

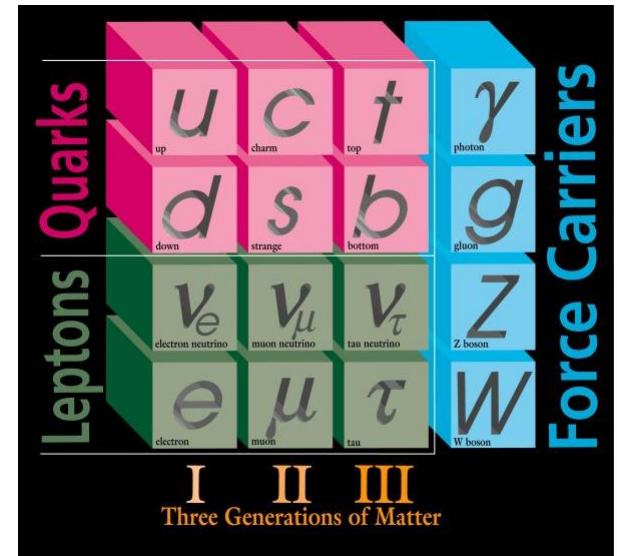
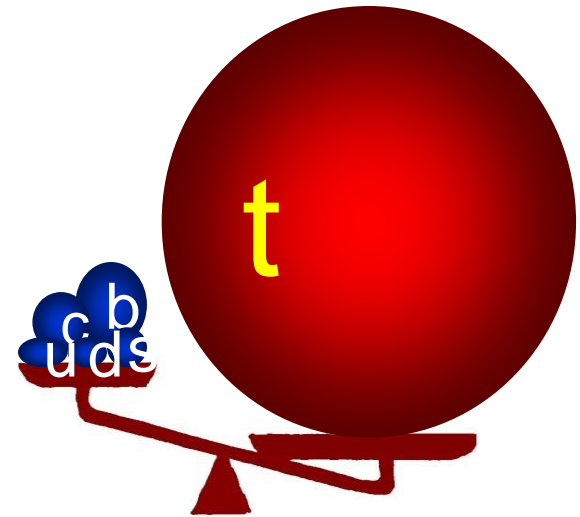
# Top Physics at Hadron Colliders

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Gottingen HASCO School 2018

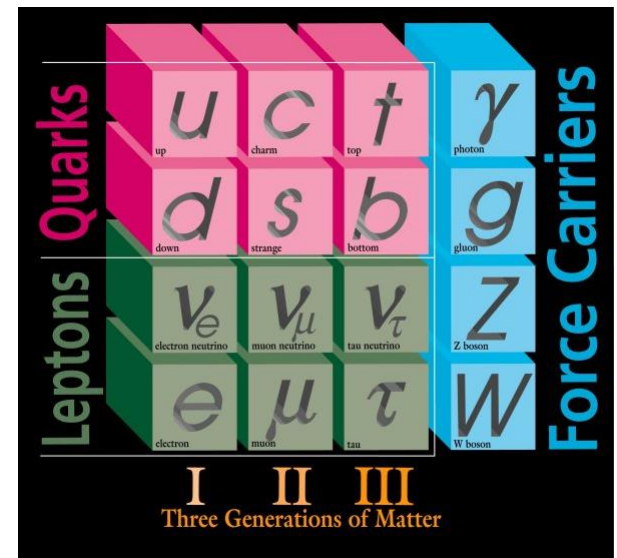
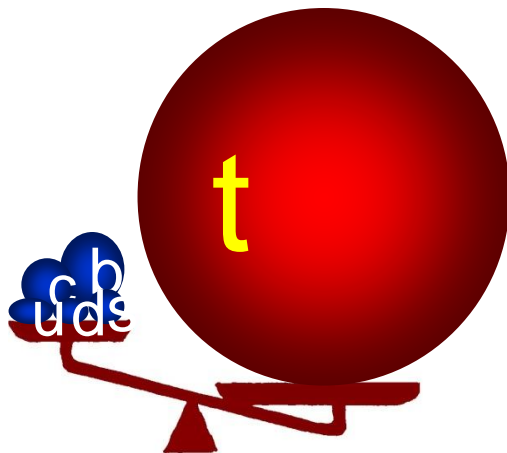
# Outline

- Motivations for studying top
- A brief history
- Top production and decay
- Identification of final states
- Cross section measurements
- Mass determination
- Single top production
- Study of top properties



# Motivations for Studying Top

- Only known fermion with a mass at the natural electroweak scale.
- Similar mass to tungsten atomic # 74, 35 times heavier than b quark.
  - ⇒ Why is Top so heavy?
  - ⇒ Is top involved in EWSB?
    - ⇒ (Does  $(2 \sqrt{2} G_F)^{-1/2} \approx M_{\text{top}}$  mean anything?)
  - ⇒ Special role in precision electroweak physics?
  - ⇒ Is top, or the third generation, special?
- New physics BSM may appear in production (e.g. topcolor) or in decay (e.g. Charged Higgs).



# Pre-history of the Top quark

**1964** Quarks (u,d,s) were postulated by Gell-Mann and Zweig, and discovered in 1968 (in electron – proton scattering using a 20 GeV electron beam from the Stanford Linear Accelerator)

**1973:** M. Kobayashi and T. Maskawa **predict the existence of a third generation** of quarks to accommodate the observed violation of CP invariance in  $K_0$  decays.

**1974: Discovery of the  $J/\psi$  and the fourth (GIM) “charm” quark** at both BNL and SLAC, and the  $\tau$  lepton (also at SLAC), with the  $\tau$  providing major support for a third generation of fermions.

**1975:** Haim Harari names the quarks of the third generation "top" and "bottom" to match the "up" and "down" quarks of the first generation, reflecting their "spin up" and "spin down" membership in a **new weak-isospin doublet** that also restores the numerical quark/ lepton symmetry of the current version of the standard model.

**1977: discovery of the fifth b quark at Fermilab** (bound with the b antiquark in Y states of quarkonium), offering new evidence for the **existence of a sixth t quark** needed to complete this isospin doublet

→ race to find the top quark starts

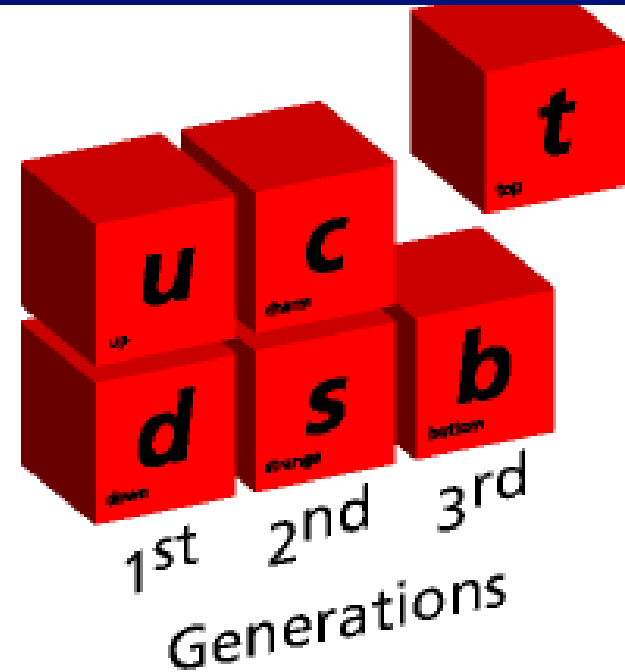


# A Brief History of Top

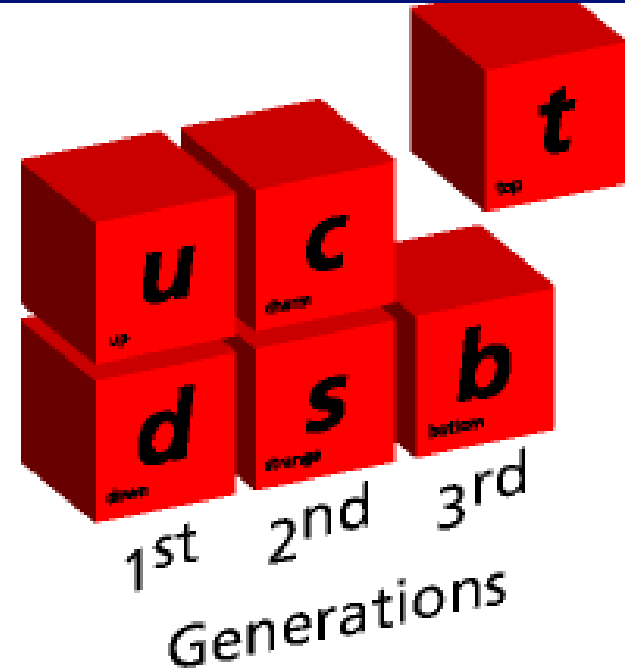
- Top quark was expected in the Standard Model (SM) of electroweak interactions as a partner of b-quark in SU(2) doublet of weak isospin for the third family of quarks

(weak isospin of b can be inferred from the forward\_backward asymmetry in  $e^+e^- \rightarrow b\bar{b}$ )

- Anomaly free SM requires the sum of the family charges to be zero: given the b (and the tau lepton) there should be a 2/3 charge quark
- Everyone thought it likely that **the top mass would be larger** than  $m_b$  but few expected a factor of  $\approx 35$  for the ratio of the masses of these supposed isospin-partner quarks.
- And few, if any, expected that it would take **so many years** to finally confirm the existence of the top quark



# A Brief History of Top II



- Initial searches for the top quark started quickly, and negative results came from  $e^+e^-$  colliders at **SLAC, DESY and KEK**.

Petra ( $e^+e^-$ ) at DESY, Hamburg,  $m_t > 23.3$  GeV (1984)  
Tristan ( $e^+e^-$ ) in Japan:  $m_t > 30.2$  GeV (late 1980s)

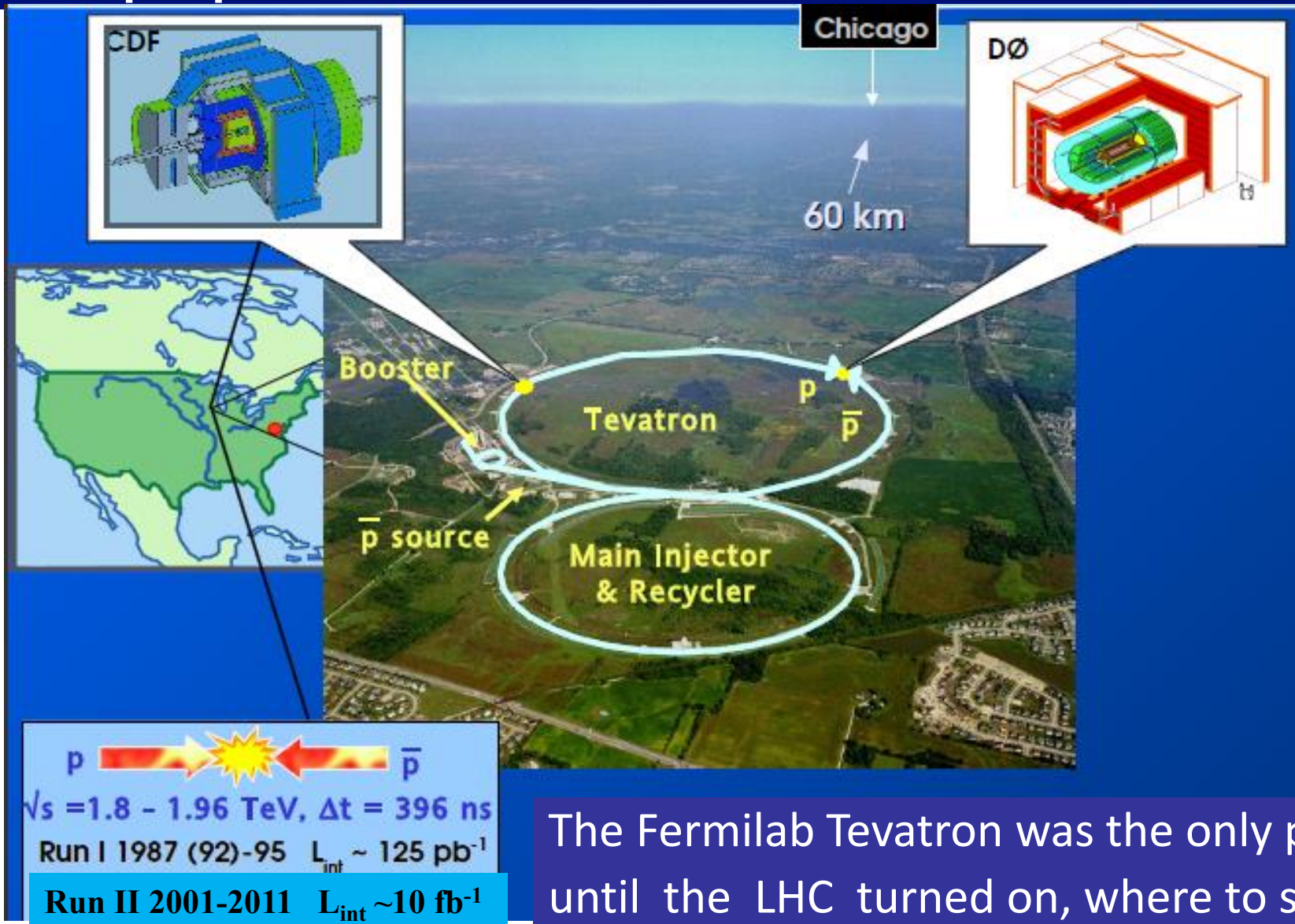
- Following the observations of the W and Z bosons at the SPS  $p\bar{p}$  collider at CERN in the early 1980s, there were claims of a discovery of the top quark in 1984 at the UA1 experiment consistent with a mass of 40 GeV (not confirmed by UA2). By 1988, this had turned into a limit ( $> 44$  GeV)

- LEP ( $e^+e^-$ ) at CERN:  $m_t > 45.8$  GeV (1990)

- This is when the **Fermilab Tevatron** entered the scene, and for more than two decades before the start of LHC operations at CERN in 2010, it was the only place in the world with enough energy to produce top quarks.

• 1977-1994: increasing lower top mass limits

# Top quark observation: at the Tevatron

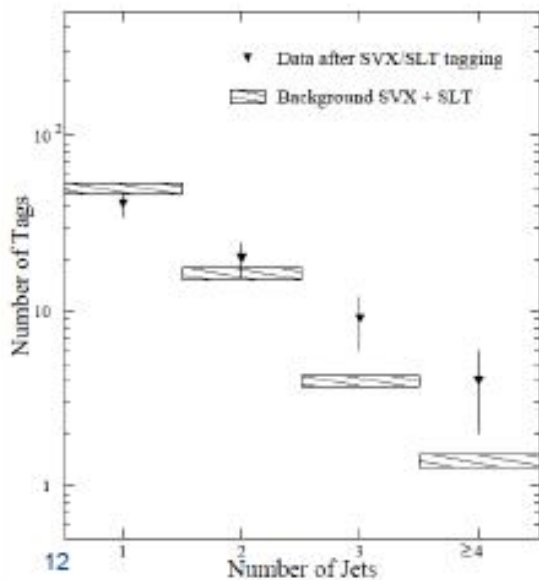


The Fermilab Tevatron was the only place, until the LHC turned on, where to study the top quark.

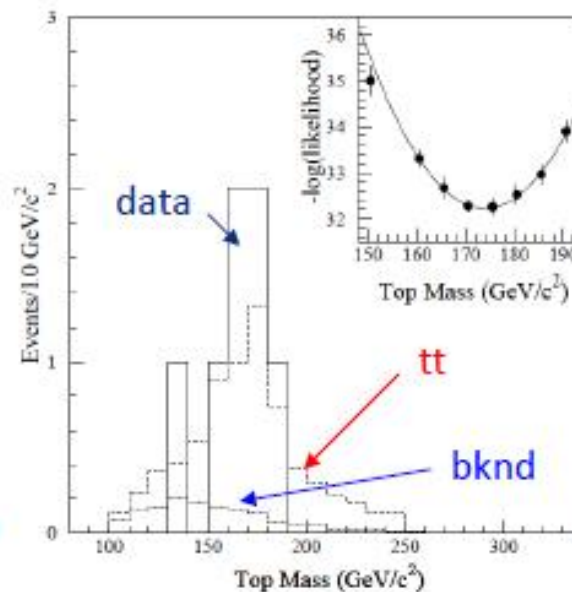
# Top quark evidence (1994)

- First top evidence in 1994 in CDF data,  $19 \text{ pb}^{-1}$ , 12 events on a background of 6, (PRL 73,225(1994)) "Evidence for Top Quark Production.."
  - $2.8 \sigma$  excess, not enough to claim discovery

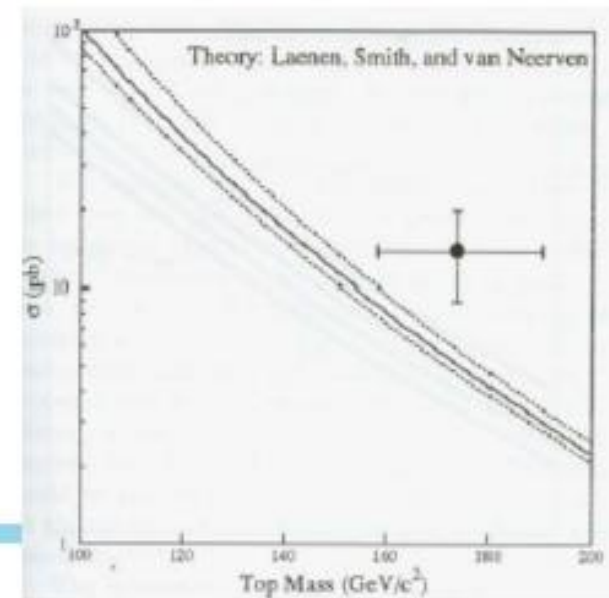
Excess over expectation appears for  $\geq 3$  jets



Mass fit from MC templates yields  $174 \pm 16 \text{ GeV}$



Cross section,  $\sigma = 13.0^{+6.1}_{-4.8} \text{ pb}$ , larger than the theoretical value of  $\sim 6 \text{ pb}$ .



# Top quark discovery (1995)



Physicists Discover Top Quark

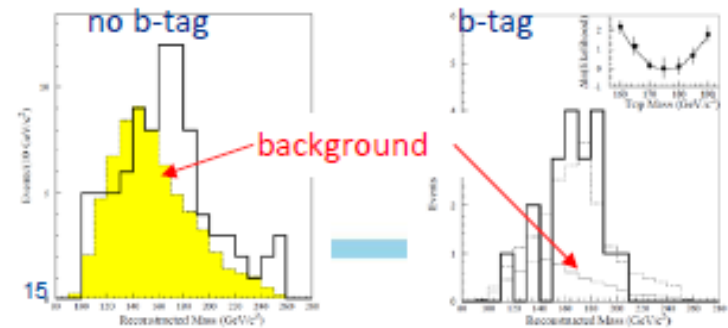
Evidence Confirmed in 1995 by CDF and D0 in first  $\sim 70 \text{ pb}^{-1}$  of run 1 data ( $4.8 \sigma$ ).

News Release - March 2, 1995

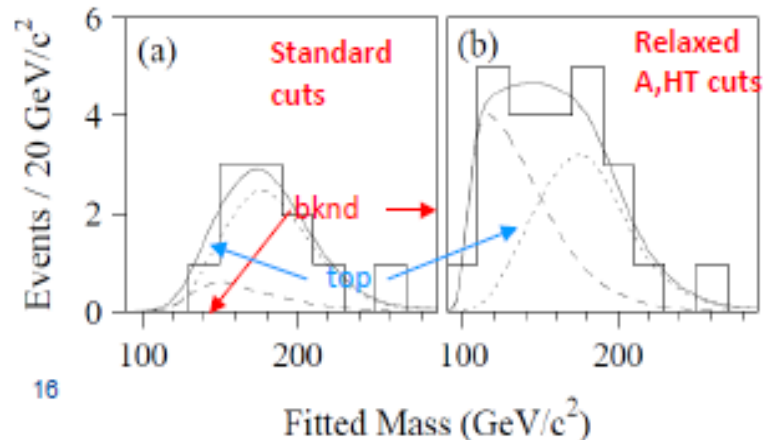
PHYSICISTS DISCOVER TOP QUARK

- **CDF top quark discovery:**
  - found 6 dilepton events and 43 lepton+jets events (50 b-tags), with estimated background of  $22.1 \pm 2.9$  tags. (PRL74,2626(1995))
  - $M_t = 176 \pm 13 \text{ GeV}$   $\sigma_{tt} = 6.8^{+3.6}_{-2.4} \text{ pb}$
- **D0 top quark discovery:**
  - found 3 dilepton events, 8 lepton+jets events (topological selection) and 6 lepton+jets events ( $\mu$  tag). Estimated background to these 17 events was  $3.8 \pm 0.6$  events (PRL74,2632(1995))
  - $M_t = 199 \pm 30 \text{ GeV}$   $\sigma_{tt} = 6.4 \pm 2.2 \text{ pb}$

Reconstructed mass distribution before and after b-tagging.



Reconstructed mass distribution





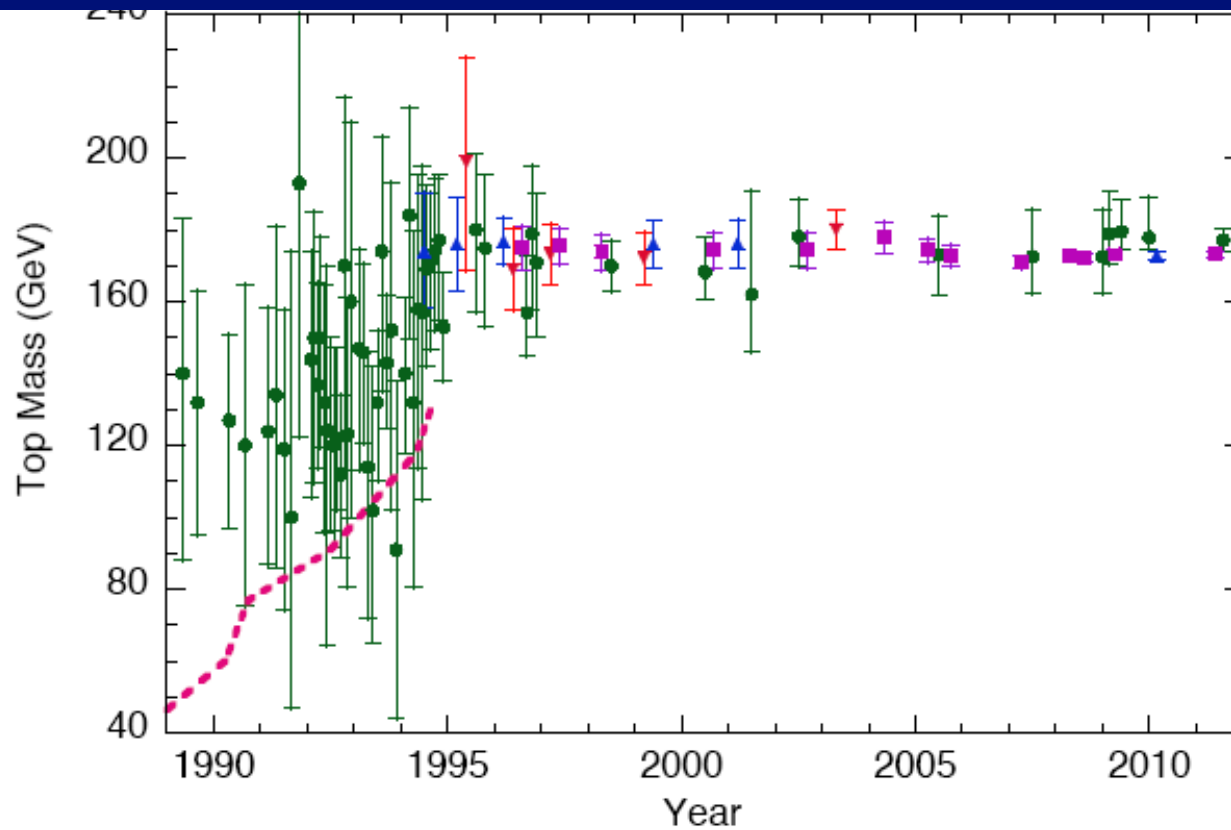
# March 2<sup>nd</sup> 1995

Discovery is always exciting!!



Adding something to the core of human knowledge is profoundly satisfying.

# Evolution of Top Mass Measurements (<2010)



**Indirect estimates** of mass of top quark from **fits to electroweak observables (green)**, and lower bounds at 95% CL on  $m_{top}$  from direct searches in ppbar collisions at CERN and at the **Tevatron (broken line)**, assuming standard  $W \rightarrow bt$  or  $t \rightarrow bW$  decays. Results on  $m_{top}$  from **CDF (up-triangle)** and **DØ (down-triangle)**, and **mean  $m_{top}$  (purple square)**.

**Top Quark is now “standard”!**



# A Brief History of Top (2011-2018)

- Tevatron Run 2 ends in 2011 after 26 years of successful operation:  $10 \text{ fb}^{-1}$  collected in Run II by each experiment
- LHC Run 1 starts in 2010 at 7 TeV :  $5 \text{ fb}^{-1}$  collected in 2011
- 2012: the energy is increased to 4 TeV per beam (8 TeV in collisions)
- 2015: RunII starts at 13 TeV
- **LHC is a top factory**

## No. of produced $t\bar{t}$ events

**2011:** ~800k (4.6/fb, 7 TeV)  
**2012:** ~5.1 million (20.3/fb, 8 TeV)  
**2015:** ~2.6 million (3.2/fb, 13 TeV)

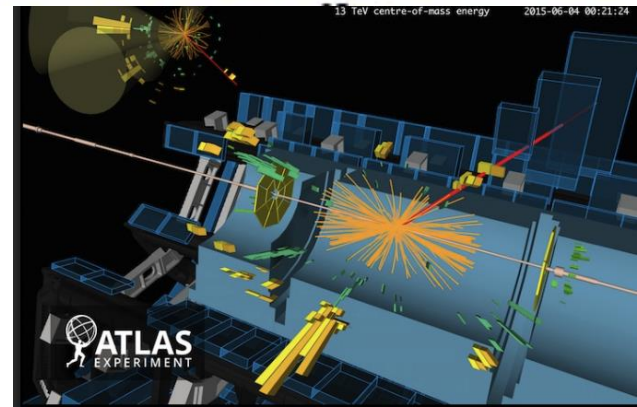
**Since 2016: > 30 million per year (36/fb, 13 TeV)**

- Tevatron produced ten t-tbar pair per day
- LHC: one t-tbar pair per second
- Top quark is one of the major subject of study at LHC



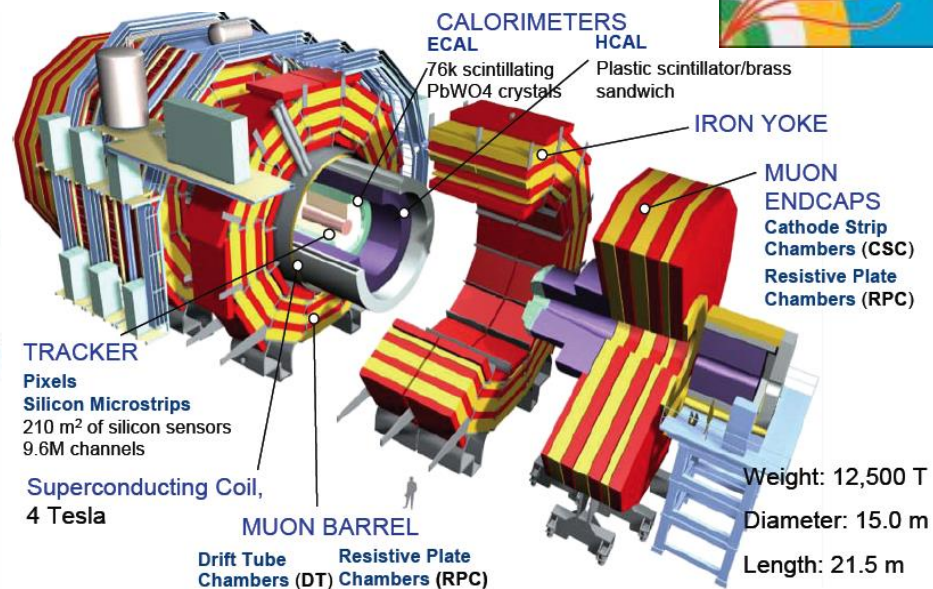
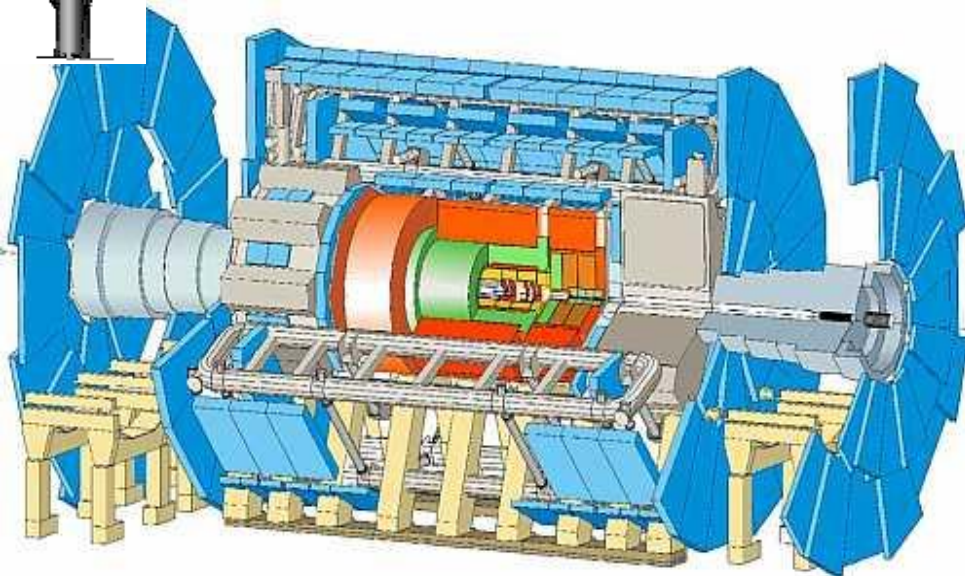
## The Large Hadron Collider:

- proton-proton collider
- high energy:  $\sqrt{s} = 7 \text{ TeV}$
- since 2012:  $\sqrt{s} = 8 \text{ TeV}$
- 2014-2030???:  $\sqrt{s} = 13 \text{ TeV}$





# ATLAS and CMS Detectors



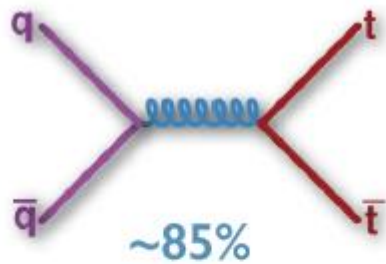
	Weight (tons)	Length (m)	Height (m)
ATLAS	7,000	42	22
CMS	12,500	21	15

**~3000 Scientists per experiment  
 + many engineers and technicians**

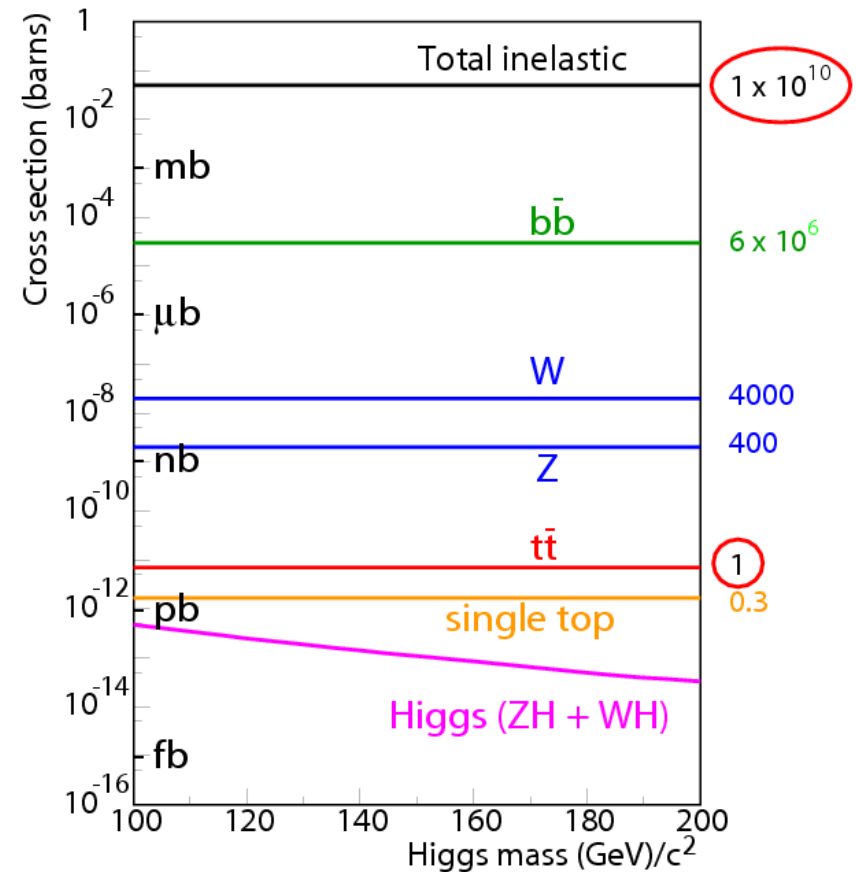
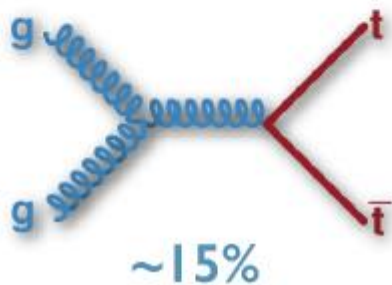
# How is top quark produced?

Tevatron: preferentially  
top Pair Production

$$\sigma_{\text{SM}} \sim 7.35 \cdot \text{pb}$$



strong pair production

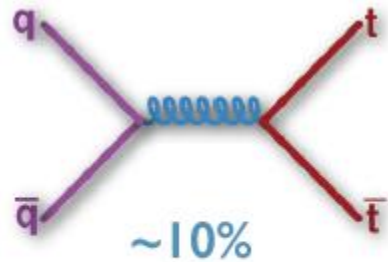


One top pair each  $10^{10}$  inelastic collisions at  $\sqrt{s} = 1.96 \text{ TeV}$

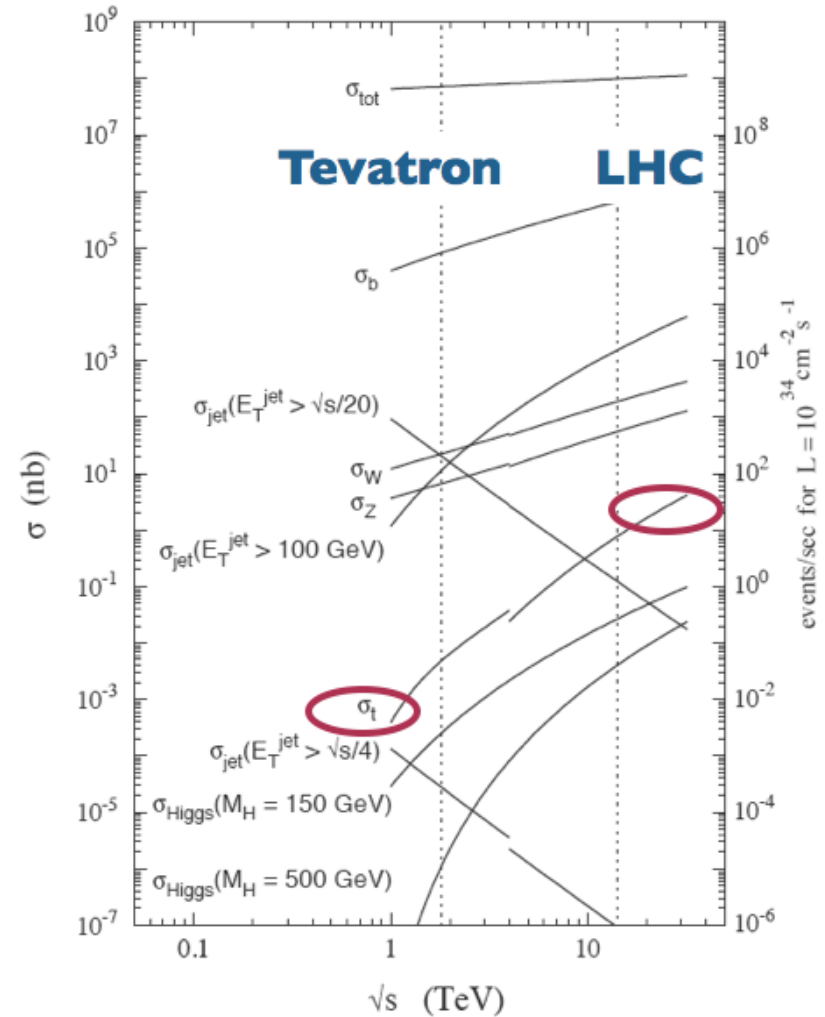
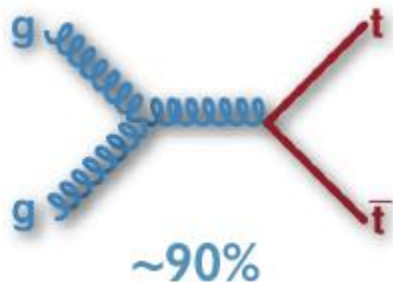
# How is top quark produced?

LHC (13 TeV) preferentially  
top Pair Production

$$\sigma_{\text{SM}} \sim 830 \text{ pb}$$



strong pair production



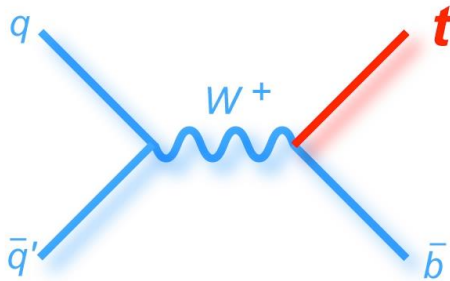
One top pair each  $10^8$  inelastic collisions at  $\sqrt{s} = 13 \text{ TeV}$

LHC is a top factory!!

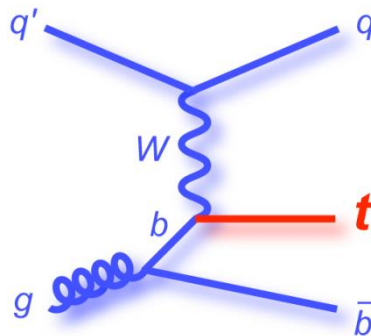
# How is top quark produced?

- Top quark can be produced also **singly, via electroweak interactions**, with a smaller cross section, at both Tevatron and LHC
- Single top observed for the first time at the Tevatron in 2009 (see later...)

