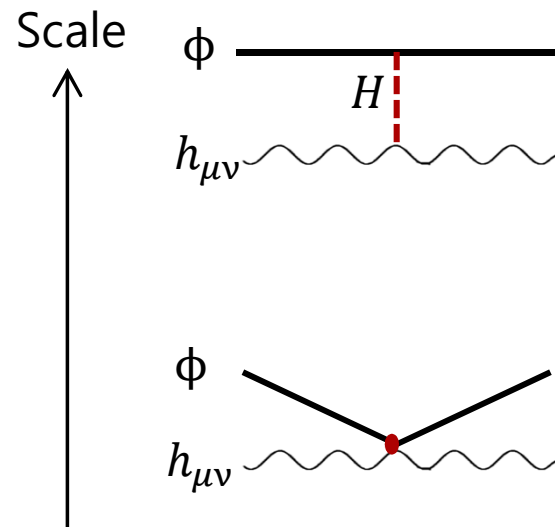


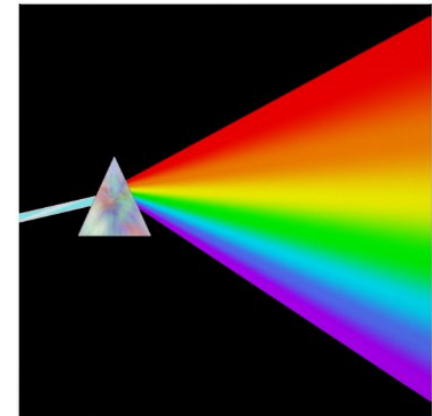
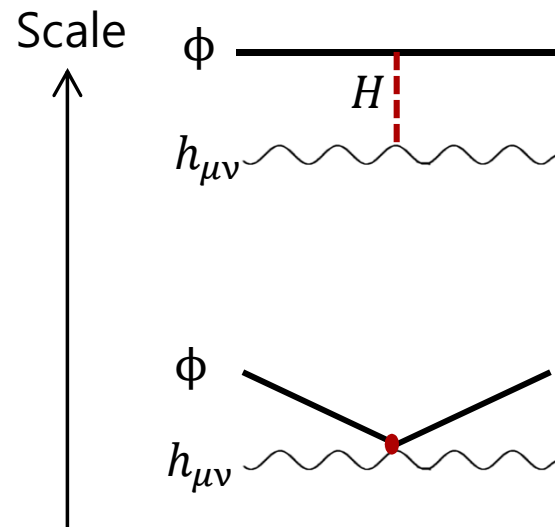
Speed Limits from Gravitational Waves

Scott Melville



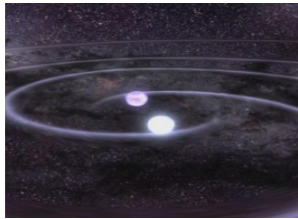
Speed Limits from Gravitational Waves

Scott Melville

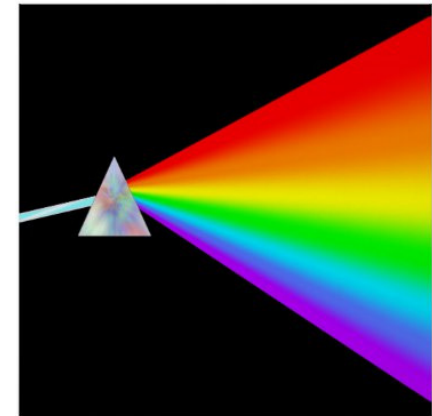
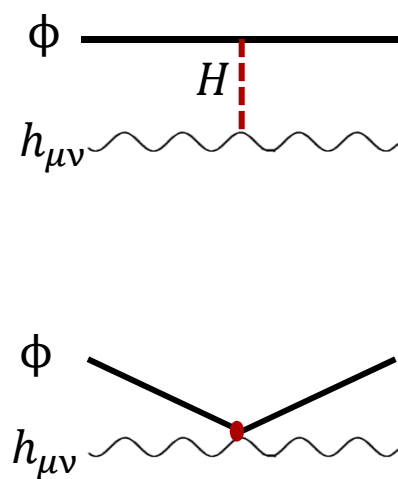


Speed Limits from Gravitational Waves

Scott Melville



Scale
↑



- Scale Dependence
- GW170817 Constraints
- The Future



- Scale Dependence
- GW170817 Constraints
- The Future

UV physics causes IR running



- Scale Dependence
- GW170817 Constraints
- The Future

UV physics causes IR running

$1 - c_T^2$ depends on scale!



- Scale Dependence
 - GW170817 Constraints
 - The Future
- UV physics causes IR running
- $1 - c_T^2$ depends on scale!
- Dark energy after GW170817



SCALE

Dependence

IR

UV



IR

UV



IR

UV



$\sim \frac{\Lambda^2}{k^2 - \Lambda^2}$

IR

UV

 $h_{\mu\nu}$ ϕ H 

Massless

Mass $\ll \Lambda$ Mass $\sim \Lambda$

$$\sum \text{[Diagram: two external lines meeting at a vertex with a red star] } \sim \sum \left(\frac{k^2}{\Lambda^2} \right)^n$$

$$\text{[Diagram: two external lines connected by a dashed internal line] } \sim \frac{\Lambda^2}{k^2 - \Lambda^2}$$

IR

UV



$h_{\mu\nu}$

ϕ

H



Massless

Mass $\ll \Lambda$

Mass $\sim \Lambda$

$$\sum \text{[Diagram: two external lines meeting at a vertex with a red star]} \sim \sum \left(\frac{k^2}{\Lambda^2} \right)^n$$

$$\text{[Diagram: two external lines connected by a dashed line]} \sim \frac{\Lambda^2}{k^2 - \Lambda^2}$$

$$\text{[Diagram: two external lines connected by a dashed line, with vertices marked with crosses and labeled $\langle \phi \rangle$]} \sim c_T^{UV}$$

IR

UV



$h_{\mu\nu}$

ϕ

H



Massless

Mass $\ll \Lambda$

Mass $\sim \Lambda$

$$\sum \text{[Diagram: graviton exchange between two wavy lines]} \sim \sum \left(\frac{k^2}{\Lambda^2} \right)^n$$

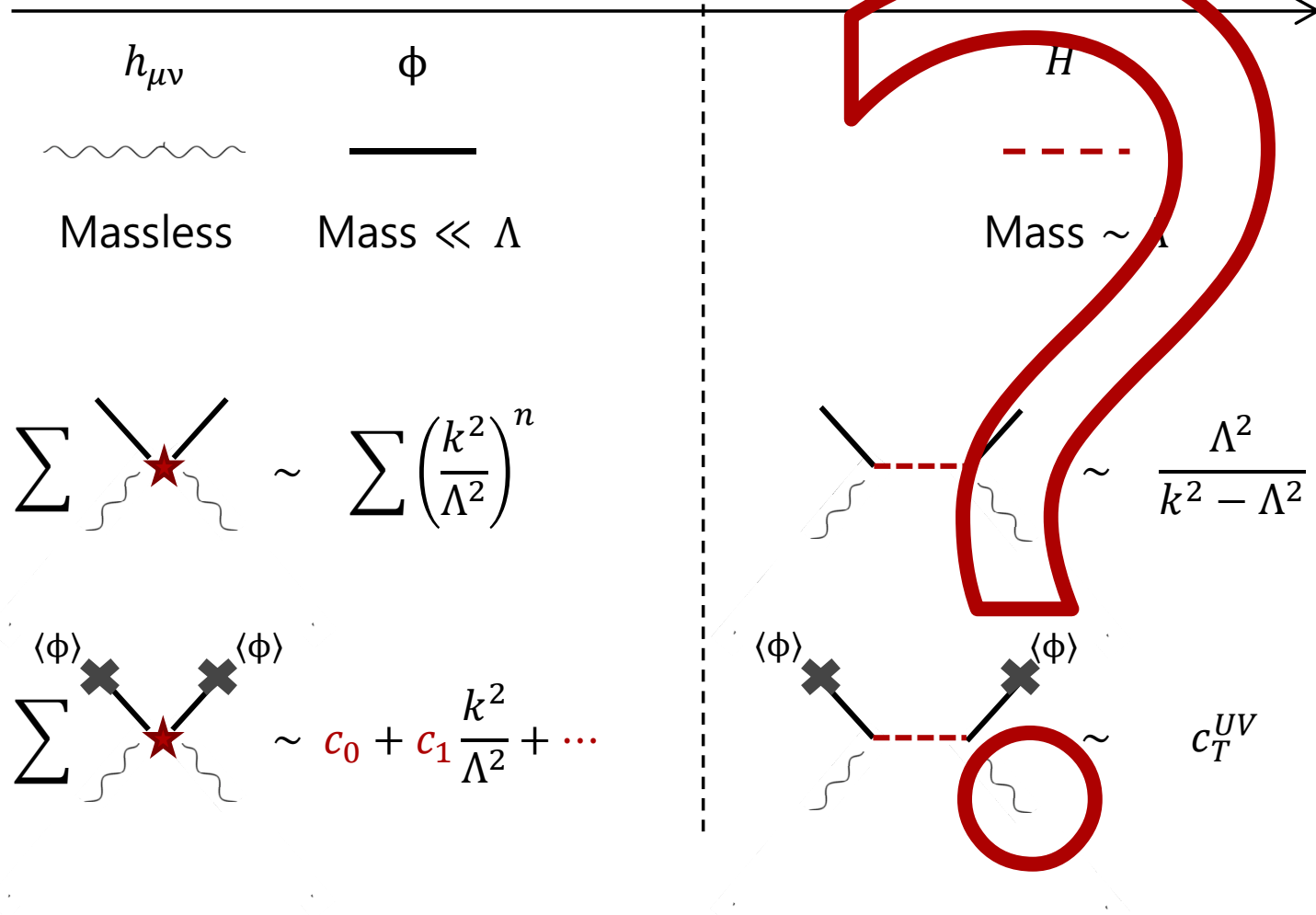
$$\text{[Diagram: Higgs exchange between two wavy lines]} \sim \frac{\Lambda^2}{k^2 - \Lambda^2}$$

$$\sum \text{[Diagram: graviton exchange with external scalar fields]} \sim c_0 + c_1 \frac{k^2}{\Lambda^2} + \dots$$

