



AC losses quantification in Nb₃Sn magnets

H. Bajas



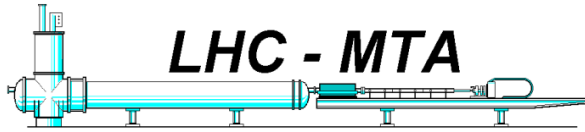
2nd International Workshop on Superconducting Magnet Tests Stands

Outline

- Origin of the AC loss
- Measurement technique
- Experimental result
- Simulation result

References

LHC-MTA-IN-2000-131
2000-10-17



Energy loss and field advance in MBP2O1 prototype magnet at different ramp rates

A. Akhmetov, Z. Ang, I. Balaazi, L. Bottura, M. Gateau, P. Pognat, L. Walckiers / LHC-MTA

Keywords: Dipole magnet, Energy loss, Field advance, Interstrand resistance

Distribution: LHC-MTA Scientific Staff; LHC-MMS distribution list; N. Siegel / LHC-ICP;
L. Evans / DG-DI; Ph. Lebrun, T. Taylor / LHC

MTA-IN-2002-208
November 18, 2002



Analysis program LMA – Loss Measurement Analysis.

N. Ponomarev, F. Patru, L. Denia, L. Bottura, LHC/MTA

Keywords: Magnet test, field measurement analysis, loss measurement analysis, inductance, LMA library

Distribution: MTA Group

Origin of AC losses

- There are 3 main sources of loss when a transport current is ramped in a superconducting magnet.
 - **Hysteretic magnetization loss** (i.e. flux flow combined with flux pinning, results in a net energy loss when subjected to a field cycle)
 - Proportional to the superconductor J_c and filament size (D_{eff})
 - **Inter-strand coupling loss (ISCC)** and **Inter-filament coupling losses (IFCC)**
 - Combination of individual superconducting filaments and a separating normal-metal matrix results in a coupling Joule loss
 - Low thanks to the use of cored cable
 - Low at the typical ramp-rate of an accelerator as LHC/FCC (10 A/s)
 - **Eddy currents** in normal-metal
 - Iron yoke and saturation effect

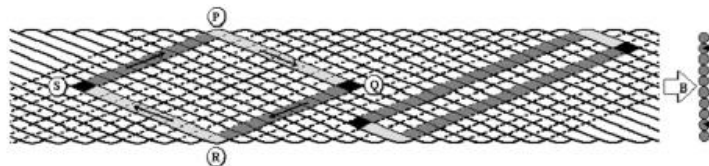
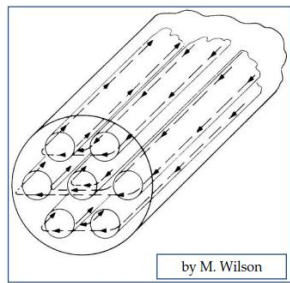
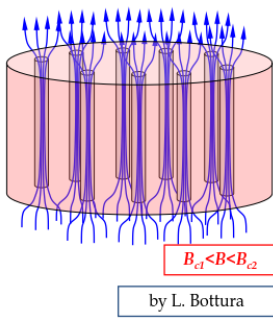
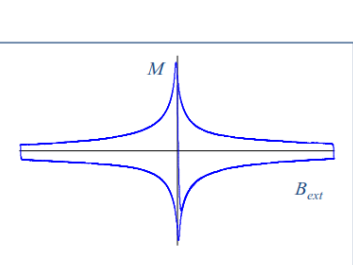
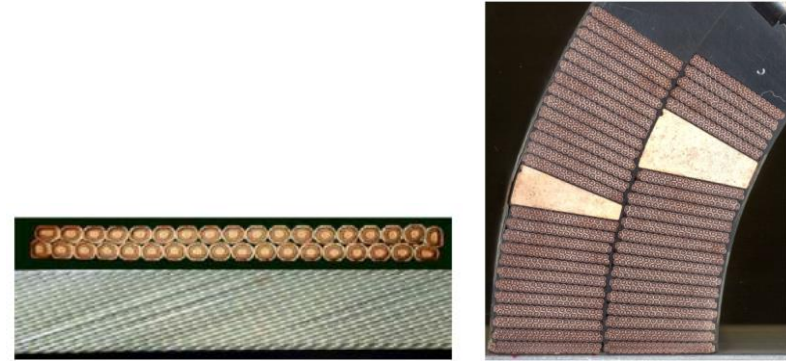


Fig. 19. Coupling currents flowing via crossover resistance R_c in transverse field (upper wires shown light grey).

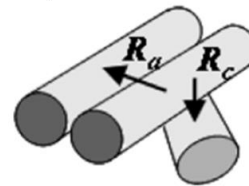
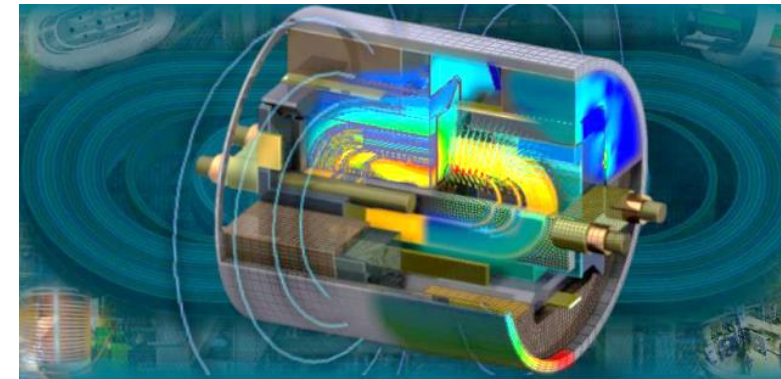


Fig. 18. Crossover resistance R_c and adjacent resistance R_a .



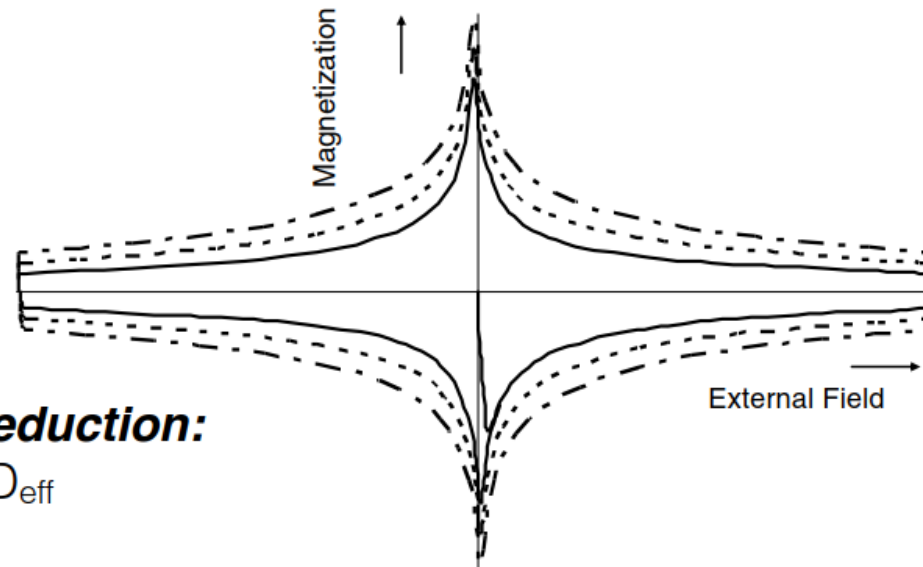
Origin of AC loss

First estimate of AC losses: Hysteresis losses

$$Q_{cyc} = \int_0^{t_0} J_c(B) \frac{2D_{eff}}{3\pi} \frac{dB}{dt} dt \quad [\text{J/m}^3, \text{ per cycle}]$$

$$Q_{hyst-tot} = Q_{cyc} * V_{sc} \quad [\text{J, per cycle}]$$

This has motivated the quest for fine filament wire!



Hysteresis loss reduction:

- minimize D_{eff}

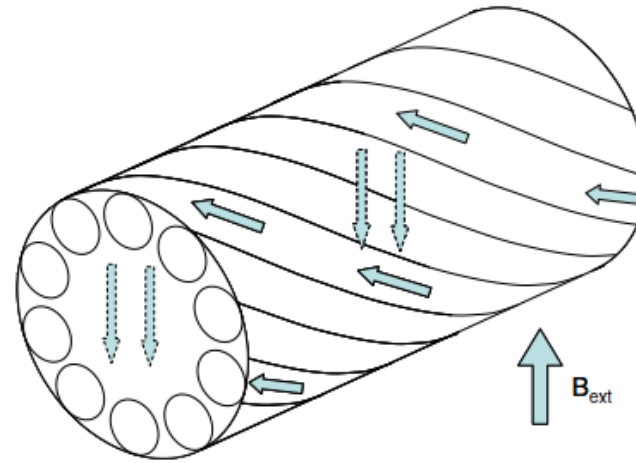
Origin of AC loss

First estimate of AC losses: Coupling losses

$$\tau = \frac{\mu_0}{2\rho_t} \left(\frac{p}{2\pi} \right)^2 \quad Q_{coupling} = \frac{(dB/dt)^2}{\mu_0} 2\tau \quad [\text{W/m}^3]$$

$$Q_{coupling-tot} = Q_{coupling} * V_{cond}$$

Coupling loss reduction:
- minimize twist pitch



AC losses measurement

- ❑ Measurement issues in superconducting magnet
 - ❑ The AC losses are delicate measurements as one has to detect *Joules* (resistive) over *hundreds of kJ* (inductive voltage).
 - ❑ It requires **High Resolution/precision Digital MultiMeters** (DMM 1 $\mu\text{V} \pm 0.01\%$).
 - ❑ Measurement requires to perform a great number of cycles at different ramp rate and level of current. Those are time-consuming measurements that are not systematically done.
 - ❑ Need a performant framework for **automatic analysis** over 10th of file, 100th of cycle, 10th of voltages.

Measurement Procedure (hardware)

- Measurement of the voltage across the coil using the voltage taps signals acquired with high precision high resolution DMM
- Measurement of the the transport current using DCCT signals
- Numerical integration of the power over current ramp cycle.