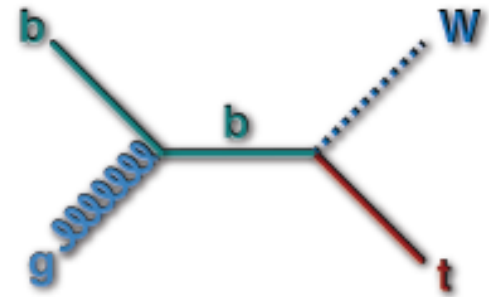
s-channel



t-channel

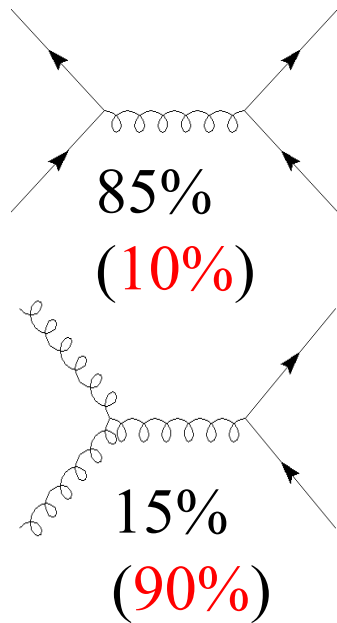


Wt-production



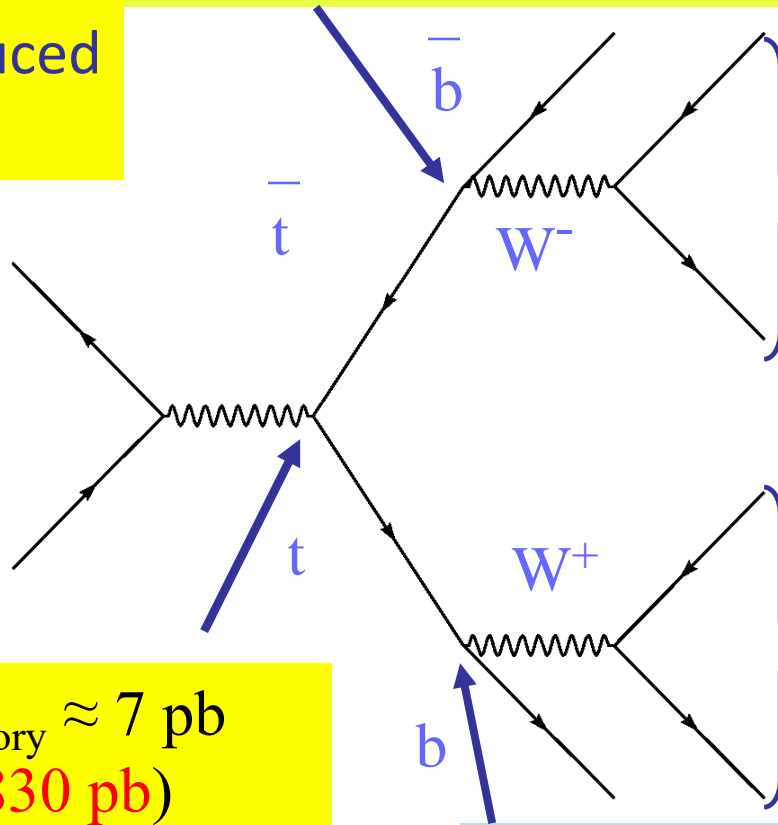
# Production and Decay Basics

At the Tevatron and LHC top quarks are mainly pair produced via strong interaction:



NB: qq, gg fractions reversed at LHC

SM predicts:  $BR(t \rightarrow Wb) \approx 100\%$



$\sigma_{\text{theory}} \approx 7 \text{ pb}$   
( $\approx 830 \text{ pb}$ )  
QCD predicts cross section well

Event topology determined by the decay modes of the 2 W's ( $W^+W^-$ ) in final state

b-jet: identify via secondary vertex or soft lepton tag

# Top Decay : add. Motivation for Studying Top

- In the SM, assuming V-A coupling:

$$\Gamma(t \rightarrow d_j W^+) \sim |V_{tj}|^2 \frac{G_F m_t^3}{8\pi\sqrt{2}}$$

assuming  $|V_{tb}| = 1$  for the  $t \rightarrow bW$  decay vertex, one gets (LO):

$$\Gamma(t \rightarrow bW) \approx 175 \text{ MeV} (M_T/M_W)^2 \quad (M_T, M_W \gg M_b)$$

$$\Rightarrow \Gamma(t \rightarrow bW) \approx 1.5 \text{ GeV} (> \Lambda_{\text{QCD}}) \Rightarrow \tau(\text{top}) \approx 5 \times 10^{-25} \text{ s}$$

- Non-perturbative QCD hadronization takes place in a time of order:

$$\Lambda_{\text{QCD}}^{-1} \sim (100 \text{ MeV})^{-1} \sim 10^{-23} \text{ s}$$

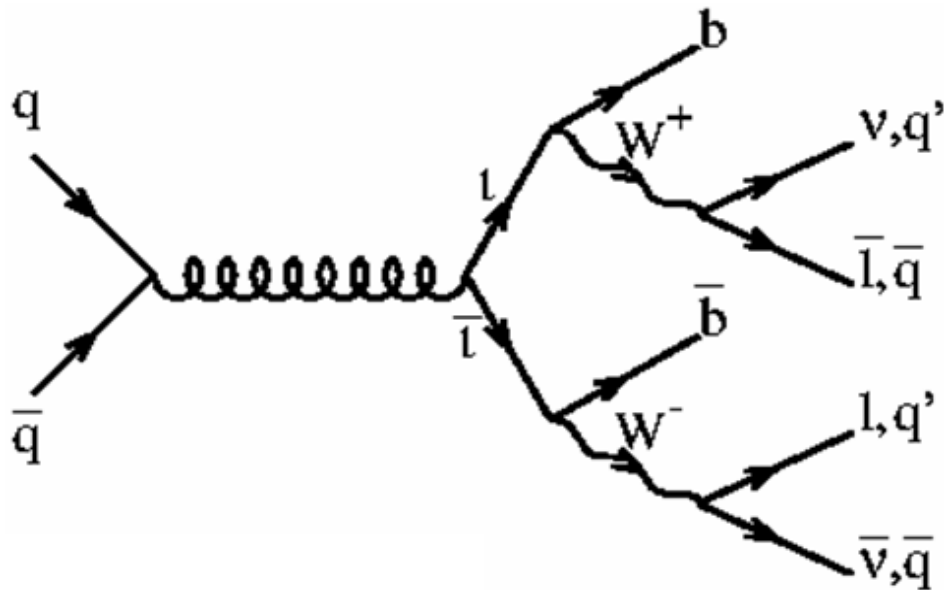
- top decays before hadronizing, as free quark (no top hadrons, no toponium spectroscopy)
- the top quark provides the first opportunity to study the decay characteristics of a “bare” quark.
- $t \rightarrow Ws$ ,  $t \rightarrow Wd$  allowed but suppressed by factors of  $\sim 10^{-3}$  and  $\sim 5 \times 10^{-5}$  respectively

# How to identify the top quark

SM:  $t\bar{t}$  pair production,  $\text{Br}(t \rightarrow bW) = 100\%$ ,  $\text{Br}(W \rightarrow lv) = 1/9 = 11\%$

dilepton	$(4/81)$	2 leptons + 2 jets + missing $E_T$
lepton+jets	$(24/81)$	1 lepton + 4 jets + missing $E_T$
fully hadronic	$(36/81)$	6 jets

(here:  $l=e,\mu$ )

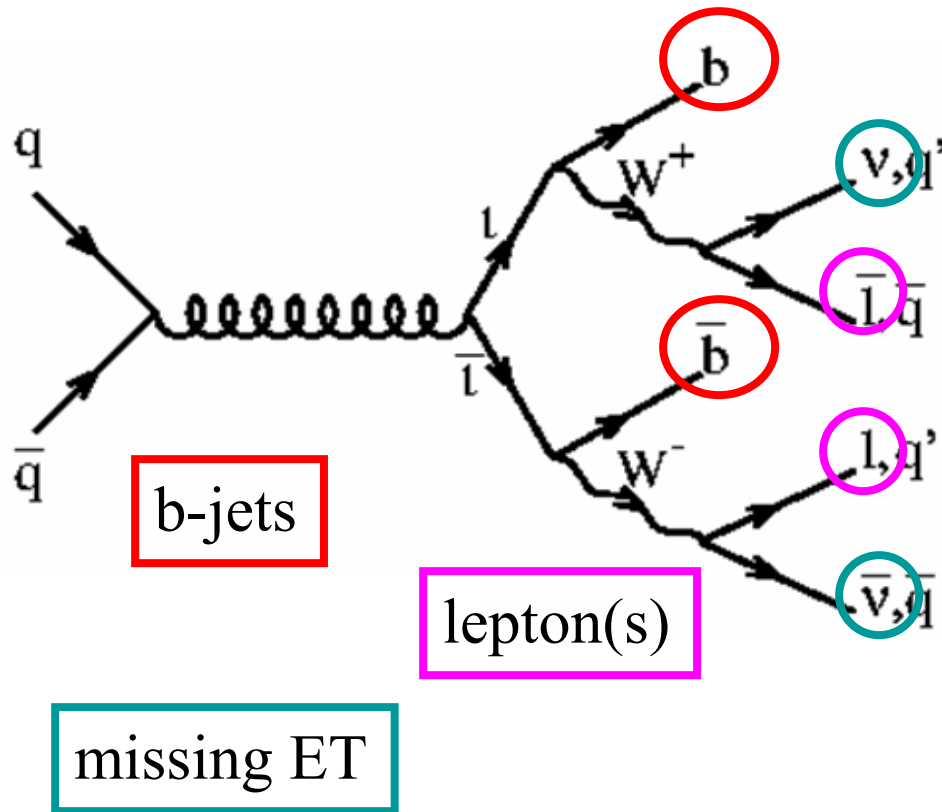




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dilepton	(4/81)	2 leptons + 2 jets + missing $E_T$
lepton+jets	(24/81)	1 lepton + 4 jets + missing $E_T$
fully hadronic	(36/81)	6 jets



Dilepton ( $ee, \mu\mu, e\mu$ )  
 $\Rightarrow \text{BR} = 5\%$

- Relatively clean:
  - Very small amount of SM bkgds
  - Down side: small event samples
- Select:
  - 2 leptons:  $ee, e\mu, \mu\mu$
  - Large missing  $E_T$
  - 2 jets (with or w/o b-tag)
- Expect:  $S/B > 1$
- Dominant backgrounds: Drell-Yan,  $W$ +jets ("fakes")

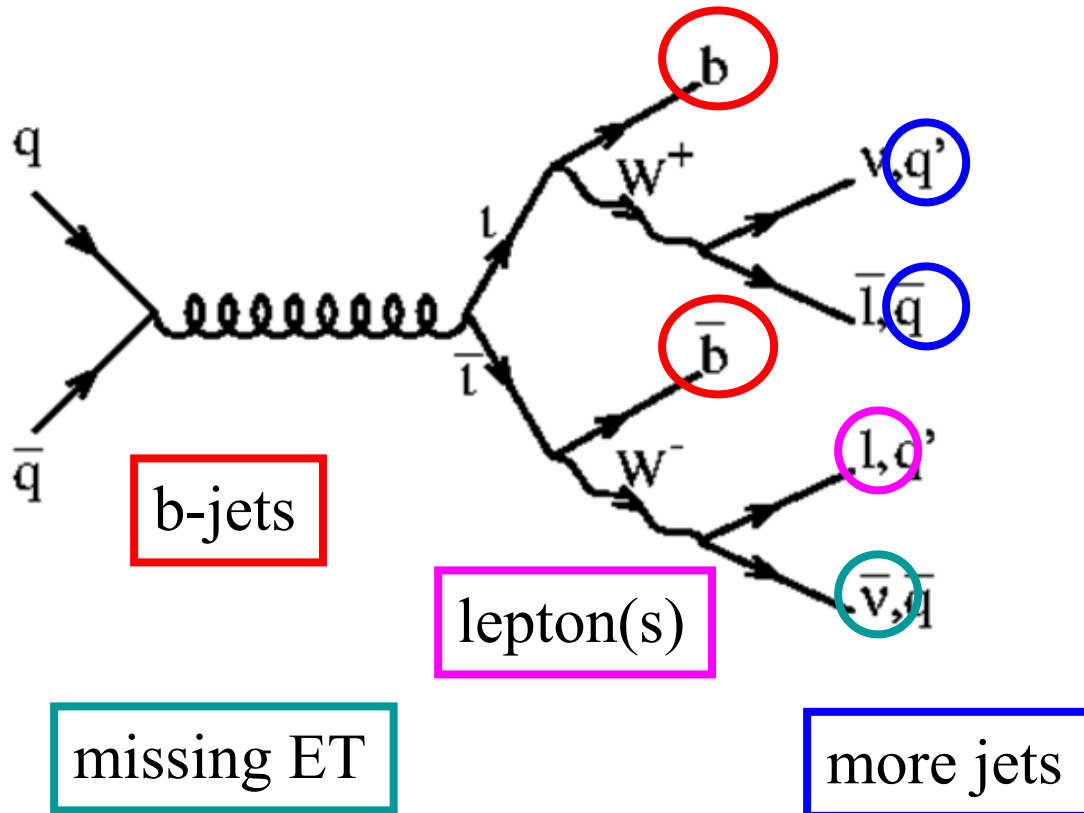


# How to identify the top quark

SM:  $t\bar{t}$  pair production,  $\text{Br}(t \rightarrow bW) = 100\%$ ,  $\text{Br}(W \rightarrow l\nu) = 1/9 = 11\%$

dilepton	(4/81)	2 leptons + 2 jets + missing $E_T$
lepton+jets	(24/81)	1 lepton + 4 jets + missing $E_T$
fully hadronic	(36/81)	6 jets

Lepton (e or  $\mu$ ) + jets  
 $\Rightarrow \text{BR} = 30\%$



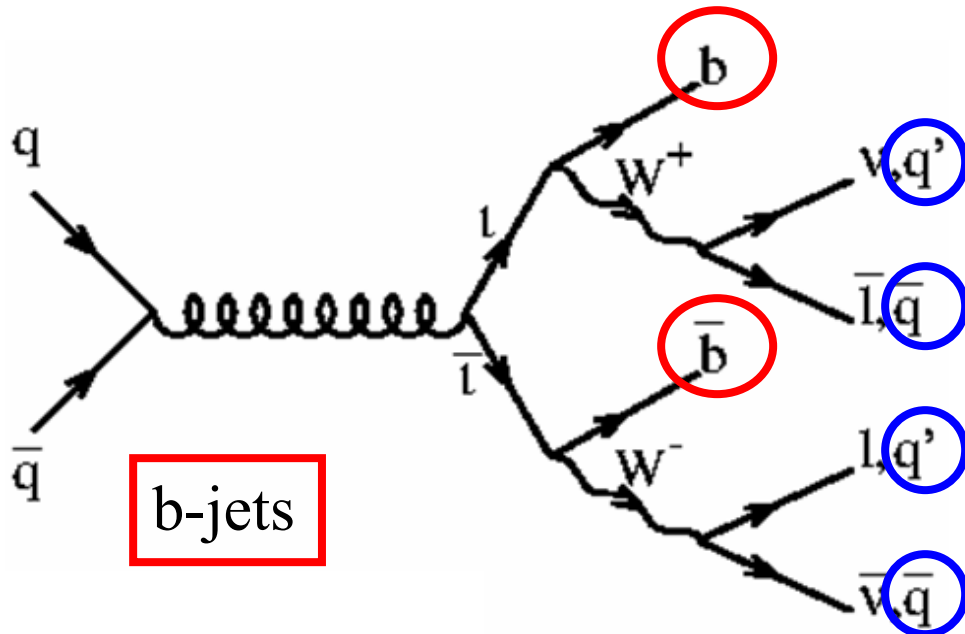
- Select:
  - 1 electron or muon
  - Large missing  $E_T$
  - 1 or 2 b-tagged jets
- Fully reconstructable, small backgrounds
- Main backgrounds:
  - W/Z +jets
  - WZ +heavy flavor
  - QCD multijet (data-driven)
  - Diboson (from MC)

# How to identify the top quark

SM:  $t\bar{t}$  pair production,  $\text{Br}(t \rightarrow bW) = 100\%$ ,  $\text{Br}(W \rightarrow l\nu) = 1/9 = 11\%$

dilepton	(4/81)	2 leptons + 2 jets + missing $E_T$
lepton+jets	(24/81)	1 lepton + 4 jets + missing $E_T$
fully hadronic	(36/81)	6 jets

All-hadronic  
 $\Rightarrow \text{BR} = 44\%$



b-jets

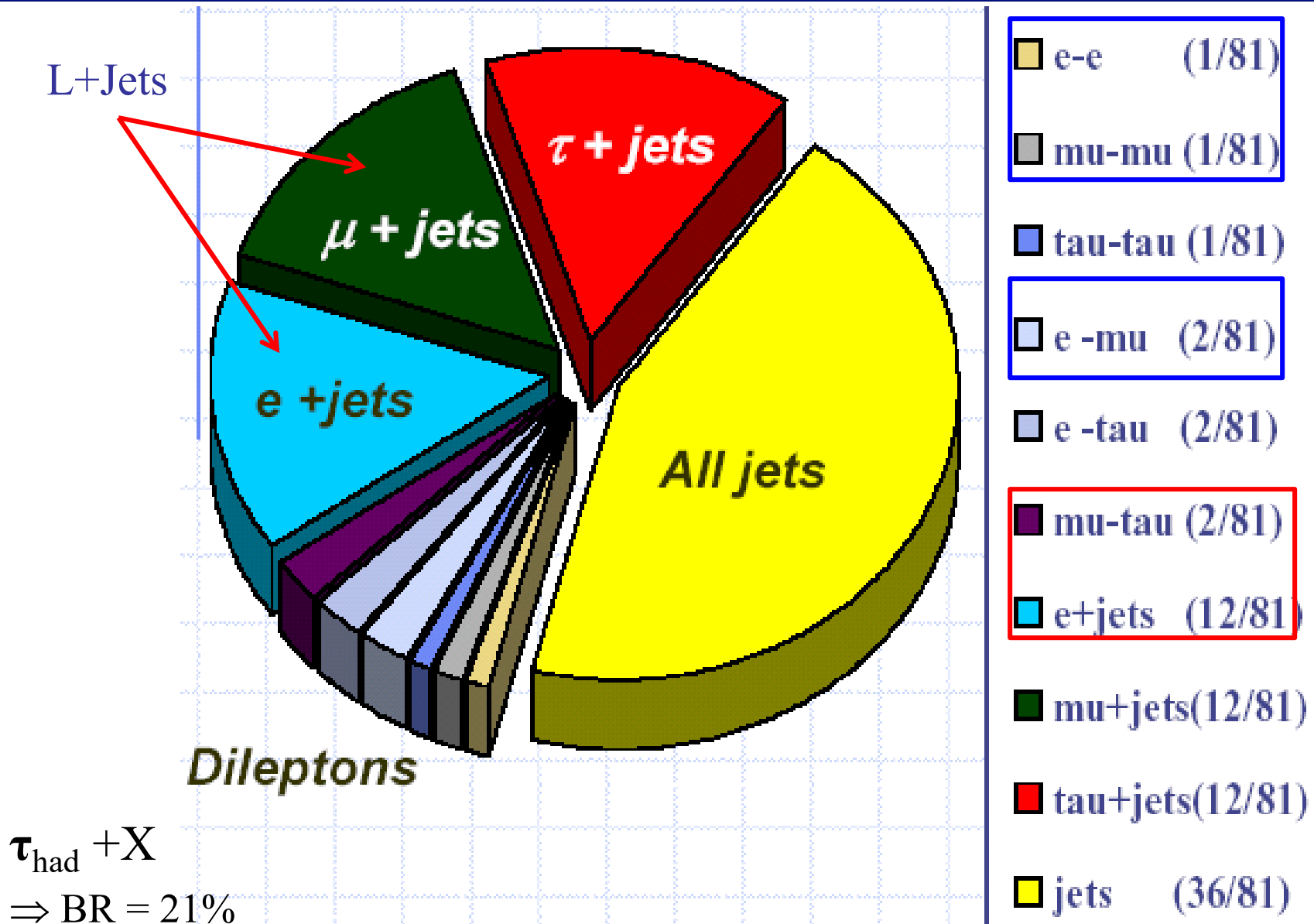
more jets

**Signature:**

- 6 or more jets
- kinematical selection
- $\geq 1$  vertex tag.

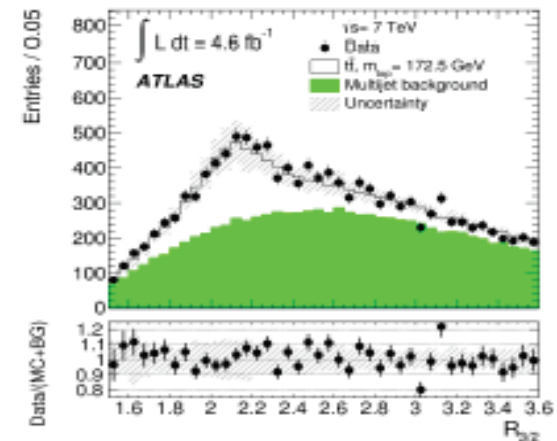
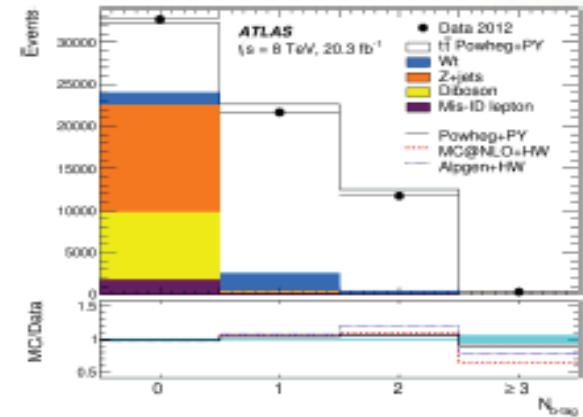
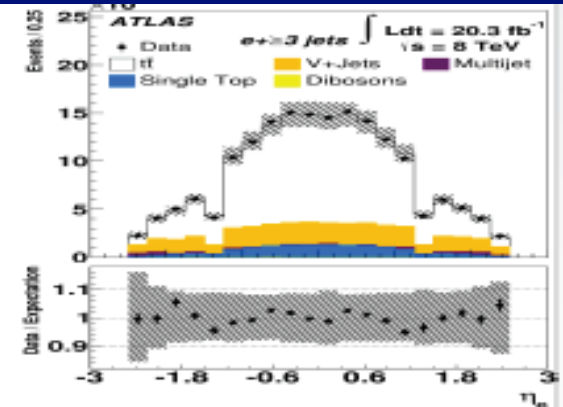
Large backgrounds from QCD multijet production

# Top Event Categories



# Pros and cons by final state channel:

- **Lepton + jets (“golden” channel)**
  - fairly good branching ratio
  - Reasonable S/B
  - One  $\nu$  so can fully reconstruct t-tbar system
- **Dilepton:**
  - Lowest branching ratio but...
  - Highest S/B
  - $2\nu \rightarrow$  reconstruction of t-tbar system ambiguous
- **All hadronic**
  - Highest branching ratio, but...
  - lowest S/B ratio
  - Dominant QCD background hard to determine
  - combinatorics of t-tbar reconstruction complex



# Method to identify a top signal

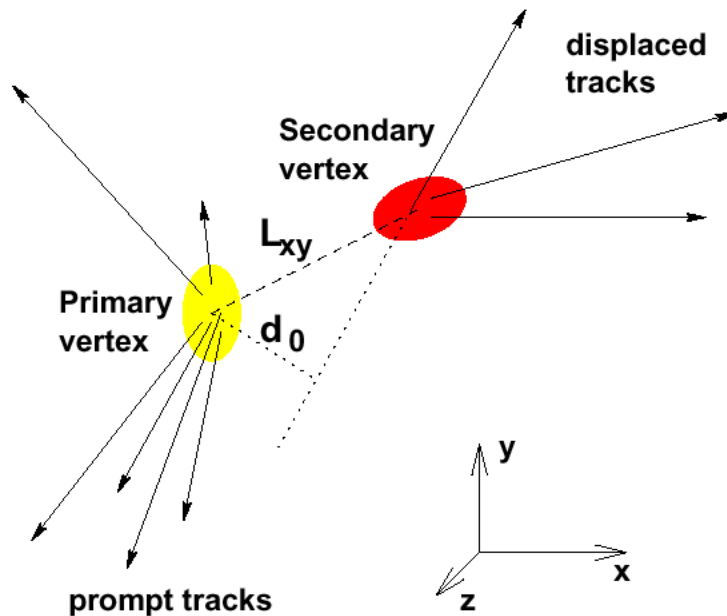
- Start from “counting events” passing cuts in all decay channels
  - ⇒ Optimization of signal region with respect to SM background processes (control region)
- Background dominates the production of  $t\bar{t}$  pairs
- How to separate signal from background:
  - ⇒ Top events have very distinctive signatures
    - ✓ Decay products (leptons, neut., jets) have large  $p_T$ 's
    - ✓ Event topology: central and spherical
    - ✓ Heavy flavor content: always 2 b jets in the final state!

# B-Tagging Tools: Vertexing and Soft Muons

B hadrons in top signal events:

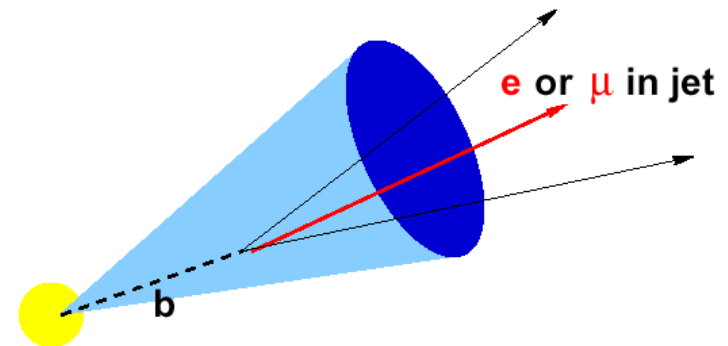
are long-lived and massive

Vertex of displaced tracks



may decay semileptonically

Identify low-pt muon from decay



- $b \rightarrow l\nu c$  (BR  $\sim 20\%$ )
- $b \rightarrow c \rightarrow l\nu s$  (BR  $\sim 20\%$ )

$\sim 60\%$   $\leftarrow$  Top Event Tag Efficiency  $\rightarrow$   $\sim 15\%$   
 $\sim 0.5\%$   $\leftarrow$  False Tag Rate (QCD jets)  $\rightarrow$   $\sim 2\%$

# Why measure the $t\bar{t}$ Cross Section?

- Basic “engineering number”, absolute measurement ( $\rightarrow$  **very difficult!**), prior step to any top property study.
- Requires detailed understanding of backgrounds and selection efficiencies.
- **Test of SM QCD predictions**
  - Departures from QCD prediction could indicate nonstandard production mechanisms, i.e. production through decays of SUSY states.
- It is Important to measure cross section in all decay channels

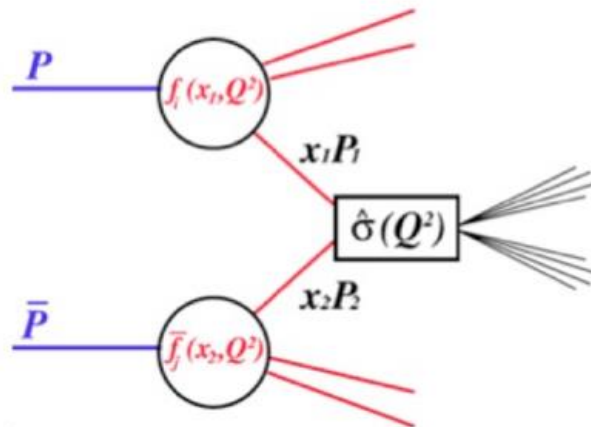
$$\sigma(t\bar{t}) = \frac{N_{obs} - N_{back}}{\epsilon \times A \times \int L dt}$$

- $\epsilon$ : selection efficiency for events in acceptance (affected by errors in trigger and reconstruction)
- $A$ : Acceptance (depends on PDF, and other modeling uncertainties)
- $\int L dt$ : integrated luminosity

# What is a cross section?

Integrated cross section:  $\sigma = \int [d\sigma/d\Omega] d\Omega$

Calculation:



$$\sigma = \sum_{i,j=q,\bar{q},g} \int dx_1 dx_2 f_i(x_1, Q^2) \cdot \bar{f}_j(x_2, Q^2) \cdot \hat{\sigma}(Q^2)$$

Sum over incoming partons  $i, j$

Momentum fraction for incoming parton

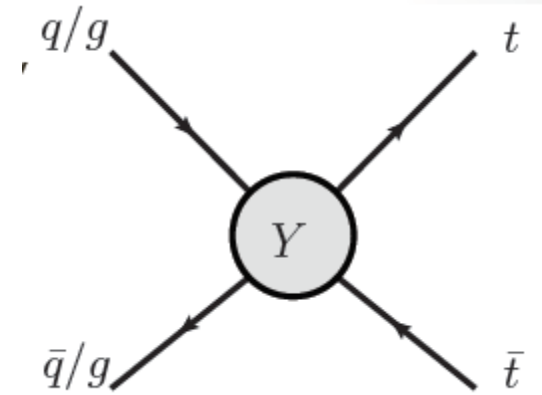
PDF for incoming parton  $i$

“partonic” cross section



# Partonic cross section

- Need to calculate everything that goes into  $Y$
- Use perturbative expansion of  $Y$  in orders of strong coupling constant ( $\alpha_s$ )
- $\alpha_s \sim 0.1$  so series should converge



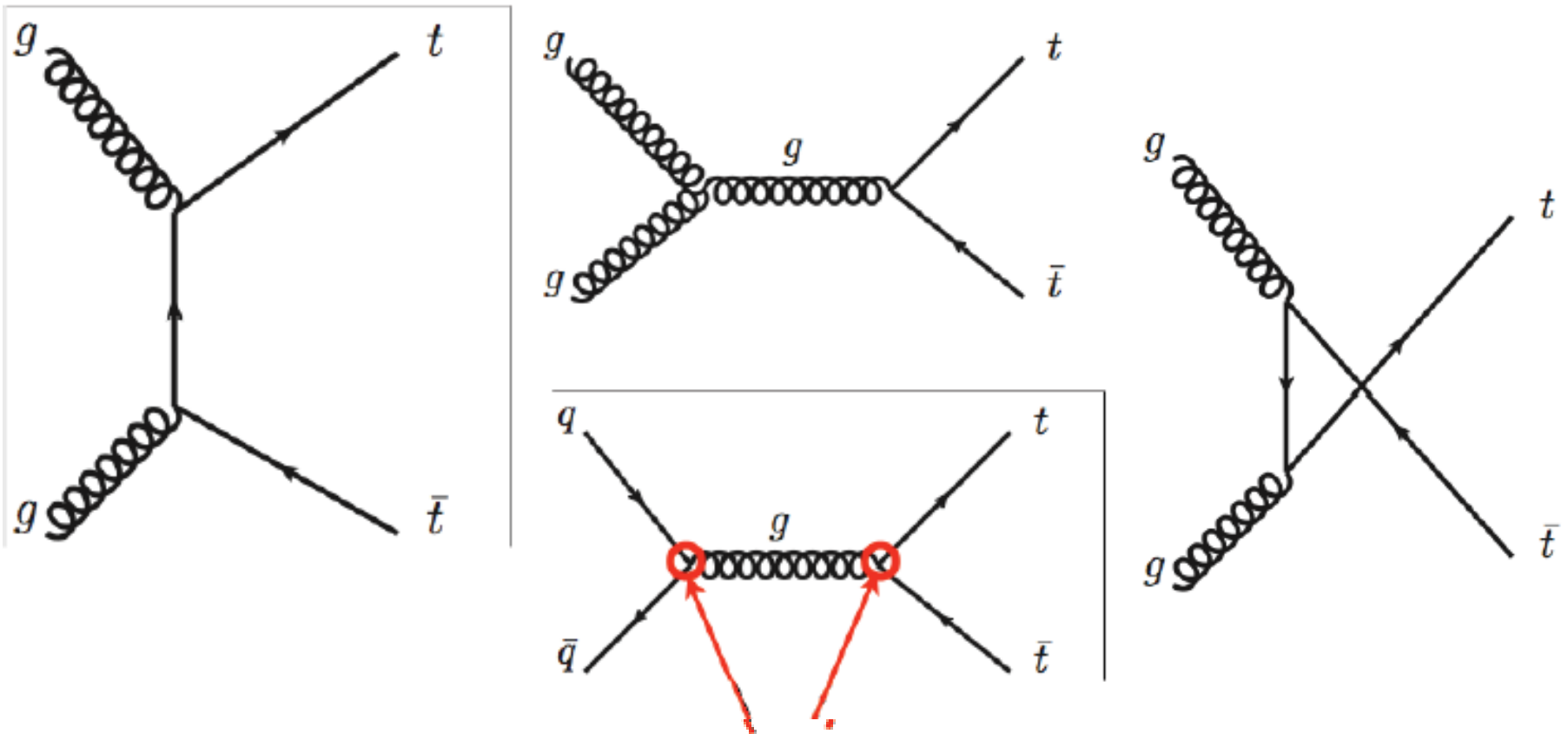
$$\sigma (q\bar{q}/gg \rightarrow t\bar{t} + X) = H^{(0)} + \alpha_s H^{(1)} + \alpha_s^2 H^{(2)} + \dots$$

Leading order (LO) term,  
proportional to  $\alpha_s^2$

Next-to-leading  
order (NLO) term,  
proportional to  $\alpha_s^3$

Next-to-next-to-leading  
order term,  
proportional to  $\alpha_s^4$

# Leading order



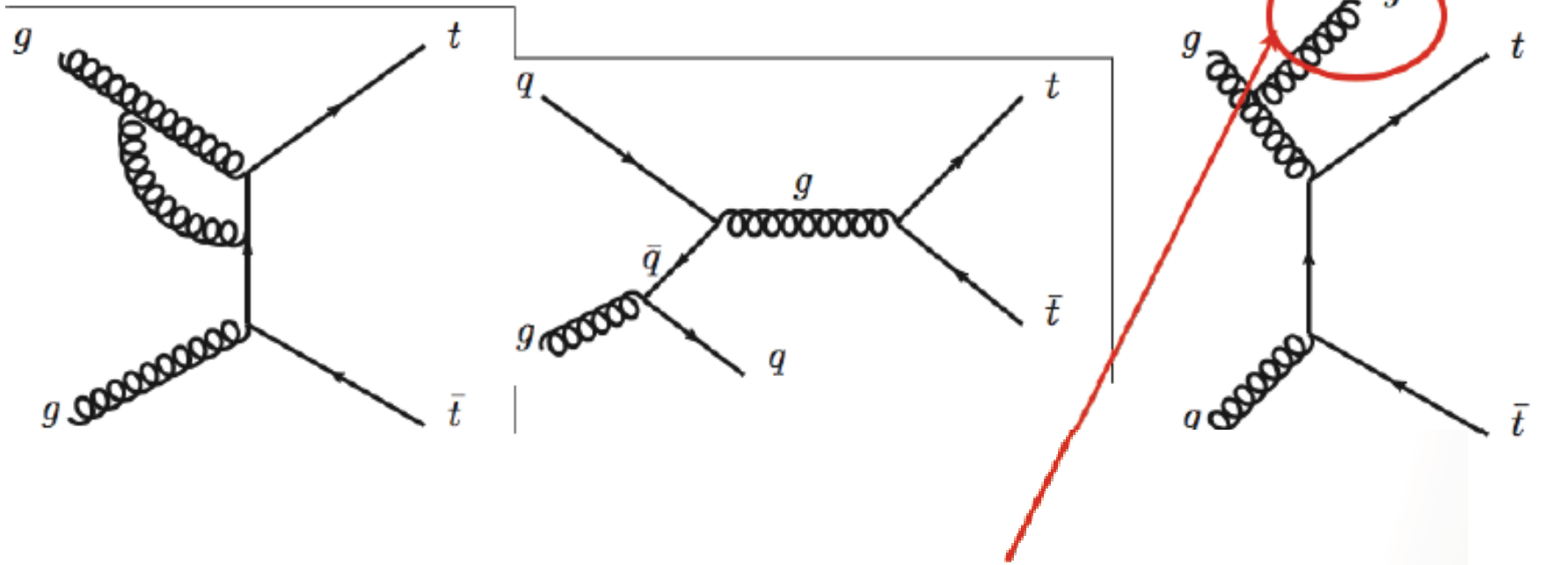
Each vertex contributes:  $\sqrt{\alpha_s}$

$\alpha_s$  = strong force (QCD) coupling constant

Leading order (LO): contains all terms

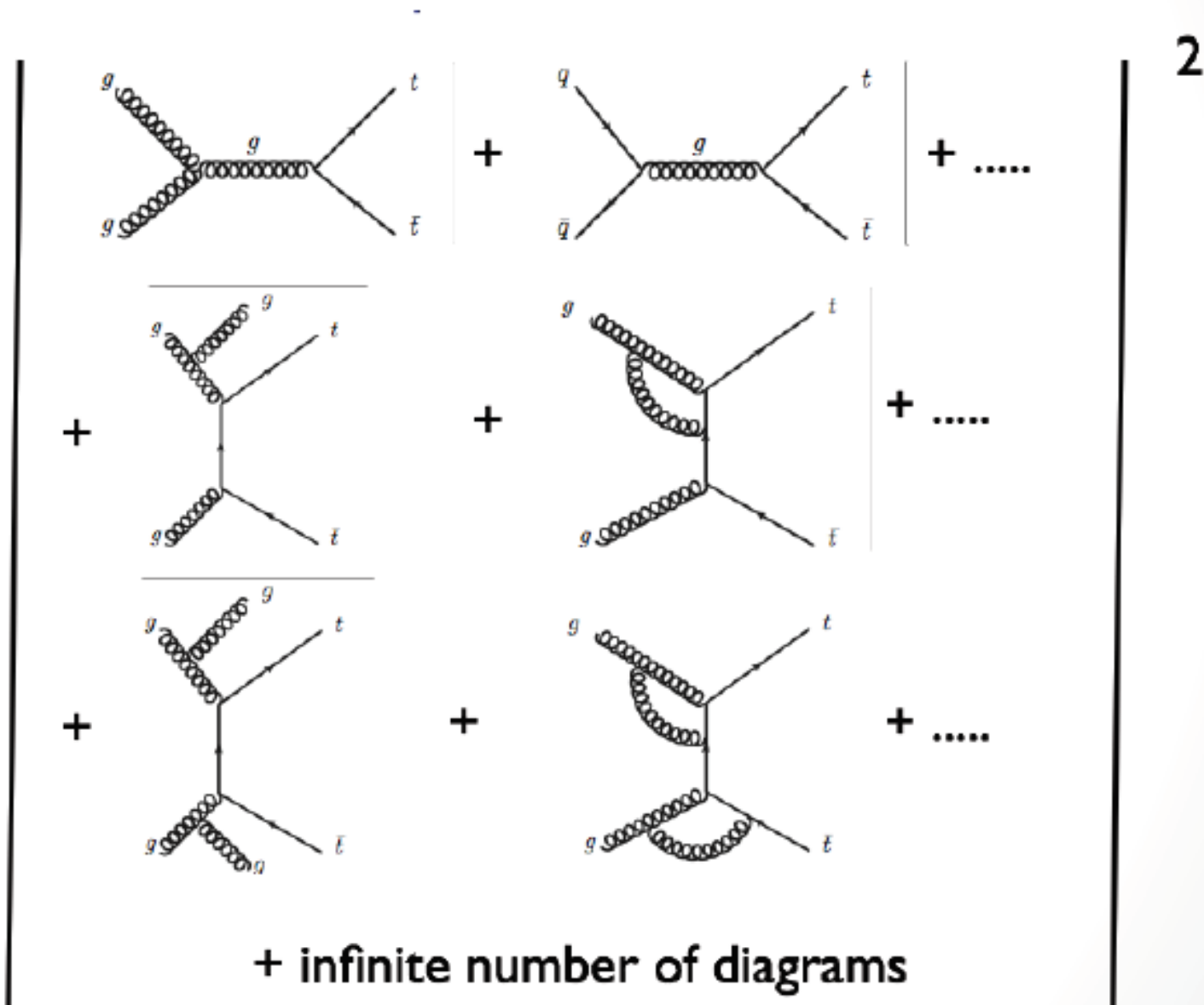
proportional to  $\alpha_s^2$

# Next to leading order



**Extra gluon  $\rightarrow$  results in extra jet of hadrons in detector**  
**Next to Leading order (NLO): contains all terms**  
**proportional to  $\alpha_s^2$  and  $\alpha_s^3$**

