



Dark Matter and the Seesaw Scale

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PASCOS, June 5th 2018



References

This talk is based on:

- P. Fileviez Perez and C. M, Dark Matter and The Scale for Lepton Number Violation, arXiv:1803.07462 [hep-ph]

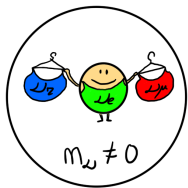
Motivation

- The Standard Model rocks as an EFT at low energies.
- However, clear evidence calling for new physics beyond:



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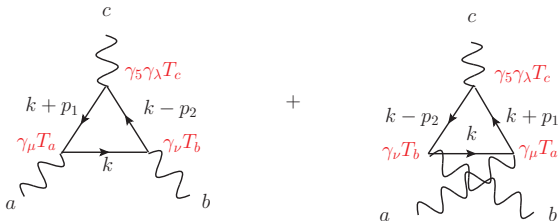
Motivation



Extra: $U(1)_{B-L}$ global

Motivation

- Gauge anomalies:



$$A^{abc} = \text{Tr} [\{T_V^a, T_V^b\}, T_A^c]$$

- In SM, a *magic* cancellation among representations and charges occurs!

Motivation

- Contributing diagrams when extra $U(1)_X$ gauged:

$$\begin{aligned}
 \text{Diagram 1: } & \text{Left: } U(1)_L \text{ (red), } SU(3) \text{ (green), } SU(3) \text{ (green). Right: } U(1)_X \text{ (red).} & A_1 &= \sum_q X_{qL} - \sum_q X_{qR} \\
 \text{Diagram 2: } & \text{Left: } U(1)_X \text{ (red), } SU(2)_L \text{ (blue), } SU(2)_L \text{ (blue). Right: } U(1)_X \text{ (red).} & A_2 &= \sum_\ell X_{\ell L} + 3 \sum_q X_{qL} \\
 \text{Diagram 3: } & \text{Left: } U(1)_X \text{ (red), } U(1)_Y \text{ (yellow), } U(1)_Y \text{ (yellow). Right: } U(1)_X \text{ (red).} & A_3 &= \sum_{\ell,q} (Y_{\ell L}^2 X_{\ell L} + 3Y_{qL}^2 X_{qL}) \\
 & & & - \sum_{\ell,q} (Y_{\ell R}^2 X_{\ell R} + 3Y_{qR}^2 X_{qR}) \\
 \text{Diagram 4: } & \text{Left: } U(1)_Y \text{ (yellow), } U(1)_X \text{ (red), } U(1)_X \text{ (red). Right: } U(1)_X \text{ (red).} & A_4 &= \sum_{\ell,q} (Y_{\ell L} X_{\ell L}^2 + 3Y_{qL} X_{qL}^2) \\
 & & & - \sum_{\ell,q} (Y_{\ell R} X_{\ell R}^2 + 3Y_{qR} X_{qR}^2) \\
 \text{Diagram 5: } & \text{Left: } U(1)_X \text{ (red), } U(1)_X \text{ (red), } U(1)_X \text{ (red). Right: } U(1)_X \text{ (red).} & A_5 &= \sum_{\ell,q} (X_{\ell L}^3 + 3X_{qL}^3) \\
 & & & - \sum_{\ell,q} (X_{\ell R}^3 + 3X_{qR}^3)
 \end{aligned}$$

$$A_6 = \sum_{\ell,q} (X_{\ell L} + 3X_{qL}) - \sum_{\ell,q} (X_{\ell R} + 3X_{qR})$$

- Simplest solution \rightarrow Addition of 3 ν_R



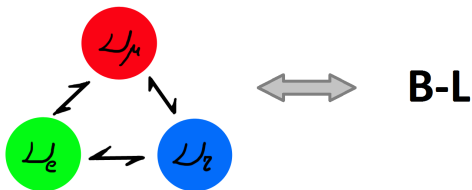
$$M_\nu \neq 0$$

Motivation



Extra: $U(1)_{B-L}$ global

- Connection



Breaking $U(1)_{B-L}$: Canonical Seesaw

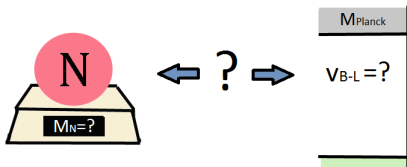
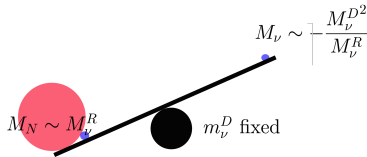
Field content: $SM + \underline{3\nu_R} + \underline{S_{BL}} \sim (1, 1, 0, 2)$

anomaly free theory \rightarrow *B-L breaking!*

$$-\mathcal{L}_\nu^{\text{type-I}} = Y_\nu \bar{\ell}_L i \sigma_2 H^* \nu_R + \lambda_R \nu_R^T C \nu_R S_{BL} + \text{h.c.}$$