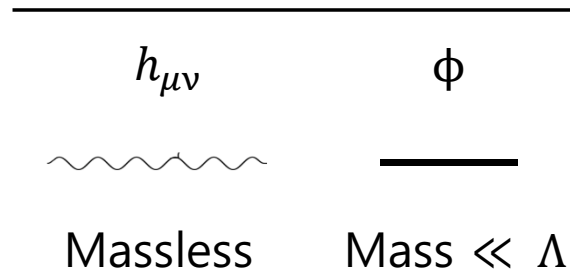
$$\text{[Diagram: Higgs exchange with external scalar fields]} \sim c_T^{UV}$$

IR

UV



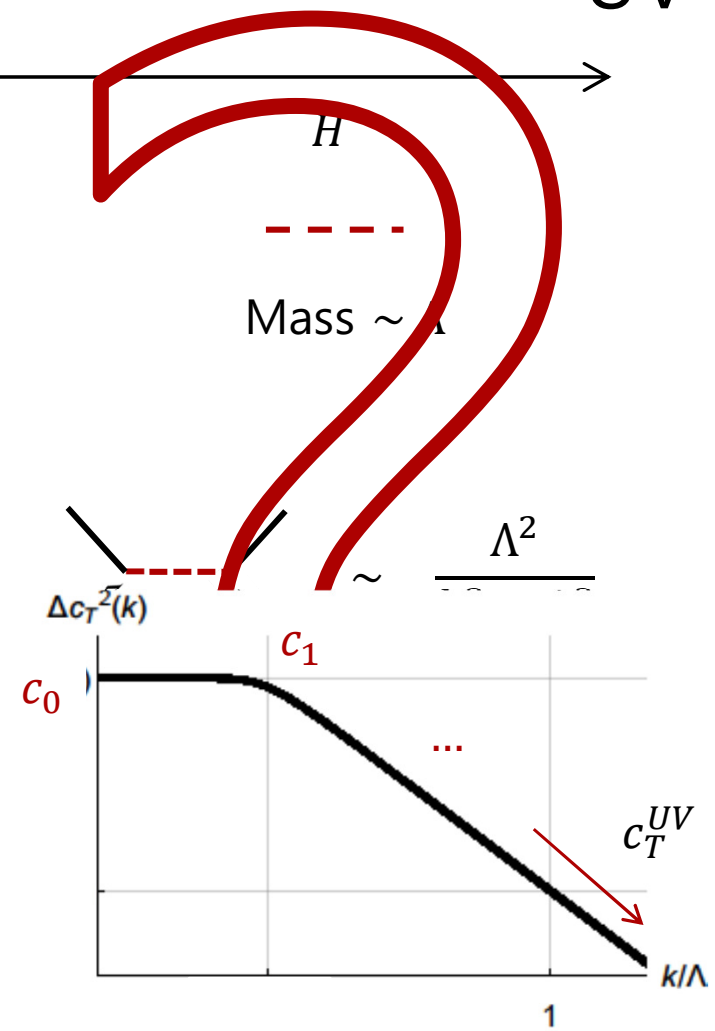
IR



$$\sum \text{[Diagram: wavy line with star] } \sim \sum \left(\frac{k^2}{\Lambda^2} \right)^n$$

$$\sum \text{[Diagram: wavy line with star and vertices] } \sim c_0 + c_1 \frac{k^2}{\Lambda^2} + \dots$$

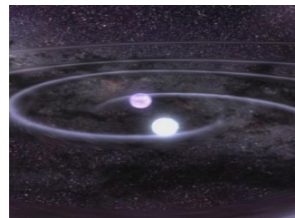
UV



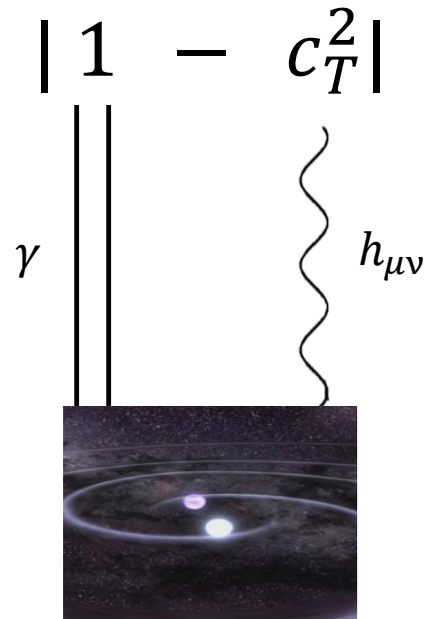
GW170817

Multi-messenger Signal

Merger



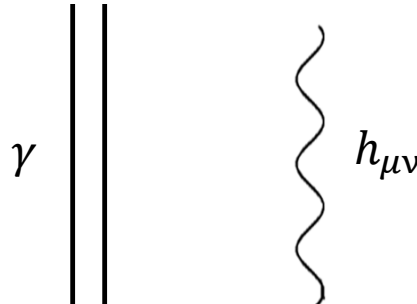
Multi-messenger Signal



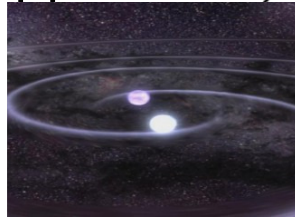
Merger

Multi-messenger Signal

$$\Delta c_T^2 = |1 - c_T^2| < 10^{-15}$$

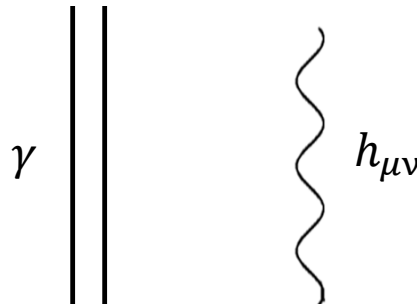


Merger



Multi-messenger Signal

$$\Delta c_T^2 = |1 - c_T^2| < 10^{-15}$$

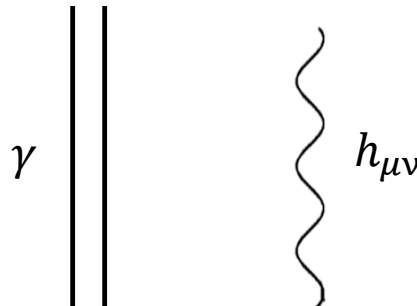


Merger

 $\approx 50\text{Hz}$ 

Multi-messenger Signal

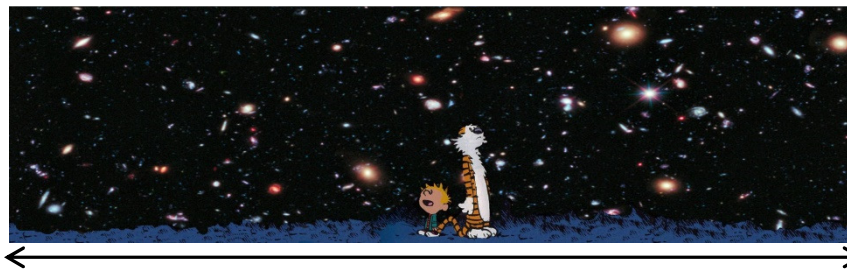
$$\Delta c_T^2 = |1 - c_T^2| < 10^{-15}$$



