

Global probes for the top-quark EFT

Gauthier Durieux
(DESY)

Global and optimal probes for the top-quark EFT at future lepton colliders
GD, Martín Perelló, Marcel Vos (Valencia), Cen Zhang (IHEP), [1807.02121],

Top-quark physics at the CLIC electron-positron linear collider
CLICdp, [1807.02441],

The top-quark window on compositeness at future lepton colliders
GD, Oleksii Matsedonskyi (DESY), [1807.10273],

Top-quark FCNC production,
in *The CLIC physics potential*, [to appear].



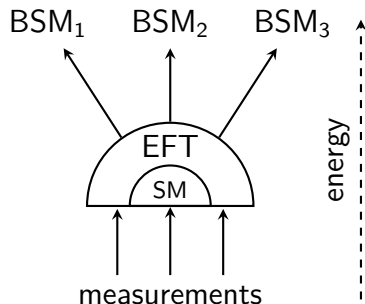
1. The top-quark EFT
2. Top-quark pair production
3. Composite Higgs interpretation
4. Top-quark FCNC production

The standard model effective field theory

systematically parametrizes the theory space
in direct vicinity of the SM

- ▶ based on SM fields and symmetries
- ▶ in a low-energy limit
- ▶ systematic (and renormalizable) when global

(...) if one writes down the most general possible Lagrangian, including all terms consistent with assumed symmetry principles, (...) the result will simply be the most general possible S-matrix consistent with analyticity, perturbative unitarity, cluster decomposition and the assumed symmetry. [Phenomenological Lagrangians, Weinberg '79]



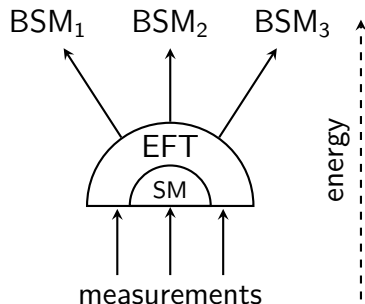
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Identify new physics through correlated deviations
in precisely measured observables.

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Make reasonable assumptions

- focus a priori on processes and operators involving top quarks
- determine which contributions are relevant
- prioritize the study of flavour structures

Fix notation

- define d.o.f. natural for top physics at the LHC
- fix notation, normalization, and indicative allowed ranges
- provide simulation tools as TH/EXP interface

Discuss analysis strategies (one example)

- address the challenges of a global EFT
- highlight useful experimental outputs

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Fix notation

- define d.o.f. naturally
- fix notation for the LHC
- provide indicative allowed ranges
- discuss as TH/EXP interface

**Quote your results in these standards
for comparison and combination with others!**

Discuss analysis strategies (one example)

- address the challenges of a global EFT
- highlight useful experimental outputs

Statistically optimal observables
&
global determinant parameter

Statistically optimal observables

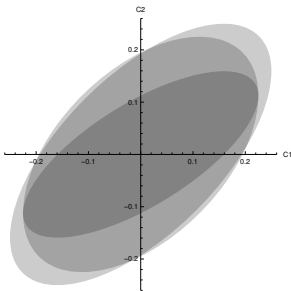
minimize the one-sigma ellipsoid in EFT parameter space

(joint efficient set of estimators, saturating the Cramér-Rao bound: $V^{-1} = I$, like MEM)

For small C_i , with a phase-space distribution $\sigma(\Phi) = \sigma_0(\Phi) + \sum_i C_i \sigma_i(\Phi)$,
the stat. opt. obs. are the average values of $O_i(\Phi) = \sigma_i(\Phi)/\sigma_0(\Phi)$.

The associated covariance at $C_i = 0, \forall i$ is

$$\text{cov}(C_i, C_j)^{-1} = \epsilon \mathcal{L} \int d\Phi \frac{\sigma_i(\Phi) \sigma_j(\Phi)}{\sigma_0(\Phi)}.$$



e.g. $\sigma(\phi) = 1 + \cos(\phi) + C_1 \sin(\phi) + C_2 \sin(2\phi)$

1. asymmetries: $O_i \sim \text{sign}\{\sin(i\phi)\}$

2. moments: $O_i \sim \sin(i\phi)$

3. statistically optimal: $O_i \sim \frac{\sin(i\phi)}{1 + \cos\phi}$

\Rightarrow area ratios 1.9 : 1.7 : 1

Previous applications in $e^+e^- \rightarrow t\bar{t}$, on different distributions:

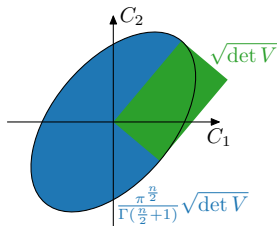
Global determinant parameter

[GD, Grojean, Gu, Wang, '17]

In a n -dimensional Gaussian fit,
with covariance matrix V ,

$$\text{GDP} \equiv \sqrt[n]{\det V}$$

provides a geometric average
of the constraints strengths.