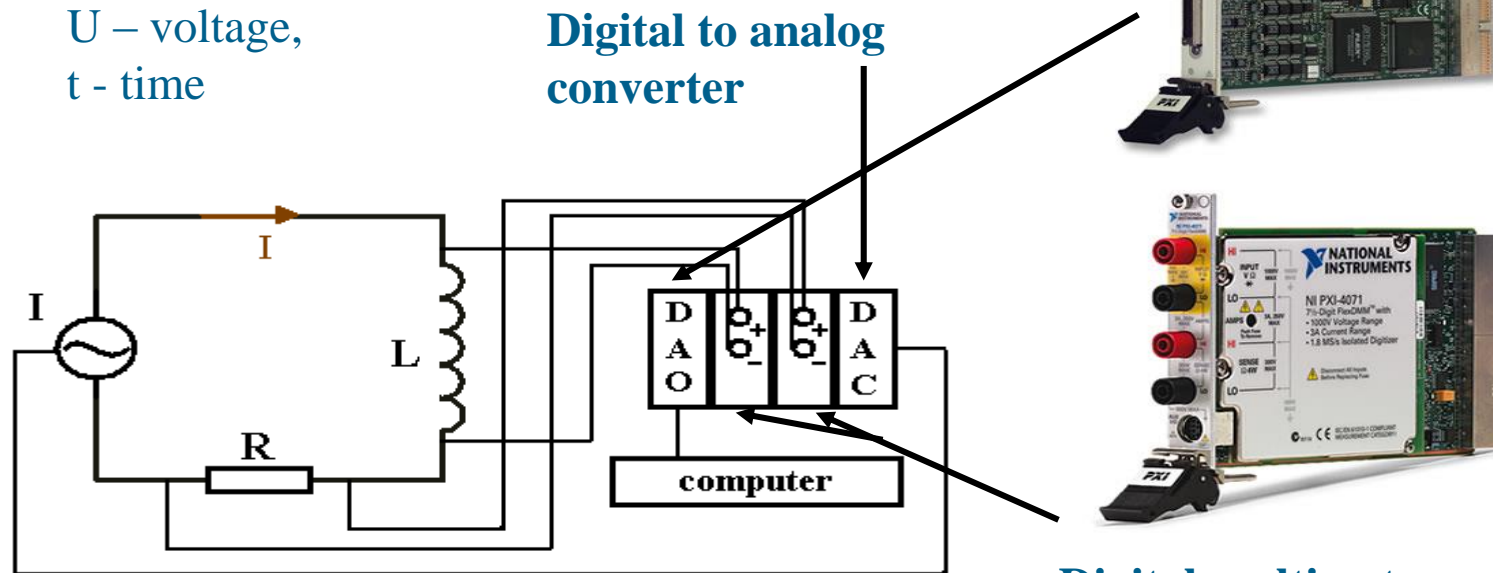
$$W = \int I \cdot U dt$$

W – energy loss

I – current,

U – voltage,

t - time



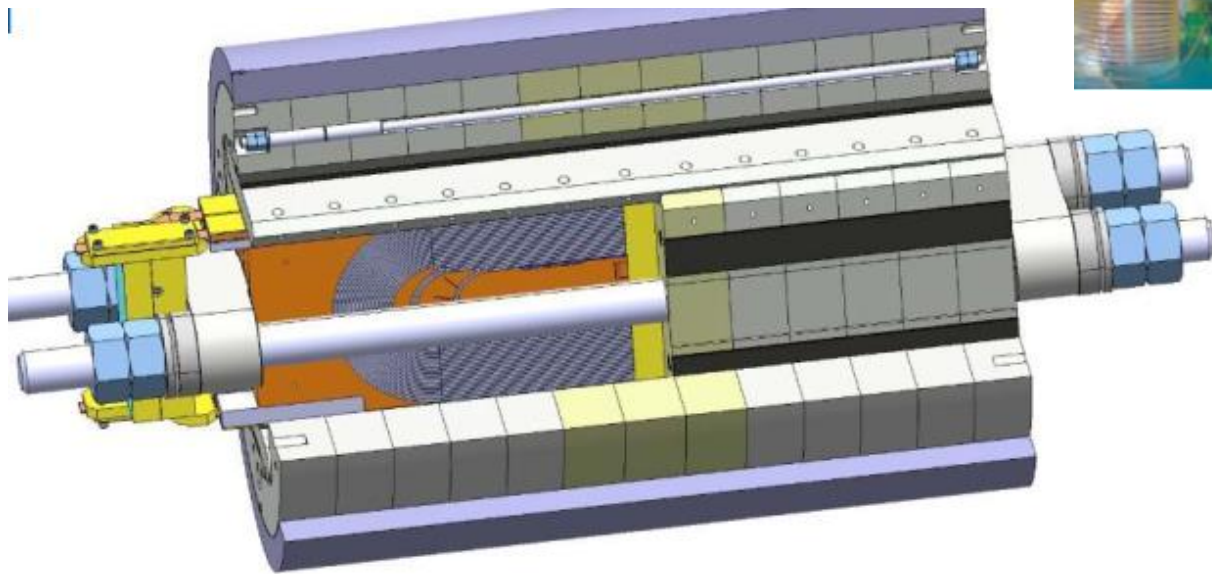
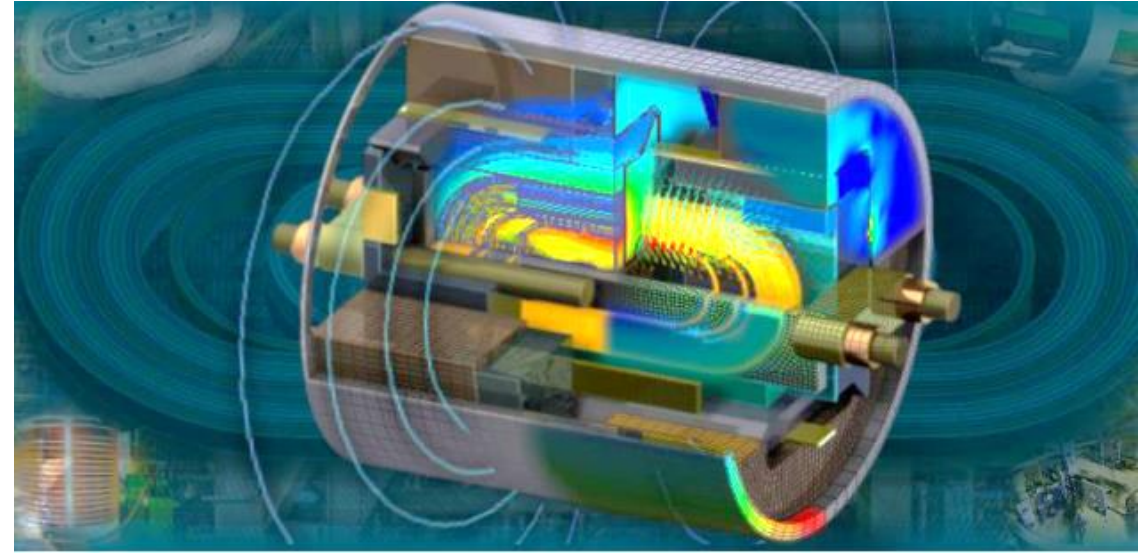
Digital analog output



Digital multimeter



Measurement Procedure (example on SMC11T)



Measurement Procedure (example on SMC11T)

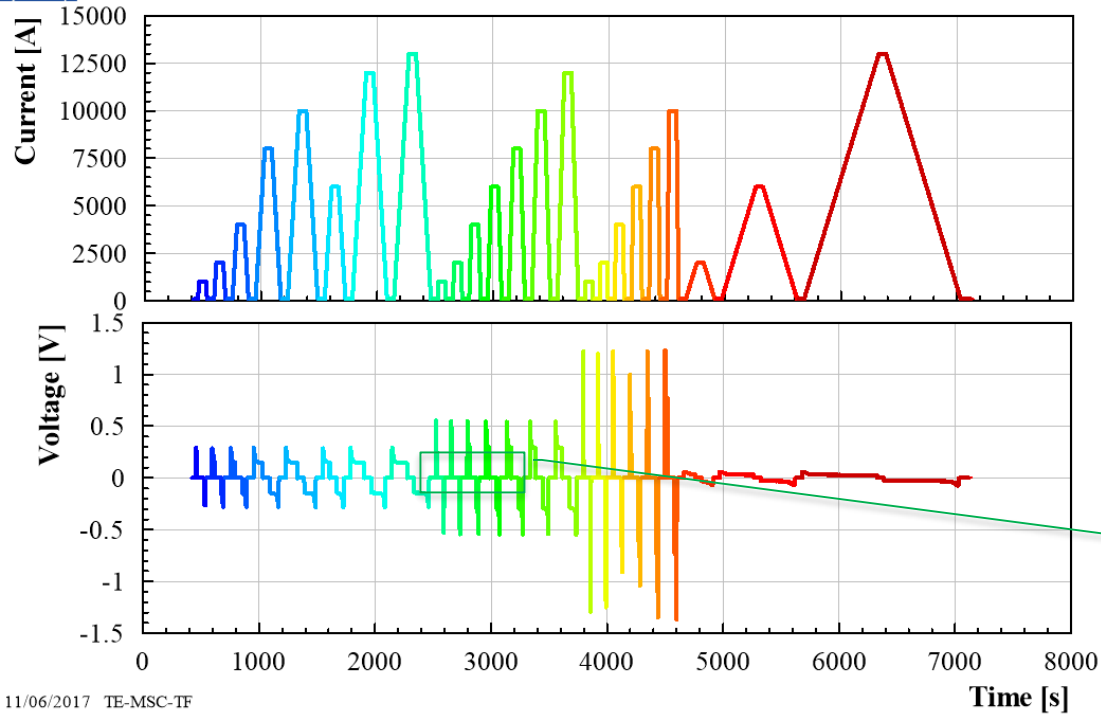
Current cycle between two level of current
@ different ramp rates