# Calculate all allowed processes

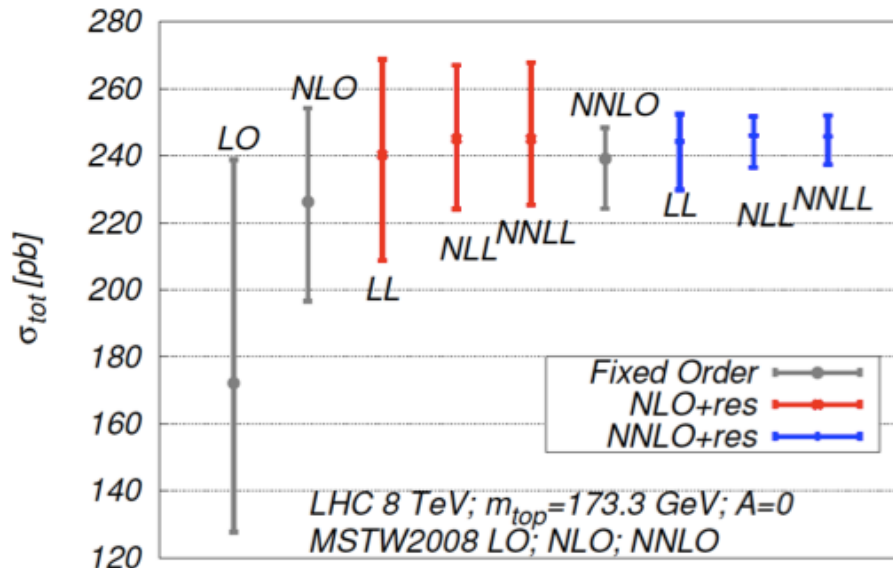


# State of the art: NNLO

- Latest calculation for the inclusive  $t\bar{t}$  cross section: NNLO
- For differential cross section: NLO

Collider	$\sigma_{\text{tot}}$ [pb]	scales [pb]	pdf [pb]
Tevatron	7.164	+0.110(1.5%) -0.200(2.8%)	+0.169(2.4%) -0.122(1.7%)
LHC 7 TeV	172.0	+4.4(2.6%) -5.8(3.4%)	+4.7(2.7%) -4.8(2.8%)
LHC 8 TeV	245.8	+6.2(2.5%) -8.4(3.4%)	+6.2(2.5%) -6.4(2.6%)
LHC 14 TeV	953.6	+22.7(2.4%) -33.9(3.6%)	+16.2(1.7%) -17.8(1.9%)

Scale variation



[Bärnreuther, Czakon, Mitov 2012]

[Czakon, Mitov 2012]

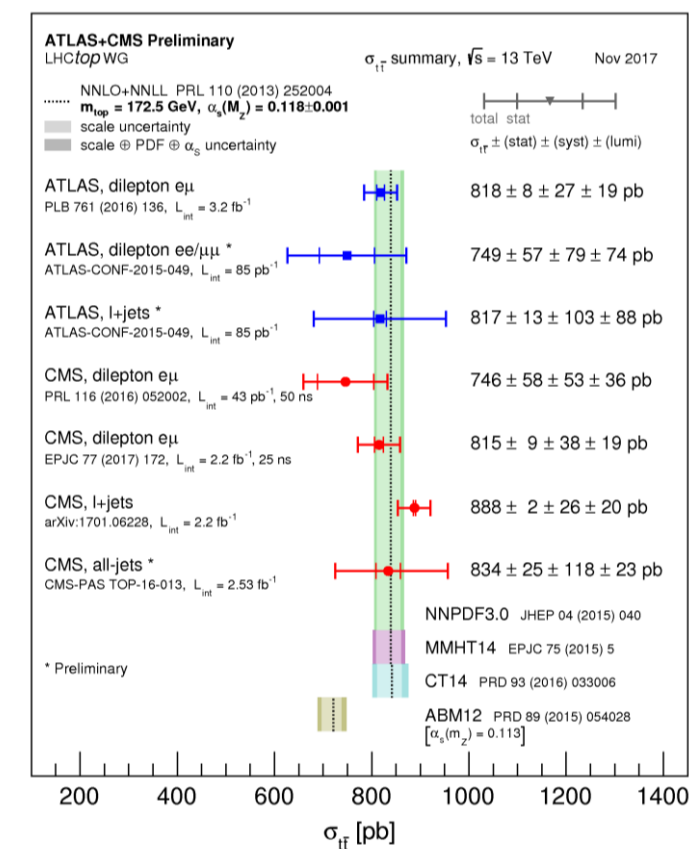
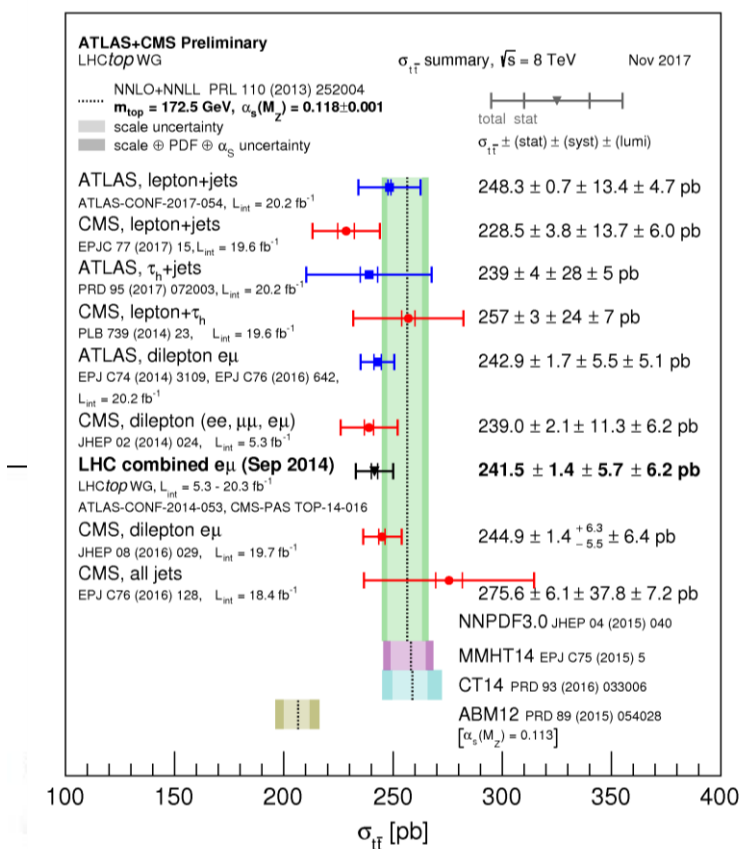
[Czakon, Mitov 2012]

[Czakon, Fiedler, Mitov 2013]

# Summary of cross section measurements at LHC

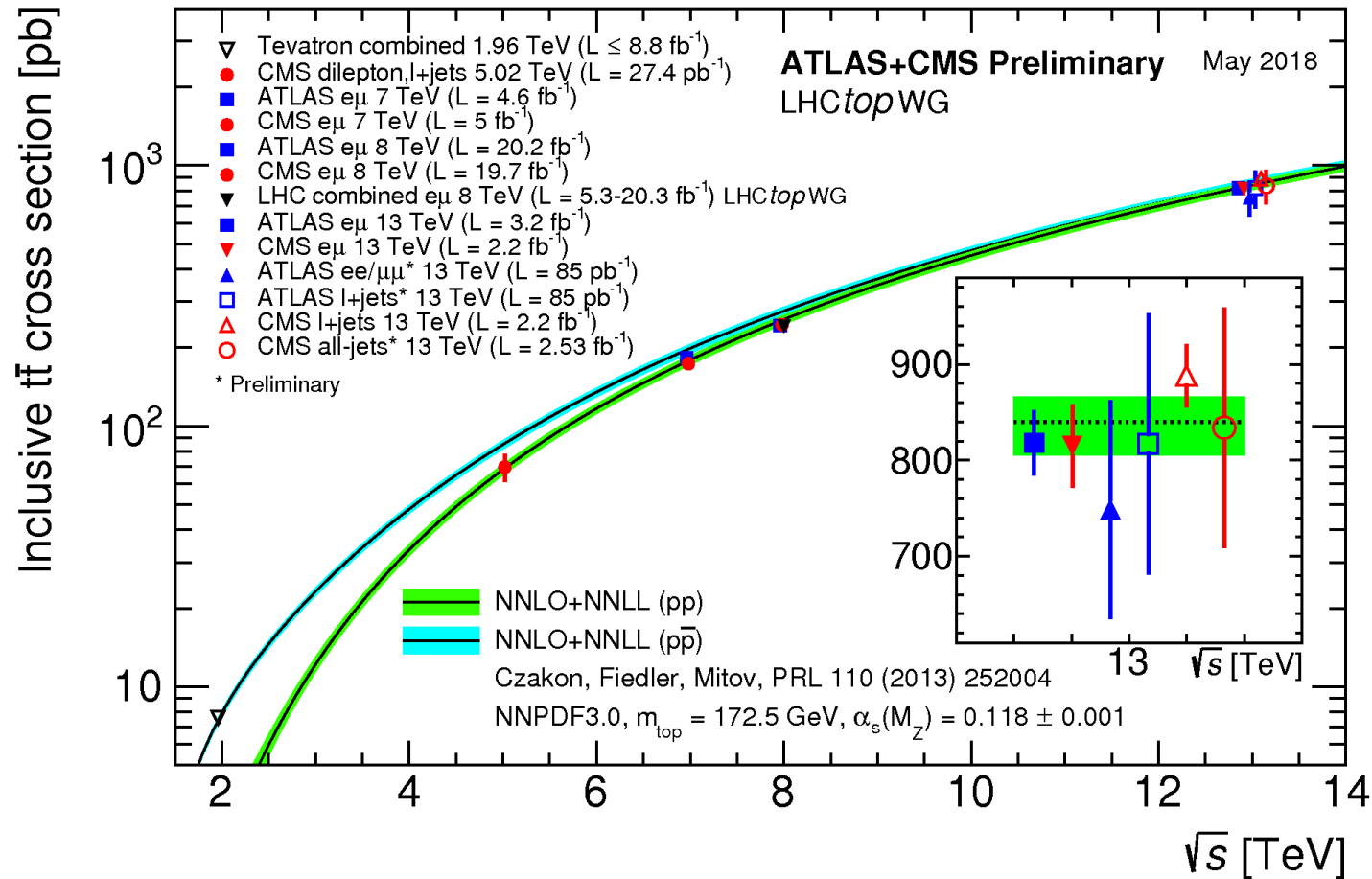
## ATLAS & CMS 8TeV

## ATLAS & CMS 13TeV



- Many measurements that use different techniques
- Good agreement
  - ⇒ between all measurements
  - ⇒ between data and theory
- Measurement precision now comparable to theory

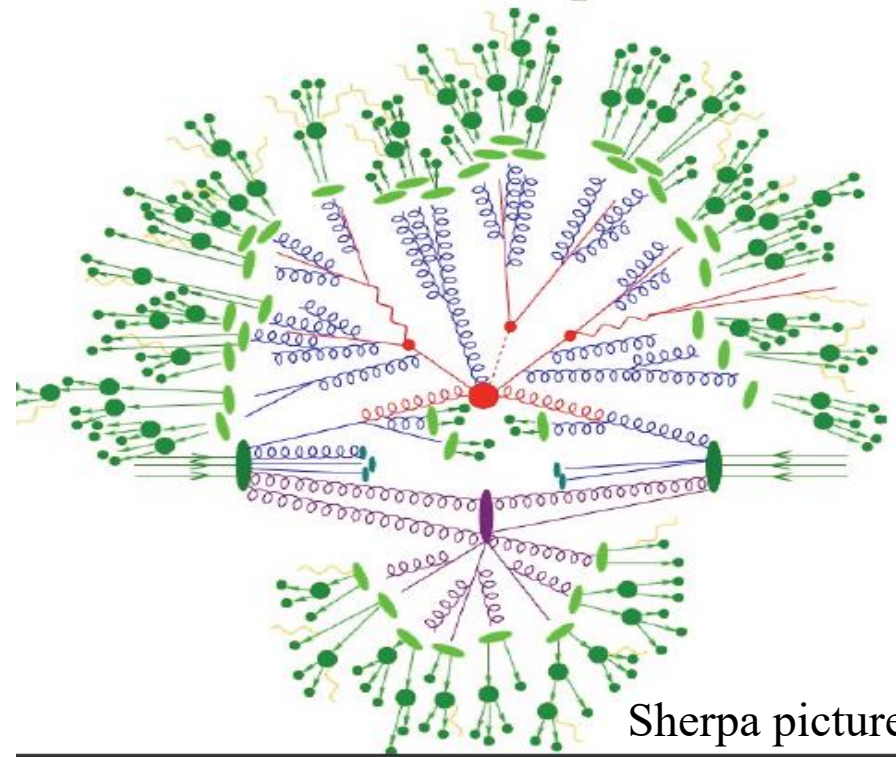
# ttbar inclusive cross section: summary



- Tevatron and LHC results consistent with NNLO+NNLL over a large range of CM energies
- Comparable uncertainties ( $\sim 6\%$  in lepton+jets,  $\sim 4\%$  in dilepton) with theoretical uncertainties at NNLO+NNLL precision ( $\sim 5.5\%$ )

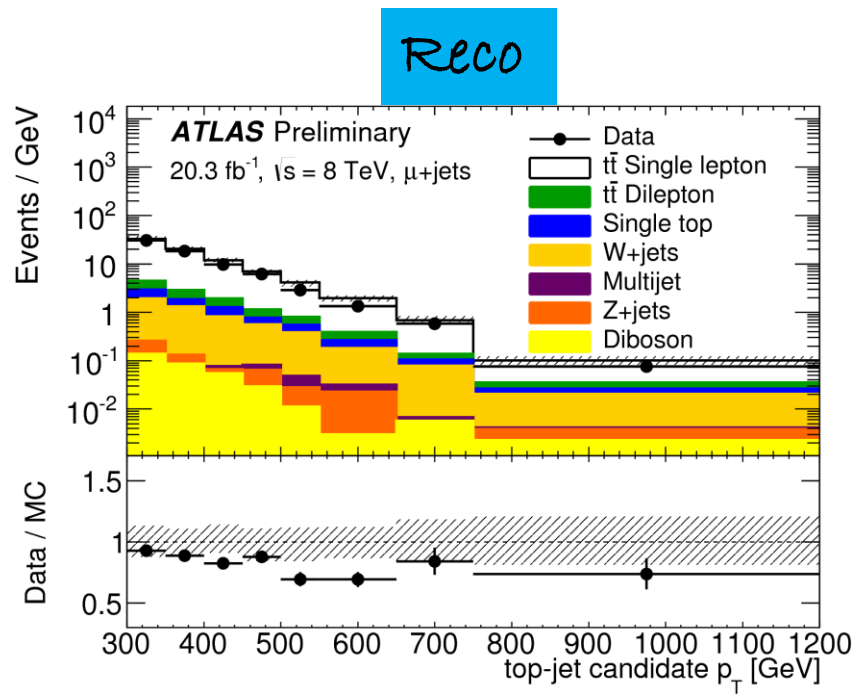
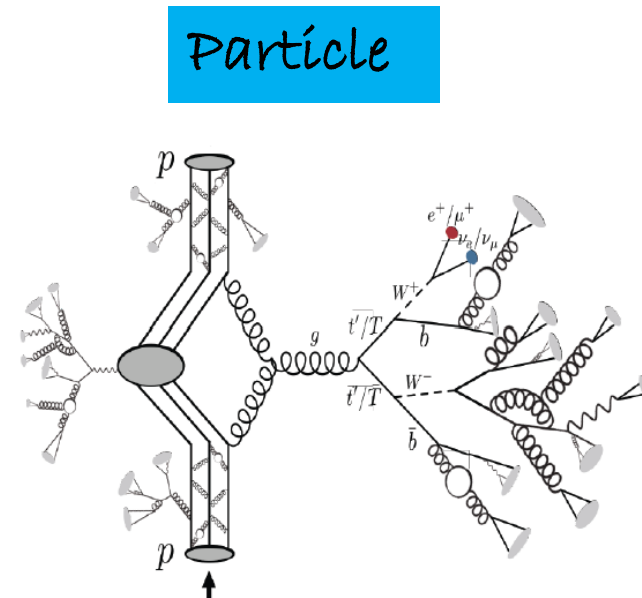
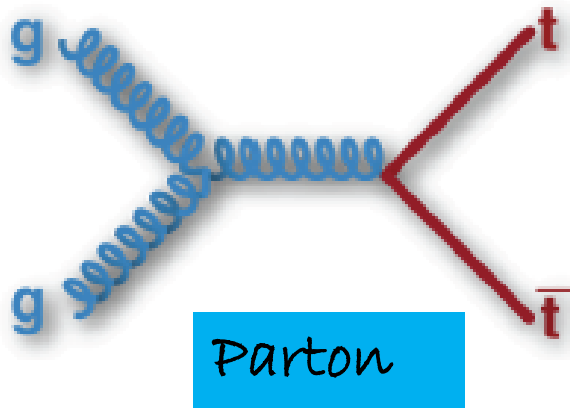
# Differential Top Cross Sections

- Given the available  $t\bar{t}$  statistics, differential measurements are the baseline now
- **It's even more complicated but ....**
  - ⇒ provides more detailed information
  - ⇒ sensitive to new physics on the tails...
- fiducial measur. to avoid large model-dependent corrections to full phase-space
  - ⇒ fiducial differential measurements unfolded to particle/parton level
- test of QCD calculations
- can constrain gluon PDF
- **double-differential** will soon provide even higher sensitivity



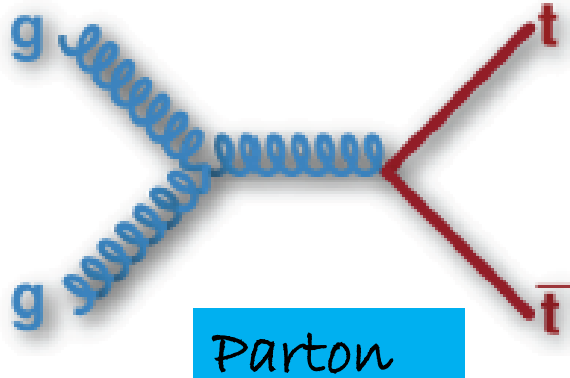


# Unfolding: parton vs particle

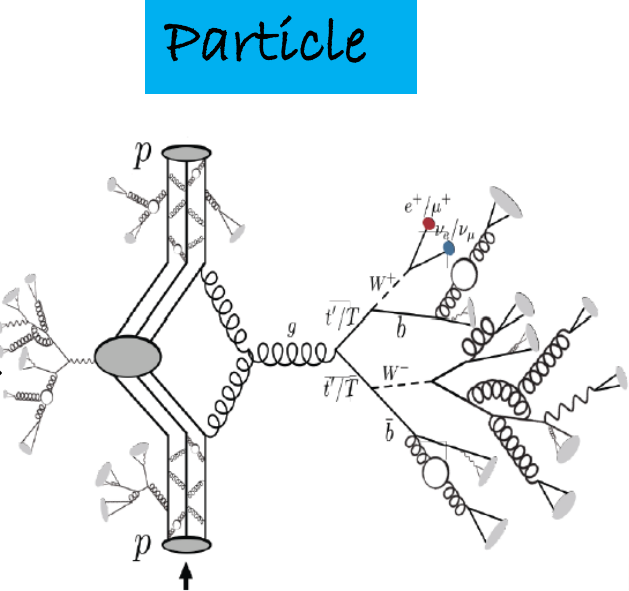


# Unfolding: parton vs particle

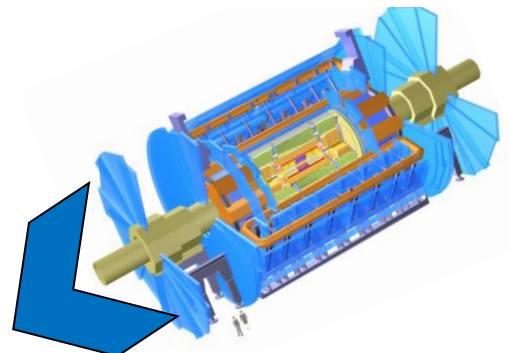
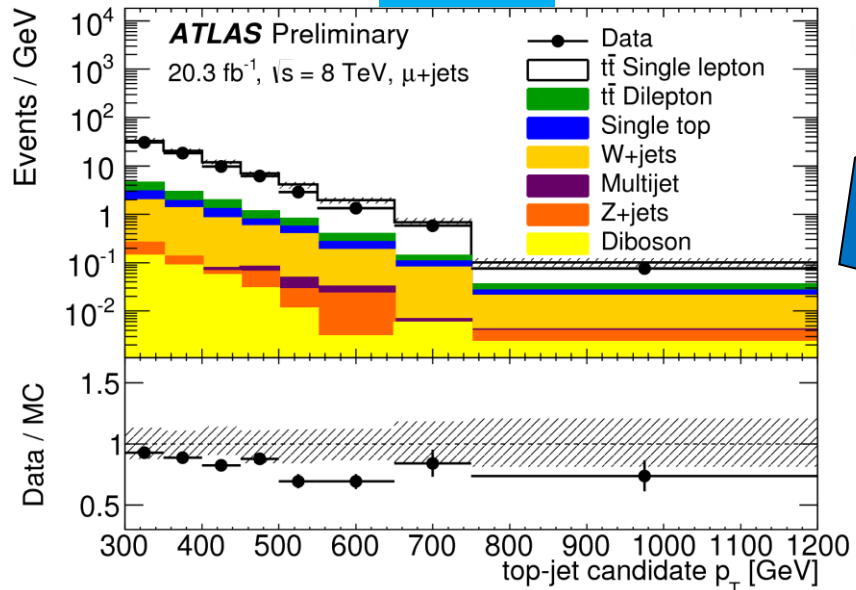
Matrix Element calculation  
(usually perturbative)



Fragmentation, parton shower, hadronization, PDFs... (often non-perturbative)



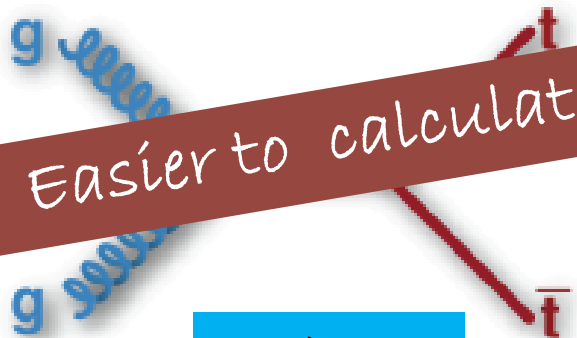
Reco



# Unfolding: parton vs particle

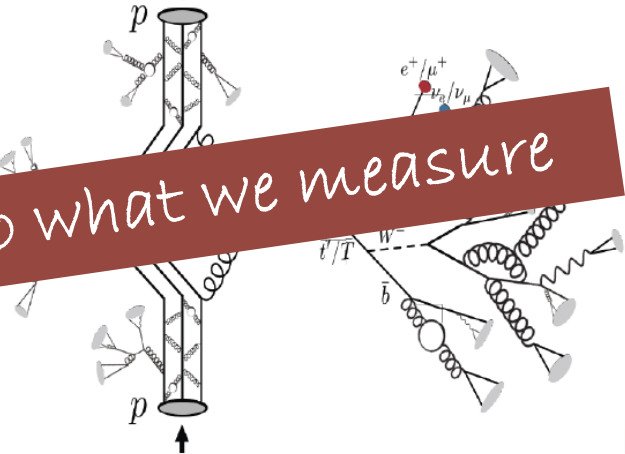
Easier to calculate

Parton

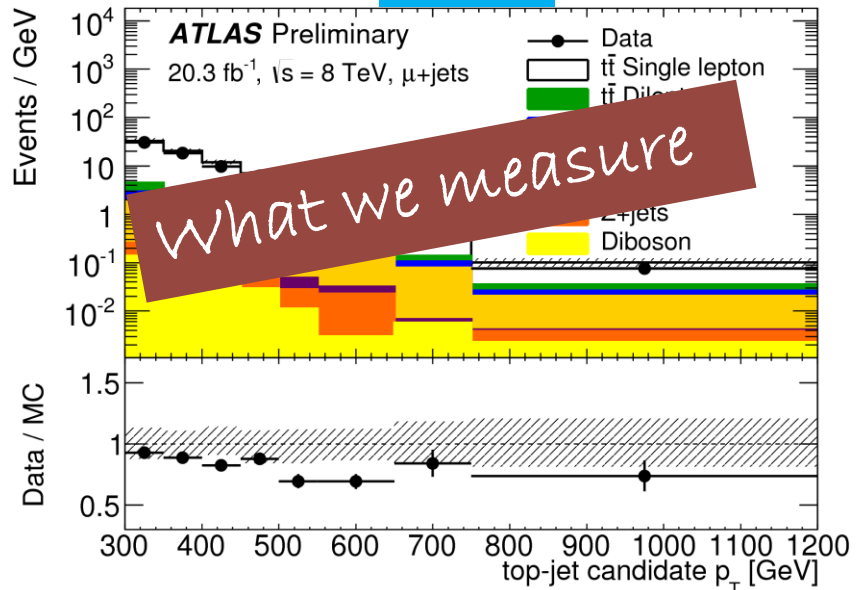


Closer to what we measure

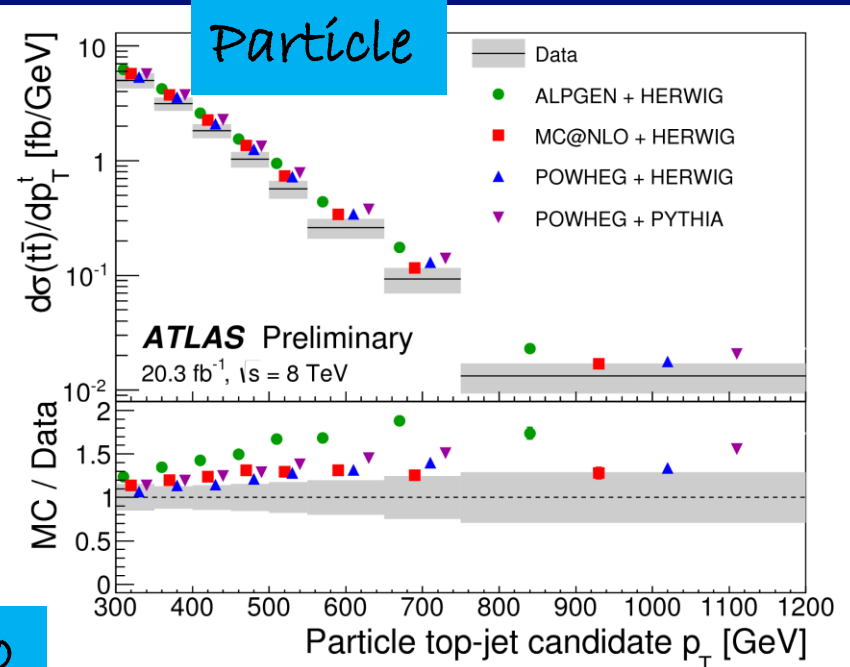
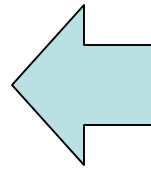
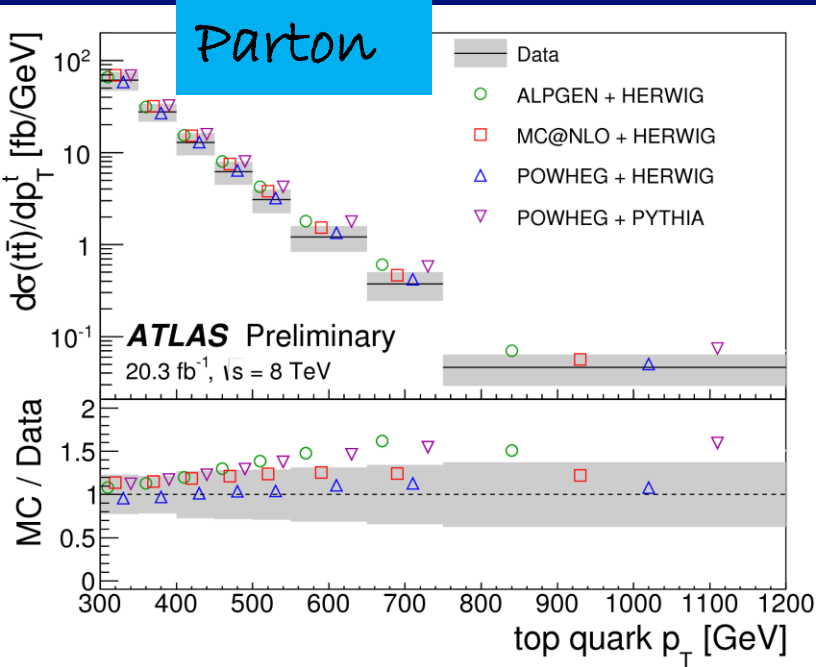
Particle



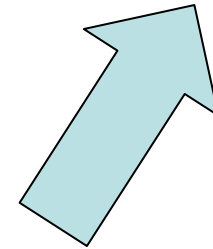
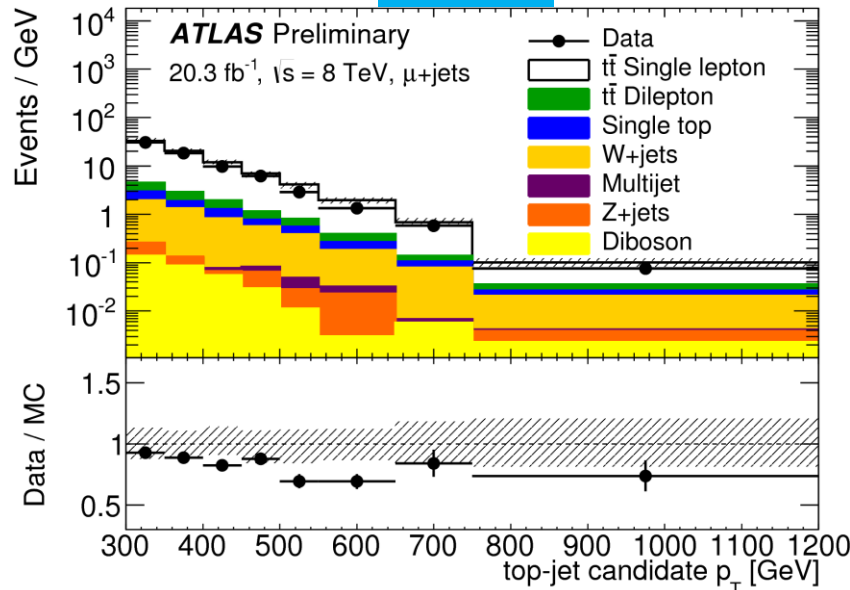
Reco



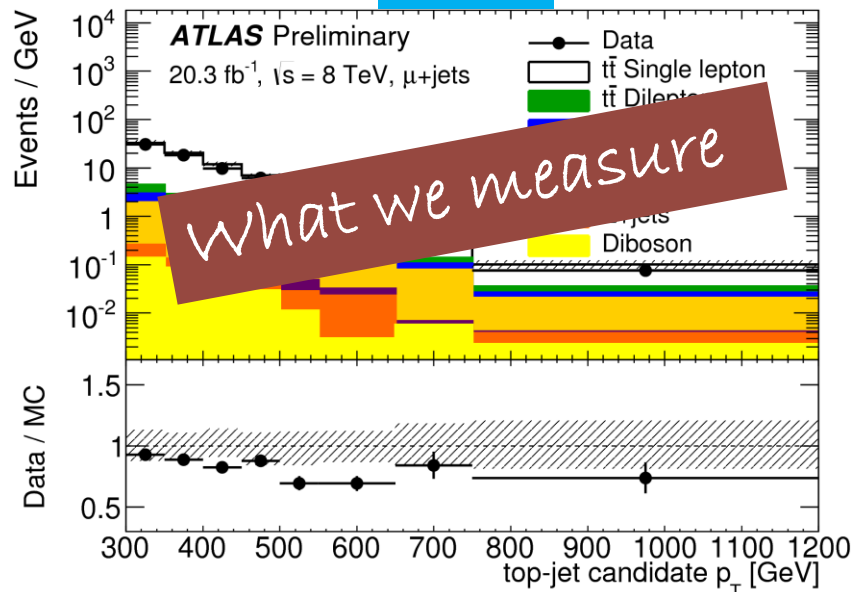
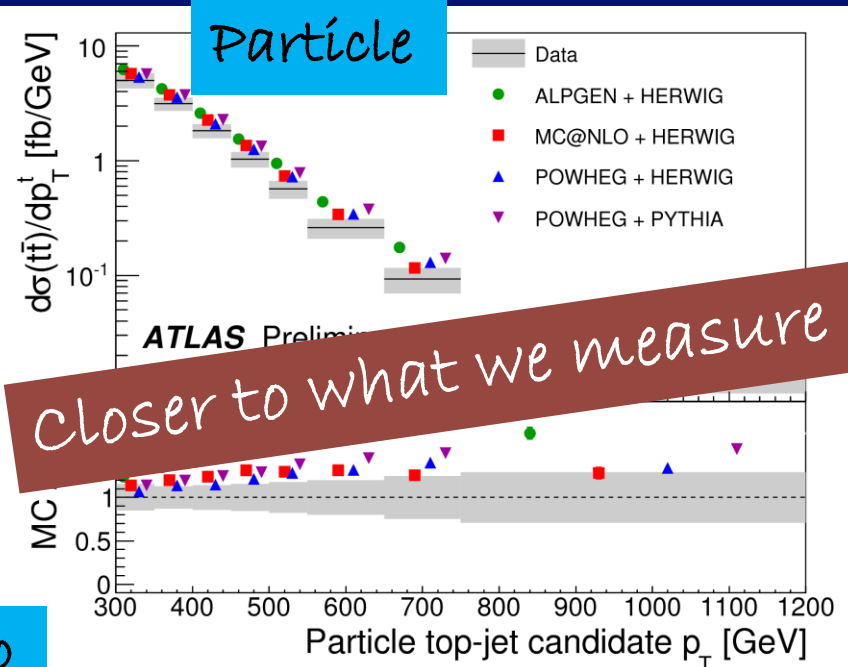
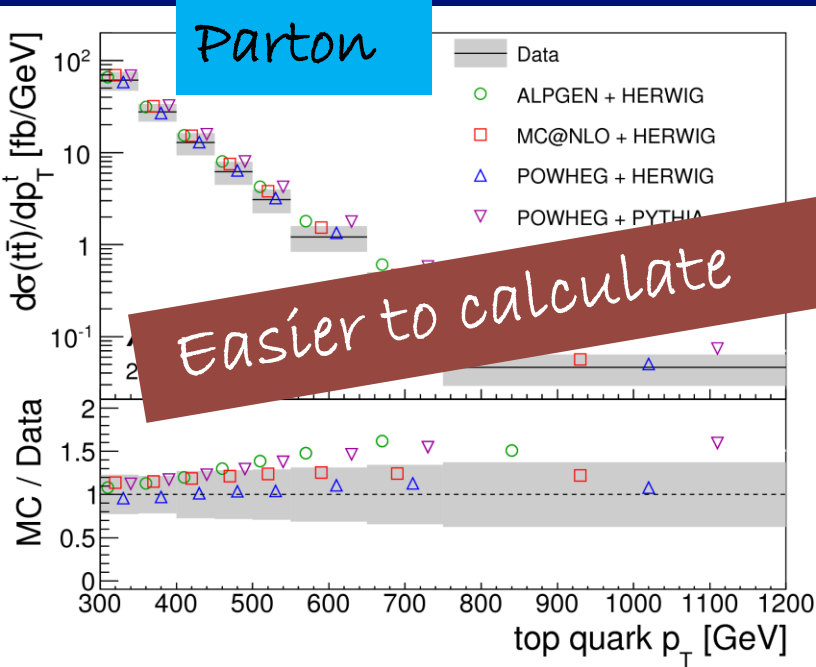
# Unfolding: parton vs particle



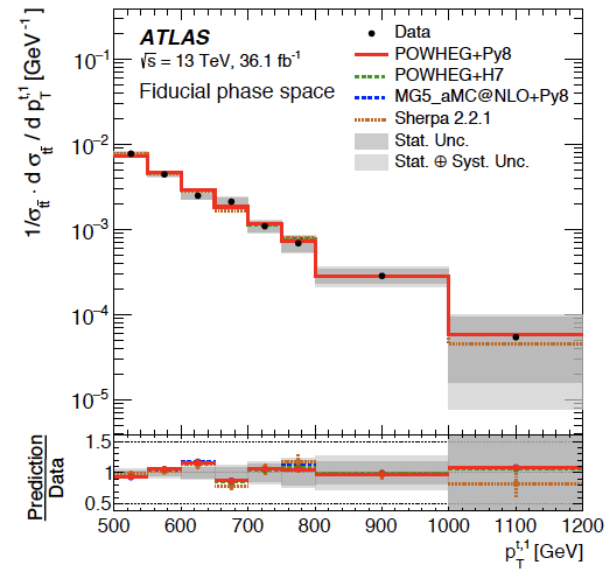
**Reco**



# Unfolding: parton vs particle

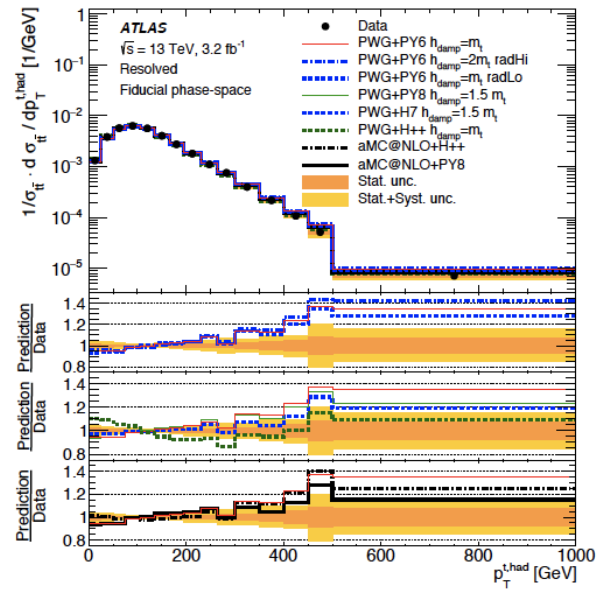


# Differential cross section at 13 TeV



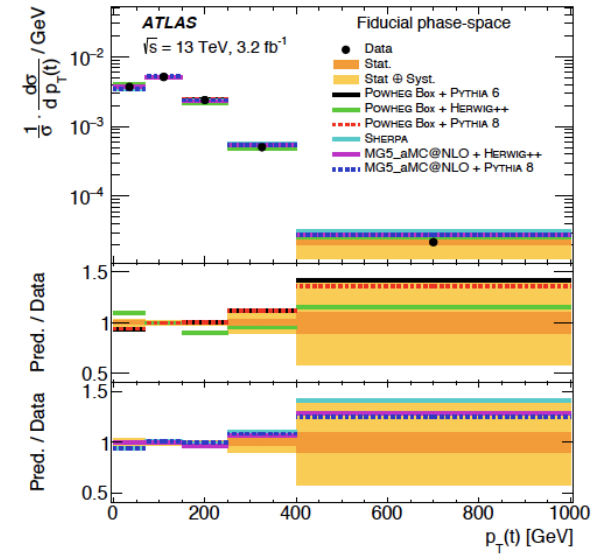
all-jets

arXiv:1801.02052



lepton+jets

JHEP 11 (2017) 191

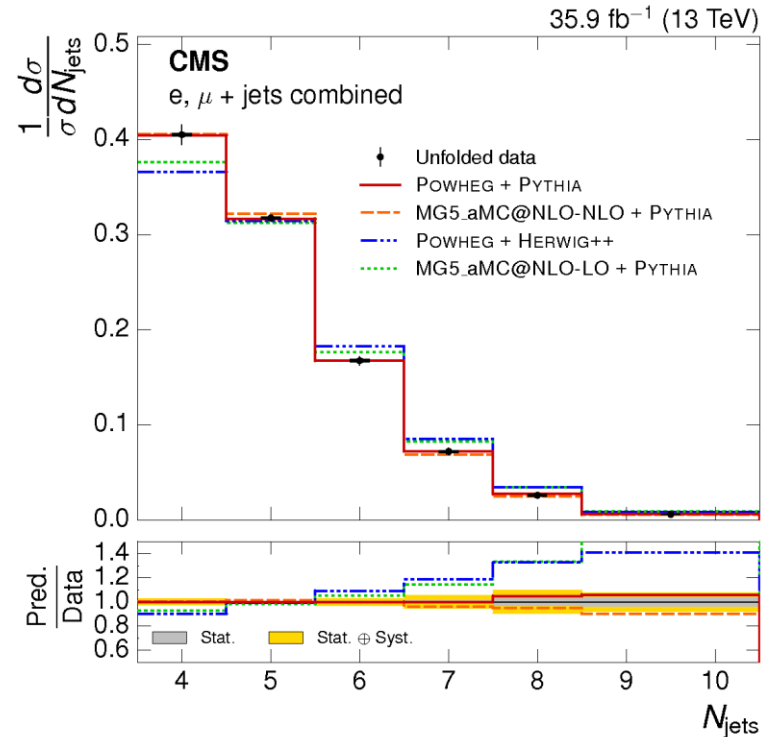
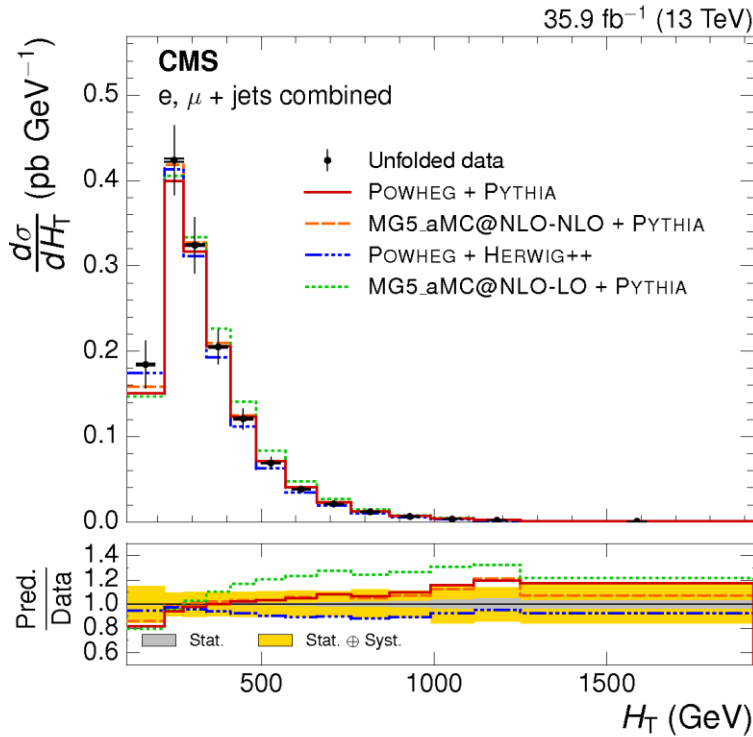


dilepton

Eur. Phys. J. C77 (2017) 292

- Main uncertainties: JES, b-tagging, signal modeling
- Most SM predictions (NLO QCD + parton shower) are consistent with data
- These measurements allow to tune MC generators for the future

# Differential cross section at 13 TeV



JHEP 06 (2018) 002

- Wide range of differential cross sections
- Precision measurements of the SM
- Improving the modelling uncertainties in  $t\bar{t}$  production can help to see new physics!

