Impact of cross section modeling on NOvA oscillation analyses

on behalf of the NOvA collaboration

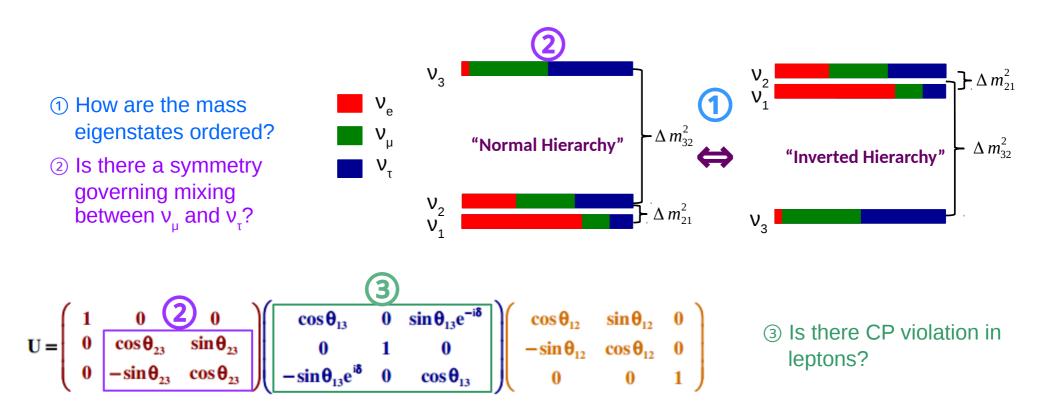


Jeremy Wolcott Tufts University

October 17, 2018 NuInt 2018 (L'Aquila, Italy)

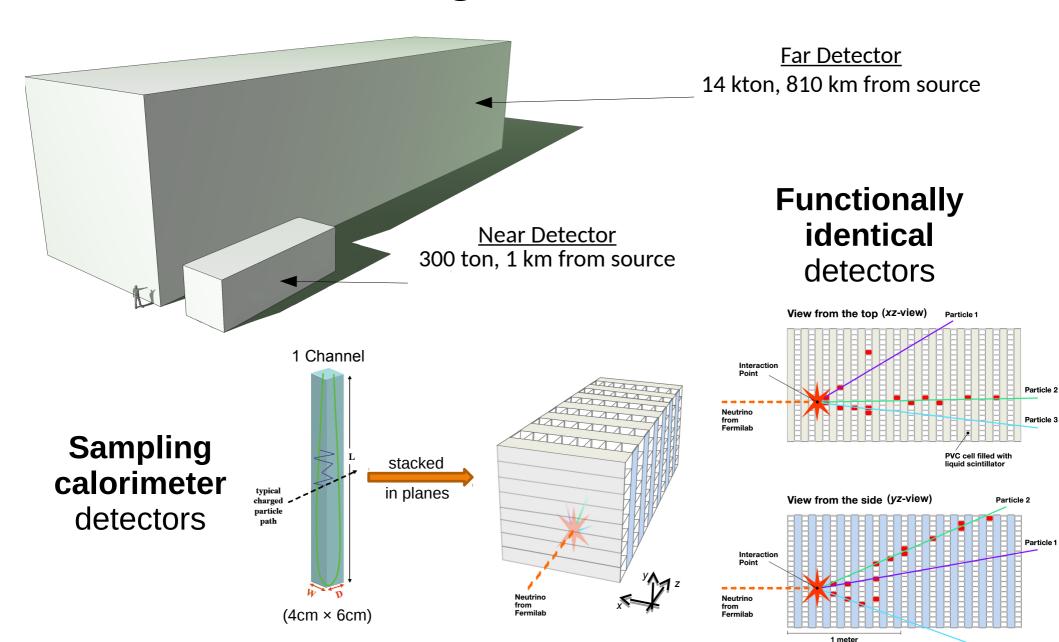


NOvA: v oscillation physics



Measuring key parameters in oscillation physics

NOvA: design considerations



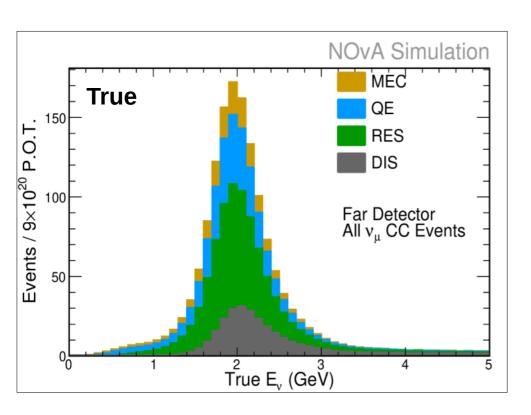
J. Wolcott

Particle 3

October 17, 2018

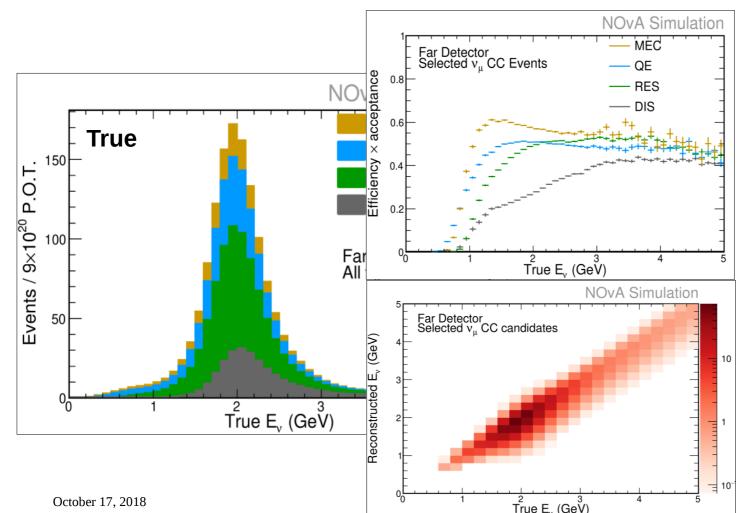
How cross sections enter the story: energy reconstruction

- $P(v_{\alpha} \rightarrow v_{\beta})$ depends on E_{true} , but detectors measure E_{reco}
- Detectors/reconstruction have different sensitivities to different processes, which have different E_{true} ↔ E_{reco}



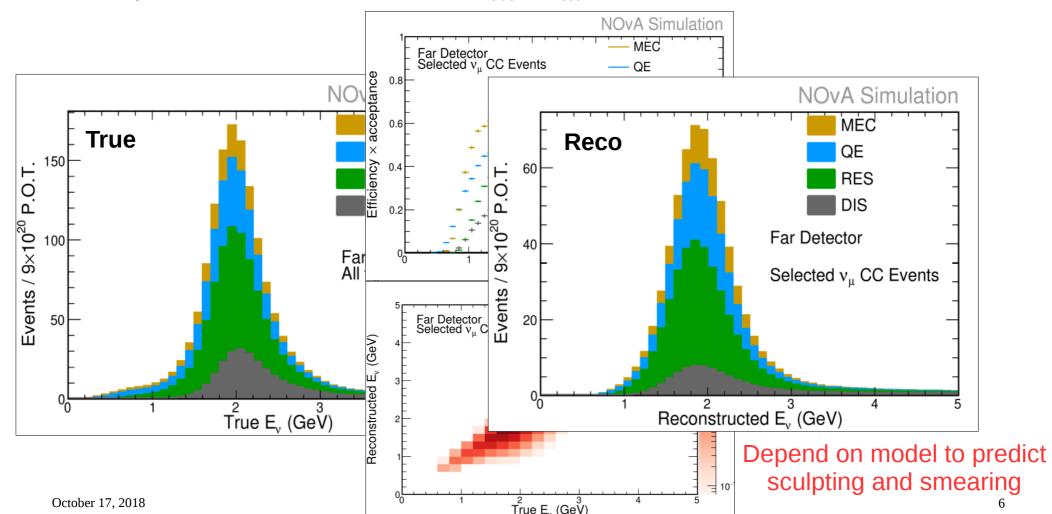
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We adjust GENIE 2.12 (base model) based on theory work and other experiments' data: thanks to the hard work of many in this room!



(fuller discussion in J. Wolcott, FNAL Neutrino Seminar, Apr. 23 2018; paper forthcoming)

Free-nucleon model

Use dipole axial FF with $M_{\Delta}^{QE} = 1.04 \pm 0.05$ GeV

based on error-weighted mean we calculated from bubble chamber data [collected in PRD 93, 113015] (GENIE default: 0.99 GeV)

Z-expansion in our future...

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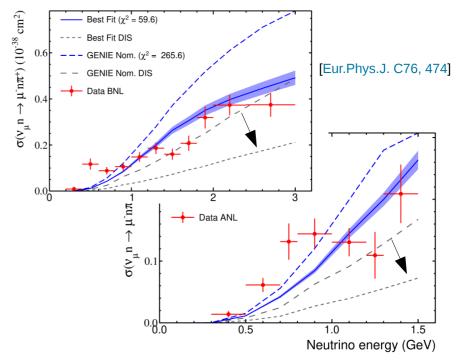
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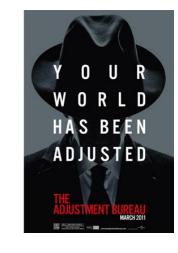
Z-expansion in our future...



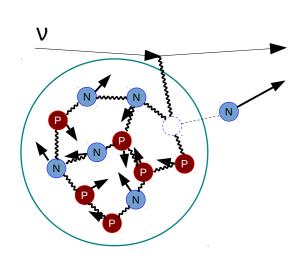
Nonresonant $1\pi^+$ production from neutrons needs to be **reduced by ~50%** based on updated fits to free-nucleon data



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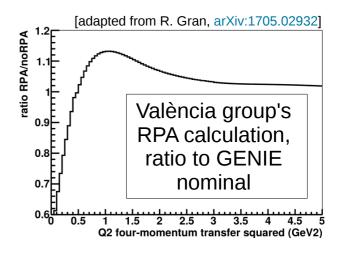


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Effective nuclear"screening" from collective excitations: treated with RPA.