File: HCLMSMC003_00000101_Loss_4.2K_2015_07_23-09_24_18_dmm

AC Loss Measurement

Data Plateau



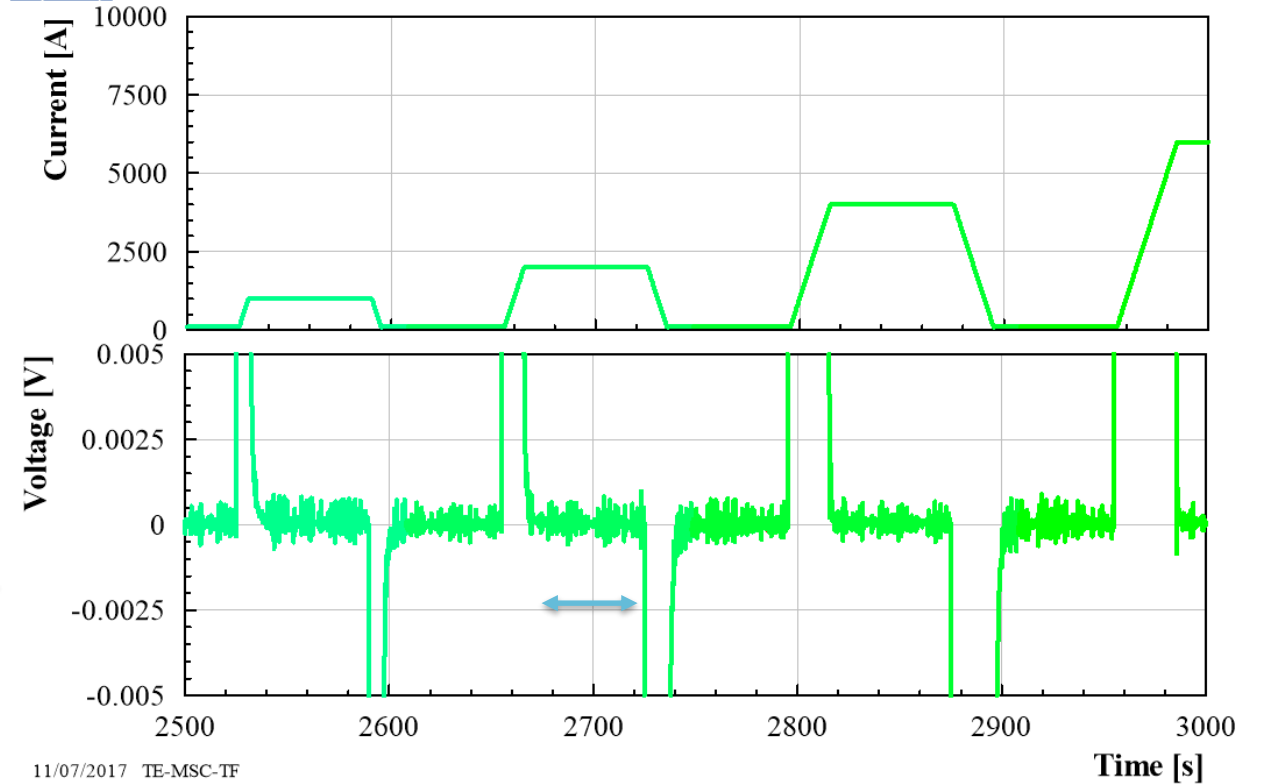
11/06/2017 TE-MSC-IF



File: HCLMSMC003_00000101_Loss_4.2K_2015_07_23-09_24_18_dmm.csv_test

AC Loss Measurement

Data Plateau



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Measurement Procedure (example on SMC11T)

Current cycle between two level of current
@ different ramp rates

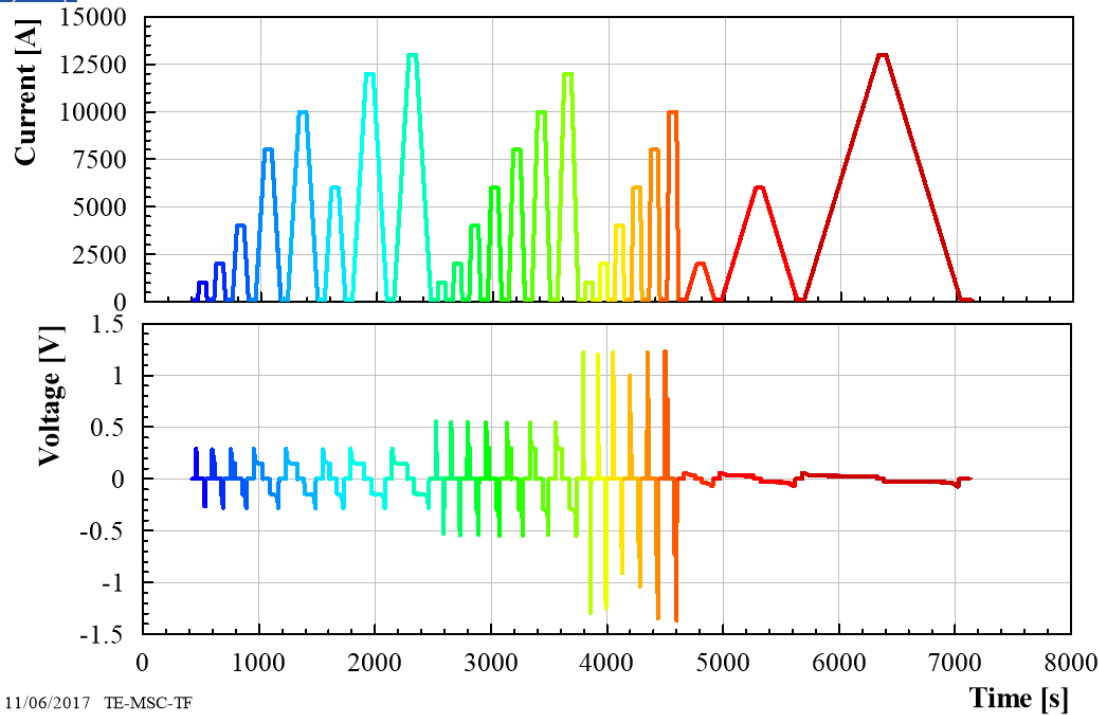
$$P = U \cdot I$$



File: HCLMSMC03_00000101_Loss_4.2K_2015_07_23-09_24_18_dmm

AC Loss Measurement

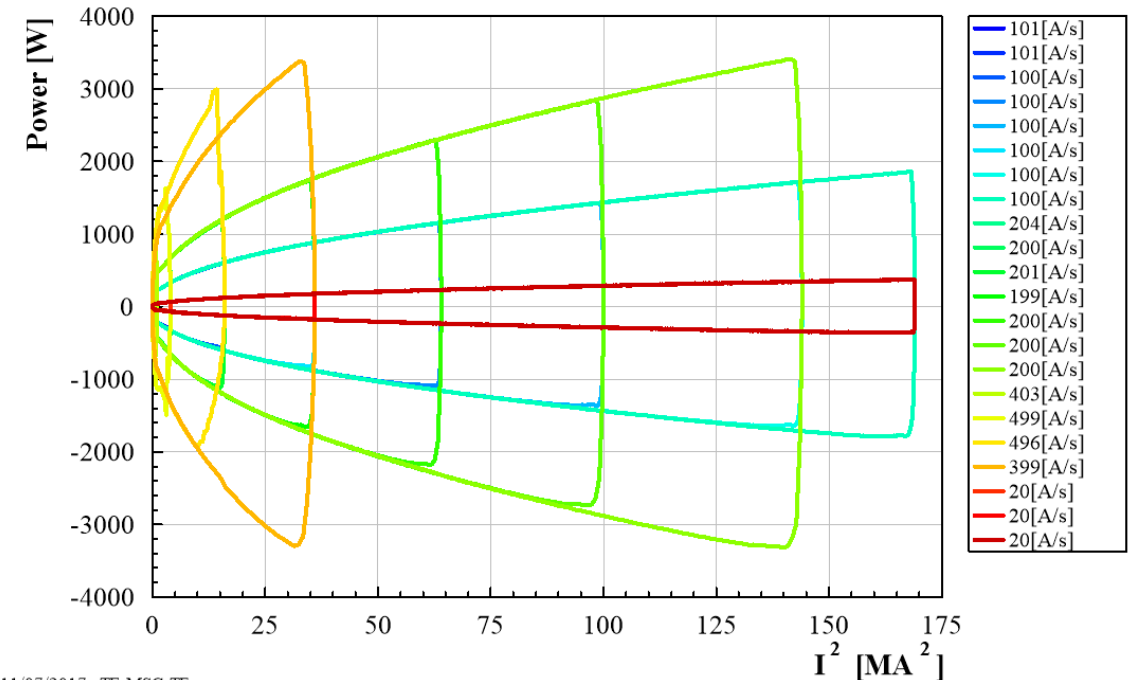
Data Plateau



File: HCLMSMC03_00000101_Loss_4.2K_2015_07_23-09_24_18_dmm.csv_test

AC Loss Measurement

VTot



Importance of the cycle and offset definition!!

Measurement Procedure (example on SMC11T)

$$E = \int_{t_i}^{t_f} U \cdot I \, dt$$

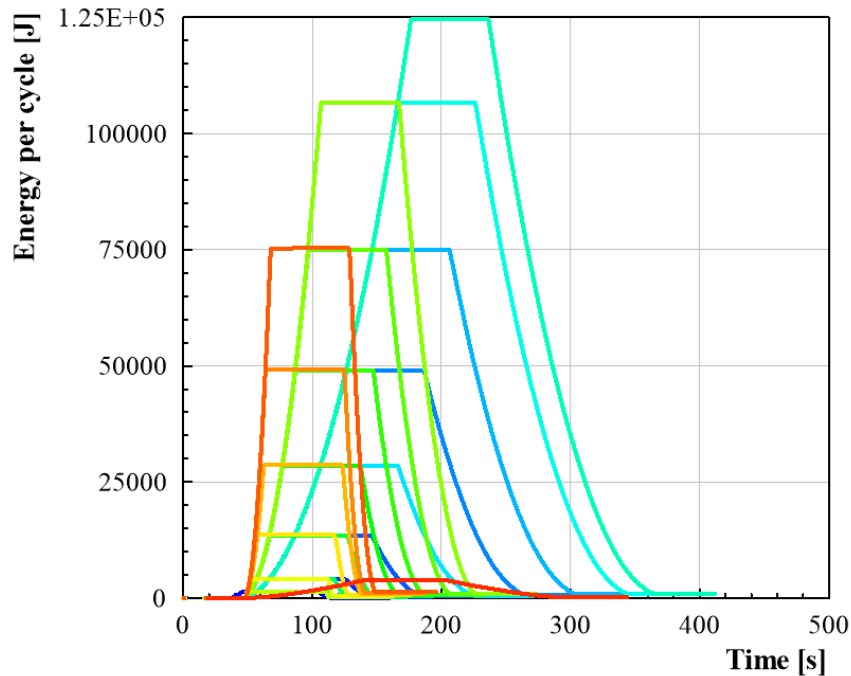
$$\text{Loss/cycle} = E_f - E_i$$



File: HCLMSMC003_00000101_Loss_4.2K_2015_07_23-09_24_18_dmm.csv

AC Loss Measurement

VTotal



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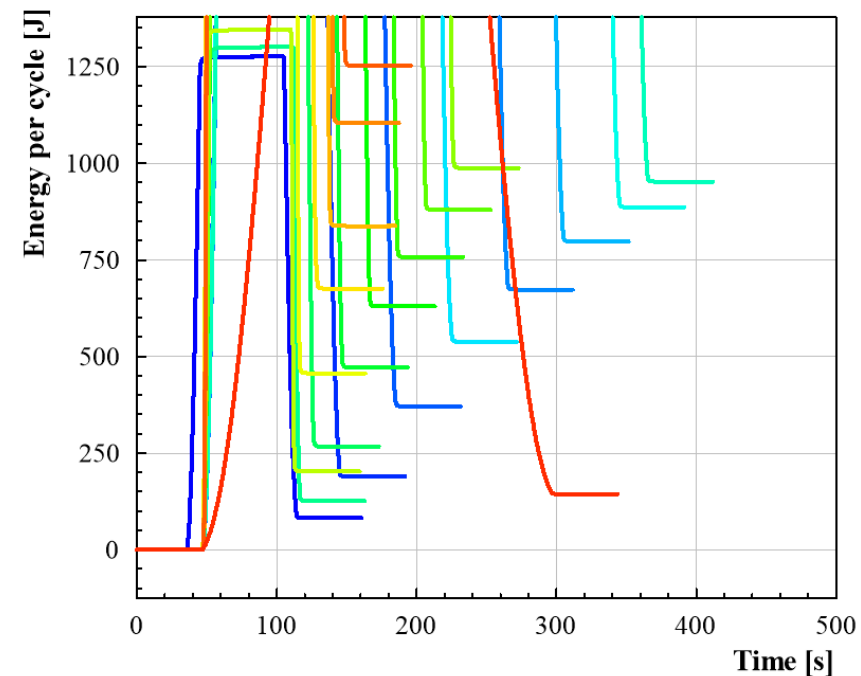
Loss [J]	$\sigma(\text{Loss})$ [J]	dI/dt [A/s]	I_max [A]
81.7	0.00	101	1001
202.4	0.01	403	1001
126.0	0.01	204	1001
144.1	0.02	20	2001
266.9	0.02	200	2001
189.5	0.02	101	2001
456.6	0.01	499	2001
472.1	0.01	201	4001
675.4	0.02	496	4001
371.1	0.01	100	4001
472.4	0.02	20	6000
629.6	0.01	199	6001
837.6	0.02	399	6001
538.4	0.02	100	6001
757.3	0.02	200	8001
1104.1	0.02	500	8001
672.9	0.01	100	8001
879.2	0.02	200	10001
1252.3	0.02	499	10001
797.6	0.02	100	10001
987.7	0.03	200	12000
886.2	0.02	100	12000
933.3	0.01	20	13000
952.3	0.01	100	13000