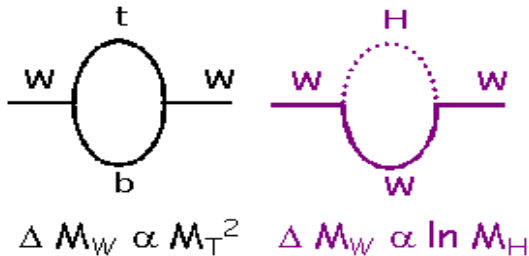


# Measurements of top mass

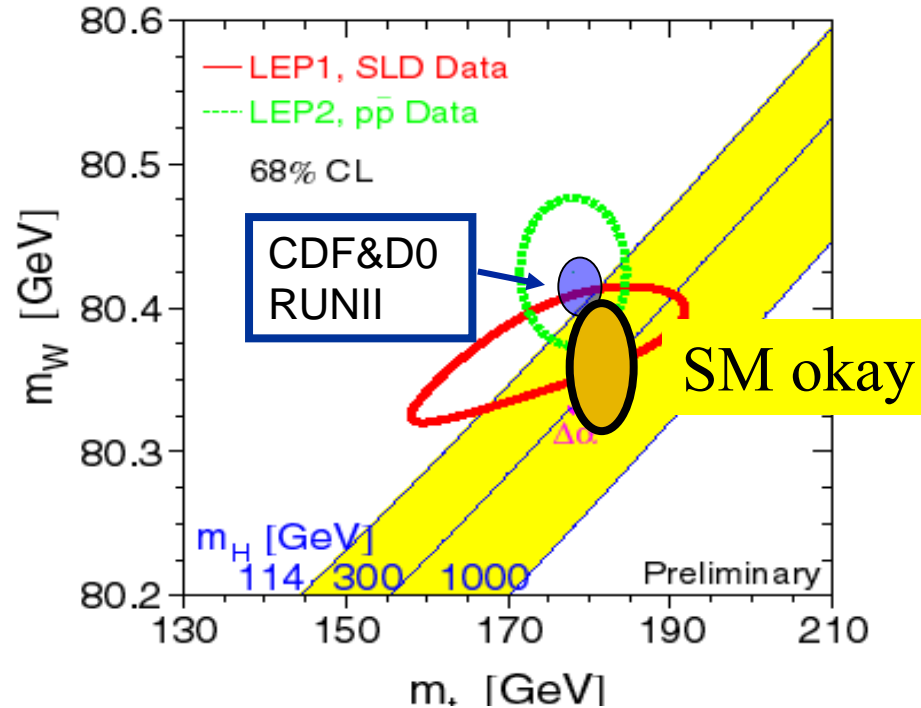
# Why is Top Mass so special?

Top mass is a fundamental SM parameter

- Related through radiative corrections to other EW observables.



- If there are new particles the relation might change
  - Very important for precision tests of SM.
  - Together with  $M_W$  and other electroweak precision measurements, it constrains  $M_{\text{higgs}}$
  - Is this large mass telling us something about electroweak symmetry breaking? (Top Yukawa coupling close to 1)

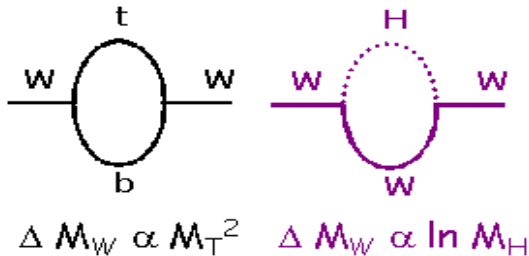


$$m_{top} = y_t v / \sqrt{2} \approx 173 \text{ GeV} \Rightarrow y_t \approx 1$$

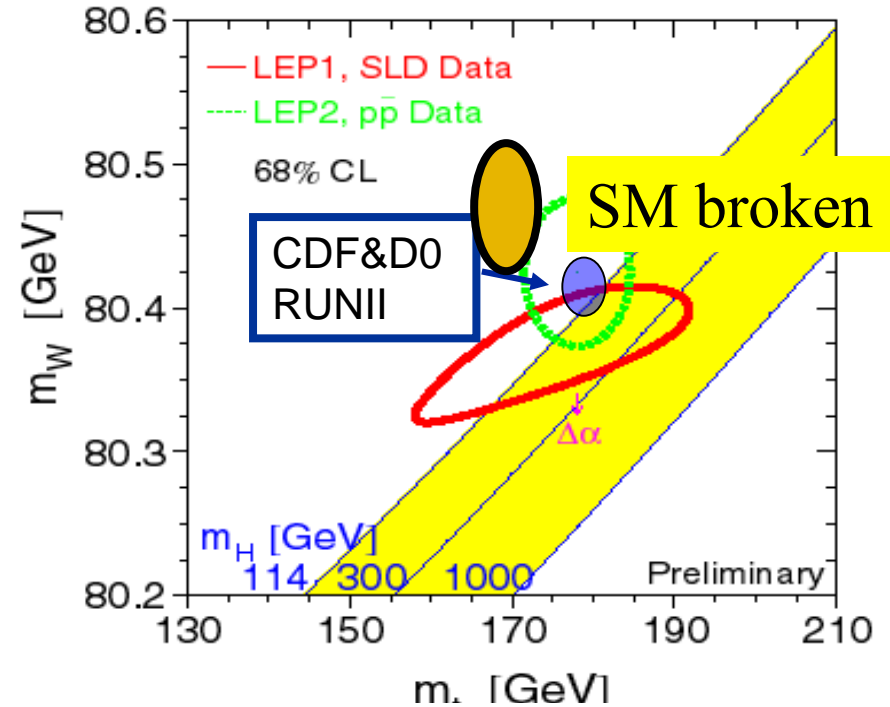
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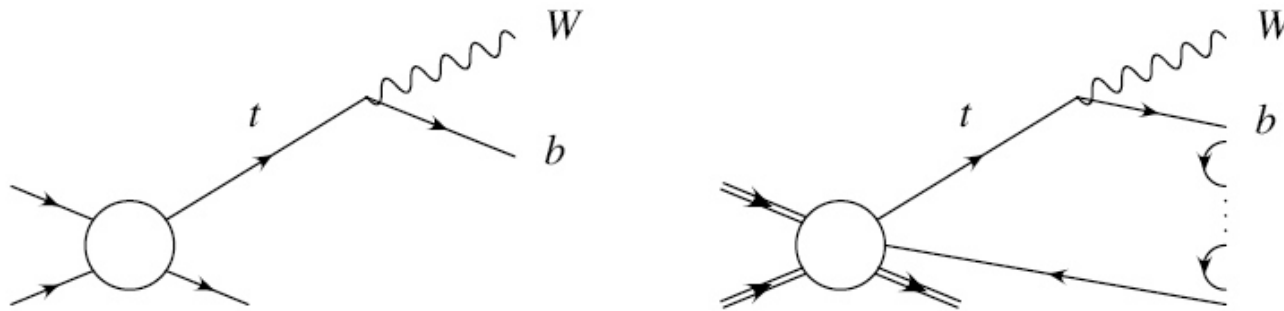
# Top mass: what do we measure?

- > 20 years ago, CDF & D0 first assembled all the pieces needed to discover the top  
→ The strategy to study the top quark remains the same today
- Top quark mass “standard” measurements:
  - make kinematic reconstruction of final state objects (leptons, jets, and missing transverse energy)
  - measurement based on comparison of kinematic observables with MC generated at different top masses (most sensitive variable: invariant mass distribution)
  - determination of the best-fit value of the MC top-quark mass parameter
- On going theoretical work:
  - to translate the measured top-quark mass into a mass in a well defined renormalization scheme
- Experimental way to address the question of the top-quark mass definition:
  - Use alternative methods to determine the top-quark mass
    - With less inputs from MC
    - With different sensitivity to systematics
    - Using theory computation with well defined mass (i.e. from cross section, single top events,  $t\bar{t}$ +jets etc.)
- Best measurements:  $\delta M_{\text{top}} \sim \pm 0.50 \text{ GeV}/c^2 (< 0.4\%)$

# Top mass: what do we measure?

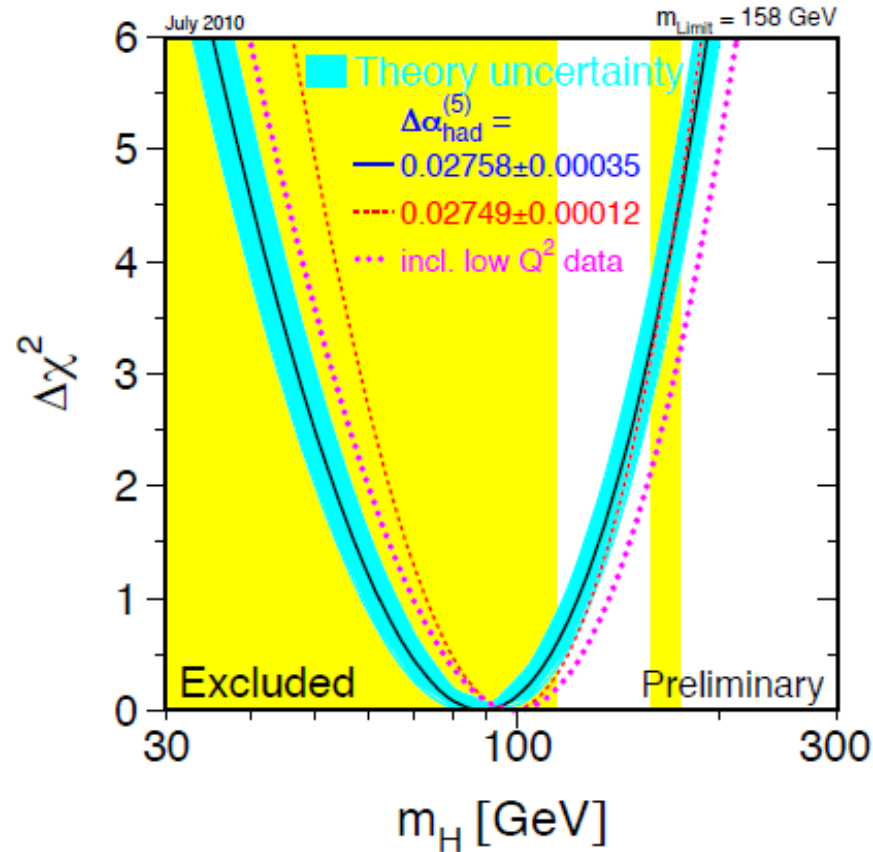
- Conceptual uncertainty of  $< 1 \text{ GeV}/c^2$  when relating the MC mass to a field theory mass....

$$\left| m_t^{\text{gen}} - m_t^{\text{pole}} \right| \leq 1 \text{ GeV}$$



- The pole mass corresponds to our physical intuition of a stable particle (pole = **top quark as a free parton**, though a quark doesn't really propagate - hadronisation!) however, **it can never be determined with accuracy better than  $O(\Lambda_{\text{QCD}})$  ( $\approx 0.2 \text{ GeV}$ )**
- The pole mass is closer to what we measure at colliders through invariant mass of the top decay products.
  - The ambiguities are in the modeling of extra radiation, the color connect effects and hadronization.
  - Uncertainties estimated by various theoretical groups between 0.1 and 0.25 GeV
- Importance of measuring the mass using alternative techniques:
  - theoretically a good approach is to extract the mass from measurements of the cross section

# W and top quark mass tells us Higgs mass



$\Delta\chi^2$  fit to electroweak precision observables as a function of the Higgs boson mass in the Standard Model. The line is the result of the fit using all available data  
**Preferred value for  $m_H$** : corresponds to the minimum of the curve

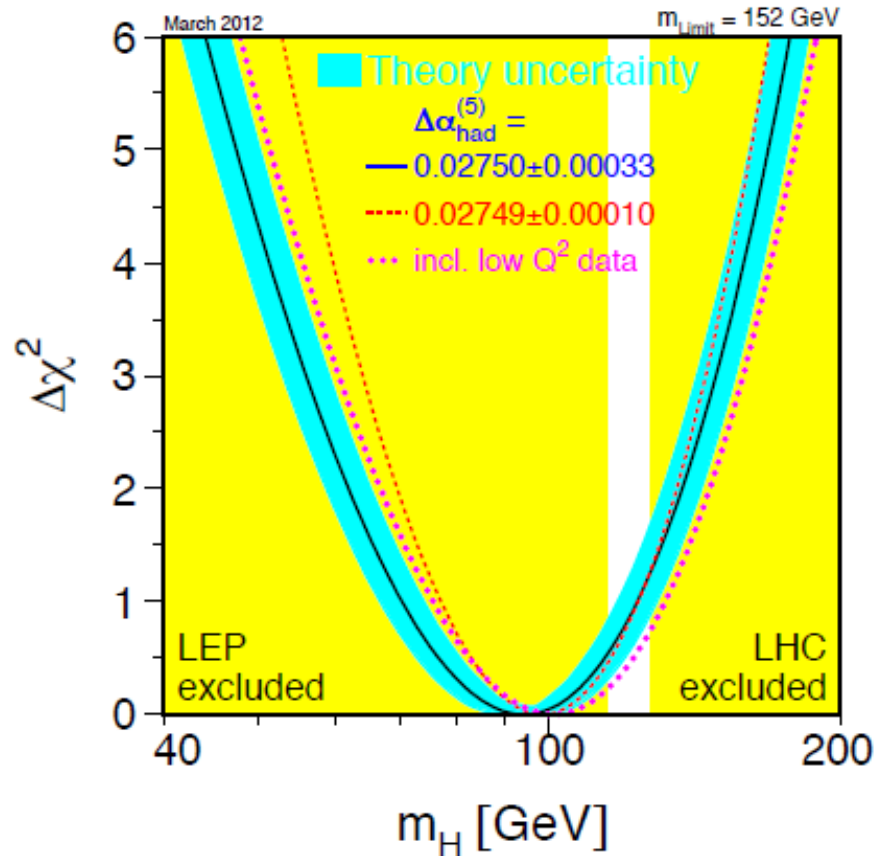
# Example of variables used in EWK fit

[arXiv:0909.0961](https://arxiv.org/abs/0909.0961)

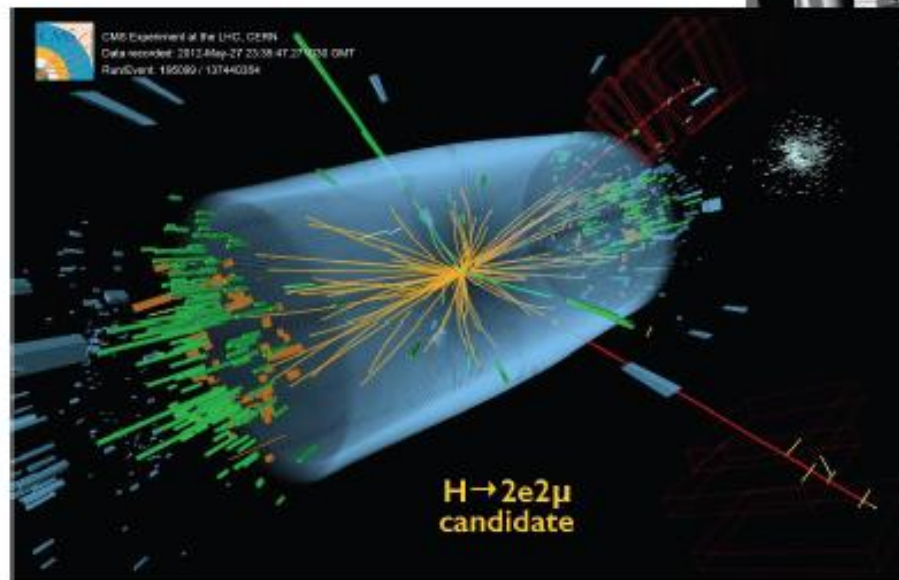
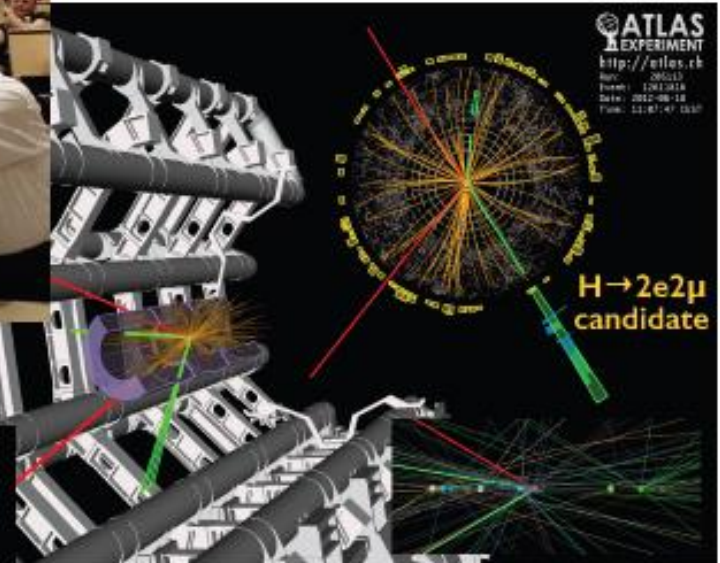
Parameter	Input value	Free in fit	Results from global EW fits:	
			<i>Standard fit</i>	<i>Complete fit</i>
$M_Z$ [GeV]	$91.1875 \pm 0.0021$	yes	$91.1874 \pm 0.0021$	$91.1876 \pm 0.0021$
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	–	$2.4960 \pm 0.0015$	$2.4956 \pm 0.0015$
$\sigma_{\text{had}}^0$ [nb]	$41.540 \pm 0.037$	–	$41.478 \pm 0.014$	$41.478 \pm 0.014$
$R_\ell^0$	$20.767 \pm 0.025$	–	$20.742 \pm 0.018$	$20.741 \pm 0.018$
$A_{\text{FB}}^{0,\ell}$	$0.0171 \pm 0.0010$	–	$0.01638 \pm 0.0002$	$0.01624 \pm 0.0002$
$A_\ell$ (*)	$0.1499 \pm 0.0018$	–	$0.1478 \pm 0.0010$	$0.1472^{+0.0009}_{-0.0008}$
$A_c$	$0.670 \pm 0.027$	–	$0.6682^{+0.00045}_{-0.00044}$	$0.6679^{+0.00042}_{-0.00036}$
$A_b$	$0.923 \pm 0.020$	–	$0.93469 \pm 0.00010$	$0.93463^{+0.00007}_{-0.00008}$
$A_{\text{FB}}^{0,c}$	$0.0707 \pm 0.0035$	–	$0.0741^{+0.0006}_{-0.0005}$	$0.0737 \pm 0.0005$
$A_{\text{FB}}^{0,b}$	$0.0992 \pm 0.0016$	–	$0.1036 \pm 0.0007$	$0.1032^{+0.0007}_{-0.0006}$
$R_c^0$	$0.1721 \pm 0.0030$	–	$0.17225 \pm 0.00006$	$0.17225 \pm 0.00006$
$R_b^0$	$0.21629 \pm 0.00066$	–	$0.21578 \pm 0.00005$	$0.21577 \pm 0.00005$
$\sin^2 \theta_{\text{eff}}^\ell(Q_{\text{FB}})$	$0.2324 \pm 0.0012$	–	$0.23142 \pm 0.00013$	$0.23151^{+0.00010}_{-0.00012}$
$M_W$ [GeV]	$80.399 \pm 0.023$	–	$80.384^{+0.014}_{-0.015}$	$80.371^{+0.008}_{-0.011}$
$\Gamma_W$ [GeV]	$2.098 \pm 0.048$	–	$2.092^{+0.001}_{-0.002}$	$2.092 \pm 0.001$
$\bar{m}_c$ [GeV]	$1.25 \pm 0.09$	yes	$1.25 \pm 0.09$	$1.25 \pm 0.09$
$\bar{m}_b$ [GeV]	$4.20 \pm 0.07$	yes	$4.20 \pm 0.07$	$4.20 \pm 0.07$
$m_t$ [GeV]	$173.1 \pm 1.3$	yes	$173.2 \pm 1.2$	$173.6 \pm 1.2$
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$ ( $\dagger\Delta$ )	$2767 \pm 22$	yes	$2772 \pm 22$	$2764^{+22}_{-21}$
$\alpha_s(M_Z^2)$	–	yes	$0.1192^{+0.0028}_{-0.0027}$	$0.1193 \pm 0.0028$
$\delta_{\text{th}} M_W$ [MeV]	$[-4, 4]_{\text{theo}}$	yes	4	4
$\delta_{\text{th}} \sin^2 \theta_{\text{eff}}^\ell$ ( $\dagger$ )	$[-4.7, 4.7]_{\text{theo}}$	yes	4.7	0.8
$\delta_{\text{th}} \rho_Z^f$ ( $\dagger$ )	$[-2, 2]_{\text{theo}}$	yes	2	2
$\delta_{\text{th}} \kappa_Z^f$ ( $\dagger$ )	$[-2, 2]_{\text{theo}}$	yes	2	2



# W and top quark mass tells us Higgs mass

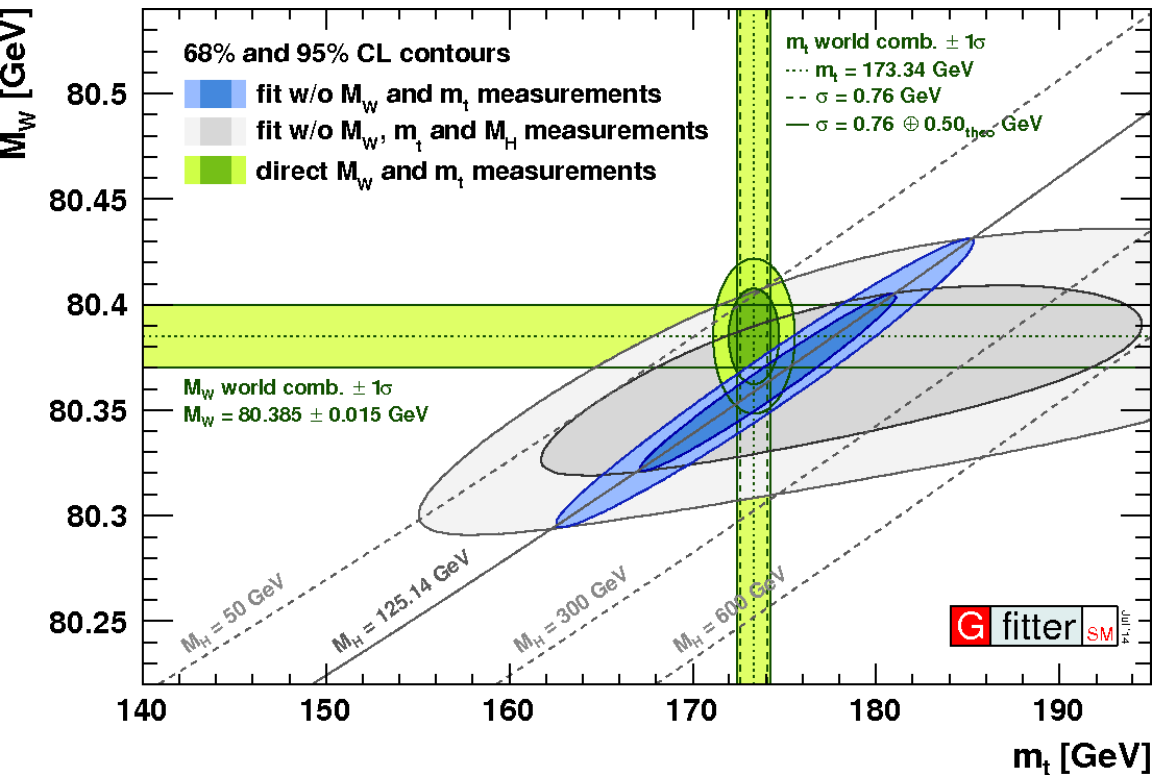


# Higgs is Discovered! 2012



theory: 1964  
design: 1984  
construction: 1998  
collisions: 2010

# Consistency of the Standard Model

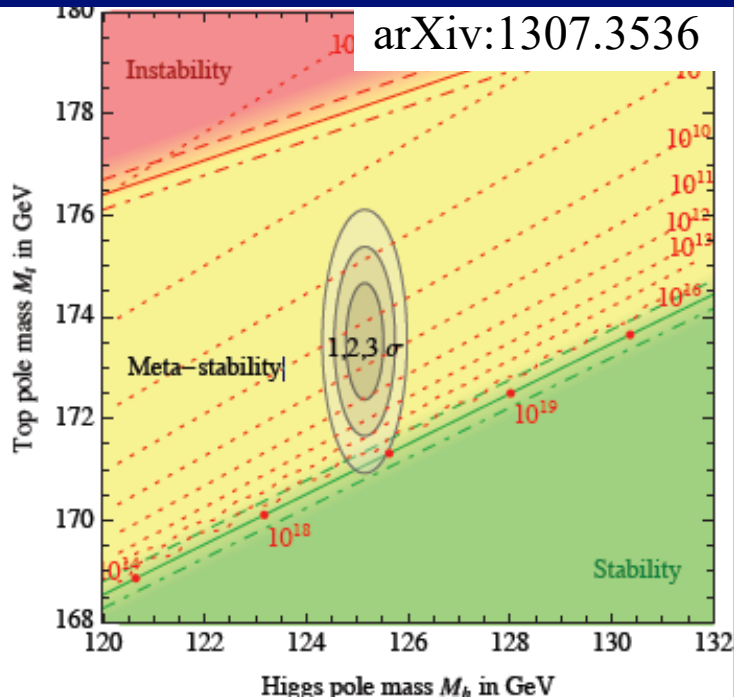


arXiv:1306.0571 (2013)

- 68% and 95% CL contours in the  $m_{\text{top}}-M_W$  plane for the fit including  $M_H$  (blue) and excluding  $M_H$  (grey).
- In both cases the direct measurements of  $M_W$  and  $m_{\text{top}}$  were excluded from the fit.

- The knowledge of  $M_H$  improves the precision of the indirect determination of  $M_W$  and  $m_{\text{top}}$  significantly.
- Very good agreement between the indirect determinations of  $M_W$  and  $m_{\text{top}}$  and the direct measurements is observed, showing impressively the consistency of the SM and leaving little room for signs of new physics.

# The Fate of the universe.....



... depends on 1GeV in  $m_{\text{top}}$

SM phase diagram in terms of Higgs and top pole masses.

Stability of the EW vacuum is an important property of the SM

- Measurements of the top mass and Higgs mass for the first time allow us to infer properties of the vacuum we live in!

The measured values of  $M_{\text{higgs}}$  and  $M_{\text{top}}$  appear to be rather special  $\rightarrow$  they place the SM vacuum in a near-critical condition, at the border between stability and metastability.

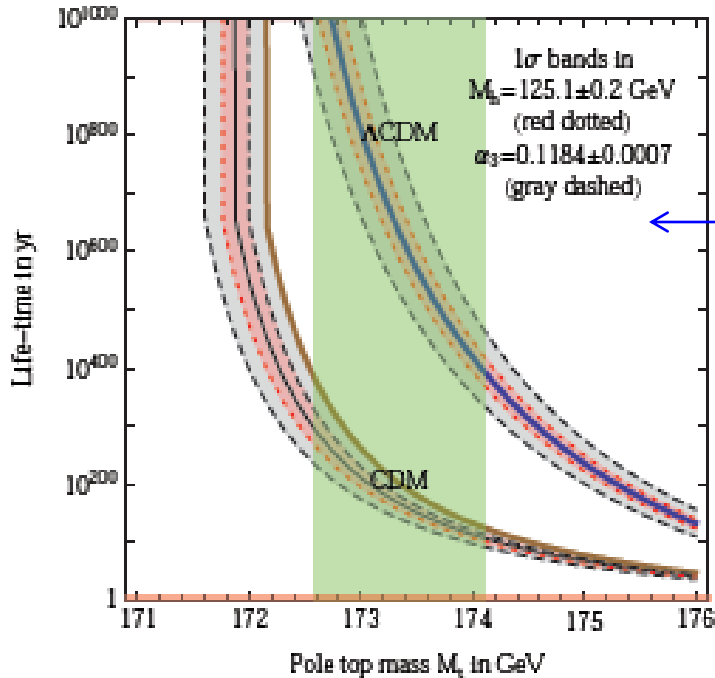
A fine-tuned situation: vacuum on the verge of being either stable or unstable.

$\sim 1$ -2 GeV in either mass could tip the scales. (But new physics could possibly change this scenario.)

- What top mass are we measuring??

# The Fate of our universe

arXiv:1307.3536



The life-time of the electroweak vacuum, with two different assumptions for future cosmology: universes dominated by the cosmological constant ( $\Lambda$ CDM) or by dark matter (CDM).

The measured values of  $M_{\text{higgs}}$  and  $M_{\text{top}}$  indicate that the SM Higgs vacuum is not the true vacuum of the theory and that our universe is potentially unstable.

The lifetime of the present EW vacuum depends on the future cosmological history: If the future universe is matter dominated (flat universe) or if instead the universe keeps being accelerated by the cosmological constant

→ As shown, the SM vacuum is likely to survive for times that are enormously longer than any significant astrophysical age

- What top mass are we measuring??

# Top Mass: Experimental Challenges

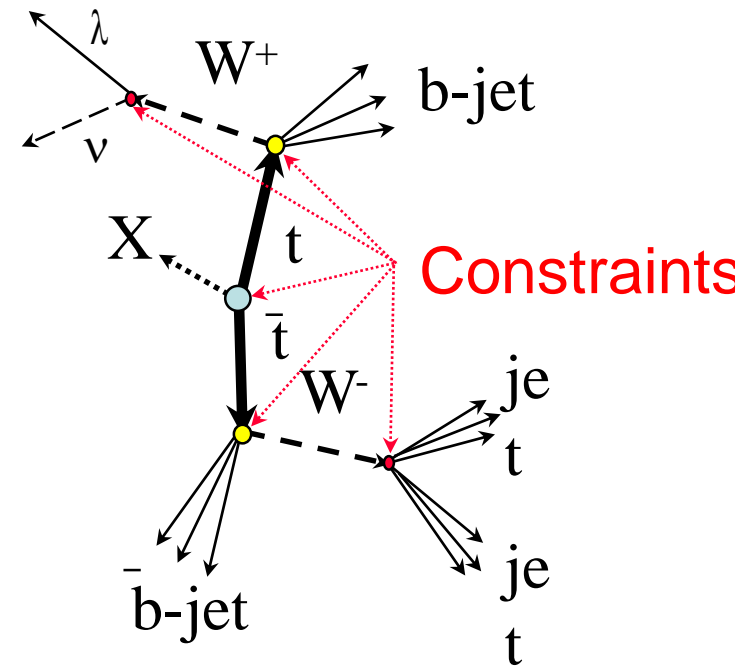
Why so challenging? It is a difficult measurement

Many combinations of leptons and jets:

⇒ Events are complicated!

⇒ Experimental observations are not as *pretty* as Feynman diagrams!