We use Valencia group calculation for QE; also use Q² shape for RES based on suppression noticed in external and NOvA data

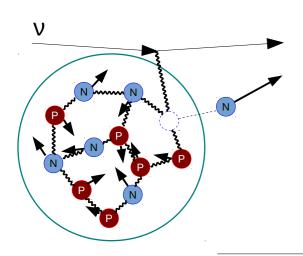




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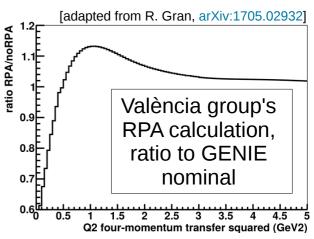


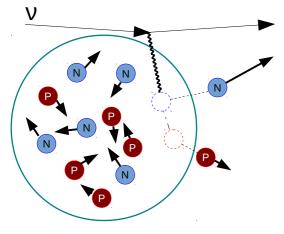




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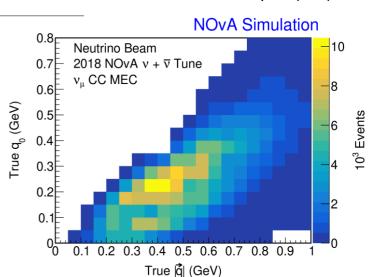




Multinucleon knockout (2p2h)

We enable GENIE "Empirical MEC", retune it based on our data.
Uncertainties from fits under different assumptions.

Nuclear model



October 17, 2018

J. Wolcott / Tufts U. / NuInt 2018

Evaluating cross section uncertainties

Depend heavily on GENIE's reweight system...

Primary process uncertainties

QE: M_△, Vector FF, Pauli supp...

RES: M_A , M_V , Δ decay isotropy...

DIS: Bodek-Yang parameters, transition region ("non-resonant background" scale), ...

COH: Rein-Sehgal M_A, R₀, ...

Final-state model (hA) uncertainties

Nucleon, pion elastic, inelastic, chg ex., abs. reaction probabilities

Hadron mean free paths

(~50 reweight knobs in all)

...and build custom knobs for our growing library of GENIE 'adjustments':

MEC model for **2p2h** (q^µ shape, E_ν shape, nn/np composition)

RPA-QE (based on València treatment; histograms from R. Gran)

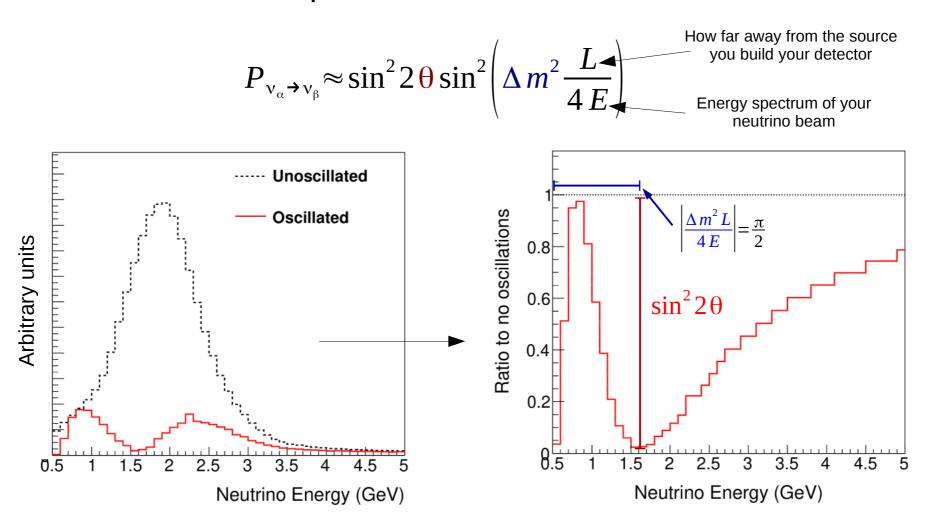
RES-Q² (conservative "on" vs "off")

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In practice: ν_{μ} disappearance

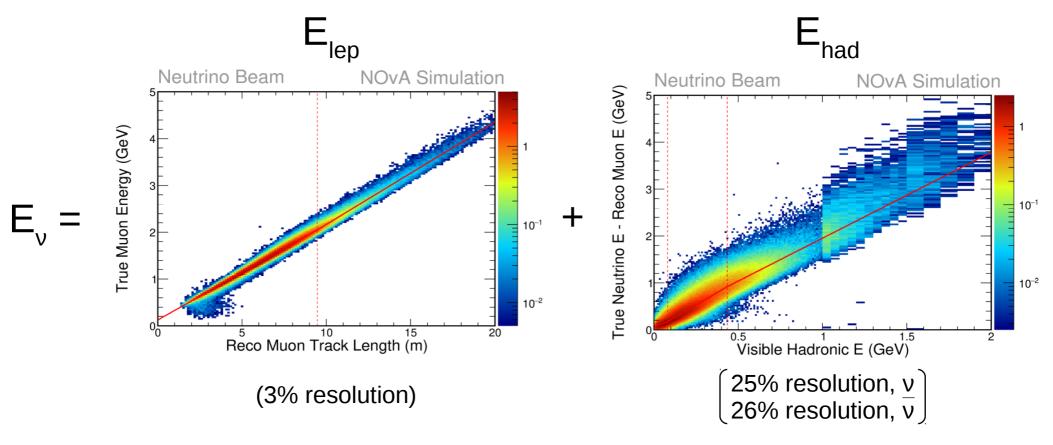
[a worked example]

$\nu_{_{\mu}}$ disappearance



Goal: measure the location and strength of the "oscillation dip" relative to no-oscillations prediction

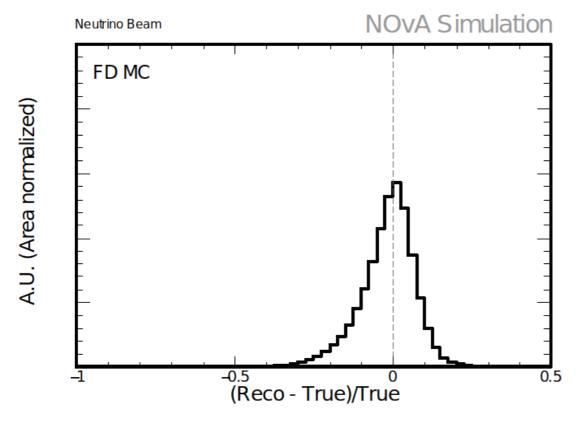
ν_{μ} disappearance: energy reconstruction



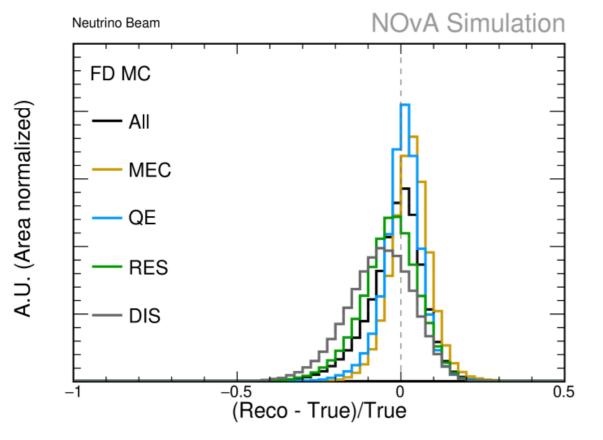
Calibrate muon track length to true E_{μ} , then remaining visible energy to (true E_{ν} – reco E_{μ}).

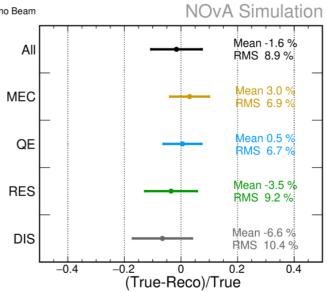
Calorimetric (not kinematic) energy reconstruction

v_{μ} disappearance: energy reconstruction



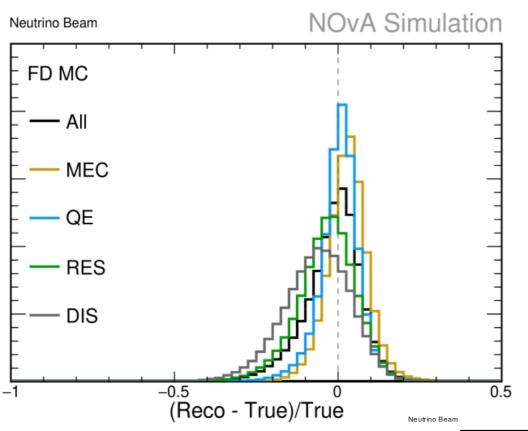
Nominal resolution on E, ~ 9%.

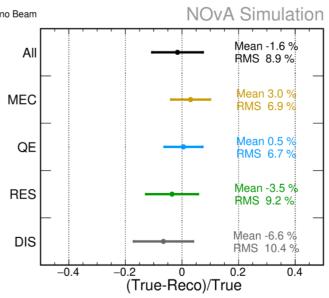




Nominal resolution on E_v ~ 9%; different by reaction

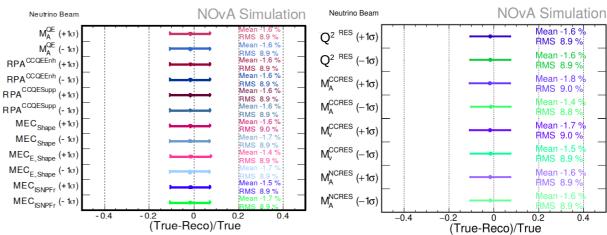
v_{μ} disappearance: energy reconstruction





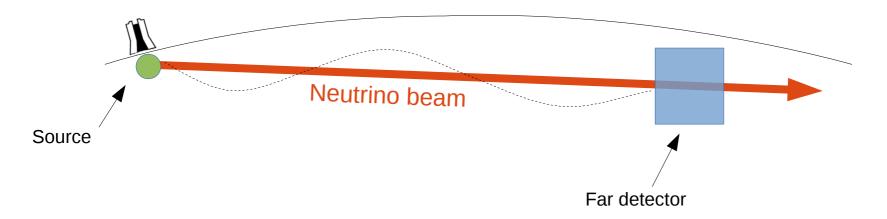
Nominal resolution on E₁ ~ 9%.