File: HCLMSMC003_00000101_Loss_4.2K_2015_07_23-09_24_18_dmm.csv

AC Loss Measurement

VTotal

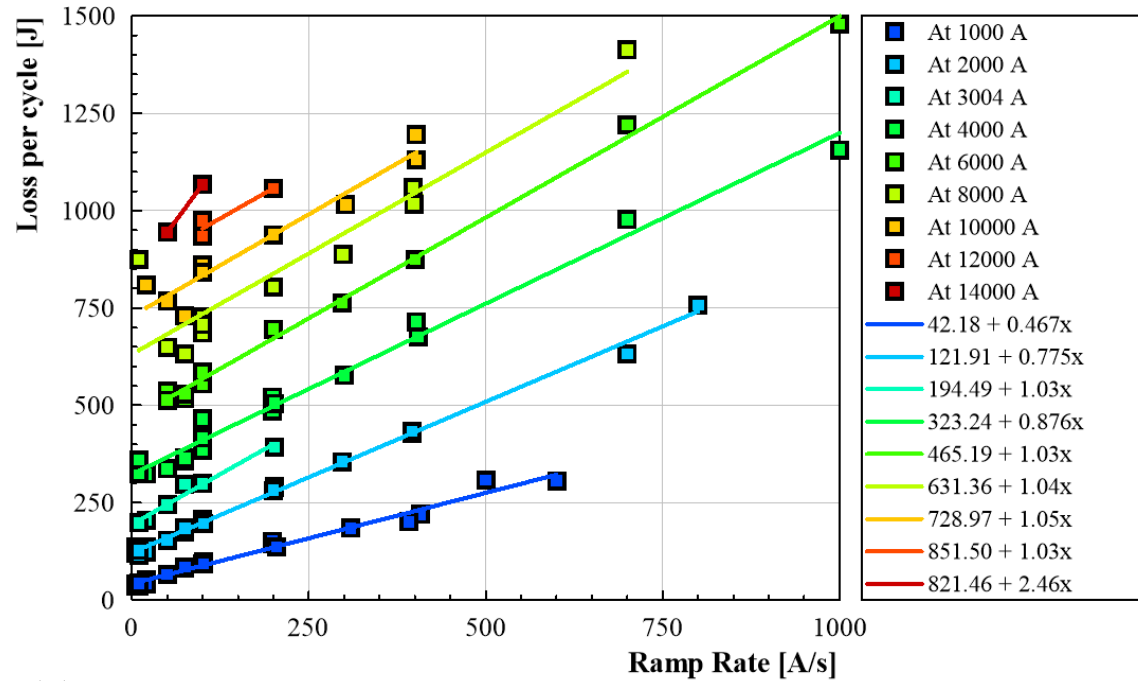


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Loss [J]	$\sigma(\text{Loss})$ [J]	dI/dt [A/s]	I_max [A]
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1252.3	0.02	499	10001
797.6	0.02	100	10001
987.7	0.03	200	12000
886.2	0.02	100	12000
933.3	0.01	20	13000
952.3	0.01	100	13000

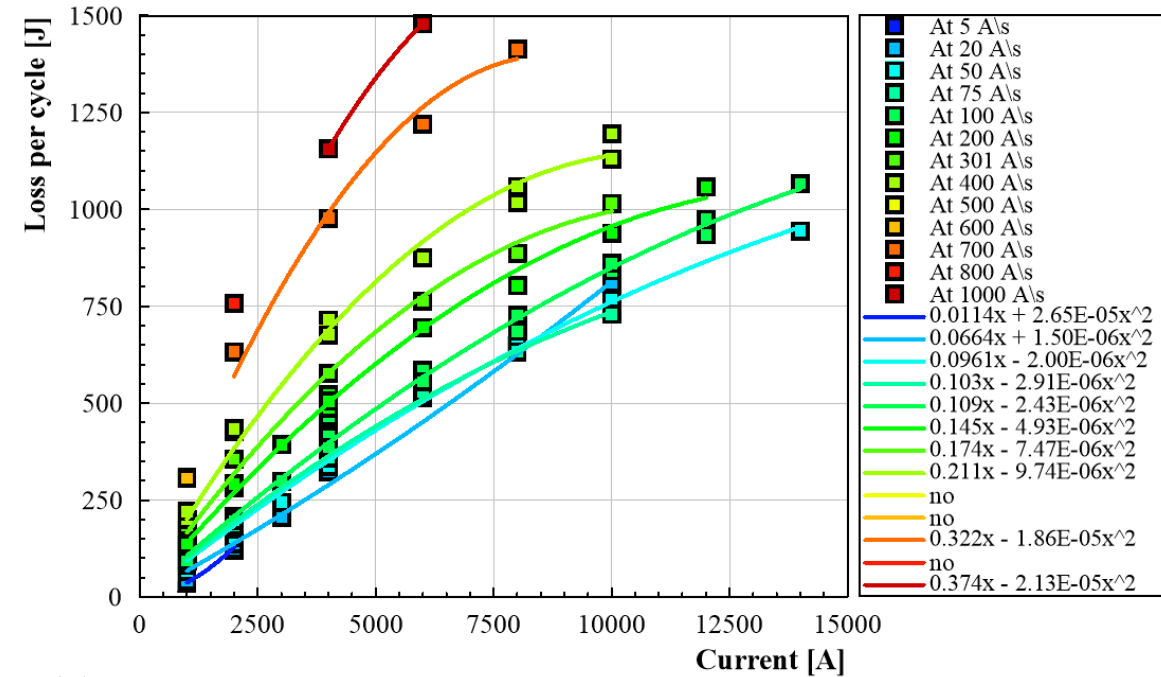
Measurement final result (example on SMC11T - RRP)

AC loss as function of the ramp rate (linear fit)



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AC loss as function of the current (quadratic fit)



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Measurement Procedure (example on SMC11T)

Algorithm to automatically process large number of:

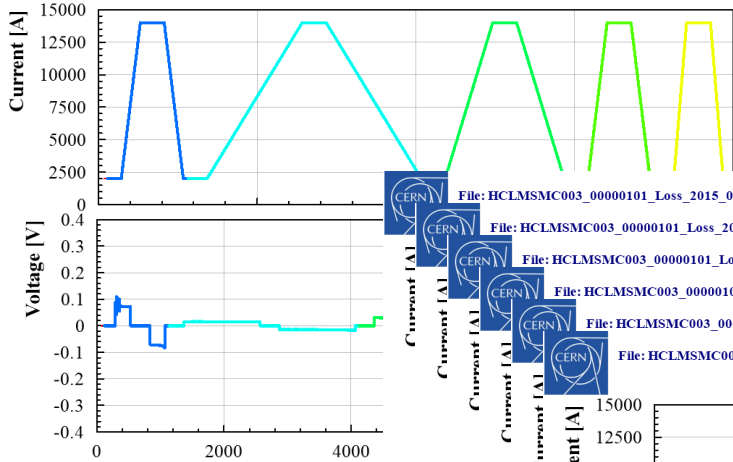
magnets / files / cycles / signals



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AC Loss Measurement

Data Plateau



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File: HCLMSMC03_00000101_Loss_2015_07_22-11_53_45_dmm

AC Loss Measurement



File: HCLMSMC03_00000101_Loss_2015_07_22-11_53_45_dmm

AC Loss Measurement



File: HCLMSMC03_00000101_Loss_2015_07_22-11_53_45_dmm

AC Loss Measurement



File: HCLMSMC03_00000101_Loss_2015_07_22-11_53_45_dmm

AC Loss Measurement



File: HCLMSMC03_00000101_Loss_2015_07_22-11_53_45_dmm

AC Loss Measurement



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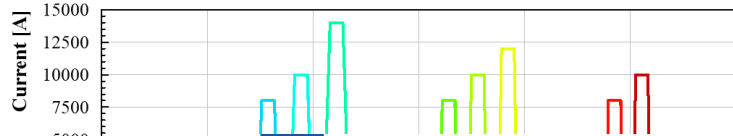
AC Loss Measurement



File: HCLMSMC03_00000101_Loss_2015_07_22-11_53_45_dmm

AC Loss Measurement

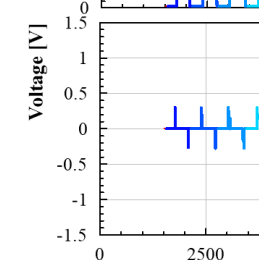
Data Plateau



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AC Loss Measurement

Data Plateau



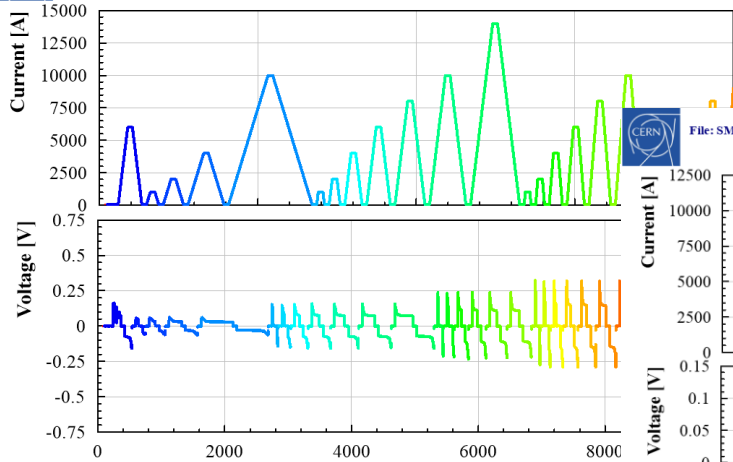
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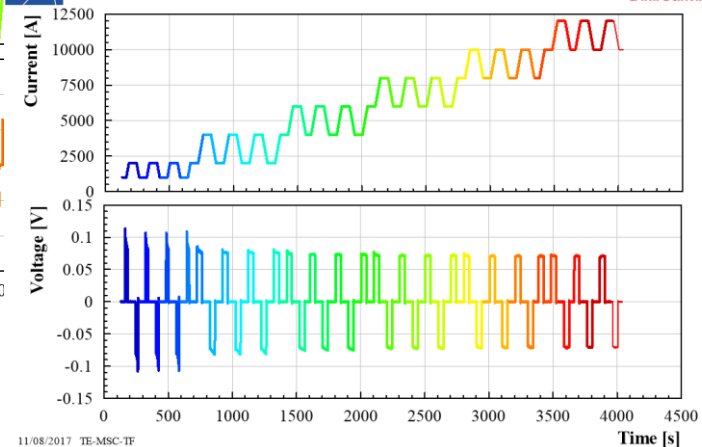