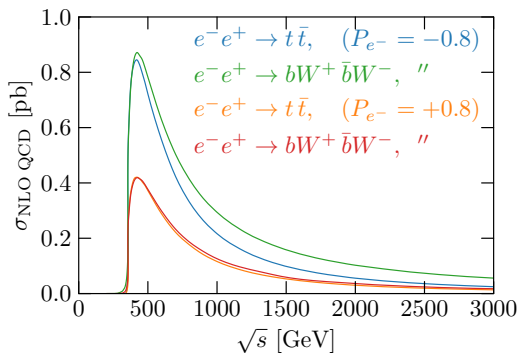
Interestingly, GDP ratios are operator-basis independent!

- as the volume scales linearly with coefficient normalization
- as the volume is invariant under rotations

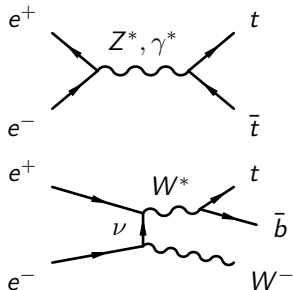
\implies conveniently assess constraint strengthening.

2. Top-quark pair production

$$e^+e^- \rightarrow bW^+ \bar{b}W^-$$



- σ peaked at about 380 GeV
- enhanced for a left-handed beam
- fall-off as $1/s$
- single-top contribution increasingly important



$$+ W^+W^- \rightarrow t\bar{t}$$

catching up at multi-TeV
 w/ unitarity breaking effects
 [Grojean, Wulzer, You, Zhang]

Up-sector SMEFT

[Grzadkowski et al '10]

Two-quark operators:

$$\mathcal{L}_{\text{EFT}} = \sum_i \frac{C_i}{\Lambda^2} O_i$$

Scalar: $O_{u\varphi} \equiv \bar{q} u \tilde{\varphi} \varphi^\dagger \varphi,$

Vector: $O_{\varphi q}^1 \equiv \bar{q} \gamma^\mu q \varphi^\dagger \overleftrightarrow{D}_\mu \varphi \equiv O_{\varphi q}^+ + O_{\varphi q}^V - O_{\varphi q}^A,$

$O_{\varphi q}^3 \equiv \bar{q} \gamma^\mu \tau^I q \varphi^\dagger \overleftrightarrow{D}_\mu^I \varphi \equiv O_{\varphi q}^+ - O_{\varphi q}^V + O_{\varphi q}^A$ (CC also)

$O_{\varphi u} \equiv \bar{u} \gamma^\mu u \varphi^\dagger \overleftrightarrow{D}_\mu \varphi \equiv O_{\varphi q}^V + O_{\varphi q}^A$

$O_{\varphi ud} \equiv \bar{u} \gamma^\mu d \tilde{\varphi}^\dagger \overleftrightarrow{D}_\mu \varphi,$ (CC only, m_b int.)

Tensor: $O_{uB} \equiv \bar{q} \sigma^{\mu\nu} u \tilde{\varphi} g_Y B_{\mu\nu}, \equiv O_{uA} - \tan \theta_W O_{uZ}$

$O_{uW} \equiv \bar{q} \sigma^{\mu\nu} \tau^I u \tilde{\varphi} g_W W_{\mu\nu}^I, \equiv O_{uA} + \cotan \theta_W O_{uZ}$ (CC also)

$O_{dW} \equiv \bar{q} \sigma^{\mu\nu} \tau^I d \tilde{\varphi} g_W W_{\mu\nu}^I,$ (CC only, m_b int.)

$O_{uG} \equiv \bar{q} \sigma^{\mu\nu} T^A u \tilde{\varphi} g_s G_{\mu\nu}^A.$ (NLO only)

Two-quark–two-lepton operators:

Scalar: $O_{1equ}^S \equiv \bar{l} e \varepsilon \bar{q} u,$ (CC also, m_e int.)

$O_{1edq} \equiv \bar{l} e \bar{d} q,$ (CC only, m_e int.)

Vector: $O_{1q}^1 \equiv \bar{l} \gamma_\mu l \bar{q} \gamma^\mu q \equiv O_{1q}^+ + O_{1q}^V - O_{1q}^A,$

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$O_{1u} \equiv \bar{l} \gamma_\mu l \bar{u} \gamma^\mu u \equiv O_{1q}^V + O_{1q}^A,$

$O_{eq} \equiv \bar{e} \gamma^\mu e \bar{q} \gamma_\mu q \equiv O_{eq}^V - O_{eq}^A,$

$O_{eu} \equiv \bar{e} \gamma_\mu e \bar{u} \gamma^\mu u \equiv O_{eq}^V + O_{eq}^A,$

Tensor: $O_{1equ}^T \equiv \bar{l} \sigma_{\mu\nu} e \varepsilon \bar{q} \sigma^{\mu\nu} u.$ (CC also, m_e int.)