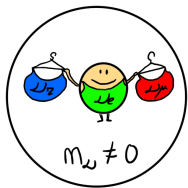
- Canonical See-saw:

$$\mathcal{M}_\nu^{\text{type-I}} = \begin{pmatrix} 0 & M_\nu^D \\ (M_\nu^D)^T & M_\nu^R \end{pmatrix}$$



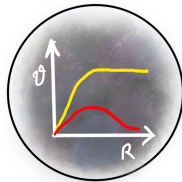
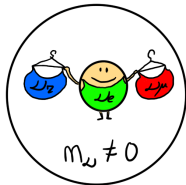
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Vector-like fermions $\chi = \chi_L + \chi_R$ as DM

$$\chi_L \sim (1, 1, 0, n), \quad \chi_R \sim (1, 1, 0, n)$$

$$\mathcal{L}_\nu^{DM} \supset i\bar{\chi}_L \gamma^\mu D_\mu \chi_L + i\bar{\chi}_R \gamma^\mu D_\mu \chi_R + (D_\mu S_{BL})^\dagger (D^\mu S_{BL}) - (M_\chi \bar{\chi}_L \chi_R + \text{h.c.}),$$

- Relevant parameters:

$$n, g_{BL}, M_\chi, M_{h_2}, M_{N_i} \text{ and } M_{Z_{BL}}.$$



A Feynman diagram illustrating a fermion loop. On the left, a shaded circular region contains the labels $\chi, \bar{\chi}$. A wavy line representing a Z_{BL}^μ boson extends from this region to the right, where it meets a vertex labeled d_{SM} .

Relic Density

- Cosmological bound on the relic density:

$$\Omega_{\text{DM}} h^2 \sim \frac{1}{\langle \sigma v \rangle} \leq 0.1199 \pm 0.0027$$

Ade et al. [Planck Collaboration], A&A, Volume 571, A16

- Relic density:

$$\Omega_{\text{DM}} h^2 = \frac{1,07 \times 10^9 \text{ GeV}^{-1}}{M_{\text{Pl}}} \left(\int_{x_f}^{\infty} \frac{g_*^{1/2}(x) \langle \sigma v \rangle(x)}{x^2} dx \right)^{-1}$$

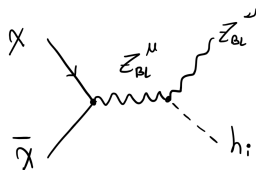
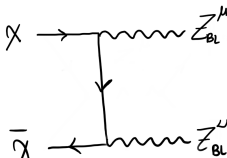
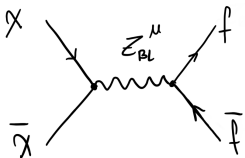
Gondolo, Gelmini, Nuclear Physics B 360(1)

- Thermal averaged cross-section:

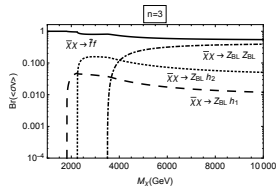
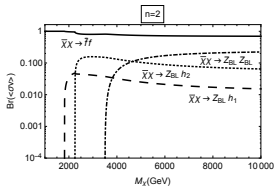
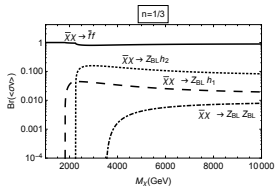
$$\langle \sigma v \rangle(x) = \frac{x}{8M_\chi^5 K_2^2(x)} \int_{4M_\chi^2}^{\infty} \sigma \times (s - 4M_\chi^2) \sqrt{s} K_1 \left(\frac{x\sqrt{s}}{M_\chi} \right) ds,$$