- Large backgrounds
  - Missing neutrino(s)
  - Confusion in ID assignment (add. Jets from ISR/FSR, b-tag: not 100% correct)
  - Measurements are not perfect!
- 
- Link observables to parton-level energies
  - Large syst uncert. from jet energy scale
  - Need accurate detector simulation





# Backgrounds

- Hadron colliders:
  - Very high backgrounds!
- Backgrounds can bias the top mass measurement

## Typical Backgrounds:

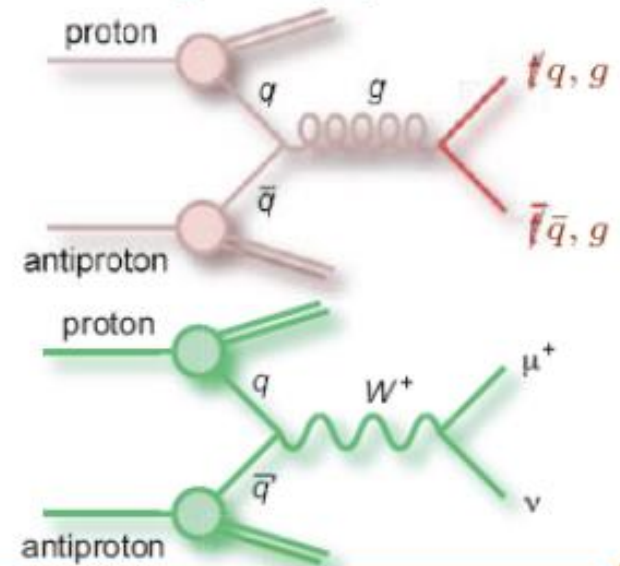
W+jets

Z+jets

QCD multijet prod'n

Diboson prod'n

Single top prod'n

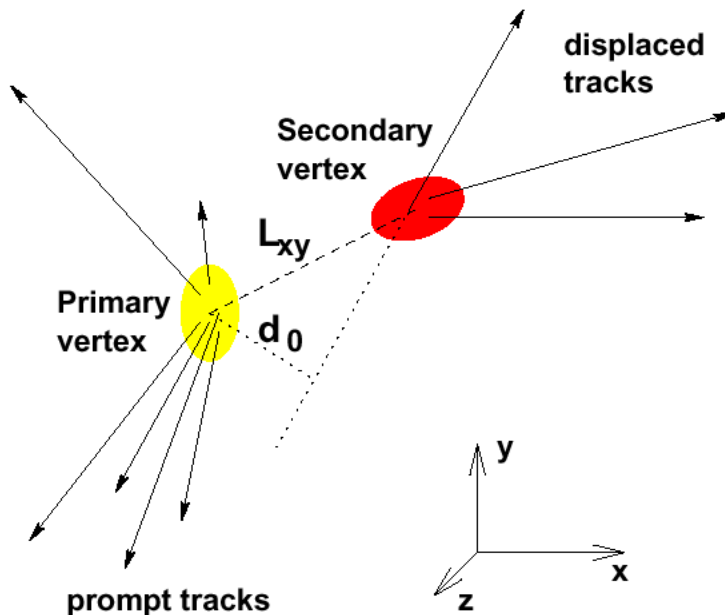




# Backgrounds & b-tagging algorithms

- Hadron colliders:
  - Very high backgrounds!
- Backgrounds can bias the top mass measurement
- Control backgrounds using b-tagging information

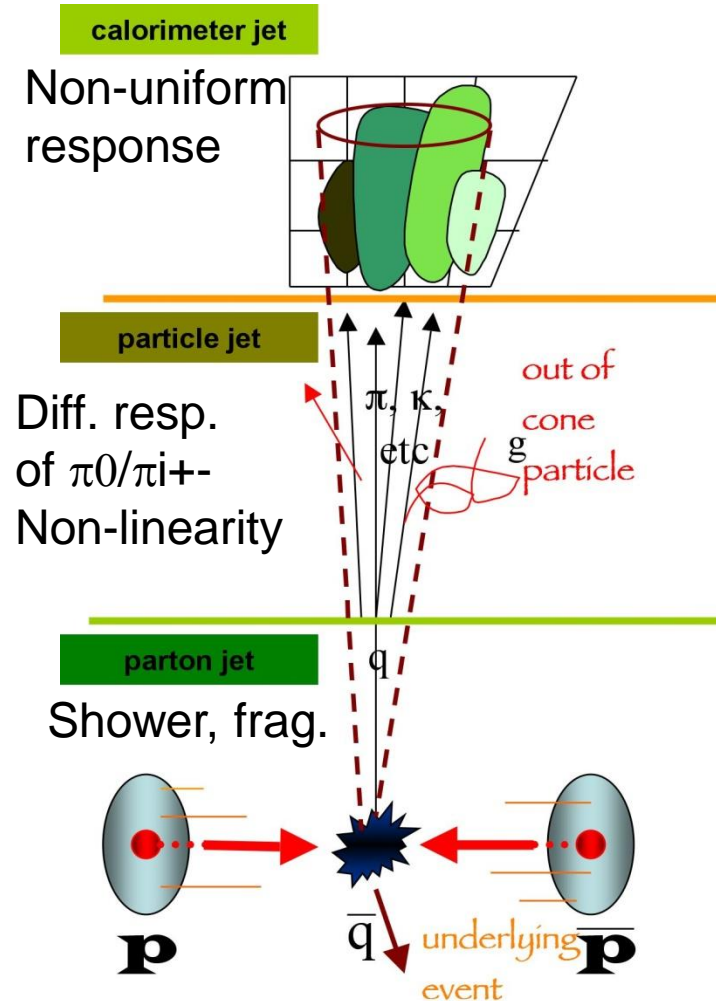
- At the same time:
  - help combinatorics!
- In lepton+jets:
  - 2 b-tags → 2 combinations
  - 1 b-tag → 6 combinations
  - 0 b-tags → 12 combinations



Channel	B-tags	S:B	Perm.
Dilepton	$\geq 0$	1:4	2
	$\geq 1$	4:1	2
Lepton+jets	$\geq 0$	< 1:1	12
	$\geq 1$	2.5:1	6
	$\geq 2$	10:1	2
All-hadronic	$\geq 1$	1:4	30
	$\geq 2$	4:1	6

# Jet Energy Correction

Determine true “parton” (or particle) energy from measured jet energy



The correction factor depends on jet  $E_T$  and  $\eta$  and is meant to reproduce the average jet  $E_T$  correctly, (not to reduce the jet fluctuations around this mean)

Corrections for generic jets:

- ⇒ Use  $Z \rightarrow ee$  for EM energy calibration
- ⇒ Absolute corrections ( $\gamma$ -jet balancing)
- ⇒ Relative corrections (central-forward calorimeters, dijet balancing)

Out-of-Cone: correction to parton outside the reconstruction cone

Underlying event: energy which enters the reconstruction cone

“top-specific correction” to light quark jets and b-jets separately

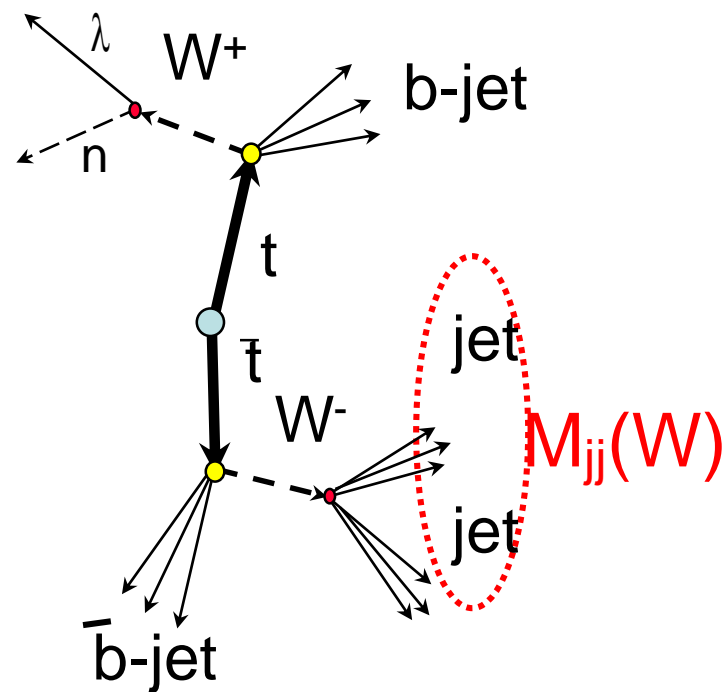
# “In situ” jet energy calibration in top events

“Creative” solution to improve jet energy scale precision:

Simultaneous fit to  $M_{jj}$  and  $M_{top}$  using top mass and jet energy scale (JES) templates for ‘lepton plus jets’ and ‘all hadronic’ final states:

$M_t$  ( true  $M_{top}$ , JES),  $M_{jj}$  ( true  $M_{top}$ , JES)

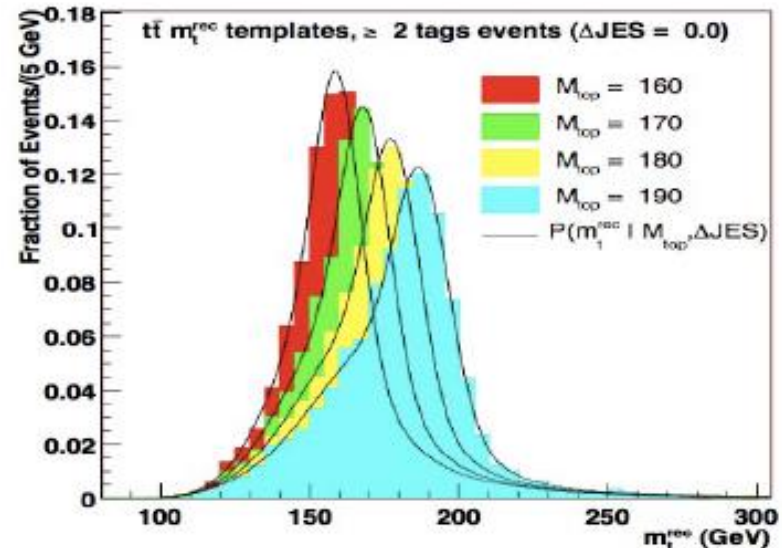
- Identify jets coming from W
  - All non-btagged jets pairs are taken into account equally.
  - 1/3/6  $m_{jj}$  per event with 2/1/0 b-tag
- Reconstruct their invariant mass  $m_{jj}$
- $M_{jj}$  strongly dependent on JES
  - Make  $M_{jj}$  templates by varying JES
  - Fit data with  $W_{jj}$  to measure JES!
- $M_W$  uncertainty is negligible (< 50 MeV)
- $M_{jj}$  mostly independent of  $M_{top}$
- This scale is applied to b-jets and light-quark jet



JES from  $W \rightarrow jj$  is mostly statistical  $\rightarrow$  luminosity scale !

# Top Mass Measurement: standard methods

- The first “standard” methods (still used) are:
  - 1) Template **method**
  - 2) Matrix Element **method**
- **1) Template method** (simplest technique):
  - ⇒ Choose a variable sensitive to the top mass ( $\xi$ )
  - ⇒ Exploit dependence on  $m_{\text{top}}$  of kinematic observable  $\xi$
  - ⇒ Create “templates” = distributions of  $\xi$  using MC
    - For signal:  $\xi = \xi(m_{\text{top}})$
    - For background
  - ⇒ Maximise consistency with the given  $m_{\text{top}}$
  - ⇒ Advantages:
    - Few assumptions
    - fairly straight-forward
  - ⇒ Drawback:
    - Sub-optimal sensitivity



Invariant mass of 3 jets, 2 from W, 1 from b

# Top Mass Measurement: standard methods

- The first standard methods (still used) are:

- 1) Template method
- 2) Matrix Element method

- **2) Matrix element method:**

⇒ Directly calculate the event probability as:

$$P_{\text{evt}}(m_{\text{top}}) \propto f P_{\text{sig}}(m_{\text{top}}) + (1 - f) P_{\text{bgr}}$$

$$P_{\text{sig}}(m_{\text{top}}) \propto \int \dots d\sigma_{t\bar{t}}(m_{\text{top}}) \quad d\sigma_{t\bar{t}} \propto |\mathcal{M}_{t\bar{t}}|^2(m_{\text{top}})$$

⇒ Advantages:

- Use full 4-vectors with maximal kinematic and topological information
- higher weight is assigned to events that are more likely to be from  $t\bar{t}$

⇒ Drawbacks:

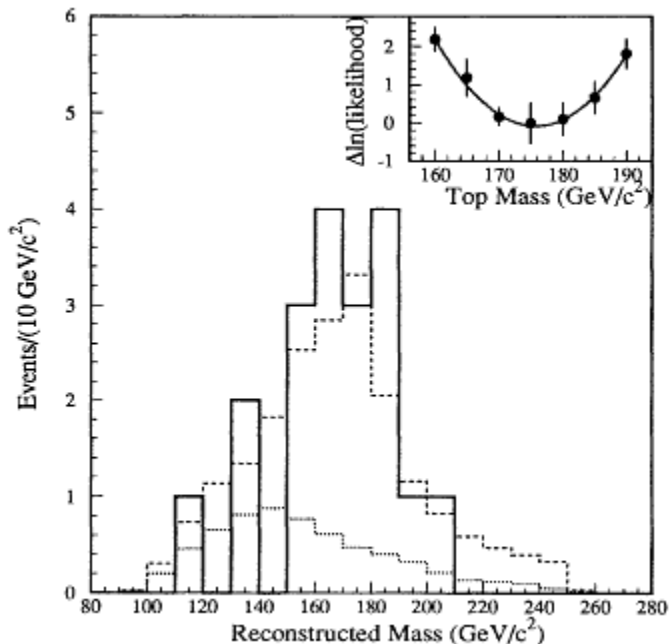
- High computational demand
- Theory assumptions: incorrect modeling due to missing theory corrections

# First measurement of top quark mass

- First measurement of top quark mass in 1995 performed in the lepton plus jets channel, using a sample of 19 events with an expected background of  $\sim 7$  at CDF and 17 events with  $\sim 4$  backg at D0 .

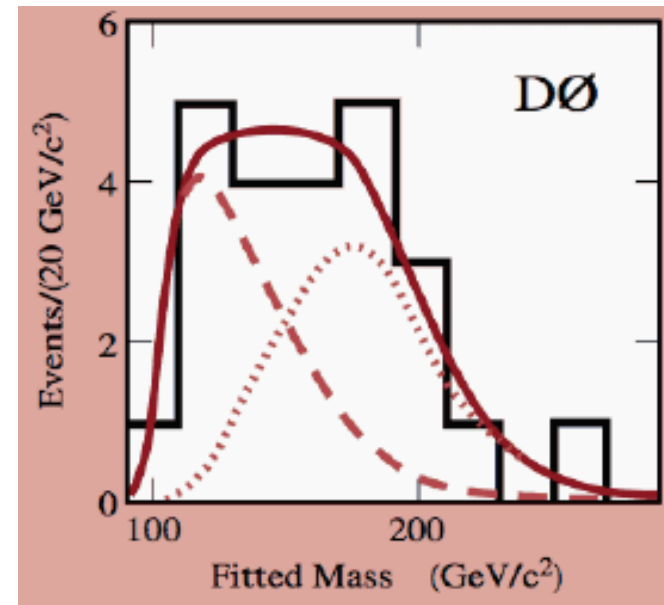
Reconstruct  $M_{\text{top}}$  with 2 constraints:  $M(W^+) = M(W^-)$ ,  $M(t) = M(\text{tbar})$

- $M_{\text{top}} = 176 \pm 13 \text{ GeV}/c^2$



PRL 74 2626 (1995)

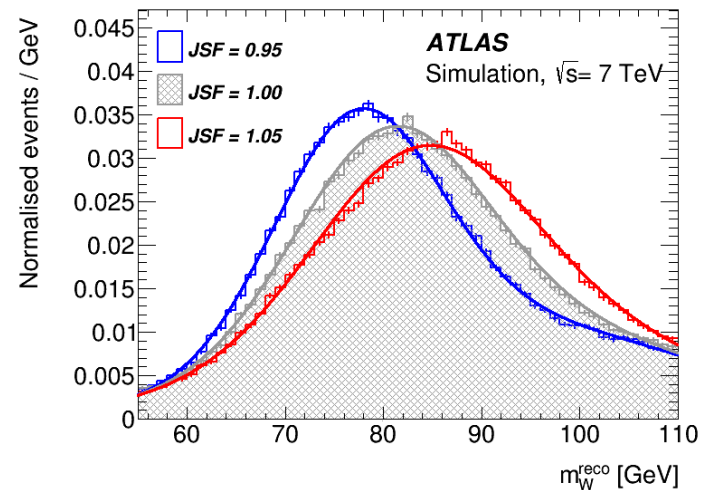
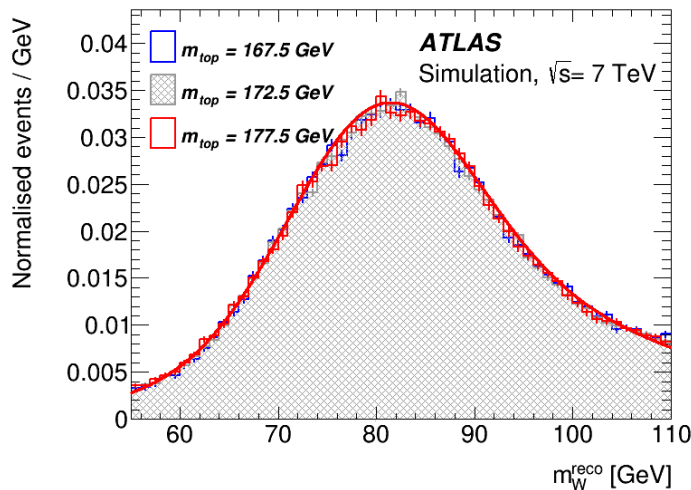
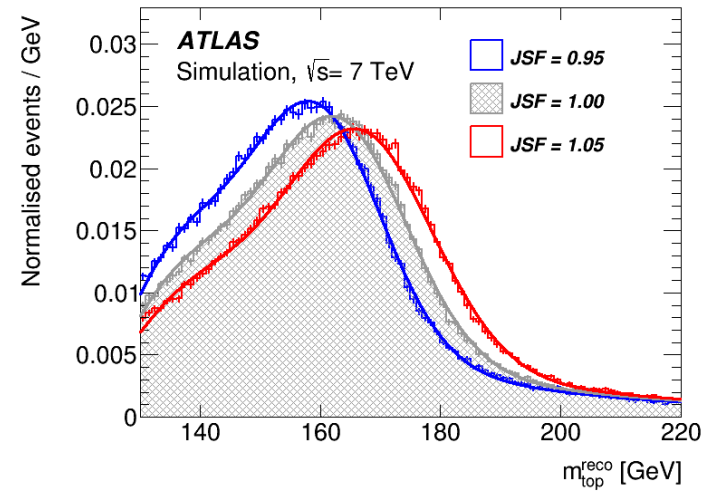
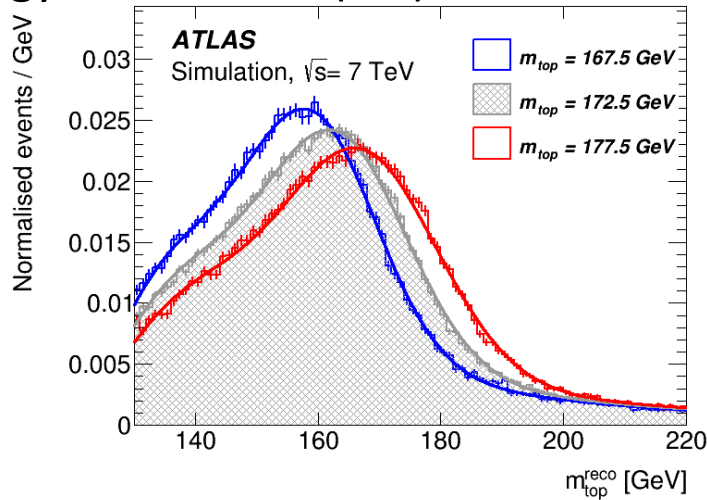
- $M_{\text{top}} = 199 \pm 30 \text{ GeV}/c^2$



PRL 74 2632 (1995)

# ATLAS top mass

- Similar template measurement in ATLAS
- W mass used to constrain the JES in situ
- Simulated plots obtained for 3 values of top quark mass and 3 values of the jet energy scale factor (JSF)

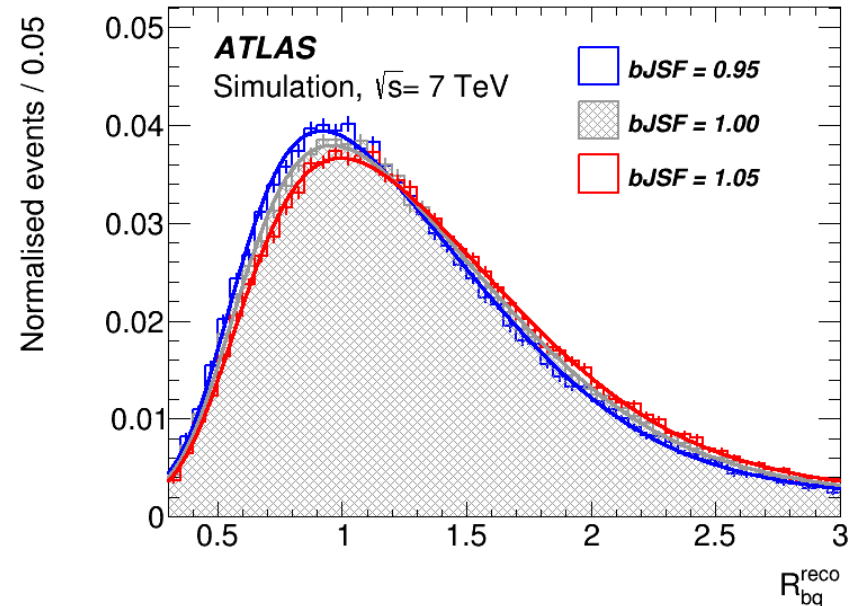
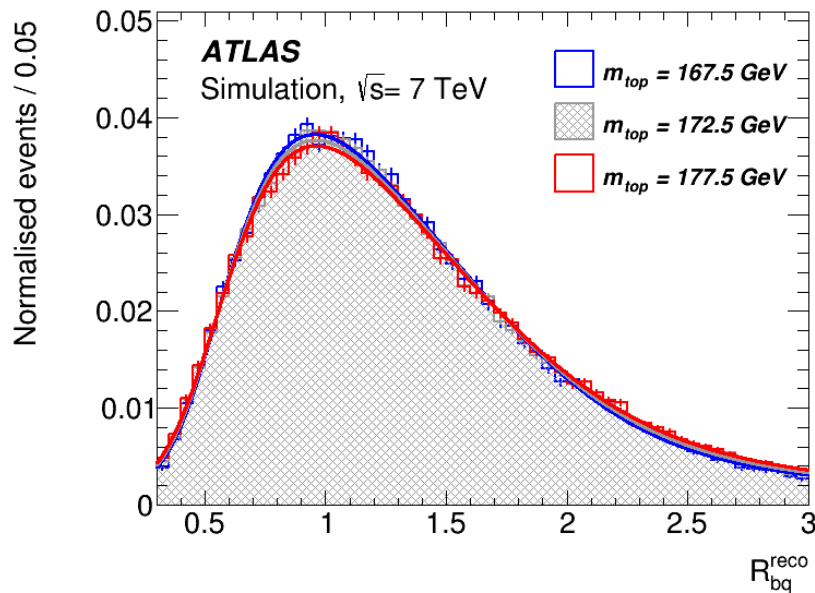




# ATLAS top mass

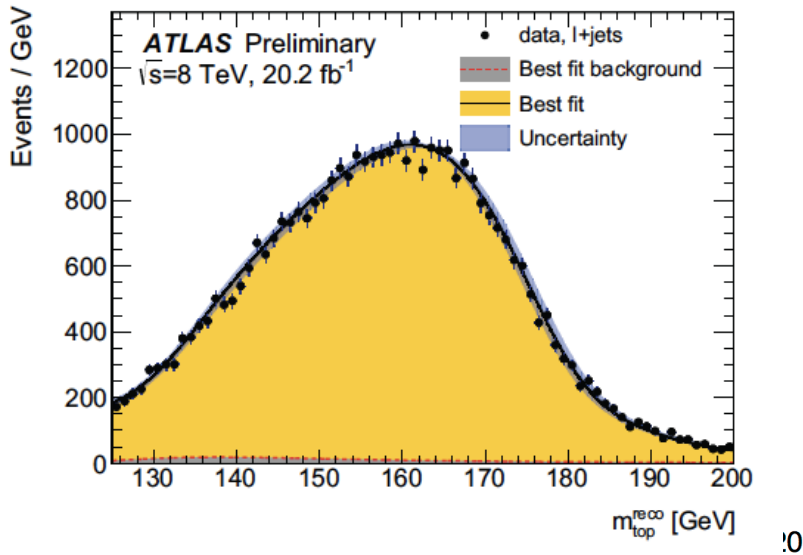
- Fitting the invariant mass of the 3 jets system is very sensitive to the jet energy scale
- $W$  mass used to constrain the JES in situ
- New Idea: Can use a variable sensitive to the relative energy scale of b-jets compared to q/g jets
- $R_{bq} = (p_T^{b1} + p_T^{b2}) / (p_T^{q1} + p_T^{q2})$

[Eur. Phys. J. C \(2015\) 75:330](#)

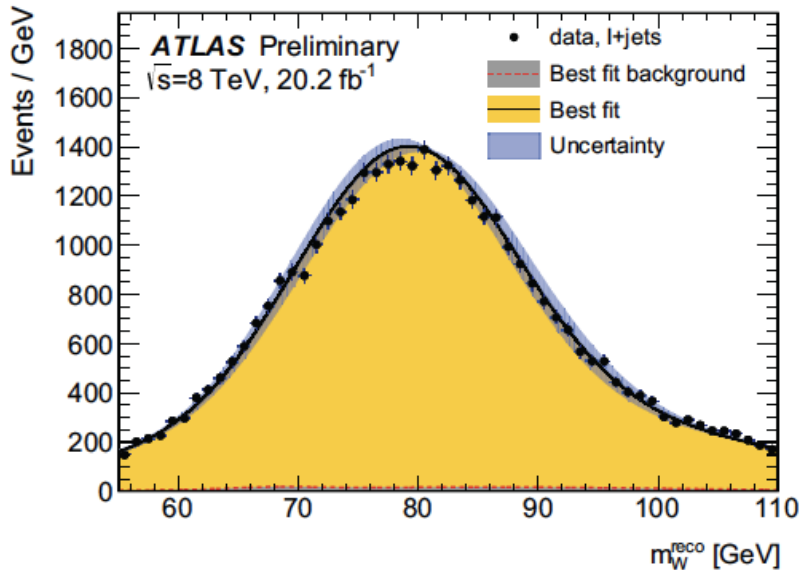


# ATLAS 3D template fit in lepton+jets

ATLAS-CONF-2017-071



(a) Reconstructed top quark mass



(b) Reconstructed W boson mass

- Reconstruct the top pairs using kinematic likelihood fit to select combination of assignments that best fits  $t\bar{t}$  hypothesis
- Use 3-dimensional template fit to determine  $m_{\text{top}}$  with the jet energy scale factor (JSF) and the relative b-to-light-jet energy scale factor (bJSF)

$$m_{\text{top}} = 172.08 \pm 0.39 \text{ (stat)} \pm 0.82 \text{ (syst)} \text{ GeV}$$

Biggest systematic uncertainties: JES, and bJES

Precision: 0.5%

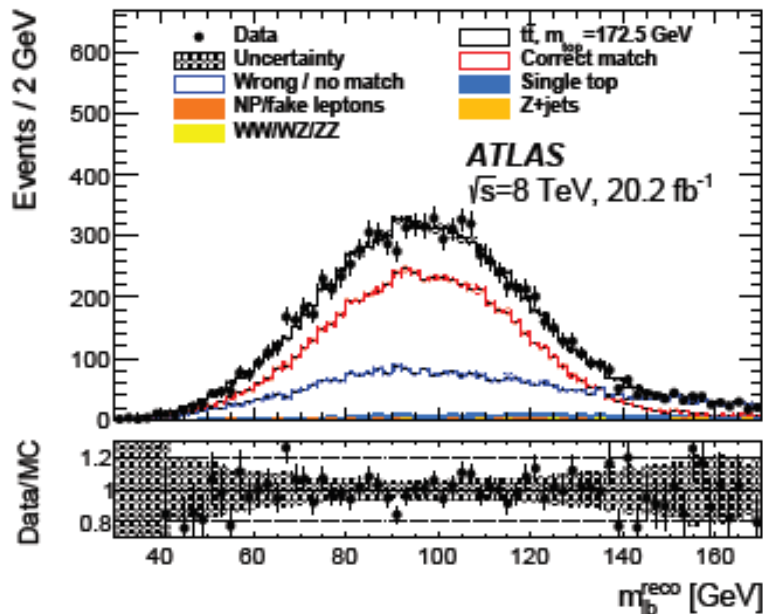
# ATLAS dilepton top quark mass @8TeV

- Dilepton analysis with 2 oppositely charged leptons + 2 b-tagged jets
- For ee and  $\mu\mu$  require  $E_T^{\text{miss}} > 60$  GeV, Z-veto and  $m_{\ell\ell} > 15$  GeV
- For  $e\mu$  require scalar sum of  $p_T$  of leptons and jets  $> 130$  GeV
- Optimisation of the final uncertainty with  $p_T(l,b) > 120$  GeV
- The analysis uses a template fit to  $m_{\text{reco}}(l,b)$  with  $m_{\text{top}}$  as free parameter
- Largest systematics from jet energy scale, relative b-to-light-jet energy scale (bJES).
- The  $m_{\text{top}}$  value that best describes the data is:

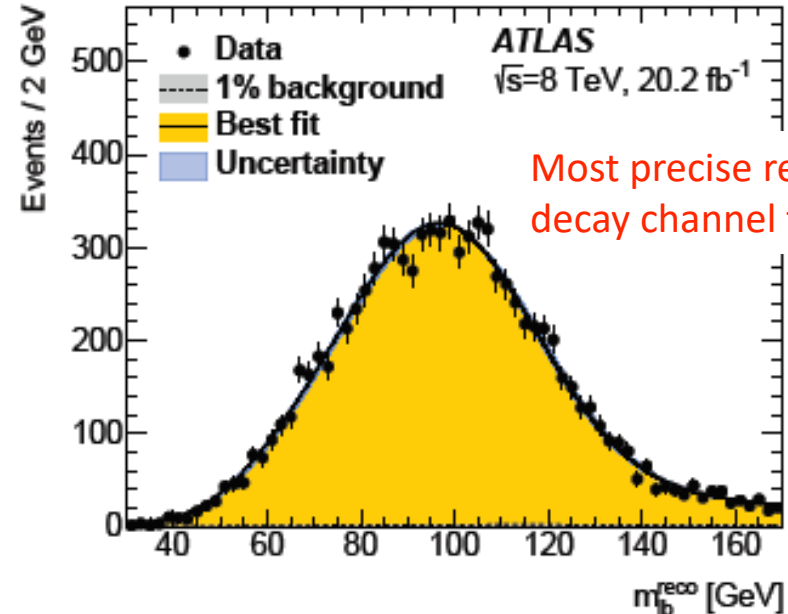
$$m_{\text{top}} = 172.99 \pm 0.41(\text{stat}) \pm 0.74(\text{syst}) \text{ GeV}$$

Precision: 0.46%

PLB 761 (2016) 350 - 371



(b)  $m_{\ell b}^{\text{reco}}$  in data and simulation



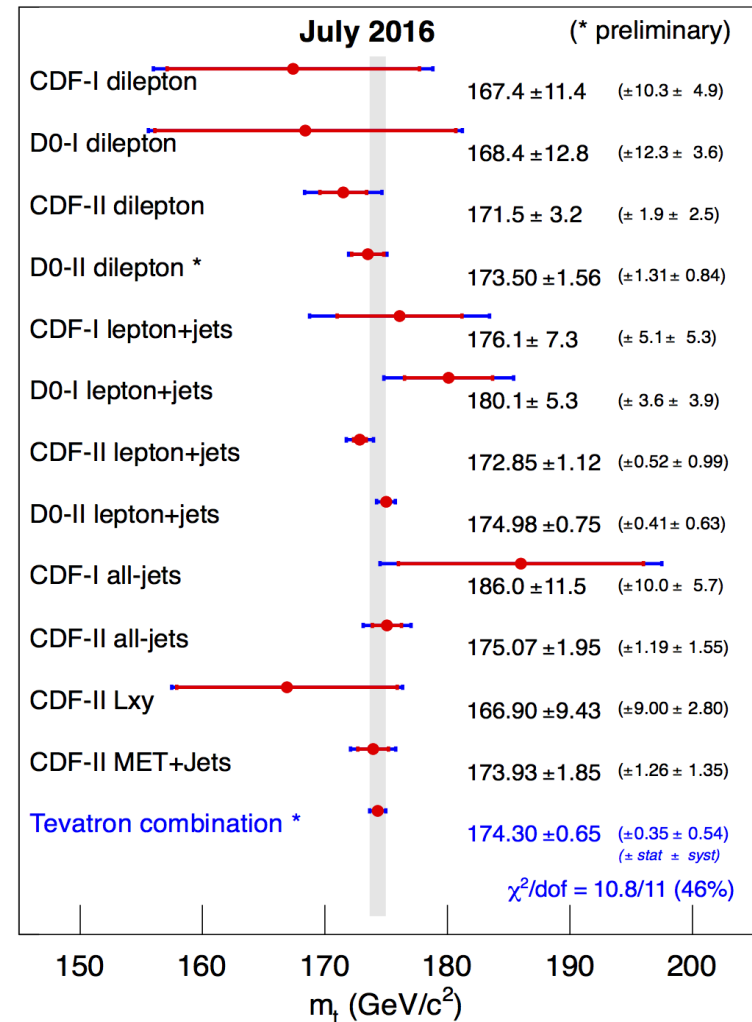
Most precise result in this decay channel to date

(c) Fit to  $m_{\ell b}^{\text{reco}}$  in data

# Tevatron top mass combination

- 5 Run I and 7 Run II results
- Combination performed using BLUE
- Limited by systematic uncertainties
  - ⇒ Dominant: signal modeling and jet energy scale uncertainties
- **Total uncertainty  $\pm 0.65 \text{ GeV}/c^2$  ( $< 0.4\%$ )**  
(better than world comb. March 2014:  $\pm 0.76 \text{ GeV}/c^2$ )

Mass of the Top Quark

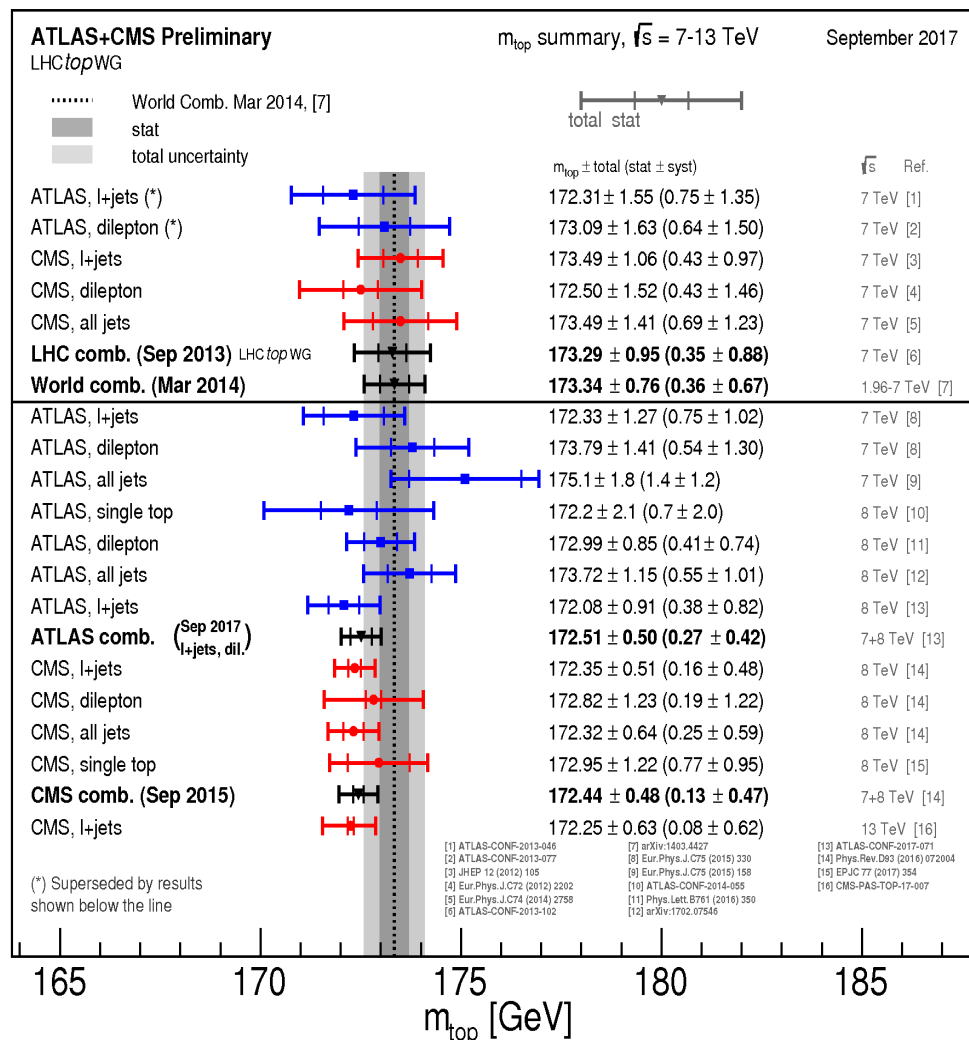


$$M_{\text{top}} = 174.30 \pm 0.35 \text{ (stat)} \pm 0.54 \text{ (syst)} \text{ GeV}/c^2$$

arXiv:1407.2682  
arXiv:1608.01881

# ATLAS and CMS top mass measurements

- Best precision is reached when combining all methods/channels across all experiments
- LHC and Tevatron results with nearly comparable precision of 3-4 permille (~0.5 GeV)
- LHC top mass systematically limited: MC modelling, (b)JES

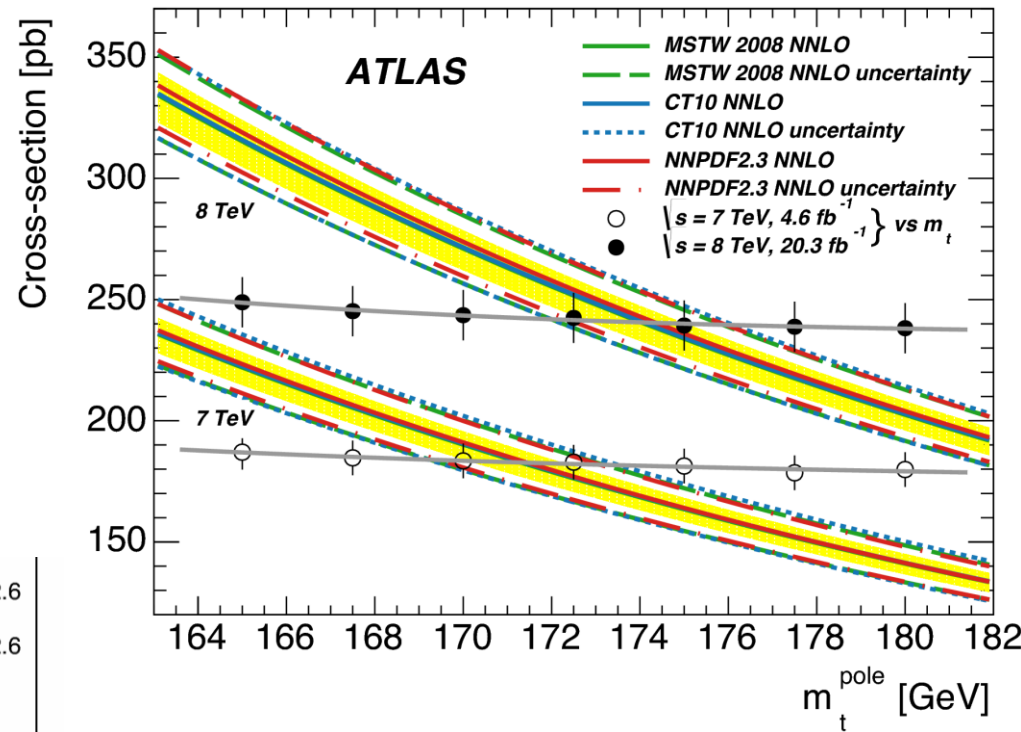
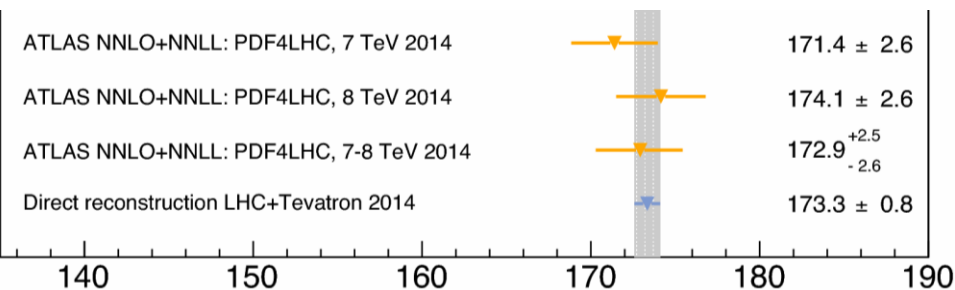


⇒ Since LHC is a top quark factory, it's all about controlling systematics  
 ⇒ new approaches with complementary systematics can constrain combined systematics

# ATLAS top pole mass in dilepton channel

- Advantage of the "indirect" method: extract the top «pole» mass in a well-defined renormalization scheme (NNLO calculations)
- Mass from precision cross section in  **$e\mu$  dilepton channel**
- ⇒ Designed to be not very sensitive to the top mass
- Plot the observed (measured) cross section as a function of top mass (**dots with error bars**)
- Plot the expected cross section as a function of top mass in the pole mass scheme (**curves**)
- Intercept of the two gives the pole mass
- Drawback: less precise than direct measurements
- Limited by theoretical uncertainties: scale and PDF

$$m_{\text{top}} = 172.9^{+2.5}_{-2.6} \text{ GeV}$$



# D0 pole mass from inclusive and differential $\sigma$

- From inclusive cross-section measur. in lepton+jets and dilepton channels, similar to ATLAS method:

$$m_{\text{top}} = 172.8 \pm 1.1 \text{ (theo.)}^{+3.3}_{-3.1} \text{ (exp.) GeV}$$

- Using the differential  $t\bar{t}$  cross section:

- ✓ additional information coming from the shape of the distributions
- ✓ possible since NNLO differential predictions are now available (JHEP 1605, 034 (2016))

