

**Impact of final state interactions on  
neutrino-nucleon pion production cross sections  
extracted from neutrino-deuteron reaction data**

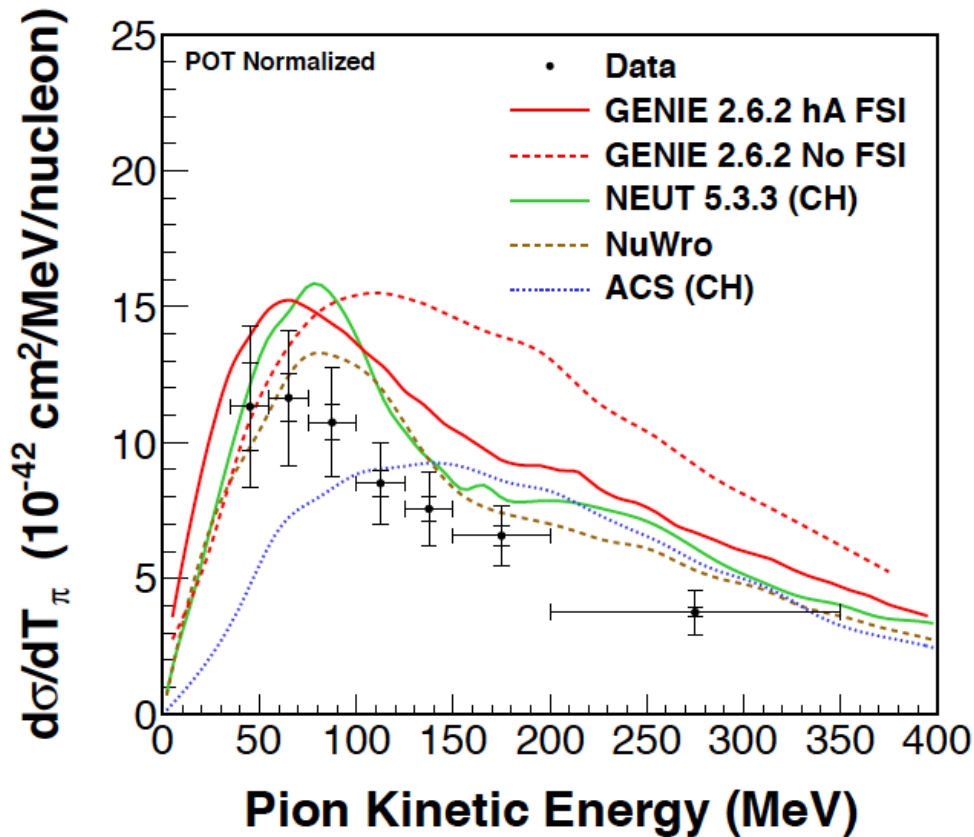
Satoshi Nakamura

Universidade Cruzeiro do Sul, Brazil

Collaborators: H. Kamano (KEK), T. Sato (Osaka U.)

# Introduction

# Neutrino experiments need neutrino-nucleus pion production model



$$\langle E_\nu \rangle = 4.0 \text{ GeV}, W < 1.4 \text{ GeV}$$

MINERvA PRD 92 (2015)

→ Model goes into analysis of oscillation data

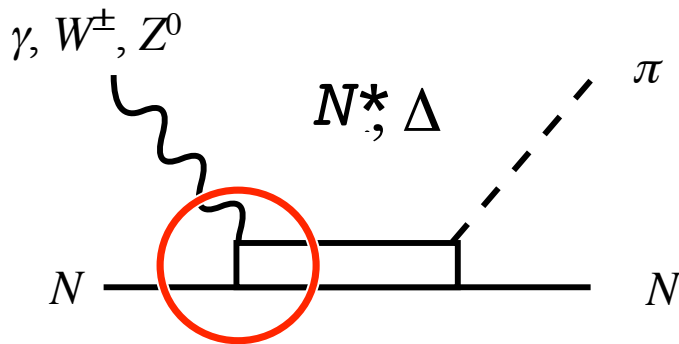
An essential ingredient of neutrino-nucleus model : elementary **neutrino-nucleon** model

We are still in a process of establishing the elementary neutrino-nucleon pion production model

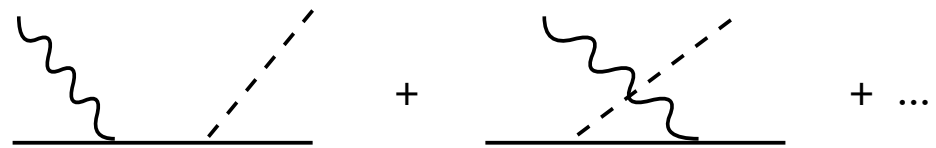
**Precision era** of neutrino experiments (CP, mass hierarchy) → models of comparable quality

# Theoretical description of elementary process in resonance region (single pion productions)

## Resonance excitations



## Non-resonant mechanisms



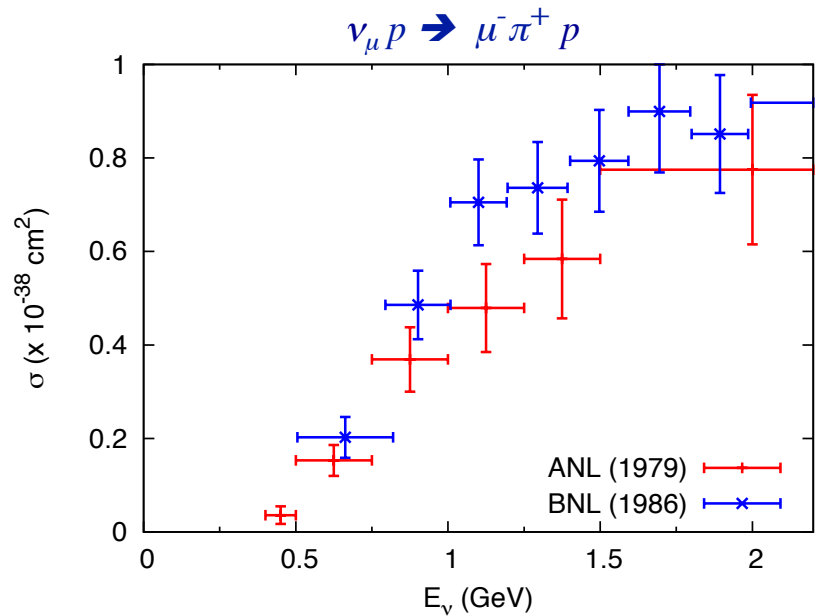
## Dominant $\Delta(1232)$ -excitation and sub-leading non-resonant mechanisms

- Accurate determination of  $N$ - $\Delta(1232)$  transition strength is of vital importance
- Experimental inputs are needed to examine pion production mechanisms

Vector current : photon- and electron-nucleon  $1\pi$  production data

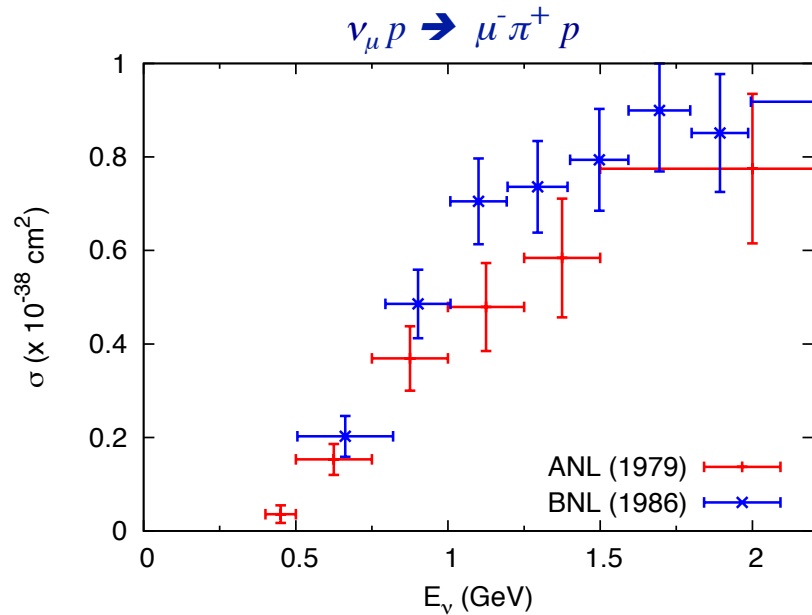
Axial current : neutrino-nucleon  $1\pi$  production data

# Neutrino interaction data in $\Delta(1232)$ region

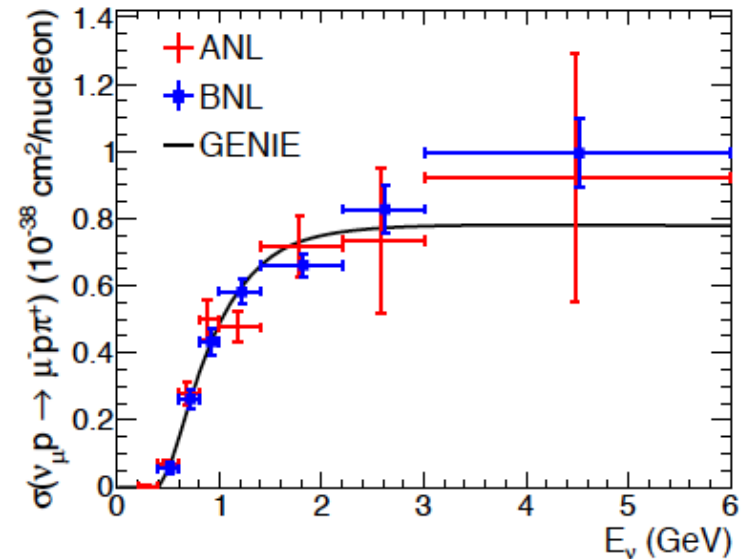


- **ALL models fit this data by adjusting  $g_{AN\Delta}$**   
→ very important data
- Discrepancy between BNL & ANL data  
→ theoretical uncertainty in neutrino-nucleus cross sections

# Neutrino interaction data in $\Delta(1232)$ region



Wilkinson et al. PRD 90 (2014)



- ALL models fit this data by adjusting  $g_{AN\Delta}$ 
  - very important data
- Discrepancy between BNL & ANL data
  - theoretical uncertainty in neutrino-nucleus cross sections

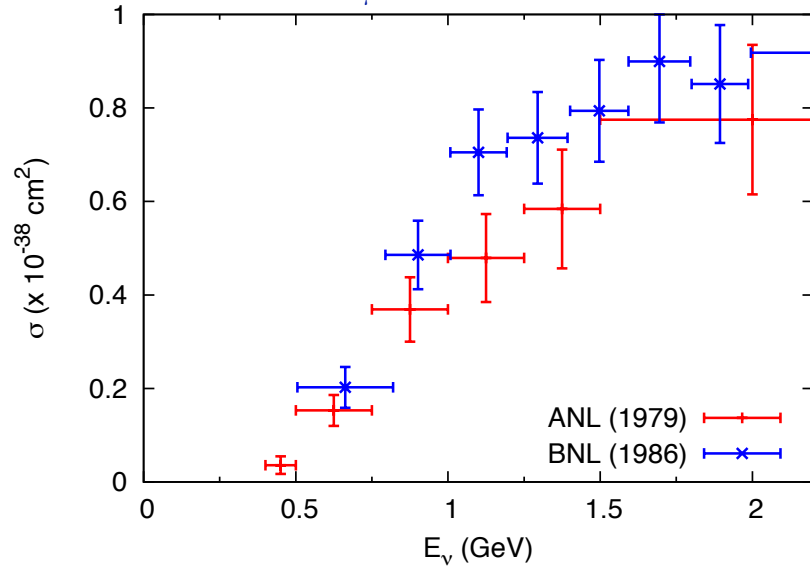
Reanalysis of original data

→ discrepancy resolved (probably)

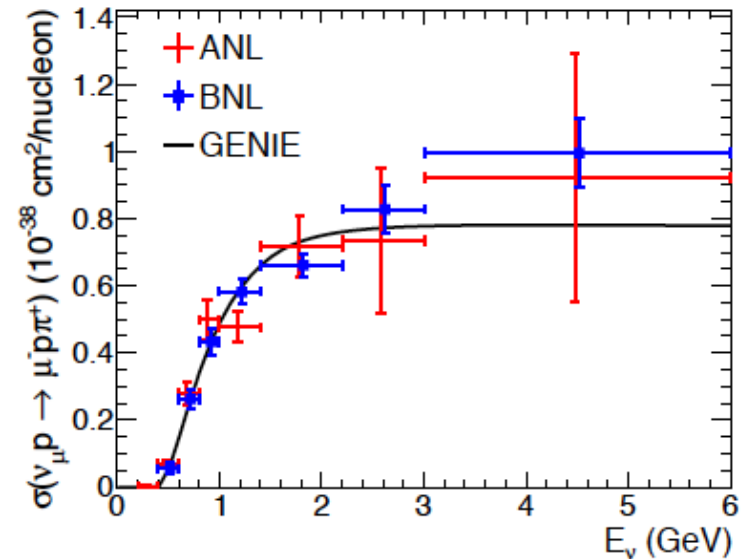
$$\frac{\sigma(\text{CC}1\pi; \text{data})}{\sigma(\text{CC}0\pi; \text{data})} \times \sigma(\text{CCQE}; \text{model})$$

Flux uncertainty is cancelled out

# Neutrino interaction data in $\Delta(1232)$ region



Wilkinson et al. PRD 90 (2014)



- ALL models fit this data by adjusting  $g_{AN\Delta}$ 
  - very important data
- Discrepancy between BNL & ANL data
  - theoretical uncertainty in neutrino-nucleus cross sections

Reanalysis of original data

→ discrepancy resolved (probably)

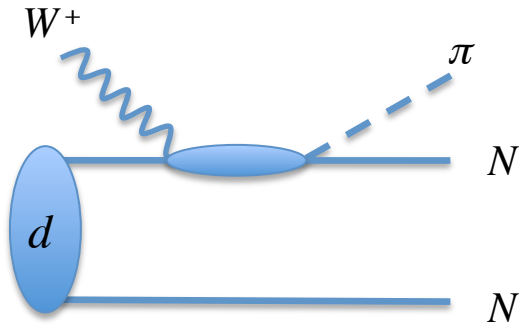
$$\frac{\sigma(\text{CC}1\pi; \text{data})}{\sigma(\text{CC}0\pi; \text{data})} \times \sigma(\text{CCQE}; \text{model})$$

Flux uncertainty is cancelled out

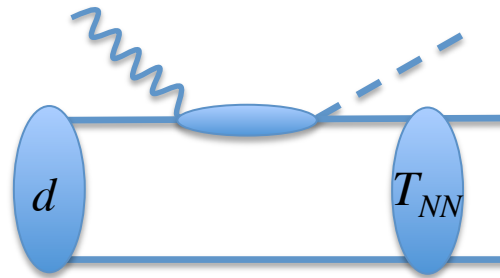
$\nu_\mu p \rightarrow \mu^- \pi^+ p$  data were extracted from  $\nu_\mu d \rightarrow \mu^- \pi^+ p n$  data    Nuclear effects matter ?

# Mechanisms (including nuclear effects) for $\nu_\mu d \rightarrow \mu^- \pi N N$

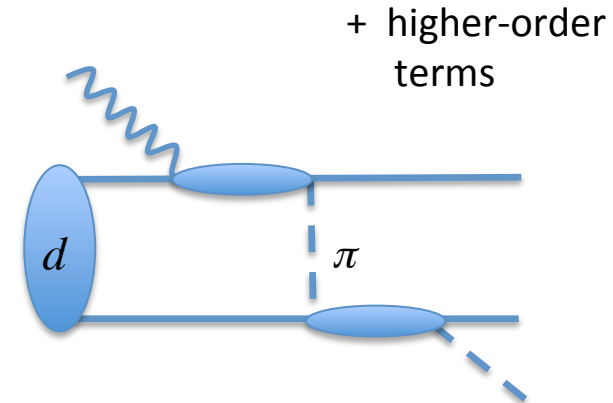
Impulse



$NN$  rescattering



$\pi N$  rescattering



## Nuclear effect managements

**Exp.** Quasi-free events were (supposedly) selected in ANL and BNL analyses

**Theory** Fermi motion considered in fixing  $g_{AN\Delta}$  Hernandez et al. (2010), Alam et al. (2016)

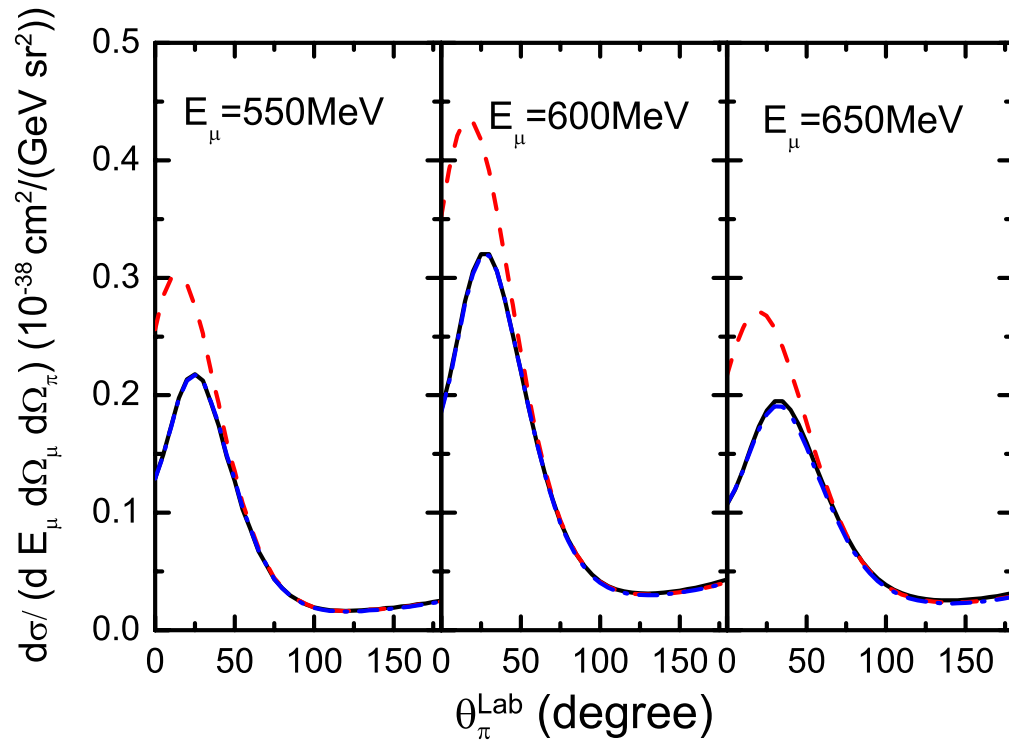
**Q:** Should we still consider final state interactions (FSI) effects ?

FSI effects on  $\nu_\mu d \rightarrow \mu^- \pi N N$  have been explored with a dynamical model Wu et al. (2015)



# FSI effects on $\nu_\mu d \rightarrow \mu^- \pi^+ p n$

Wu, Lee, Sato, PRC91, 035203 (2015)



$$E_\nu = 1 \text{ GeV},$$

$$E_\mu = 550, 600, 650 \text{ MeV}, \theta_\mu = 25^\circ, \phi_{\pi^-} = 0^\circ$$

--- Impulse approx.

- · - NN FSI

— NN +  $\pi$ N FSI

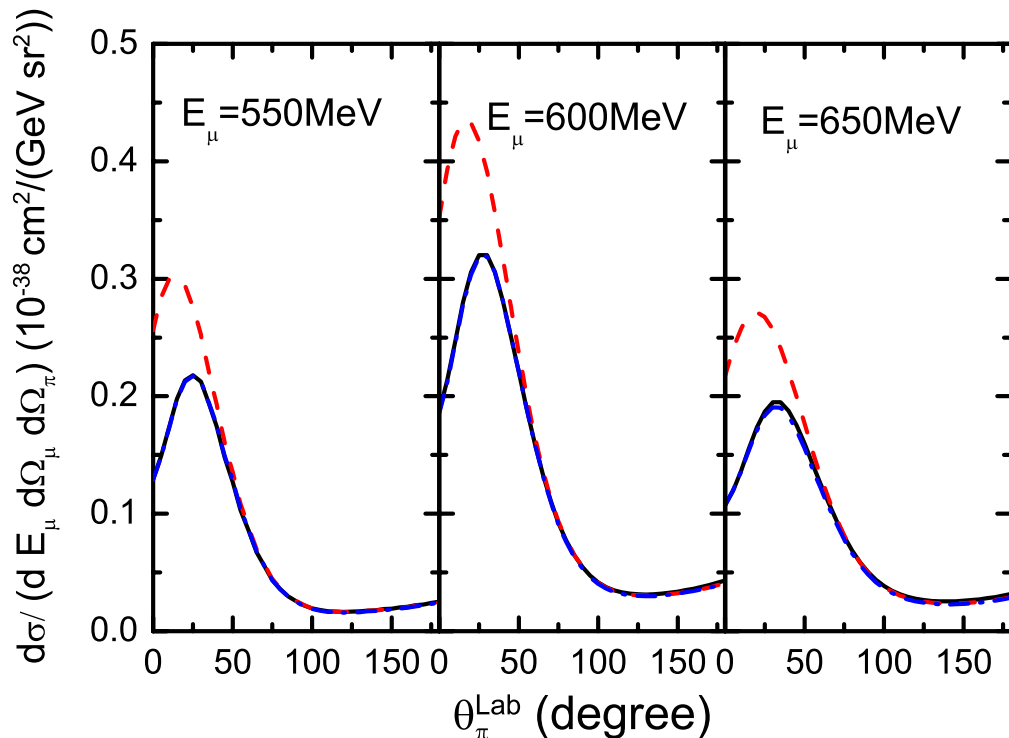
Significant reduction due to NN FSI



Orthogonality of  $pn$  and  $d$  wave functions

# FSI effects on $\nu_\mu d \rightarrow \mu^- \pi^+ p n$

Wu, Lee, Sato, PRC91, 035203 (2015)



$$E_\nu = 1 \text{ GeV},$$

$$E_\mu = 550, 600, 650 \text{ MeV}, \theta_\mu = 25^\circ, \phi_\pi = 0^\circ$$

--- Impulse approx.