Despite sculpting effect, calorimeter-style detectors ensure cross section systematics don't significantly degrade energy resolution



A.U. (Area normalized)

Near detectors



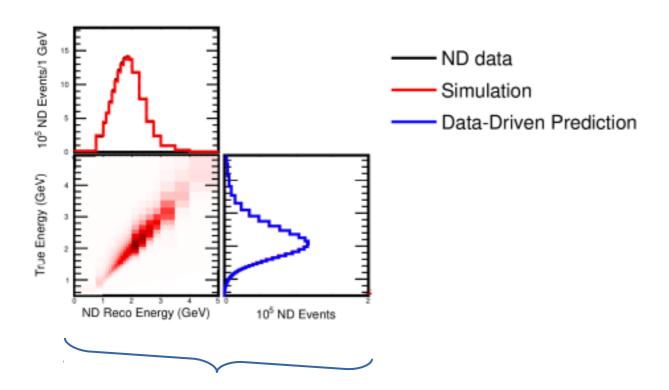
Want to measure oscillation probability.

Many other variables...

$$N(E_{\nu}^{rec}) = \Phi(E_{\nu}^{true}) \times P_{osc}(E_{\nu}^{true}) \times \sigma(E_{\nu}^{true}, A) \times R(E_{\nu}^{true}) \times \epsilon(...)$$

ν_{μ} disappearance: "extrapolation"

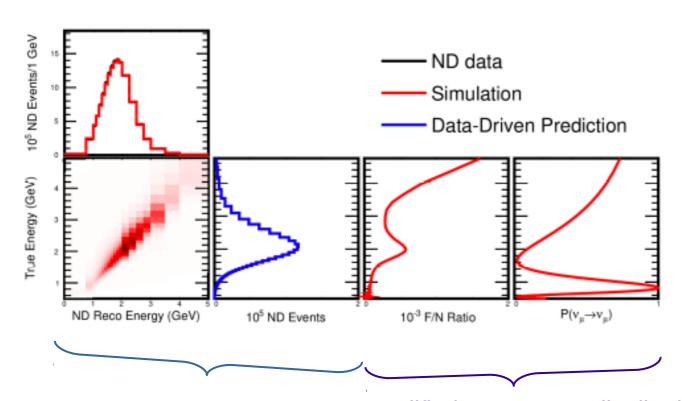
To produce a data-driven prediction at FD, based on ND:



True energy distribution is corrected so that reconstructed data & MC agree at the ND...

ν_{μ} disappearance: "extrapolation"

To produce a data-driven prediction at FD, based on ND:

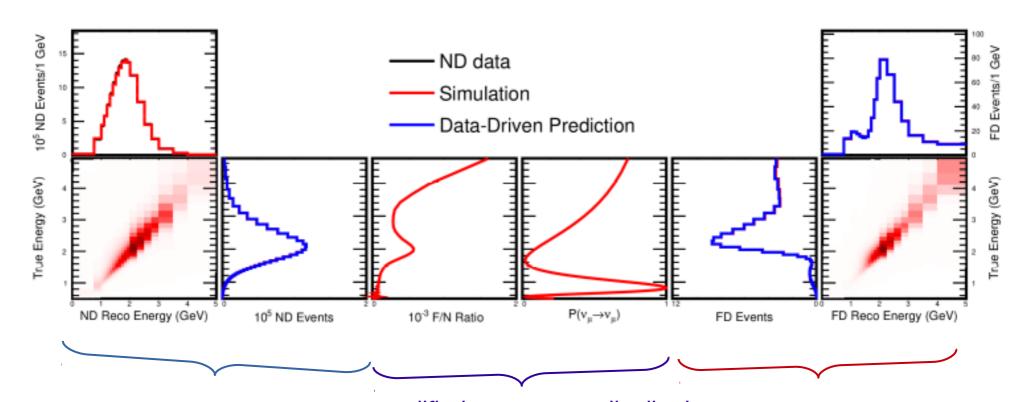


True energy distribution is corrected so that reconstructed data & MC agree at the ND...

...modified true energy distribution is propagated through predicted geometric beam dispersion & acceptance ratio, oscillations...

$ν_μ$ disappearance: "extrapolation"

To produce a data-driven prediction at FD, based on ND:



True energy distribution is corrected so that reconstructed data & MC agree at the ND...

...modified true energy distribution is propagated through predicted geometric beam dispersion & acceptance ratio, oscillations...

... and "extrapolated" reconstructed energy distribution computed to compare to data



Illustrating XS systematics: MEC

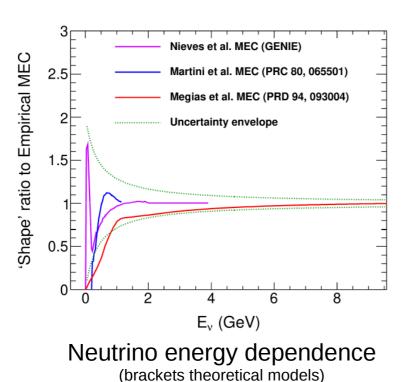
Examine this procedure through the lens of reaction of interest:

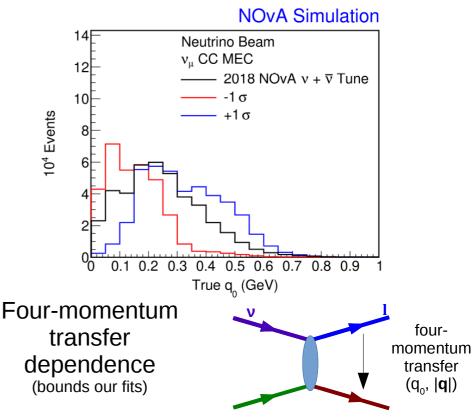
2p2h via

Meson Exchange Currents

(GENIE 'Empirical MEC' w/ ND tuning)

Illustrate behavior through two different knobs:







Illustrating XS systematics: MEC

Examine this procedure through the lens of reaction of interest:

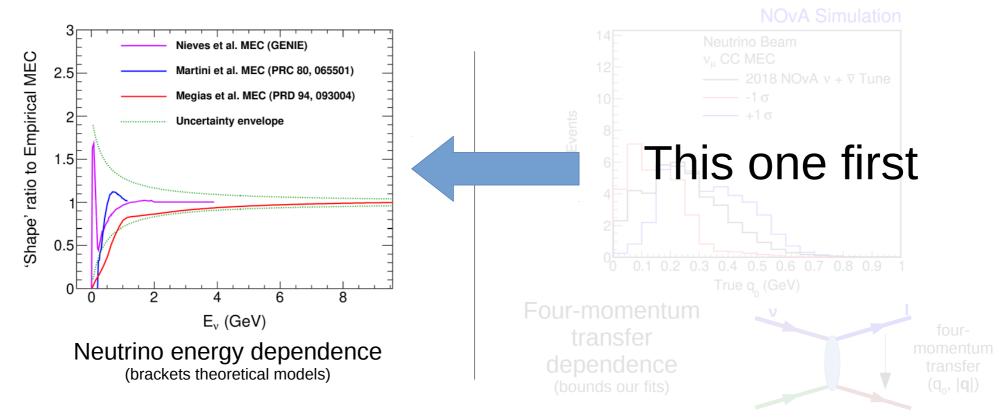
2p2h
via

Meson Exchange Currents

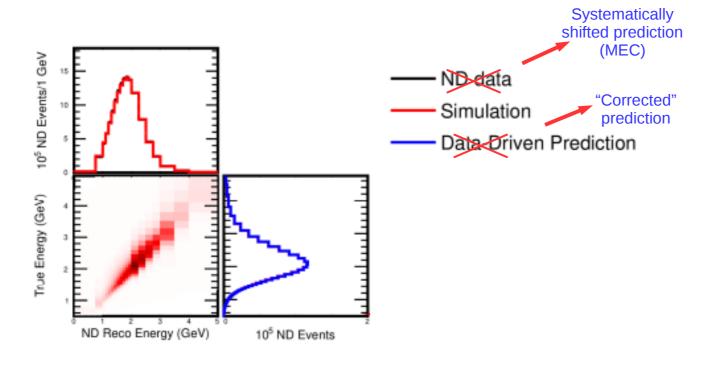
(GENIE 'Empirical MEC' w/ ND tuning)

23

Illustrate behavior through two different knobs:



To examine the effect of extrapolation:

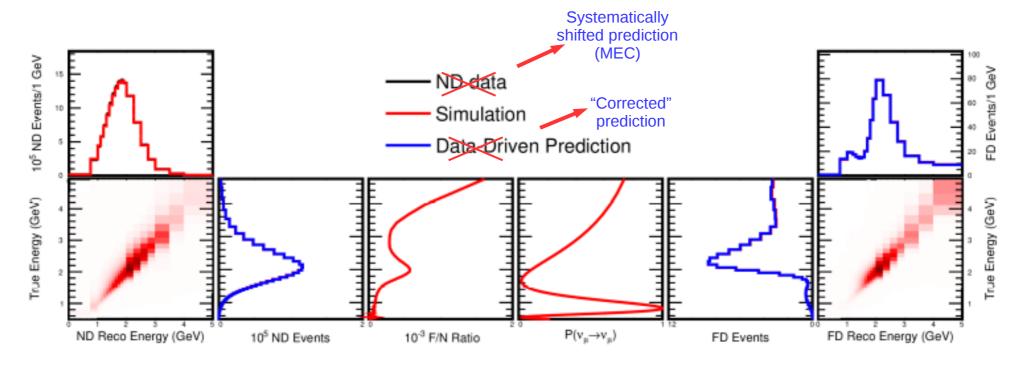


Replace "ND Data" with "ND prediction under systematic shift".

(Asks: "if data exhibits this effect, and we use baseline simulation, how well does extrapolation compensate?")

