Can Baryon Stopping be understood within the String Model

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HELMHOLTZ RESEARCH FOR GRAND CHALLENGES





FIAS Frankfurt Institute for Advanced Studies

CRC-TR 21

Exploring the QCD Phase Diagram



Investigate regions with high µ_B to search for a phase transition and a critical point

Baryon Stopping

 \blacktriangleright Net proton number $N^{p-\bar{p}}$ to measure stopped protons from initial nuclei



C. Shen, B. Schenke, 10.1103/PhysRevC.97.024907

First nucleon-nucleon interactions play most important role

- Shape of $dN^{p-\bar{p}}/dy$ is strongly energy dependent
- $\sqrt{s_{NN}} \approx 5 \,\text{GeV}$: Baryons are stopped around mid rapidity
- ▶ $\sqrt{s_{NN}} > 60 \,\text{GeV}$: Nuclei pass through each other

Transport Model SMASH

- Hadronic degrees of freedom
- Geometric collision criterion:

$$d_{\rm trans} < \sqrt{\frac{\sigma_{\rm tot}}{\pi}}$$

- \blacktriangleright Established hadrons from PDG up to $m\approx 2\,{\rm GeV}$
- Effectively solving relativistic Boltzmann equation

J.Tindall et al. 10.1016/j.physletb.2017.04.080

 Inelastic processes via resonances, soft strings or Pythia directly, depending on energy





Gold-gold collision at $\sqrt{s_{NN}}=10~{\rm GeV}$ In SMASH

J.Weil et al. 10.1103/PhysRevC.94.054905

String Model

- Massless quarks with momentum p₁, p₂ and position x₁, x₂
- Motion according to:

 $H = |p_1| + |p_2| + \kappa |x_1 - x_2|$

- $\blacktriangleright~\kappa\approx 1~{\rm GeV/fm:}$ String tension
- New $q\bar{q}$ pairs are produced
- String fragments into hadrons
- Hadrons are formed around a constant proper time

B. Anderson et al. 10.1016/0370-1573(83)90080-7



Strings in SMASH

Hard processes:

- \blacktriangleright Dominate for high \sqrt{s}
- Pythia to excite and fragment strings
- Map colliding hadron species to nucleons and pions

Soft processes:

- \blacktriangleright Dominate at intermediate \sqrt{s}
- Excite strings and call Pythia only for fragmentation
- Includes single diffractive, double diffractive and non-diffractive subprocesses



System and Observables

- Reproduce experimental p+p data before investigating baryon stopping in larger systems
- Most important are dynamics of string fragments and initial protons
- Particle multiplicities
- Rapidity spectra
- $\langle p_T \rangle$ as function of x_F

$$x_F = \frac{p_z}{p_{z,\text{beam}}}$$



NA61 10.1140/epjc/s10052-017-5260-4

Which results are influenced by string parameters and how?

Fragmentation Function for Leading Baryons

- Fragmentation function for sampling light cone momentum fraction for each string fragment
- Use a different fragmentation function for leading baryons to increase longitudinal momentum of protons



- Old version: use Lund fragmentation function consistently
- ▶ New version: use Gaussian with $\mu = 1$ and $\sigma = 0.6$ for leading Baryons
- Slightly better agreement with data for longitudinal momentum

$$x_F = \frac{p_z}{p_{z,\text{beam}}}$$

Transverse Momentum



 Reasonable agreement for transverse momentum using only symmetric Lund fragmentation function

Proton Mean Transverse Mass



- Transverse momentum underestimated at mid rapidity as shown before
- Energy dependence looks reasonable

Overview p+p Rapidity Spectra



 Fragmentation function, strangeness suppression and diquark suppression tuned to data

Overview p+p mean p_T



 Transverse momentum transfer and transverse momentum production from string fragmentation tuned to data

Heavy Ion Collisions



- First calculation for heavy ions after tuning to p+p data
- Protons are stopped too much but less than in UrQMD
- Understand interaction of string fragments

Formation Times

- String fragments need time to form
- Formation times are distributed around constant proper time
- Calculate formation times from yoyo-formalism

$$\langle \tau_{\rm form} \rangle = \frac{\sqrt{2}m}{\kappa}$$



Effect of Formation Times

- Multiply formation time from yoyo-formalism with factor b_{form}
- Protons stopped more at mid rapidity for larger formation times
- Unexpected since larger formation times means less interactions
- Need to study time dependence of collision number and rapidity distribution



