7 TeV [ATLAS Collaboration '15]
- Measurements: LHC 8 TeV [ATLAS, CMS Collaboration '16]

on-shell tops: Corrections only to the production mechanism

- NLO QCD fixed-order
[Duan, Guo, Han, Ma, Wang, Zhang '09 '11]
[Maltoni, Pagani, Tsinikos '15]
- NLO EW fixed-order
[Duan, Guo, Han, Ma, Wang, Zhang '16]

Towards more realistic final states

- Powheg + Pythia → no spin correlations, top decay in PS
[Kardos, Trocsanyi '14]
- NLO QCD in NWA → spin correlated, radiative decays
[Melnikov, Schulze, Scharf '11]
- Full off-shell calculation in dilepton channel
[Bevilacqua, Hartanto, MK, Weber, Worek '18]



Large contribution from radiative top decays

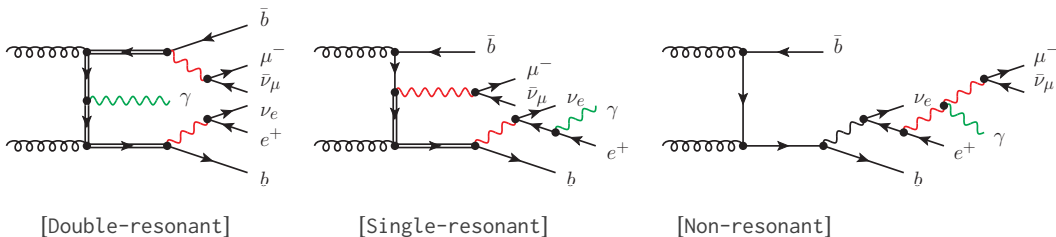
$$\sigma^{\text{NLO}} = 138.1\text{fb}$$

$$\sigma_{\gamma\text{-Prod.}}^{\text{NLO}} = 60.9\text{fb} ,$$

$$\sigma_{\gamma\text{-Dec.}}^{\text{NLO}} = 77.2\text{fb}$$

[Melnikov, Schulze, Scharf '11]

Quality of the NWA?



- NWA:

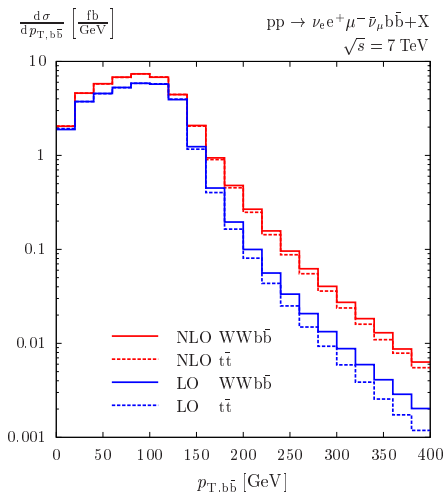
$$\frac{1}{(p^2 - m_t^2)^2 + m_t^2 \Gamma_t^2} \rightarrow \frac{\pi}{m_t \Gamma_t} \delta(p^2 - m_t^2) + \mathcal{O}\left(\frac{\Gamma_t}{m_t}\right)$$

- Keep diagrams with only two resonant top-quarks
- Sufficiently accurate for inclusive observables: $\Gamma_t/m_t \sim 0.8\%$
- Confirmed case-by-case:

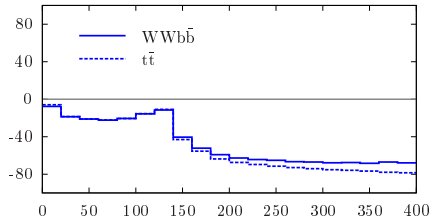
- $t\bar{t}$ (di-lepton) [Denner, Dittmaier, Kallweit, Pozzorini '11'12]
- $t\bar{t}$ (semi-lepton) [Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek '11]
- $t\bar{t}H$ (di-lepton) [Denner, Pellen '18]
- $t\bar{t}j$ (di-lepton) [Denner, Feger '18]
- $t\bar{t}\gamma$ (di-lepton) [Bevilacqua, Hartanto, MK, Worek '16'18]
- $t\bar{t}\gamma$ (di-lepton) [Bevilacqua, Hartanto, MK, Weber, Worek '18]

NWA vs. Off-shell effects in $t\bar{t}$

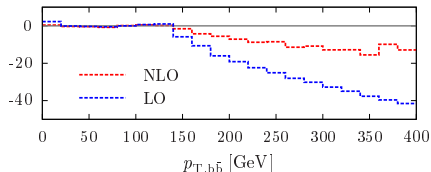
- Comparison: NWA @ NLO QCD vs. Full off-shell @ NLO QCD
- Large off-shell effects, where $t\bar{t}$ is suppressed as a signal
- Important as background to [Higgs and BSM searches](#)