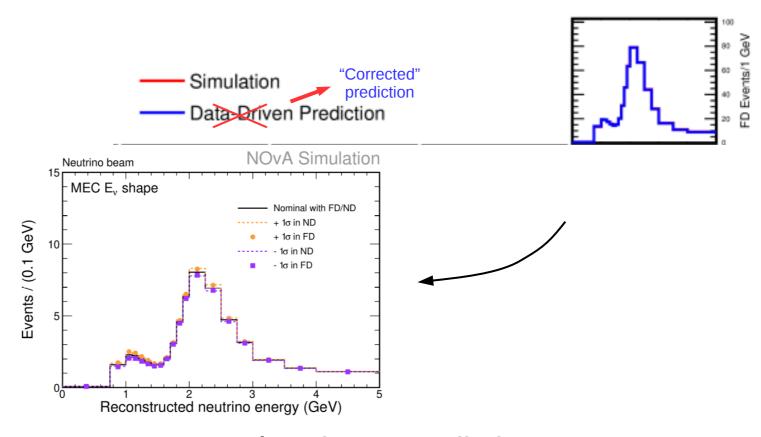
24

To examine the effect of extrapolation:



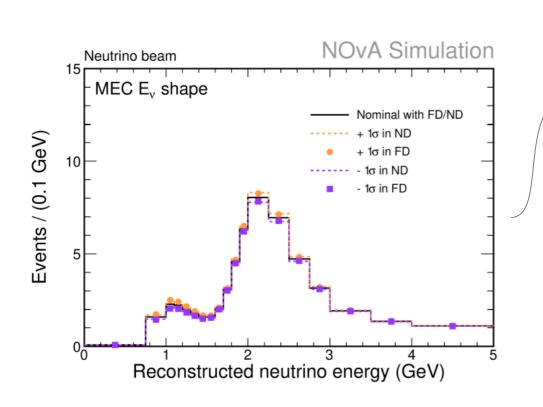
Transport "corrected" prediction through extrapolation process

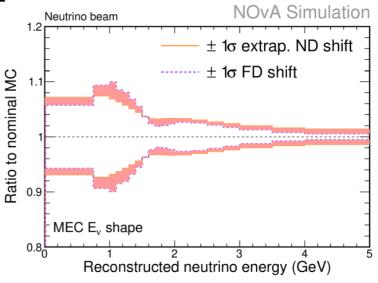
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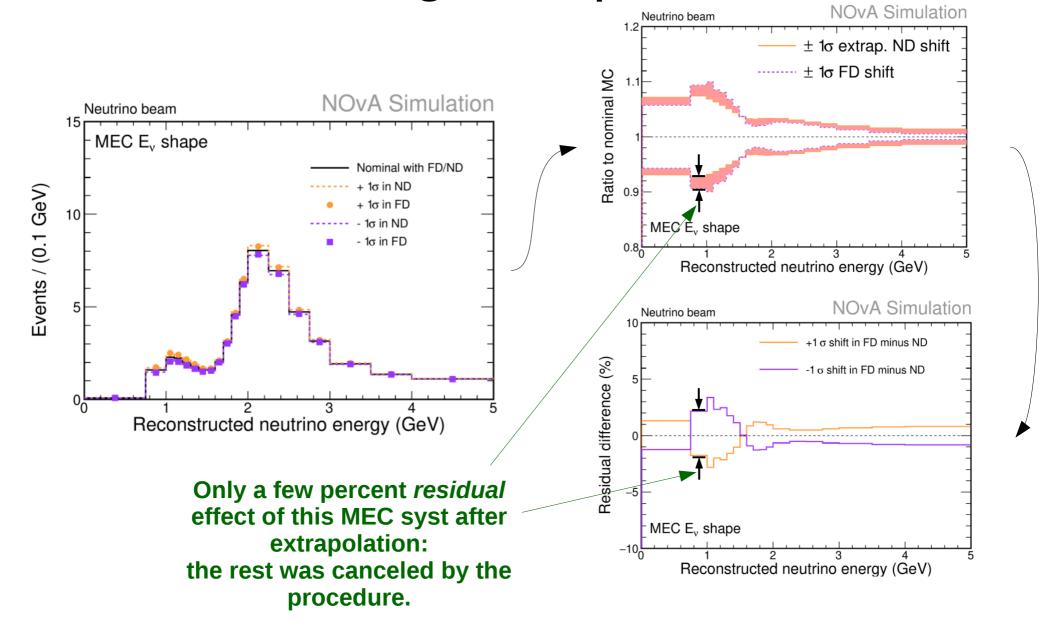


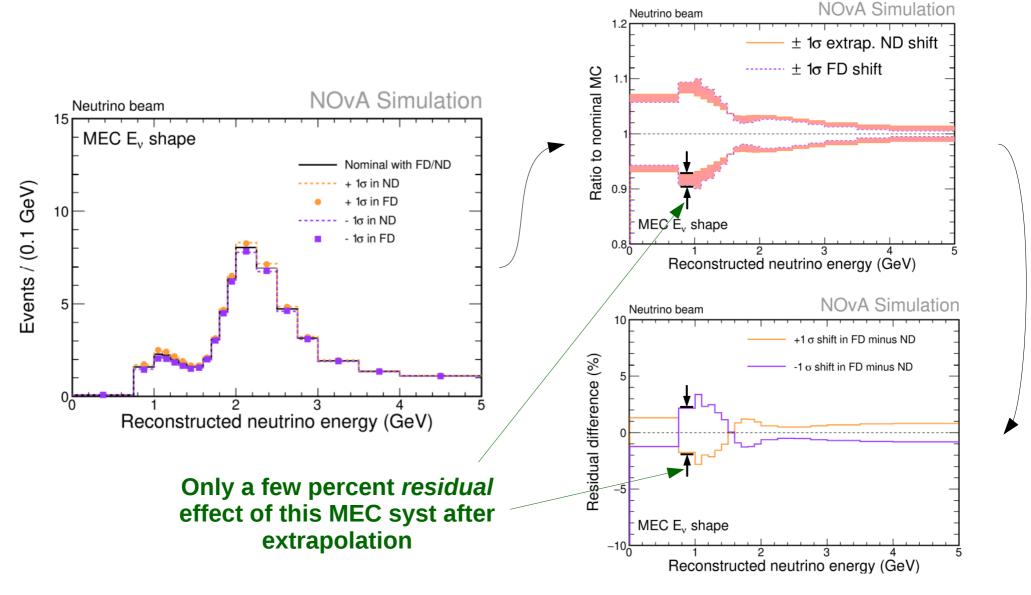
Compare "extrapolated" FD prediction to prediction obtained by varying FD directly.

If they match, extrapolation perfectly 'cancels' the effect.

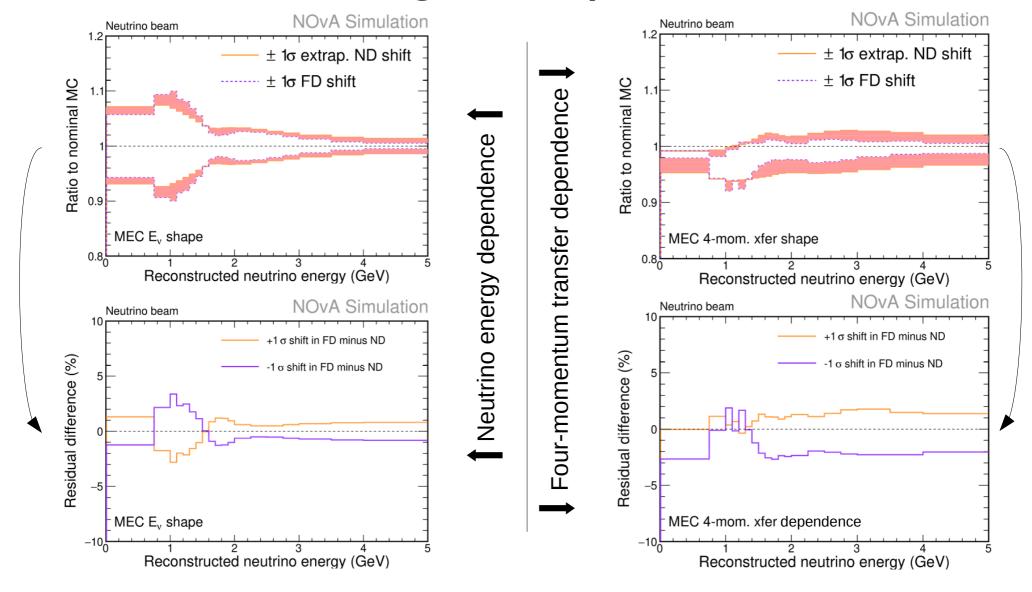








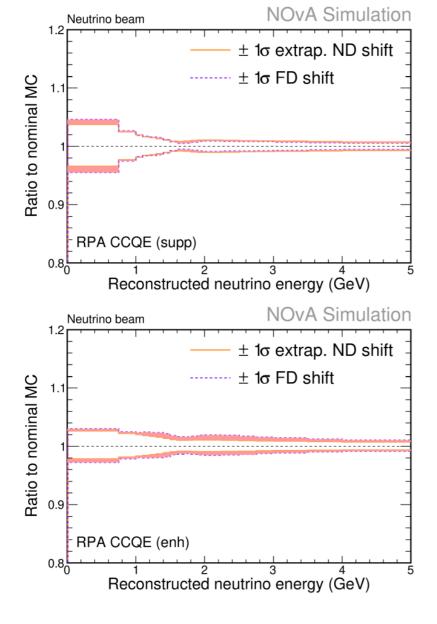
Though extrapolation procedure can't remove *all* effect of cross section uncertainties like MEC, extrapolation significantly reduces sensitivity to XS systs



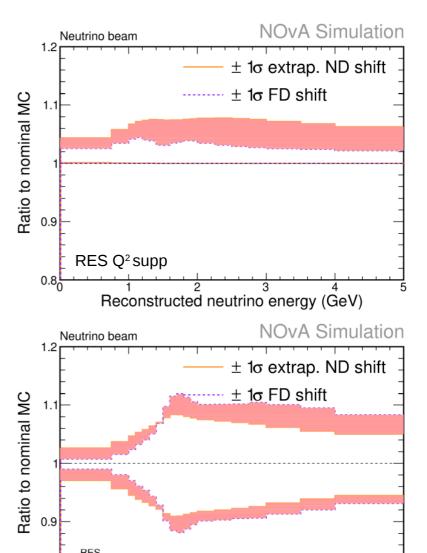
Far/Near extrapolation works best with *neutrino energy* systs, but we derive benefit from it for the other shape dependence as well