- $p_T^{\text{top}}$  and  $m_{t\bar{t}}$  distributions sensitive to pole mass

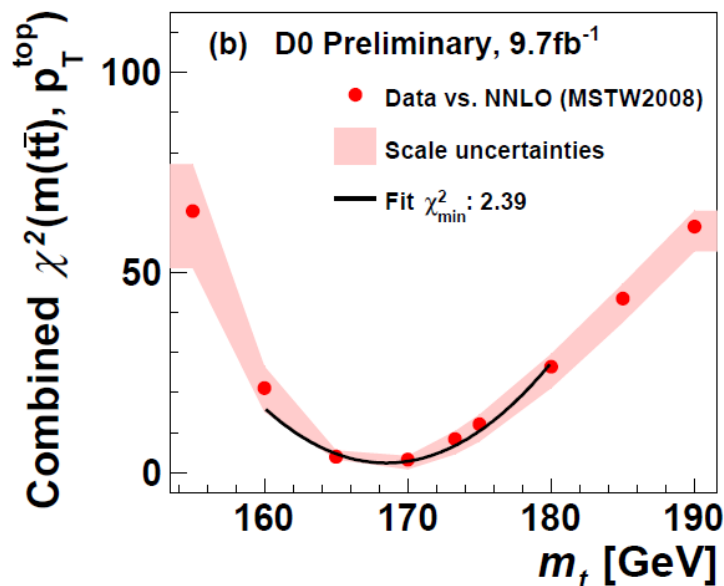
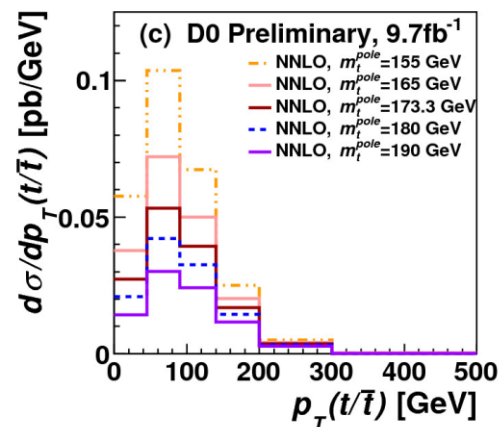
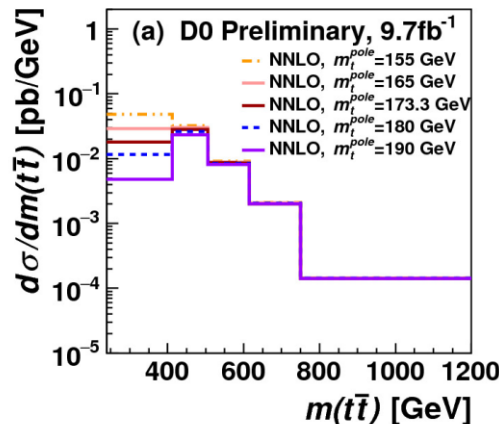
- compared to NNLO QCD calc. , four different PDF sets

- $\chi^2$  fit to both distributions

- $p_T$  vs.  $m_{t\bar{t}}$

$$m_{\text{top}} = 169.1 \pm 2.5 \text{ (total) GeV}$$

- smaller uncertainty than from D0 inclusive cross section (1.5%)



FERMILAB-CONF-16-383-PPD

D0 Note 6473-CONF



# D0 pole mass from inclusive and differential $\sigma$

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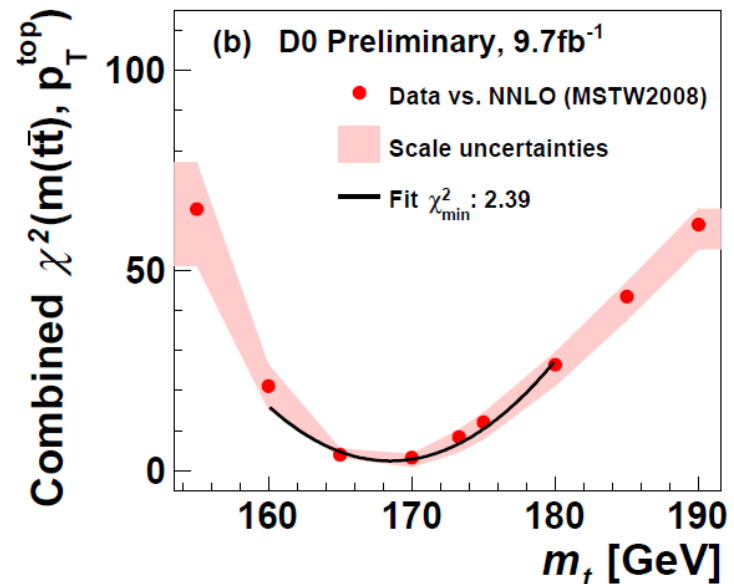
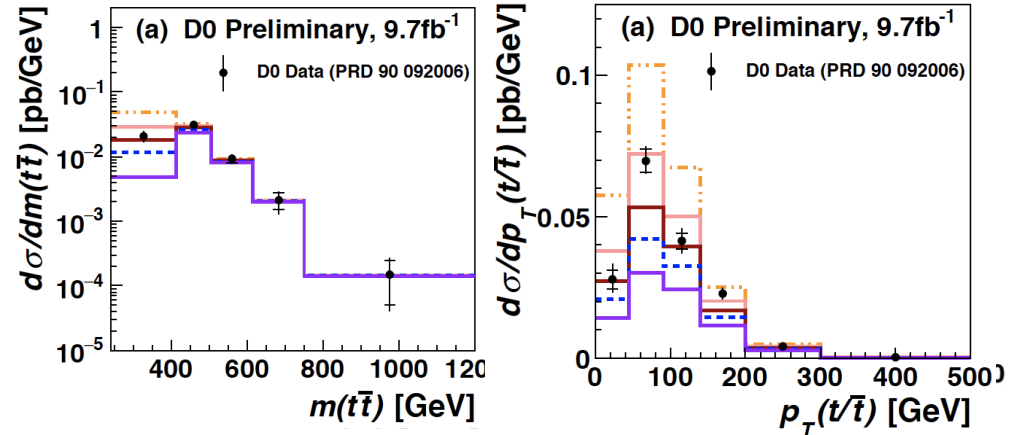
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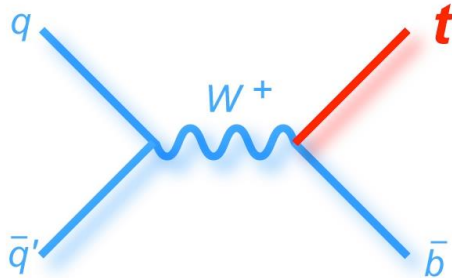


# Single top production

# How else is top quark produced?

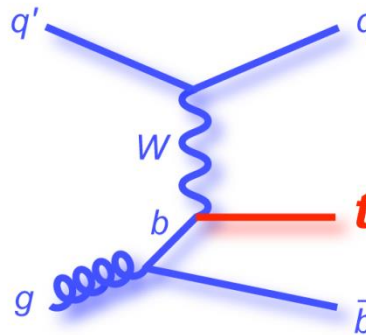
- Electroweak single top production:

s-channel



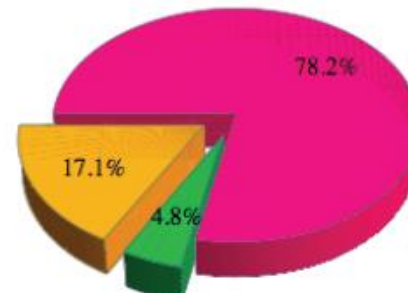
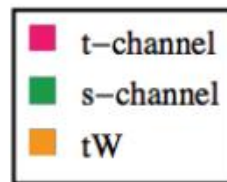
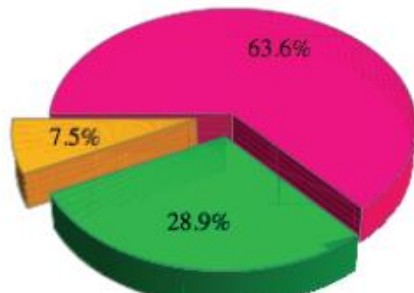
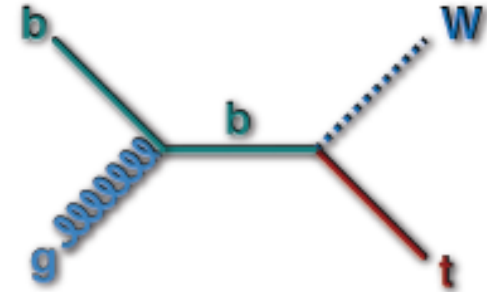
Tevatron:  $\sigma_{\text{tot}} = 3 \text{ pb}$

t-channel



LHC:  $\sigma_{\text{tot}} = 114 \text{ pb @ 8 TeV}$

Wt-production



Cross section(pb)

*tt*

s-channel

t-channel

Wt

Tevatron(1.96 TeV)

7.08

1.05

2.08

0.12

LHC(8 TeV)

234

5.55

87.2

20

LHC(13 TeV)

830

10.5

217

72

**x33**

**x5.3**

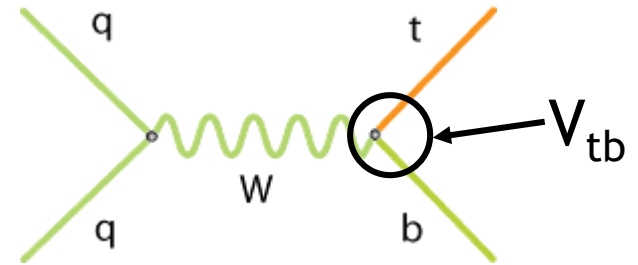
**x42**

**x160**

(N. Kidonakis, arXiv:1210.7813)

# Why measure Single Top Production ?

- $\sigma_{\text{single top}} \propto |V_{tb}|^2$
- Give access to the W-t-b vertex
  - ⇒ probe V-A structure
  - ⇒ access to top quark spin
- Allows direct measurement of Cabibbo-Kobayashi-Maskawa (CKM) matrix element  $|V_{tb}|$ :



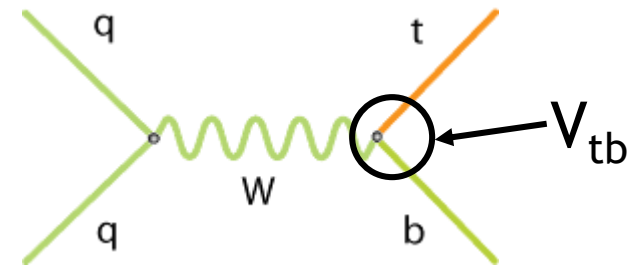
Direct measurements

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Ratio from Bs oscillations      Not precisely measured  
Inferred using unitarity

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$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} & V_{uX} ? \\ V_{cd} & V_{cs} & V_{cb} & V_{cX} ? \\ V_{td} & V_{ts} & V_{tb} & V_{tX} ? \\ V_{Yd} ? & V_{Ys} ? & V_{Yt} ? & V_{YX} ? \end{pmatrix}$$

- Is this Matrix 3x3 ?
- Is there a 4<sup>th</sup> generation ?
- Does unitarity hold ?

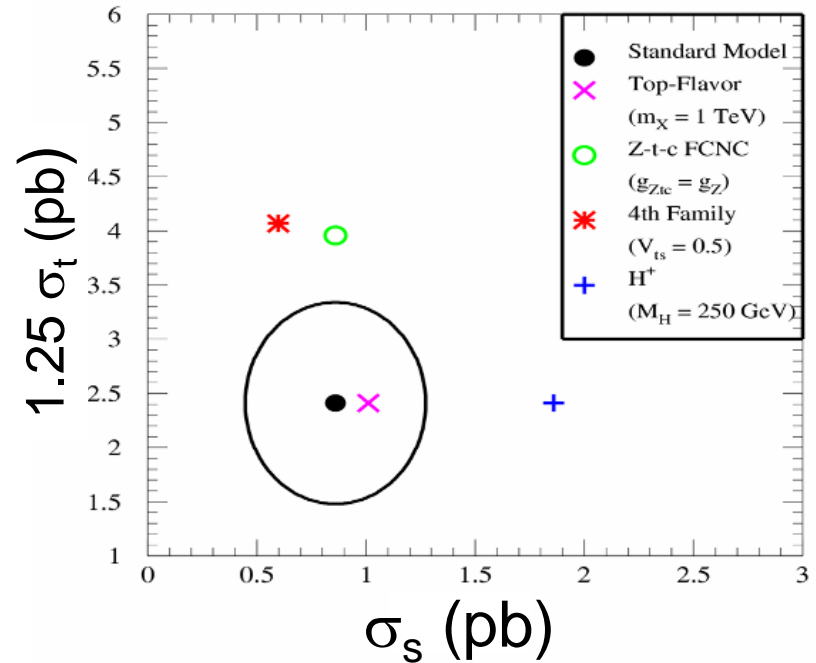
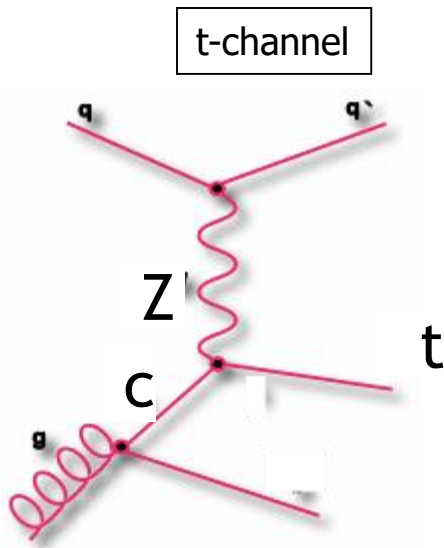
$$|V_{ub}|^2 + |V_{cb}|^2 + |V_{tb}|^2 \stackrel{?}{=} 1$$

- Precision electroweak measurements rule out “simple” fourth generation extensions, but see for example:

J. Alwall et. al., “Is  $|V_{tb}| \sim 1$ ?” Eur. Phys. J. C49 791-801 (2007).

# Sensitivity to New Physics

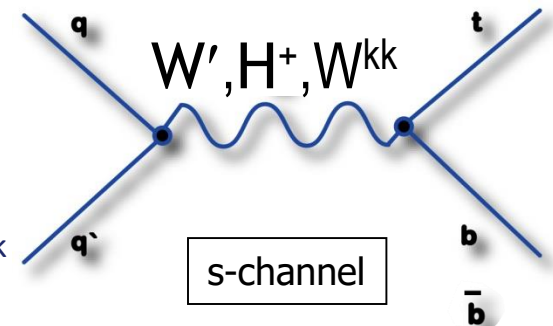
- New physics may affect the rate of t and s channel differently



T. Tait, CP Yuan PRD63, 014018 (2001)

- Flavor changing neutral currents (t-Z-c, t- $\gamma$ -c, t-g-c)

- heavy  $W'$  boson
- charged Higgs  $H^+$
- Kaluza Klein excited  $W^{kk}$

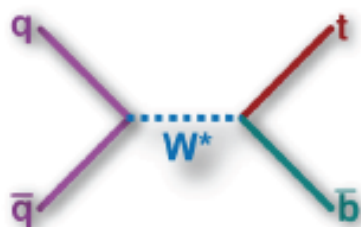


# The Challenge (1)

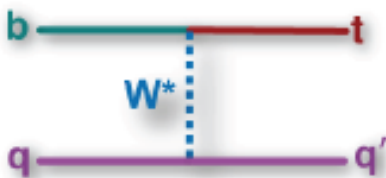
- Single Top observation came 14 years after top discovery....

⇒ Single Top production was a rare process at the Tevatron:  
 S/B  $\sim 1:10^9$  before any selection

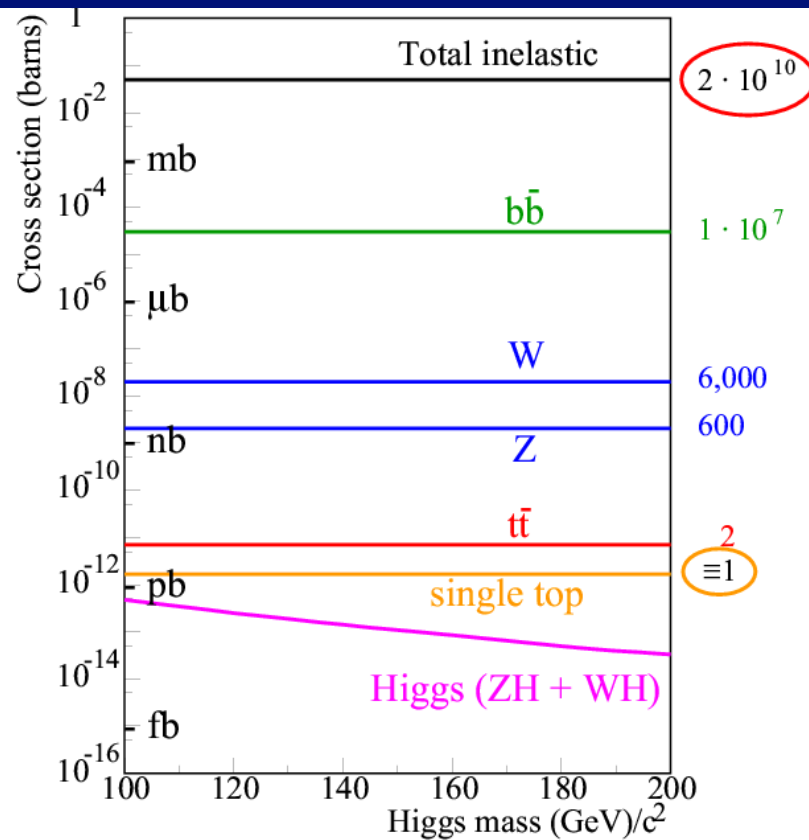
- not an easy measurement



s-channel  
 $1.05 \pm 0.06 \text{ pb}$

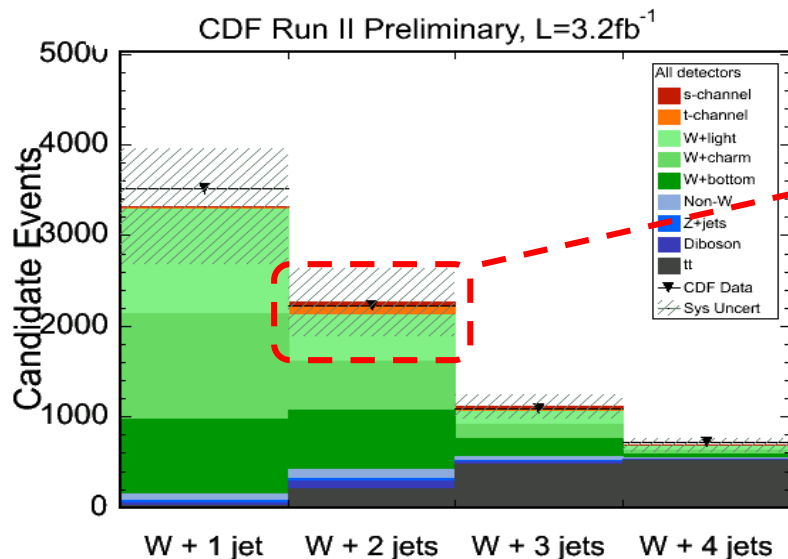


t-channel  
 $2.12 \pm 0.16 \text{ pb}$





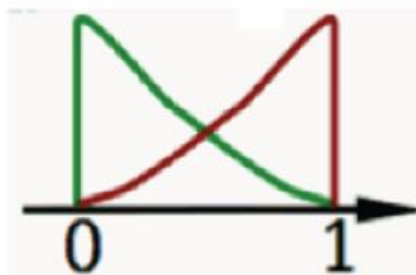
# The Challenge (2)



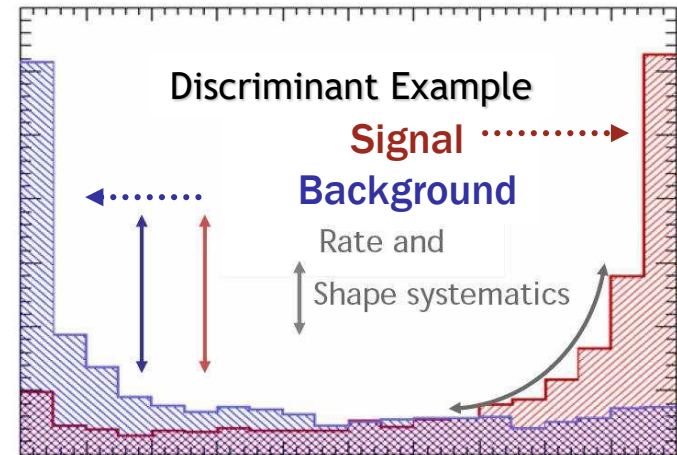
Single top top quark production with decay into **Lepton + 2 Jets** final state hidden behind **large backgrounds** with large uncertainties (i.e. W+HF uncertainty  $\sim 30\%$ )  
 $\Rightarrow$  **Makes counting experiment impossible!**

- **Third step:** no single variable provides sufficient signal-background separation:  
 $\Rightarrow$  take advantage of small signal-background separation in many variables  
 $\Rightarrow$  **Perform multivariate analysis (MV)**  
 $\Rightarrow$  Multiple variables combined into a single more powerful discriminant to separate S from B

**background**      **signal**



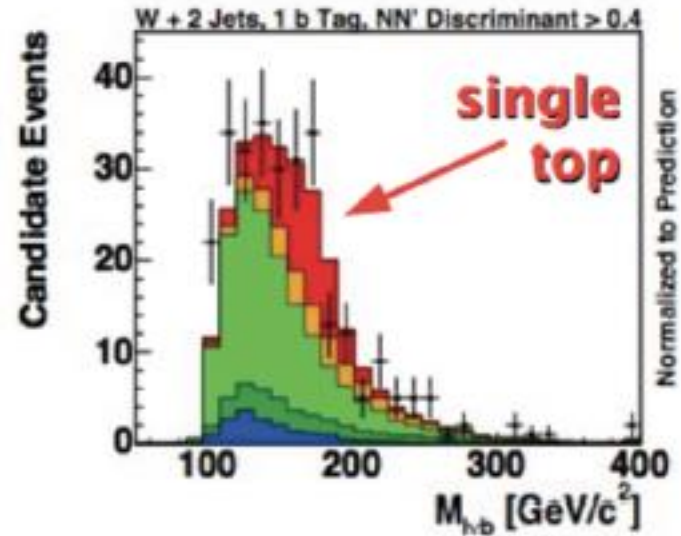
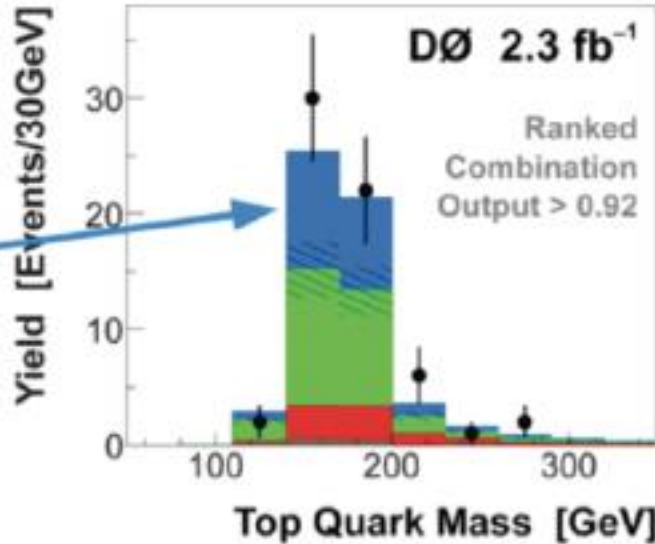
- Maximize signal acceptance
- Calculate discriminant functions that separate signal from background
  - Likelihood functions
  - Matrix element
  - Neural network (NN)
  - Bayesian Neural Network (BNN)
  - Boosted decision tree
- Check discriminant performance using data control samples
- Perform the statistical analysis



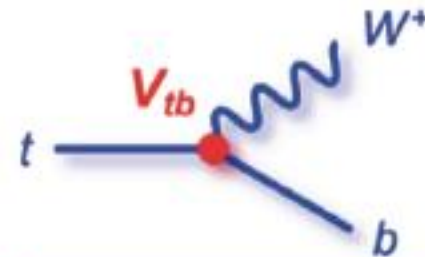
# 2009: Single top discovered at Tevatron



single top



Single Top Cross Section	Signal Significance	
	Expected	Observed
<b>DØ</b> 2.3 fb <sup>-1</sup> arXiv.0903.0850 $m_{top} = 170$ GeV		
3.94 ± 0.88 pb	4.5 σ	5.0 σ
<b>CDF</b> 3.2 fb <sup>-1</sup> arXiv.0903.0885 $m_{top} = 175$ GeV		
2.3 <sup>+0.6</sup> / <sub>-0.5</sub> pb	>5.9 σ	5.0 σ



$$|V_{tb}| = 1.07 \pm 0.12$$



$$|V_{tb}| = 0.91 \pm 0.13$$

⇒ observation with 5.0σ!



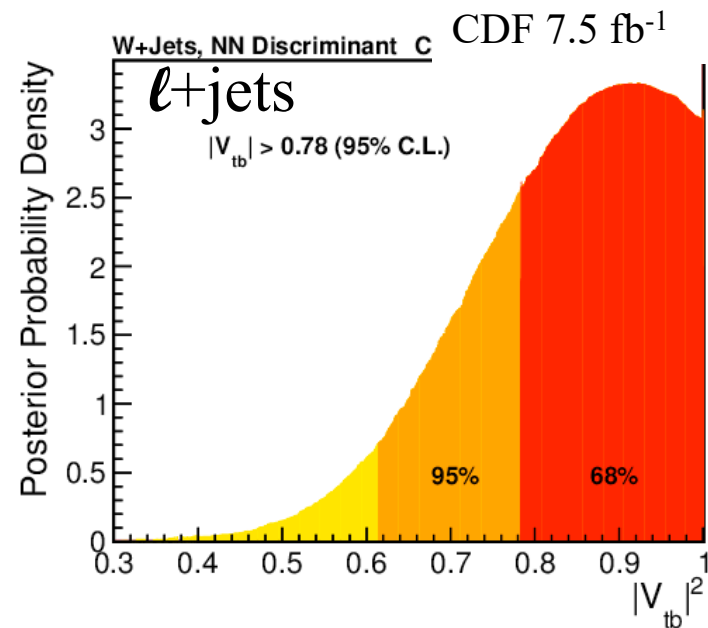
# CKM matrix element $|V_{tb}|$

- $\sigma(s+t+Wt) \propto |V_{tb}|^2 \rightarrow$  calculate posterior probability density function in terms of  $|V_{tb}|^2$
- To transform  $\sigma(s+t)$  measurement into  $|V_{tb}|$ , assume:
  - $\Rightarrow$  SM top quark decay:  $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$
  - $\Rightarrow$  V-A and CP conserving  $Wtb$  vertex
  - $\Rightarrow$  No assumption on number of families or CKM unitarity

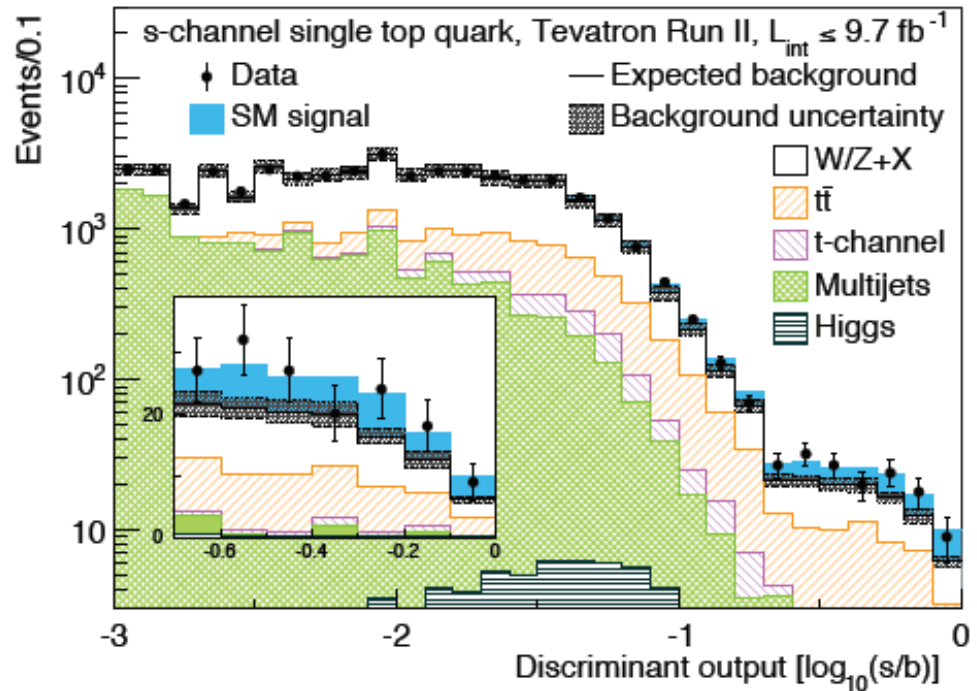
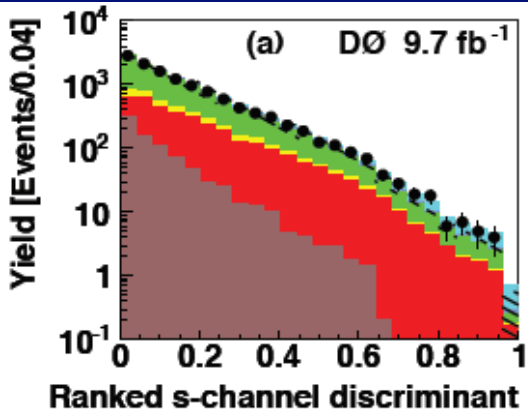
$$|V_{tb,meas}|^2 = \frac{\sigma_{meas}}{\sigma_{SM}} \cdot |V_{tb,SM}|^2$$

$$|V_{tb}| = 0.95 \pm 0.09 \text{ (stat+syst)} \pm 0.05 \text{ (theo)}$$
$$|V_{tb}| > 0.78 \text{ (95 \% C.L.)}$$

11% precision



# Tevatron s-channel results

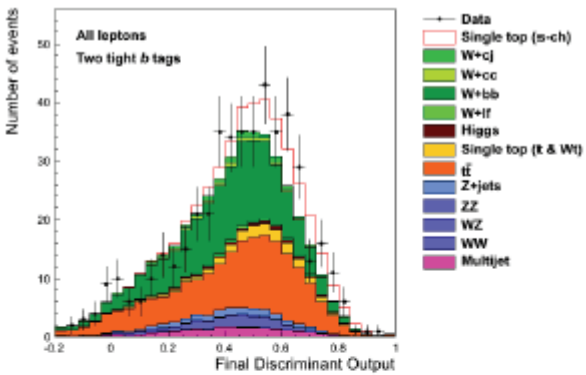


$$\sigma_{\text{s-channel}} = 1.29^{+0.26}_{-0.24} \text{ pb}$$

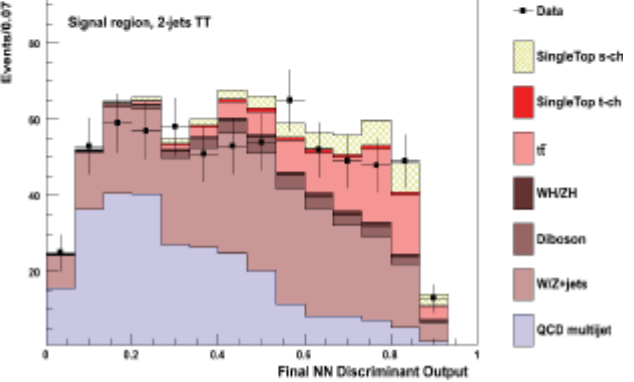
Obs (exp) significance: 6.3 (5.1)  $\sigma$

[Phys. Rev. Lett. 112, 231803](#)

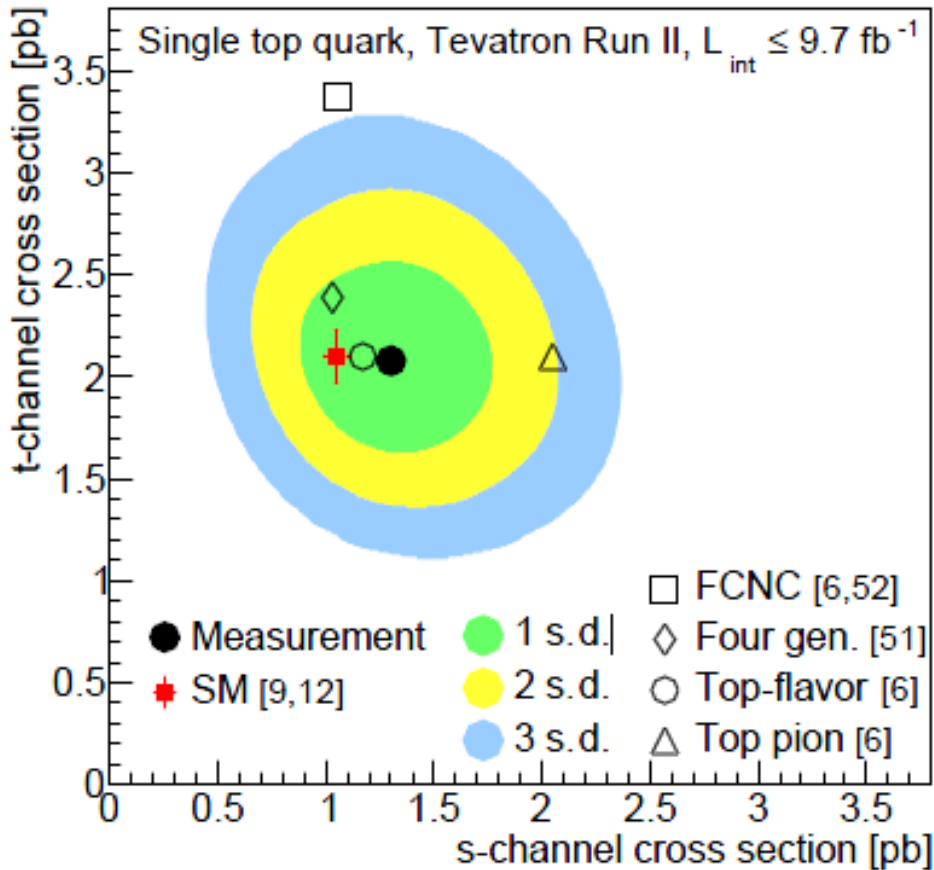
Single Top s-channel in Lepton+Jets, CDF Run II Preliminary ( $9.4 \text{ fb}^{-1}$ )



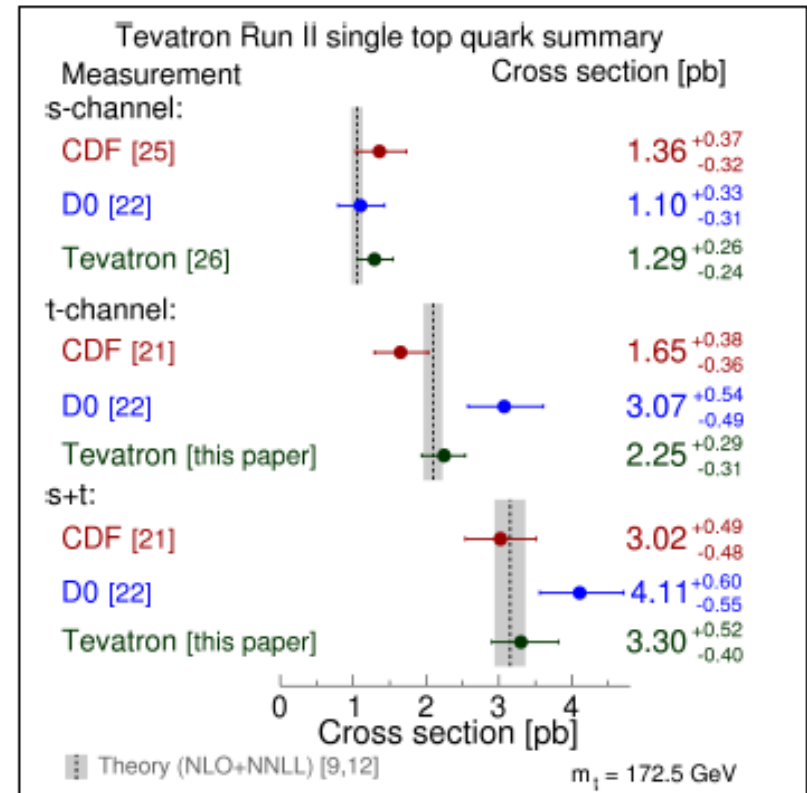
Single Top s-channel in  $\bar{\nu}_e$ +jets, CDF Run II Preliminary,  $L = 9.5 \text{ fb}^{-1}$



# Single top at the Tevatron: summary



Phys. Rev. Lett. 115, 152003 (2015)



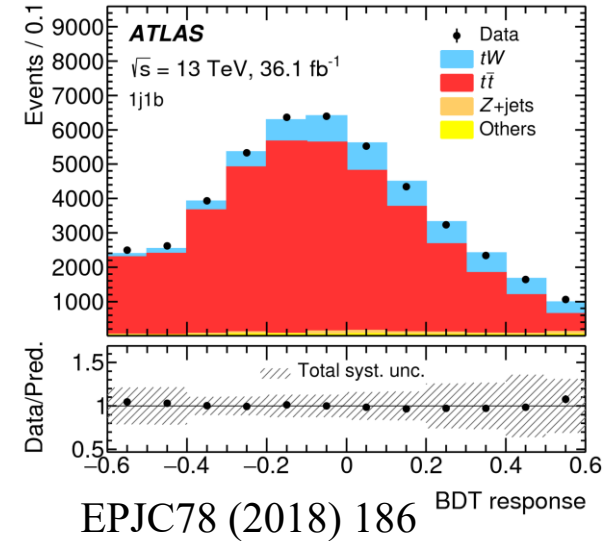


# Single top at the LHC: full program of studies

## ATLAS 13 TeV - $Wt$ channel

### BDT used to separate signal and background

- Main background:  $t\bar{t}$
- The differential cross-section for the production of a  $W$  boson in association with a top quark is measured for several particle-level observables.
- Results are found to be in good agreement with predictions from several MC event generators.