LO/NLO - 1 [%]



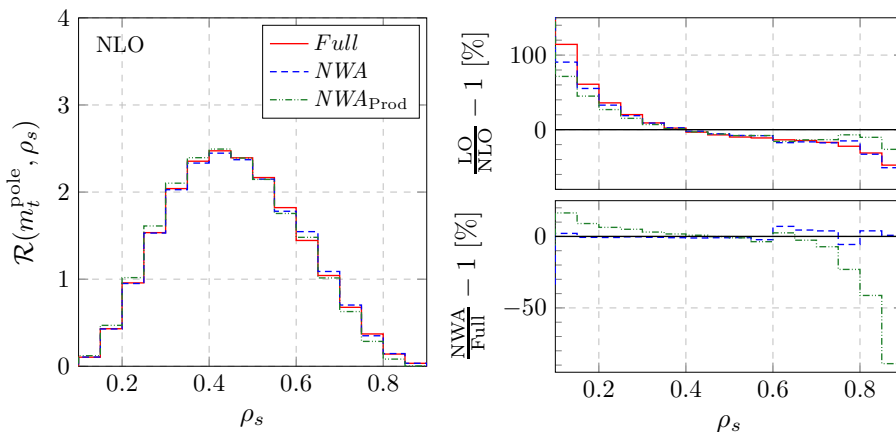
$t\bar{t}/WWb\bar{b} - 1$ [%]



[Denner, Dittmaier, Kallweit, Pozzorini, Schulze '12]

Can impact top-quark mass determination in $pp \rightarrow t\bar{t}j$

$$\mathcal{R}(m_t, \rho_s) = \frac{1}{\sigma_{t\bar{t}j}} \frac{d\sigma_{t\bar{t}j}}{d\rho_s}(m_t, \rho_s) \quad \rho_s = \frac{2m_0}{\sqrt{s_{t\bar{t}j}}}$$

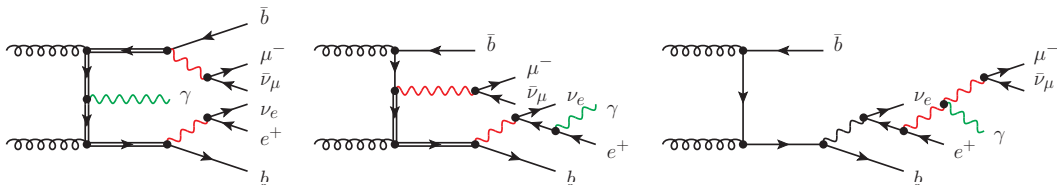


[Bevilacqua, Hartanto, MK, Worek, Schulze '18]

NWA vs. Off-shell effects in $t\bar{t}j$

Theory, NLO QCD CT14 PDF	$m_t^{out} \pm \delta m_t^{out}$ [GeV]	Averaged $\chi^2/\text{d.o.f.}$	Probability <i>p-value</i>	$m_t^{in} - m_t^{out}$ [GeV]
<i>31 bins</i>				
<i>Full</i> , $\mu_0 = H_T/2$	173.38 ± 1.34	1.04	0.40 (0.8 σ)	-0.18
<i>Full</i> , $\mu_0 = E_T/2$	172.84 ± 1.33	1.05	0.39 (0.9 σ)	+0.36
<i>Full</i> , $\mu_0 = m_t$	174.11 ± 1.39	1.07	0.37 (0.9 σ)	-0.91
<i>NWA</i> , $\mu_0 = m_t$	175.70 ± 0.96	1.17	0.24 (1.2 σ)	-2.50
<i>NWA_{Prod.}</i> , $\mu_0 = m_t$	169.93 ± 0.98	1.20	0.20 (1.3 σ)	+3.27
<i>5 bins</i>				
<i>Full</i> , $\mu_0 = H_T/2$	173.15 ± 1.32	0.93	0.44 (0.8 σ)	+0.05
<i>Full</i> , $\mu_0 = E_T/2$	172.55 ± 1.18	1.07	0.37 (0.9 σ)	+0.65
<i>Full</i> , $\mu_0 = m_t$	173.92 ± 1.38	1.48	0.20 (1.3 σ)	-0.72
<i>NWA</i> , $\mu_0 = m_t$	175.54 ± 0.97	1.38	0.24 (1.2 σ)	-2.34
<i>NWA_{Prod.}</i> , $\mu_0 = m_t$	169.37 ± 1.43	1.16	0.33 (1.0 σ)	+3.83

