



# Lepton flavor violation at CLIC

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based on

P. S. B. Dev, R. N. Mohapatra & YCZ, **PRL120**(2018)221804 [1711.08430]

P. S. B. Dev, R. N. Mohapatra & YCZ, 1803.11167

- Motivations of the LFV processes
- Beyond SM neutral scalar  $H$  at CLIC
  - ▶ On-shell production
  - ▶ Off-shell production
  - ▶ Prospects at CLIC
- Doubly-charged scalar  $H^{\pm\pm}$  at CLIC
  - ▶ On-shell production through the (LFV) Yukawa couplings
  - ▶ Off-shell production
  - ▶ Prospects at CLIC
- Conclusion

# Why lepton-flavor violation (LFV) at CLIC?

- “Smoking-gun” signal beyond the SM;
- Clean SM background at lepton colliders
- CLIC is the highest  $e^+e^-$  collider being planned, i.e. 3 TeV (in particular important for the doubly-charged scalars).

...Connection to neutrino mass generation (and other pheno)

- ▶ Beyond SM **neutral scalar  $H$**  from e.g. left-right model, sneutrino in RPV SUSY models;
- ▶ **Doubly-charged scalar  $H^{\pm\pm}$**  in type-II seesaw and its extensions like left-right model;
- ▶ Might also be connected to the heavy neutrino searches, effective 4-fermion interaction, or even DM pheno at CLIC.

Beyond SM neutral scalar  $H$  @ CLIC 3 TeV

# Well-motivated underlying models

- RPV SUSY: sneutrinos ( $\tilde{\nu}$ )

[Aulakh, Mohapatra '82; Hall, Suzuki '84; Ross, Valle '85; Barbier+ '04; Duggan, Evans, Hirschauer '13]

$$\mathcal{L}_{\text{RPV}} = \frac{1}{2} \lambda_{\alpha\beta\gamma} \hat{L}_{\alpha} \hat{L}_{\beta} \hat{E}_{\gamma}^c$$

- Left-right symmetric models: the  $SU(2)_R$ -breaking scalar  $H_3$

[Dev, Mohapatra, YCZ '16; '16; '17; Maiezza, Senjanović, Vasquez '16]

LFV couplings are generated at tree and/or loop level

- 2HDM: CP-even or odd (heavy) scalars from the 2nd doublet

[Branco+ '11; Crivellin, Heeck, Stoffer '15]

LFV couplings are induced from small deviation  
from the lepton-specific structure.

- Mirror models: singlet scalar connecting the SM leptons to heavy mirror leptons [Hung '06, '07; Bu, Liao, Liu '08; Chang, Chang, Nugroho+ '16; Hung, Le, Tran+ '17]

LFV couplings arise from the SM-heavy lepton mixing

# Beyond SM neutral Higgs & effective LFV couplings

- Model-independent effective LFV couplings of  $H$

$$\mathcal{L}_Y = h_{\alpha\beta} \bar{\ell}_{\alpha,L} H \ell_{\beta,R} + \text{H.c.}.$$

For simplicity, we assume  $h_{\alpha\beta}$  are real, symmetric,  $H$  is CP-even, hadrophobic and the mixing with the SM Higgs  $h$  is small.

*$H$  might originate from a isospin singlet, doublet or triplet, depending on specific underlying models.*

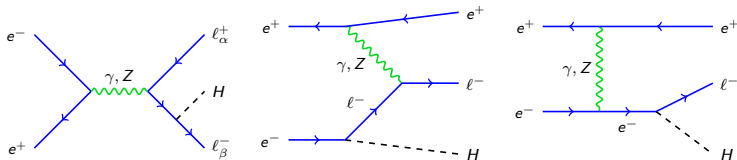
- Effective Dim-4 couplings  $\neq$  Effective 4-fermion couplings like  $\frac{1}{\Lambda^2}(\bar{e}e)(\bar{e}\mu)$   
[Kabachenko, Pirogov '97; Ferreira, Guedes, Santos '06; Aranda, Flores-Tlalpa, Ramirez-Zavaleta+ '09; Murakami, Tait '14; Cho, Shimo '14]

$$m_H < \sqrt{s} \Rightarrow \text{on-shell production}$$

# On-shell production of $H$ at lepton colliders

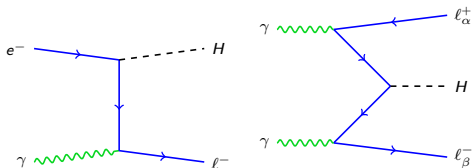
- the  $e^+e^-$  process

$$e^+e^- \rightarrow \ell_\alpha^\pm \ell_\beta^\mp + H$$



- involving the laser photon(s)

$$e^\pm \gamma \rightarrow \ell^\pm + H, \quad \gamma\gamma \rightarrow \ell_\alpha^\pm \ell_\beta^\mp + H$$