Annihilation channels

$$\mathcal{L}_\nu^{DM} \supset i\bar{\chi}_L \gamma^\mu D_\mu \chi_L + i\bar{\chi}_R \gamma^\mu D_\mu \chi_R + (D_\mu S_{BL})^\dagger (D^\mu S_{BL}) - (M_\chi \bar{\chi}_L \chi_R + \text{h.c.}),$$

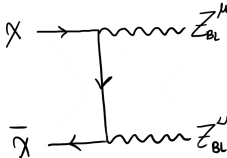
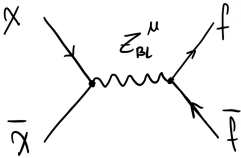


- Branching ratios of $\langle\sigma v\rangle$ for above channels:

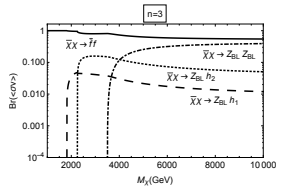
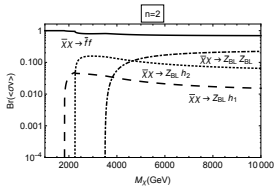
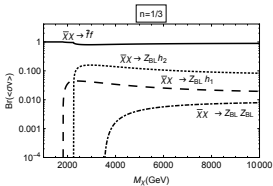


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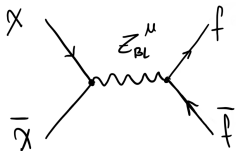


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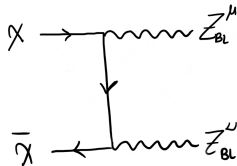


Annihilation channels

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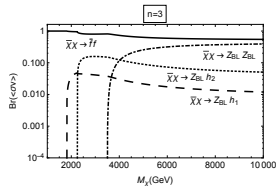
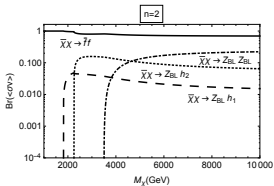
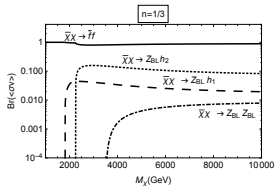


$$\sim g_{BL}^4 n^2 \frac{1}{L^2}$$



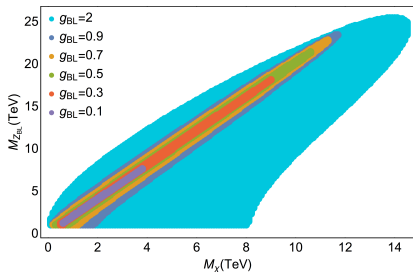
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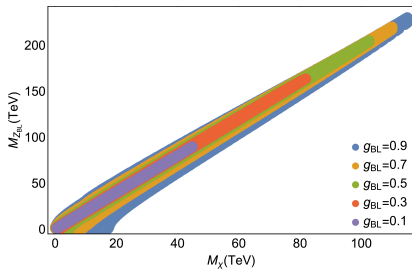


Phase Space allowed by Relic Density constraints

- In agreement with Relic Density constraint: $\Omega h^2 < 0.1199 \pm 0.0027$



$$n = 1/3$$



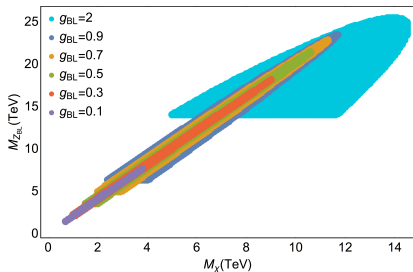
$$n = 3$$

Bounded below!

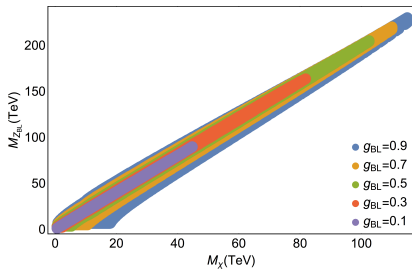
Collider bounds: LEP

- LEP:

$$\frac{M_{Z_{BL}}}{g_{BL}} > 7 \text{ TeV}$$

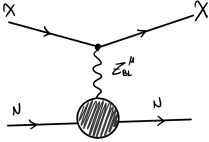


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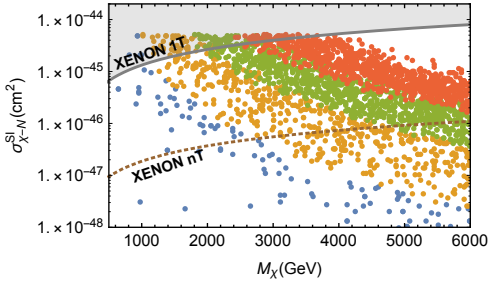