Full off-shell $t\bar{t}\gamma$ @ NLO

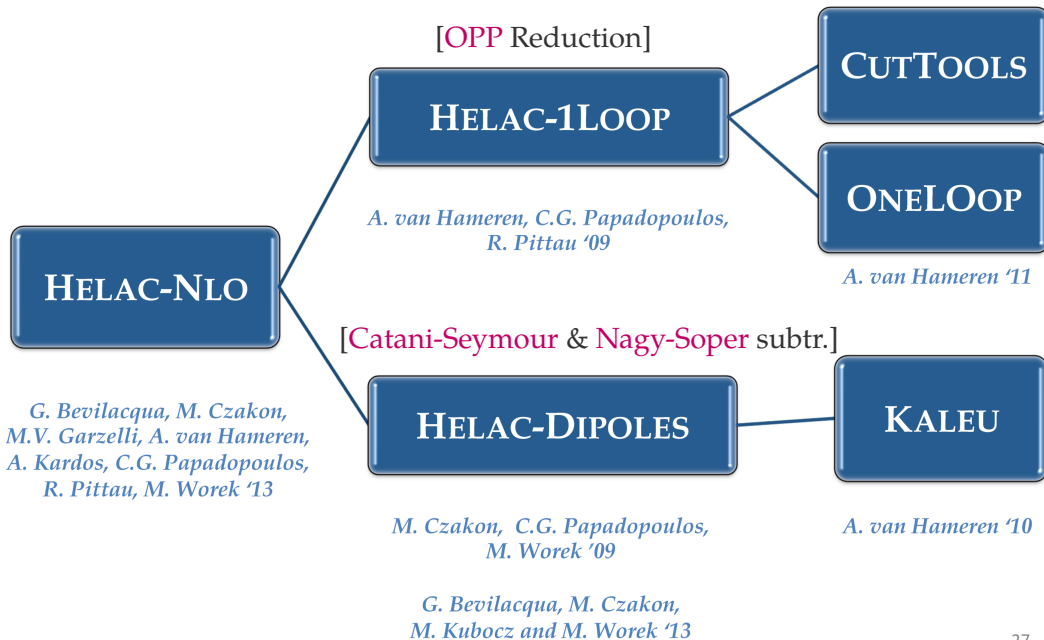


- 628 diagrams for gg channel for $t\bar{t}\gamma$ @ $\mathcal{O}(\alpha_s^2\alpha^5)$
- 36032 one-loop diagrams for gg channel for $t\bar{t}\gamma$ @ $\mathcal{O}(\alpha_s^3\alpha^5)$
 - includes up to 958 hexagons and 90 heptagons
 - scalar integrals with complex masses
 - NWA only up to pentagons!
- Number of subtraction terms for representative subprocesses

Subprocess	# Diags	# CS dipoles	# NS dipoles
$gg \rightarrow e^+v_e\mu^-\bar{v}_\mu b\bar{b}\gamma g$	4348	27	9
$qg \rightarrow e^+v_e\mu^-\bar{v}_\mu b\bar{b}\gamma q$	2344	15	5
$\bar{q}g \rightarrow e^+v_e\mu^-\bar{v}_\mu b\bar{b}\gamma \bar{q}$	2344	15	5
$q\bar{q} \rightarrow e^+v_e\mu^-\bar{v}_\mu b\bar{b}\gamma g$	2344	15	5

HELAC-NLO

*G. Ossola, C.G. Papadopoulos,
R. Pittau '08*



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- **NEW:** Ntuple generation + re-weighting for different $\mu_{R,F}$ and PDFs

Final state and parameters

- Fully leptonic decays: $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$
- Light quarks (also bottom) and leptons are massless \rightarrow **5 FS**
- Top quark mass and width: [Jesabek, Kühn, '99, Denner et al. '12]
 $m_t = 173.2 \text{ GeV}$ $\Gamma_t^{\text{LO}} = 1.47834 \text{ GeV}$ $\Gamma_t^{\text{NLO}} = 1.35146 \text{ GeV}$
- Complex Mass Scheme: $m_t^2 \rightarrow m_t^2 - im_t \Gamma_t$ [Denner et al. '99, '05]