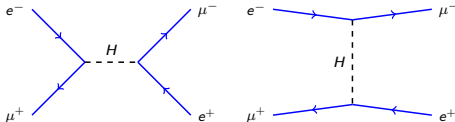


# Constraints on the LFV couplings: on-shell

On-shell production amplitudes depend *linearly* on the LFV couplings

- muonium anti-muonium oscillation:  $(\bar{\mu}e) \leftrightarrow (\mu\bar{e})$  ( $h_{e\mu}$ )

[Clark, Love '03]

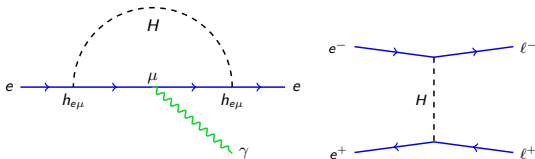


- Electron and muon  $g - 2$  ( $h_{el}, h_{\mu\ell}$ )

[Lindner, Platscher, Queiroz '16]

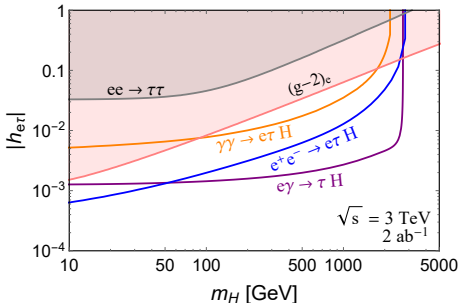
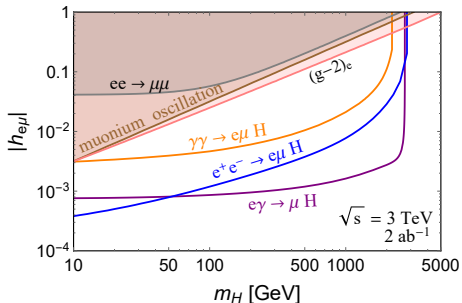
- Bhabha scattering, LEP  $ee \rightarrow \ell\ell$  data ( $h_{el}$ )

[OPAL '03; L3 '03; DELPHI '05]





# CLIC prospects of $H$ : on-shell production

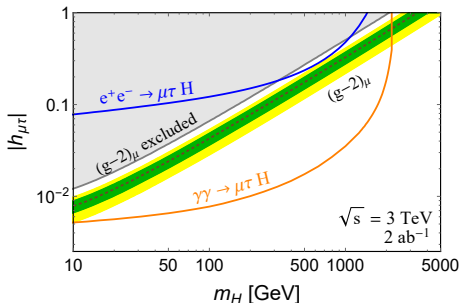


$\gamma\gamma$  ( $e\gamma$ ) channel: laser photon collision.

Shaded regions are excluded.

Assuming the dominant decay mode  $H \rightarrow e^\pm \mu^\mp$  (left),  $e^\pm \tau^\mp$  (right).

# CLIC prospects of $H$ : on-shell production



$\gamma\gamma$  ( $e\gamma$ ) channel: laser photon collision.

Shaded regions are excluded.

Assuming the dominant decay mode  $H \rightarrow \mu^\pm \tau^\mp$ .

Dotted brown line: central values of muon  $g-2$  anomaly,  
green and yellow bands: the  $1\sigma$  and  $2\sigma$  regions.

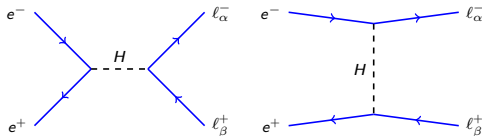
The muon  $g-2$  discrepancy can be directly tested at CLIC  
via the searches of  $\gamma\gamma \rightarrow \mu\tau + H$ .