Other important XS uncertainties

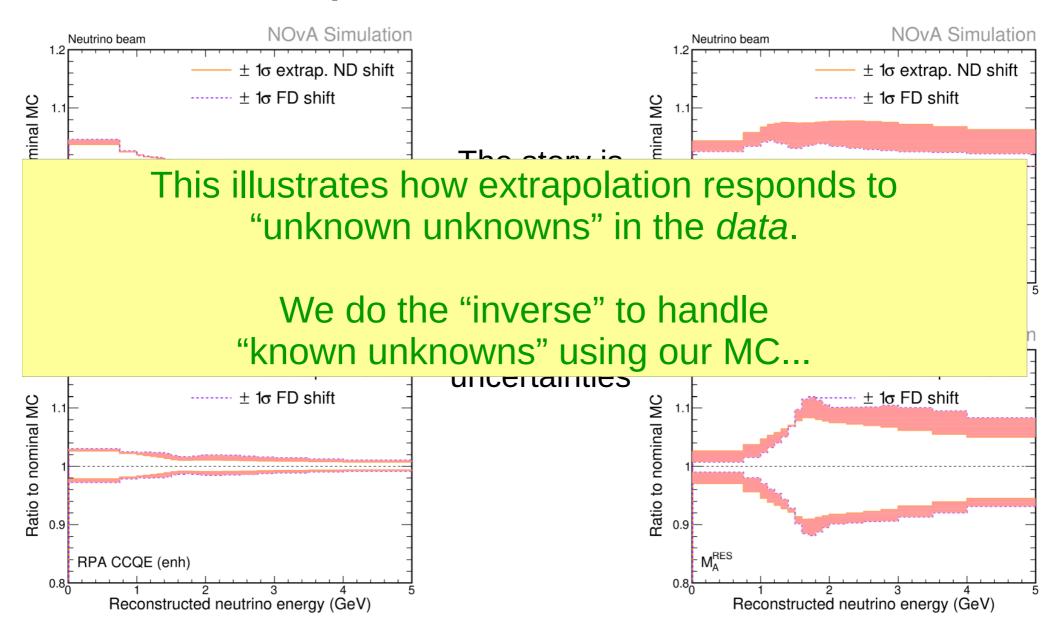


The story is similar for other important cross section uncertainties

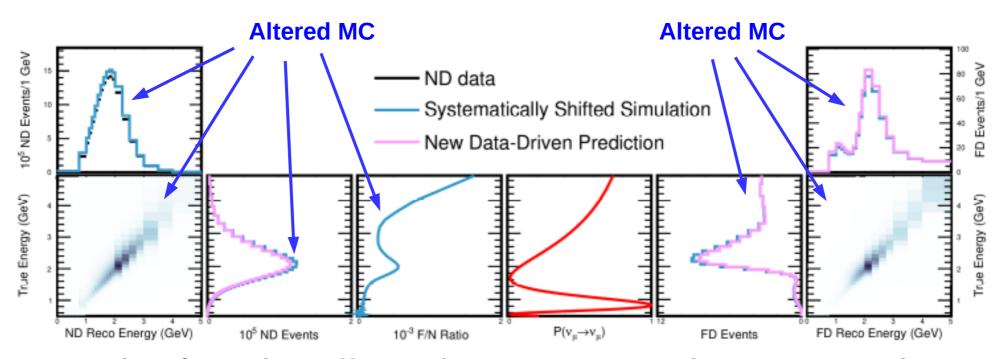


Reconstructed neutrino energy (GeV)

Other important XS uncertainties



"Extrapolation" and uncertainties



We simulate the effect of our cross section systematics' residual effect after extrapolation

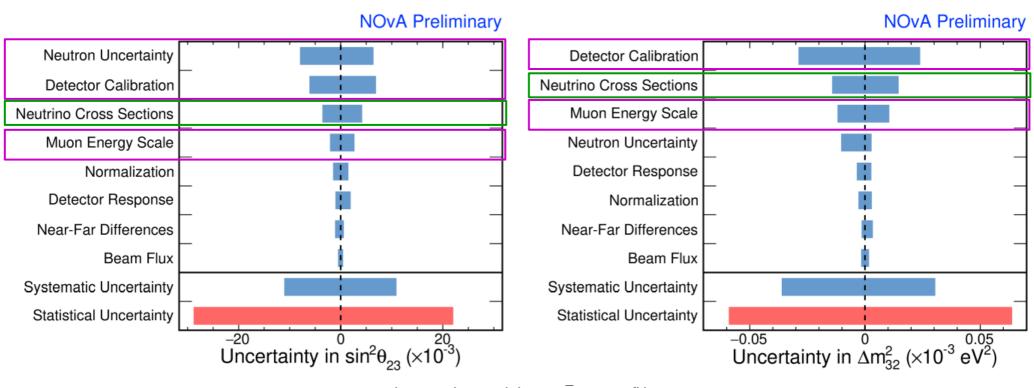
by re-doing the entire analysis for each systematic

(each of which can affect multiple both signal & bknd)

and use the difference to extrapolated nominal MC as nuisance parameters in our oscillation fits

33

Effect on analysis



(Uncertainty on joint $v + \overline{v}$, $v_{\mu} + v_{e}$ fit)

Cross section systematics are not dominant systematic uncertainties due to detector design & power of extrapolation.

But... dedicated **test beam program** (data taking in 2019) will likely drive detector response uncertainty down in the future, so soon enough cross sections will likely be atop the list...

Now: ν_e appearance

v_e appearance

$$P(\stackrel{(-)}{\nu}_{\mu} \rightarrow \stackrel{(-)}{\nu}_{e}) \approx \sin^{2} 2\theta_{13} \sin^{2} \theta_{23} \frac{\sin^{2} (A-1)\Delta}{(A-1^{2})}$$

$$\stackrel{(+)}{-} 2\Omega \sin \theta_{13} \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{A-1} \sin \Delta$$

$$+ 2\Omega \sin \theta_{13} \cos \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{A-1} \cos \Delta$$

$$\text{Where:} \quad \alpha = \frac{\Delta m_{21}^{2}}{\Delta m_{31}^{2}} \quad \Delta = \Delta m_{31}^{2} \frac{L}{4E} \quad A = \stackrel{(-)}{+} G_{f} N_{e} \frac{L}{\sqrt{2}\Delta}$$

Besides the dependence on the mixing parameters, we learn about the mass ordering (via α) and δ_{CP} ...

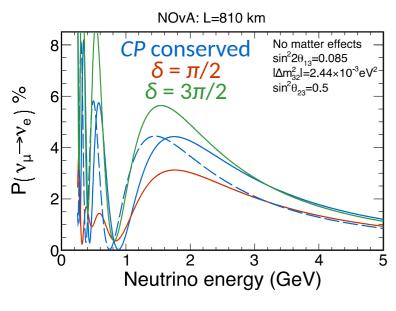
v_e appearance

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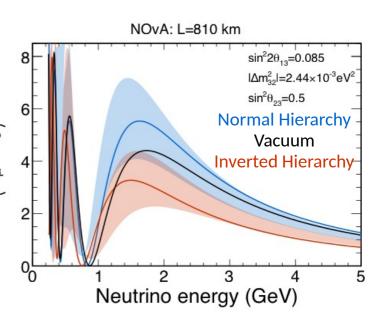
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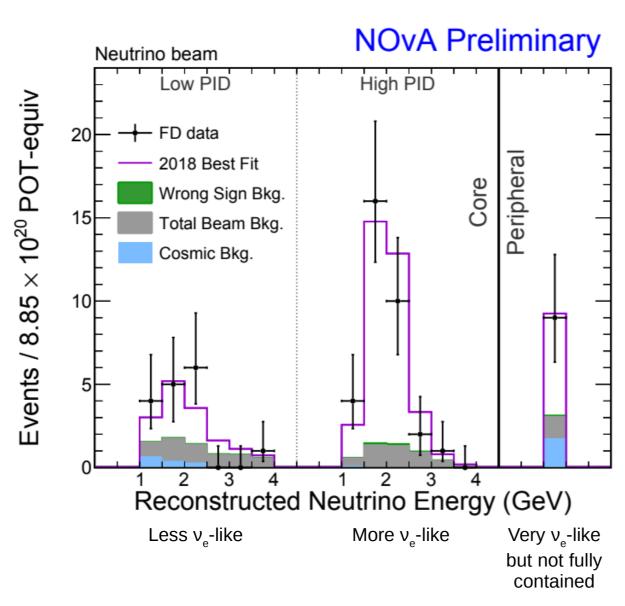
Besides the dependence on the mixing parameters, we learn about the mass ordering (via α) and δ_{CP} ...



...but smallness of θ₁₃ makes it a very challenging measurement



v_e appearance



Added challenges:

- No signal at ND
 - Need to assume relationship between ν_{μ} and ν_{μ} XSs
 - Different acceptance, v_{μ} ND vs. v_{e} FD
- Nontrivial beam backgrounds which oscillate differently
 - Beam v_e oscillate very little over this L/E
 - ν_μ almost entirely disappear
 - NC doesn't change due to oscillations (assume no steriles)

(Need to disentangle ["decompose"] before applying Far/Near makes any sense.)