Up-sector SMEFT

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Two-quark

Scalar

Vector

Tensor:

$O_{1eq}^T \equiv \bar{l}\sigma_{\mu\nu} e \varepsilon \bar{q}\sigma^{\mu\nu} u.$ (CC also, m_e int.)

8+2 CPV d.o.f.'s can be probed linearly
in $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+ \bar{b}W^-$
at LO and in the $m_b/m_t \rightarrow 0$ limit.

Anomalous vertices

$$\begin{aligned}
 t\bar{t}\gamma : & \quad \gamma_\mu \overbrace{(F_{1V}^\gamma + \gamma_5 F_{1A}^\gamma)}^{\sim \phi} + \frac{\sigma_{\mu\nu} i q^\nu}{2m_t} \overbrace{(F_{2V}^\gamma + i\gamma_5 F_{2A}^\gamma)}^{\sim \text{Re,Im}\{C_{uA}\}} \\
 t\bar{t}Z : & \quad \gamma_\mu \overbrace{(F_{1V}^Z + \gamma_5 F_{1A}^Z)}^{\sim C_{\varphi q}^V, C_{\varphi q}^A} + \frac{\sigma_{\mu\nu} i q^\nu}{2m_t} \overbrace{(F_{2V}^Z + i\gamma_5 F_{2A}^Z)}^{\sim \text{Re,Im}\{C_{uZ}\}} \\
 t\bar{t}W : & \quad \gamma_\mu \overbrace{(F_{1V}^W + \gamma_5 F_{1A}^W)}^{\sim C_{\varphi q}^+ - \frac{1}{2}(C_{\varphi q}^V - C_{\varphi q}^A) \pm C_{\varphi ud}} + \frac{\sigma_{\mu\nu} i q^\nu}{2m_t} \overbrace{(F_{2V}^W + i\gamma_5 F_{2A}^W)}^{\sim s_W^2 C_{uA} + s_W c_W C_{uZ} \pm C_{dW}^*}
 \end{aligned}$$

Insufficiencies:

- miss four-fermion operators,
- conflict with gauge invariance,
do not allow for radiative corrections to be computed,
- complex couplings where the tree-level EFT prescribes real ones,
- hide correlations induced by gauge invariance,
preclude the combination of measurements in various sectors

CLIC prospects

resonant $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+ \bar{b}W^-$

$m_b/m_t \rightarrow 0$, analytical LO observable def.

effective stat. efficiencies determined with full sim.

in semi-leptonic final state

500 fb^{-1} at $\sqrt{s} = 380 \text{ GeV}$

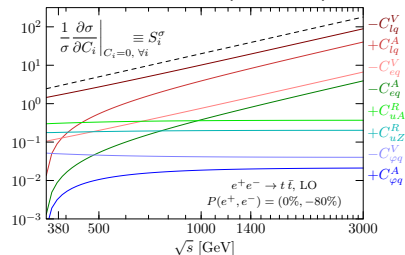
1.5 ab^{-1} at $\sqrt{s} = 1.4 \text{ TeV}$

3 ab^{-1} at $\sqrt{s} = 3 \text{ TeV}$

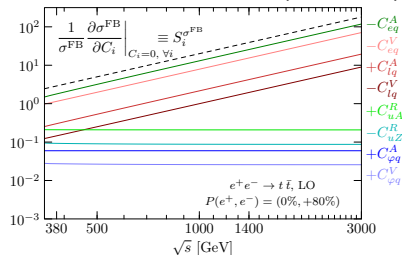
$P(e^+, e^-) = (0\%, \mp 80\%)$

Sensitivities

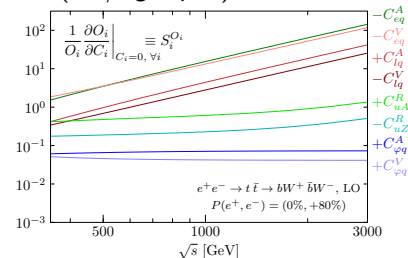
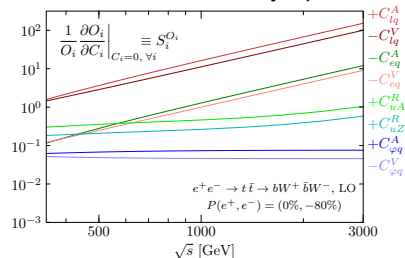
Total cross section (left pol.):



FB-integrated cross section (right pol.):