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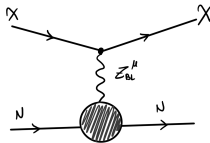
Direct searches



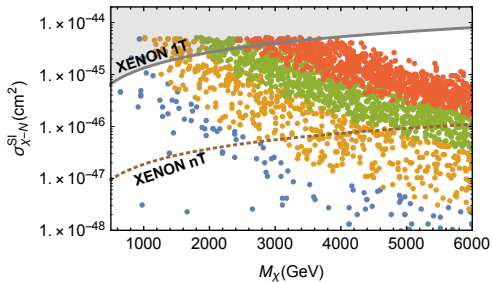
$$\sigma_{\chi N}^{\text{SI}} = \frac{M_N^2 M_\chi^2}{\pi (M_N + M_\chi)^2} \frac{g_{BL}^4}{M_{Z_{BL}}^4} n^2$$



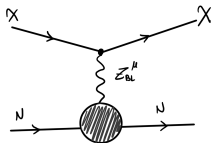
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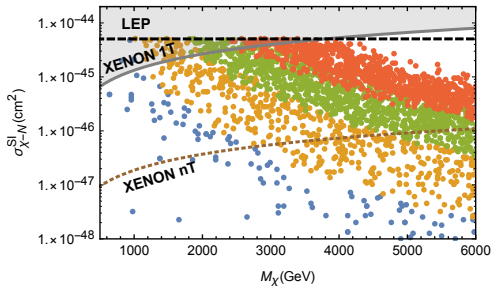


Direct searches

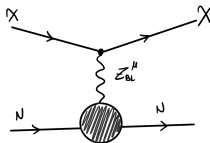


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$$\sigma_{\chi N}^{\text{SI}} (\text{cm}^2) = 12.4 \times 10^{-41} \left(\frac{\mu}{1 \text{GeV}} \right)^2 \left(\frac{1 \text{TeV}}{r_{BL}} \right)^4 n^2 \text{cm}^2,$$

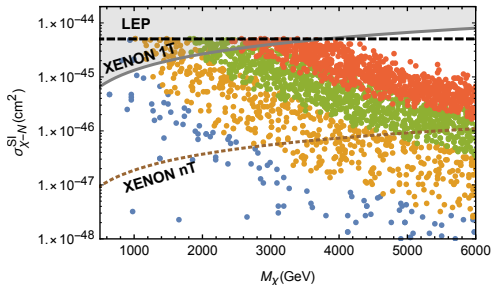


Direct searches: XENON-1T

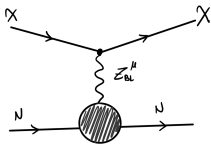


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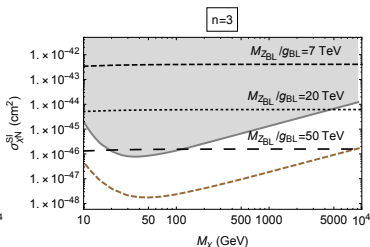
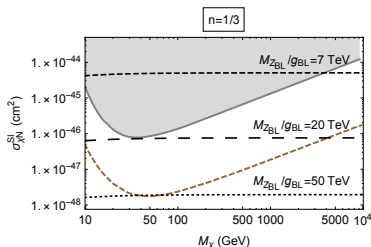


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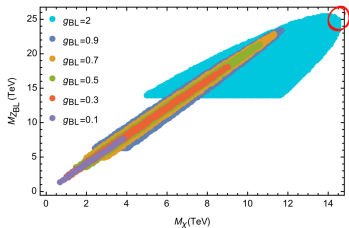
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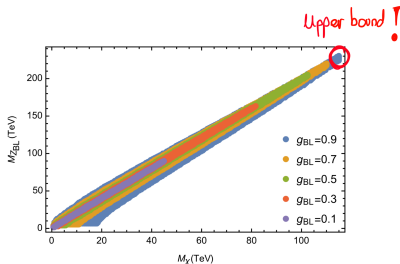
Bounded above!

