

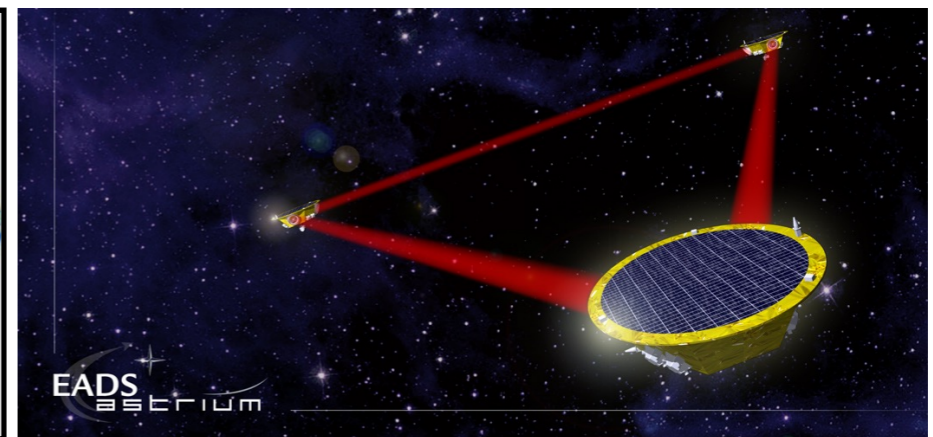
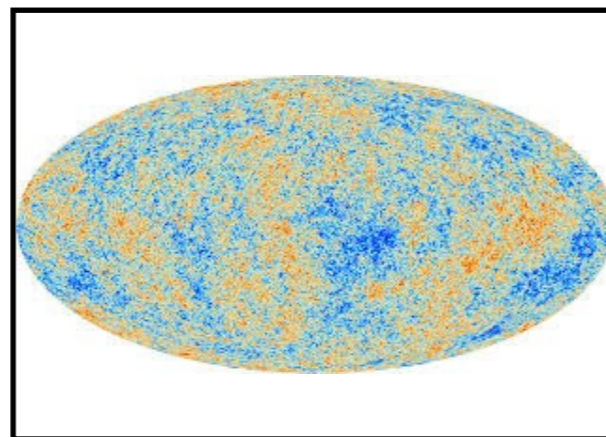
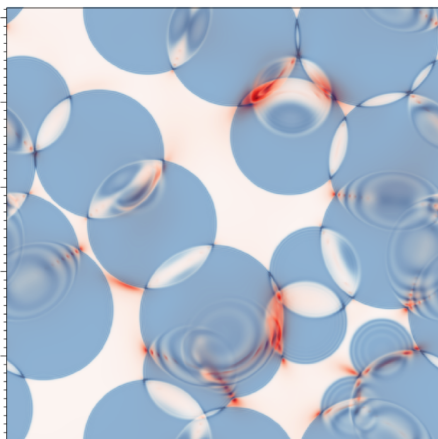
# Anisotropies in the Gravitational Wave

## Background from Cosmological Phase Transitions

Michael Geller

University of Maryland and TAU

arXiv:1803.10780 M. G., Anson Hook, Raman Sundrum, Yuhsin Tsai



# Gravitational Wave (GW) Cosmology

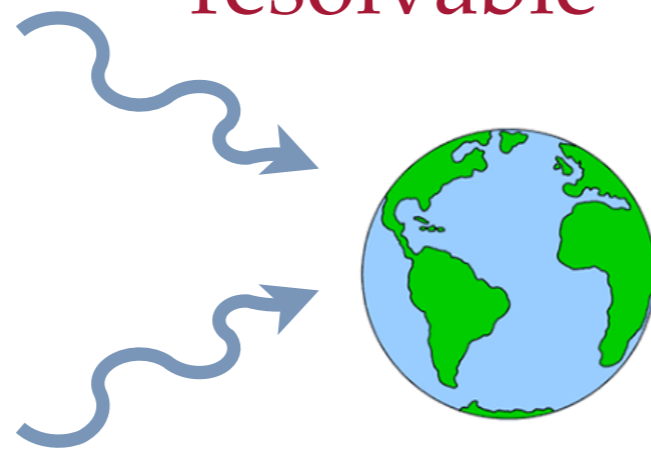
Different sources of GW in the sky

## Astrophysical sources

black hole, neutron star, white dwarf mergers



resolvable



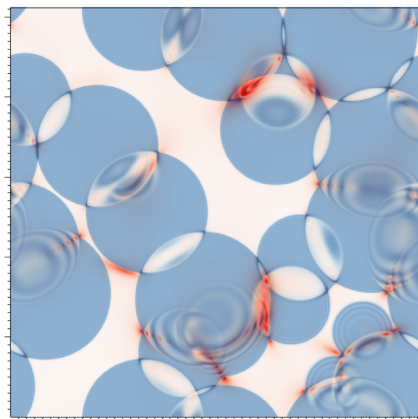
Study physics of  
gravity, astro dynamics,  
QCD,