- · - NN FSI

— NN +  $\pi$ N FSI

Significant reduction due to NN FSI



Orthogonality of  $pn$  and  $d$  wave functions

Wu et al. focused on quasi-free kinematics only

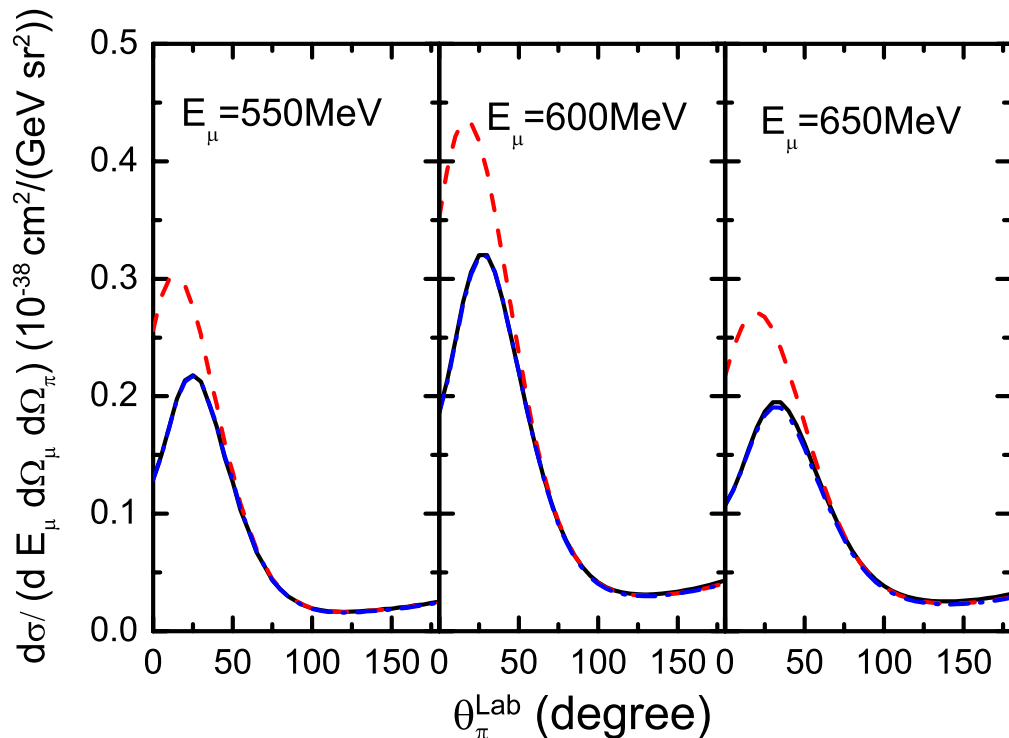
→ whole phase-space need to be examined to understand FSI effects on ANL and BNL data

$$\sigma = \int dp_{N_1} dp_{N_2} dp_\mu dp_\pi \delta^{(4)}(P_i - P_f) |M|^2 \quad (7 \text{ dim. non-trivial numerical integral})$$

Numerically challenging problem

# FSI effects on $\nu_\mu d \rightarrow \mu^- \pi^+ p n$

Wu, Lee, Sato, PRC91, 035203 (2015)



$$E_\nu = 1 \text{ GeV},$$

$$E_\mu = 550, 600, 650 \text{ MeV}, \theta_\mu = 25^\circ, \phi_\pi = 0^\circ$$

--- Impulse approx.

- · - NN FSI

— NN +  $\pi$ N FSI

Significant reduction due to NN FSI



Orthogonality of  $pn$  and  $d$  wave functions

Wu et al. focused on quasi-free kinematics only

→ whole phase-space need to be examined to understand FSI effects on ANL and BNL data

$$\sigma = \int dp_{N_1} dp_{N_2} dp_\mu dp_\pi \delta^{(4)}(P_i - P_f) |M|^2 \quad (7 \text{ dim. non-trivial numerical integral})$$

Numerically challenging problem *will be managed with Monte-Carlo integral*

# This work

- $\nu_\mu d \rightarrow \mu^- \pi NN$  cross sections of the whole phase-space are calculated with a dynamical model including FSI ; for the first time
- FSI effect on spectator momentum distribution  $d\sigma/dp_s$  is examined
- Find a useful recipe to extract elementary  $\nu_\mu N \rightarrow \mu^- \pi N$  cross sections from  $\nu_\mu d \rightarrow \mu^- \pi NN$  spectator momentum distribution
- Extract  $\nu_\mu N \rightarrow \mu^- \pi N$  total cross sections by correcting (flux-corrected) ANL and BNL data for FSI and Fermi motion

## Future impact

- Significantly improved elementary  $\nu_\mu N \rightarrow \mu^- \pi N$  model to be implemented in neutrino-nucleus reaction model for oscillation experiments of the precision era

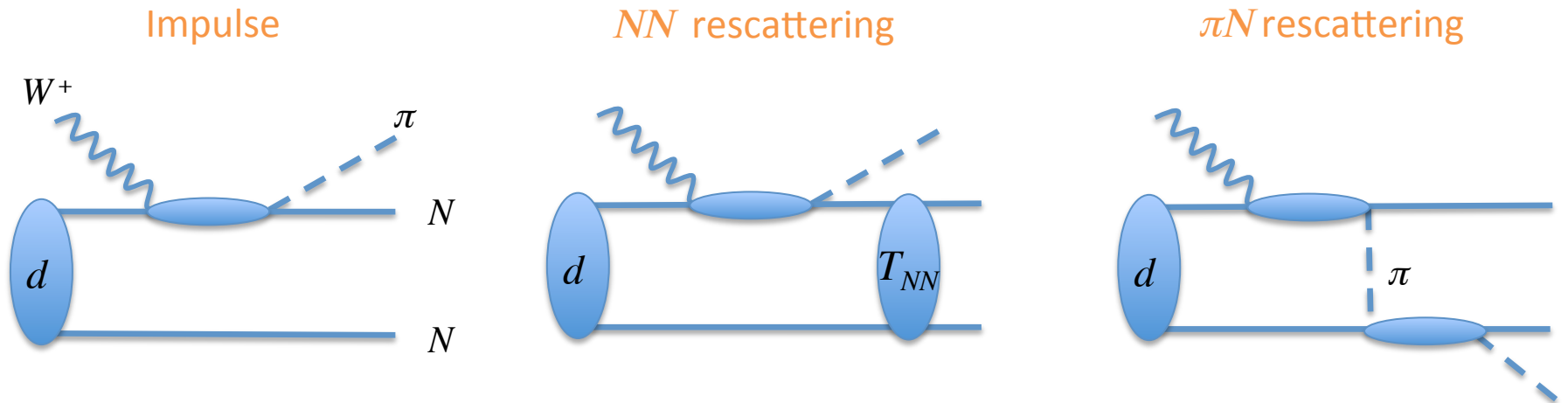
$\nu_{\mu} d \rightarrow \mu^{-} \pi NN$  reaction model

based on

dynamical coupled-channels model

# Model for $\nu_\mu d \rightarrow \mu^- \pi N N$

Multiple scattering theory truncated at the first-order rescattering



## Elementary amplitudes

$W^\pm N \rightarrow \pi N$ ,  $\pi N \rightarrow \pi N$  (off-shell) amplitude  $\leftarrow$  DCC model (SXN et al., PRD92 (2015))

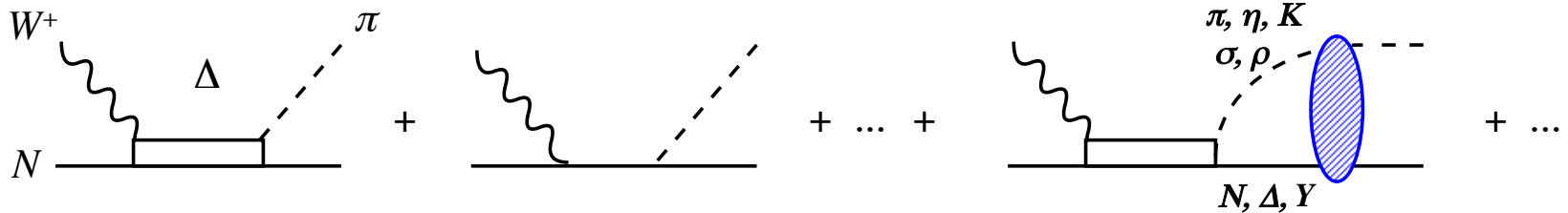
$T_{NN}$ , deuteron w.f.

$\leftarrow$  CD-Bonn potential (Machleidt et al., PRC 63 (2001))

3-dim. loop integral with off-shell amplitudes are numerically evaluated

# Dynamical coupled-channels model

Kamano, SXN, Lee, Sato, PRC 88, 035209 (2013)  
 SXN, Kamano, Lee, Sato, PRD 92, 074024 (2015)



Developed through analyzing  $\gamma^{(*)}N, \pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$  data ( $\sim 27,000$  data pts.)

$\rightarrow$  Extended to  $\nu N \rightarrow l^- X$  ( $X = \pi N, \pi\pi N, \eta N, K\Lambda, K\Sigma$ )

## Unique features

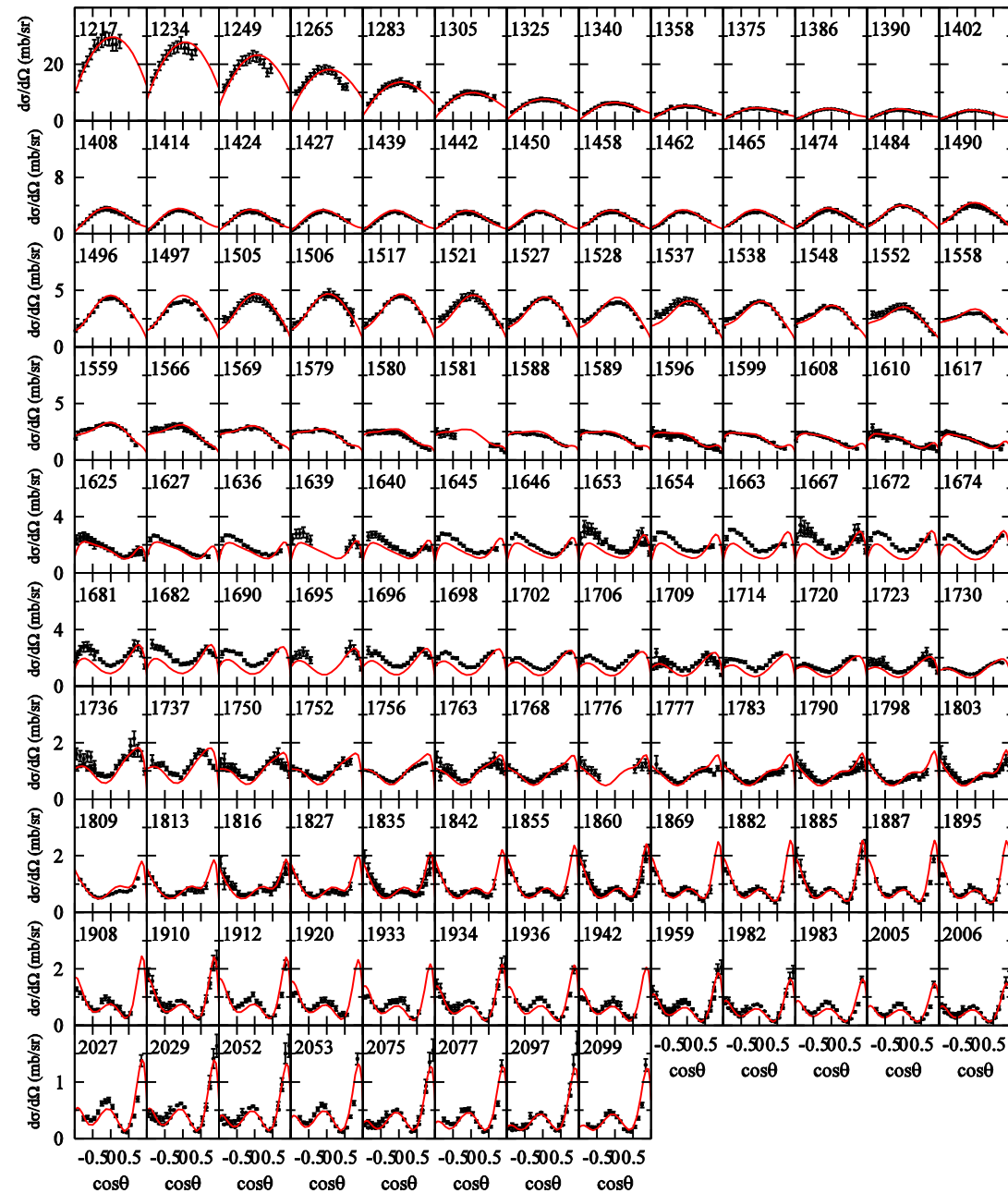
- Hadronic rescattering and channel-couplings are taken into account  
 $\leftarrow$  requirement from the unitarity
- Interference among resonant and non-resonant mechanisms are under control within the model
- One-pion AND two-pion productions for the whole resonance region are described

$\gamma p \rightarrow \pi^0 p$

$d\sigma/d\Omega$  for  $W < 2.1$  GeV

Comparison of DCC model with data

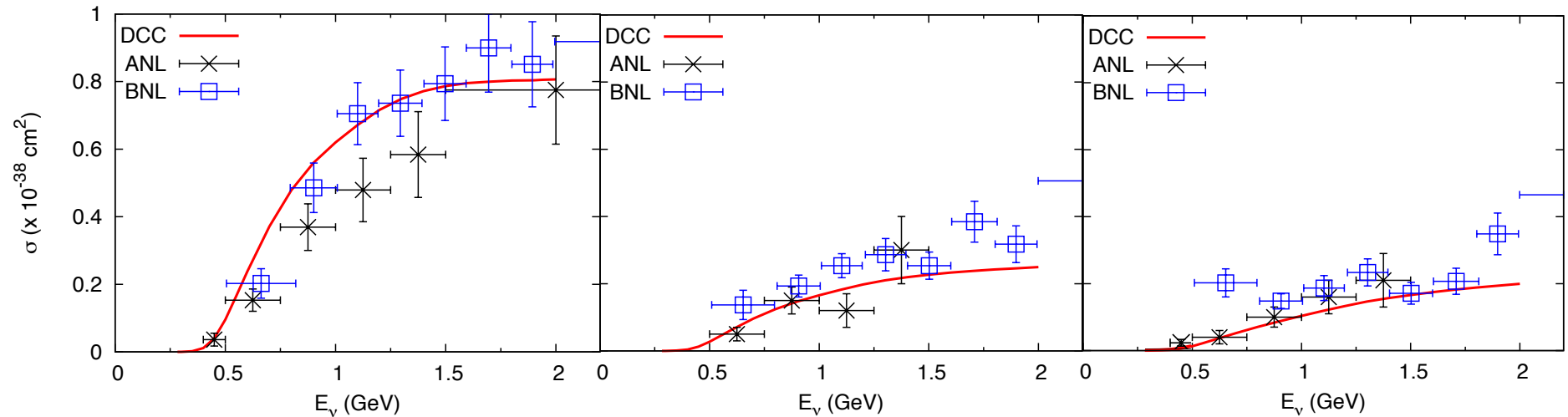
Kamano, Nakamura, Lee, Sato, PRC 88 (2013)



Vector current ( $Q^2=0$ ) for  $1\pi$   
Production is well-tested by data



# Comparison of DCC model with single pion data



ANL Data : PRD **19**, 2521 (1979)

BNL Data : PRD **34**, 2554 (1986)

DCC model **prediction** is consistent with BNL data (before flux correction)

DCC model has flexibility to fit ANL data ( $ANN^*(Q^2)$ )

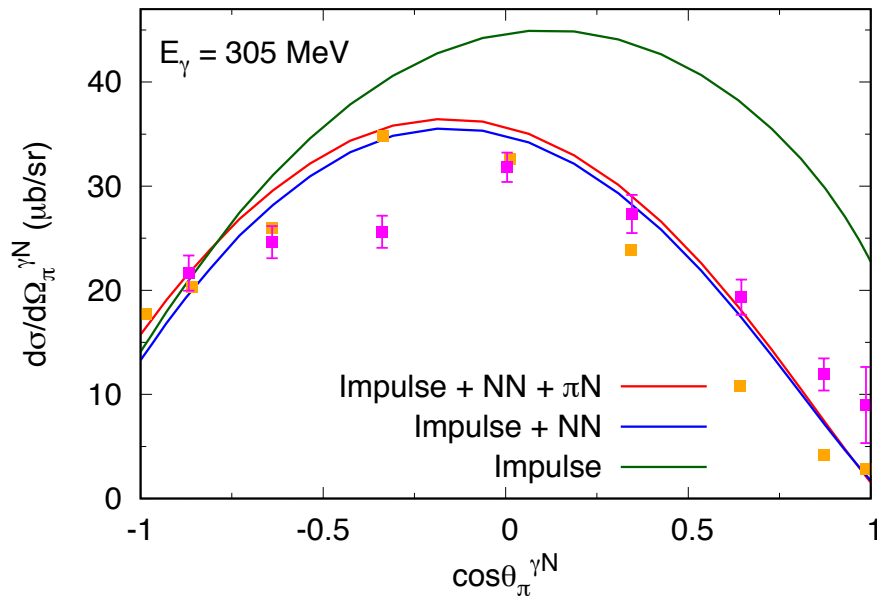
We will fit data after the issue of nuclear effects on the data is clarified

# Results

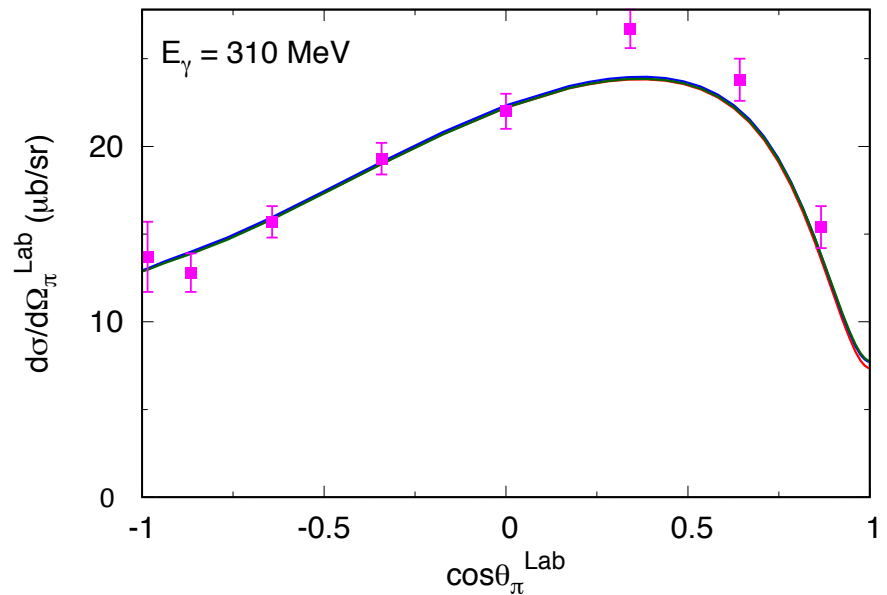
# $\gamma d \rightarrow \pi NN$ : model predictions and data

Purpose : validate our DCC-based deuteron-reaction model

$\gamma d \rightarrow \pi^0 pn$



$\gamma d \rightarrow \pi^- pp$



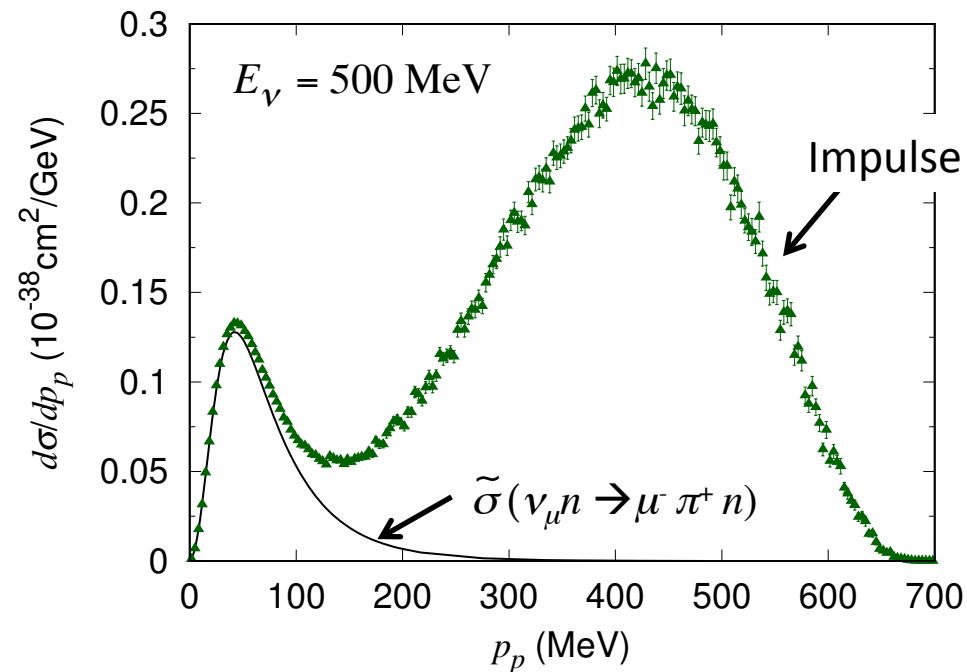
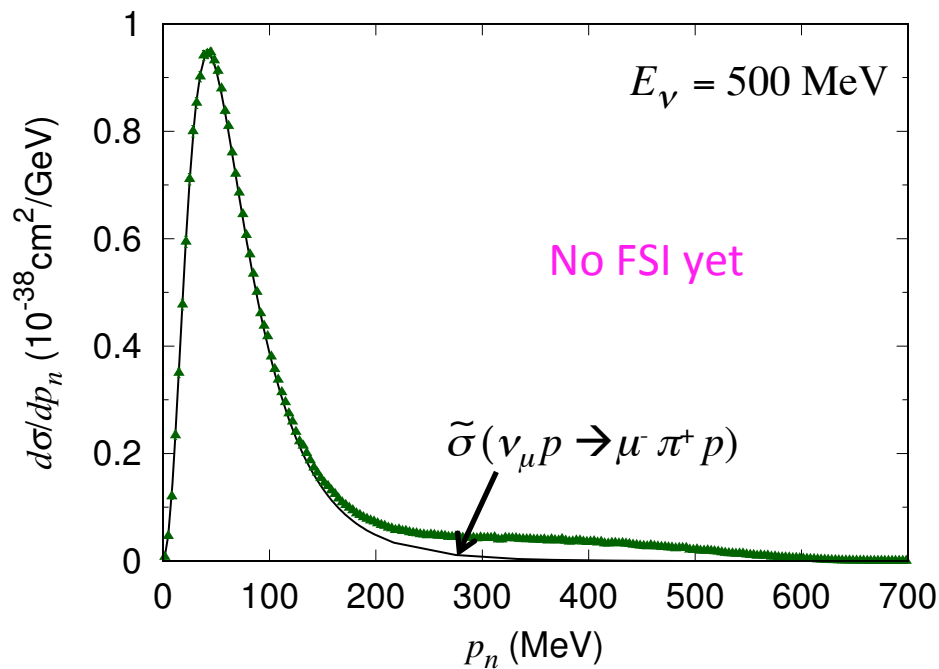
- Large NN FSI effect for  $\pi^0$  productions  $\leftarrow$  NN and deuteron wave fn. are orthogonal
- FSI effects are small for  $\pi^-$  productions
- Reasonable agreement with data  $\rightarrow$  reliable estimate of FSI effects on neutrino-deuteron