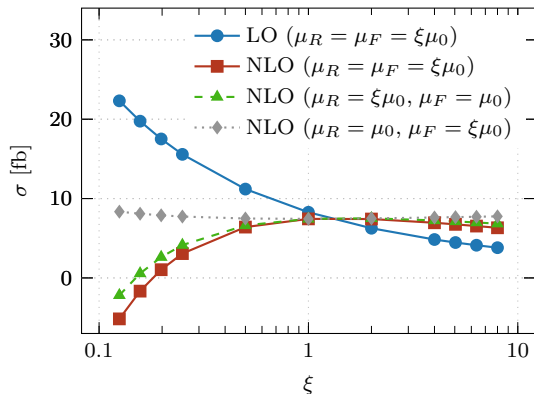
Kinematics

- exactly 2 b-jets, 1 photon, 2 charged leptons, missing p_T
- partons with $|\eta| < 5$, anti- k_T , $\Delta R = 0.4$
- cuts:

$$\begin{aligned}
 p_{T\ell} > 30 \text{ GeV}, & \quad p_{Tb} > 40 \text{ GeV}, & \quad \cancel{p}_T > 20 \text{ GeV}, & \quad p_{T,\gamma} > 25 \text{ GeV}, \\
 \Delta R_{bb} > 0.4, & \quad \Delta R_{\ell\ell} > 0.4, & \quad \Delta R_{\ell b} > 0.4, & \\
 |y_\ell| < 2.5, & \quad |y_b| < 2.5, & \quad |y_\gamma| < 2.5 &
 \end{aligned}$$

- Frixione isolation: $R_{\gamma i} = 0.4$ [Frixione '98]
- For hard photon: $\alpha = \alpha(0) = 1/137$

Inclusive cross section



$$\sigma_{pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X}^{\text{LO}} = 8.27^{+2.92 (+35\%)}_{-2.01 (-24\%)} \text{ fb}$$

$$\sigma_{pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X}^{\text{NLO}} = 7.44^{+0.07 (+1\%)}_{-1.03 (-14\%)} \text{ fb}$$

$$\frac{1}{2} < \mu_R / \mu_F < 2$$

- fixed scale: $\mu_0 = m_t/2$
- at LO: $gg \sim 79\%$, and $q\bar{q} \sim 21\%$
- Photon radiation dominated by final state radiation
- NLO corrections: -10%

[Bevilacqua, Hartanto, MK, Weber, Worek '18]

- Assuming same setup for LO and NLO

$$\mathcal{R} = \frac{\sigma_{t\bar{t}\gamma}^{\text{LO}}}{\sigma_{t\bar{t}}^{\text{LO}}} = (4.94 \pm 0.08) \cdot 10^{-3}$$

$$\mathcal{R} = \frac{\sigma_{t\bar{t}\gamma}^{\text{NLO}}}{\sigma_{t\bar{t}}^{\text{NLO}}} = (4.56 \pm 0.28) \cdot 10^{-3}$$

- uncertainties from scale dependence assuming correlation of the processes
- -8% NLO corrections
- $\pm 6\%$ scale uncertainties at NLO \rightarrow underestimated at LO
- Ratio more stable against radiative corrections
- Allows to probe new physics at the LHC

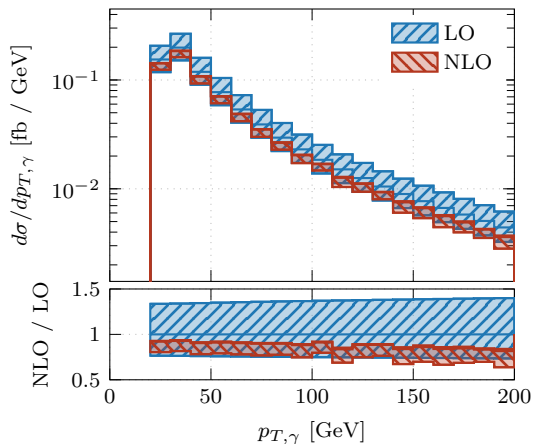
[Bevilacqua, Hartanto, MK, Weber, Worek '18]

Distributions

- Impact of corrections on differential distributions?
- Focus on BSM relevant observables
 $p_{T,\gamma}$ and $\Delta R(b_2, \gamma)$

[Baur, Buice, Orr '01]

[Baur, Juste, Orr, Rainwaite '04]



- $p_{T,\gamma}$
- Uncertainties: (μ_R, μ_F) envelopes
- K-factor: -8% to -18%
- Stable wrt radiative corrections
- Good candidate for BSM searches