File: SMC11T_4a_Loss_2016_08_18-14_23_19_dmm

AC Loss Measurement

Data Plateau

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Time [s]

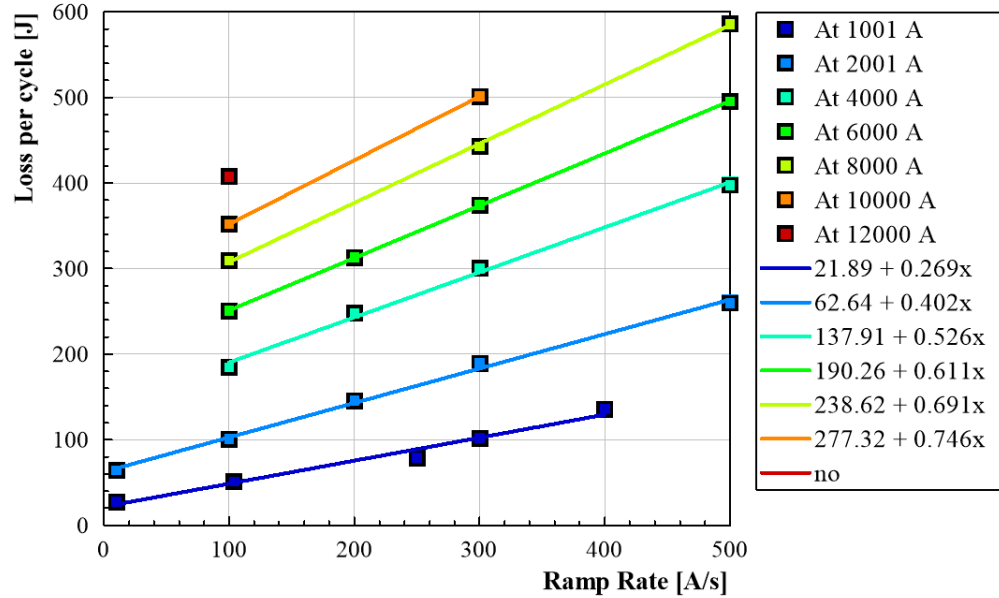
Measurement final result (example on SMC11T4 - PIT)



File: SMC11T_4a_Loss_2016_08_18-12_21_17_dmm

AC Loss Measurement

Vlow



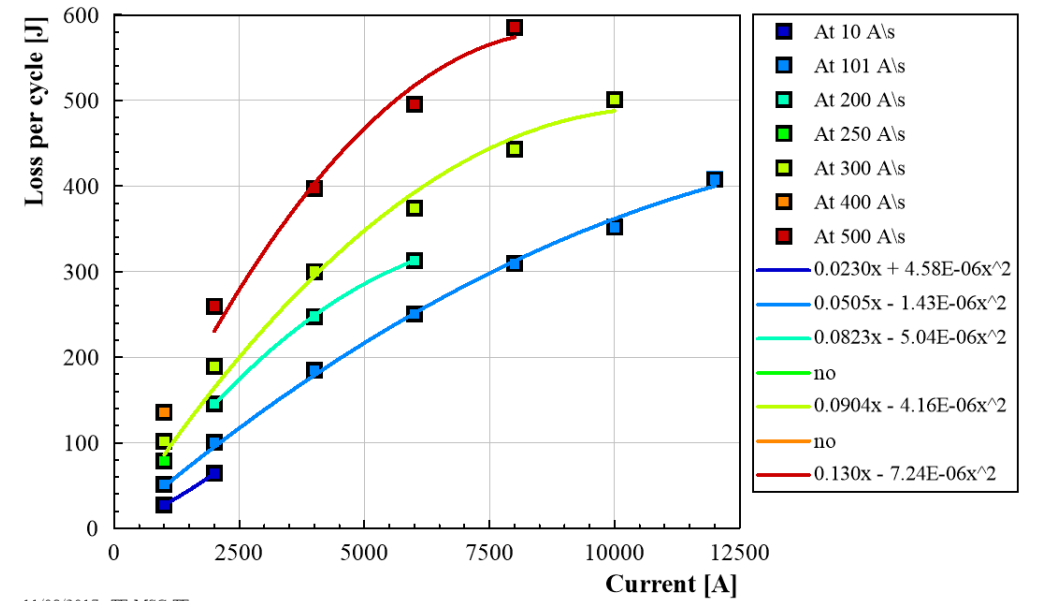
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AC Loss Measurement

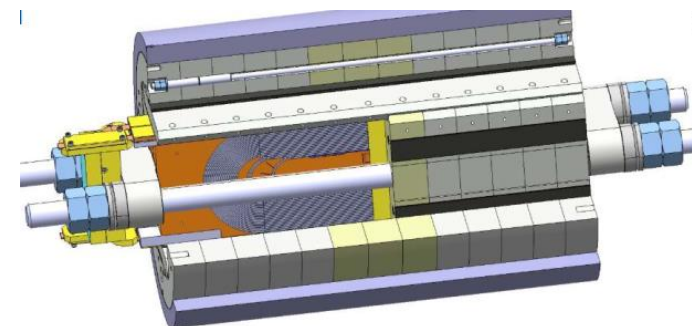
Vlow



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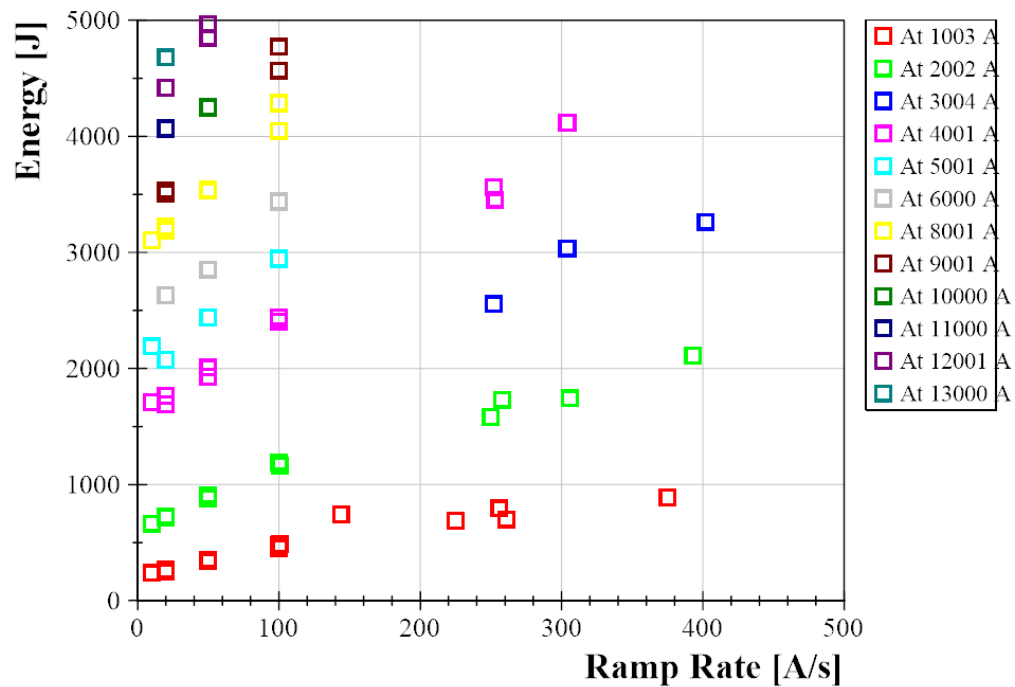
Another example of RMC...

Result for RMC_QXF



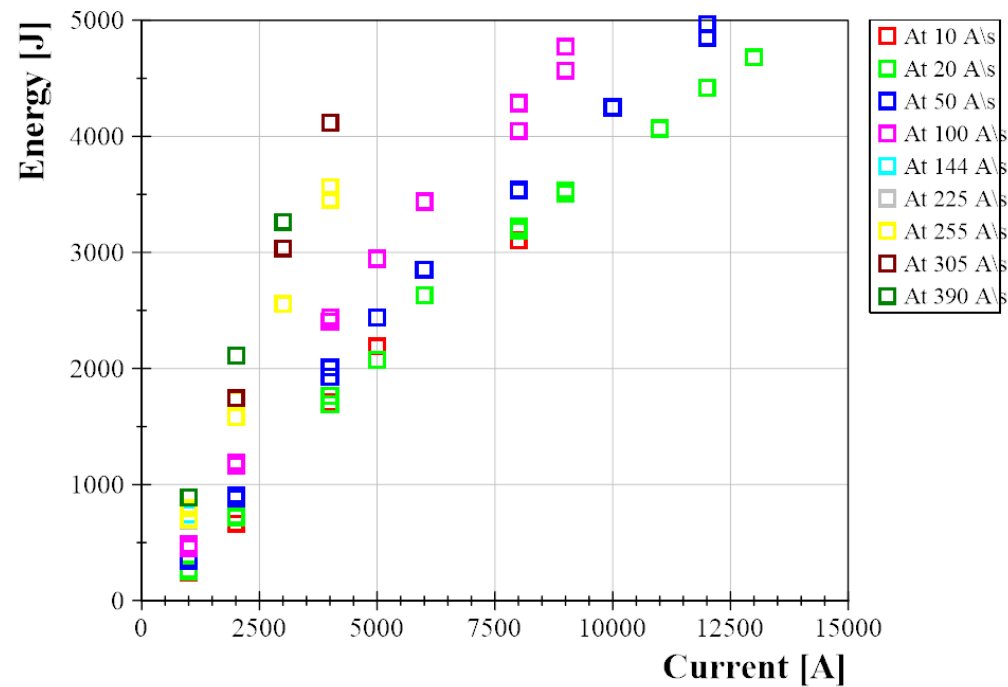
Quench file: RMC_QXF_Loss_2017_04_10-14_27_52_dmm.csv