Phase Space allowed by Relic Density constraints

- In agreement with Relic Density constraint: $\Omega h^2 < 0.1199 \pm 0.0027$



$$n = 1/3$$



$$n = 3$$

Upper bound

$$\sigma(\bar{\chi}\chi \rightarrow \bar{f}f) \propto \frac{g_{BL}^4 n^2}{\Gamma_{Z_{BL}}^2} \xrightarrow{\Gamma_{Z_{BL}}^2 \sim g_{BL}^4 \Lambda^2} n^2 \frac{1}{\Lambda^2}$$

$$\sigma(\bar{\chi}\chi \rightarrow Z_{BL}Z_{BL}) \propto g_{BL}^4 n^4 \frac{1}{\Lambda^2}$$

Upper bound

$$\begin{aligned}\sigma(\bar{\chi}\chi \rightarrow \bar{f}f) &\propto n^2 \frac{1}{\Lambda^2} \\ \sigma(\bar{\chi}\chi \rightarrow Z_{BL}Z_{BL}) &\propto g_{BL}^4 n^4 \frac{1}{\Lambda^2}\end{aligned}$$

$$n < 1$$

Upper bound

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$$n < 1$$

$$n > 1$$

$$(\mathcal{L}_K \supset n g_{BL} \bar{\chi} \gamma_\mu Z_{BL}^\mu \chi)$$

$$\text{Perturbative bound} \Rightarrow n g_{BL} < \sqrt{2\pi}$$

Upper bound

$$\sigma(\bar{\chi}\chi \rightarrow \bar{f}f) \propto n^2 \frac{1}{\Lambda^2}$$

$$\sigma(\bar{\chi}\chi \rightarrow Z_{BL}Z_{BL}) \propto \tilde{n}^4 \frac{1}{\Lambda^2}$$

$$n < 1$$

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$$(\mathcal{L}_K \supset n g_{BL} \bar{\chi} \gamma_\mu Z_{BL}^\mu \chi)$$

$$\text{Perturbative bound} \Rightarrow \underbrace{n g_{BL}}_{\tilde{n}} < \sqrt{2\pi}$$

What if $n \rightarrow \infty$?!

Upper bound

In the hypothetical (non "pheno-interesting") case of $n \rightarrow \infty$:

$$\begin{aligned}\sigma(\bar{\chi}\chi \rightarrow \bar{f}f) &\propto \frac{g_{BL}^4 n^2}{\Gamma_{Z_{BL}}^2} \\ \sigma(\bar{\chi}\chi \rightarrow Z_{BL}Z_{BL}) &\propto \tilde{\mathbf{n}}^4 \frac{1}{\Lambda^2}\end{aligned}$$

! $(\Gamma_{Z_{BL}}^{\text{tot}})^2 \sim \Gamma^2(Z_{BL} \rightarrow \bar{\chi}\chi) \propto g_{BL}^4 n^2 \Lambda^2$

Upper bound

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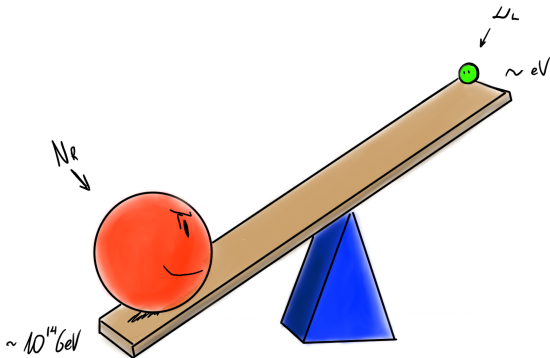
$$\begin{aligned}\sigma(\bar{\chi}\chi \rightarrow \bar{f}f) &\propto \frac{g_{BL}^4 n^2}{\Gamma_{Z_{BL}}^2} \rightarrow \frac{1}{\Lambda^2} \\ \sigma(\bar{\chi}\chi \rightarrow Z_{BL}Z_{BL}) &\propto \tilde{n}^4 \frac{1}{\Lambda^2}\end{aligned}$$

$$! (\Gamma_{Z_{BL}}^{\text{tot}})^2 \sim \Gamma^2(Z_{BL} \rightarrow \bar{\chi}\chi) \propto g_{BL}^4 n^2 \Lambda^2$$