Data: EPJA 6, 309 (1999); 10, 365 (2001) for  $\gamma d \rightarrow \pi^0 pn$ , NPB 65, 158 (1973) for  $\gamma d \rightarrow \pi^- pp$

# $\nu_\mu d \rightarrow \mu^- \pi^+ p n$ spectator momentum distribution

Minimal information to extract  $\nu_\mu N \rightarrow \mu \pi N$  cross sections

Contribution from other nucleon (spectator) is expected to be small in small  $p_s$  region



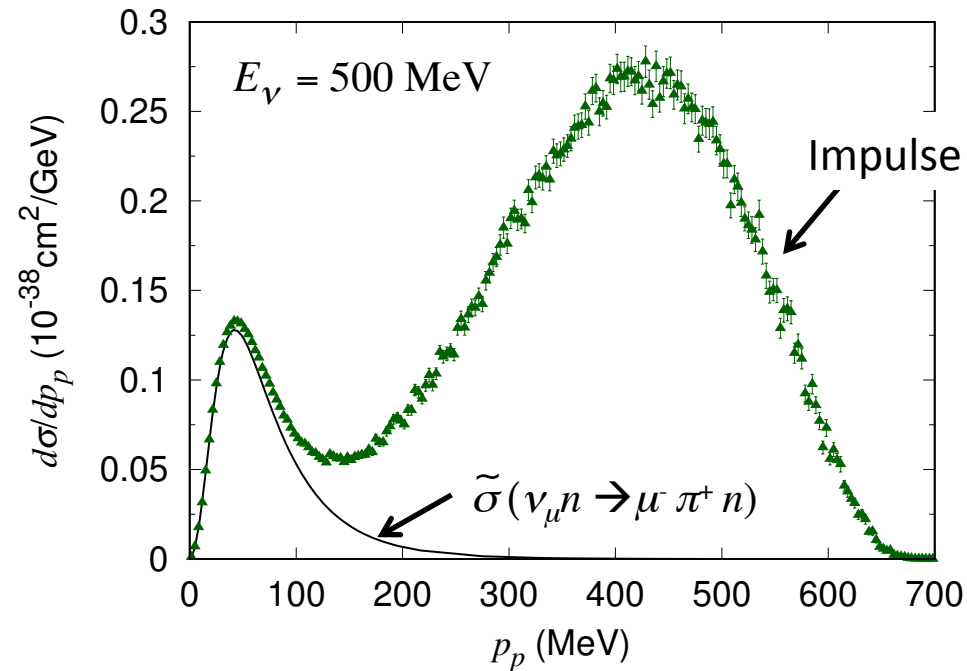
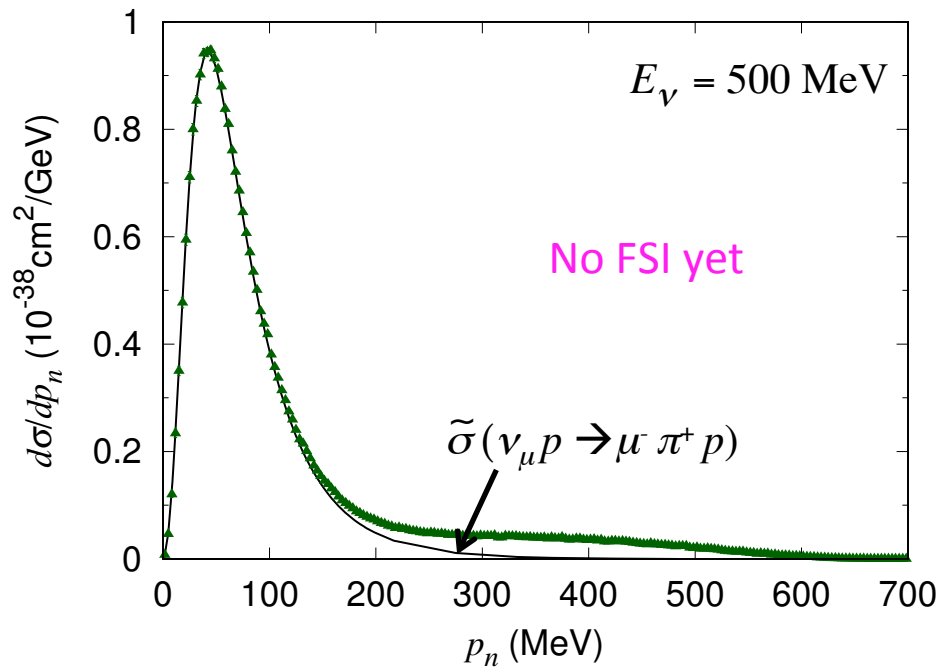
Phase-space integral for  $\nu_\mu d \rightarrow \mu \pi^+ p n$  is done with Monte-Carlo method

→ central values with statistical errors

# $\nu_\mu d \rightarrow \mu^- \pi^+ p n$ spectator momentum distribution

Minimal information to extract  $\nu_\mu N \rightarrow \mu^- \pi^+ N$  cross sections

Contribution from other nucleon (spectator) is expected to be small in small  $p_s$  region



Convolutd cross section ( $\tilde{\sigma}$ ): 
$$\frac{d\tilde{\sigma}_\alpha(E_\nu)}{dp_s} = p_s^2 \int d\Omega_{p_s} \underbrace{\sigma_\alpha(\tilde{E}_\nu)}_{\text{cross section for free nucleon}} |\Psi_d(\vec{p}_s)|^2 \quad \alpha = \nu_\mu N \rightarrow \mu^- \pi^+ N$$

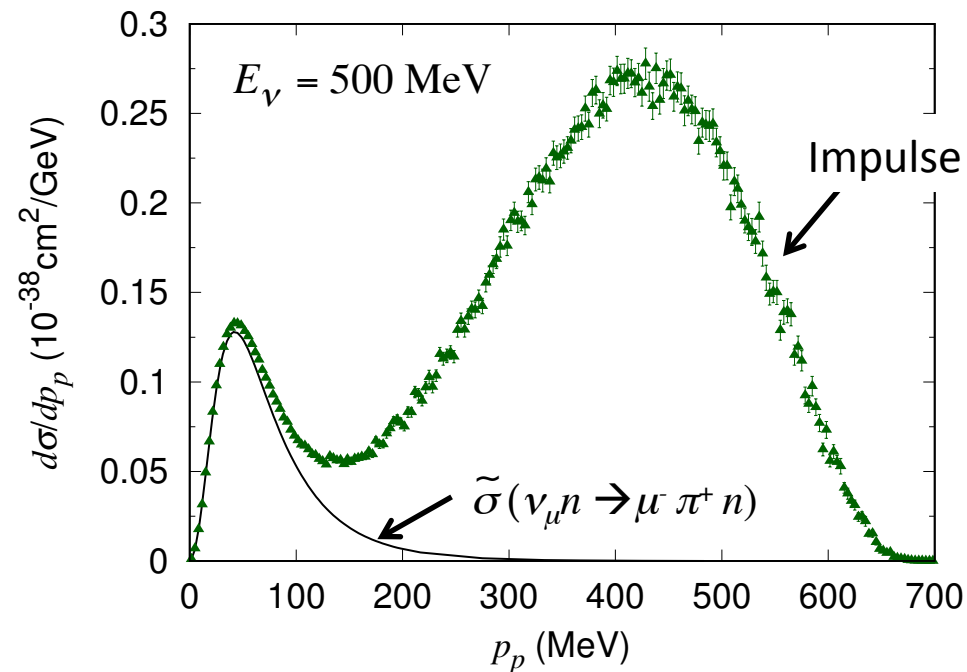
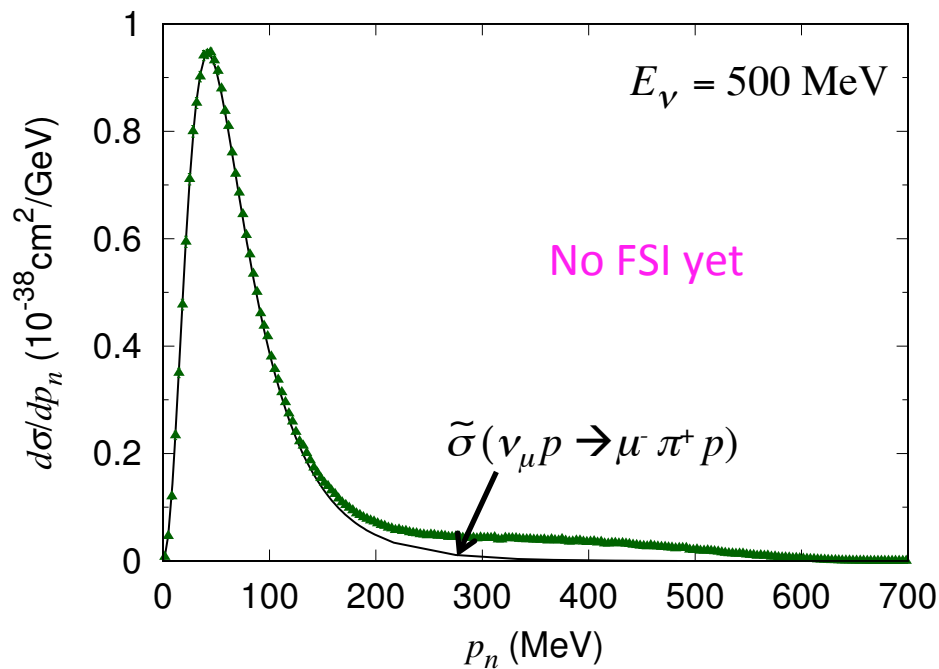
= **Quasi-free** contribution

$\Psi_d$  : deuteron w.f.

# $\nu_\mu d \rightarrow \mu^- \pi^+ p n$ spectator momentum distribution

Minimal information to extract  $\nu_\mu N \rightarrow \mu \pi N$  cross sections

Contribution from other nucleon (spectator) is expected to be small in small  $p_s$  region



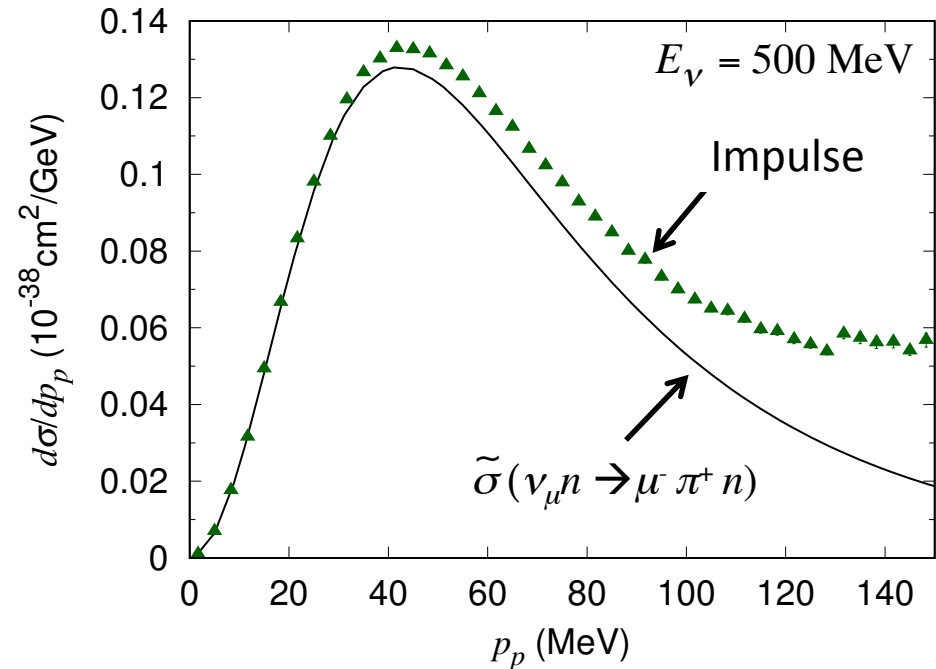
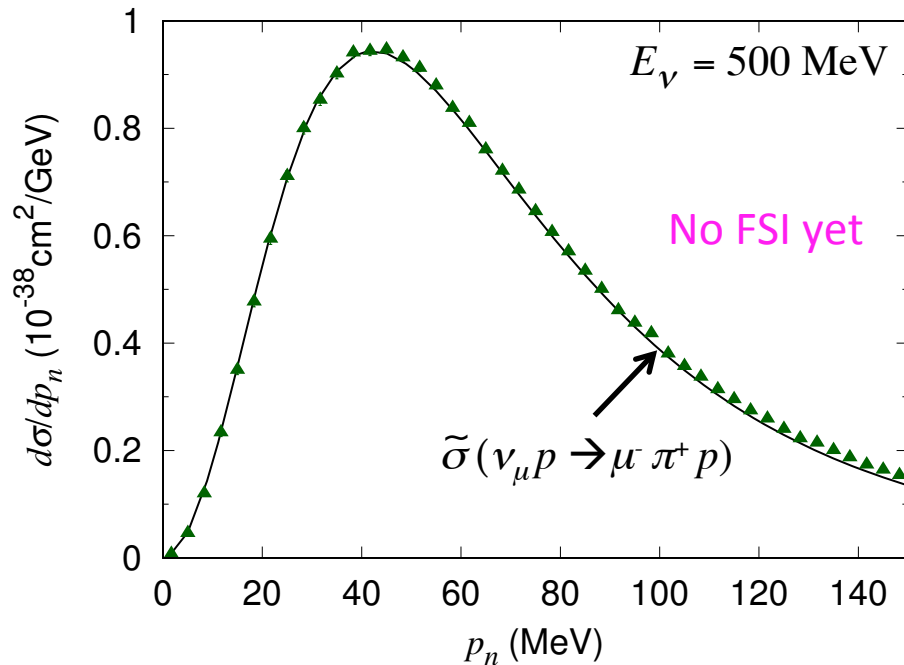
Difference between  $\sigma$  (Impulse) and  $\tilde{\sigma} \rightarrow$  contribution from the other nucleon

$$\sigma(\nu_\mu p \rightarrow \mu \pi^+ p) \approx 9 \times \sigma(\nu_\mu n \rightarrow \mu \pi^+ n)$$

# $\nu_\mu d \rightarrow \mu^- \pi^+ p n$ spectator momentum distribution

Minimal information to extract  $\nu_\mu N \rightarrow \mu \pi N$  cross sections

Contribution from other nucleon (spectator) is expected to be small in small  $p_s$  region



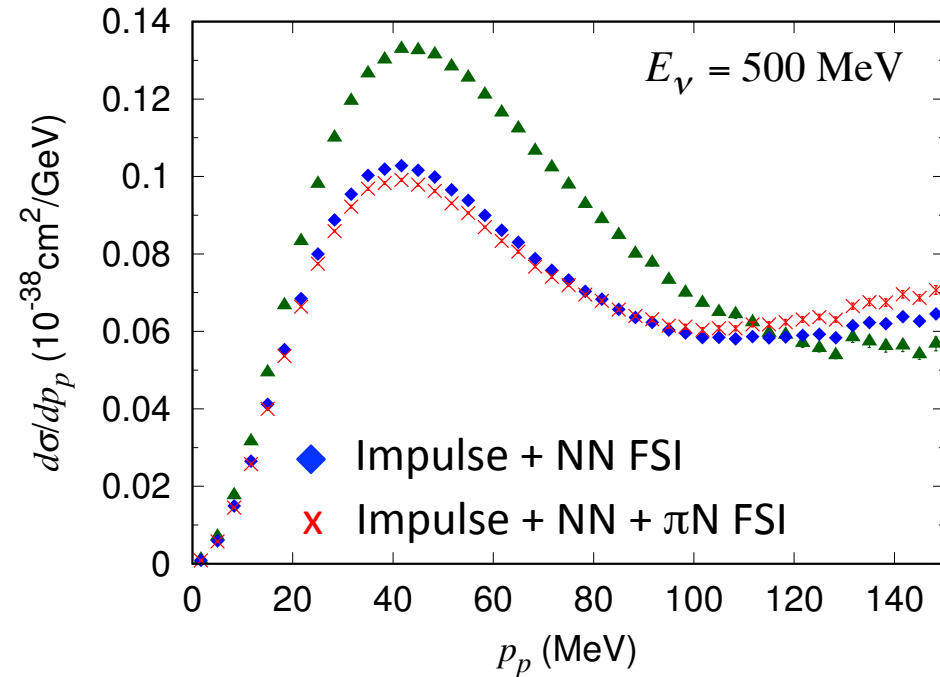
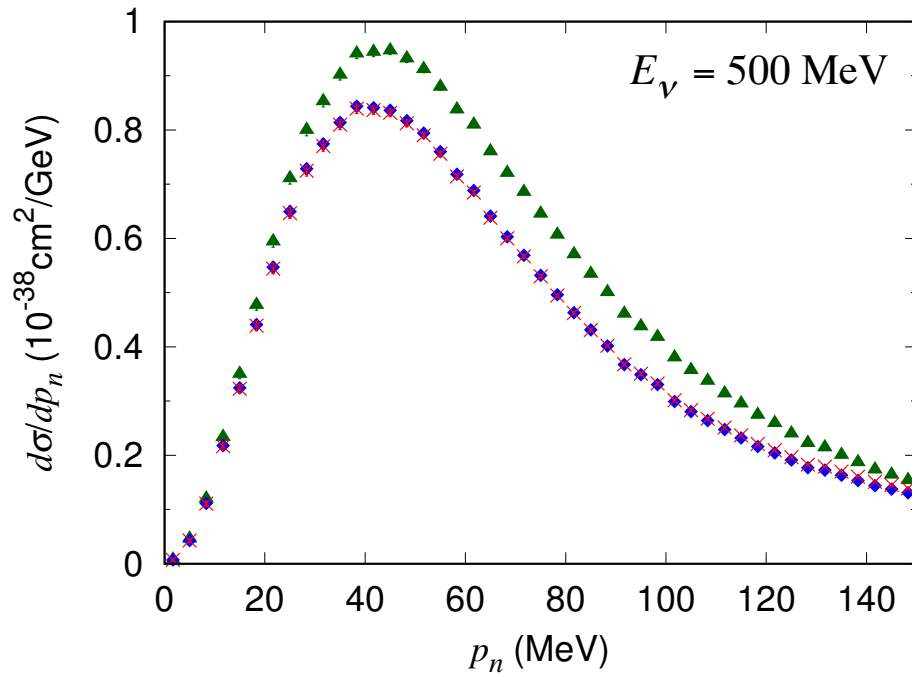
Small  $p_s$  region

Larger contamination of  $\nu_\mu p \rightarrow \mu \pi^+ p$  in quasi-free neutron (small  $p_p$ ) region

$$\leftarrow \sigma(\nu_\mu p \rightarrow \mu \pi^+ p) \approx 9 \times \sigma(\nu_\mu n \rightarrow \mu \pi^+ n)$$

$\nu_\mu d \rightarrow \mu^- \pi^+ p n$  spectator momentum distribution

## FSI effect



**Naïve expectation** : FSI affects high  $p_s$  region, leaving small  $p_s$  region unchanged

**Reality** : FSI significantly reduces spectrum in small  $p_s$  (quasi-free peak) region

large NN FSI effect  $\leftarrow$  orthogonality between NN scattering state and deuteron

FSI effect is small for  $\nu_\mu d \rightarrow \mu \pi^0 p p$  spectator momentum distribution



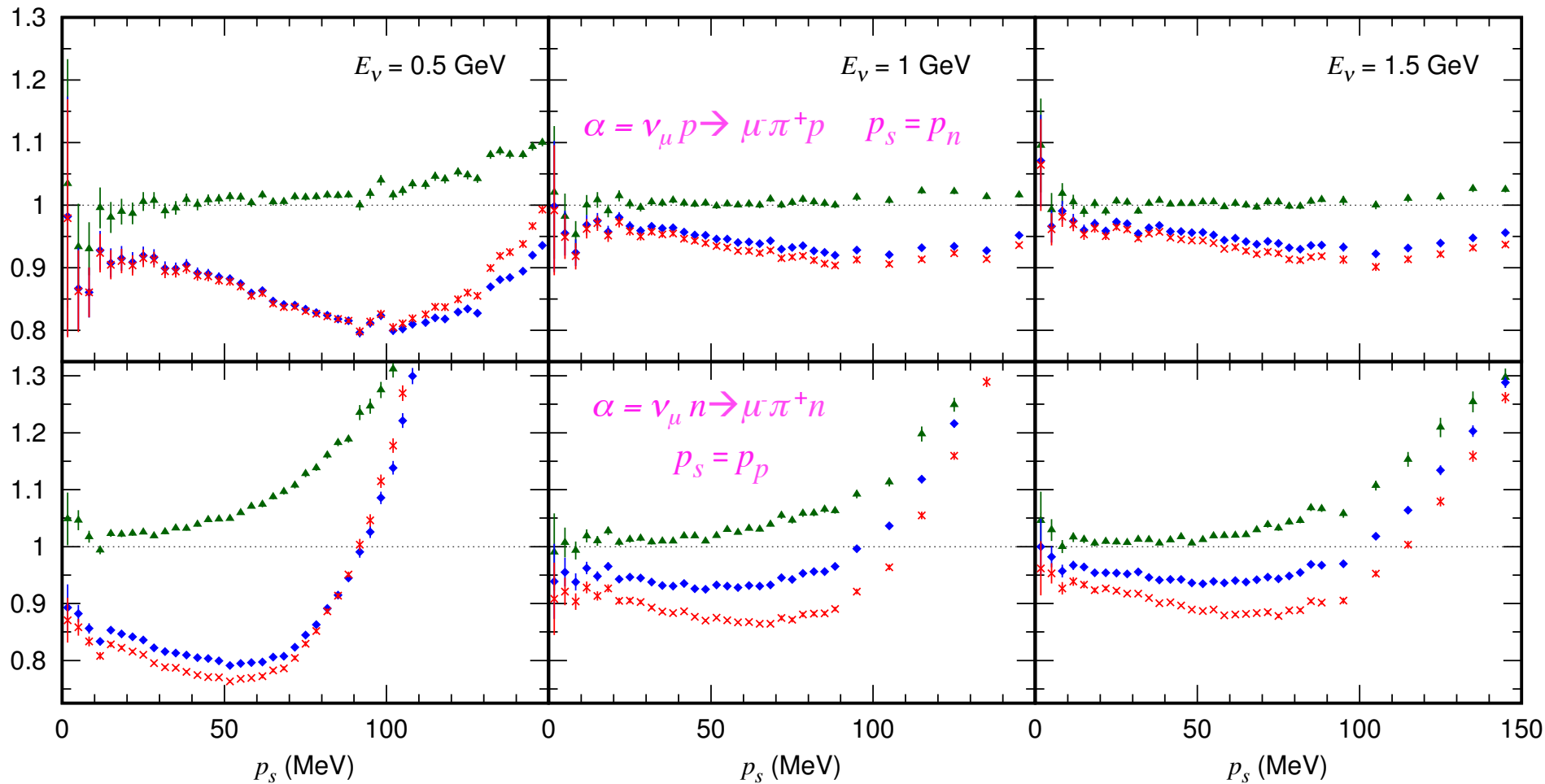
$$N_{\alpha}(E_{\nu}, p_s) \equiv \frac{d\sigma_{\nu d}(E_{\nu}) / dp_s}{d\tilde{\sigma}_{\alpha}(E_{\nu}) / dp_s}$$