Vsum



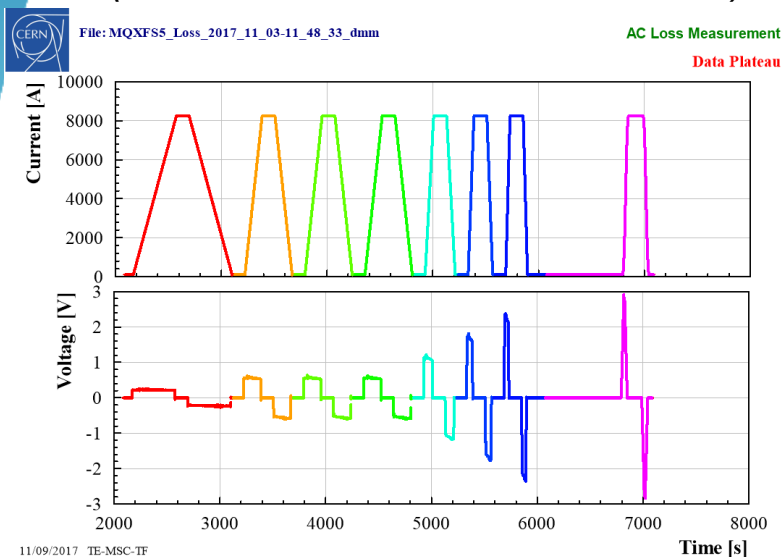
Quench file: RMC_QXF_Loss_2017_04_10-14_27_52_dmm.csv

Vsum

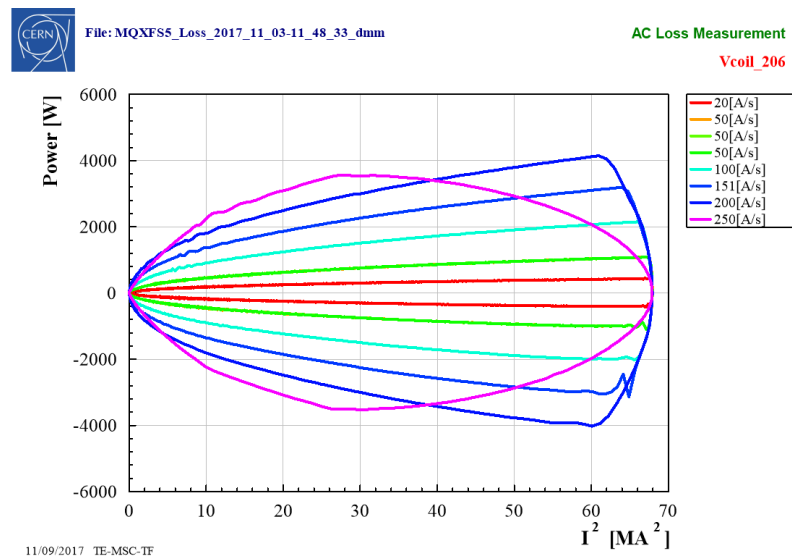


Example of analysis on MQXFS5

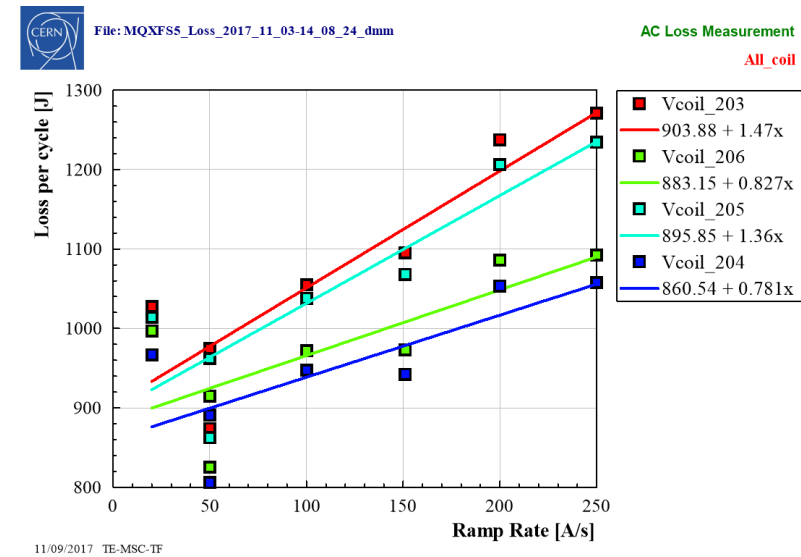
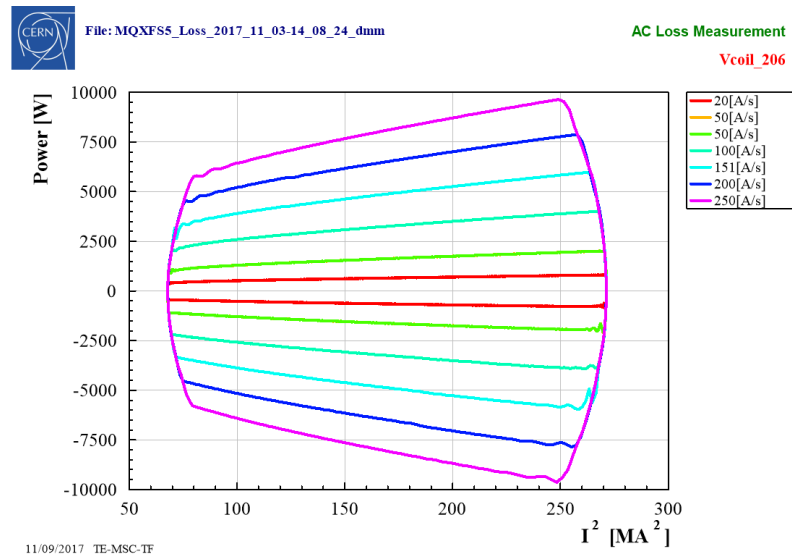
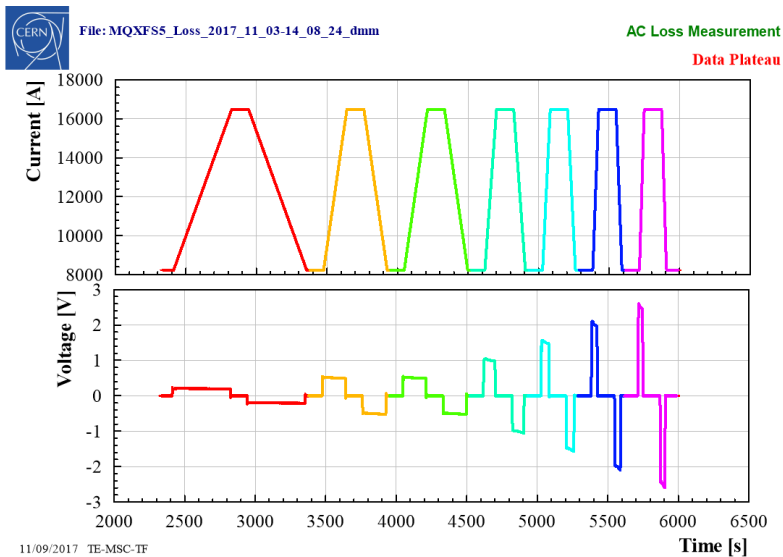
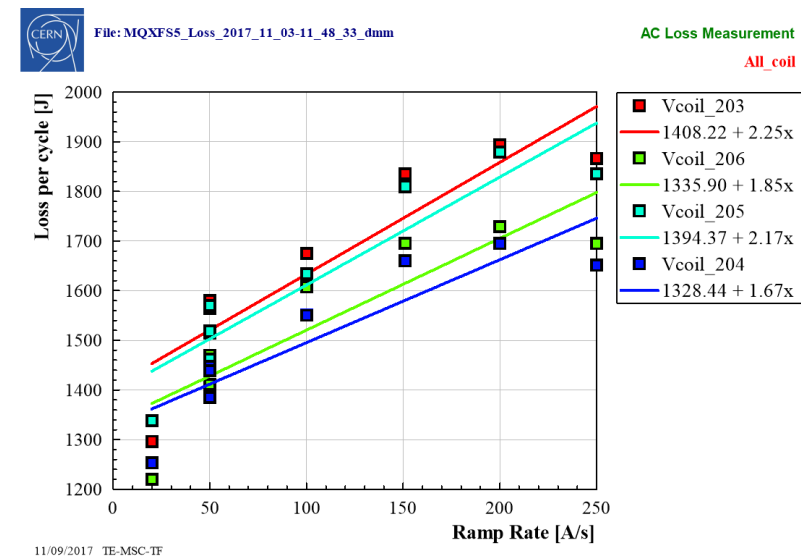
Current/voltage
(0-50 % I_{nom} & 50 -100 % I_{nom})



Power over cycle (1 coil)



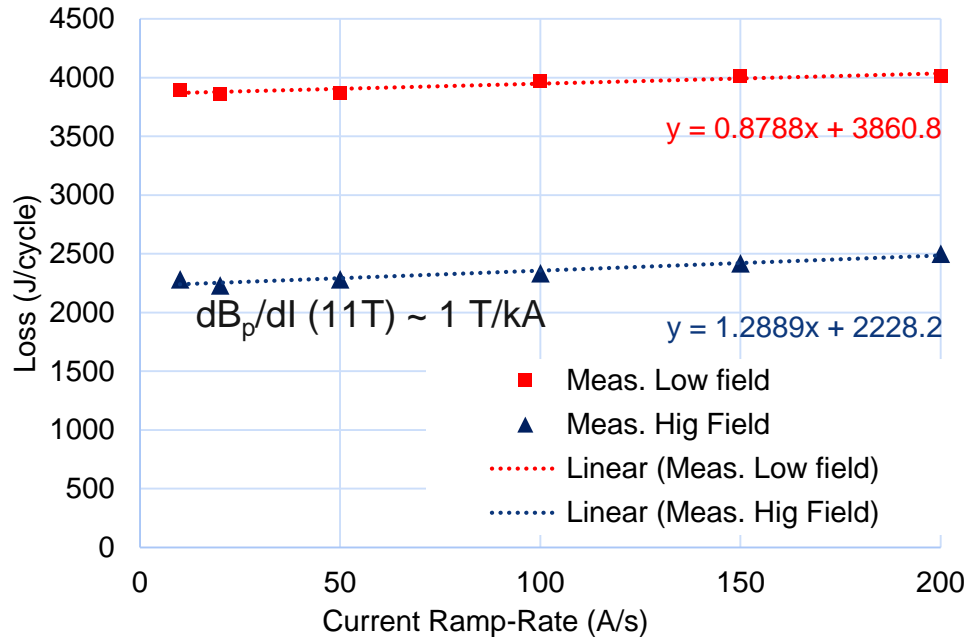
Loss per cycle function of ramp rate (4 coils)