## CMS 13 TeV $t$ -channel

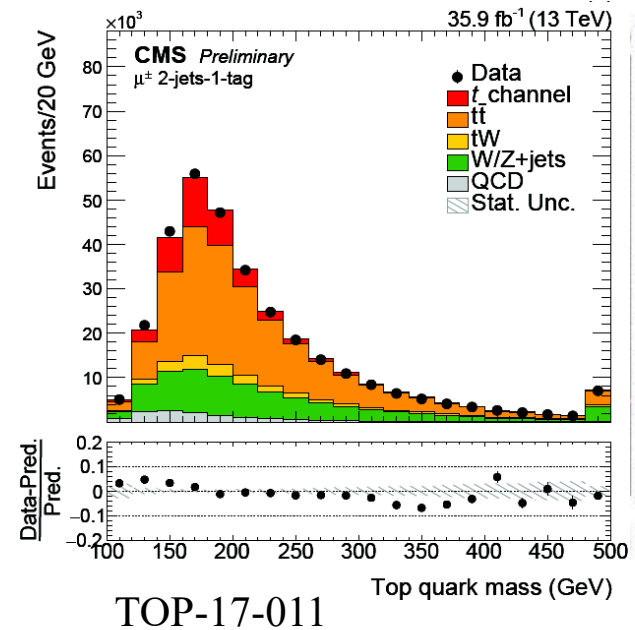
### Measurement focused on $\sigma(t)/\sigma(t\bar{t})$

- Measurement of cross section limited by systematics
- Train BDTs for signal extraction
- CKM Matrix element  $V_{tb}$  assuming:

$$B(t \rightarrow Wb) \approx 1 \Rightarrow f_{LV}^2 V_{tb}^2 = \sigma_{\text{meas.}} / \sigma_{\text{theo.}}$$

$$|f_{LV} V_{tb}| = 1.00 \pm 0.05 \text{ (exp)} \pm 0.02 \text{ (theo.)}$$

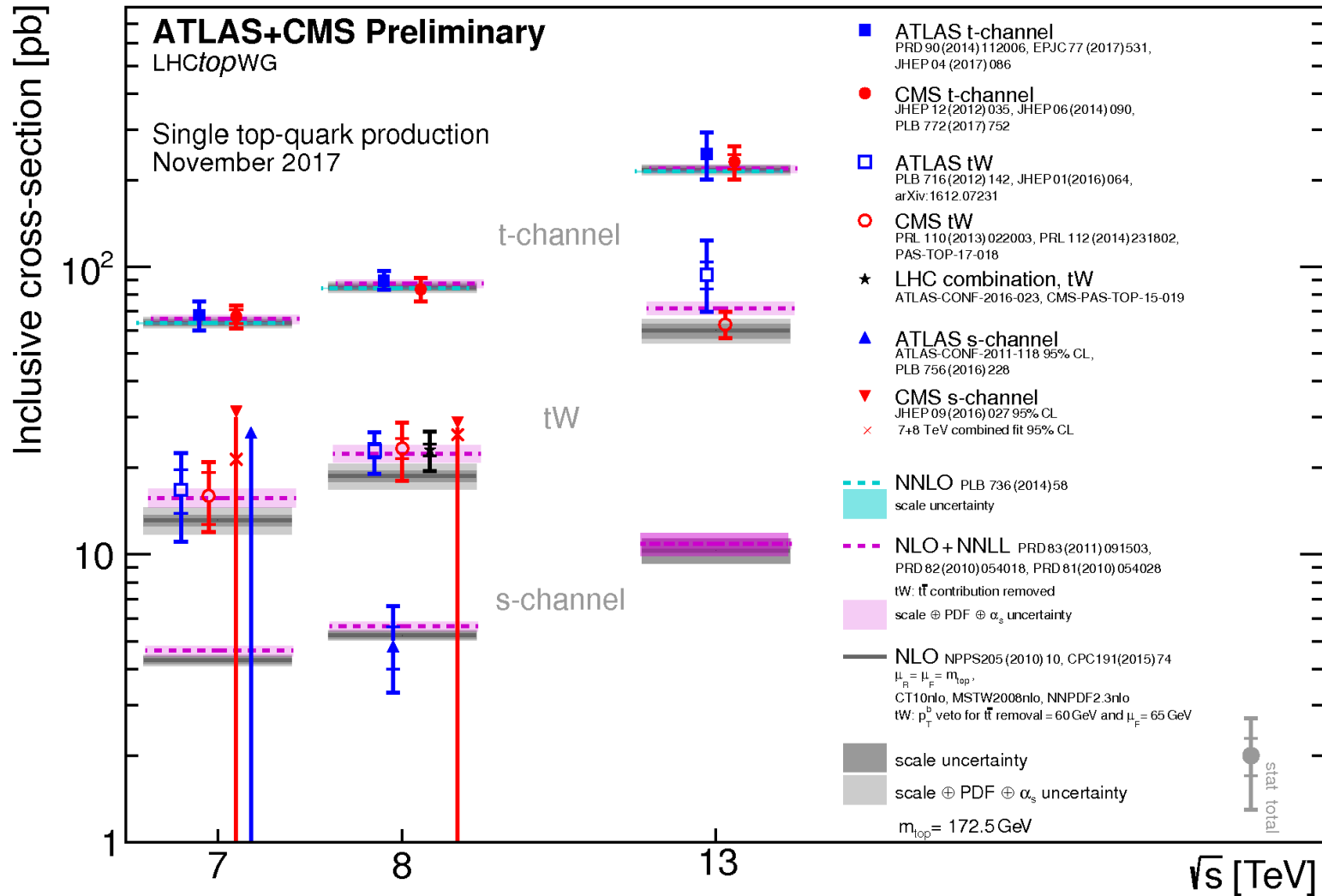
$$\left[ f_{LV}^{\text{SM}} = 1 \right]$$





# Single top at the LHC

LHC: observed t-channel and W-t, getting closer to s-channel!



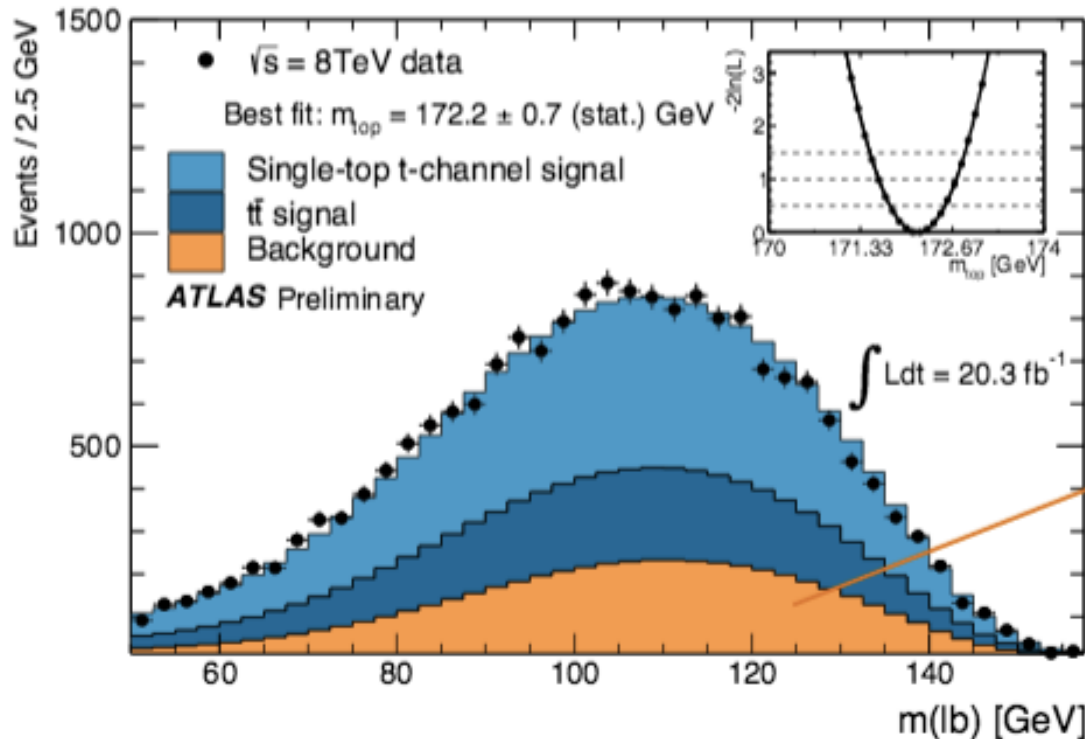
# $m_t$ in single top events (ATLAS)

ATLAS-CONF-2014-055



$$m_t = 172.2 \pm 0.7 \text{ (stat)} \pm 2.0 \text{ (syst)} \text{ GeV}$$

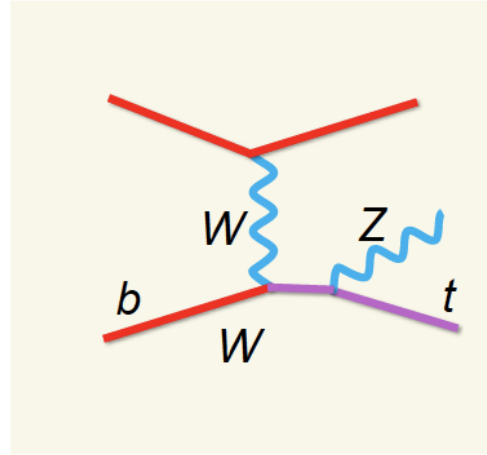
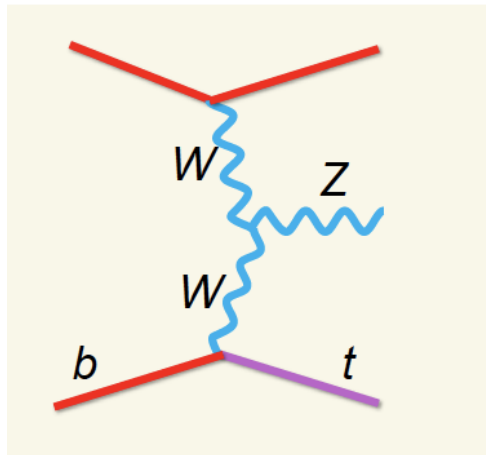
- Results are **complementary to  $t\bar{t}$  measurements**.
  - Different regime for single top production.



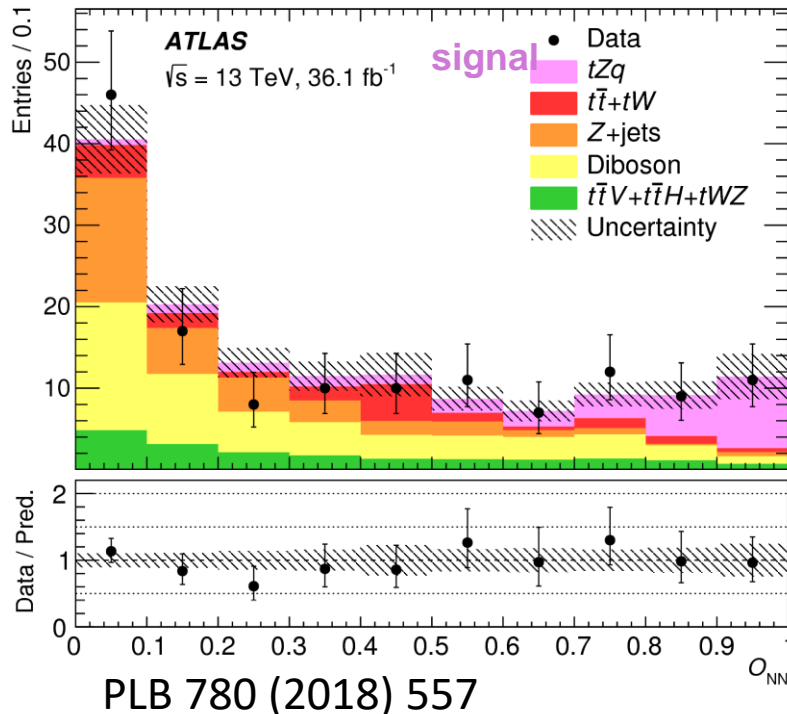
Dominant systematics:

- JES + bJES:** 1.5 GeV.
- t-channel parton showering & hadronization:** 0.7 GeV.
- W+jets shape & normalization:** 0.5 GeV.
  - Shape component due to PDFs and flavor of jets produced in association with the W.

# tZq production: a rare SM channel



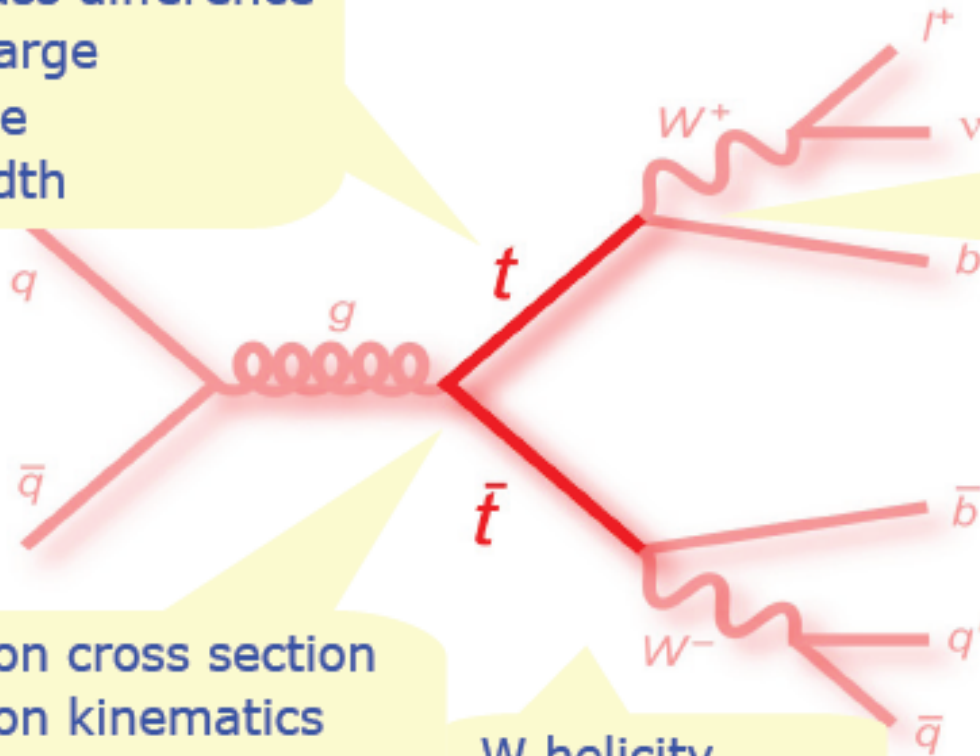
- Sensitive to WWZ and tZ coupling
- Not seen before
- Background to tH channel
- Signal region:
  - Three charged leptons in final state
  - 1 b-tagged jet
  - 1 untagged jet



- Neural network to separate signal and backgr
- Signal obtained in likelihood fit
- $\sigma = 600 \pm 170 \text{ (stat)} \pm 140 \text{ (syst)} \text{ fb}$
- (theory NLO  $800 \text{ fb} \pm 7\%$ )
- Main systematics:
  - Radiation signal MC
  - Jet energy scale
  - b-tagging
- Significance 4.2 (5.4 expected) → EVIDENCE
- The hunt for rare single-top processes started!

# Other top properties

Top mass  
Top mass difference  
Top charge  
Lifetime  
Top width



Branching ratios  
 $|V_{tb}|$   
Anomalous coupling  
New/Rare decays

Spin correlation  
Charge asymmetry  
Color Flow

W helicity

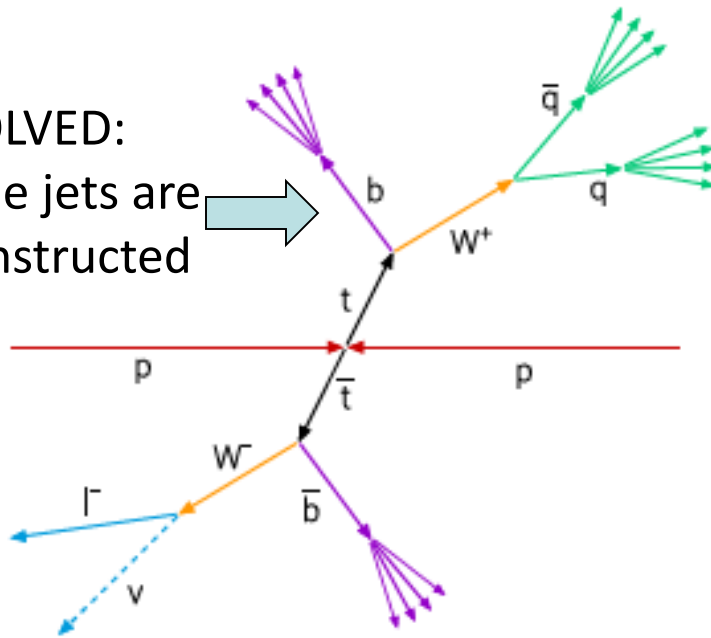
s- & t- channel production,  
properties and searches in  
single top events

Production cross section  
Production kinematics  
Production via resonance  
New particles

# Event selection: resolved vs boosted

At higher energies, more top-quark candidates are boosted:

RESOLVED:  
All the jets are  
reconstructed



Resolved topology:

- =1 lepton
- >=4 small-R jets
- >=2 b-tags

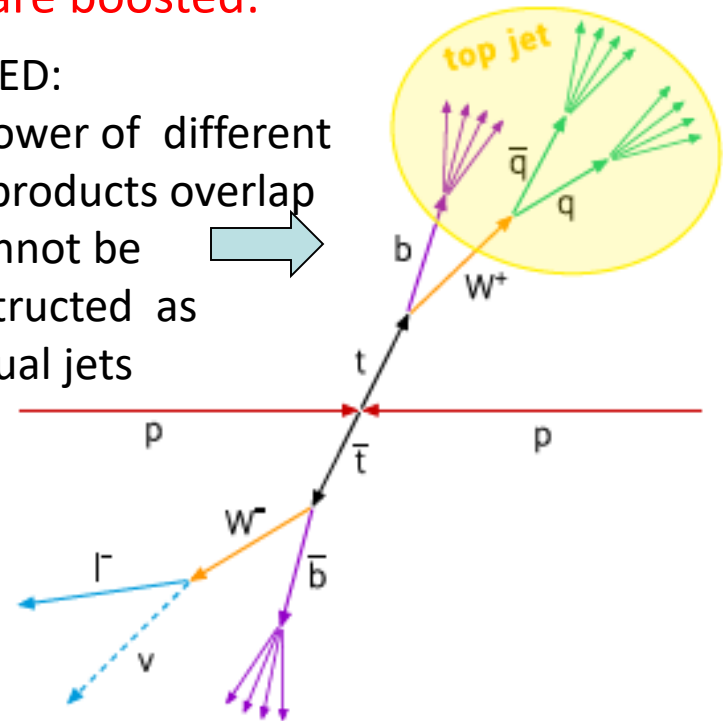
Pseudo-top object definitions:

$$\hat{t}^{\text{lep}} = \ell + E_{\text{T}}^{\text{miss}} + \text{b-jet closest to } \ell$$

$$\hat{t}^{\text{had}} = \text{other b-jet} + 2 \text{ jets with min. } |m_{jj} - m_W|$$

BOOSTED:

The shower of different  
decay products overlap  
and cannot be  
reconstructed as  
individual jets



Boosted topology:

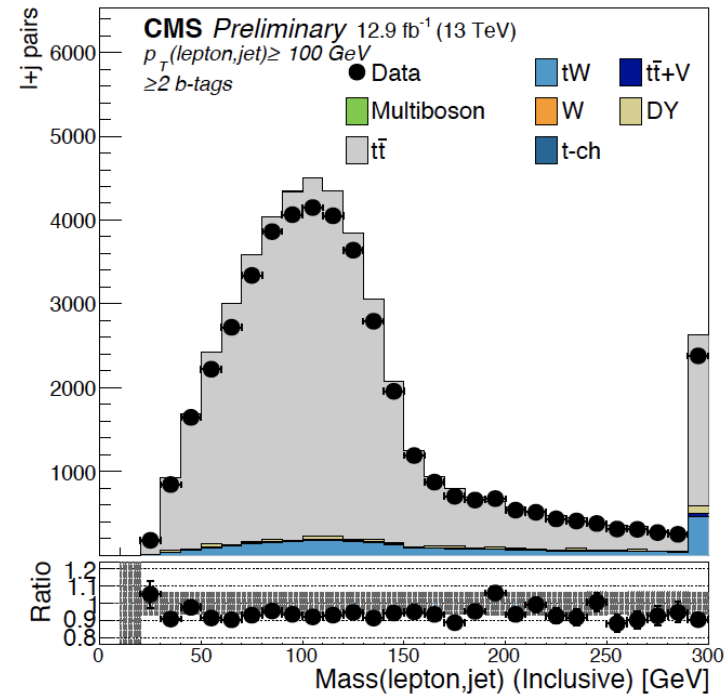
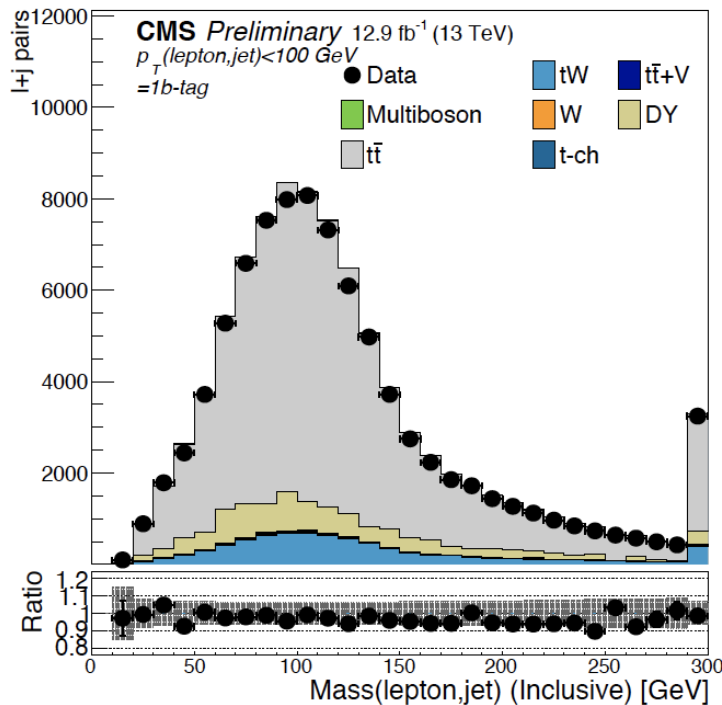
- =1 lepton
- >=1 large-R jet and >=1 small-R jet
- >=1 top-tag (large-R)
- >=1 b-tag (small-R) within the top-jet  
or close to the lepton
- + some additional topological cuts

Highest- $p_{\text{T}}$  top-jet serves as  $\hat{t}^{\text{had}}$

# Top quark width

## CMS first direct measurement at 13TeV

- Dilepton channel used: very small background contamination but small BR
- 2 categories: =1 or  $\geq 2$  b-tagged jets, boosted or non-boosted

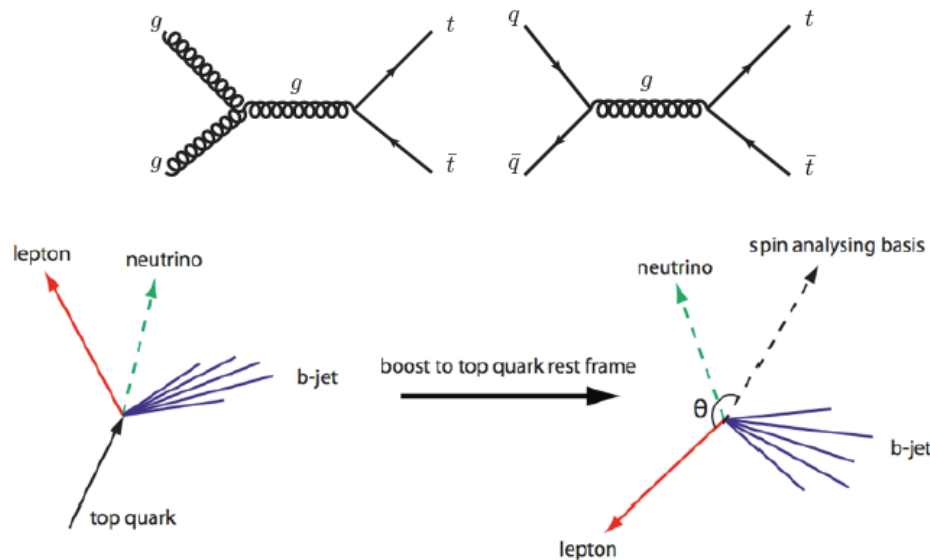


- Compare the SM expectation for different width scenarios to data.  
Measured bounds at 95% C.L.:  **$0.6 < \Gamma_t < 2.5 \text{ GeV}$**

- The most precise direct bound of the top quark width to date
- Systematically limited by MC modeling

# Top spin correlation

- Top quark decays before it hadronizes → spin information is transferred to the decay products
- Hadron colliders: top quarks produced un-polarized, but:
  - New physics (NP) could induce polarization
  - Spins of top and anti-top are slightly correlated due to QCD production mechanism
- Correlations depend on production mechanism:  
⇒ i.e. difference for gluon fusion vs quark annihilation
- Highest spin analysing power: leptons from top decay
- Use dileptonic events
- Unfolded differential measurements at parton level and particle level
- Full  $t\bar{t}$  event reconstruction



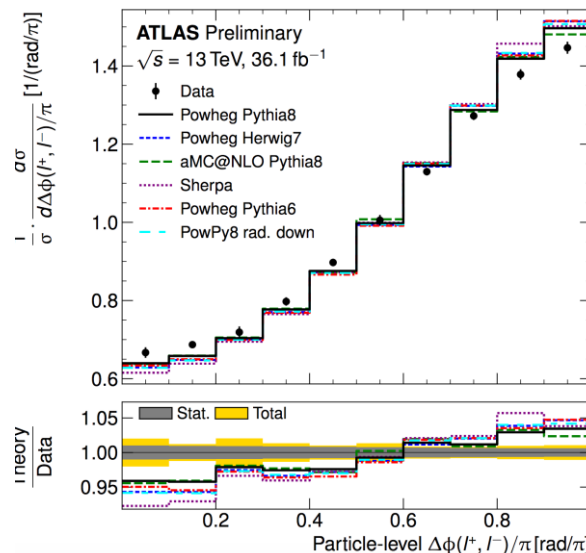
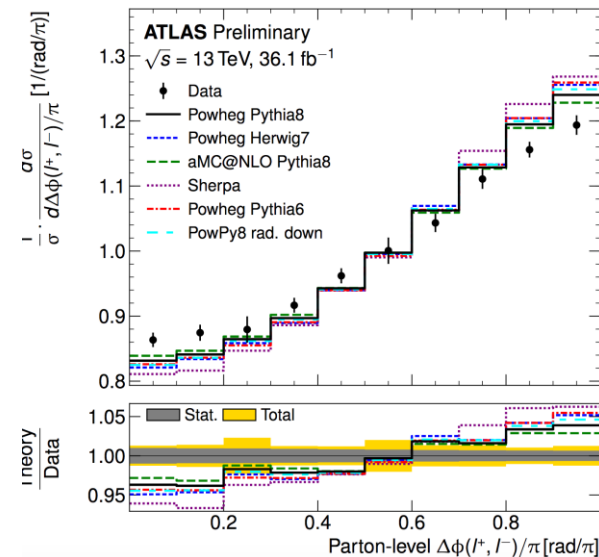


# Top spin correlation

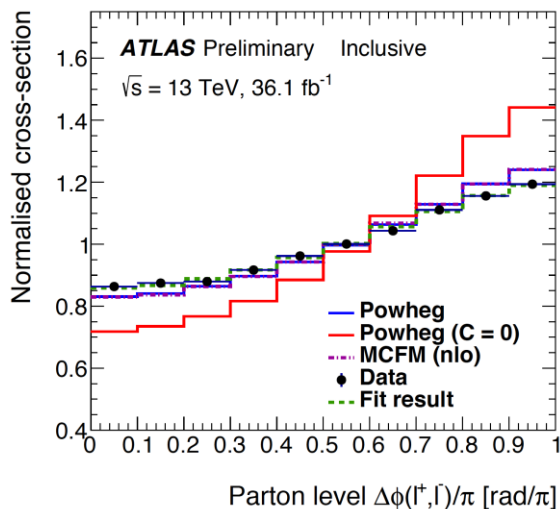
Unfolded distributions compared to different MC predictions:

ATLAS-CONF-2018-027

Data shows shallower slope than prediction



Fitting spin and no-spin hypotheses to parton-level distributions:

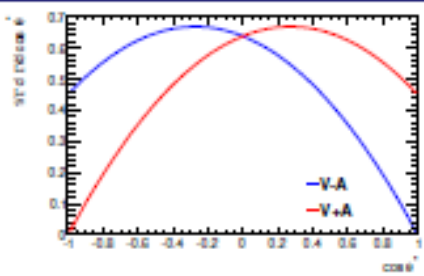


Region	$f_{\text{SM}}$	Significance (incl. theory uncertainties)
$m_{t\bar{t}} < 450 \text{ GeV}$	$1.11 \pm 0.04 \pm 0.13$	0.85 (0.84)
$450 < m_{t\bar{t}} < 550 \text{ GeV}$	$1.17 \pm 0.09 \pm 0.14$	1.00 (0.91)
$550 < m_{t\bar{t}} < 800 \text{ GeV}$	$1.60 \pm 0.24 \pm 0.35$	1.43 (1.37)
$m_{t\bar{t}} > 800 \text{ GeV}$	$2.2 \pm 1.8 \pm 2.3$	0.41 (0.40)
inclusive	$1.250 \pm 0.026 \pm 0.063$	3.70 (3.20)

Spin correlations higher than SM prediction by  $3.7 \sigma$   
 ( $3.2 \sigma$  including theory uncertainty)

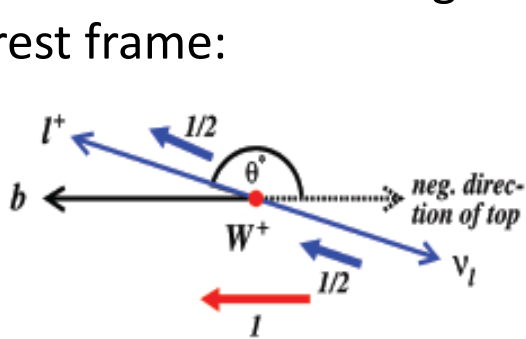
# Measurement of the W polarisation in top-quark decays

- W bosons from top-quark decays  $t \rightarrow Wb$  are polarised due to the V-A structure of the  $Wtb$  vertex

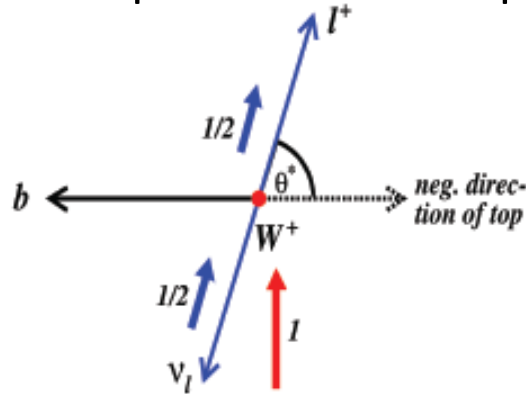


$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta^*} = \frac{3}{8} (1 - \cos \theta^*)^2 F_L + \frac{3}{4} \sin^2 \theta^* F_0 + \frac{3}{8} (1 + \cos \theta^*)^2 F_R$$

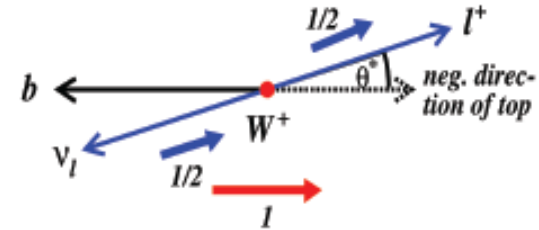
- The angle  $\theta^*$  between the “spin analyser” (charged lepton or down-type quark) and the reversed direction of flight of the b-quark from the top-quark decay in the W-boson rest frame:



$$\frac{dN(h_W = -1)}{d \cos \theta^*} \propto \frac{3}{8} (1 - \cos \theta^*)^2$$



$$\frac{dN(h_W = 0)}{d \cos \theta^*} \propto \frac{3}{4} (1 - \cos^2 \theta^*)$$



$$\frac{dN(h_W = +1)}{d \cos \theta^*} \propto \frac{3}{8} (1 + \cos \theta^*)^2$$

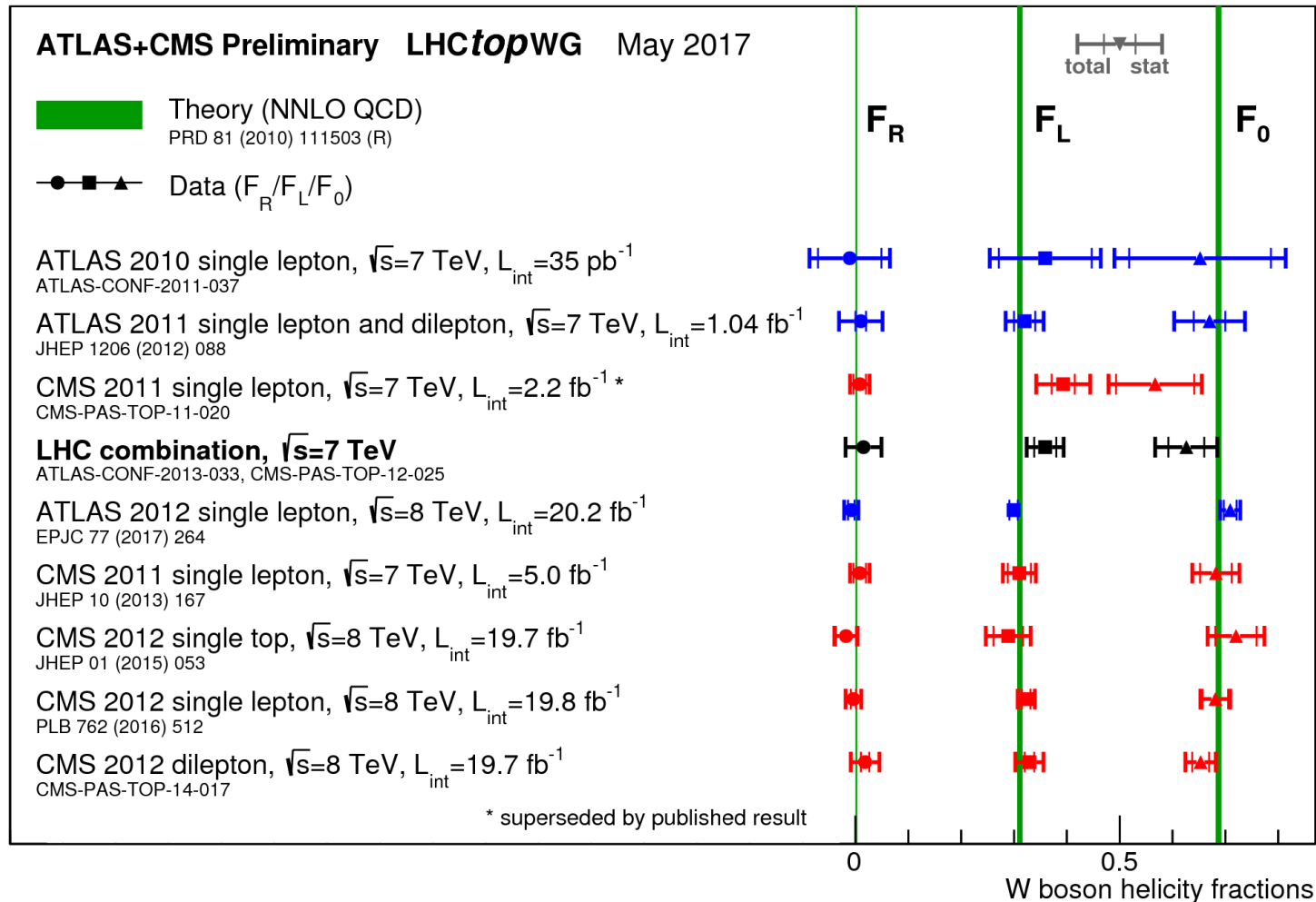
SM prediction (NNLO)  **$F_L = 0.311 \pm 0.005$**

**$F_0 = 0.687 \pm 0.005$**

**$F_R = 0.0017 \pm 0.0001$**

W-boson helicity fractions

# Measurement of the W polarisation in top-quark decays



Summary of the W boson helicity fraction measurements from ATLAS and CMS compared to the theory predictions. The uncertainty on the theory predictions is shown by the width of the green band.