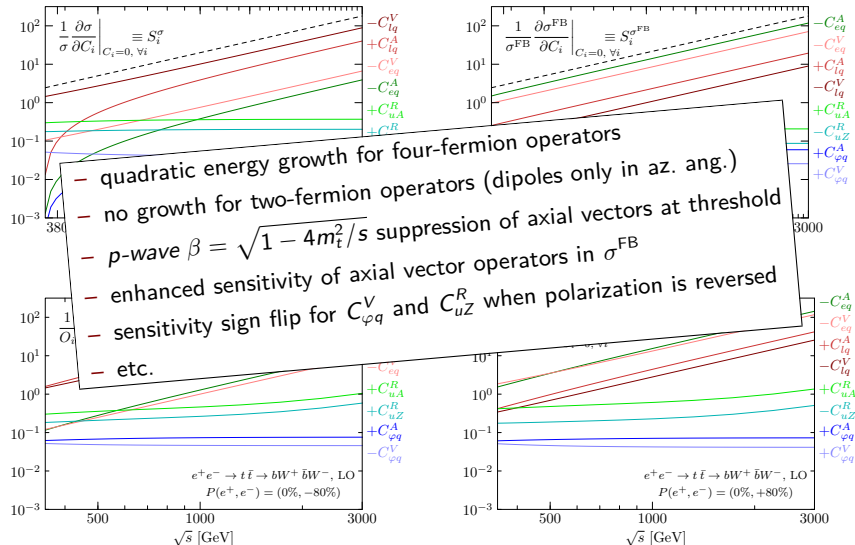
Statistically optimal observable (left/right pol.)



Sensitivities

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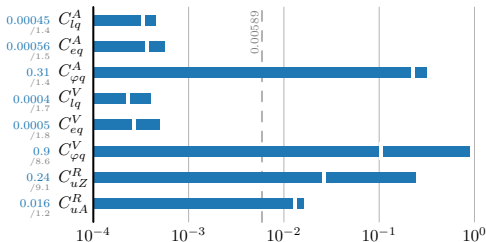
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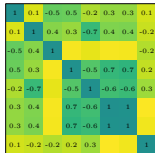
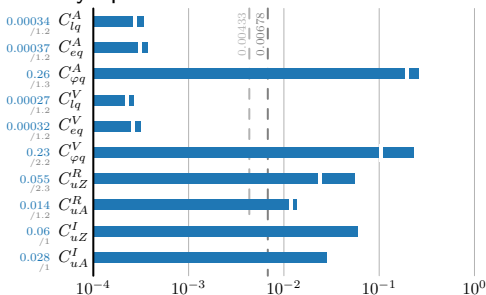
Global sensitivities

- in TeV^{-2} , $\Delta\chi^2 = 1$
- white marks: individual constraints
- dashed vertical lines: GDPs
- gray numbers: global/individual ratios

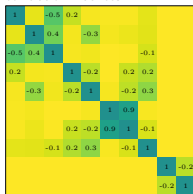
$\sigma + A^{\text{FB}}$:



Statistically optimal observables:



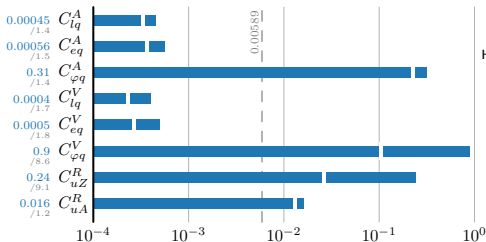
correlation matrices



factor of 1.6 improvement
of the 8-coefficient GDP
with linear coefficient
dependence only

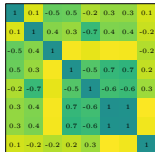
Global sensitivities

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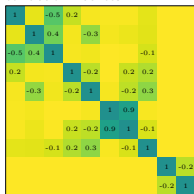


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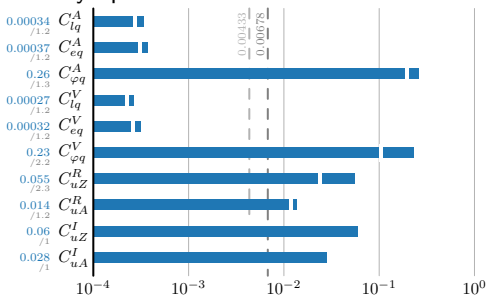
HL-LHC (ind.)



correlation matrices



Statistically optimal observables:

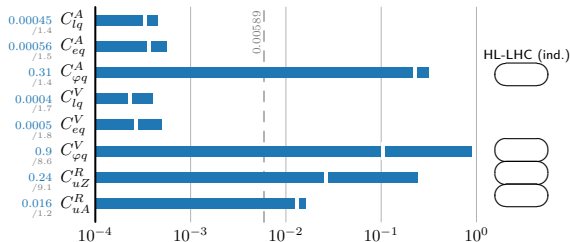


$\mathcal{O}(10^{-3})$ better
than HL projections
with linear coefficient
dependence only