Cross Section Scaling Factors

- During formation time cross section is scaled down by factor f_σ
- \blacktriangleright By default use a Heavyside function in time for f_σ
- One can also have f_σ grow with a given power α in time

K. Gallmeister U. Mosel 10.1016/j.nuclphysa.2007.12.009



Results for Different Powers $\boldsymbol{\alpha}$



- Lines labeled $\alpha = 0$ use a step function
- Large impact on dN/dy when going to $\alpha = 0.5$
- Very short time after initial collision most important
- Steady increase of scaling factor dissolves bump at mid rapidity

Summary

- \blacktriangleright String model parameters tuned to p+p data at SPS energies
- ▶ p+p results agree with experimental data for produced hadrons
- Proton y or x_F improved but still needs investigation
- Calculation for heavy ion collisions show slightly too much stopping
- Insights on the role of formation times and cross section scaling factors for baryon stopping gained

Outlook

Experimental p+p and Pb+Pb proton rapidity spectra look similar
 Turn off all secondary collisions

Understand which kind of reactions are responsible for stopping

 More rigorous study of parameter dependencies in fragmentation functions to match p+p data

Investigate interplay of formation times and cross-section scaling factors

Backup: Formation Time Distribution



$$\langle \tau_{\rm form} \rangle = \frac{\sqrt{2}m}{\kappa}$$

Backup: Strangeness Suppression

> Pythia parameter to define the probability to produce an $s\bar{s}$ relative to $u\bar{u}$ or $d\bar{d}$



Non-strange hadrons are also slightly affected

 \blacktriangleright Strangeness suppression set to 0.12

Backup: Strangeness Suppression

Energy dependence of Kaon yields hard to reproduce for all species simultaneously



Strangeness suppression not energy dependent in SMASH

Backup: Diquark Suppression

- Pythia parameter to define probability to produce $qq\bar{q}\bar{q}$ relative to $q\bar{q}$
- Antiprotons sensitive to diquark suppression



Reasonable agreement with data for a value of 0.042

Backup: Transverse Momentum Transfer



- \blacktriangleright Varying the width σ_T in Gaussian to sample transverse momentum transfer
- Allowing more transverse momentum transfer increases $\langle p_T \rangle$
- Protons and other mesons not simultaneously reproducible

Backup: Fragmentation Function

Fragmentation function used in PYTHIA:





- Sample light cone momentum fraction z for each string fragment
- \blacktriangleright Is tuned to the shape of pion dN/dy

Backup: Soft String Processes in SMASH

Single diffractive: $A + B \rightarrow A + X$ or $A + B \rightarrow X + B$

- Two hadrons collide, exchange momentum and **one** of the hadrons is excited to a string
- Mass M_X of the string and transferred transverse momentum p_T are sampled according to:

$$rac{d^3N}{dM_X^2 d^2 \mathbf{p_T}} \propto rac{1}{M_X^2} \exp\left(-rac{p_T^2}{\sigma_T^2}
ight)$$

G. Ingelman and P. E. Schlein 10.1016/0370-2693(85)91181-5

Double diffractive: $A + B \rightarrow X + X$

- Two hadrons exchange a pomeron and are **both** excited to a string
- Light-cone momentum fraction x of gluons exchanging a pomeron is sampled from PDF:

PDF
$$\propto \frac{1}{x}(1-x)^{\beta+1}$$

Backup: Soft String Processes in SMASH Non-diffractive:

- > Two hadrons exchange a valence quark and are excited to strings
- ► Light cone momentum fraction of quarks sampled from PDF:

PDF
$$\propto x^{\alpha-1}(1-x)^{\beta-1}$$

Transverse momentum sampled from Gaussian

A.Capella et al. 10.1016/0370-2693(79)90718-4

Subprocess selection:

 \blacktriangleright From experimental σ_{tot} and σ_{el}

$$\sigma_{\rm inel} = \sigma_{\rm tot} - \sigma_{\rm el}$$

 \blacktriangleright With parametrization of $\sigma_{\rm SD}$ and $\sigma_{\rm DD}$ from Pythia

$$\sigma_{\rm ND} = \sigma_{\rm inel} - \sigma_{\rm SD} - \sigma_{\rm DD}$$

Backup: Fragmentation Function

 Symmetric Lund fragmentation function used in PYTHIA

$$f(z) = \frac{1}{z}(1-z)^a \exp\left(-b\frac{m_T^2}{z}\right)$$

 Fragmentation function for leading baryons

$$f_{\text{leading}}(z) \propto \exp\left(-\frac{(z-1.0)^2}{0.6^2}\right)$$