The Canonical Seesaw

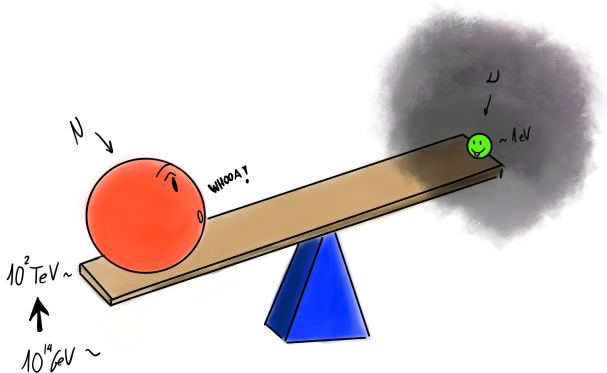
- In general, the upper bound for the $B - L$ breaking scale is the canonical seesaw scale, i.e. $v_{B-L} \leq 10^{14}$ GeV.



- The new theory could live anywhere up to the GUT scale...

The Canonical “Dark” Seesaw

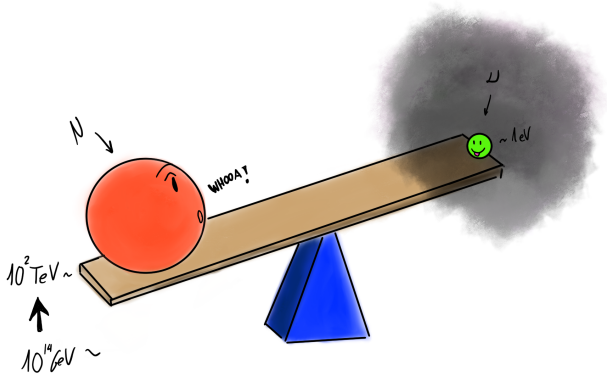
- The presence of Dark Matter in the game lowers considerably the upper bound to $\nu_{B-L} \lesssim 200$ TeV.



- Hope to see signals in a near future!!!

The Canonical “Dark” Seesaw

- The presence of Dark Matter in the game lowers considerably the upper bound to $\nu_{B-L} \lesssim 200 \text{ TeV}$.



- Hope to see signals in a near future!!!



Consequences of a low B-L breaking scale

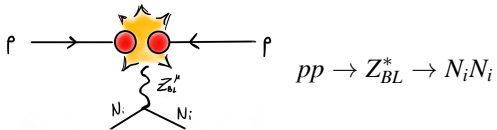
Low B-L scale ($v_{BL} \ll$)

$$M_{N_R} = \frac{\lambda_R}{\sqrt{2}} v_{BL} \rightarrow \text{Hope to see LNV signals at colliders!}$$

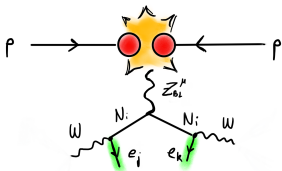
Lepton Number Violation at the LHC



Lepton Number Violation at the LHC

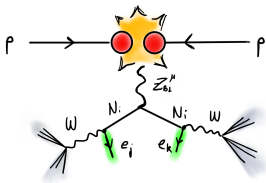


Lepton Number Violation at the LHC



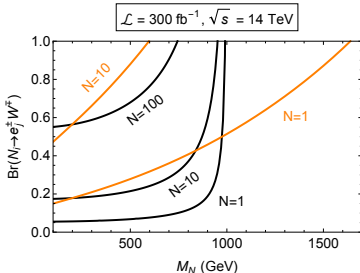
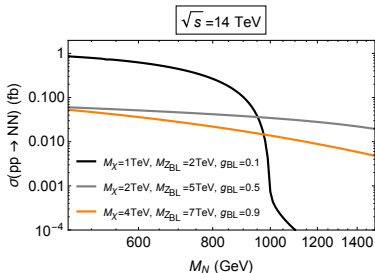
$$pp \rightarrow Z_{BL}^* \rightarrow N_i N_i \rightarrow e_j^\pm W^\mp e_k^\pm W^\mp$$