Ratio of spectator momentum distribution  
and convoluted cross section

Other nucleon's contribution and FSI effects on the spectator momentum distributions  
can be seen more clearly and quantitatively

$$N_\alpha(E_\nu, p_s) \equiv \frac{d\sigma_{\nu d}(E_\nu) / dp_s}{d\tilde{\sigma}_\alpha(E_\nu) / dp_s}$$

- ▲ Impulse
- ◆ Impulse + NN FSI
- × Impulse + NN +  $\pi$ N FSI

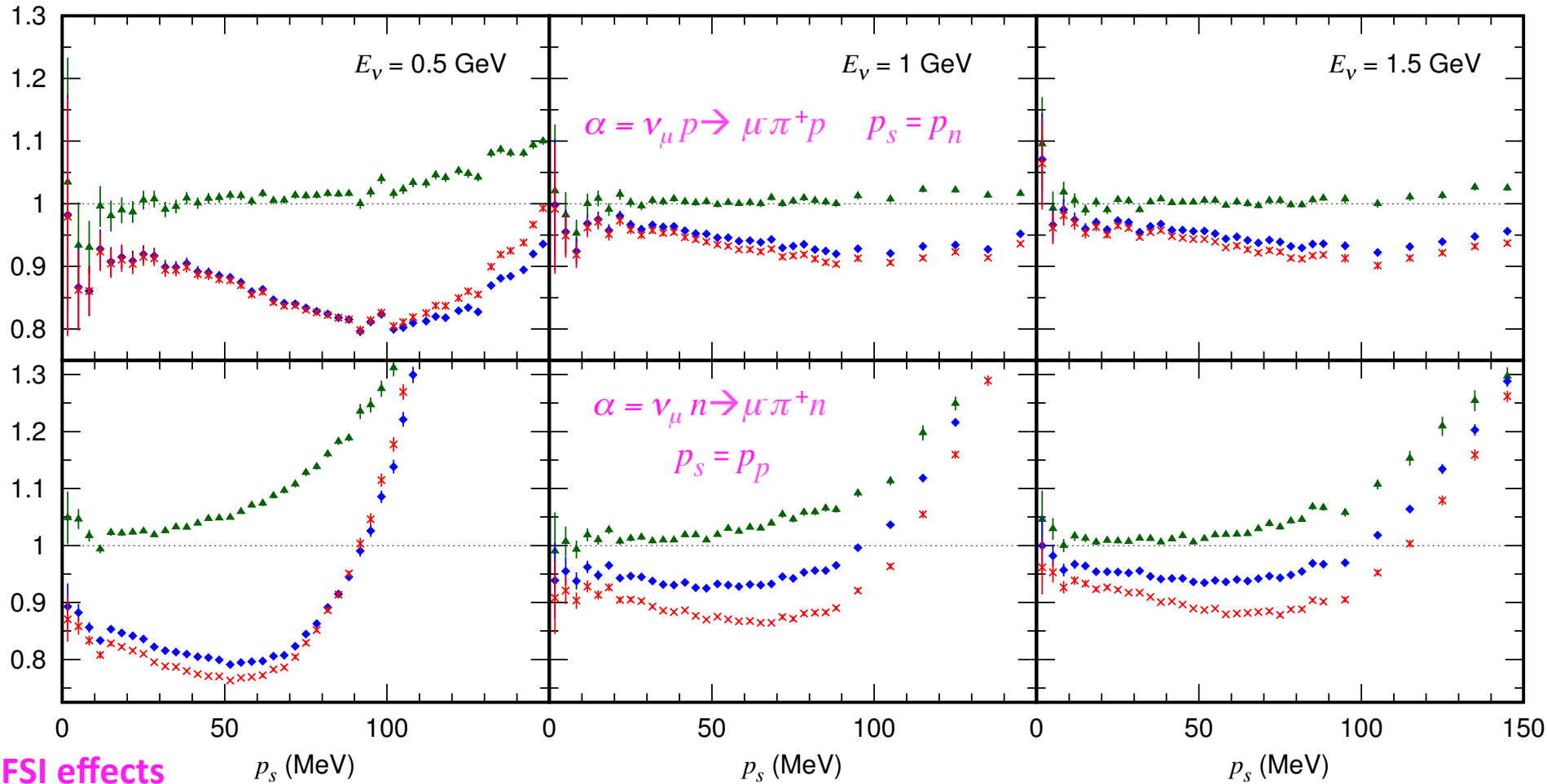


$N_\alpha(E_\nu, p_s) \approx 1 \rightarrow$  quasi-free process dominates

$\neq 1 \rightarrow$  other nucleon's contribution and/or FSI

$$N_\alpha(E_\nu, p_s) \equiv \frac{d\sigma_{\nu d}(E_\nu) / dp_s}{d\tilde{\sigma}_\alpha(E_\nu) / dp_s}$$

- ▲ Impulse
- ◆ Impulse + NN FSI
- × Impulse + NN +  $\pi$ N FSI



### FSI effects

- NN FSI effect is larger for smaller  $E_\nu$
- $\pi$ N FSI is large correction to quasi-free  $\nu_\mu n \rightarrow \mu \pi^+ n$  ;  $\sigma(\pi^+ p \rightarrow \pi^+ p) \approx 9 \times \sigma(\pi^+ n \rightarrow \pi^+ n)$
- FSI effects depend on spectator momentum

$$N_\alpha(E_\nu, p_s) \equiv \frac{d\sigma_{\nu d}(E_\nu)/dp_s}{d\tilde{\sigma}_\alpha(E_\nu)/dp_s}$$

Phenomenological formula fitted to  $N_\alpha(E_\nu, p_s)$  is practically useful

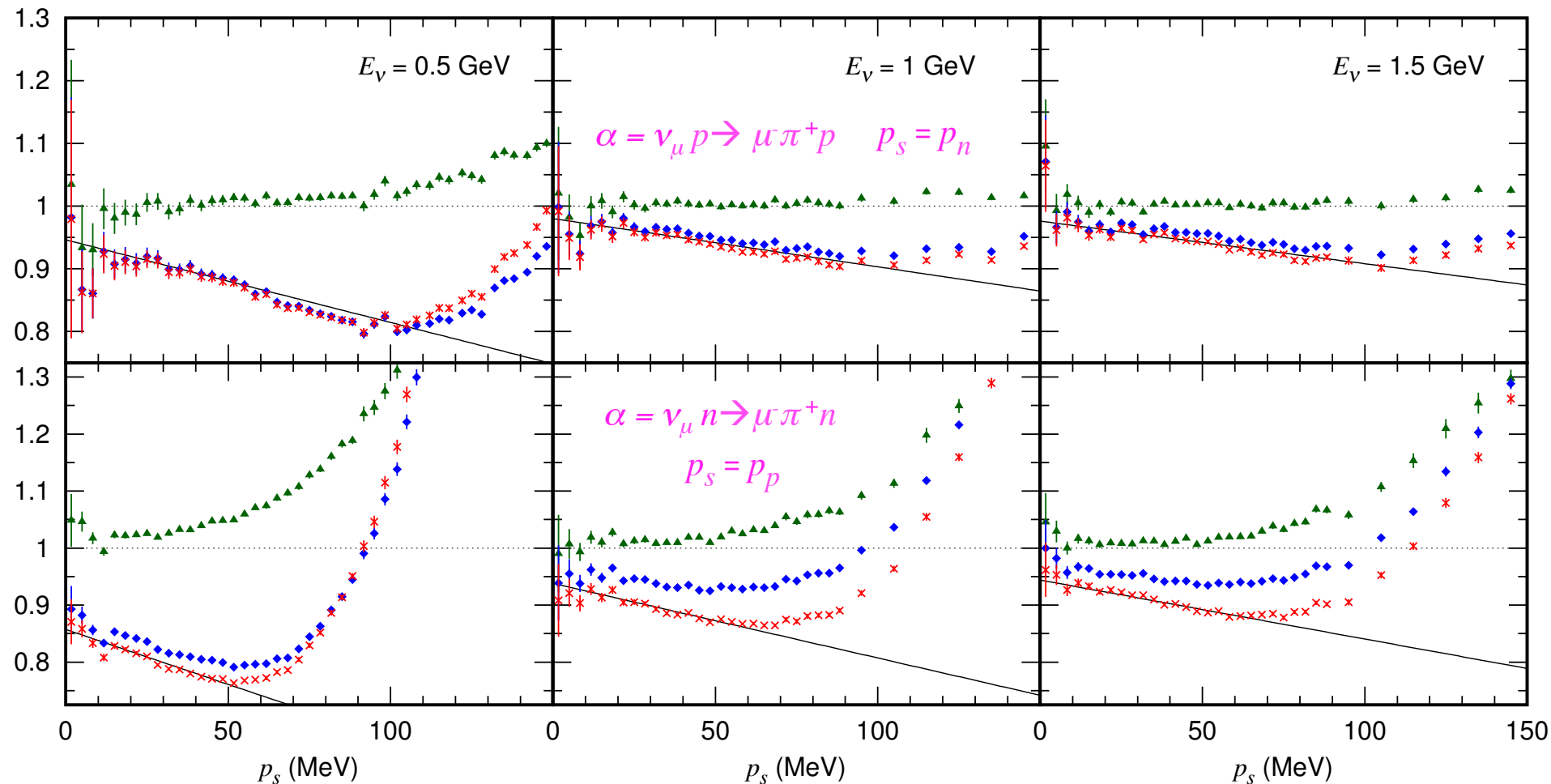
- From  $d\sigma_{\nu d}(E_\nu)/dp_s$  data,  $d\tilde{\sigma}_\alpha(E_\nu)/dp_s$  can be extracted with FSI taken into account
- Model can be easily tested against  $d\tilde{\sigma}_\alpha(E_\nu)/dp_s$
- $d\sigma_{\nu d}(E_\nu)/dp_s$  data may be obtained in future neutrino-deuteron experiment

INT embedded workshop, June 25-29, 2018

- $N_\alpha(E_\nu, p_s)$  is ratio  
 → model dependence from using DCC  $\nu_\mu N \rightarrow \mu\pi N$  model is expected to be small

$$N_\alpha(E_\nu, p_s) \equiv \frac{d\sigma_{\nu d}(E_\nu) / dp_s}{d\tilde{\sigma}_\alpha(E_\nu) / dp_s}$$

- ▲ Impulse
- ◆ Impulse + NN FSI
- × Impulse + NN +  $\pi$ N FSI



$$N_\alpha^{\text{fit}}(E_\nu, p_s) = A_\alpha(E_\nu) + B_\alpha(E_\nu)p_s \quad A_\alpha(x) = \frac{a_\alpha x^2 + b_\alpha x + c_\alpha}{x^2 + d_\alpha x + e_\alpha}, \quad B_\alpha(x) = \frac{f_\alpha x + g_\alpha}{x + h_\alpha}$$

Parameters ( $a_\alpha - h_\alpha$ ) are fitted to  $N_\alpha(E_\nu, p_s)$  over  $p_s < 50 \text{ MeV}$  and  $0.4 < E_\nu < 2 \text{ GeV}$

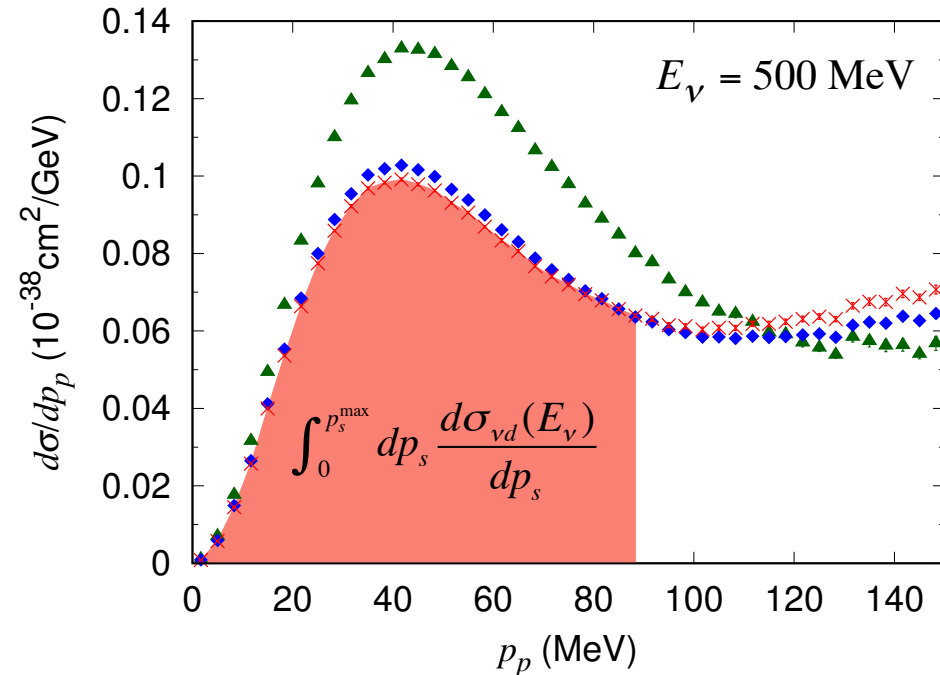
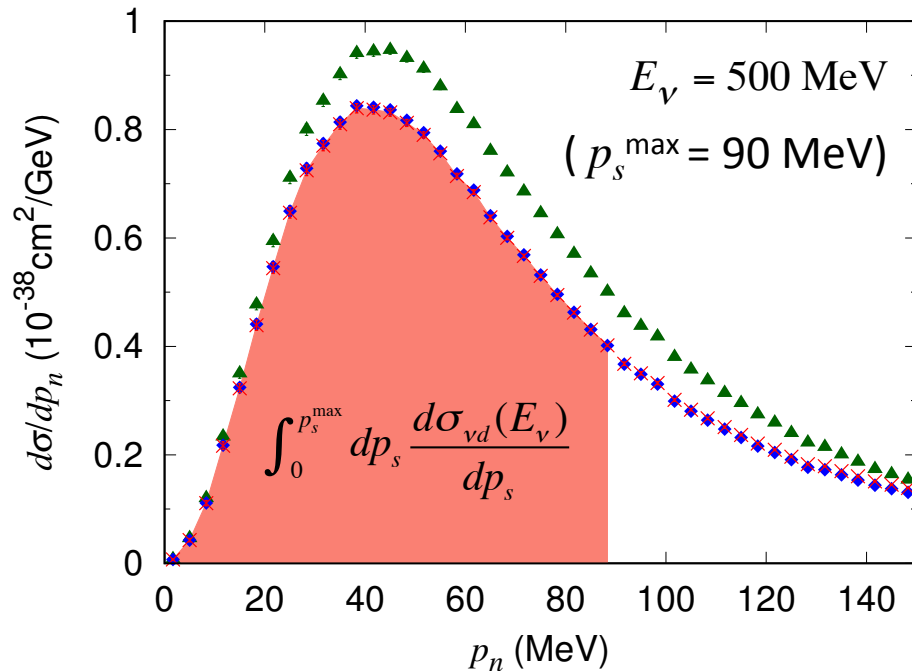
# $\nu_{\mu} N \rightarrow \mu^{-} \pi N$ cross section data corrected for FSI and Fermi-motion

- Significant FSI effects on spectator momentum distributions of  $\nu_{\mu} d \rightarrow \mu^{-} \pi^{+} p n$  in quasi-free peak region
- (Flux-corrected) ANL and BNL data have not been corrected for FSI but need to be
- We extract  $\nu_{\mu} N \rightarrow \mu^{-} \pi N$  cross section from flux-corrected ANL and BNL data by further correcting it for FSI and Fermi-motion
- Details of ANL and BNL analyses have been lost  
→ A reasonable assumption needs to be made

# $\nu_\mu N \rightarrow \mu^- \pi N$ cross section data corrected for FSI and Fermi-motion

**Procedure** (temporary; still under study)

1. Fit  $d\sigma_{\nu d}(E_\nu)/dp_s$  with  $\sigma_{\nu N}^{\text{fit}}(E_\nu)$  so that  $\int_0^{p_s^{\text{max}}} dp_s \frac{d\sigma_{\nu d}(E_\nu)}{dp_s} \approx \int_0^{p_s^{\text{max}}} d^3 p_s \sigma_{\nu N}^{\text{fit}}(E_\nu) |\Psi_d(\vec{p}_s)|^2$



# $\nu_\mu N \rightarrow \mu^- \pi N$ cross section data corrected for FSI and Fermi-motion

**Procedure** (temporary; still under study)

1. Fit  $d\sigma_{\nu d}(E_\nu)/dp_s$  with  $\sigma_{\nu N}^{\text{fit}}(E_\nu)$  so that  $\int_0^{p_s^{\text{max}}} dp_s \frac{d\sigma_{\nu d}(E_\nu)}{dp_s} \approx \int_0^{p_s^{\text{max}}} d^3 p_s \sigma_{\nu N}^{\text{fit}}(E_\nu) |\Psi_d(\vec{p}_s)|^2$

**Assumption:**

For  $p_s < p_s^{\text{max}}$  (small  $p_s$  region including quasi-free peak),

$d\sigma_{\nu d}(E_\nu)/dp_s$  is from quasi-free  $\nu_\mu N \rightarrow \mu^- \pi N$  process (no effect from the other nucleon)

and mostly follows Fermi motion shape,  $|\Psi_d(\vec{p}_s)|^2$

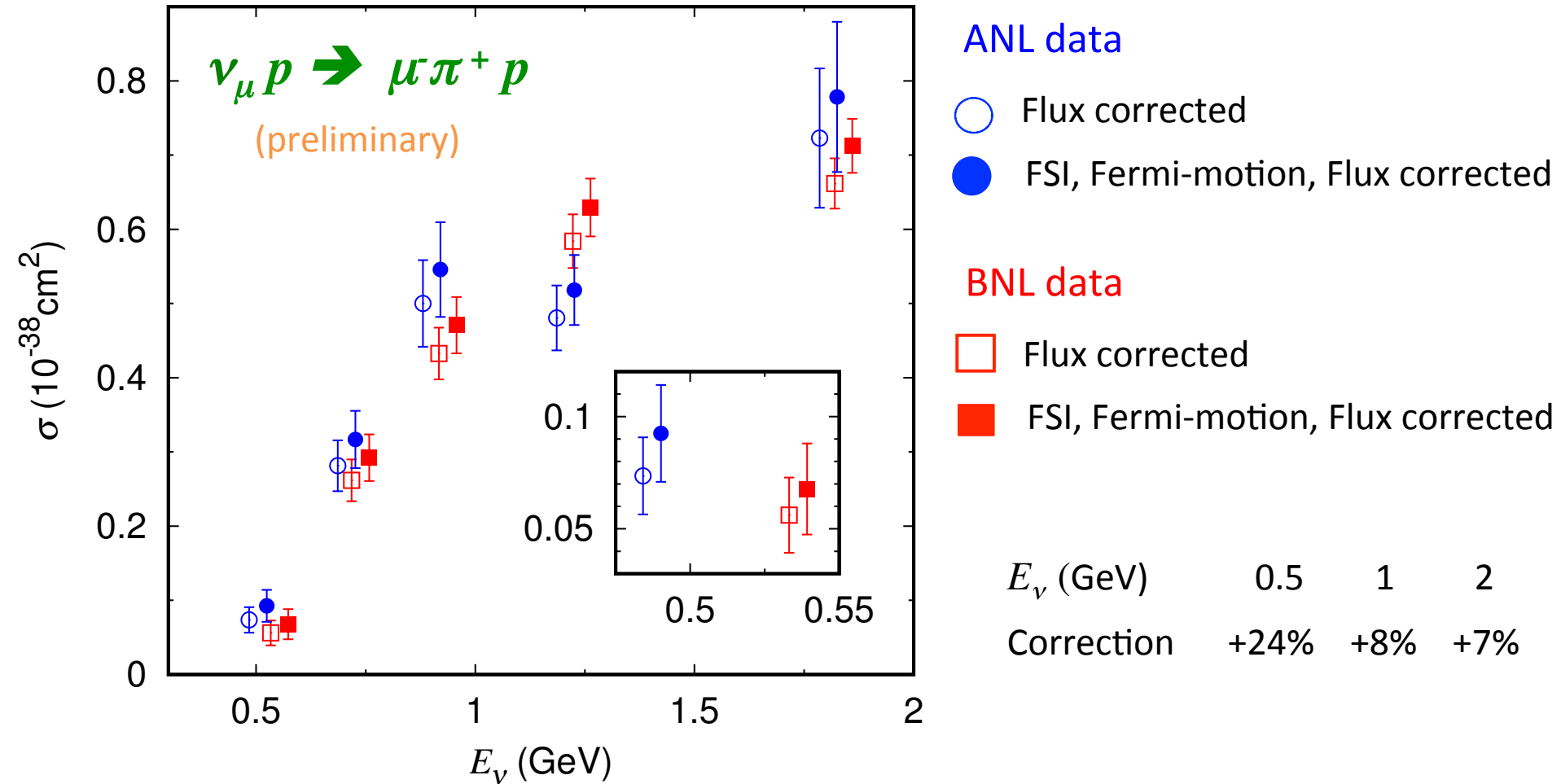


# $\nu_\mu N \rightarrow \mu^- \pi N$ cross section data corrected for FSI and Fermi-motion

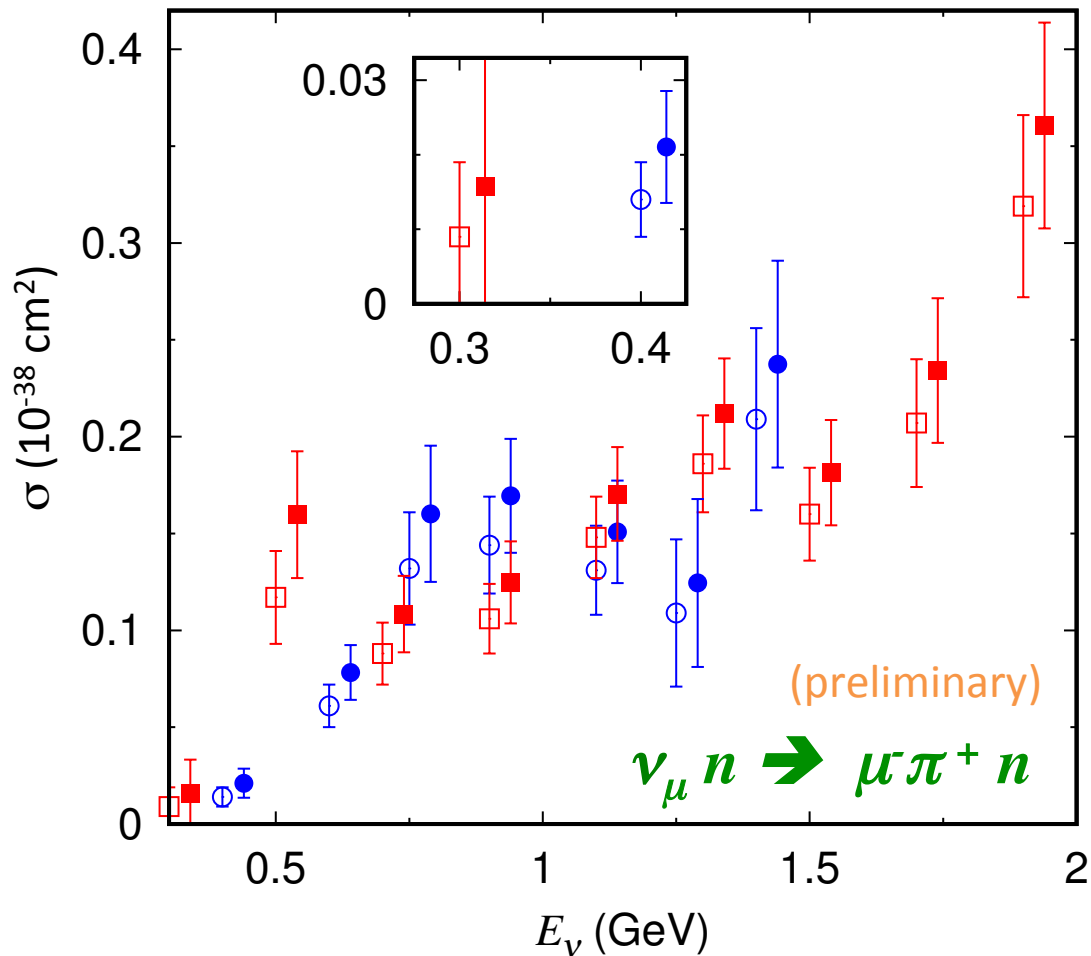
**Procedure** (temporary; still under study)