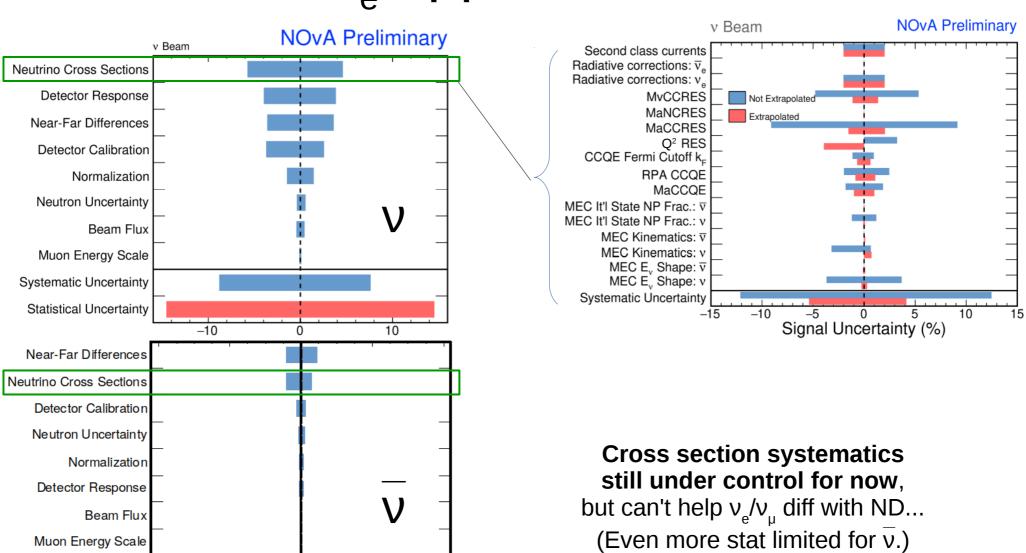
Systematic Uncertainty

Statistical Uncertainty

-40

Signal Uncertainty (%)

v_e appearance



We expect to continue to benefit from ongoing work by this audience as well to keep them that way...

- Refinement of 1p1h initial state prediction
 - Unified nuclear model treatment in GENIE (move past RFG+RPA?)
 - Study binding/separation/removal energy situation (A. Bodek, arXiv:1801.07975)...
- More/better models for multinucleon knockout in GENIE
 - Need theory models that describe inclusive data at $E_{\nu} > 1$ GeV. SuSA-MEC in GENIE soon?
 - Need to study effect of anisotropic ejection of nucleon pairs
- Nuclear models for inelastic processes
 - Examine alternatives to GENIE hA FSI
 - What's causing low-Q² suppression? ("On-off" syst one of our largest)
- v_e/v_μ for inelastic processes
- More antineutrino data

• ...

Summary

- NOvA relies on strong internal constraints on cross section uncertainties for its oscillation program
 - Calorimeter design minimizes *a priori* impact
 - Functionally identical detectors enable major cancellation of residual errors in oscillation analyses
- Comprehensive program underway to ensure all relevant cross section issues are considered
 - Necessary ingredients in base model
 - Appropriate uncertainties
- We look forward to continuing the conversation:
 - Continued development of models & systematic treatments
 - New measurements of cross sections
 - Neutrino oscillation physics results!

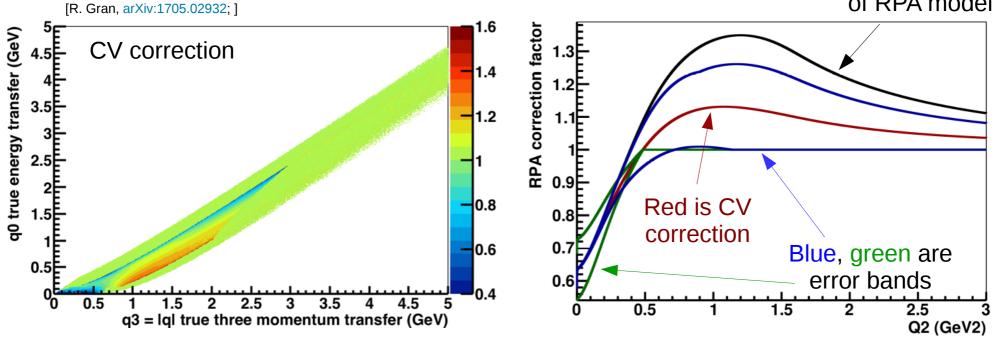


Thank you for your attention!

Overflow

Modeling the nucleus: collective effects (RPA)

Black is nonrelativistic variant of RPA model

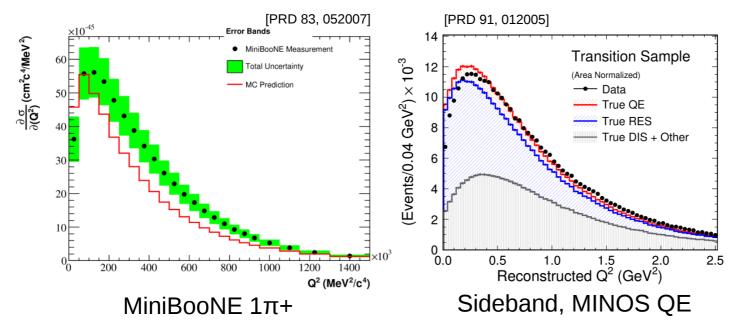


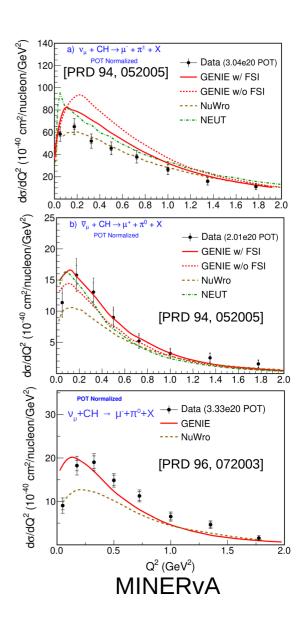
Rik Gran's work (originally for MINERvA) to extend the València RPA CCQE effect (PRC 70, 055503) to a correction for GENIE's central value and his work to extend the uncertainties in the model to higher energies (PLB 638, 325, PRD 88, 113007) naturally work reasonably well for NOvA

we apply using Rik's code

Modeling the nucleus: collective effects (RPA)

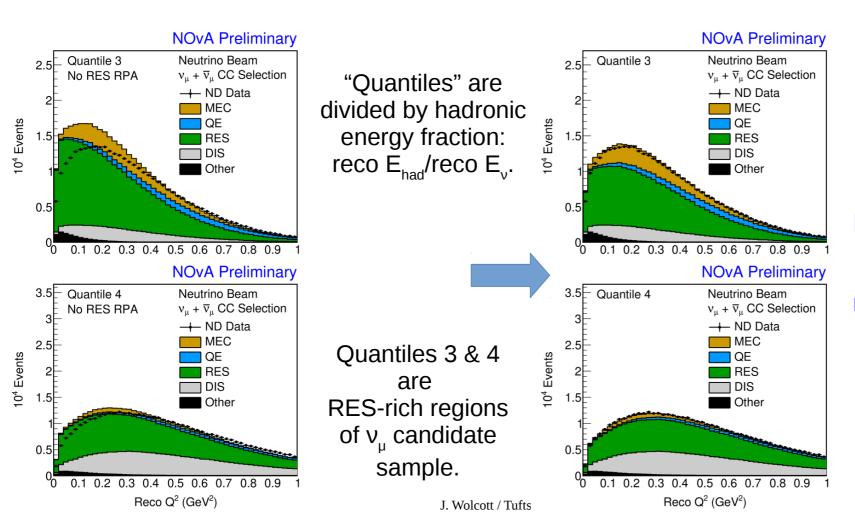
- Should Δ production also be affected?
 - Energy transfers are large (>100 MeV), so perhaps not "traditional" RPA...
 - But suppression at low Q² appears in many data sets: MiniBooNE, MINOS, MINERvA





Modeling the nucleus: collective effects (RPA)

- Should Δ production also be affected?
 - Not surprising that *some* initial-state nuclear effects might influence resonances (relative to RFG)...

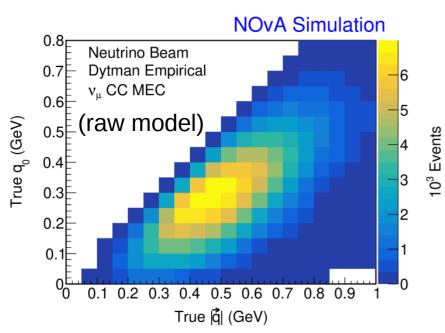


We apply the Q²-based RPA weight from QE to resonant production as a stand-in for whatever nuclear effect it may be (w/ unmodified version as uncertainty variation)

Modeling the nucleus: tuning 2p2h-MEC

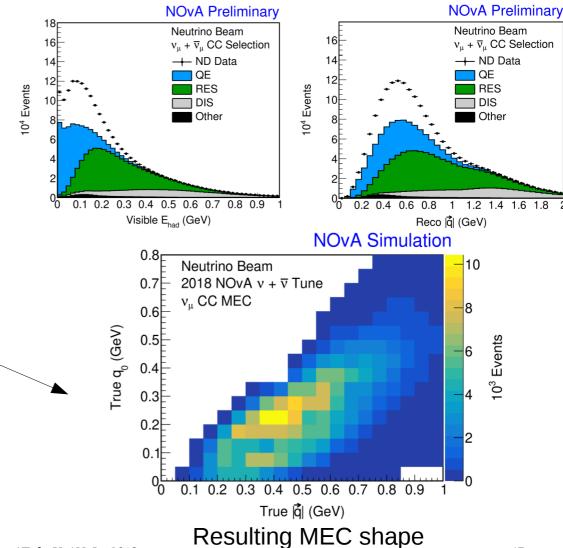
Our tuning is done in a two-dimensional space of the four-momentum transfer variables:

energy transfer q₀ and momentum transfer |q|

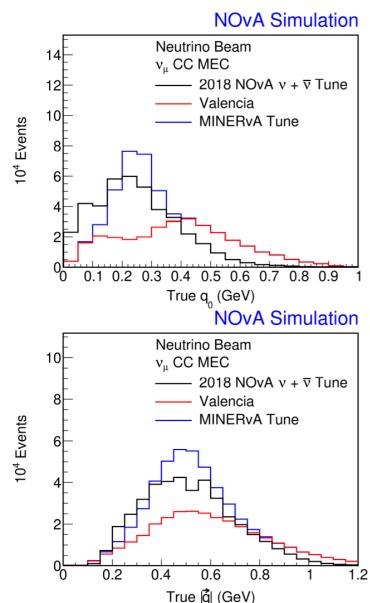


fit a weight factor for each cell in this plot

Fit in 2D space of nearest observables: Visible E_{had} ($\sim q_0$) and reco $|\mathbf{q}|$

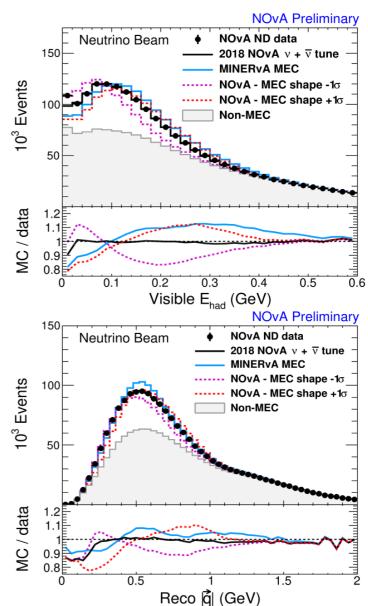


Modeling the nucleus: tuning 2p2h-MEC



MINERVA carried out a tuning procedure similar in spirit to ours (though with fewer degrees of freedom) using their data (PRD 116, 071802) which they kindly shared with us (private communication).