Simulation with Roxie (11T dipole)

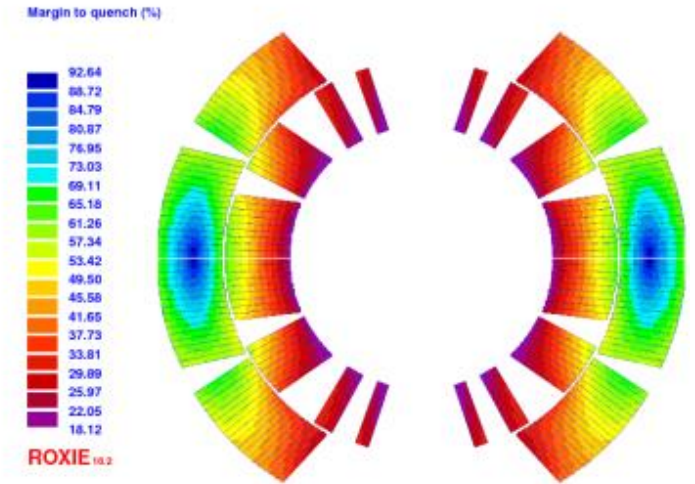
11 T (2 apertures) loss per cycle (up+down) ≈ 7 kJ/m

Measured losses on 11 T short model MBHSP012



Low field: from 0.1 to 6 kA
High field: From 6 kA to 11.85 kA

Courtesy of S.I. Bermudez and G. Willering



Margin on the loadline

Our assumption: ISCC and IFCC are negligible, **only strand magnetization losses** are considered

Strand magnetization, which depends on

- Sub-element diameter (d_{sub})
- Critical current density (non-Cu) (J_c)
- Cu/non-Cu ratio (λ)

$$M(B) \propto d_{sub} \cdot J_c(B) \cdot \frac{1}{\lambda + 1}$$

Roxie Model Input

- Superconductor current density as specified for HiLumi

- $T_{c0} = 16 \text{ K}$
- $B_{c20} = 29.38 \text{ T}$
- $\alpha = 0.96$
- $C_0 = 188870 \text{ A/mm}^2 \text{ T}$
- 3 % cabling degradation

$$B_{c2}(T) = B_{c20} \cdot (1 - t^{1.52})$$

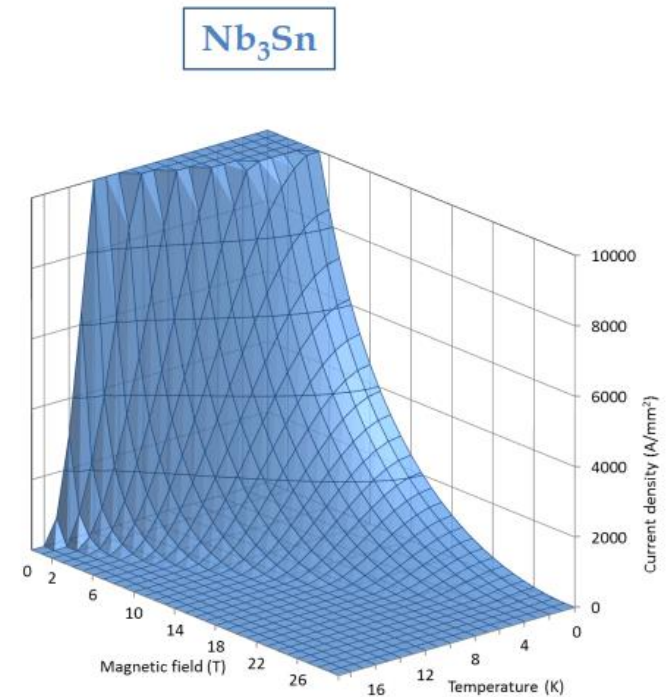
$$J_c = \frac{C(t)}{B_p} \cdot b^{0.5} \cdot (1 - b)^2$$

$$C(t) = C_0 \cdot (1 - t^{1.52})^\alpha \cdot (1 - t^2)^\alpha$$

- Reference: $D_{\text{eff}} = 50 \mu\text{m}$, no reduction due to flux jumps

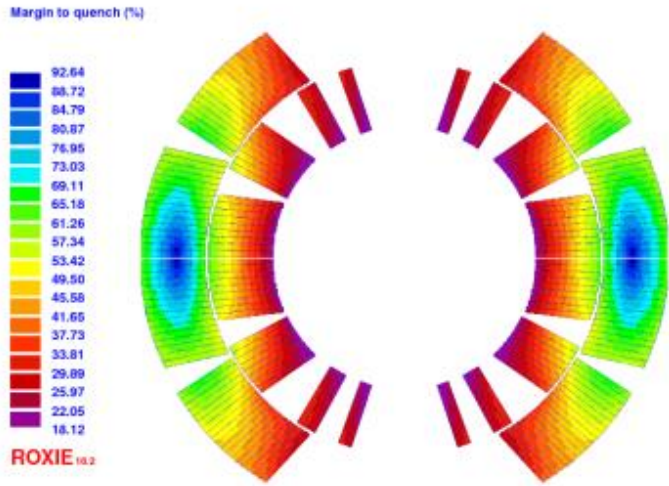
- Sensitivity analysis to:

- Effective filament size $D_{\text{eff}} = 20 \mu\text{m}$, $D_{\text{eff}} = 50 \mu\text{m}$
- Reduction of strand magnetization at low field due to flux jumps $\chi = 0.5-1$

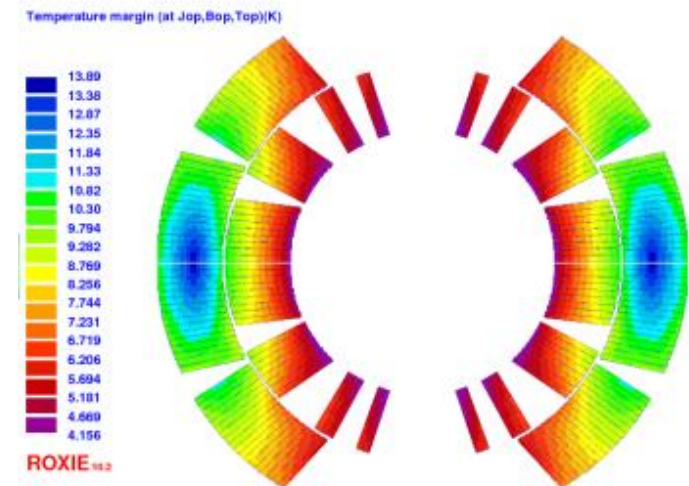


Courtesy of P. Ferracin

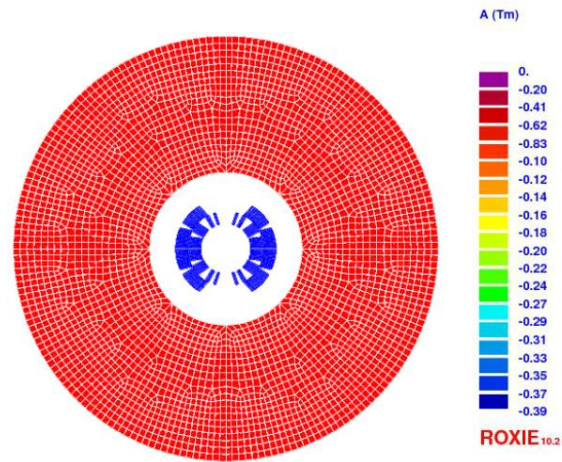
Roxie Model Input



Margin on the loadline



Temperature margin at nominal current

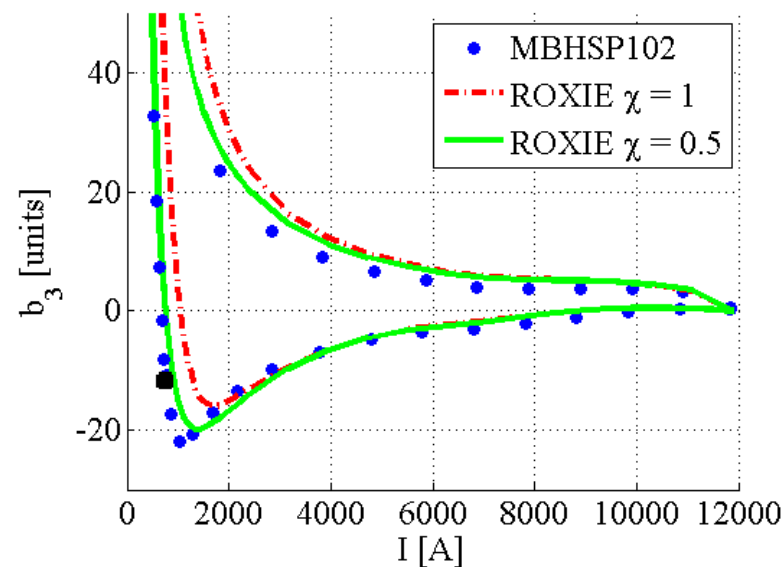
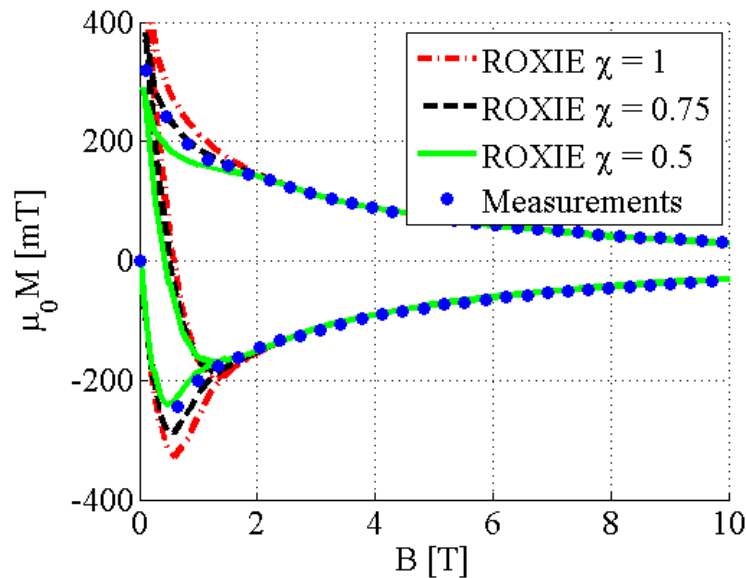


Iron mesh and vector potential

Courtesy of S.I. Bermudez
and F. Murgia

Modelling SC magnetization

- Semi-analytical hysteresis model for the superconductor, developed in [1], and implemented in ROXIE [1].
- Limited accuracy at low field, partially due the reduction on magnetization observed in Nb₃Sn due to flux jumps [2], which can be overcome by introducing a reduction on the strand magnetization below a given field level.
- Model has been validated in 11 T [2] and MQXF [3] magnets