1. Fit  $d\sigma_{\nu d}(E_\nu)/dp_s$  with  $\sigma_{\nu N}^{\text{fit}}(E_\nu)$  so that  $\int_0^{p_s^{\text{max}}} dp_s \frac{d\sigma_{\nu d}(E_\nu)}{dp_s} \approx \int_0^{p_s^{\text{max}}} d^3 p_s \sigma_{\nu N}^{\text{fit}}(E_\nu) |\Psi_d(\vec{p}_s)|^2$
2. Ratio  $\sigma_{\nu N}(E_\nu)/\sigma_{\nu N}^{\text{fit}}(E_\nu)$  is the correction factor to be multiplied to  
flux-corrected ANL and BNL data ( PRD 90, 112017 (2014), EPJC 76, 474 (2016) )  
(  $\sigma_{\nu N}(E_\nu)$  : DCC  $\nu_\mu N \rightarrow \mu^- \pi N$  model )

# $\nu_\mu N \rightarrow \mu\pi N$ cross section data corrected for FSI and Fermi-motion



# $\nu_\mu N \rightarrow \mu^- \pi N$ cross section data corrected for FSI and Fermi-motion



ANL data

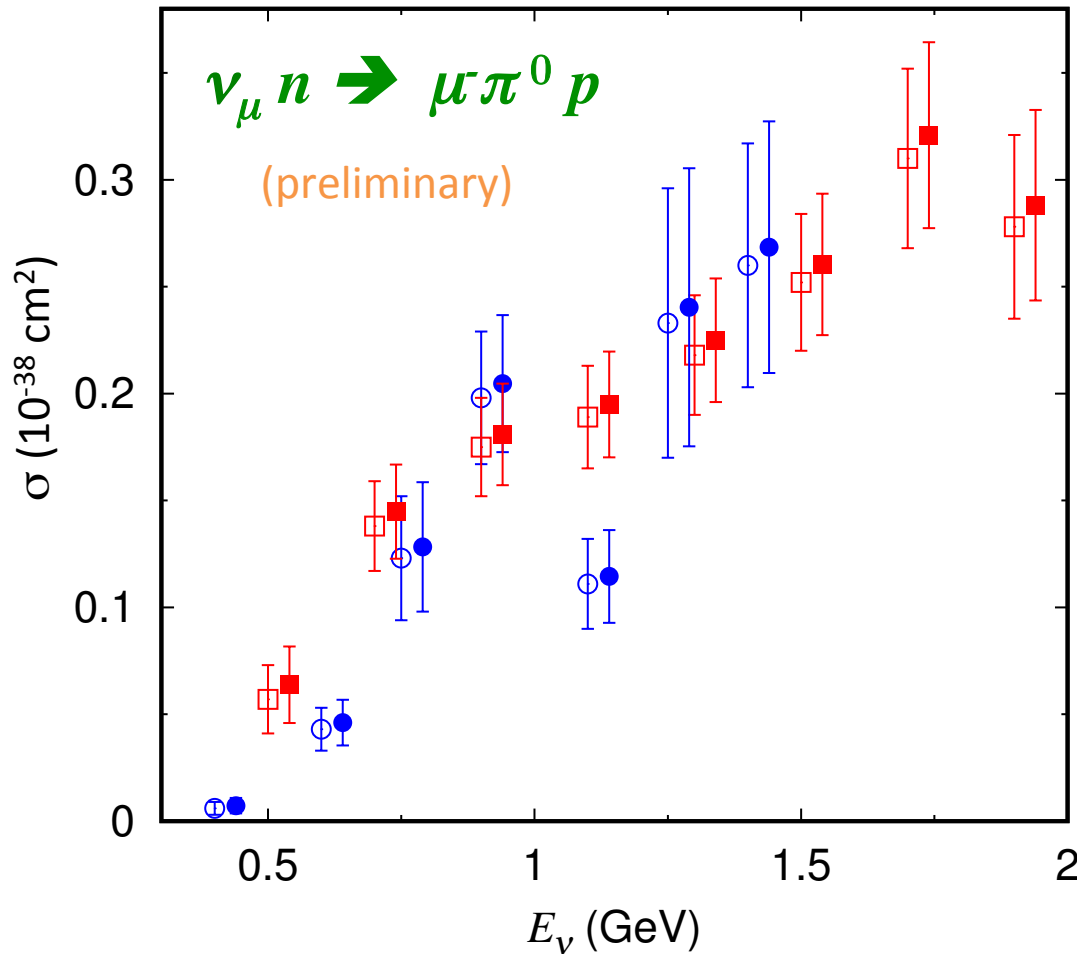
- Flux corrected
- FSI, Fermi-motion, Flux corrected

BNL data

- Flux corrected
- FSI, Fermi-motion, Flux corrected

$E_\nu$ (GeV)	0.5	1	2
Correction	+37%	+16%	+13%

# $\nu_\mu N \rightarrow \mu \pi N$ cross section data corrected for FSI and Fermi-motion



ANL data

- Flux corrected
- FSI, Fermi-motion, Flux corrected

BNL data

- Flux corrected
- FSI, Fermi-motion, Flux corrected

$E_\nu$ (GeV)	0.5	1	2
Correction	+12%	+3%	+4%

# Summary

# Summary

- $\nu_\mu d \rightarrow \mu^- \pi NN$  cross sections of the whole phase-space are calculated with a dynamical model including FSI ; for the first time
- Examined FSI effect on spectator momentum distribution  $d\sigma/dp_s$
- Found a useful recipe to extract  $\nu_\mu N \rightarrow \mu^- \pi N$  cross sections from  $\nu_\mu d \rightarrow \mu^- \pi NN$  spectator momentum distribution (from future exp.)
- Extracted  $\nu_\mu N \rightarrow \mu^- \pi N$  total cross sections by correcting (flux-corrected) ANL and BNL data for FSI and Fermi motion (preliminary)

## Future impact

- Significantly improved elementary  $\nu_\mu N \rightarrow \mu^- \pi N$  model to be implemented in neutrino-nucleus reaction model for oscillation experiments of the precision era

Thank you very much  
for your attention

## Acknowledgments

- Financial support for this work

KAKENHI JP25105010

FAPESP 2016/15618-8

- Computing resource

SR16000 at YITP in Kyoto University

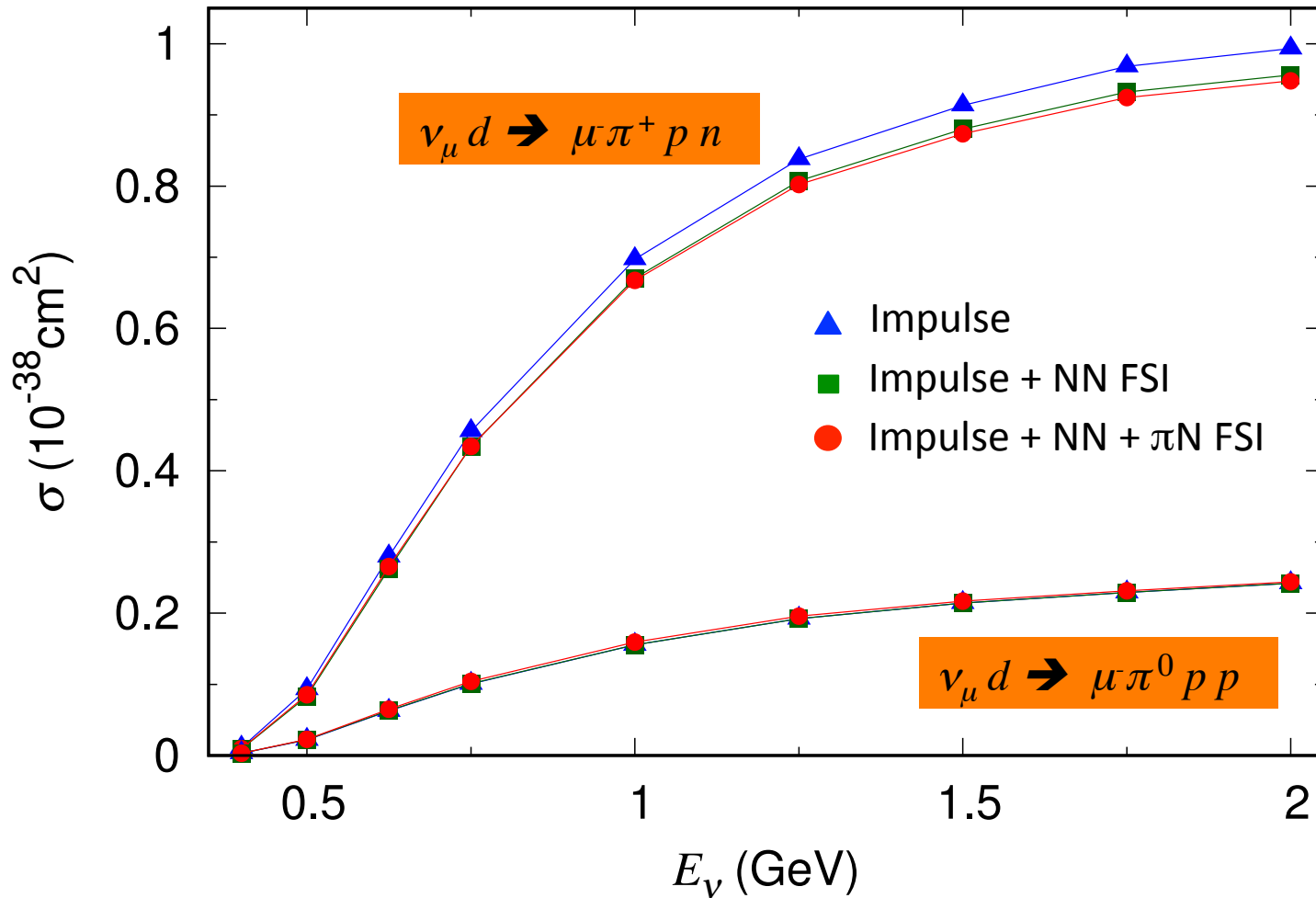
Bebop at Argonne National Laboratory

Cori at National Energy Research Scientific Computing Center

BACKUP

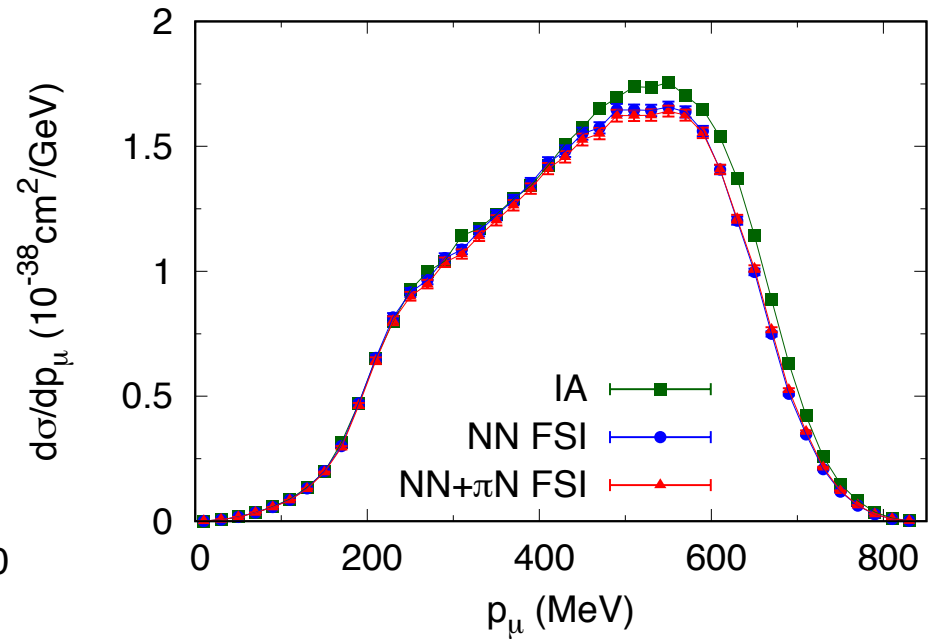
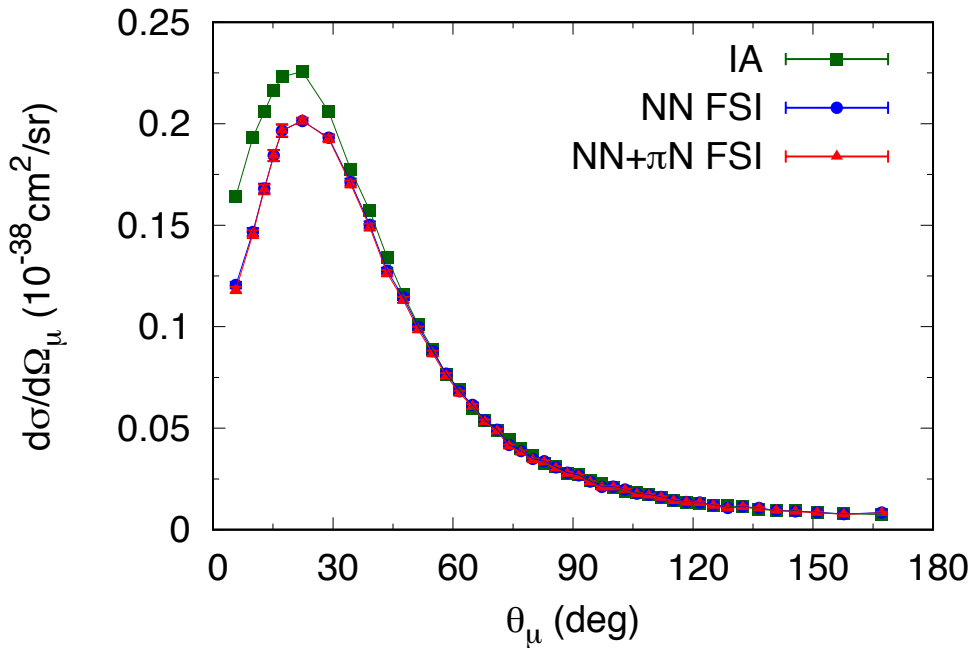


# $\nu_\mu d \rightarrow \mu^- \pi NN$ total cross sections

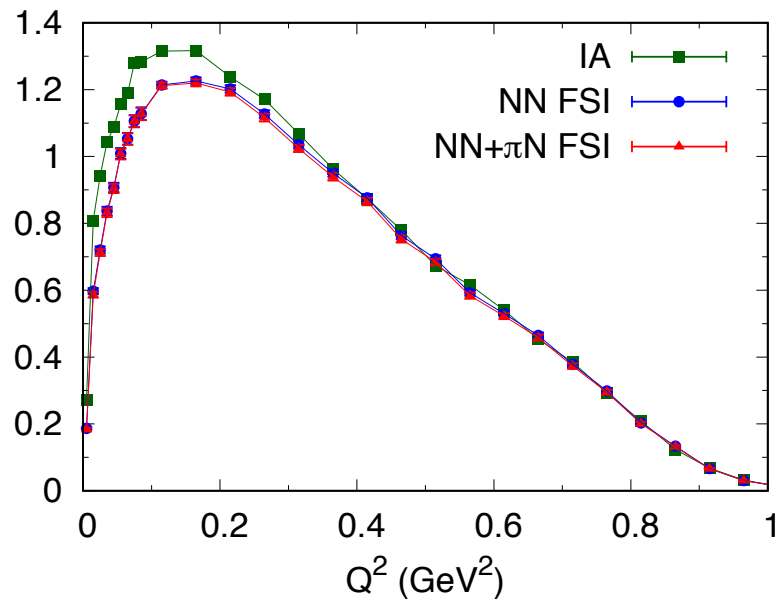
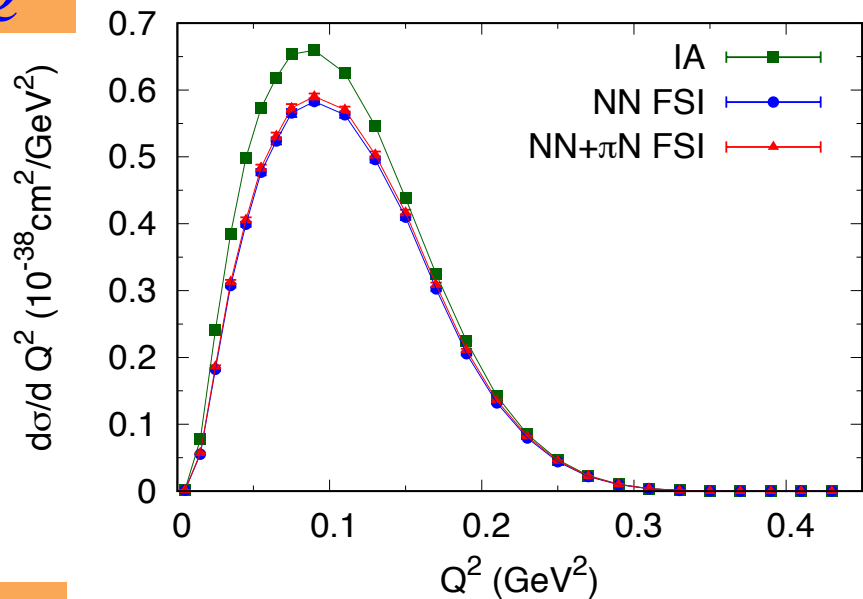
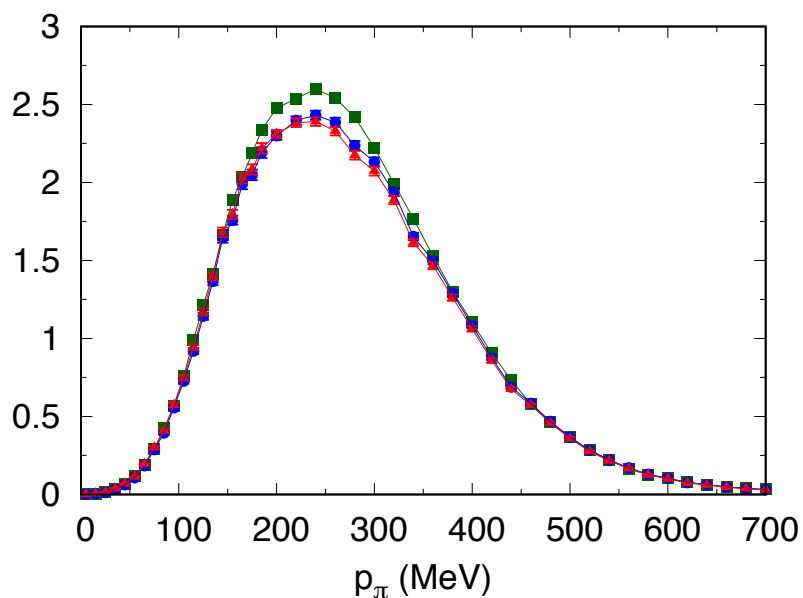
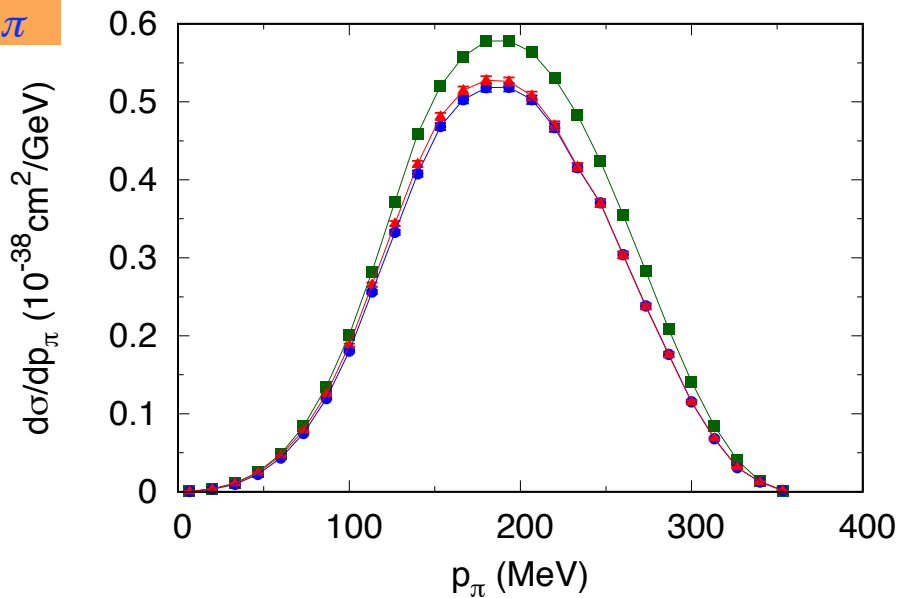


- (Mostly NN) FSI reduces  $\sigma$  by 10%, 6%, 5% at  $E_\nu = 0.5, 1, 1.5$  GeV
- $\pi N$  FSI hardly changes  $\sigma(\nu_\mu d \rightarrow \mu \pi^+ p n)$
- FSI effects are very small for  $\sigma(\nu_\mu d \rightarrow \mu \pi^0 p p)$