# Off-shell production of $H$ at lepton colliders

- Off-shell production (at resonance when  $m_H \simeq \sqrt{s}$ )

might also be mediated by a (light) gauge boson  $Z'$  with LFV couplings [Heeck '16]

$$e^+ e^- \rightarrow \ell_\alpha^\pm \ell_\beta^\mp$$



# Constraints on the LFV couplings: off-shell

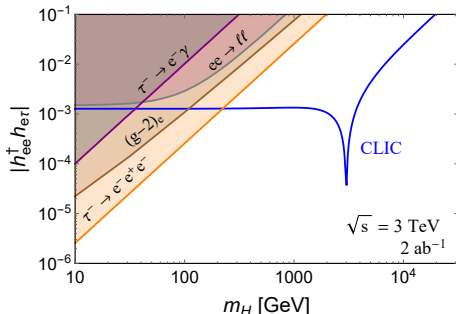
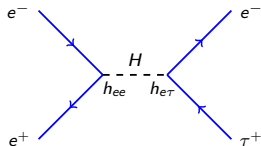
Off-shell production amplitudes depend *quadratically* on the LFV couplings

process	current data	constraints [ $\text{GeV}^{-2}$ ]
$\mu^- \rightarrow e^- e^+ e^-$	$< 10^{-12}$	$ h_{ee}^\dagger h_{e\mu} /m_H^2 < 6.6 \times 10^{-11}$
$\tau^- \rightarrow e^- e^+ e^-$	$< 2.7 \times 10^{-8}$	$ h_{ee}^\dagger h_{e\tau} /m_H^2 < 2.6 \times 10^{-8}$
$\tau^- \rightarrow \mu^- e^+ e^-$	$< 1.8 \times 10^{-8}$	$ h_{ee}^\dagger h_{\mu\tau} /m_H^2 < 1.5 \times 10^{-8}$
$\tau^- \rightarrow \mu^+ e^- e^-$	$< 1.5 \times 10^{-8}$	$ h_{e\mu}^\dagger h_{e\tau} /m_H^2 < 1.9 \times 10^{-8}$
$\tau^- \rightarrow e^- \gamma$	$< 3.3 \times 10^{-8}$	$ h_{ee}^\dagger h_{e\tau} /m_H^2 < 1.0 \times 10^{-6}$
$\tau^- \rightarrow \mu^- \gamma$	$< 4.4 \times 10^{-8}$	$ h_{e\mu}^\dagger h_{e\tau} /m_H^2 < 1.2 \times 10^{-6}$
$(g-2)_e$	$< 5.0 \times 10^{-13}$	$ h_{ee}^\dagger h_{e\tau} /m_H^2 < 1.1 \times 10^{-7}$
		$ h_{e\mu}^\dagger h_{e\tau} /m_H^2 < 1.0 \times 10^{-8}$
$ee \rightarrow ee, \tau\tau$	$\Lambda > 5.7 \text{ \& } 6.3 \text{ TeV}$	$ h_{ee}^\dagger h_{e\tau} /m_H^2 < 1.4 \times 10^{-7}$
$ee \rightarrow \mu\mu, \tau\tau$	$\Lambda > 5.7 \text{ \& } 7.9 \text{ TeV}$	$ h_{e\mu}^\dagger h_{e\tau} /m_H^2 < 1.3 \times 10^{-7}$

The  $\mu \rightarrow 3e$  limit is so strong that it leaves no hope to see any signal in the channel  $ee \rightarrow e\mu$  at CLIC.

# CLIC prospects of $H$ : off-shell production

$$e^+e^- \rightarrow e^\pm\tau^\mp$$



Resonance effect at  $m_H \simeq \sqrt{s}$  with width  $\Gamma_H = 30$  GeV

The off-shell scalar could be probed well beyond 10 TeV scale  
(or even up to 100 TeV).