Merger

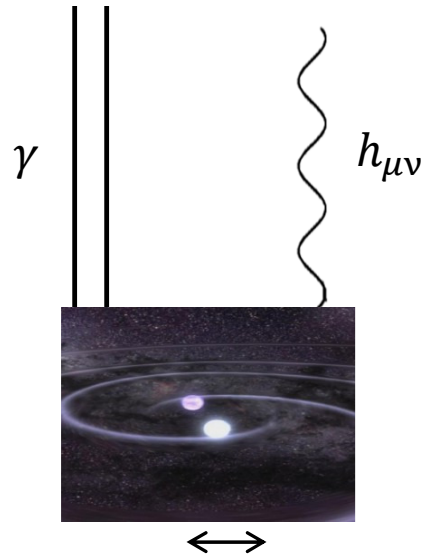
 $\approx 50\text{Hz}$ 

Cosmology

 10^{-18} Hz

Multi-messenger Signal

$$\Delta c_T^2(50\text{Hz}) = |1 - c_T^2(50\text{Hz})| < 10^{-15}$$



Merger

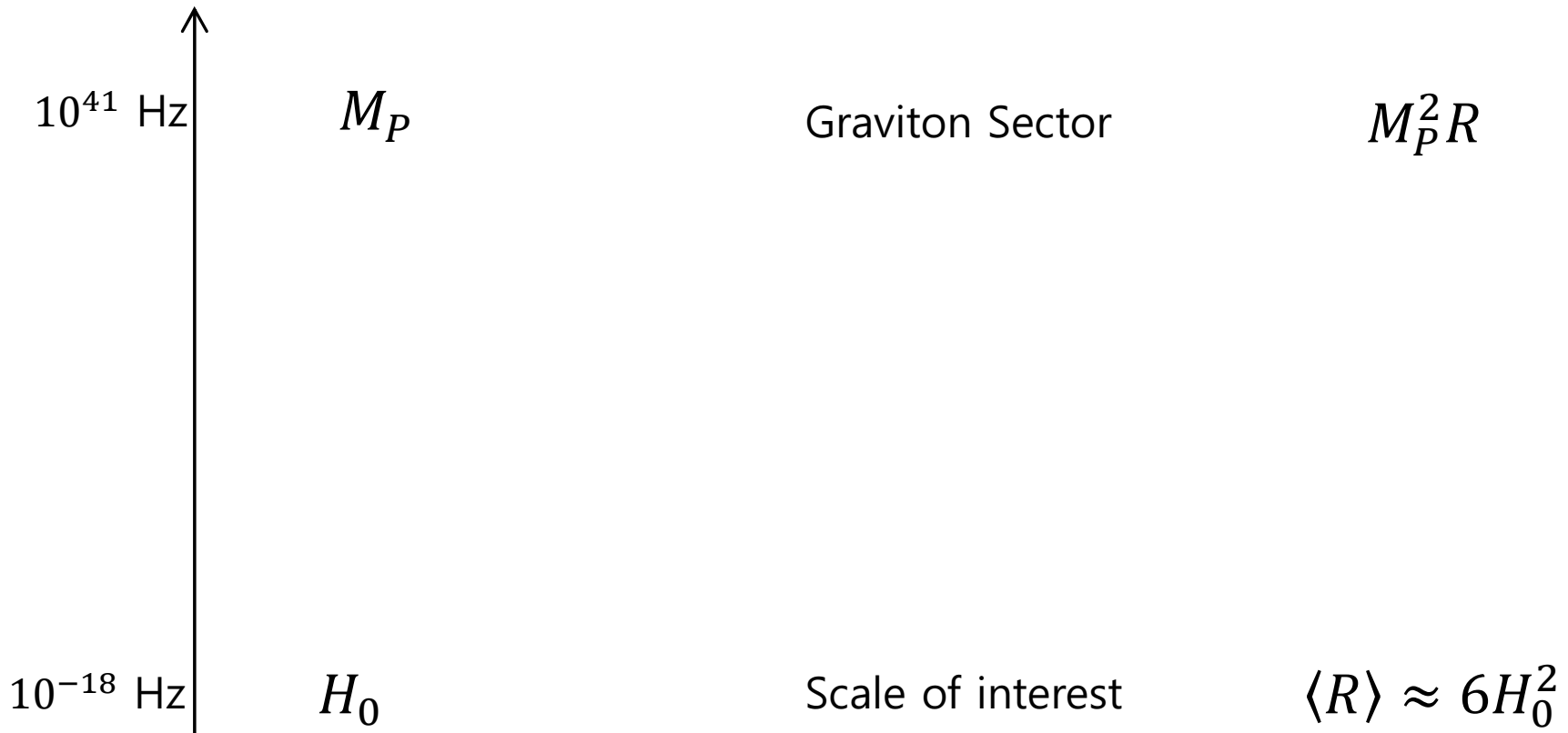
 $\approx 50\text{Hz}$

Cosmology

 10^{-18} Hz

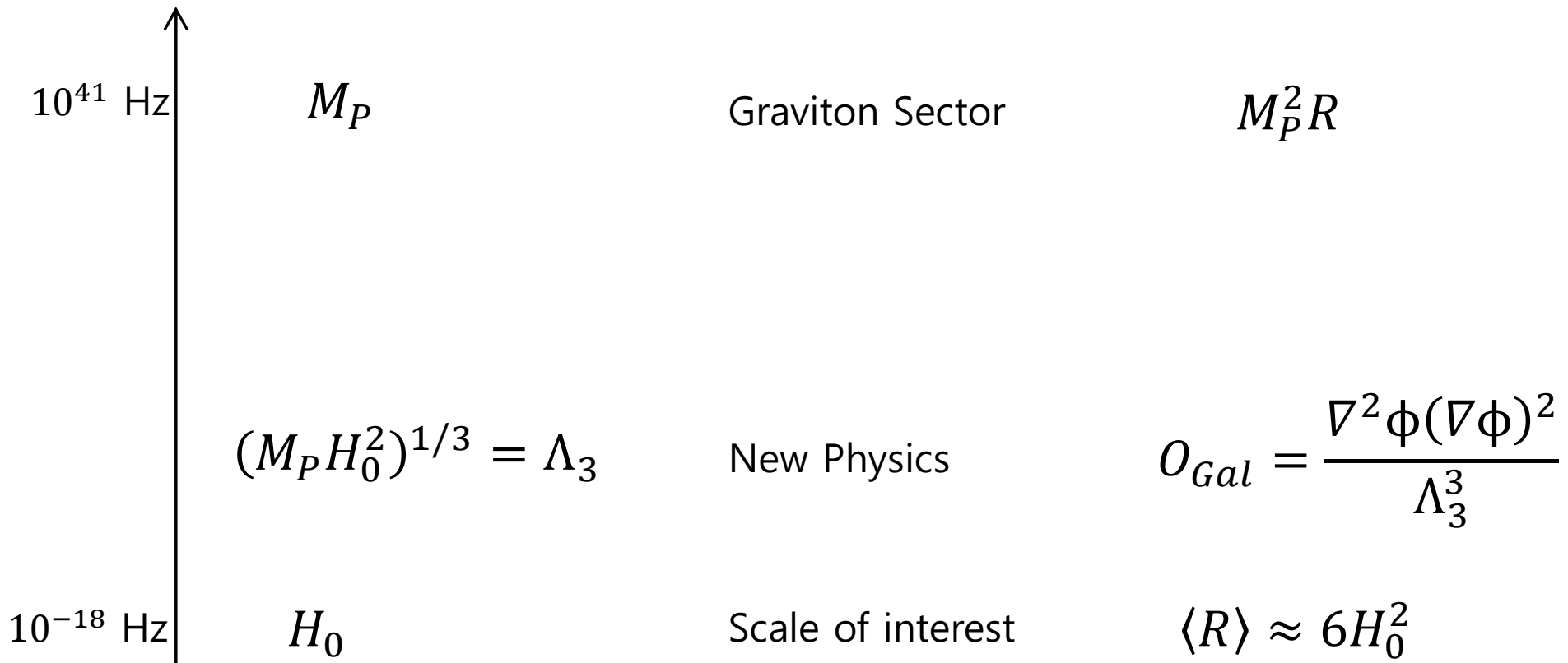
Dark Energy

Scales



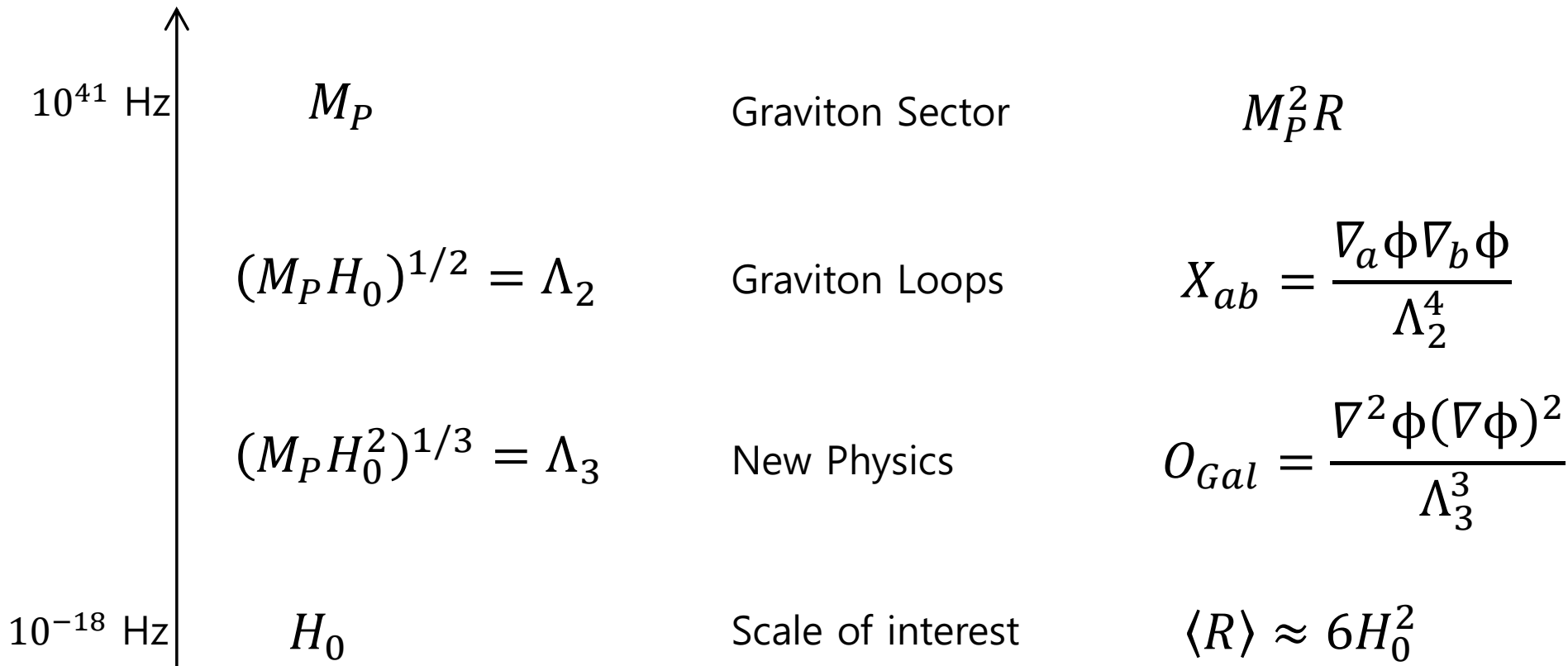
Dark Energy

Scales



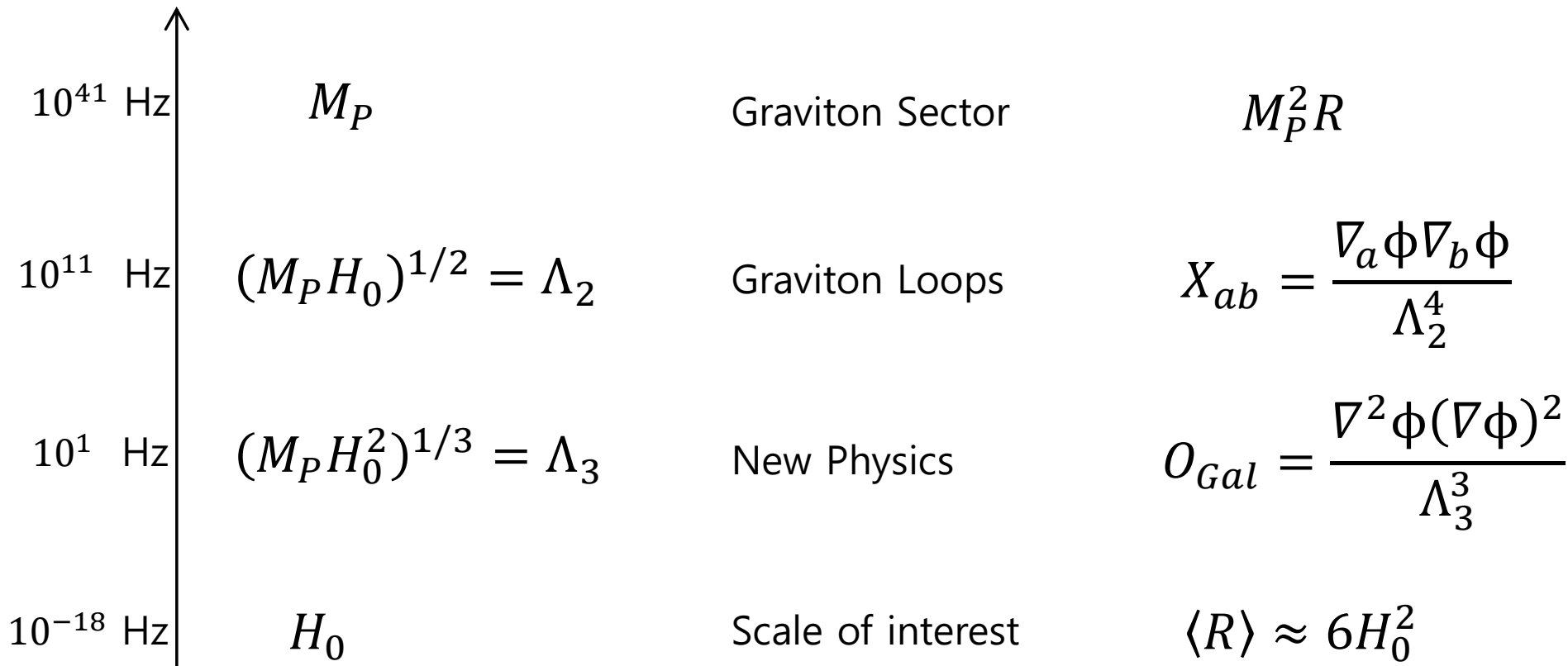
Dark Energy

Scales



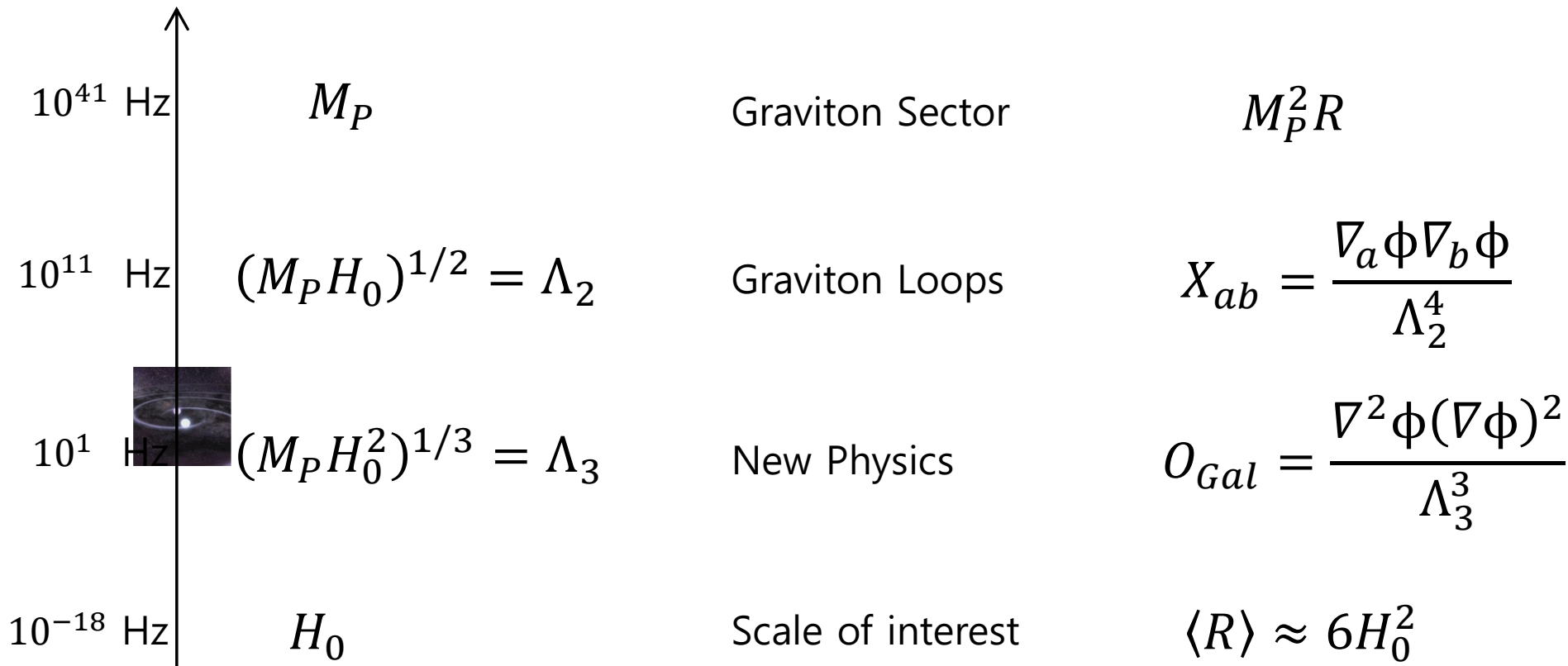
Dark Energy

Scales



Dark Energy

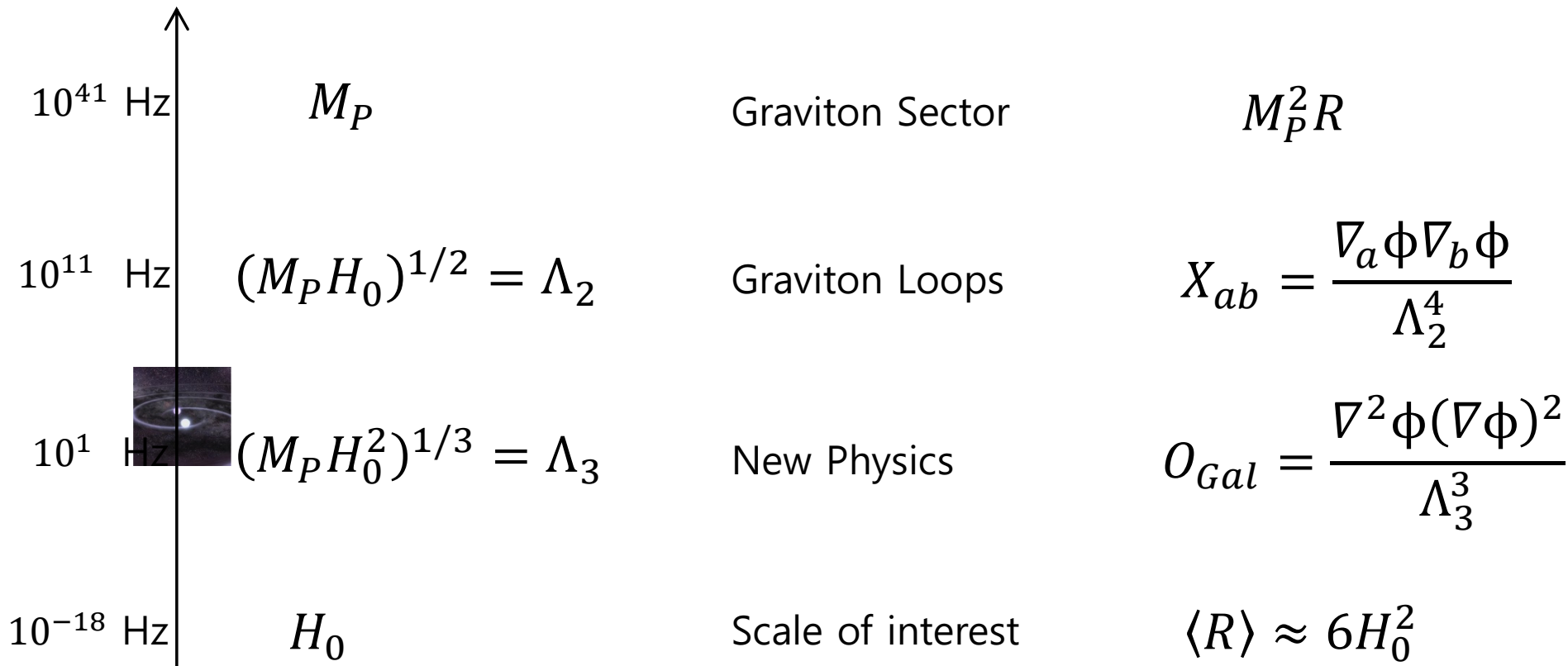
Scales



Dark Energy

$$M_P^2 R \quad X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4} \quad \frac{\nabla_a}{\Lambda_3}$$

Scales



Dark Energy

$$M_P^2 R \quad X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4} \quad \frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT

$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4} \quad \frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT

$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT

$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$\Delta c_T^2(50\text{Hz}) = 2 c_0$$

Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT

$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$\Delta c_T^2(50\text{Hz}) = 2 c_0$$

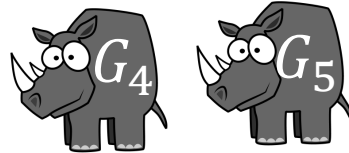
$$< 10^{-15}$$

Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4} \quad \frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$\Delta c_T^2(50\text{Hz}) = 2 c_0 < 10^{-15}$$