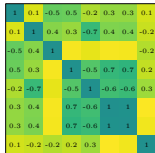
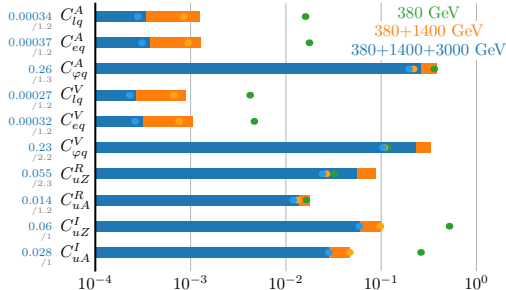
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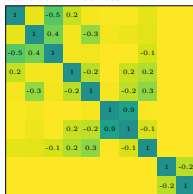
$\sigma + A^{\text{FB}}$:



Statistically optimal observables:



correlation matrices



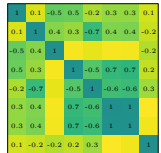
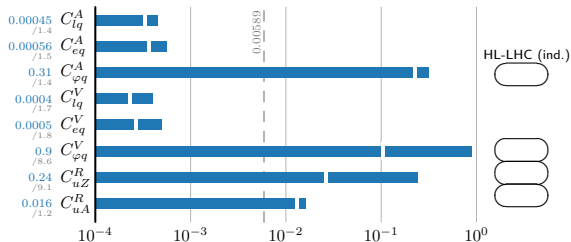
high energy benefits
four-fermion op.

with linear coefficient
dependence only

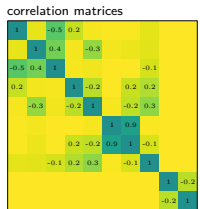
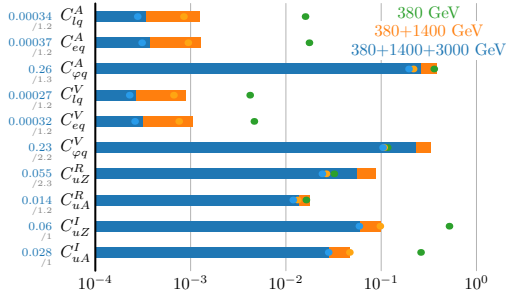
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Statistically optimal observables:

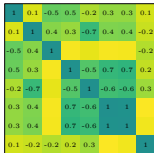
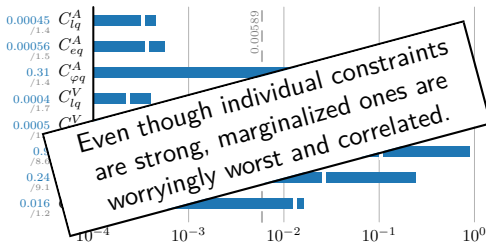


runs at two \sqrt{s}
are required
with linear coefficient
dependence only

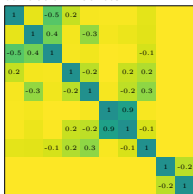
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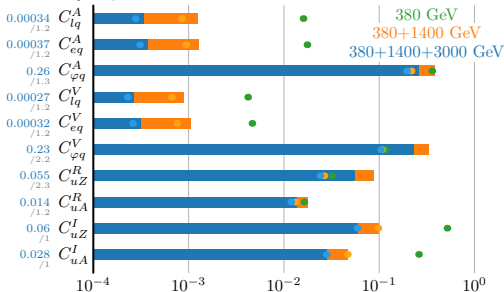
$\sigma + A^{\text{FB}}$:



correlation matrices



Statistically optimal observables:



runs at two \sqrt{s}
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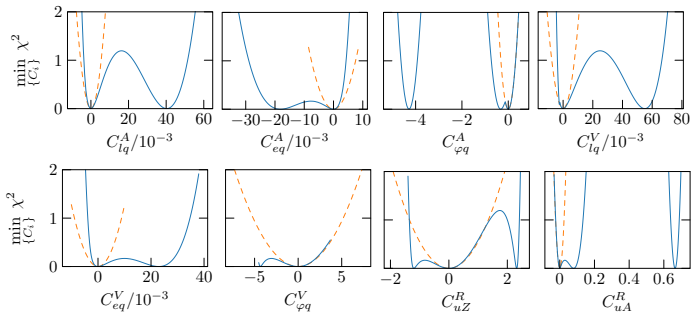
with linear coefficient
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Robustness

Linear EFT truncation

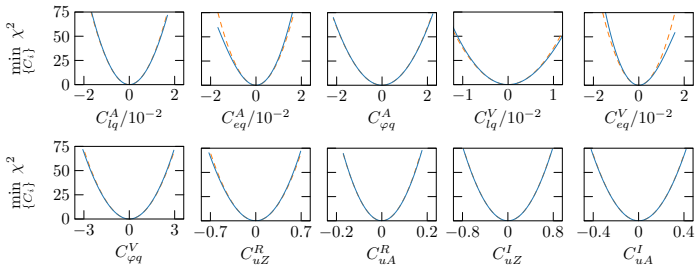
$\sigma + A^{\text{FB}}$:

dashed: linear dependence only
plain: linear+quadratic dep.