# CLIC prospects of $H$ : off-shell production

$$e^+e^- \rightarrow \mu^\pm \tau^\mp$$

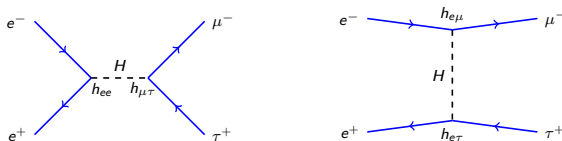
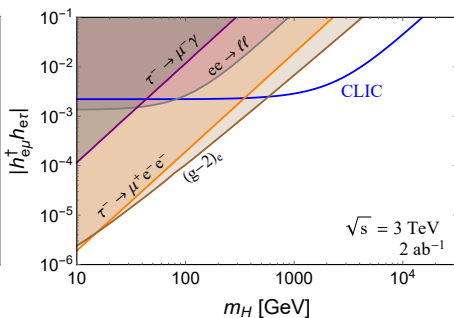
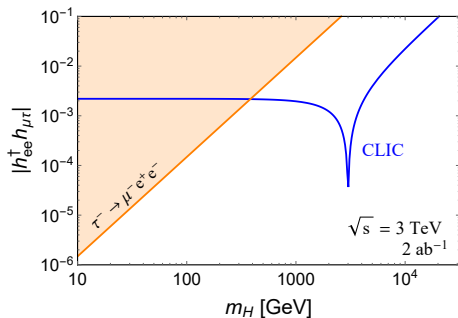


Figure: The  $s$  and  $t$  channels depend on different  $h^\dagger h$  couplings.



Doubly-charged scalar  $H^{\pm\pm}$  @ CLIC 3 TeV

# $H^{\pm\pm}$ at lepton (and hadron) colliders

- The (left- and right-handed)  $H^{\pm\pm}$  can be pair produced from the gauge interactions to the  $\gamma/Z$  bosons.
- The Drell-Yan production channels can not be used to measure *directly* the (LFV) Yukawa couplings  $f_{\alpha\beta}$  of  $H^{\pm\pm}$  to charged leptons, unless  $H^{\pm\pm}$  is long-lived.
- The current LHC same-sign dilepton limits depend largely on the branching fractions  $\text{BR}(H^{\pm\pm} \rightarrow \ell_{\alpha}^{\pm} \ell_{\beta}^{\pm})$ .

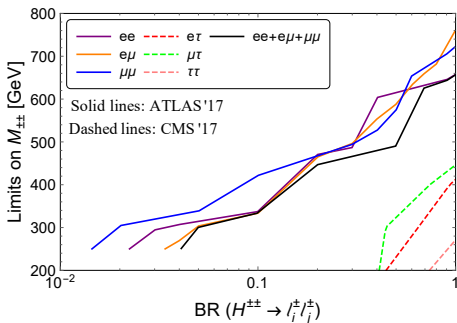


Figure: LHC dilepton limits on the right-handed  $H^{\pm\pm}$ .



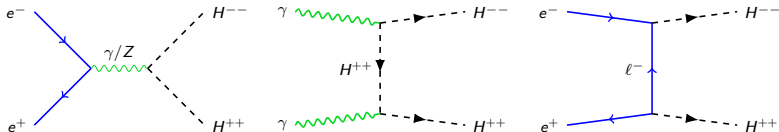
# On-shell Production of $H^{\pm\pm}$ at lepton colliders through the (LFV) Yukawa couplings $f_{\alpha\beta}$

Model-independent effective couplings of (right-handed)  $H^{\pm\pm}$

$$\mathcal{L}_Y = f_{\alpha\beta} H^{++} \overline{\ell}_\alpha^c \ell_\beta + \text{H.c.}$$

- Pair production through the gauge and Yukawa couplings

[Chakrabarti+, hep-ph/9804297]

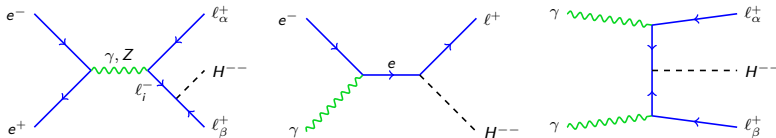


The Drell-Yan processes dominate the pair production if the Yukawa couplings  $f_{e\ell}$  are very small.