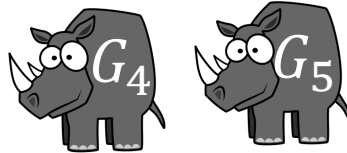
Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$\Delta c_T^2(50\text{Hz}) = 2 c_0$$

$$< 10^{-15}$$



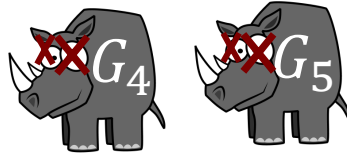
Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$\Delta c_T^2(50\text{Hz}) = 2 c_0$$

$$< 10^{-15}$$

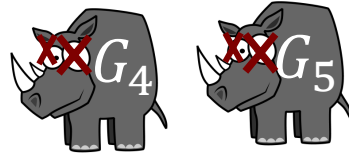


Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4} \quad \frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$+ O\left(\frac{\nabla^2}{\Lambda_3^2}\right)$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$+ O\left(\frac{k^2}{\Lambda_3^2}\right)$$

$$\Delta c_T^2(50\text{Hz}) = 2c_0 + O(1)$$

$$< 10^{-15}$$



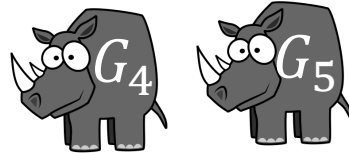
Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$+ O\left(\frac{\nabla^2}{\Lambda_3^2}\right)$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$+ O\left(\frac{k^2}{\Lambda_3^2}\right)$$

$$\Delta c_T^2(50\text{Hz}) = 2c_0 + O(1)$$

$$< 10^{-15}$$



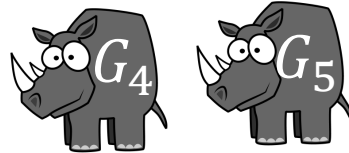
Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$+ M_P^2 \left[c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac} \right]$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$+ 4 c_0 c_2 \frac{k^2}{\Lambda_3^2}$$

$$\Delta c_T^2(50\text{Hz}) = 2c_0 + 4c_0 c_2$$

$$< 10^{-15}$$



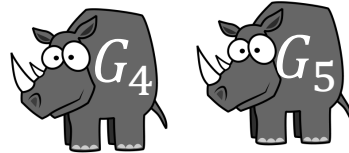
Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$+ M_P^2 \left[c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac} \right]$$