Courtesy of S.I. Bermudez

$$D_{eff}^{LF}(B) = D_{eff}(\chi + (1 - \chi)(B/B_o))$$

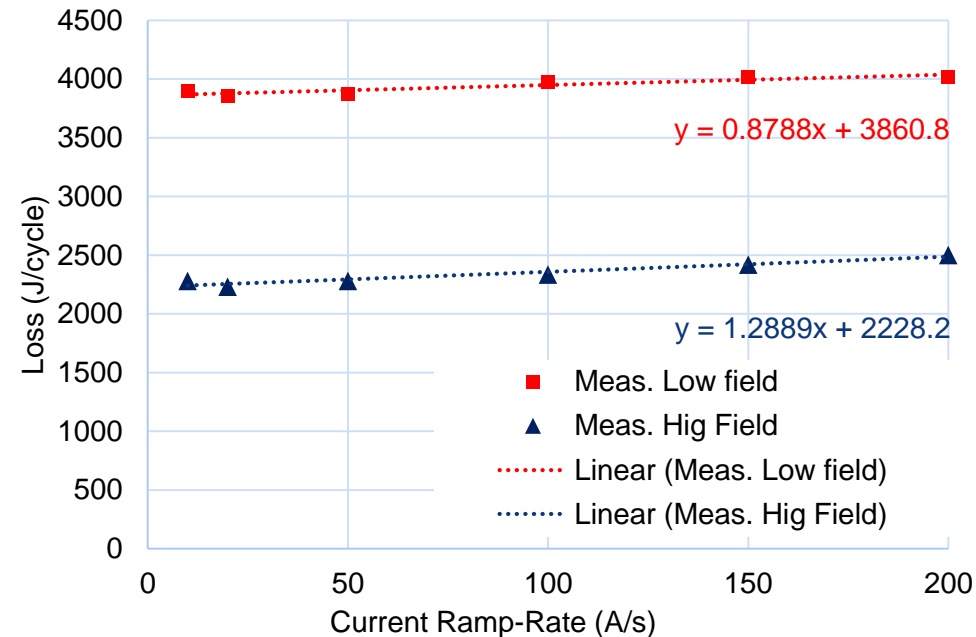
- [1] C. Vollinger, Superconductor magnetization modelling for the numerical calculation of field errors in accelerator magnets. PhD thesis, 202
- [2] S. Izquierdo Bermudez, et.al, Persistent Current Magnetization effects in High-Field Superconducting Accelerator magnets, IEEE 2016
- [3] S. Izquierdo Bermudez, et.al, Magnetic Analysis of the Nb3Sn low-beta Quadrupole for the High Luminosity LHC, IEEE 2017

ROXIE vs AC loss measurement: 11T

- Measured ramp up + ramp down around 6 kJ, $6/1.7 = 3.6$ kJ/m for a single aperture (ROXIE gives 4 kJ/m, a bit conservative, but good enough for a first approximation).

11 T - Magnetization loss per aperture (Deff = 0.046 mm, RRP 108/127)	ROXIE	
	J/m	J/m ³
Pre-Cycle (0- 11.85 kA-0.1 kA)	4133	8.139E+05
Ramp up (0.1 kA -11.85 kA)	1853	3.650E+05
Ramp down (11.85 kA - 0.1 kA)	2207	4.346E+05
Ramp down + Ramp up (11.85 kA-0.1 kA-11.85 kA)	4060	7.996E+05

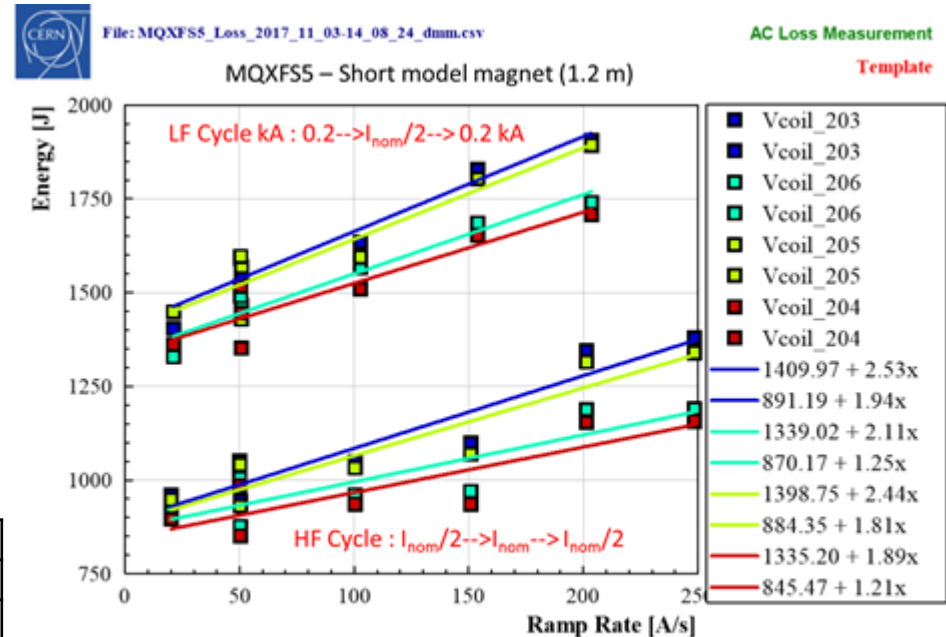
Measured losses on 11 T short model MBHSP012



ROXIE vs AC loss measurement: MQXFS

- Measurements: 7.5 kJ/m, so reasonably close to the 8.3 kJ/m predicted by ROXIE (actually Jc is 5 % lower than the spec in MQXFS5, so the difference is explained with that)

MQXF - Magnetization loss (Deff = 0.039 mm, PIT bundle)	ROXIE	
	J/m	J/m3
Pre-Cycle (0-16.47 kA-0.1 kA)	8474	5.994E+05
Ramp up (0.1 kA -16.47 kA)	3782	2.675E+05
Ramp down (16.47 kA -0.1 kA)	4503	3.186E+05
Ramp down + Ramp up (16.47 kA-0.1 kA-16.47 kA)	8286	5.861E+05

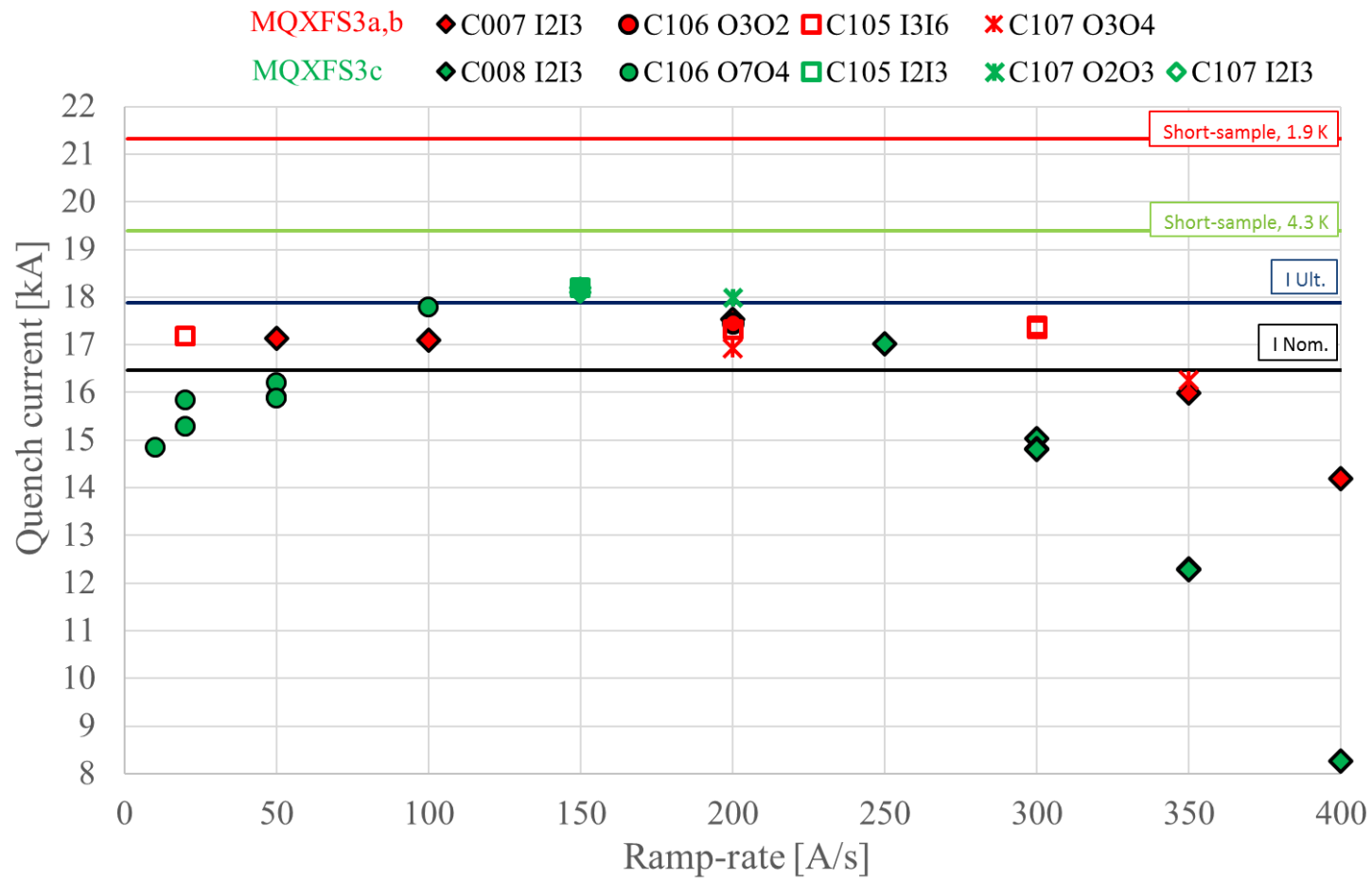


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Total magnetization loss for HF + LF (i.e., ramp up and ramp down to nominal current) ≅ (5.5 + 3.5)/1.2 = 7.5 kJ/m

Conclusion

- If the theory behind AC loss is well understood, the **literature** about Nb₃Sn magnet is **rather limited** and mainly referring to ITER magnet (central solenoid pulse mode).
- Experimental results on recent Nb₃Sn magnet shows values **one order of magnitude higher** than NbTi (0.5 kJ/m vs. 8 kJ/m)
- A large amount of **experimental data is now available** from (SMC, RMC, 11T, MQXF) with a defined procedure for AC loss quantification.
- A **new framework of analysis** has been developed following literature procedure to process a large number of files (including old file with different format) can now be treated massively.
- So far only **electrical method** has been used. Next would be to perform **calorimetric method**.
- Simulation work is just recently started at CERN...
- Subsidiary goal... can we simulate **quench current versus ramp rate using AC loss measurement?**



Thank you for your attention!