# On/off-shell production of $H^{\pm\pm}$ at lepton colliders

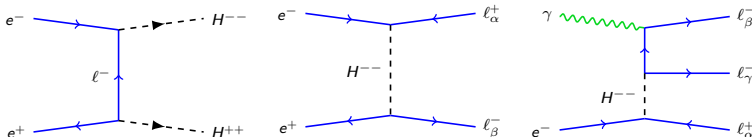
- Single production through the Yukawa couplings

[Kuze & Sirois, hep-ex/0211048; Barenboim, Huitu, Maalampi & Raidal, hep-ph/9611362; Lusignoli & Petrarca, PLB226, 397; Yue & Zhao, hep-ph/0701017; Godfrey, Kalyniak, Romanenko, hep-ph/0108258; hep-ph/0207240; Rizzo, PRD25, 1355; Yue, Zhao & Ma, 0706.0232]

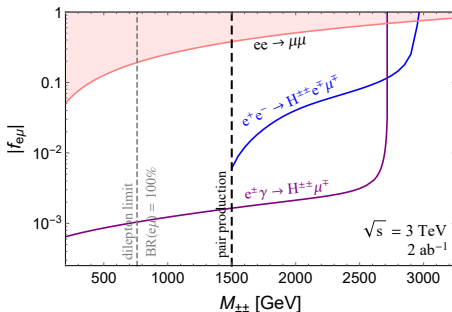


- Off-shell production

[Godfrey, Kalyniak, Romanenko, hep-ph/0108258; hep-ph/0207240; Rizzo, PRD25, 1355]



# CLIC prospects of $H^{\pm\pm}$ : single production



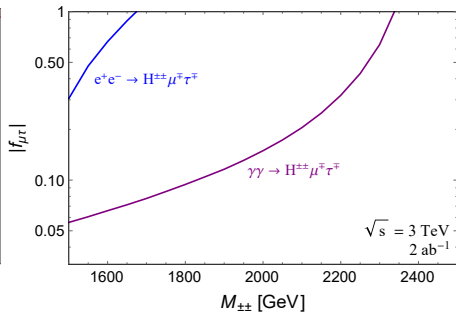
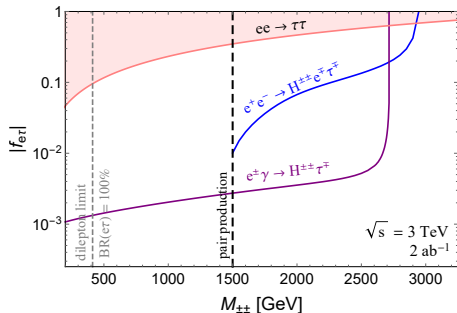
Assuming the dominant decay mode  $H^{\pm\pm} \rightarrow e^\pm \mu^\pm$ .

Below  $\sqrt{s}/2 = 1.5$  TeV, the process  $e^+e^- \rightarrow H^{\pm\pm} \ell_\alpha^\mp \ell_\beta^\mp$  is dominated by the Drell-Yan pair production  $e^+e^- \rightarrow H^{++}H^{--}$  with the subsequent decay  $H^{\mp\mp} \rightarrow \ell_\alpha^\mp \ell_\beta^\mp$ .

The  $\gamma\gamma \rightarrow H^{\pm\pm} \ell_\alpha^\mp \ell_\beta^\mp$  sensitivity is weaker than the  $e^+e^-$  process.

The electron and muon  $g-2$  limits are highly suppressed by the charge lepton masses and are not shown in the plot.

# CLIC prospects of $H^{\pm\pm}$ : single production



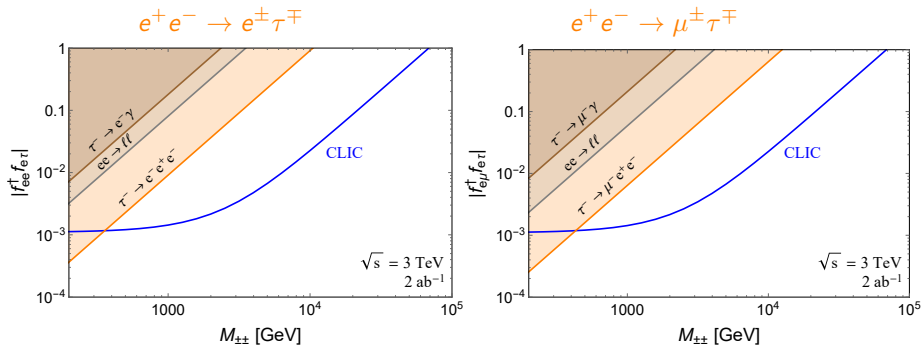
Assuming the dominant decay mode  $H^{\pm\pm} \rightarrow e^{\pm} \tau^{\pm}$  (left),  $\mu^{\pm} \tau^{\pm}$  (right).