$$+ O\left(\frac{\nabla^4}{\Lambda_3^4}\right)$$

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$+ 4 c_0 c_2 \frac{k^2}{\Lambda_3^2}$$

$$+ O\left(\frac{k^4}{\Lambda_3^4}\right)$$

$$\Delta c_T^2(50\text{Hz}) = 2c_0 + 4c_0 c_2 + O(1) < 10^{-15}$$



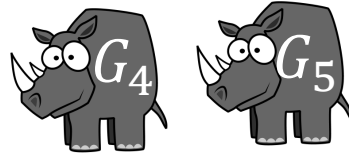
Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$+ M_P^2 \left[c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac} \right]$$

+ ...

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$+ 4 c_0 c_2 \frac{k^2}{\Lambda_3^2}$$

$$+ \sum c_n \left(\frac{k^2}{\Lambda_3^2} \right)^n$$

$$\Delta c_T^2(50\text{Hz}) \approx 2c_0 + 4c_0 c_2 + \sum_{n=2}^{\infty} c_n < 10^{-15}$$



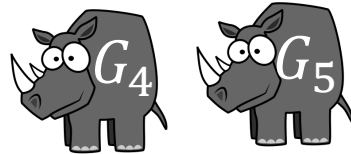
Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$+ M_P^2 \left[c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac} \right]$$

+ ...

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$+ 4 c_0 c_2 \frac{k^2}{\Lambda_3^2}$$

$$+ \sum c_n \left(\frac{k^2}{\Lambda_3^2} \right)^n$$

$$\Delta c_T^2(50\text{Hz}) \approx 2c_0 + 4c_0 c_2 + \sum_{n=2}^{\infty} c_n < 10^{-15}$$

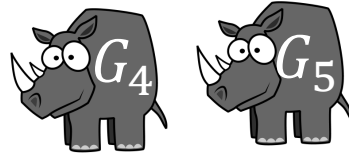
Dark Energy

$$M_P^2 R$$

$$X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4}$$

$$\frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$+ M_P^2 \left[c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R \right]$$

+ ...

At least
we're not all
dead!