Statistically optimal observables:

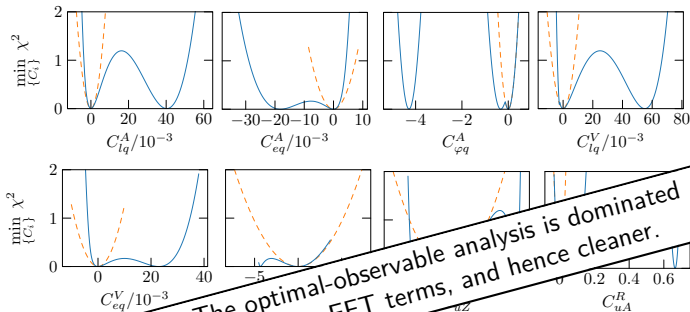
Note the vertical scale!



Linear EFT truncation

$\sigma + A^{\text{FB}}$:

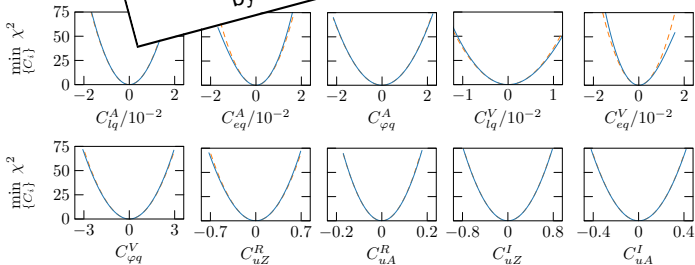
dashed: linear dependence only
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The optimal-observable analysis is dominated by linear EFT terms, and hence cleaner.

Statistically of

Note the vertical scale!



Experimental reconstruction

[1807.02441]

Full-detector simulation performed by CLICdp.

Good reconstruction can be obtained with moderate quality cuts.

Effective $t\bar{t}$ reco. efficiency in semileptonic channel ($\text{Br}^{e+\mu} \simeq 29\%$):

\sqrt{s} [GeV]	380		1400		3000	
$P(e^-)$	-80%	+80%	-80%	+80%	-80%	+80%
ϵ	12.9% (σ) 4.7% (A_{FB}) 7.8% (OO)	12.1%	6%	5.8%	4.6%	4.7%

- bW mis-pairing with left-handed beam at low energy
- larger beam energy spectrum tails at high energies
- larger single-top bkg. at high energies

Systematics expected to be controlled to the level of statistics

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\sqrt{s} [GeV]	380		1400		3000	
$P(e^-)$	-80%	+80%	-80%	+80%	-80%	+80%
ϵ	10% (σ)					
	10% (A_{FB})	10%	6%	6%	5%	5%
	10% (OO)					

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Systematics expected to be controlled to the level of statistics

numbers used here, for simplicity

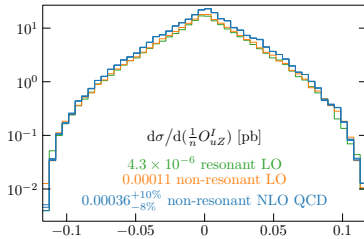
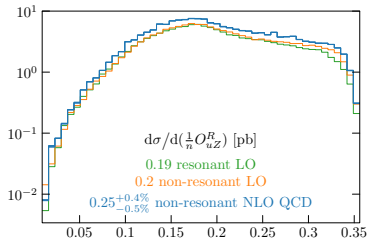
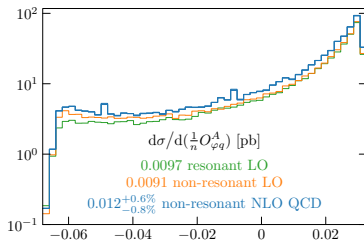
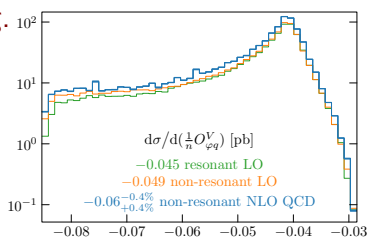
Theoretical prediction

[similar procedure in Gristan et al]

Non-resonant and NLO QCD effects can be studied

- mostly flat k factor (24% at $\sqrt{s} = 500$ GeV)
- couple-of-percent shape effects, excepted on axial operators ($O(10)\%$)

e.g.