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The  $\gamma\gamma \rightarrow H^{\pm\pm} \ell_{\alpha}^{\mp} \ell_{\beta}^{\mp}$  sensitivity is weaker than the  $e^+e^-$  process.

The electron and muon  $g - 2$  limits are highly suppressed by the charge lepton masses and are not shown in the plots.

# CLIC prospects of $H^{\pm\pm}$ : off-shell production



Suppressed by the three-body phase space, the sensitivities in the  $e\gamma$  processes are comparatively much weaker.

As in the neutral scalar case, the limit from  $\mu \rightarrow eee$  are so stringent that it has precluded the  $H^{\pm\pm}$ -mediated signal  $ee \rightarrow e\mu$  at CLIC.

The effective cutoff scale  $\Lambda \simeq M_{\pm\pm}/|f|$  can be probed at CLIC up to few 10 TeV.

# Conclusion

- A large variety of well-motivated models accommodate a beyond SM neutral scalar  $H$  and/or doubly-charged scalar  $H^{\pm\pm}$ , with LFV couplings to the SM charged leptons.
- These LFV couplings can be studied in a *model-independent* way at future lepton colliders like CLIC, which strengthens the physics case for future lepton colliders.
- The neutral scalar  $H$  can be produced on-shell via  $e^{\pm}\gamma \rightarrow \ell^{\pm} + H$  and  $e^{+}e^{-}, \gamma\gamma \rightarrow \ell_{\alpha}^{\pm}\ell_{\beta}^{\mp} + H$  or off-shell via  $e^{+}e^{-} \rightarrow \ell_{\alpha}^{\pm}\ell_{\beta}^{\mp}$ .
- The doubly-charged scalar  $H^{\pm\pm}$  can be (doubly & singly) on-shell and off-shell produced from the (LFV) Yukawa couplings to the charged leptons.
- It is promising that CLIC could probe a broad region of mass and coupling parameters for both  $H$  and  $H^{\pm\pm}$ , which go well beyond the existing low-energy LFV constraints like  $\tau \rightarrow eee$ .
- The neutral scalar explanation of the muon  $g - 2$  anomaly can be directly tested at CLIC in the  $\gamma\gamma \rightarrow \mu^{\pm}\tau^{\mp} + H$  process.

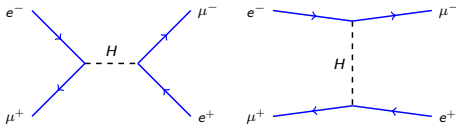
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# Constraints on the LFV couplings $h_{\alpha\beta}$

On-shell production amplitudes depend *linearly* on the LFV couplings

- muonium anti-muonium oscillation:  $(\bar{\mu}e) \leftrightarrow (\mu\bar{e})$  ( $h_{e\mu}$ )



Oscillation probability [Clark, Love '03]

$$\mathcal{P} = \frac{2(\Delta M)^2}{\Gamma_\mu^2 + 4(\Delta M)^2}$$

with the  $H$ -induced mass splitting

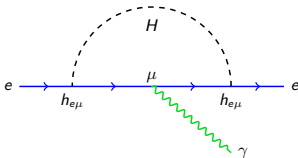
$$\Delta M = \frac{2\alpha_{\text{EM}}^3 h_{e\mu}^2 \mu^3}{\pi m_H^2}, \quad \mu = \frac{m_e m_\mu}{m_e + m_\mu}$$



# Constraints on the LFV couplings $h_{\alpha\beta}$

- Electron and muon  $g - 2$  ( $h_{e\ell}, h_{\mu\ell}$ )

[Lindner, Platscher, Queiroz '16]



$$\Delta a_e \simeq \frac{h_{e\mu}^2 m_e m_\mu}{16\pi^2 m_H^2} \left[ 2 \log \left( \frac{m_H^2}{m_\mu^2} \right) - 3 \right].$$

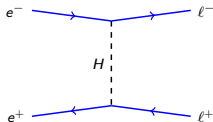
The value of  $h_{e\mu}$  to explain  $(g - 2)_\mu$  discrepancy is excluded by the  $(g - 2)_e$  constraint.

$$\Delta a_\mu \equiv \Delta a_\mu^{\text{exp}} - \Delta a_\mu^{\text{th}} = (2.87 \pm 0.80) \times 10^{-9}$$