Natalie Dee.com

$$\Delta c_T^2(k^2) \approx 2 c_0$$

$$+ 4 c_0 c_2 \frac{k^2}{\Lambda_3^2}$$

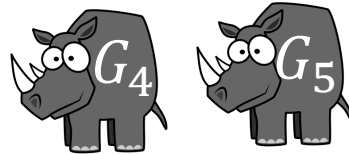
$$+ \sum c_n \left(\frac{k^2}{\Lambda_3^2} \right)^n$$

$$\Delta c_T^2(50\text{Hz}) \approx 2c_0 + 4c_0 c_2 + \sum_{n=2}^{\infty} c_n < 10^{-15}$$

Dark Energy

$$M_P^2 R \quad X_{ab} = \frac{\nabla_a \phi \nabla_b \phi}{\Lambda_2^4} \quad \frac{\nabla_a}{\Lambda_3}$$

Horndeski EFT



$$\mathcal{L}_{hh} = M_P^2 [R - c_0 R^{ab} X_{ab}]$$

$$+ M_P^2 \left[c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R \right]$$

At least we're not all dead!

$$\Delta c_T^2(k^2) \approx 2 c_0$$

Hmm...



$$\approx c_2 \frac{k^2}{\Lambda_3^2}$$

$$\approx c_n \left(\frac{k^2}{\Lambda_3^2} \right)^n$$

$$\Delta c_T^2(50\text{Hz}) \approx 2c_0 + 4c_0 c_2 + \sum_{n=2}^{\infty} c_n < 10^{-15}$$

Dark Energy

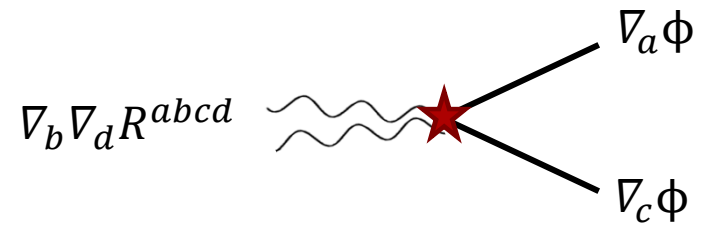
Partial

UV Completion

Dark Energy

Partial
UV Completion

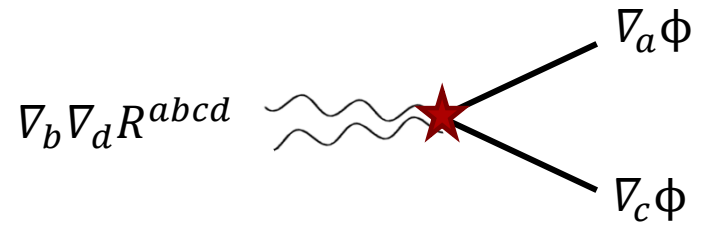
$$c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac}$$



Dark Energy

Partial
UV Completion

$$c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac}$$



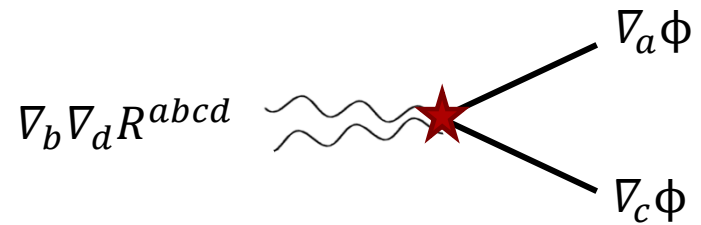
$$(\nabla_c H_{ab})^2 - \Lambda_3^2 H^{ab} H_{ab}$$

$$H_{ab} \text{ --- } H_{ab}$$

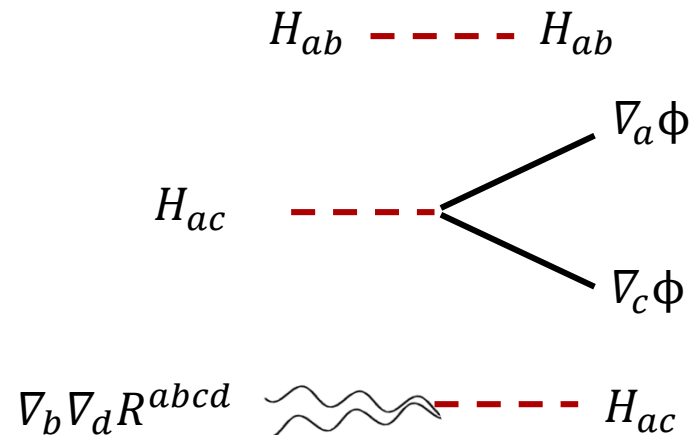
Dark Energy

Partial
UV Completion

$$c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac}$$



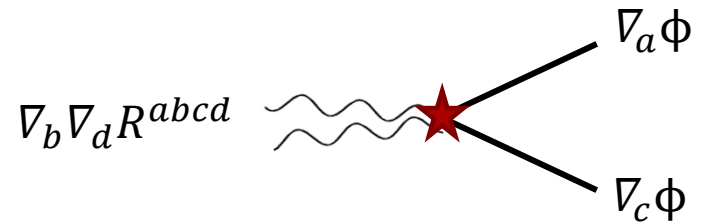
$$(\nabla_c H_{ab})^2 - \Lambda_3^2 H^{ab} H_{ab}$$



Dark Energy

Partial
UV Completion

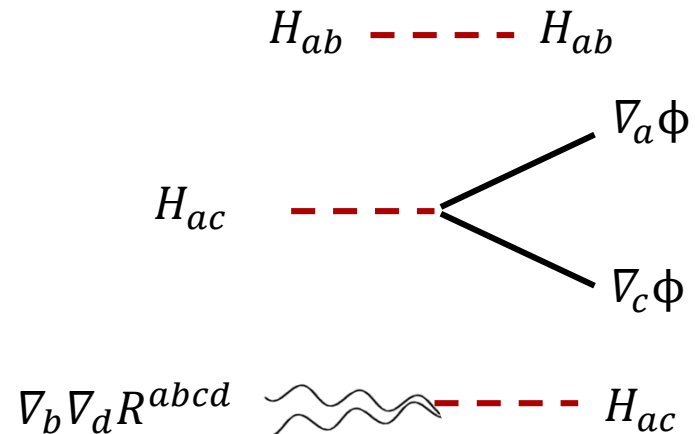
$$c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac}$$



$$(\nabla_c H_{ab})^2 - \Lambda_3^2 H^{ab} H_{ab}$$

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi$$

$$\frac{\alpha_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$



Dark Energy

Partial
UV Completion

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi \quad \frac{\alpha_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$

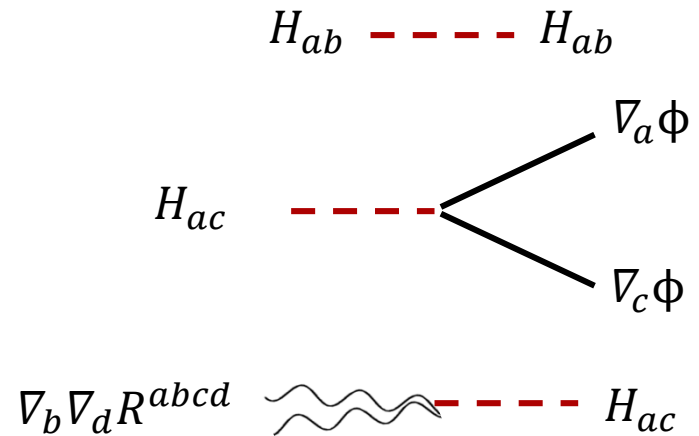
$$c_2 \frac{\nabla_b \nabla_d}{\Lambda_3^2} R^{abcd} X_{ac}$$



$$(\nabla_c H_{ab})^2 - \Lambda_3^2 H^{ab} H_{ab}$$

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi$$

$$\frac{\alpha_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$



Dark Energy

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi$$

$$\frac{a_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$

Dark Energy

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi$$

$$\frac{a_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$

Any IR sound speed can be made consistent with GW170817 by a suitable choice of UV parameters

Dark Energy

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi \quad \frac{a_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$

Any IR sound speed can be made consistent with GW170817 by a suitable choice of UV parameters

$$\Delta c_T^2(0) \approx 2 \frac{\Lambda_3^2}{\Lambda_*^2}$$

$$\Delta c_T^2(\Lambda_3) \approx \frac{\Lambda_3^2 \Lambda_*^2}{a_R \Lambda_2^4} < 10^{-15}$$

Dark Energy

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi \quad \frac{a_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$

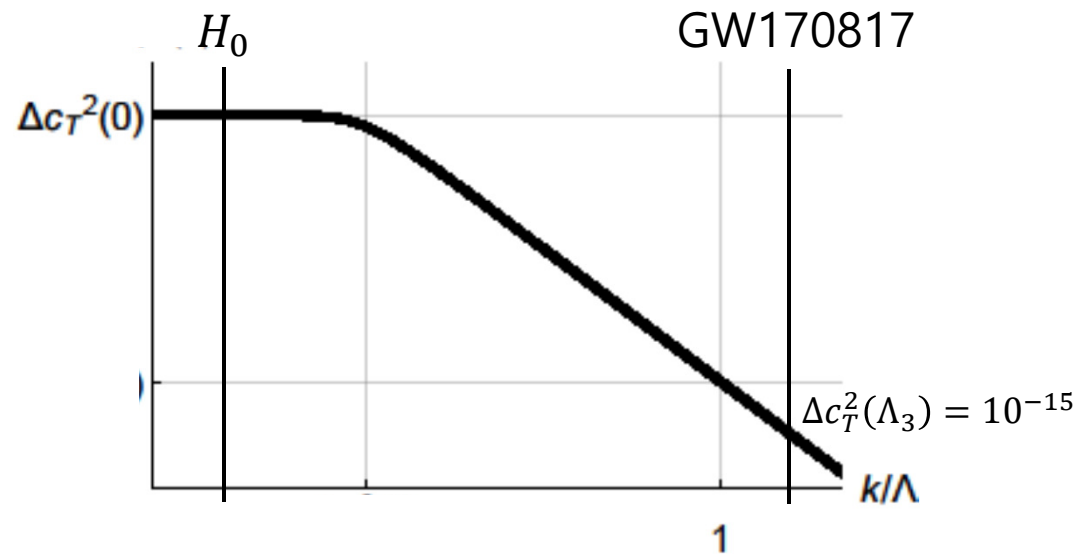
Any IR sound speed can be made consistent with GW170817 by a suitable choice of UV parameters

$$\Delta c_T^2(0) \approx 2 \frac{\Lambda_3^2}{\Lambda_*^2}$$

$$\Delta c_T^2(\Lambda_3) \approx \frac{\Lambda_3^2 \Lambda_*^2}{a_R \Lambda_2^4} < 10^{-15}$$