Lepton Number Violation at the LHC

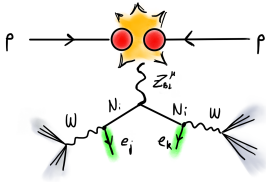


$$pp \rightarrow Z_{BL}^* \rightarrow N_i N_i \rightarrow e_j^\pm W^\mp e_k^\pm W^\mp \rightarrow e_j^\pm e_k^\pm 4j$$

$$N_{e_j^\pm e_k^\pm 4j} = 2\mathcal{L}\sigma(pp \rightarrow N_i N_i)\text{Br}(N_i \rightarrow e_j^\pm W^\mp)\text{Br}(N_i \rightarrow e_k^\pm W^\mp)\text{Br}(W \rightarrow jj)^2$$

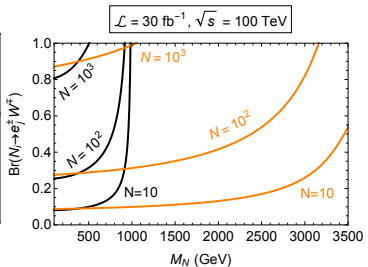
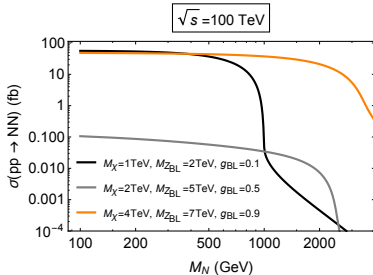


Lepton Number Violation at future colliders



$$pp \rightarrow Z_{BL}^* \rightarrow N_i N_i \rightarrow e_j^\pm W^\mp e_k^\pm W^\mp \rightarrow e_j^\pm e_k^\pm 4j$$

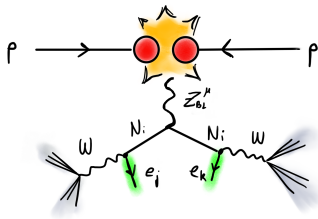
$$N_{e_j^\pm e_k^\pm 4j} = 2\mathcal{L}\sigma(pp \rightarrow N_i N_i)\text{Br}(N_i \rightarrow e_j^\pm W^\mp)\text{Br}(N_i \rightarrow e_k^\pm W^\mp)\text{Br}(W \rightarrow jj)^2$$



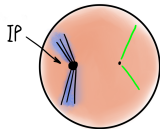
Consequences of a low B-L breaking scale

Low B-L scale ($v_{BL} \ll$)

$$M_{N_R} = \frac{\lambda_R}{\sqrt{2}} v_{BL} \rightarrow \text{Hope to see LNV signals at colliders!}$$

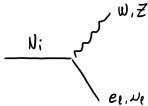


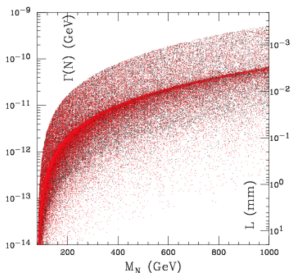
$$M_\nu = M_D^T M_R^{-1} M_D \sim \frac{Y_\nu^2 v_H^2}{M_{N_R}} \lesssim \text{eV} \Rightarrow Y_\nu \text{ small}$$



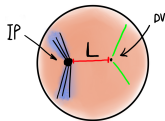
→ Displaced vertices!

Displaced vertices

- Total decay width of N :  $\Gamma_N^{\text{tot}} \sim |V_{li}|^2 \frac{M_{Ni}^3}{M_W^2}$
- Neutrino mixing: $|V_{li}|^2 \propto M_\nu / M_{NR}$, $M_{\nu N} = \begin{pmatrix} 0 & M_\nu \\ M_\nu & M_{NR} \end{pmatrix}$
- $\Gamma_{NR} \propto \frac{M_\nu M_N^2}{M_W} \sim \frac{\mathbf{Y}_\nu v_H M_N^2}{v_H^2} \Rightarrow \tau_{NR} \gg \rightarrow$ Long-lived particles



As an example: $M_N \sim 400$ GeV
 $\Rightarrow L = (10^{-3} - 10^{-1})$ mm



Summary

- We present a simple theory based on $U(1)_{B-L}$, which is the simplest and natural **connection between neutrino masses and dark matter**.
- This simple theory predicts an **upper bound** for the new $B - L$ scale of the order of 100 TeV.
- Therefore, there is hope to test the theory at colliders! Consequences of a **low $B - L$ scale**:
 - Low M_N : we have studied the main **lepton number violating signals** at the LHC and future colliders.
 - Tiny Y_ν : exotic signals of **displaced vertices** are expected.

Thanks for your attention!