$d\sigma/d\Omega_\mu$  and  $d\sigma/dp_\mu$  for  $\nu_\mu d \rightarrow \mu \pi^+ p n$  at  $E_\nu = 1$  GeV

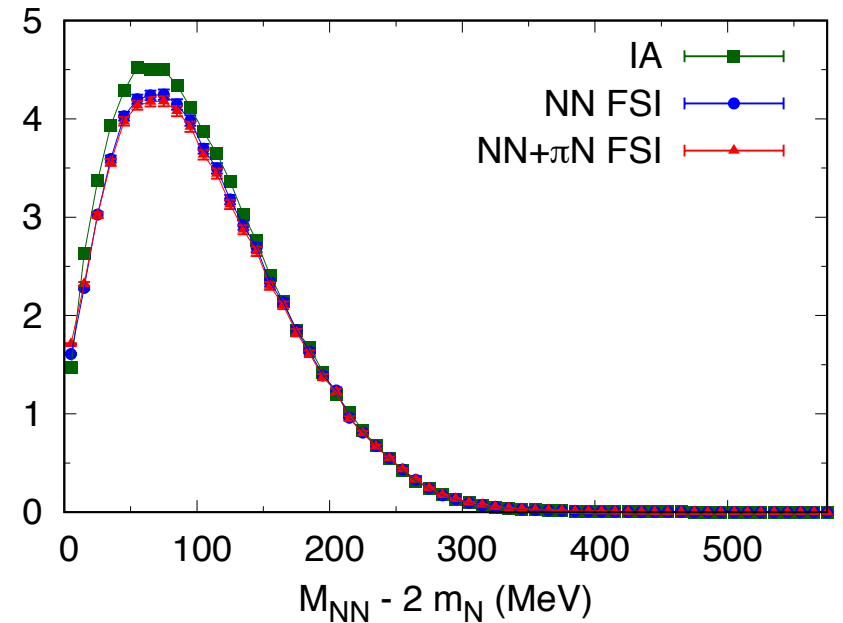
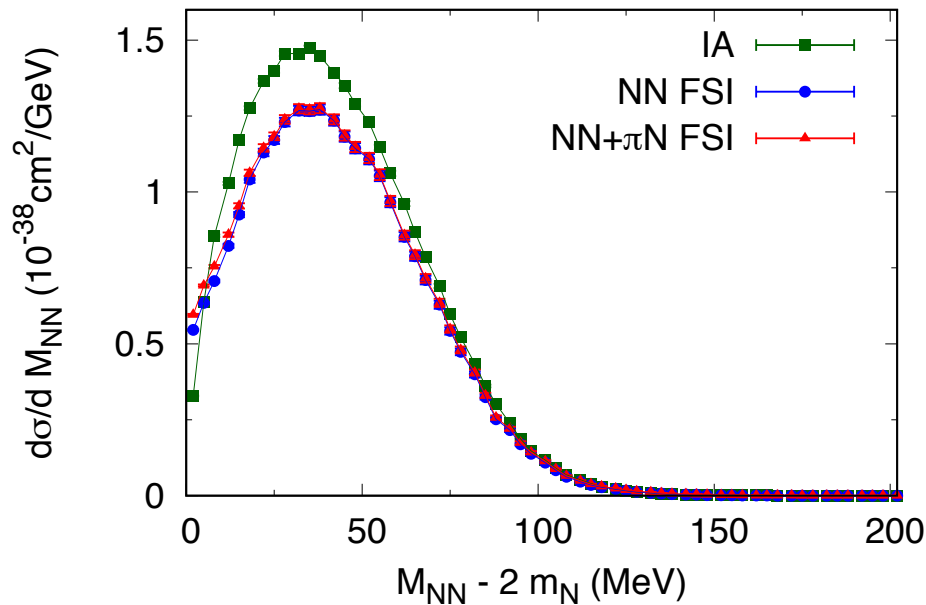


- Significant FSI effects are seen in narrow kinematical windows  
→ moderate reduction of total cross sections

$E_\nu = 0.5 \text{ GeV}$ vs  $E_\nu = 1 \text{ GeV}$  $Q^2$  $p_\pi$ 

$E_\nu = 0.5 \text{ GeV}$ 

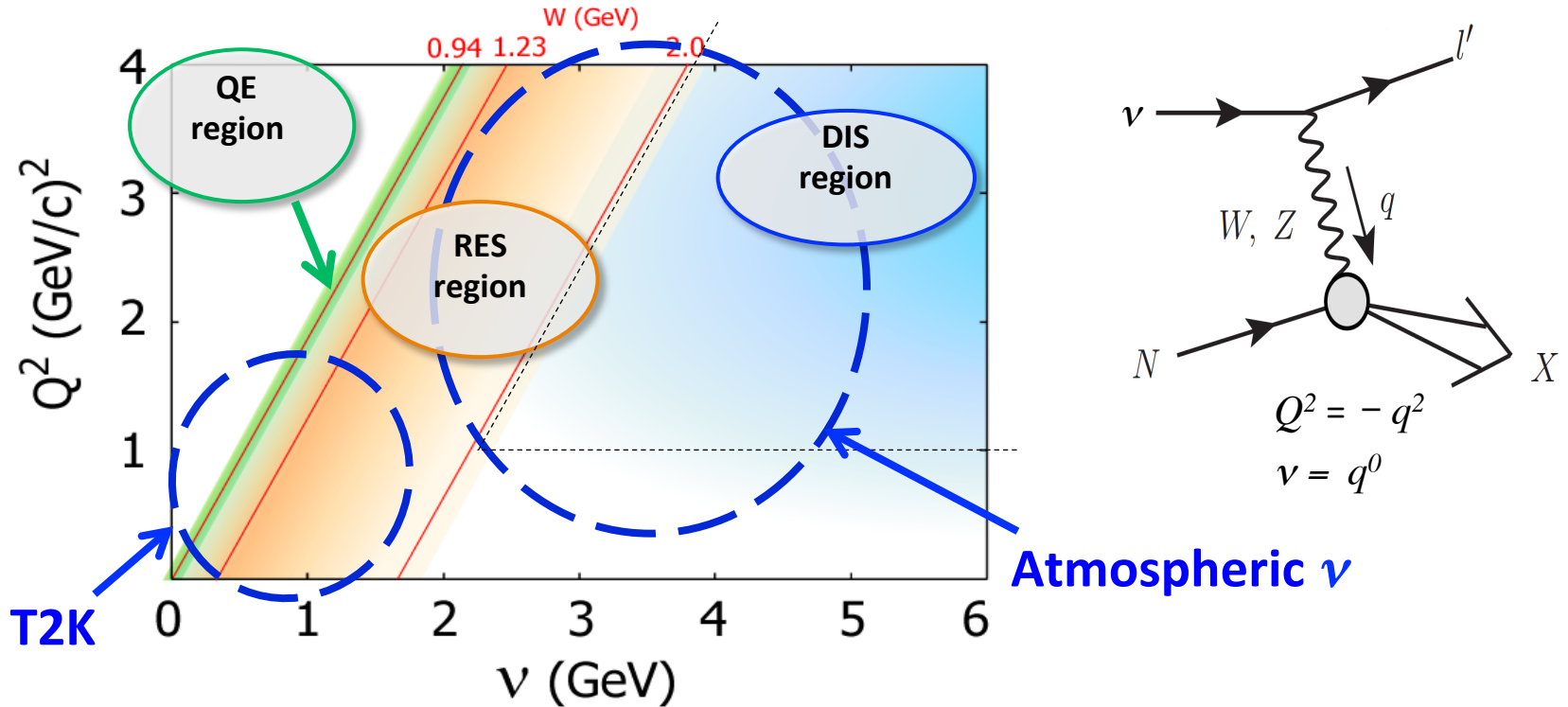
vs

 $E_\nu = 1 \text{ GeV}$ 

- NN FSI effect is large at low NN energy region ( $\lesssim 50 \text{ MeV}$ ) where orthogonality between  $pn$  scattering states and deuteron is most effective
  - Low NN energy region occupies a relatively larger portion of phase-space for low  $E_\nu$
- Larger NN FSI effect for low  $E_\nu$

# Neutrino-nucleus scattering for $\nu$ -oscillation experiments

Wide kinematical region with different characteristic  $\rightarrow$  Different expertise need integrated



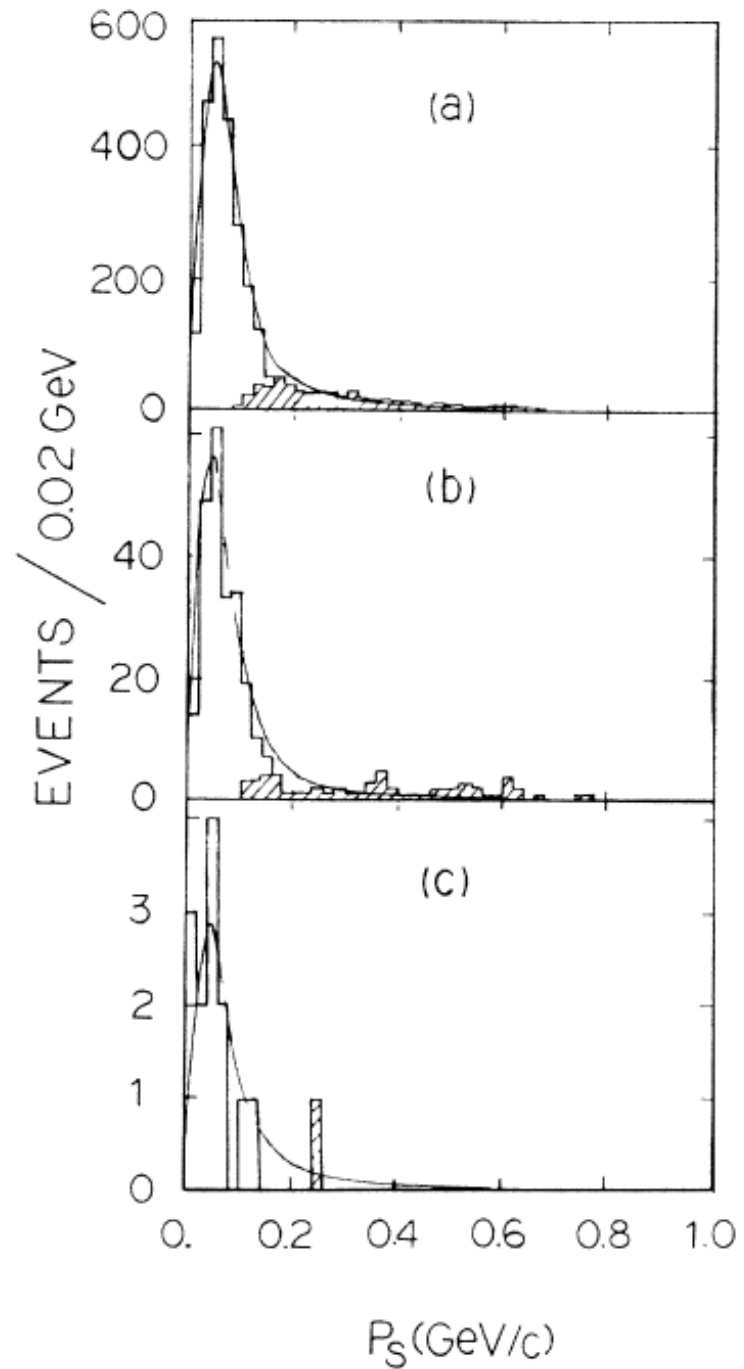
Collaboration at J-PARC Branch of KEK Theory Center

Current status reviewed in *Reports on Progress in Physics* **80** (2017) 056301

“Towards a Unified Model of Neutrino-Nucleus Reactions for Neutrino Oscillation Experiments”

# BNL analysis

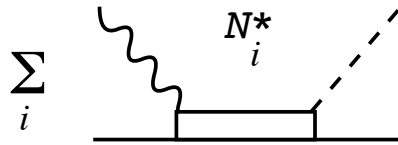
PRD 34, 2554 (1986)



# Previous models for $\nu$ -induced $1\pi$ production in resonance region

resonant only

Rein et al. (1981), (1987); Lalalulich et al. (2005), (2006)



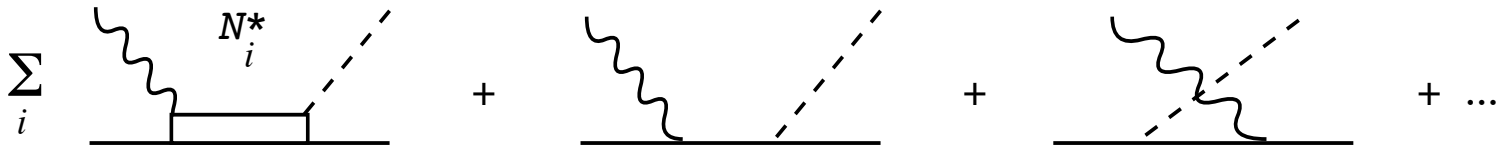
$VNN^*$  : helicity amplitudes listed in PDG

$ANN^*$  : quark model, PCAC relation to  $|\pi NN^*|$  (PDG)

relative phases among  $N^*$ 's are out of control

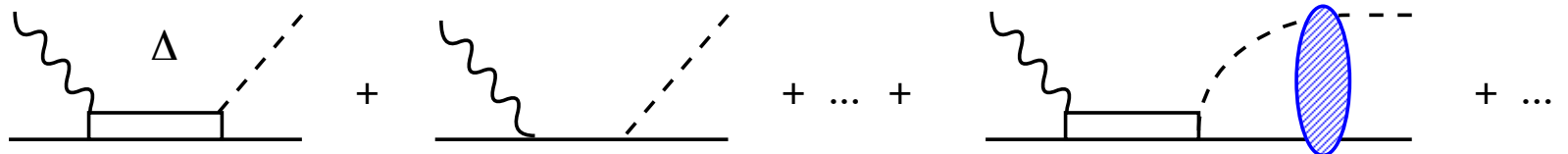
+ non-resonant (tree-level non-res)

Hernandez et al. (2007), (2010); Lalakulich et al. (2010)



+ rescattering ( $\pi N$  unitarity,  $\Delta(1232)$  region)

Sato, Lee (2003), (2005)



# DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

Kamano et al., PRC **88**, 035209 (2013)

Coupled-channel Lippmann-Schwinger equation for meson-baryon scattering

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$

$$\{a, b, c\} = \pi N, \eta N, \pi\pi N, \pi\Delta, \sigma N, \rho N, K\Lambda, K\Sigma$$

By solving the LS equation, coupled-channel unitarity is fully taken into account



# DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

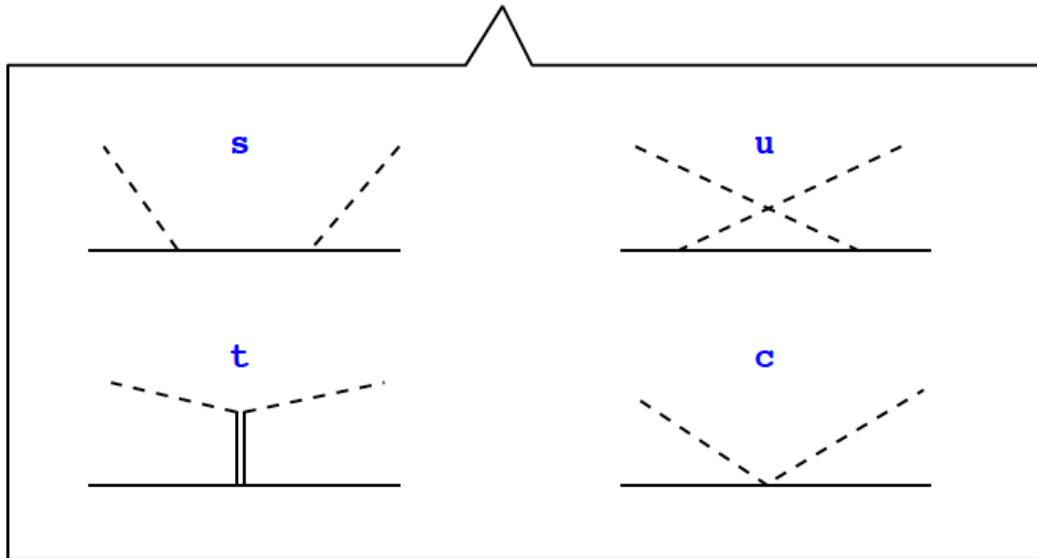
Kamano et al., PRC 88, 035209 (2013)

Coupled-channel Lippmann-Schwinger equation for meson-baryon scattering

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$

$$\mathbf{V}_{ab} = \text{[diagram 1]} + \text{[diagram 2]}$$

The diagram shows the vertex  $\mathbf{V}_{ab}$  as the sum of two terms. The first term is a vertex with a solid horizontal line below and two dashed lines above meeting at a central black dot. The second term is a vertex with a solid horizontal line below, a rectangular box on the line, and two dashed lines above meeting at a central point labeled "bare N\*".



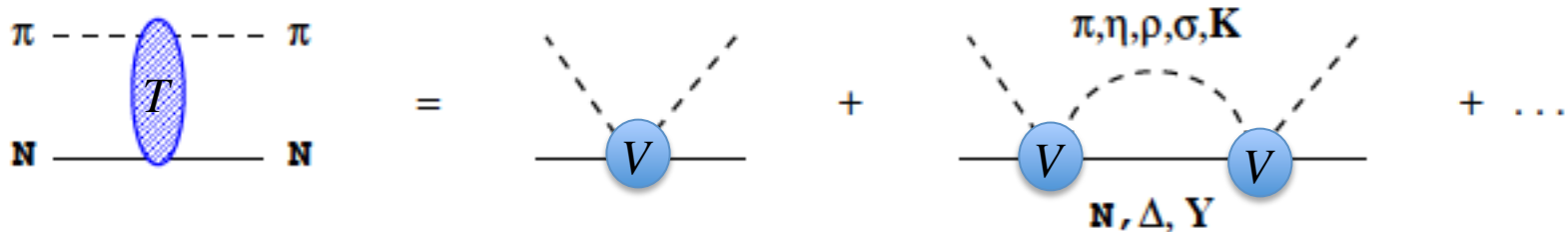
# DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

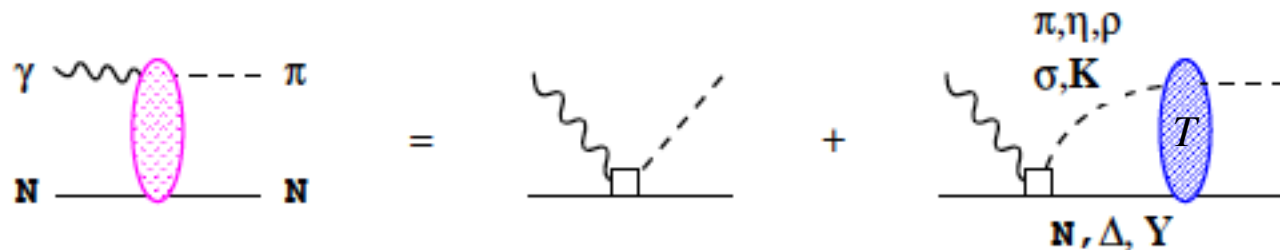
Kamano et al., PRC 88, 035209 (2013)

Coupled-channel Lippmann-Schwinger equation for meson-baryon scattering

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$



In addition,  $\gamma N$ ,  $W^\pm N$ ,  $ZN$  channels are included perturbatively



# Relation between neutrino and electron (photon) interactions

Charged-current (CC) interaction (e.g.  $\nu_\mu + n \rightarrow \mu^- + p$ )

$$L^{cc} = \frac{G_F V_{ud}}{\sqrt{2}} [J_\lambda^{cc} \ell_{cc}^\lambda + h.c.] \quad J_\lambda^{cc} = V_\lambda - A_\lambda \quad \ell_{cc}^\lambda = \bar{\psi}_\mu \gamma^\lambda (1 - \gamma_5) \psi_\nu$$

Electromagnetic interaction (e.g.  $\gamma^{(*)} + p \rightarrow p$ )

$$L^{em} = e J_\lambda^{em} A_{em}^\lambda \quad J_\lambda^{em} = V_\lambda + V_\lambda^{IS}$$

$V$  and  $V^{IS}$  in  $J^{em}$  can be separately determined by analyzing photon ( $Q^2=0$ ) and electron reaction ( $Q^2 \neq 0$ ) data on both proton and neutron targets, because:

$$\langle p | V_\lambda | p \rangle = - \langle n | V_\lambda | n \rangle \quad \langle p | V_\lambda^{IS} | p \rangle = \langle n | V_\lambda^{IS} | n \rangle$$

Matrix element for the weak vector current is obtained from analyzing electromagnetic processes

$$\langle p | V_\lambda | n \rangle = \sqrt{2} \langle p | V_\lambda | p \rangle$$

# DCC model for axial current

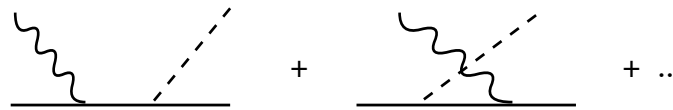
Because neutrino reaction data are scarce, axial current cannot be determined phenomenologically  
 → **Chiral symmetry** and **PCAC** (partially conserved axial current) are guiding principle

**PCAC relation**  $\langle X' | q \cdot A | X \rangle \sim i f_\pi \langle X' | T | \pi X \rangle$

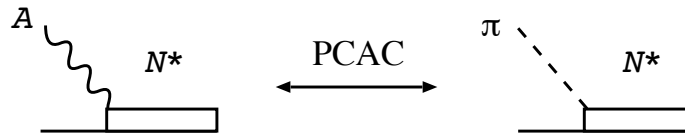
$Q^2=0$

non-resonant mechanisms

$$\partial_\mu \pi \rightarrow f_\pi A_\mu^{external}$$



resonant mechanisms



*Interference among resonances and background can be uniquely fixed within DCC model*

# DCC model for axial current

$Q^2 \neq 0$   $F_A(Q^2)$  : axial form factors

non-resonant mechanisms  $F_A(Q^2) = \left( \frac{1}{1 + Q^2 / M_A^2} \right)^2$   $M_A = 1.02 \text{ GeV}$

resonant mechanisms  $F_A(Q^2) = \left( \frac{1}{1 + Q^2 / M_A^2} \right)^2$

More neutrino data are necessary to fix axial form factors for  $ANN^*$

*Neutrino cross sections will be predicted with this axial current*

DCC analysis of  $\gamma N, \pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$

and electron scattering data

# DCC analysis of meson production data

Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

Fully combined analysis of  $\gamma N, \pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$  data

$d\sigma / d\Omega$  and polarization observables ( $W \leq 2.1$  GeV)