For example,

$$a_R = 10^{-25} \frac{\Lambda_*^2}{\Lambda_3^2}$$



Dark Energy

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi$$

$$\frac{a_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$

Any IR sound speed can be made consistent with GW170817 by a suitable choice of UV parameters

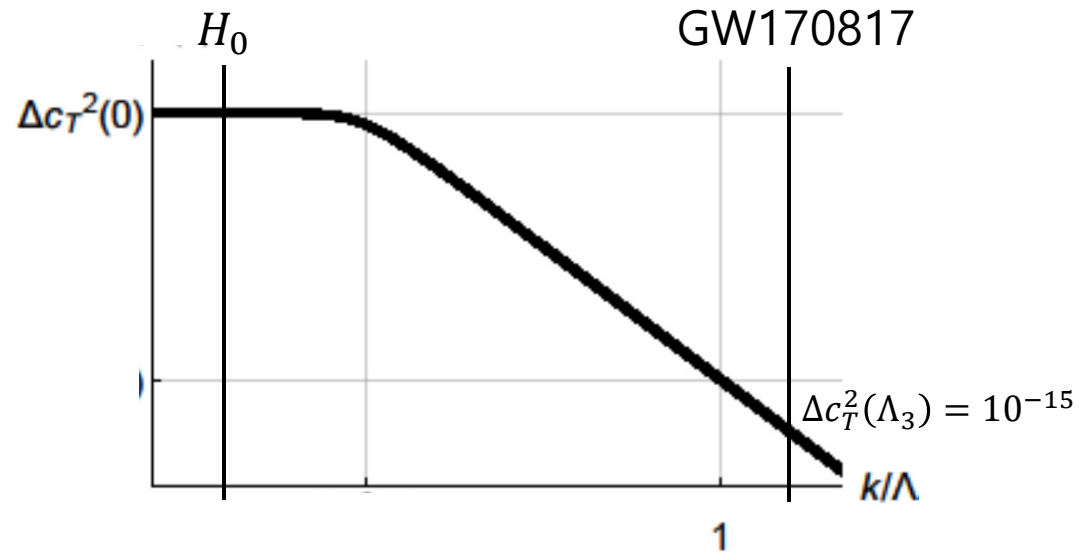
$$\Delta c_T^2(0) \approx 2 \frac{\Lambda_3^2}{\Lambda_*^2}$$

$$\Delta c_T^2(\Lambda_3) \approx \frac{\Lambda_3^2 \Lambda_*^2}{a_R \Lambda_2^4} < 10^{-15}$$

For example,

$$a_R = 10^{-25} \frac{\Lambda_*^2}{\Lambda_3^2}$$

Vary Λ_* to get desired $\Delta c_T^2(0)$



Dark Energy

$$\frac{1}{\Lambda_*} H^{ac} \nabla_a \phi \nabla_c \phi \quad \frac{a_R M_P^2}{\Lambda_*^3} \nabla_b \nabla_d R^{abcd} H_{ac}$$

Any IR sound speed can be made consistent with GW170817 by a suitable choice of UV parameters

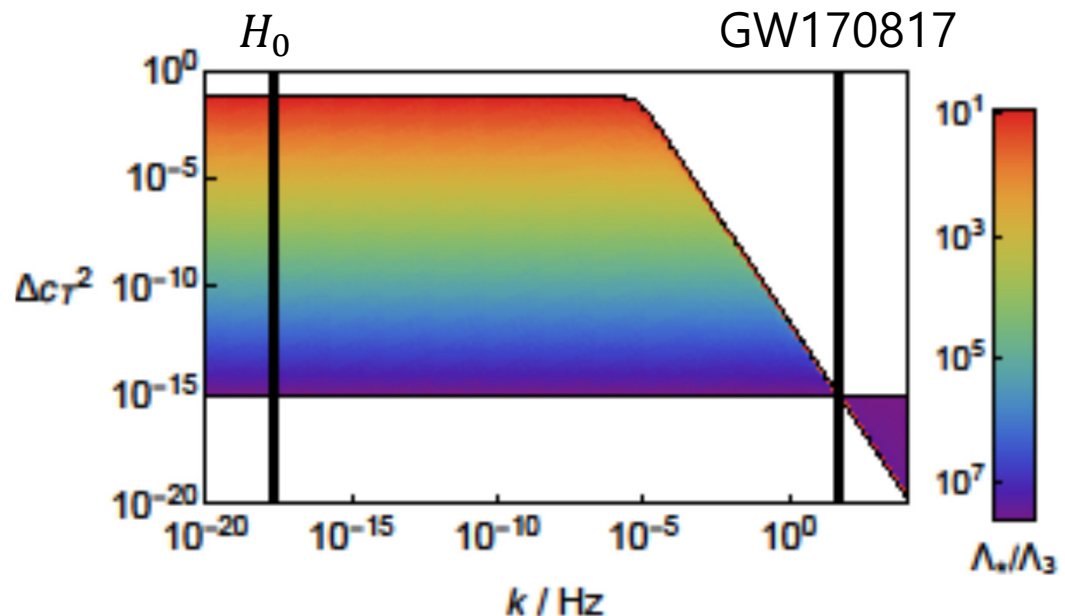
$$\Delta c_T^2(0) \approx 2 \frac{\Lambda_3^2}{\Lambda_*^2}$$

$$\Delta c_T^2(\Lambda_3) \approx \frac{\Lambda_3^2 \Lambda_*^2}{a_R \Lambda_2^4} < 10^{-15}$$

For example,

$$a_R = 10^{-25} \frac{\Lambda_*^2}{\Lambda_3^2}$$

Vary Λ_* to get desired $\Delta c_T^2(0)$



The Future

Theory

Experiment

Theory

$$\mathcal{L}_{EFT} = \mathcal{L}_{LO} + \mathcal{L}_{NLO} + \dots$$

Experiment

Theory

e.g.

$$\mathcal{L}_{EFT} = \text{Horndeski } \mathcal{L}_{LO} + \text{Higher Derivatives } \mathcal{L}_{NLO} + \dots$$

Experiment

Theory

e.g.

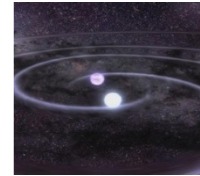
Horndeski

Higher Derivatives

$$\mathcal{L}_{EFT} = \mathcal{L}_{LO} + \mathcal{L}_{NLO} + \dots$$



Cosmology



Mergers

Experiment

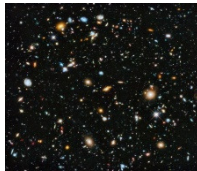
Theory

e.g.

Horndeski

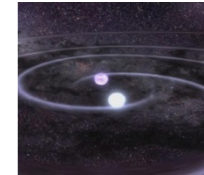
Higher Derivatives

$$\mathcal{L}_{EFT} = \mathcal{L}_{LO} + \mathcal{L}_{NLO} + \dots$$



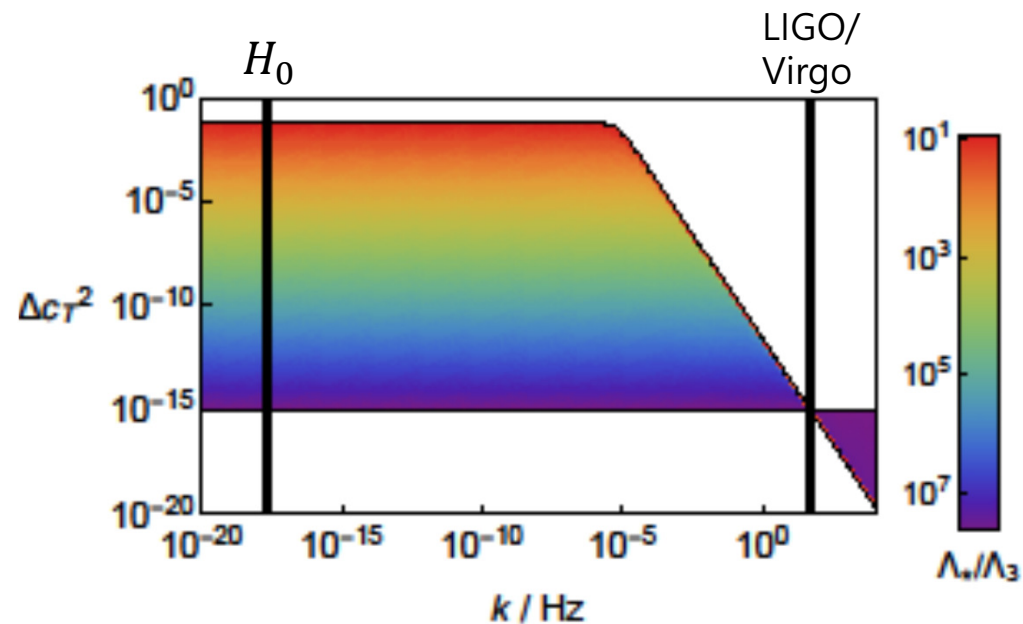
Cosmology

Mergers



Experiment

Lower energy
measurements



Theory

e.g.