$\sqrt{s} = 500$ GeV, $P(e^+, e^-) = (+30\%, -80\%)$,
quoted average values of distribution are \bar{O}_i/\mathcal{L} in pb,
QCD scale variation from $m_t/2$ to $2m_t$

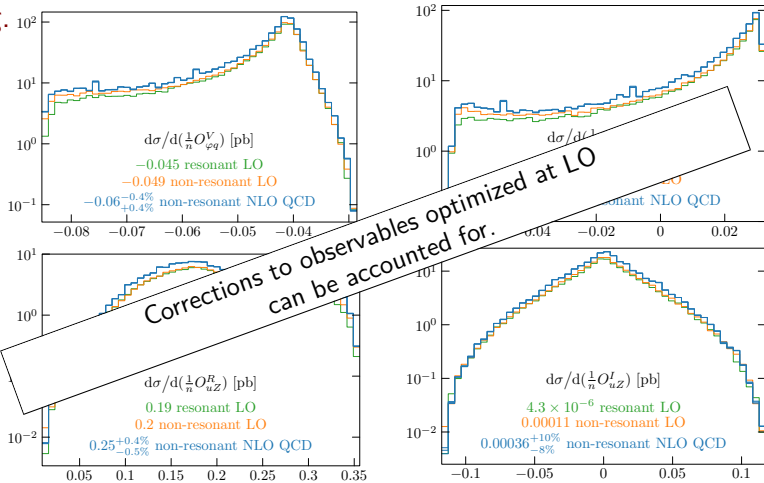
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[similar procedure in Gristan et al]

Non-resonant and NLO QCD effects can be studied

- mostly flat k factor (24% at $\sqrt{s} = 500$ GeV)
- couple-of-percent shape effects, excepted on axial operators ($O(10)\%$)

e.g.



$\sqrt{s} = 500$ GeV, $P(e^+, e^-) = (+30\%, -80\%)$,
quoted average values of distribution are \bar{O}_i/\mathcal{L} in pb,
QCD scale variation from $m_t/2$ to $2m_t$

Run parameter optimization

Warning: In specific models, certain EFT directions would have more weight.

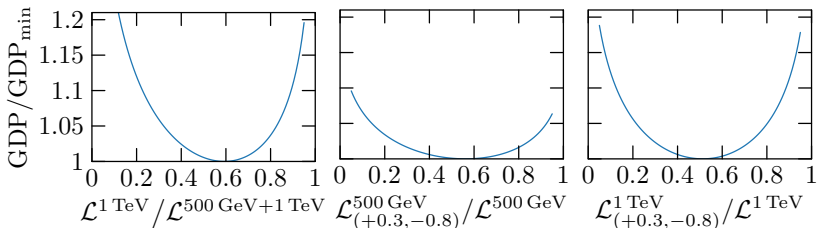
Sharing 1.5 ab^{-1} between two energies and polarizations

Optimal repartition:

$\sqrt{s} = 500 \text{ GeV}$	570 fb^{-1}	61% with $P(e^+, e^-) = (+0.3, -0.8)$
1 TeV	930 fb^{-1}	52%

→ GDP is 1.02 times better than the benchmark one

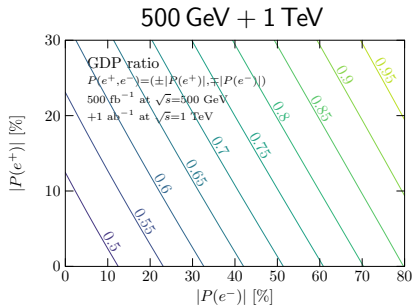
(for the OO analysis with all 10 coefficients)



Same performances require 5.6 ab^{-1} with only $\sqrt{s} = 380 + 500 \text{ GeV}$:

$\sqrt{s} = 380 \text{ GeV}$	1.7 ab^{-1}	59%	with $P(e^+, e^-) = (+0.3, -0.8)$
500 GeV	3.9 ab^{-1}	53%	

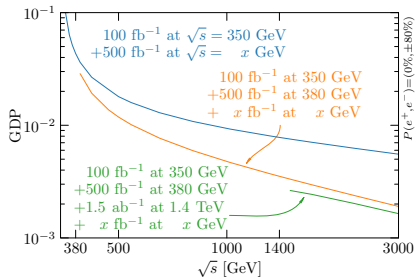
Degrading polarization or energy lever arm



10% polarization costs $\sim 5\%$ of GDP

w.r.t. $P(e^+, e^-) = (\pm 30\%, \mp 80\%)$:

- $P(e^+)$ compensated by 140% lumi
- $P(e^+, e^-)$ " by 460% lumi



\sqrt{s} lever arm is necessary

3. Interpretation in composite Higgs models

Framework

- The Higgs is composite, pNGB of a new strong sector
- Typical strong sector coupling and mass: g_* , m_*
- Linear mixings between SM states and composite ones: ϵ_u , ϵ_q