It is not dissimilar to the 1 σ error band we arrive at (details on error construction next slide)



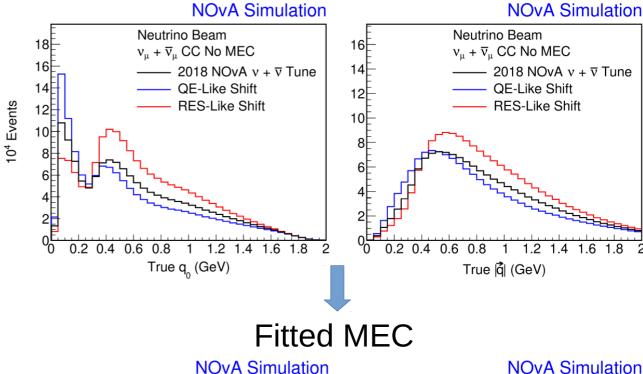
Modeling the nucleus: 2p2h-MEC uncertainties

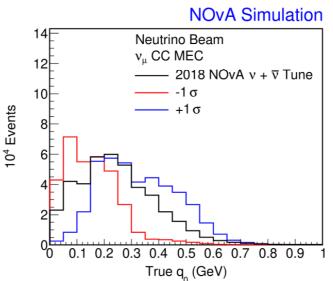
Non-MEC base

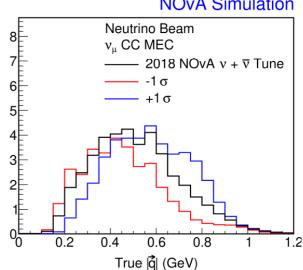
Two alternate fits:

Choose combinations of uncertainties to push initial MC more towards QE or RES

Knob	"QE-like" shift	"RES-like" shift
QE MA	+1σ (+5%)	-1σ (-5%)
QE RPA low-Q ²	+1σ	-1σ
QE RPA high-Q ²	+1σ	-1σ
QE Pauli Supp.	-1σ	+1σ
RES MA	-1σ	+1σ
RES MV	-1σ	+1σ
RES RPA	on (CV)	off

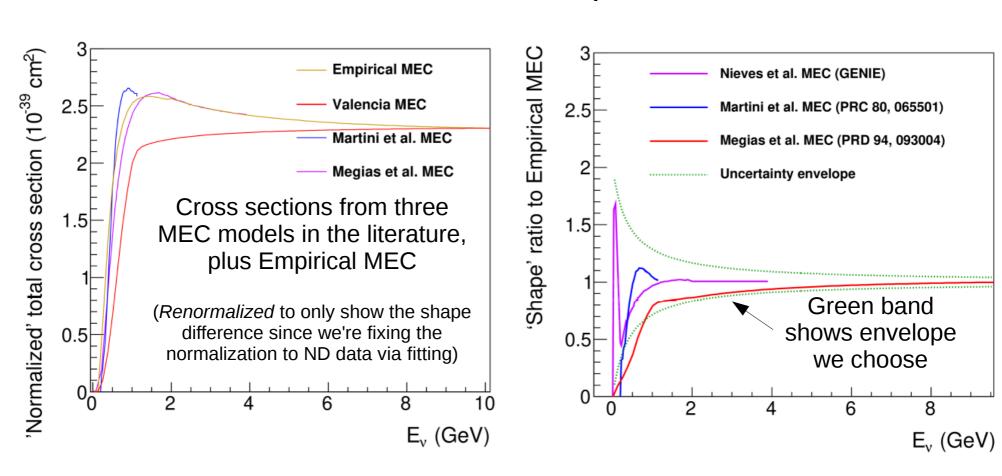






Modeling the nucleus: 2p2h-MEC uncertainties

Cross section E_v shape



Choose an envelope that more or less encloses the shapes of the predictions for our " $\pm 1\sigma$ " uncertainty

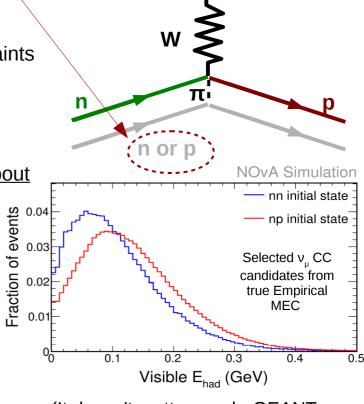
Modeling the nucleus: 2p2h-MEC uncertainties

nn-np initial state composition

• Diagrams for ν CC 2p2h allow two nucleon "pairs" in initial state: nn or np (ν has np or pp)

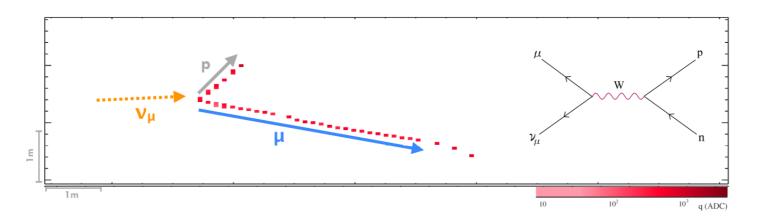
- Challenging to measure the real composition in data
 - LAr will help eventually?
 - MINERvA has made valiant efforts in the meantime, but not strong constraints on the *value* of the ratio (yet?)
- Stuck with theory for now
 - València prediction (via GENIE): ~70% np/(nn+np).
- SuSA prediction (PRC 94, 054610), detailed study: "The [np/nn] ratio is about 5-6 [i.e., np/(nn+np) ~ 80-90%] for a wide range of neutrino energies."
- Empirical MEC default is 80%

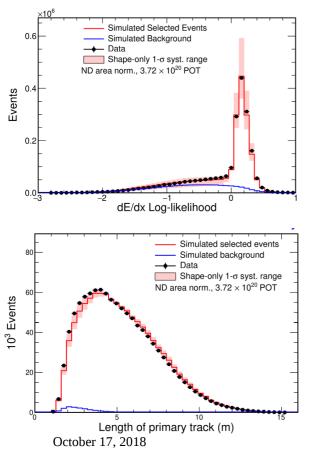
We choose
$$0.7 \le \frac{np}{(np+nn)} \le 0.9$$
 at 1σ .



(It doesn't matter much; GEANT says we get ~similar response)

ν_{μ} disappearance: selection

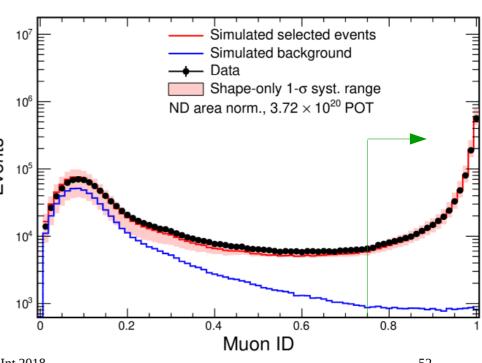




classifier uses 4 inputs:

- Track length

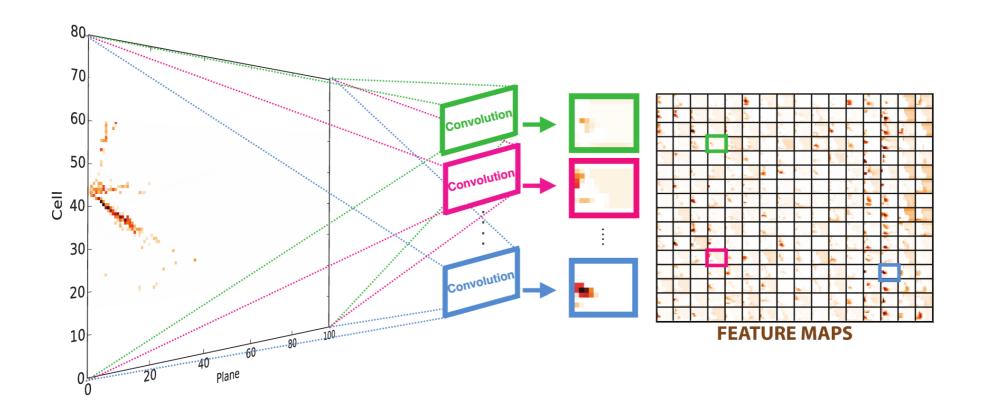
- Fraction of track planes consistent w/ single varticle de '



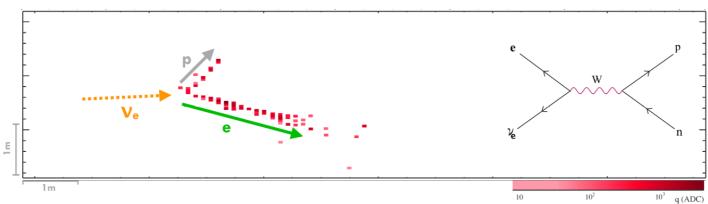
v_e appearance: selection

Event selection via a "Convolutional Neural Network":