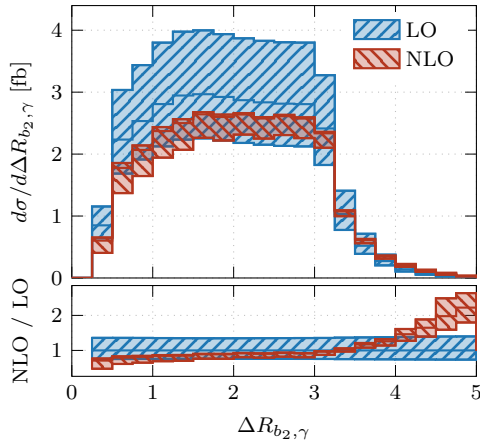
[Bevilacqua, Hartanto, MK, Weber, Worek '18]

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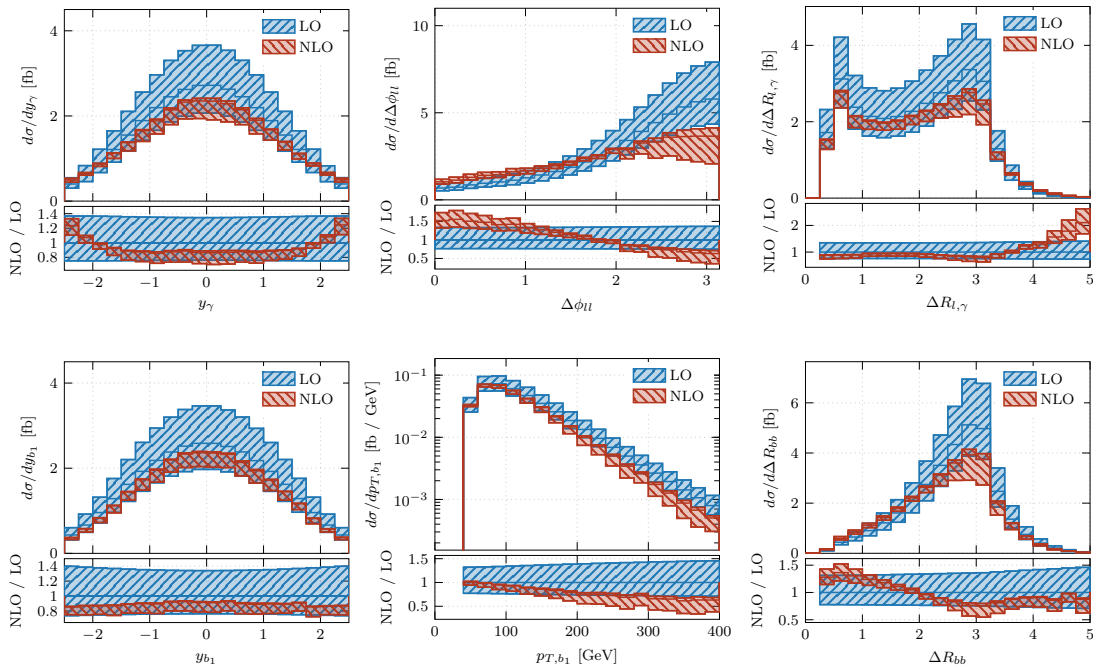
[Baur, Juste, Orr, Rainwaite '04]



- $\Delta R(b_2, \gamma)$
- Uncertainties: (μ_R, μ_F) envelopes
- K-factor: -29% to $+122\%$
- Shape distortion up to 150%
- Similar effect in other observables

[Bevilacqua, Hartanto, MK, Weber, Worek '18]

Distributions



Conclusions



Full calculation of $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma + X$ at NLO QCD

► arXiv:1803.09916

- NLO QCD corrections for $t\bar{t}\gamma$ with all resonant and non-resonant contributions completed
- Includes:
 - QCD corrections to production and radiative decays of tops
 - Photon radiation from tops and top decay products
 - Spin correlated top decays
 - off-shell effects
 - QCD corrections to non-resonant background processes

Outlook:

- Dynamical scales, PDF uncertainties
- Comparison with NWA approximation
- Anomalous top-quark couplings

$$\mathcal{L}_{t\bar{t}\gamma} = -eQ_t \bar{t}\gamma^\mu t A_\mu - e\bar{t} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (d_V^\gamma + id_A^\gamma \gamma_5) t A_\mu$$

- Relevant for BSM searches

$$\mathcal{R} = \frac{\sigma_{t\bar{t}\gamma}}{\sigma_{t\bar{t}}} , \quad \frac{d\mathcal{R}}{dX} = \frac{\sigma_{t\bar{t}\gamma}/dX}{\sigma_{t\bar{t}}/dX}$$