# ttbar charge asymmetry

- NLO QCD predicts small ( $\sim 8\%$ ) asymmetry from qqbar  $\rightarrow$  ttbar, while gg remains symmetric ( $\rightarrow$  asymmetry DIFFERENT at Tevatron and LHC).  
Recent NNLO calculation predicts inclusive  $A_{\text{Tevatron}} \sim 9.5\%$  (arXiv:1411.3007)
- New physics can modify this asymmetry ( $Z'$ , axiguons,..)
- Experimentally, asymmetries based on fully reconstructed top using the rapidity difference ( $\Delta y$ ) of  $t \rightarrow l\nu b$  and antitop  $\bar{t} \rightarrow j\bar{j}b$  or using decay leptons

■ In terms of top-antitop rapidity difference:  $\longrightarrow$

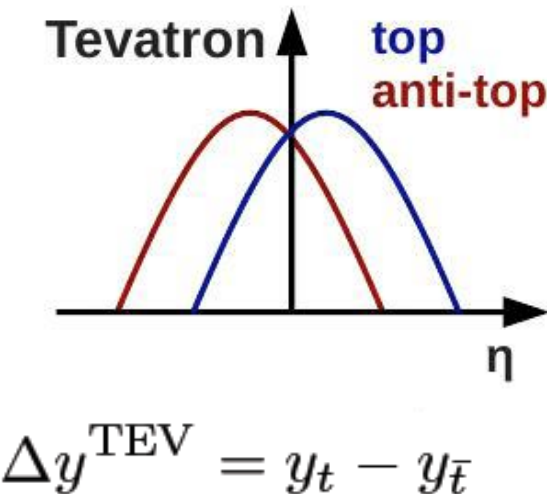
$$A_{\text{FB}}^{t\bar{t}} = \frac{N(\Delta y_{t\bar{t}} > 0) - N(\Delta y_{t\bar{t}} < 0)}{N(\Delta y_{t\bar{t}} > 0) + N(\Delta y_{t\bar{t}} < 0)}$$

■ In terms of rapidity of charged lepton from top decay:  $\longrightarrow$

$$A_{\text{FB}}^{\ell} = \frac{N(q_e \eta_e > 0) - N(q_e \eta_e < 0)}{N(q_e \eta_e > 0) + N(q_e \eta_e < 0)}$$

■ For dilepton channel in terms of  $\Delta \eta$  between  $l^+$  and  $l^-$   $\longrightarrow$

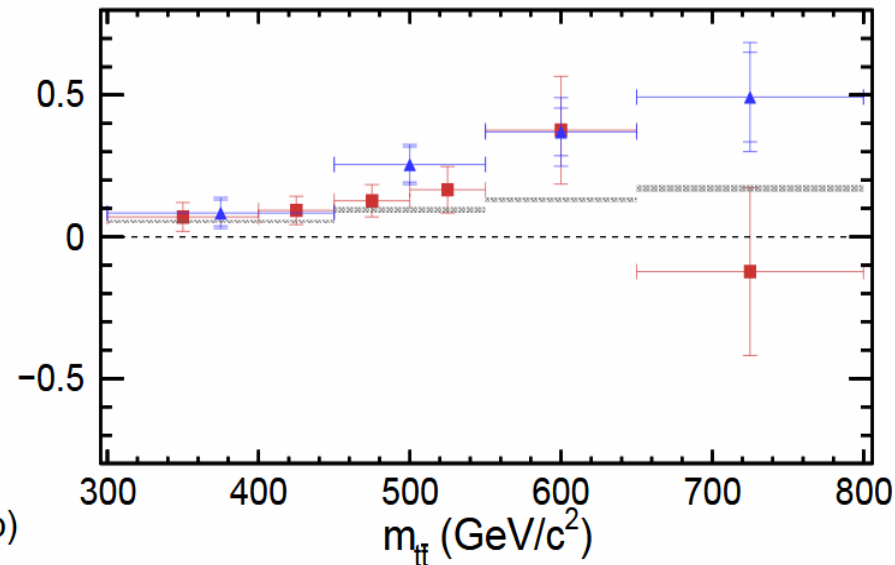
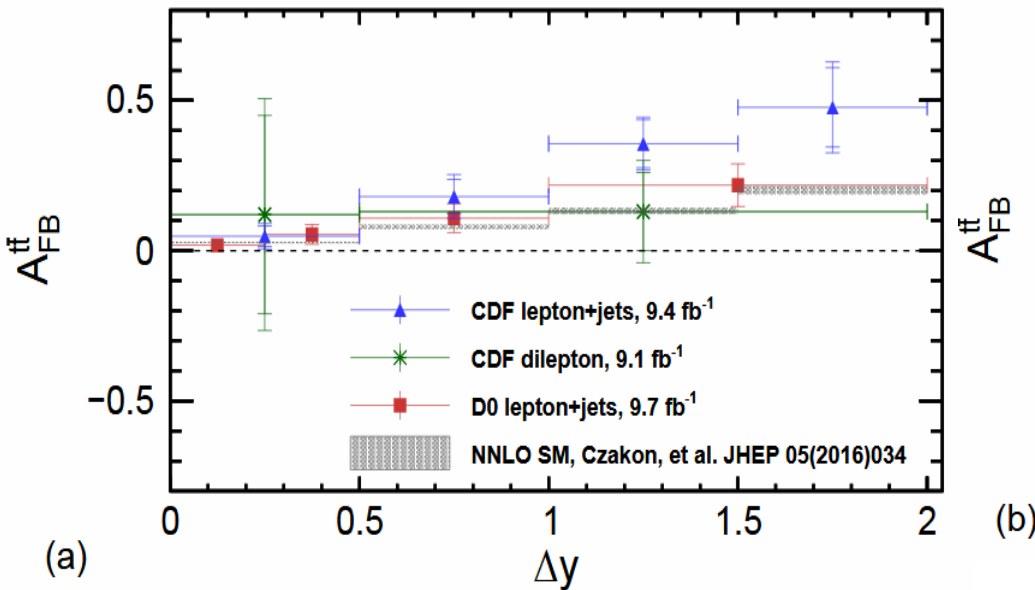
$$A_{\text{FB}}^{\ell\ell} = \frac{N(\Delta \eta > 0) - N(\Delta \eta < 0)}{N(\Delta \eta > 0) + N(\Delta \eta < 0)}$$



# Forward backward asymmetry ( $A_{FB}^{t\bar{t}}$ )

Lepton + jets and dilepton channels:

- Check rapidity and mass kinematic dependence of asymmetry

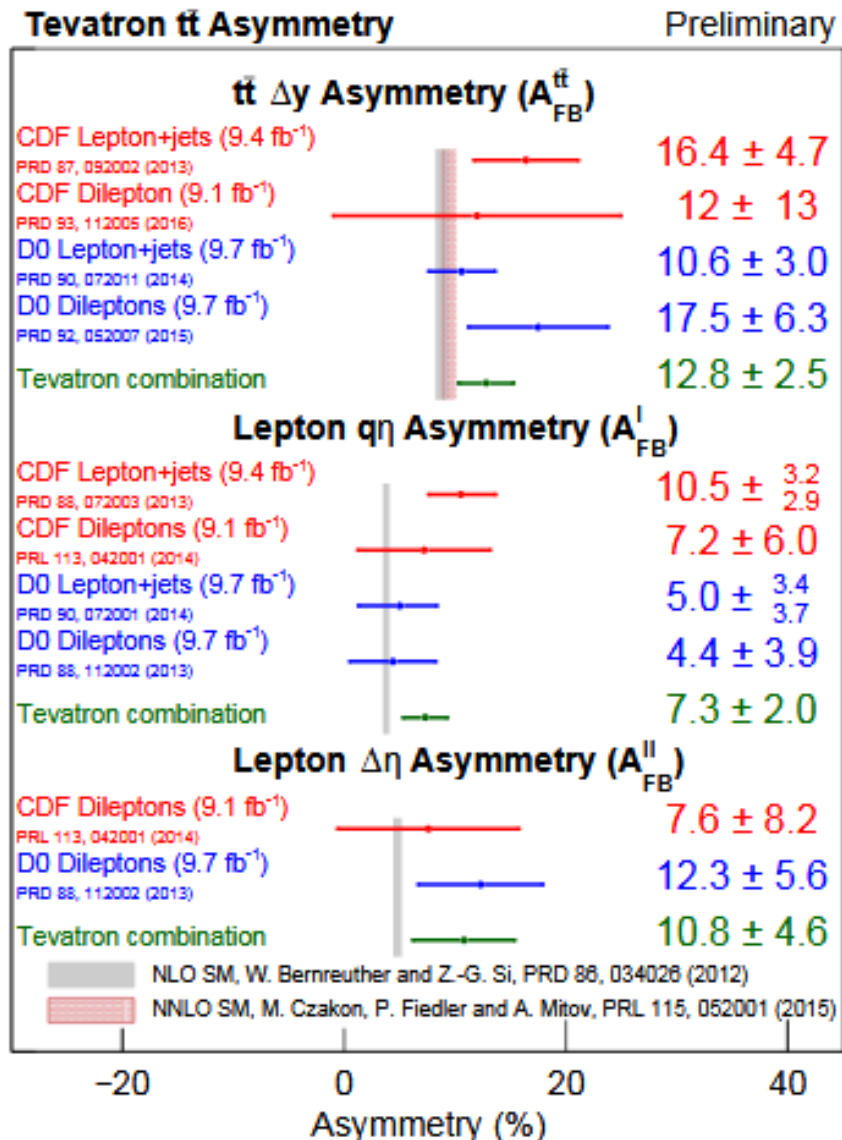
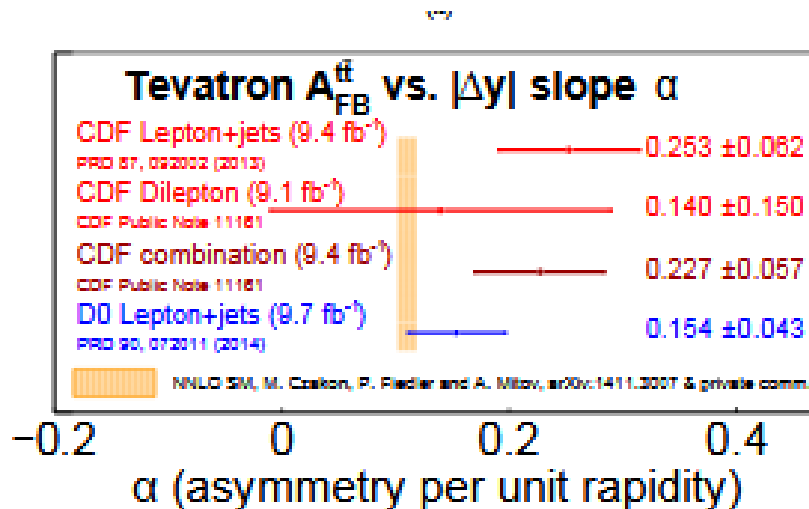


- Kinematic dependencies in CDF data slightly larger than predicted by SM at both NLO and NNLO ( $\sim 2$  s.d. effect)
- Overall NNLO predicted asymmetry;  $9.5 \pm 0.7 \%$

M. Czakon, P. Fiedler and A. Mitov arXiv:1411.3007

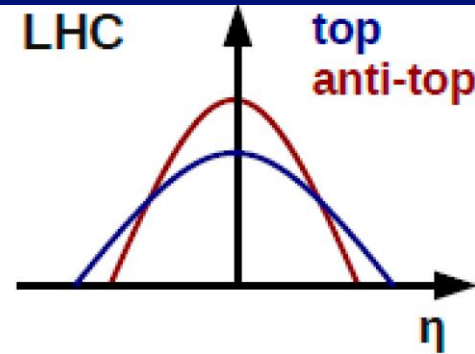
# Summary of top asymmetries at Tevatron

- $t\bar{t}$ -based and lepton-based results using full RunII dataset
- The measurements are in agreement with the existing predictions of the SM



# ATLAS charge asymmetry in dilepton

Asymmetries expected from valence quark – sea antiquark fusion → antitop more central than top



Leptonic asymmetries:

$$A_C^{\ell\ell} = \frac{N(\Delta|\eta| > 0) - N(\Delta|\eta| < 0)}{N(\Delta|\eta| > 0) + N(\Delta|\eta| < 0)}, \quad \Delta|\eta| = |\eta_{e^+}| - |\eta_{e^-}|$$

$t\bar{t}$  asymmetries:

$$A_C^{t\bar{t}} = \frac{N(\Delta|y| > 0) - N(\Delta|y| < 0)}{N(\Delta|y| > 0) + N(\Delta|y| < 0)}, \quad \Delta|y| = |y_t| - |y_{\bar{t}}|$$

■ 3 different measurements of both observables:

⇒ inclusive measurements on parton level in the full phase space

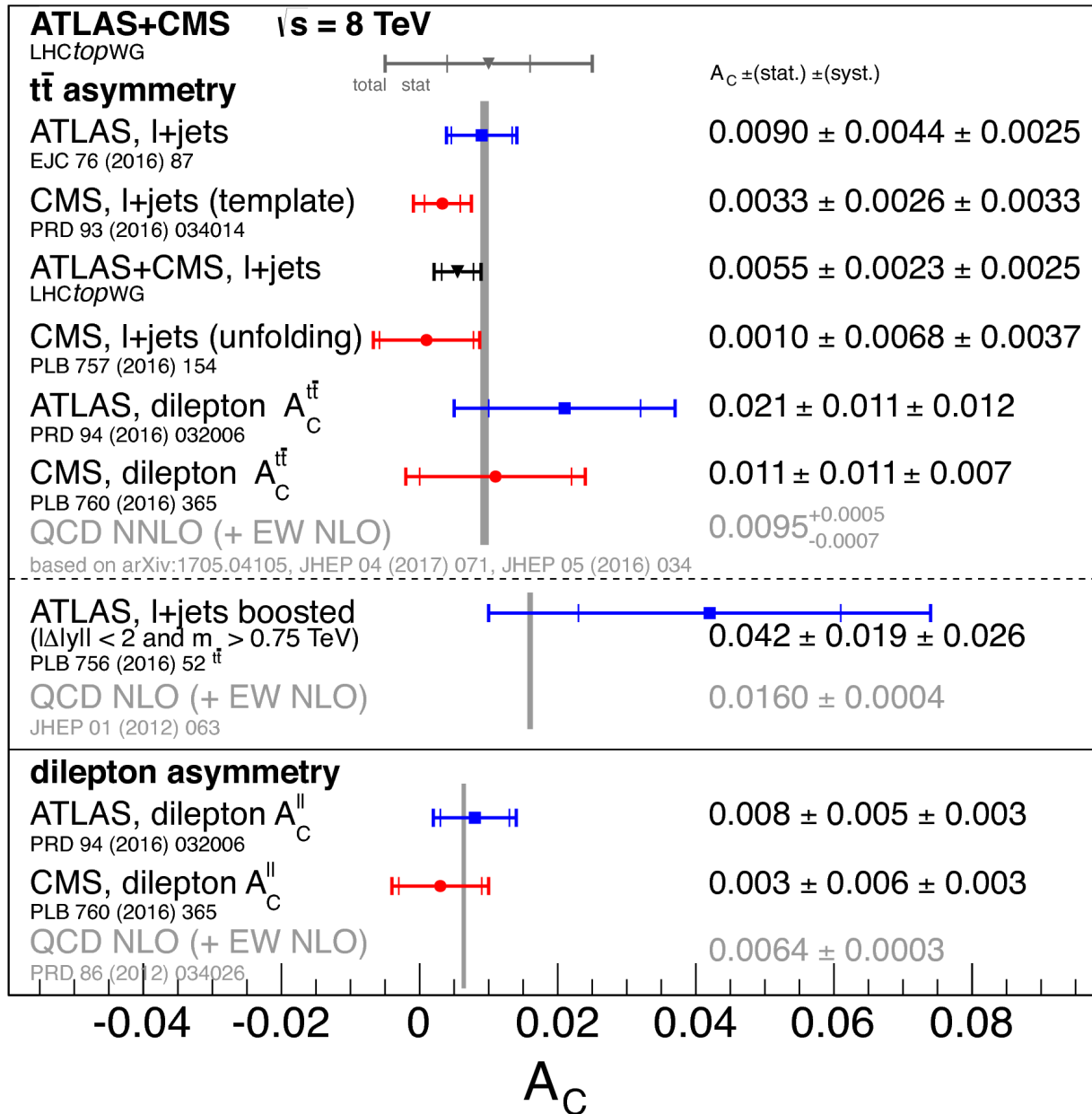
⇒ inclusive measurements on particle level in the fiducial region

⇒ differential measurements:

inv. Mass,  $p_T$  ( $m_{t\bar{t}}$ ),  $p_{T,t\bar{t}}$  and longitudinal boost ( $\beta_{z,t\bar{t}}$ ) of  $t\bar{t}$  system in the fiducial regions and the full phase space



# ATLAS and CMS charge asymmetry



# Summary

- Despite being discovered more than 20 years ago, there are still many intriguing things to learn about the top quark
- LHC is a top factory
  - ⇒ Can make precision measurements on:
    - Production, decay and properties
    - Mass as a fundamental parameter of the SM
  - ⇒ Investigate kinematics of events
    - Constrain ‘empirical’ models in MC generators and in PDFs
    - Look at agreement with NLO and NNLO predictions
- Top may show us the way to narrowing down BSM physics

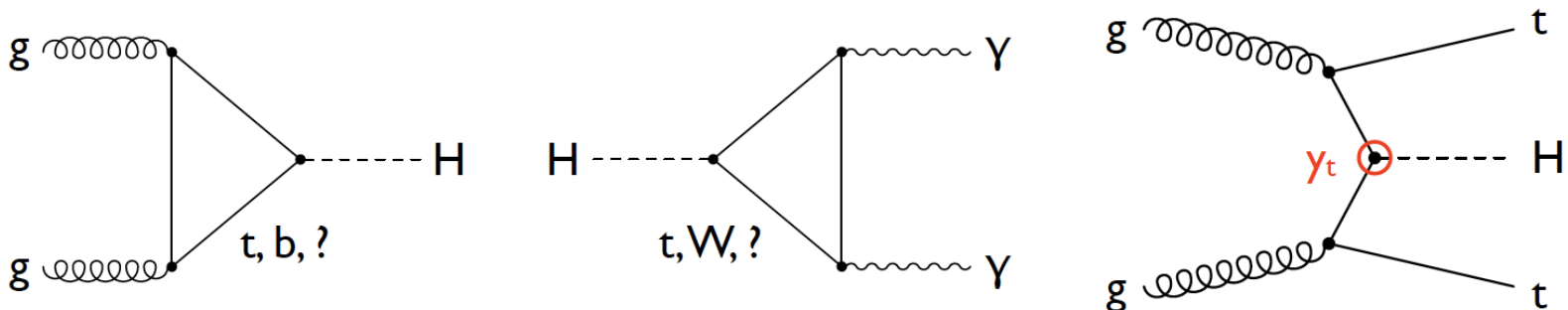
<https://twiki.cern.ch/twiki/bin/view/AtlasPublic/TopPublicResults>

<https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsTOP>

# Backup

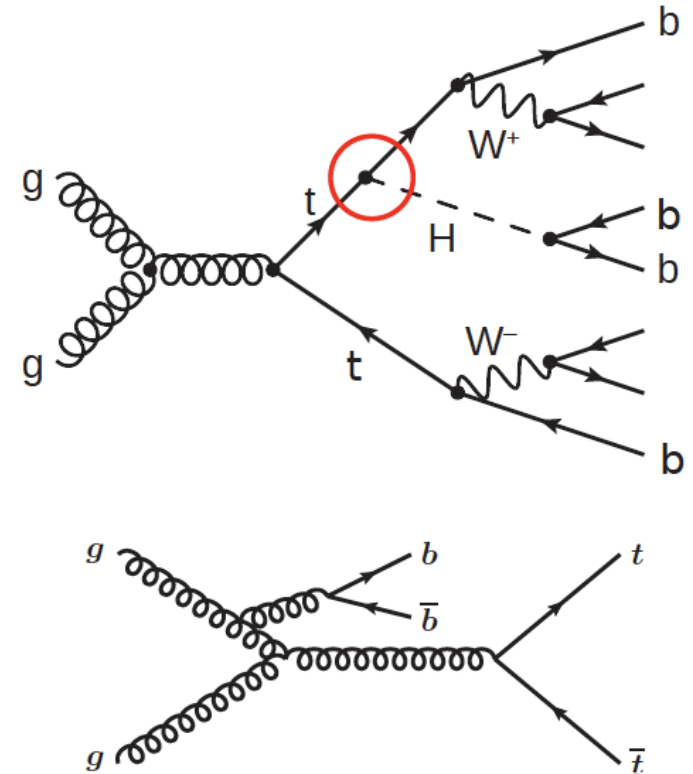
# Observation of ttH

- Best direct probe of the top-Higgs Yukawa coupling, vital step towards verifying the SM nature of the Higgs boson
  - Top quark is the most strongly-coupled SM fermion ( $y_t \sim 1$ )
  - Direct measurement of  $y_t$  in ttH production:
    - gluon-gluon fusion: assumes no BSM coupling
    - Allows probing new physics in  $gg \rightarrow H$  and  $H \rightarrow \gamma\gamma$  effective vertices
- Top quark x Higgs decay channels
- Challenges: ttH  $\sim 0.5$  pb, ttbar = 830 pb @13 TeV
  - Crucial to understand tt+X (X = b-bbar, W, Z)
  - Large combinatorics of leptons and jets from top quark decays
- Exploiting all ttbar decay channels and Higgs decays to:
  - **bottom quarks**  $\rightarrow$  large BR, large background contributions
  - **W, Z bosons, taus**  $\rightarrow$  smaller production rate, lower backgrounds
  - **photons**  $\rightarrow$  clean final state, very small rate



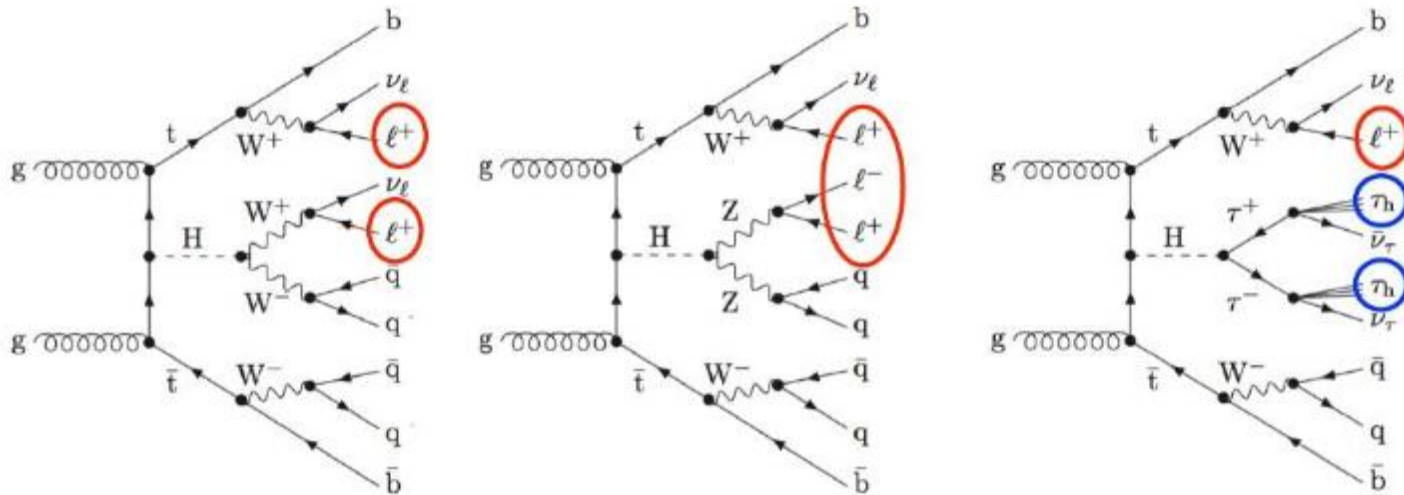
# ttH (b-bbar) production

- Large  $B(H \rightarrow bb)$ , access to coupling 3<sup>rd</sup> generation quarks
- Challenging final state:
  - Huge combinatorics in event reconstruction
  - Poor  $H \rightarrow b\text{-}b\text{bar}$  mass resolution
  - Large  $t\bar{t} + b\bar{b}$  background of  $O(10)\text{pb}$  with associated large theory uncertainties: from simulation
- Search channels:
  - Leptonic  $t\bar{t}b\bar{b}$  : higher purity
  - Fully-hadronic  $t\bar{t}b\bar{b}$  : higher rate



# ttH multilepton

- Multilepton final states: Higgs decay to  $W^+W^-$ ,  $ZZ$ , and  $\tau\tau$
- Events categorised based on number of leptons and  $\tau_h$  candidates
- 1 lepton + 2  $\tau_h$ , 2 same-sign leptons + 0, 1  $\tau_h$ , 3 leptons + 0, 1  $\tau_h$ , 4 leptons
- Additional requirements on jets, b-tagged jets
- Major backgrounds:
  - Irreducible:  $t\bar{t} + V$  and diboson, predicted from simulation and control regions
  - Reducible: non-prompt leptons in  $t\bar{t} + \text{jets}$  events, estimated from data
  - Large  $t\bar{t} + \text{fake } \tau_h$  for 1 lepton + 2  $\tau_h$
- BDT and MEM discriminants to separate signal from backgrounds

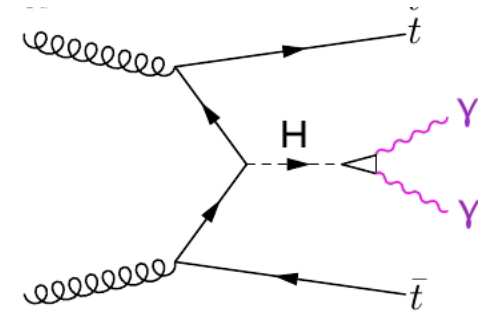


# $ttH \rightarrow ZZ^* \rightarrow 4 \text{ leptons}$

# $ttH (\gamma\gamma)$

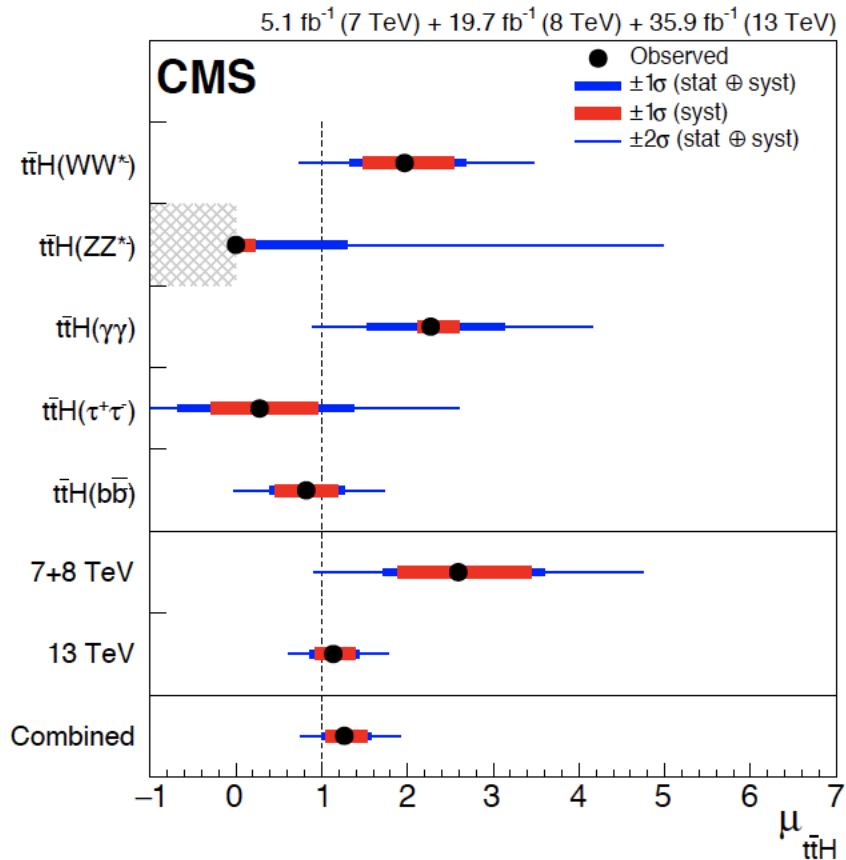
- Analysis with full 2017 dataset
- Very clean final state, but tiny branching fraction
- Dedicated ttH channel part of the global  $H \rightarrow ZZ$  analysis
- ttbar hadronic and leptonic channels
  - $\geq 4$  jets,  $\geq 1$  b-tagged jet and additional 0/1 leptons
- Combined fit (relying on  $m_{4\text{leptons}}$  and a kinematic discriminant) with analysis of 2016 data

- Clear signature coming from the photons
- Higgs boson can be reconstructed as a narrow peak
- Dedicated ttH channel part of the global  $H \rightarrow \gamma\gamma$  analysis
- ttbar hadronic and leptonic channels
- Signal extracted from fit to  $m_{\gamma\gamma}$





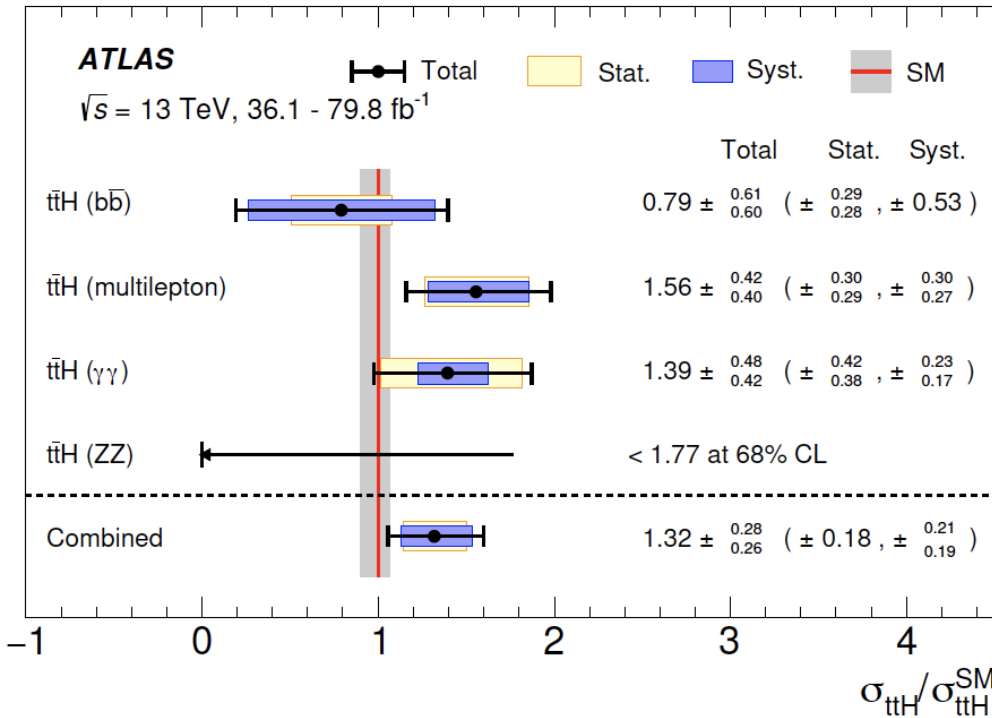
# First observation of $t\bar{t}H$ (CMS)



$$\mu_{t\bar{t}H} = 1.26^{+0.31}_{-0.26} = 1.26^{+0.16}_{-0.16}(\text{stat})^{+0.17}_{-0.15}(\text{expt})^{+0.14}_{-0.13}(\text{Th. bkg})^{+0.15}_{-0.07}(\text{Th. sig})$$

Observed significance is  $5.2\sigma$  ( $4.2\sigma$  exp.)

# First observation of $t\bar{t}H$ (ATLAS)



Significance

Obs. (Exp.)

$1.4\sigma$  ( $1.6\sigma$ )

$4.1\sigma$  ( $2.8\sigma$ )

$4.1\sigma$  ( $3.7\sigma$ )

$0\sigma$  ( $1.2\sigma$ )

**$5.8\sigma$  ( $4.9\sigma$ )**

13 TeV only

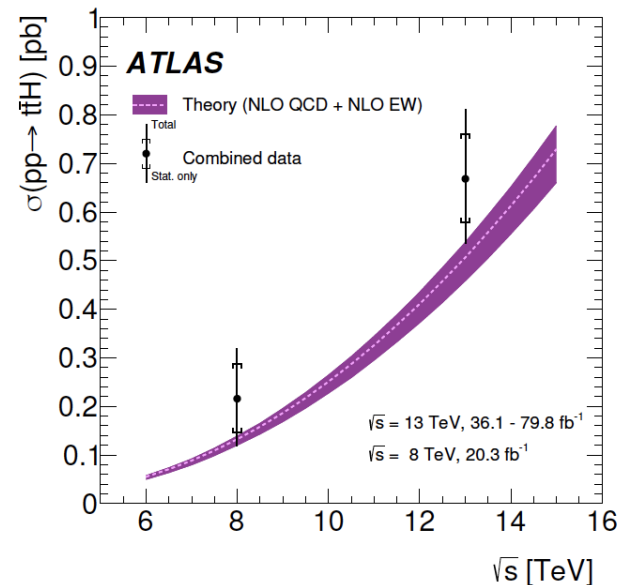
**Observation of  $t\bar{t}H$  production!**

**$6.3\sigma$  ( $5.1\sigma$ )**

7, 8, and 13 TeV

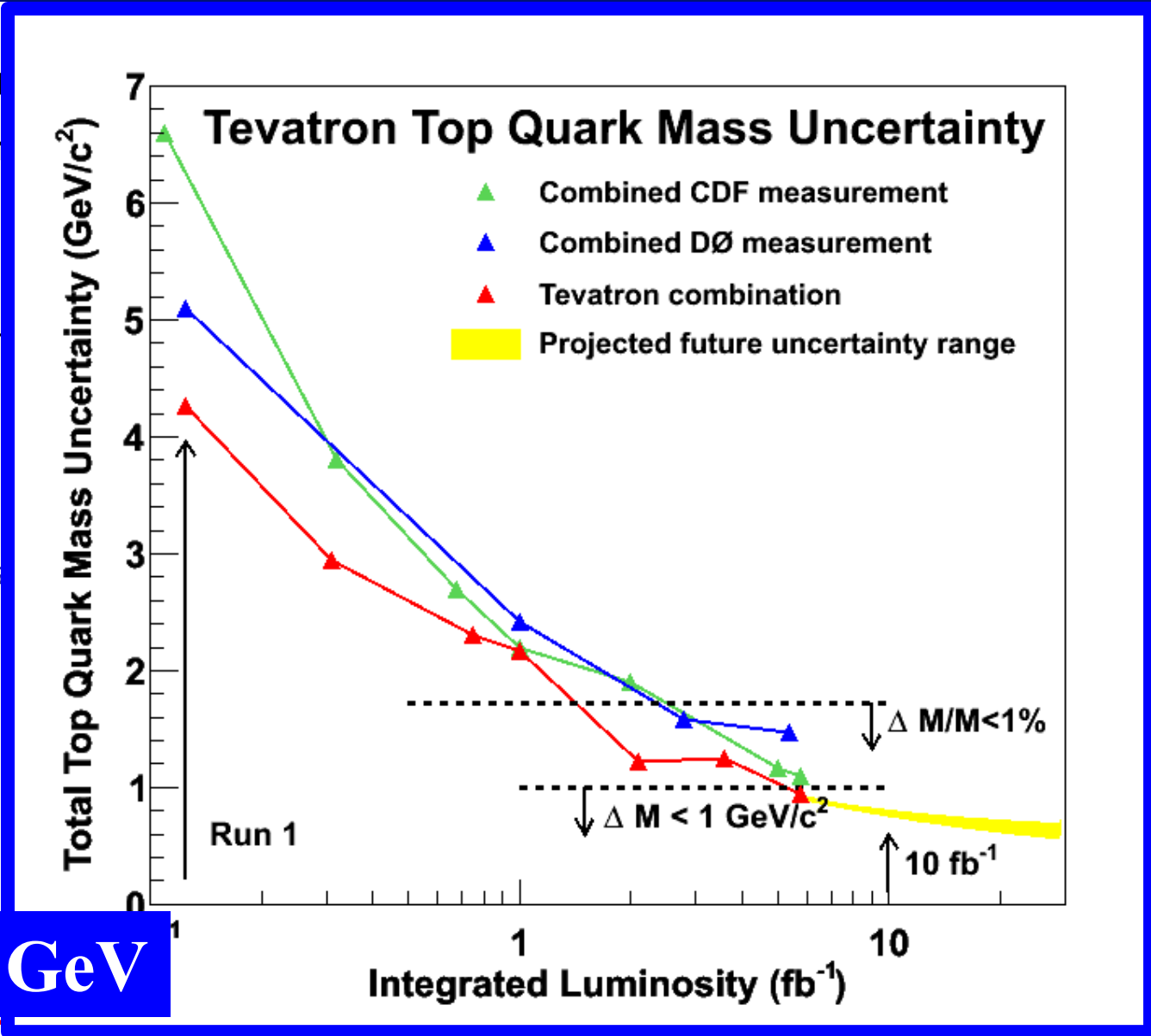
Cross section for  $pp \rightarrow t\bar{t}H$  is extracted assuming SM branching ratios.

Analysis	$t\bar{t}H$ cross section [fb]
$H \rightarrow \gamma\gamma$	$710_{-190}^{+210}$ (stat.) $_{-90}^{+120}$ (syst.)
$H \rightarrow \text{multilepton}$	$790 \pm 150$ (stat.) $_{-140}^{+150}$ (syst.)
$H \rightarrow b\bar{b}$	$400_{-140}^{+150}$ (stat.) $\pm 270$ (syst.)
$H \rightarrow ZZ^* \rightarrow 4\ell$	$< 900$ (68% CL)



# Tevatron top mass combination

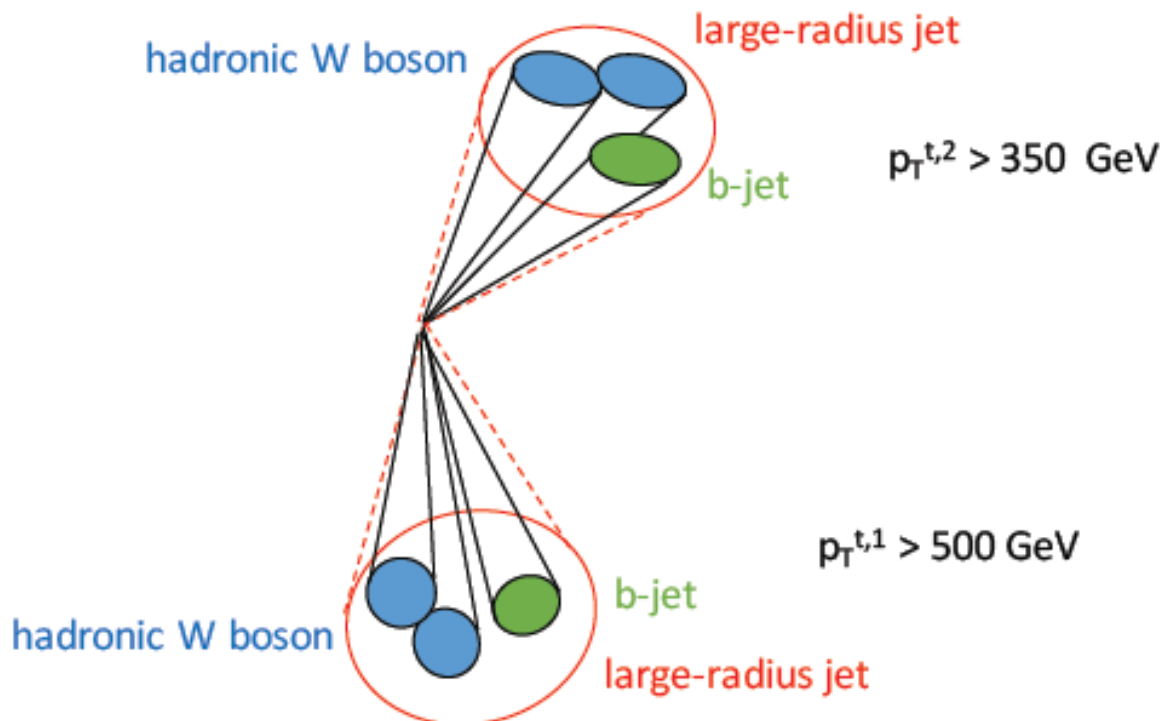
- 5 Run I and 7 Run II
- Combination performed
- Limited by systematic
  - ⇒ Dominant: signal
  - uncertainties
- Total uncertainty  $\pm$ 
  - (better than world comb. M)



**goal was <1 GeV**

# Boosted differential cross section in all had

- All hadronic channel with boosted top quark
- Use  $14.7 \text{ fb}^{-1}$  of 2015 and 2016 data at  $\sqrt{s} = 13 \text{ TeV}$



## all-hadronic boosted

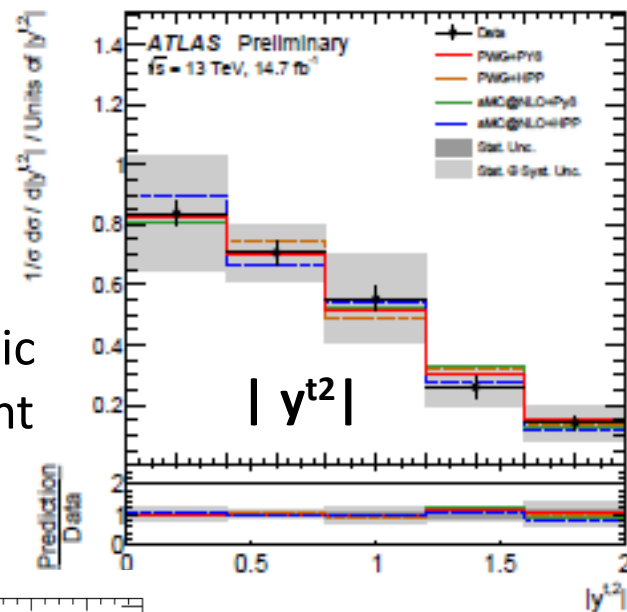
- ▶ highest BR  $\rightarrow$  large statistics
- ▶ high QCD multijet background
- ▶ top-tagged jets can be used directly as top-quark proxies
- ▶ boosted topologies allow to reach higher in top  $p_T$
- ▶ more precise  $t\bar{t}$  reconstruction thanks to the lack of neutrinos

### Event selection:

0 leptons,  $\geq 2$  top-tagged large-R jets, each containing a b-jet

# Boosted differential cross section in all had

- Use 12 observable of top quarks and  $t\bar{t}$  system
- Most important uncertainties:
  - ⇒ large-R jet calibration and reconstruction
  - ⇒  $t\bar{t}$  MC modelling
  - ⇒ b-tagging
- All generators provide good agreement in wide kinematic range, but each one shows local disagreements in different parts of the phase-space ⇒ must further improve the generators and the tuning.



No deviations seen in top rapidity