Horndeski

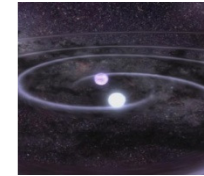
Higher Derivatives

$$\mathcal{L}_{EFT} = \mathcal{L}_{LO} + \mathcal{L}_{NLO} + \dots$$



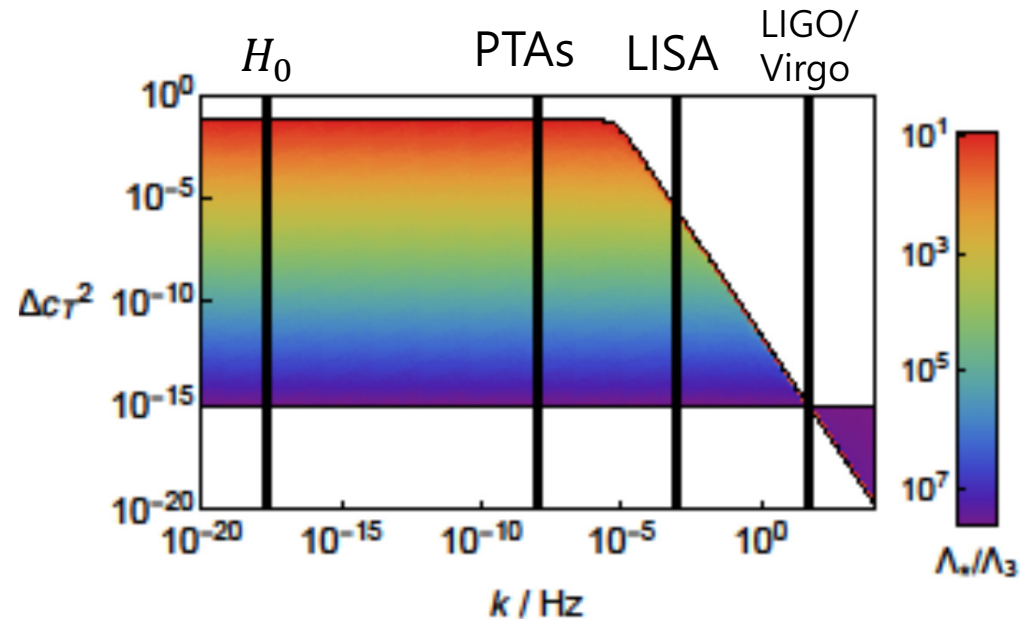
Cosmology

Mergers



Experiment

Lower energy
measurements



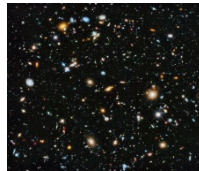
Theory

e.g.

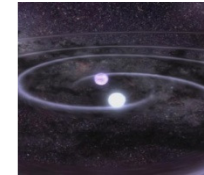
Horndeski

Higher Derivatives

$$\mathcal{L}_{EFT} = \mathcal{L}_{LO} + \mathcal{L}_{NLO} + \dots$$



Cosmology

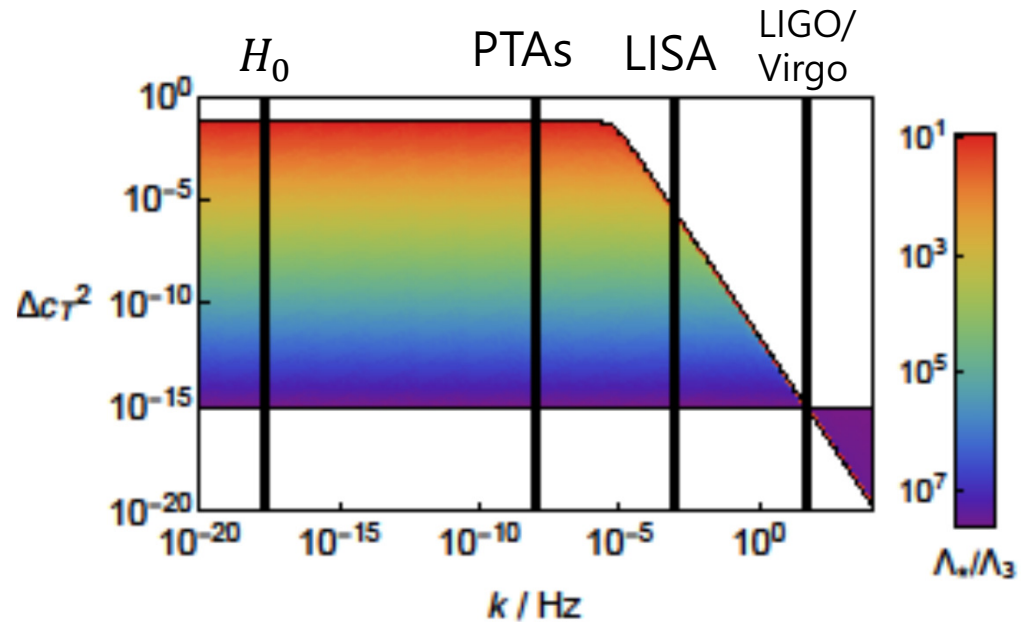
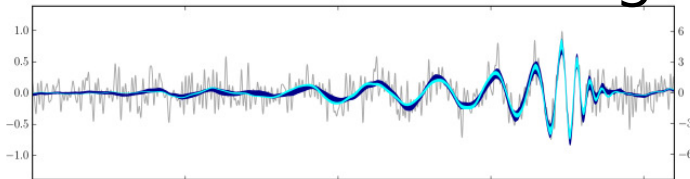


Mergers

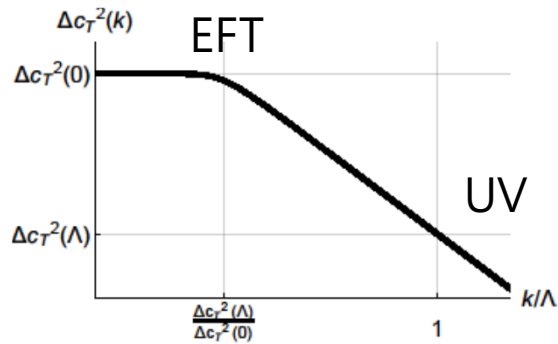
Experiment

Lower energy measurements

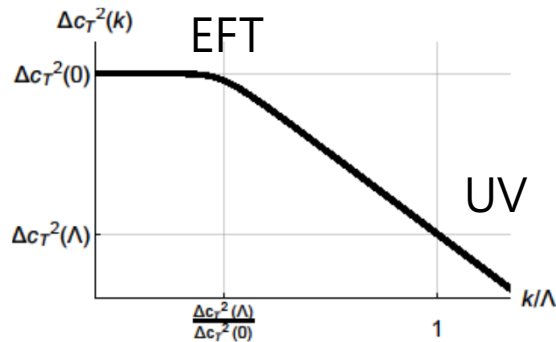
'Rainbow' stretching



Summary



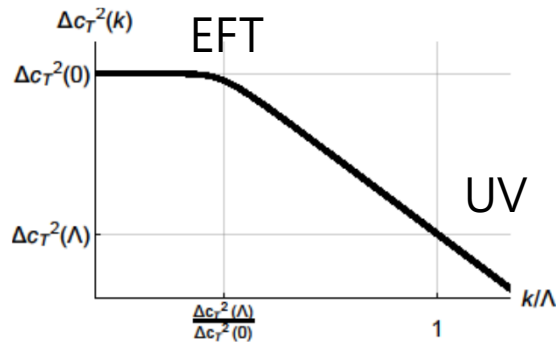
Only **low energy** measurements constrain **EFT** parameters!



Only **low energy** measurements constrain **EFT** parameters!

$$\Delta c_T^2(50\text{Hz}) < 10^{-15} \quad \Rightarrow \quad \sum_n c_n \left(\frac{50\text{Hz}}{\Lambda_3} \right)^n < 10^{-15} \quad \text{in EFT}$$

$$a_2 \left(\frac{50\text{Hz}}{\Lambda_*} \right)^2 + \dots < 10^{-15} \quad \text{in 'UV'}$$



Only **low energy** measurements constrain **EFT** parameters!

$$\Delta c_T^2(50\text{Hz}) < 10^{-15} \Rightarrow \sum_n c_n \left(\frac{50\text{Hz}}{\Lambda_3}\right)^n < 10^{-15} \quad \text{in EFT}$$

$$a_2 \left(\frac{50\text{Hz}}{\Lambda_*}\right)^2 + \dots < 10^{-15} \quad \text{in 'UV'}$$

$$1 \gtrsim \Delta c_T^2(H_0) > \Delta c_T^2(\text{LISA}) > \Delta c_T^2(\text{LIGO}) \gtrsim 0$$