→ dimensional analysis for strong-sector operator coefficients

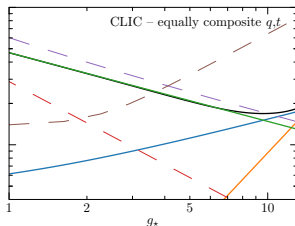
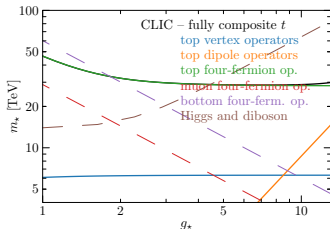
$$\frac{m_*^4}{g_*^2} O^{\text{dim-6}} \left(\epsilon_\psi \frac{g_*}{m_*^{3/2}} \psi, \frac{g}{m_*^2} F^{\mu\nu}, \frac{g_*}{m_*} \phi \right) \quad \text{up to order-one factors or justified suppressions}$$

in particular $y_t \simeq \epsilon_u \epsilon_q g_*$

fix either $\epsilon_u = \epsilon_q \simeq \sqrt{\frac{y_t}{g_*}}$: equally composite top left and right

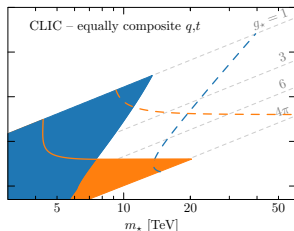
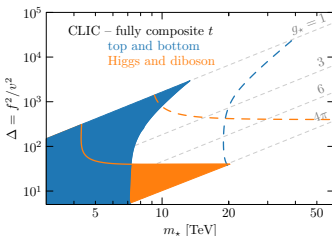
$\epsilon_u = 1$, $\epsilon_q \simeq \frac{y_t}{g_*}$: fully composite top right

One-sigma sensitivities in (coupling, mass) plane



power counting exactly satisfied

Five-sigma discovery reach in (mass, tuning) plane

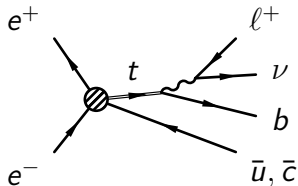


power counting satisfied up to $\pm[1/2, 2]$ \rightarrow filled: pessimistic
 \rightarrow dashed: optimistic

4. Top-quark FCNC production

accessible from the lowest energies
still benefiting from the highest

$e^+ e^- \rightarrow tj$ setup



- ▶ Use pseudo OO's (quadratic dependence!) on the semileptonic final state

- ▶ Choose ϵ to match existing studies

[TESLA: hep-ph/0102197]

[FCC-ee: 1408.2090]

\sqrt{s} [GeV]	\mathcal{L} [fb^{-1}]	$P(e^+, e^-)$	$\text{Br}(t \rightarrow j\gamma)$ before fit	ϵ before fit	ϵ after fit	Br after fit
240	3000	(0, 0)	3.70×10^{-5}	0.30	0.30	3.7×10^{-5}
350	3000	(0, 0)	9.86×10^{-6}	0.19	0.14	1.1×10^{-5}
500	3000	(0, 0)	6.76×10^{-6}	0.057	0.072	6.0×10^{-6}
500	300	(0, 0)	2.2×10^{-5}	0.054	0.072	1.9×10^{-5}
800	500	(0, 0)	7.8×10^{-6}	0.037	0.029	8.7×10^{-6}

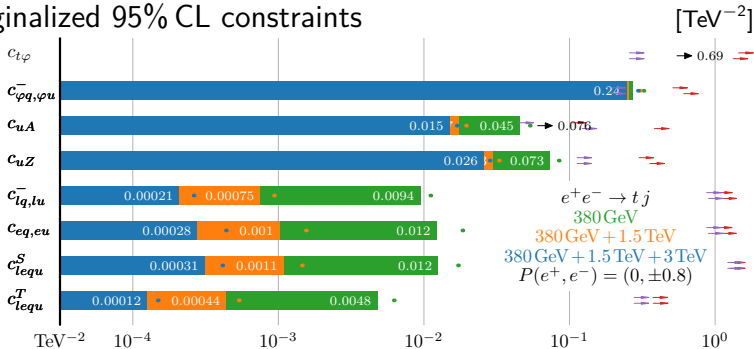
- ▶ Extrapolate to CLIC run parameters and go global

- $\epsilon = \epsilon(\sqrt{s}) = (125 \text{ GeV}/\sqrt{s})^{1.92}$
- include four-fermion operators

- ▶ Use LHC TOP WG standards

[1802.07237]

Marginalized 95% CL constraints



- compared to decay: black arrows
- compared to current limits: red arrows^{up}_{charm}
- compared to HL-LHC estimates: purple arrows^{up}_{charm}
- without beam polarization: blobs

[CLIC YR]

Global probes for the top-quark EFT

Clean global EFT analyses are feasible
at future lepton colliders.

Statistically optimal observables are
theoretically well-motivated and experimentally amenable.

CLIC would cover orders of magnitude of unexplored top-quark
EFT parameter space.

High-energy top pair production is particularly relevant to
composite Higgs models.

Single top FCNC production is a powerful probe
that should be further studied experimentally.