~ 23,000 data points are fitted

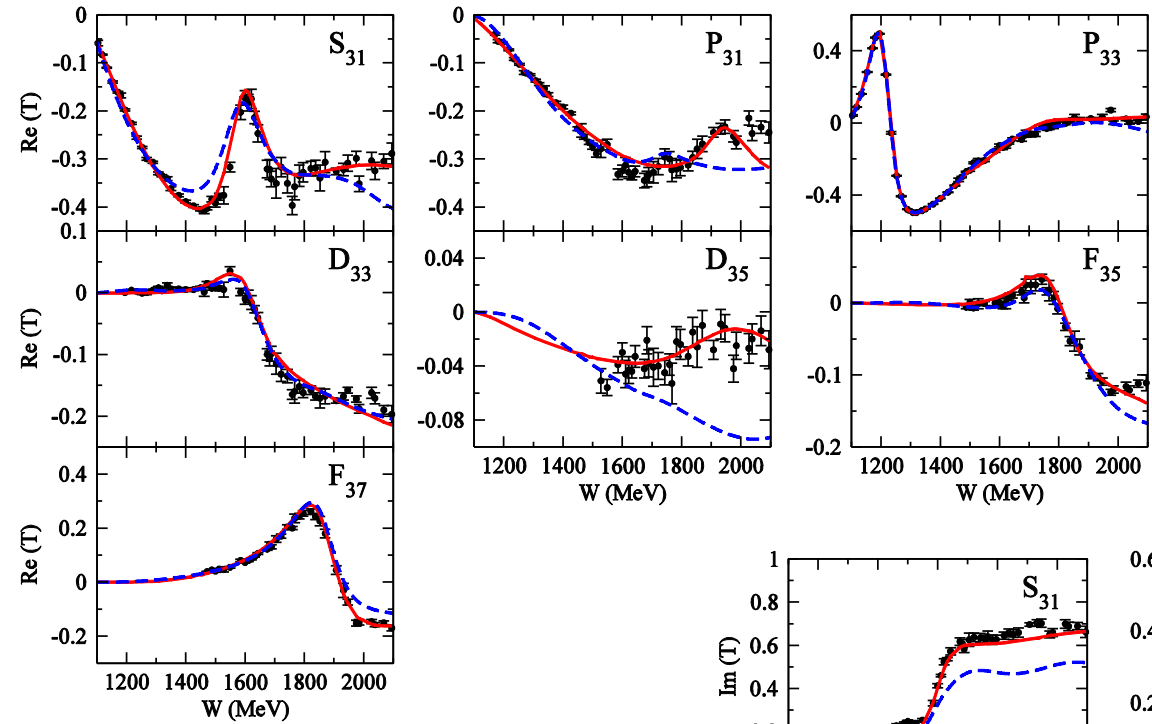
by adjusting parameters ( $N^*$  mass,  $N^* \rightarrow MB$  couplings, cutoffs)



Data for electron scattering on proton and neutron are analyzed by adjusting

$\gamma^* N \rightarrow N^*$  coupling strength at different  $Q^2$  values ( $Q^2 \leq 3$  (GeV/c)<sup>2</sup>)

# Partial wave amplitudes of $\pi N$ scattering



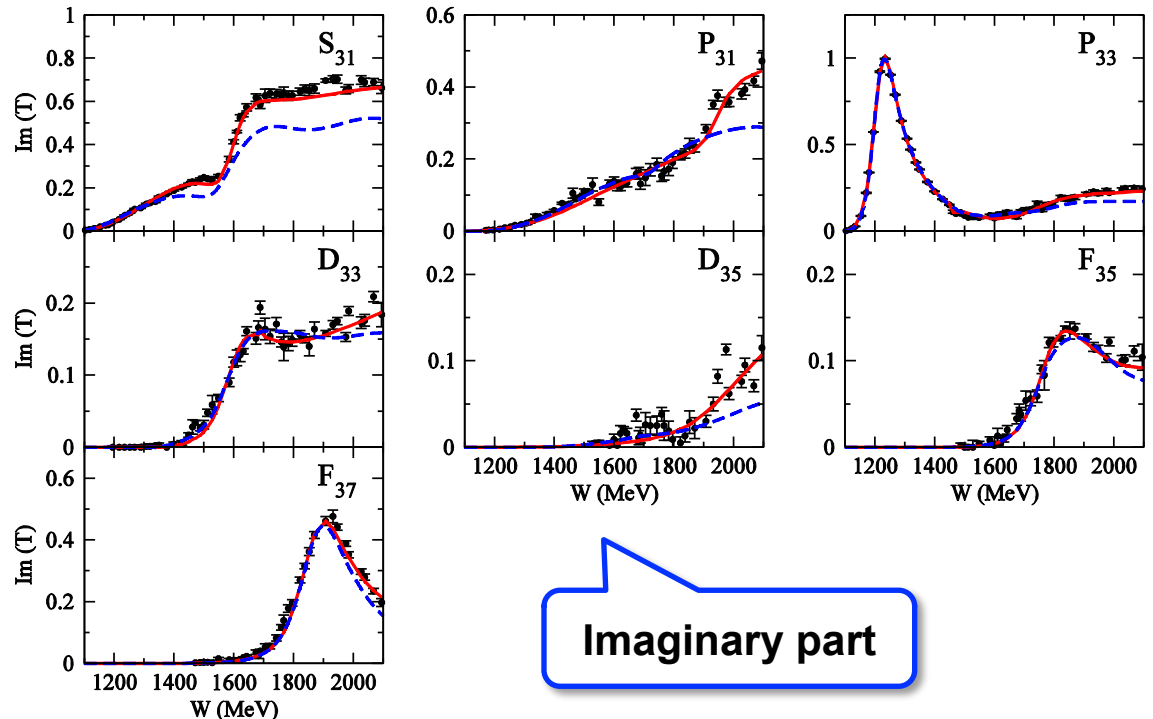
Real part

$$I = \frac{3}{2}$$

— Kamano, Nakamura, Lee, Sato,  
PRC 88 (2013)

- - - Previous model  
(fitted to  $\pi N \rightarrow \pi N$  data only)  
[PRC 76 065201 (2007)]

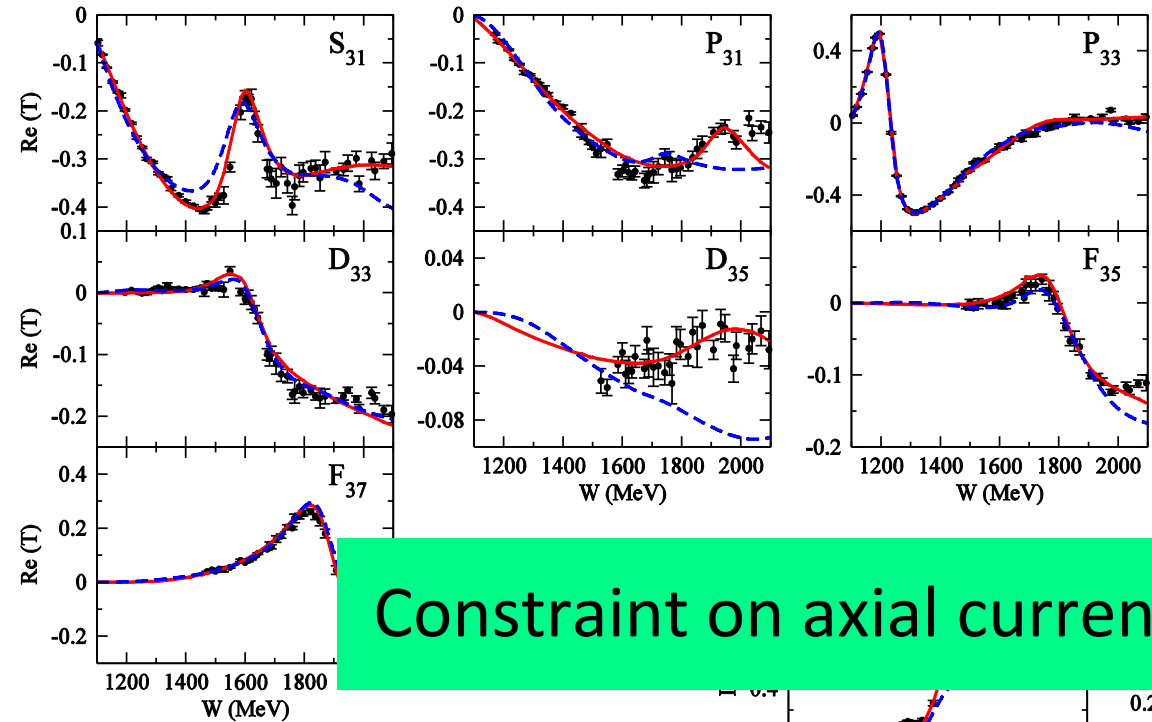
Data: SAID  $\pi N$  amplitude



Imaginary part



# Partial wave amplitudes of $\pi N$ scattering



Real part

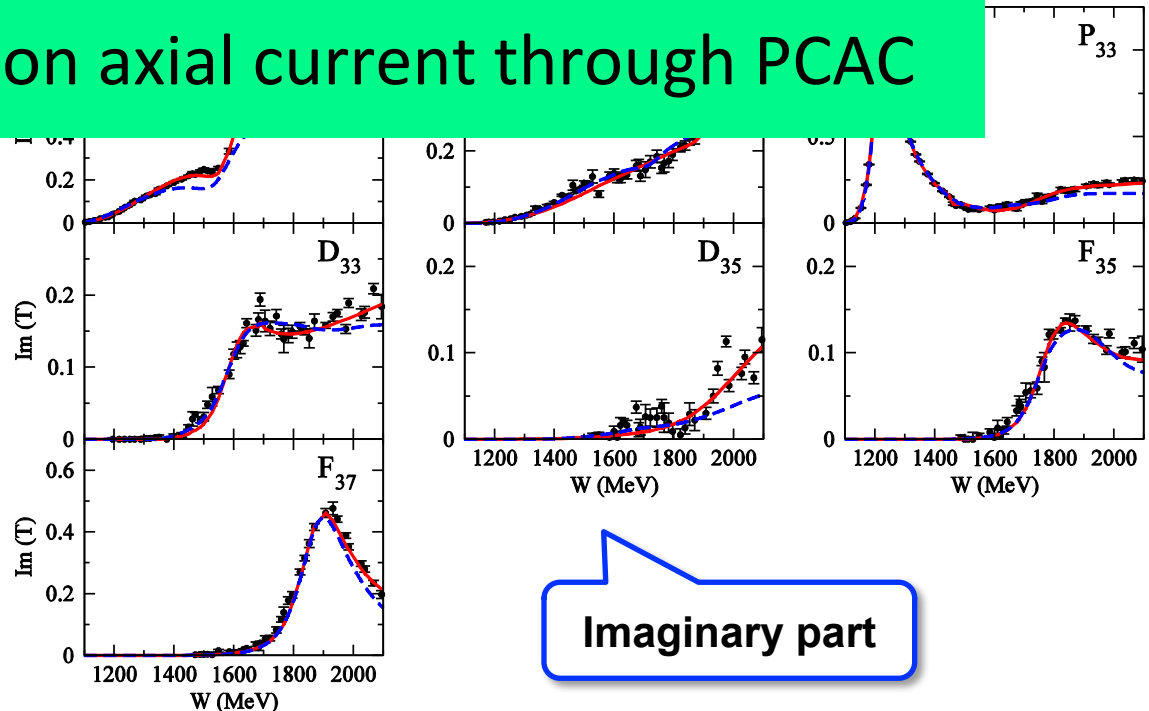
$$I = \frac{3}{2}$$

Constraint on axial current through PCAC

— Kamano, Nakamura, Lee, Sato,  
PRC 88 (2013)

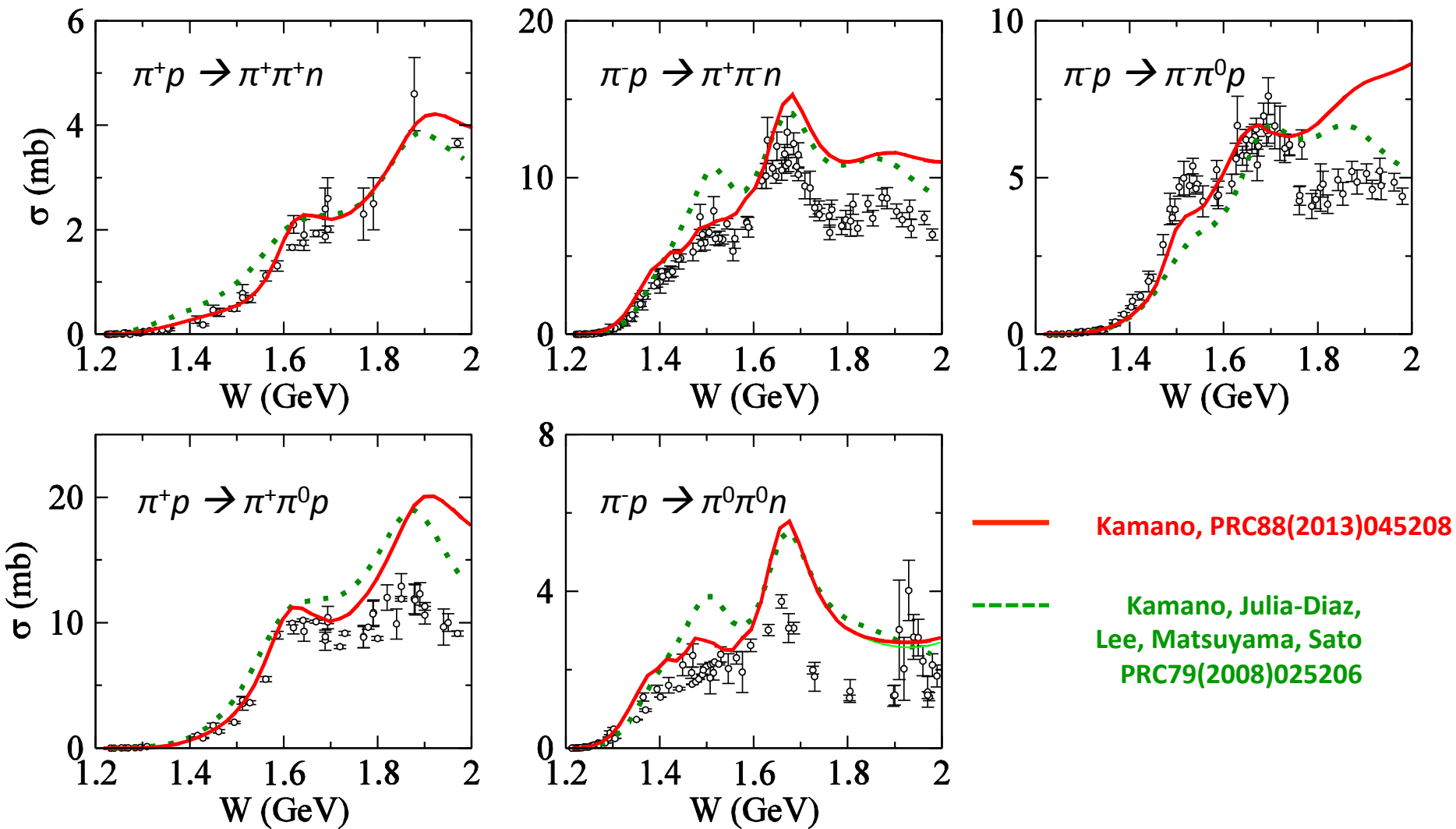
- - - Previous model  
(fitted to  $\pi N \rightarrow \pi N$  data only)  
[PRC76 065201 (2007)]

Data: SAID  $\pi N$  amplitude



Imaginary part

# Predicted $\pi N \rightarrow \pi\pi N$ total cross sections with our DCC model

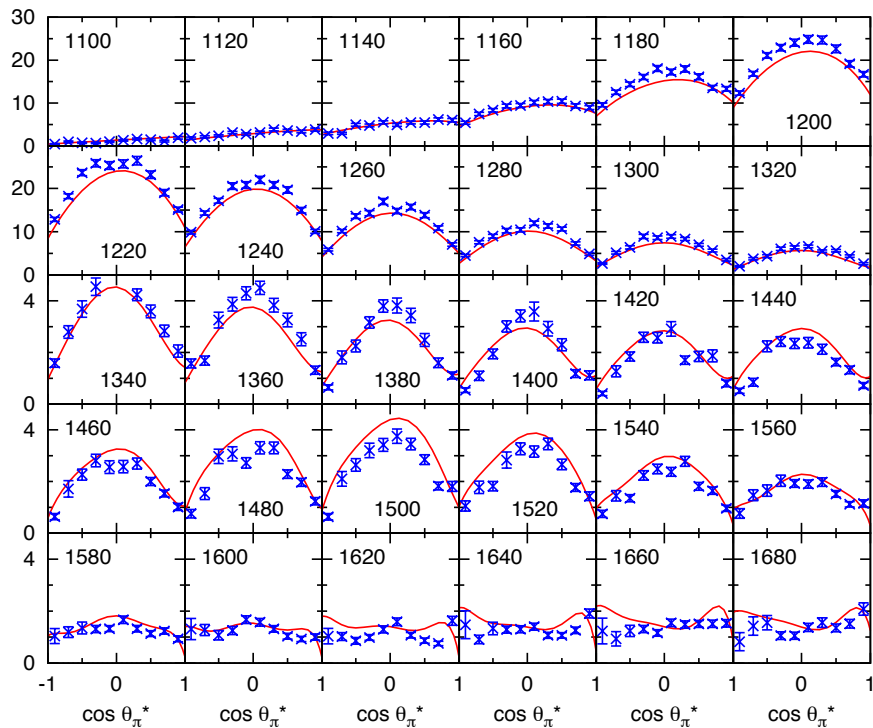


# Single $\pi$ production in electron-proton scattering

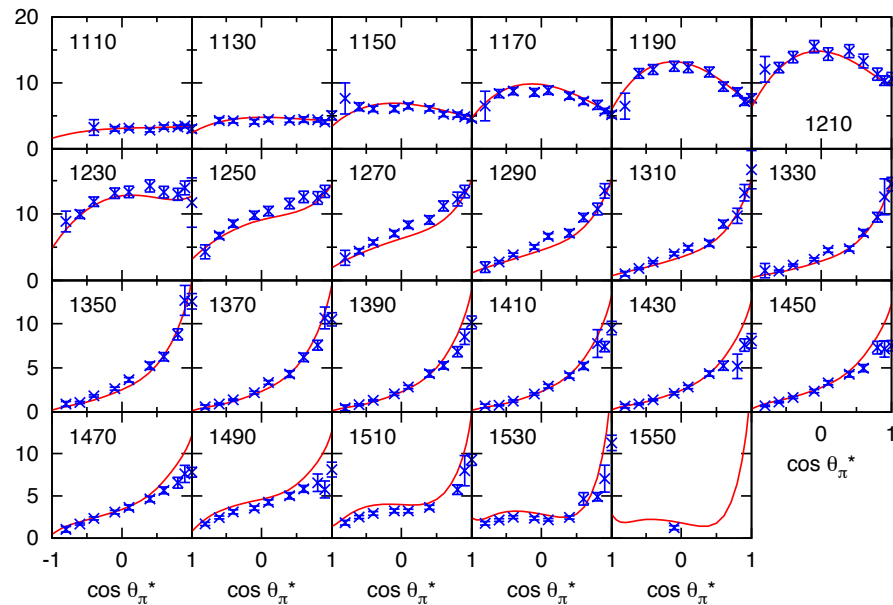
**Purpose** : Determine  $Q^2$ -dependence of vector coupling of  $p$ - $N^*$  :  $V_{pN^*}(Q^2)$

$\sigma_T + \varepsilon \sigma_L$  for  $Q^2=0.40$  (GeV/c) $^2$  and  $W=1.1 - 1.68$  GeV

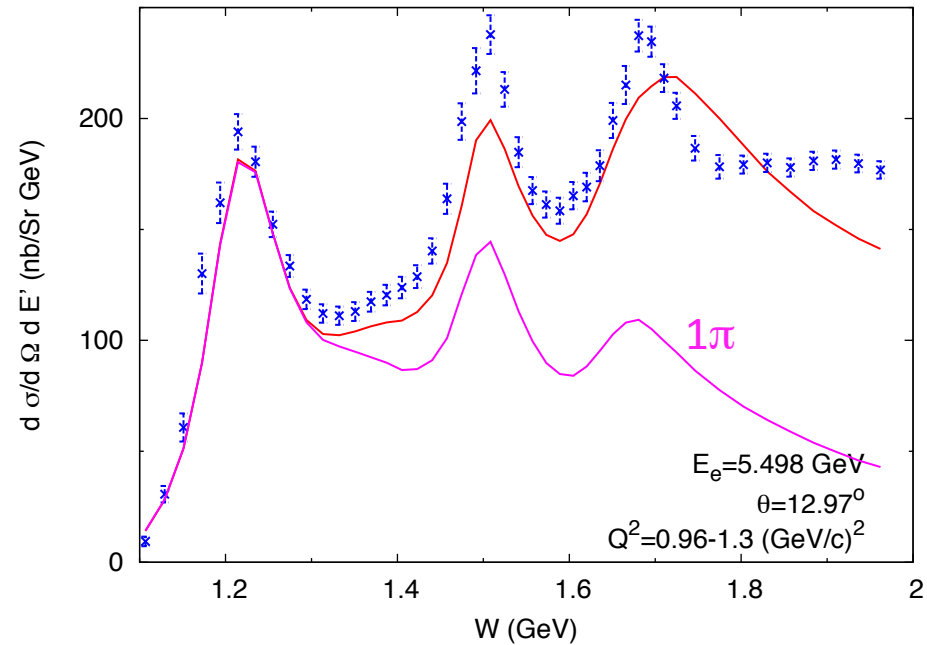
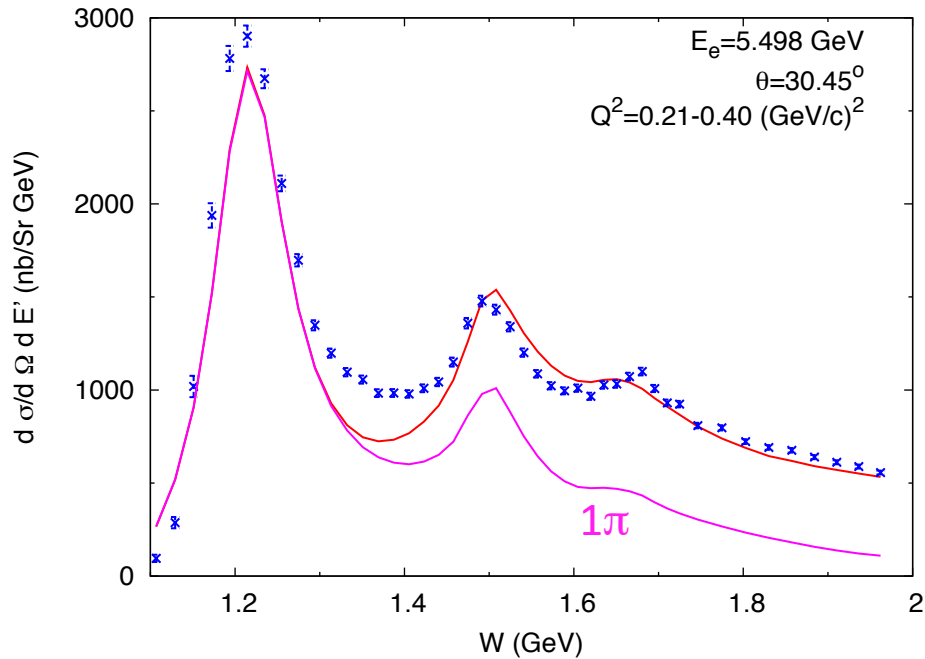
$p(e, e' \pi^0)p$