# Constraints on the LFV couplings $h_{\alpha\beta}$

- Bhabha scattering, LEP  $ee \rightarrow \ell\ell$  data ( $h_{e\ell}$ )

[OPAL '03; L3 '03; DELPHI '05]



Effective 4-fermion interaction

$$\frac{h_{e\ell}^2}{m_H^2} (\bar{e}\ell)(\bar{e}\ell) \xrightarrow{\text{Fierz transf.}} \frac{1}{\Lambda^2} (\bar{e}\gamma_\mu e)(\bar{\ell}\gamma^\mu \ell)$$

If  $m_H \lesssim \sqrt{s}$ , the LEP limits on the cut-off scale  $\Lambda$  do not apply, and we have to consider the kinetic dependence

$$\frac{1}{m_H^2} \rightarrow \frac{1}{q^2 - m_H^2} \simeq \frac{1}{-s \cos \theta/2 - m_H^2}$$

# Constraints on the LFV couplings $h_{\alpha\beta}$

Off-shell production amplitudes depend *quadratically* on the LFV couplings

- 3-body LFV decays of muon and tauon, e.g. [Sher, Yuan '91]

$$\Gamma(\tau^- \rightarrow e^+ e^- e^-) \simeq \frac{1}{\delta} \frac{|h_{ee}^\dagger h_{e\tau}|^2 m_\tau^5}{3072 \pi^3 m_H^4}, \quad (\delta = 2)$$

- 2-body LFV decays of muon and tauon, e.g. [Harnik, Kopp, Zupan '12]

$$\Gamma(\tau \rightarrow e \gamma) = \frac{\alpha_{\text{EM}} m_\tau^5}{64 \pi^4} (|c_L|^2 + |c_R|^2), \quad c_L = c_R \simeq \frac{h_{ee}^\dagger h_{e\tau}}{24 m_H^2}.$$

- $h_{ee, e\mu, e\tau}$  contribute to  $(g-2)_e$  & LEP  $ee \rightarrow \ell\ell$  data,  
[DELPHI '05; Hou, Wong '95]

$$|h_{ee}^\dagger h_{e\tau}| \Rightarrow ee \rightarrow e\tau$$

$$|h_{e\mu}^\dagger h_{e\tau}| \Rightarrow ee \rightarrow \mu\tau \text{ (} t\text{-channel)}$$

# SM backgrounds for on-shell production of $H$

Main SM backgrounds are particle misidentification for

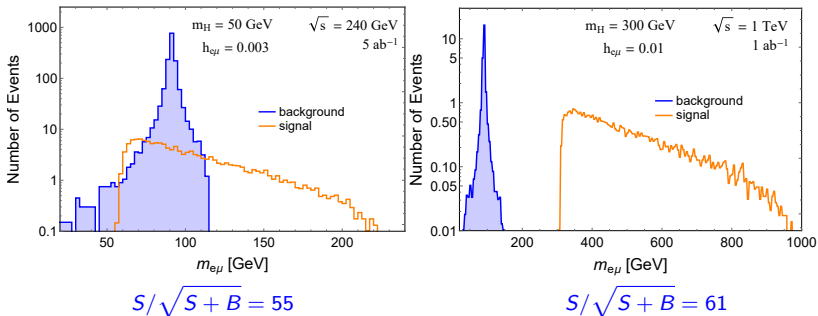
$$e^+e^- \rightarrow \ell_\alpha^+ \ell_\beta^- + X, \quad (\alpha \neq \beta)$$

The mis-identification rate is expected to be small, of order  $10^{-3}$

[Milstene, Fisk, Para '06; Hammad, Khalil, Un '16; Yu, Ruan, Boudry+ '17]

Example:

$$e^+e^- \rightarrow Zh \rightarrow (e^+e^-/\mu^+\mu^-)h \rightsquigarrow e^\pm \mu^\mp + h$$



# SM backgrounds for off-shell production of $H$

Main SM backgrounds:

$$e^+e^- \rightarrow W^+W^- \rightarrow \ell_\alpha^+ \ell_\beta^- \nu \bar{\nu}$$

The backgrounds can be well controlled by

[Kabachenko, Pirogov '97; Cho, Shimo '16; Bian, Shu, YCZ '15]

requiring that the constructed energy  $E_\ell \simeq \sqrt{s}/2$ ,  
kinetic distribution analysis of the backgrounds and signals