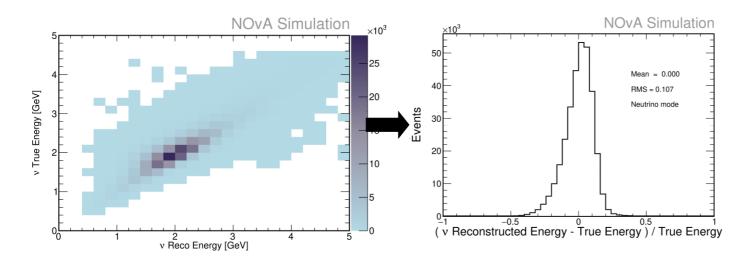
energy deposition patterns treated as images, algorithm extracts representative abstract features by applying learned filters



v_{e} appearance: selection & reconstruction



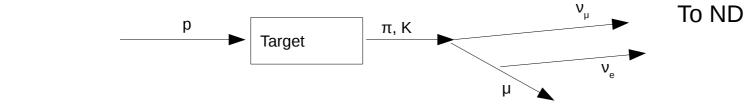
Convolutional neural network selects events via transformations applied to energy deposits treated as images

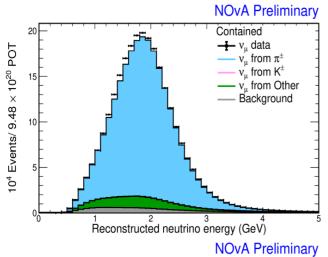


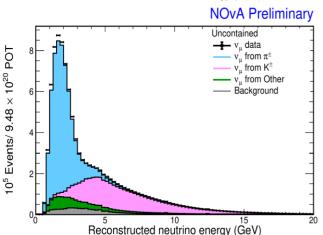
Energy estimator is quadratic function of E_e and E_{had} .

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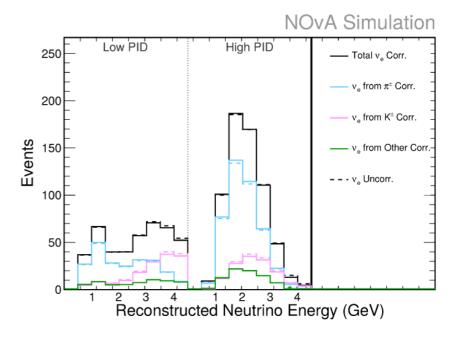
v_e appearance: constraining beam v_e bknd







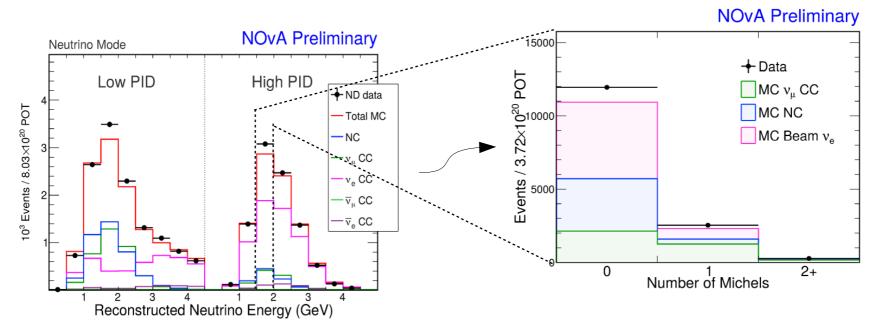
Assign discrepancies in ND v_{μ} contained and uncontained samples to flux; derive corrections according to parent mesons (which also result in beam v_{μ})



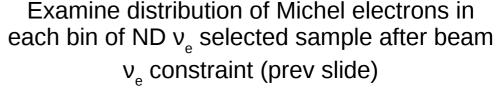
Pion-ancestor neutrinos are corrected in bins of parent (p_z , p_T). Average ~ +2%

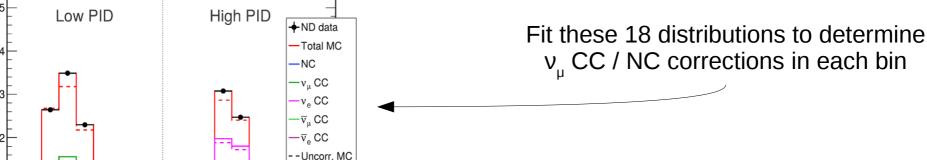
Kaon-ancestor neutrinos get a single weight: -6.3%

v_e appearance: constraining v_μ CC/NC ratio



NOvA Preliminary



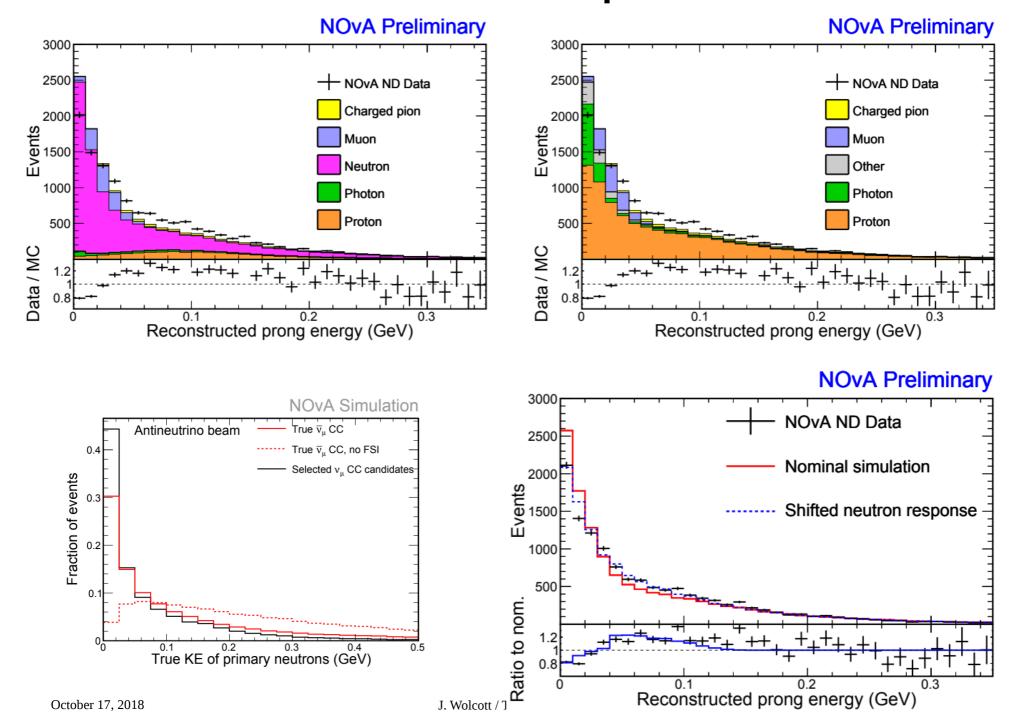


Reconstructed Neutrino Energy (GeV)

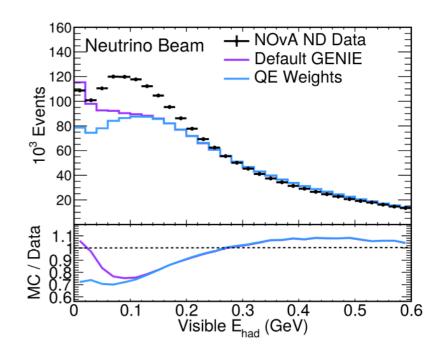
0³ Events / 8.03×10²⁰ POT

Neutrino Mode

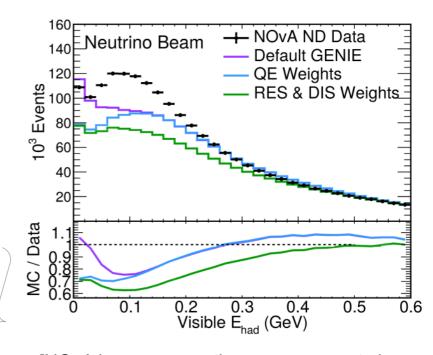
Neutron response



- More certainty about 1p1h initial state
 - RPA treatments differ in sophistication - how much detail do we need?
 - Uncertainties (from València)
 still large, not completely
 canceled by extrapolation
 - Binding/separation/removal energy situation (A. Bodek, arXiv:1801.07975)...



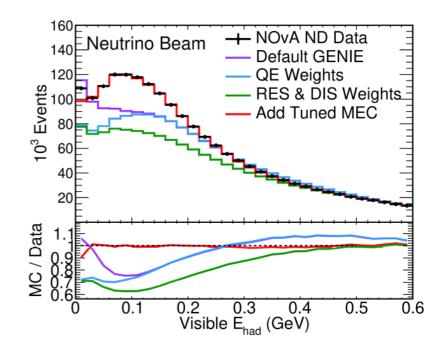
- Nuclear models for inelastic processes as well as QE
 - Apparent low-Q² suppression relative to RFG suggests nuclear effects important
 - Suggested by data (MINERvA+MINOS ND+MiniBooNE+NOvA ND)... no theory basis (yet?)
 - "On-off" treatment for syst one of our largest
 - Inelastic continuum at low E_v
 - What does "shallow" inelastic scattering on carbon at E_v = 2 GeV look like?
 - How does it interfere with RES? → GENIE uncertainties large
 - Free nucleon data helps only so much
 - Does diffractive scattering from H matter? How close are models?
- v_e/v_μ differences for inelastic processes
 - Current uncertainties are ad hoc



[NOvA has cross section measurements in progress which will help address some of these questions:

see L. Aliaga's and M. Judah's talks, next]

- More/better models for multinucleon knockout in GENIE
 - València model agrees poorly with MINERVA, NOVA ND data; no alternatives in current versions (but good things on the horizon?)
 - GENIE assumes nucleon pair ejected isotropically. Need ("semi-inclusive") models for what should *really* happen
 - Empirical tuning procedure doesn't prescribe **correlations between** ν and ν so left uncorrelated...



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- Much more v scattering data
 - Every issue mentioned above applies also for antineutrinos, only there are fewer data constraints
 - Abundance of fast neutrons an interesting challenge for calorimetry: final-state particle measurements especially helpful