$p(e, e' \pi^+)n$



# Inclusive electron-proton scattering



Data: JLab E00-002 (preliminary)

- Reasonable fit to data for application to neutrino interactions
- Important  $2\pi$  contributions for high  $W$  region

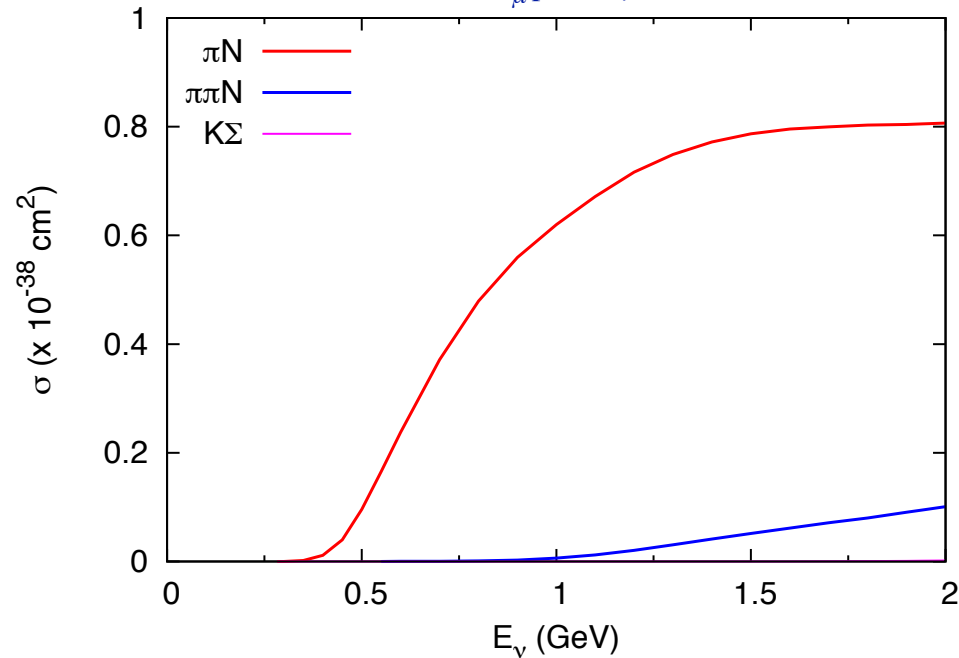
Similar analysis of **electron-neutron scattering** data has also been done

*DCC vector currents has been tested by data for whole kinematical region*

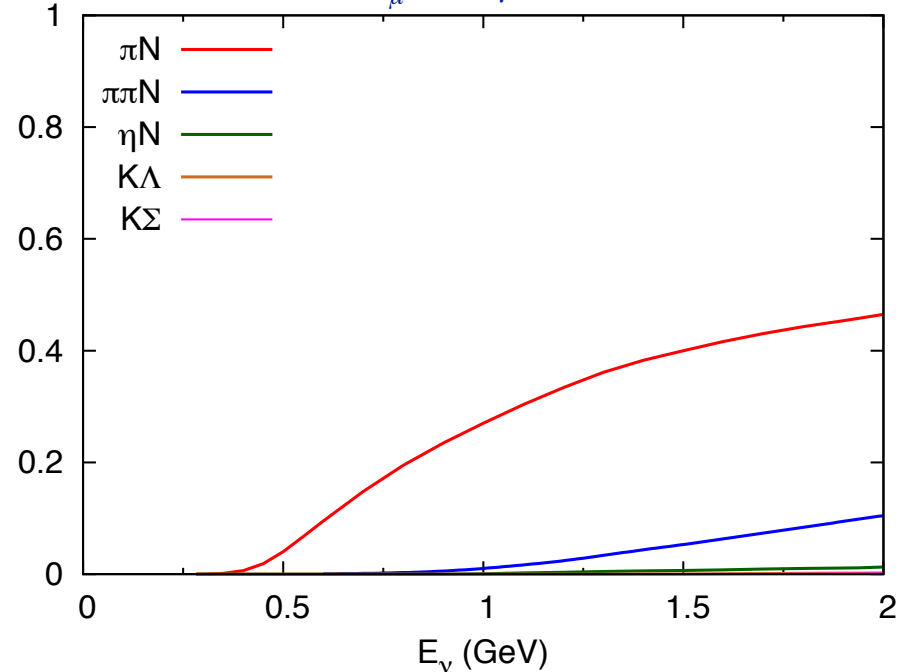
*relevant to neutrino interactions of  $E_\nu \leq 2$  GeV*

# Cross section for $\nu_\mu N \rightarrow \mu^- X$

$\nu_\mu p \rightarrow \mu^- X$

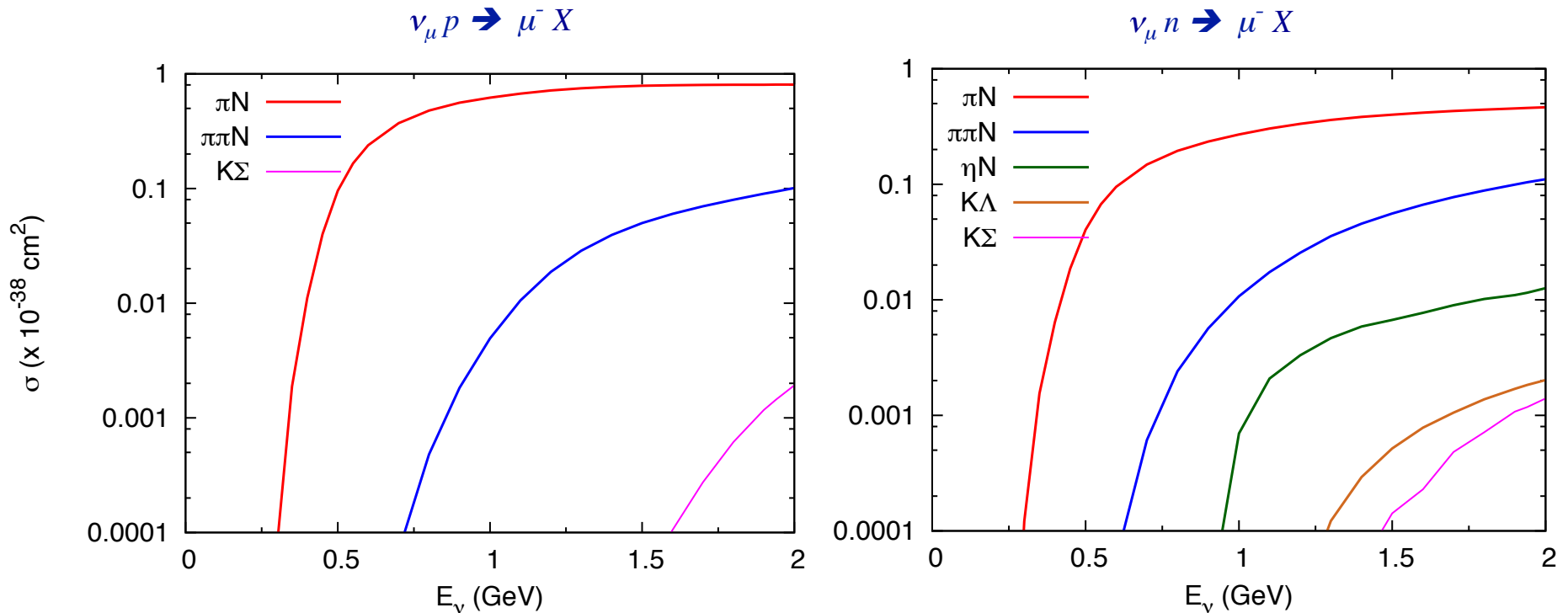


$\nu_\mu n \rightarrow \mu^- X$



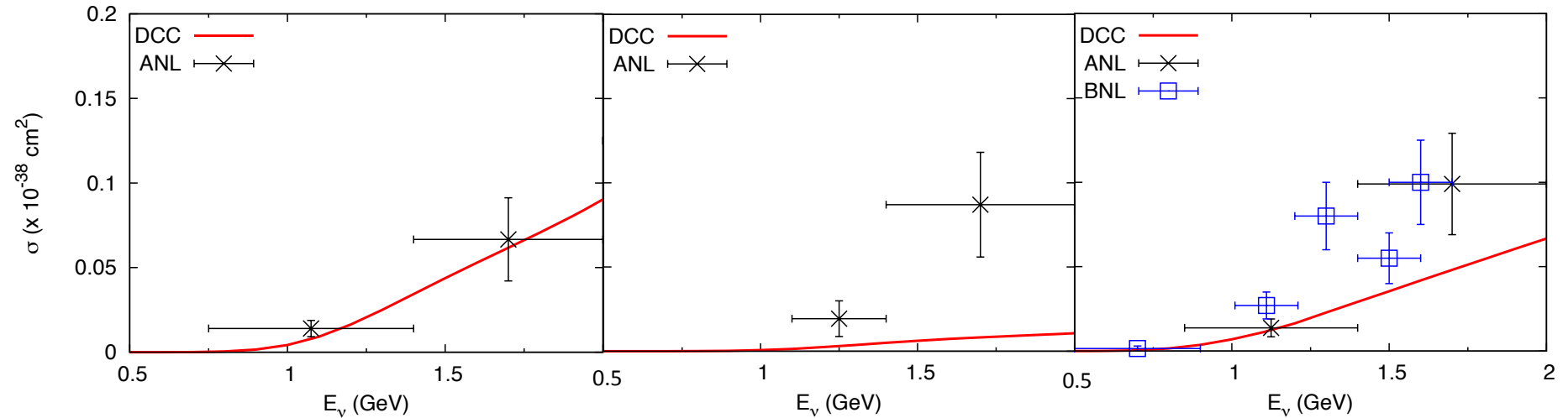
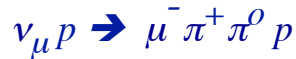
- $\pi N$  &  $\pi\pi N$  are main channels in few-GeV region
- DCC model gives predictions for **all final states**
- $\eta N$ ,  $KY$  cross sections are  $10^{-1} - 10^{-2}$  smaller

# Cross section for $\nu_\mu N \rightarrow \mu^- X$



- $\pi N$  &  $\pi\pi N$  are main channels in few-GeV region
- DCC model gives predictions for **all final states**
- $\eta N$ ,  $KY$  cross sections are  $10^{-1} - 10^{-2}$  smaller

# Comparison with double pion data



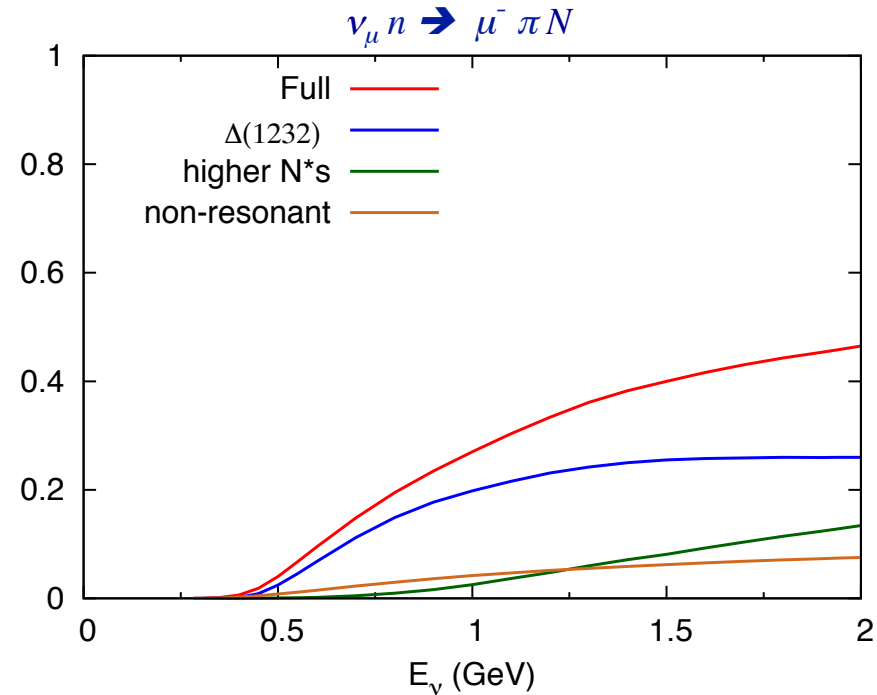
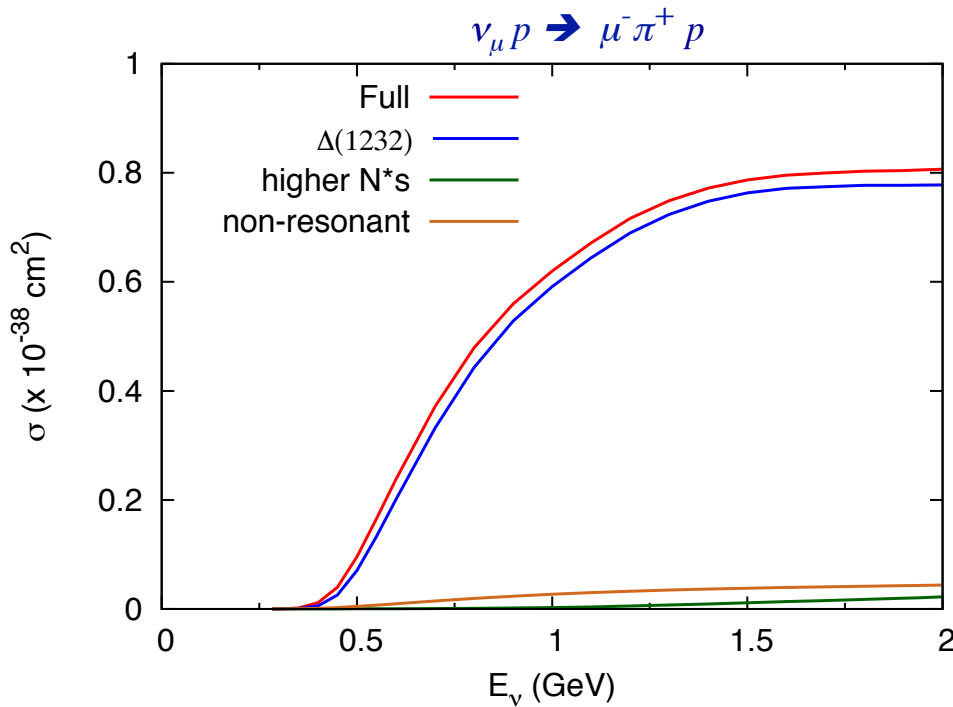
Fairly good DCC predication

ANL Data : PRD **28**, 2714 (1983)

BNL Data : PRD **34**, 2554 (1986)

First dynamical model for 2  $\pi$  production in resonance region

# Mechanisms for $\nu_\mu N \rightarrow \mu^- \pi N$



- $\Delta(1232)$  dominates for  $\nu_\mu p \rightarrow \mu^- \pi^+ p$  ( $I=3/2$ ) for  $E_\nu \leq 2$  GeV
- Non-resonant mechanisms contribute significantly
- Higher  $N^*$ s becomes important towards  $E_\nu \approx 2$  GeV for  $\nu_\mu n \rightarrow \mu^- \pi N$

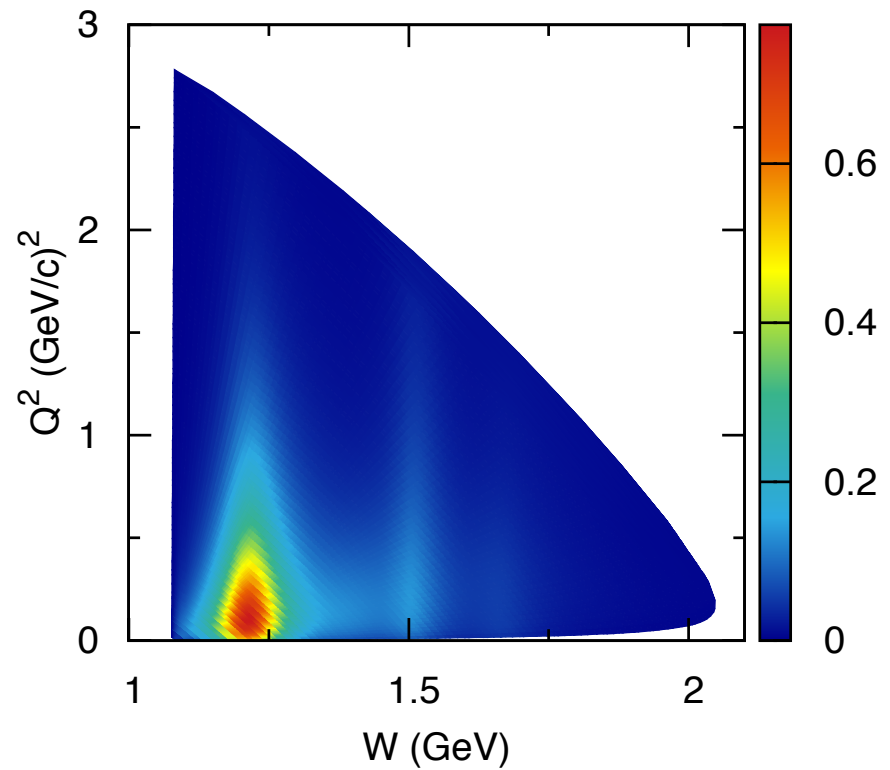
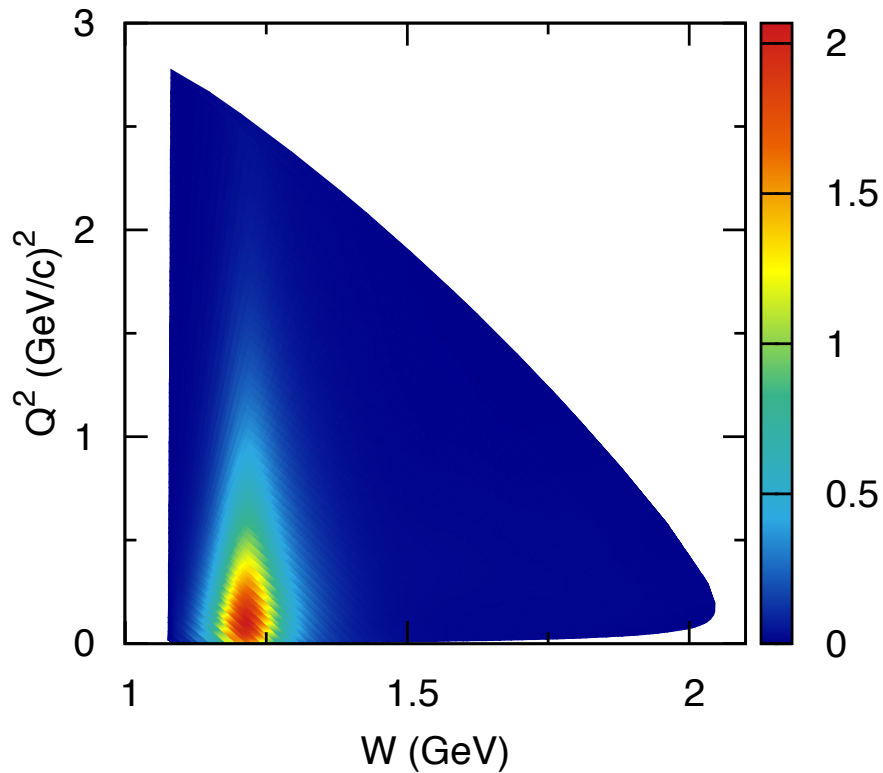


$$d\sigma / dW dQ^2 \quad (\times 10^{-38} \text{ cm}^2 / \text{ GeV}^2)$$

$$E_\nu = 2 \text{ GeV}$$

$$\nu_\mu p \rightarrow \mu^- \pi^+ p$$

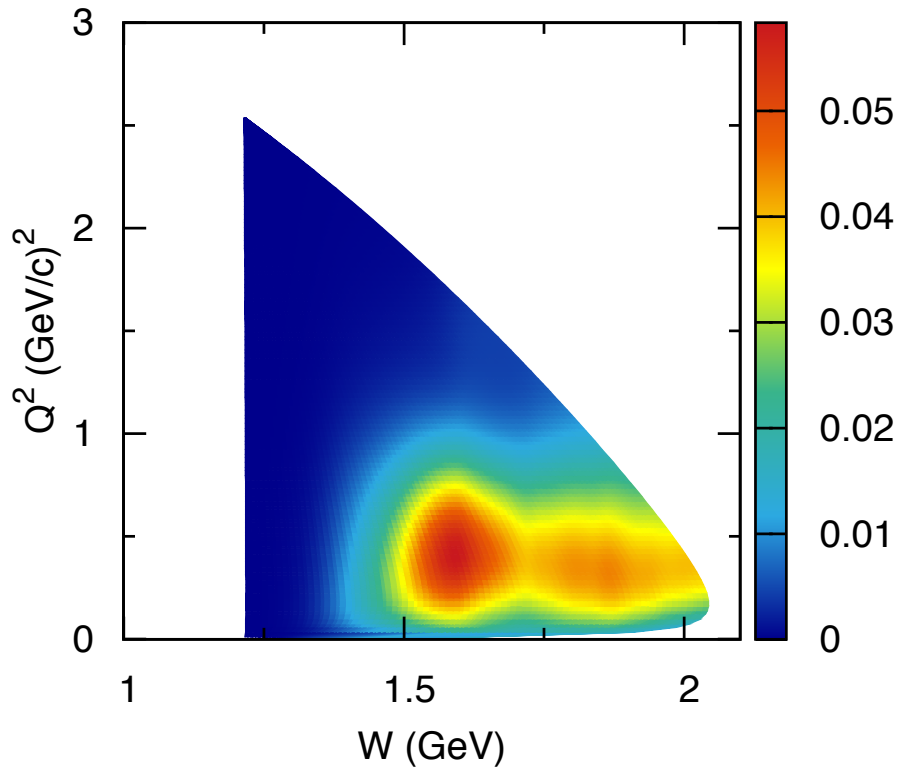
$$\nu_\mu n \rightarrow \mu^- \pi N$$



$$d\sigma / dW dQ^2 \quad (\times 10^{-38} \text{ cm}^2 / \text{GeV}^2)$$

$$E_\nu = 2 \text{ GeV}$$

$$\nu_\mu p \rightarrow \mu^- \pi^+ \pi^0 p$$



$$\nu_\mu n \rightarrow \mu^- \pi^+ \pi^- p$$