# Gravitational Wave (GW) Cosmology

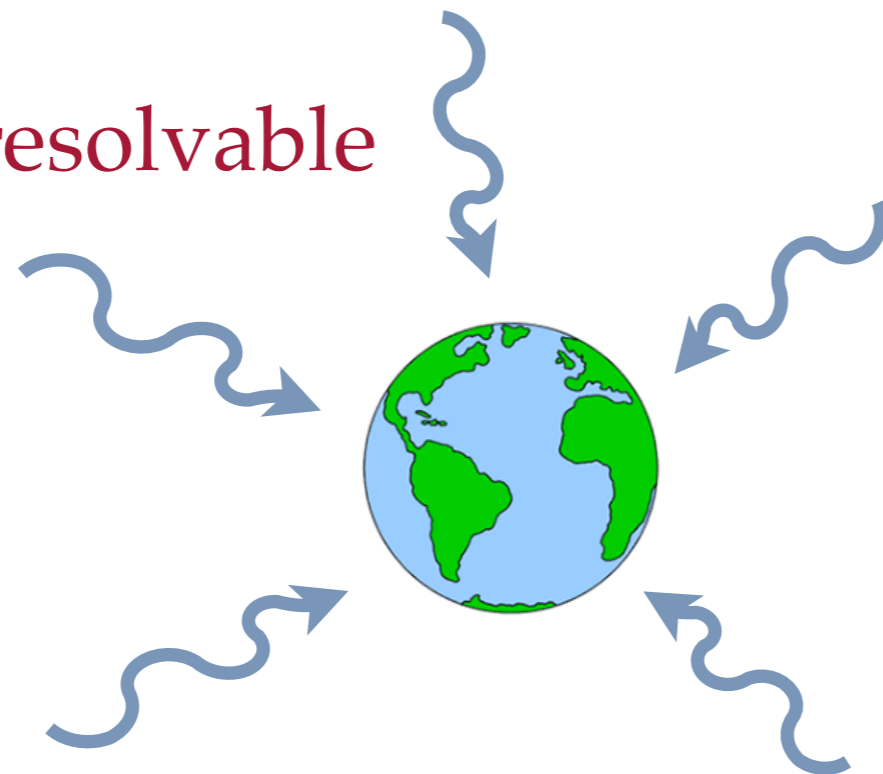
Different sources of GW in the sky

Cosmological sources

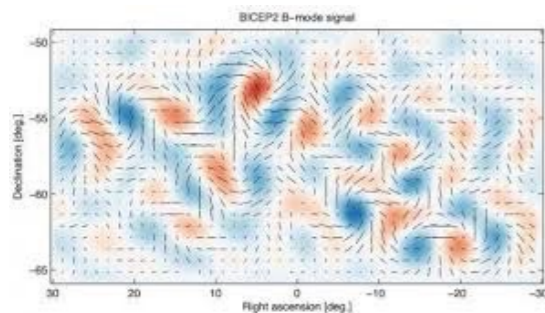
Phase transition (PT), inflation, pre-heating, cosmic string,...



unresolvable

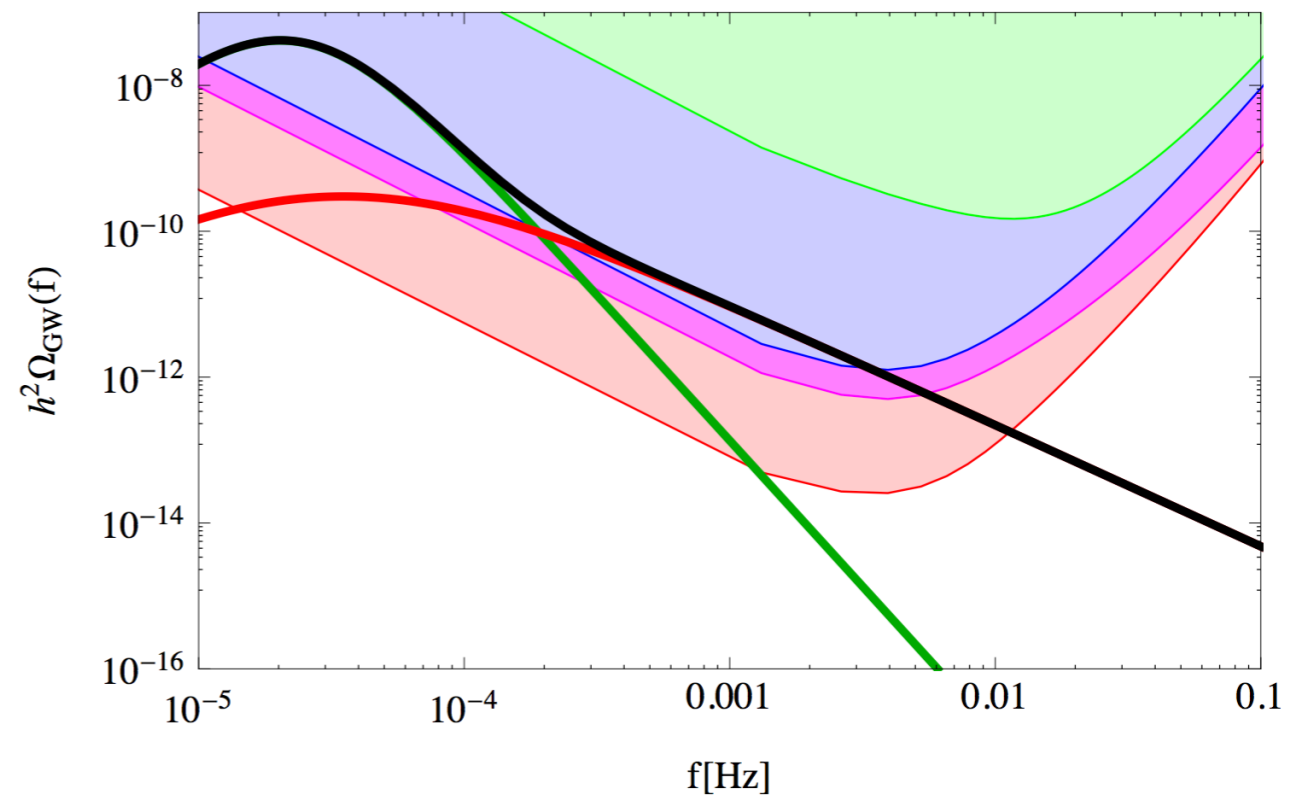
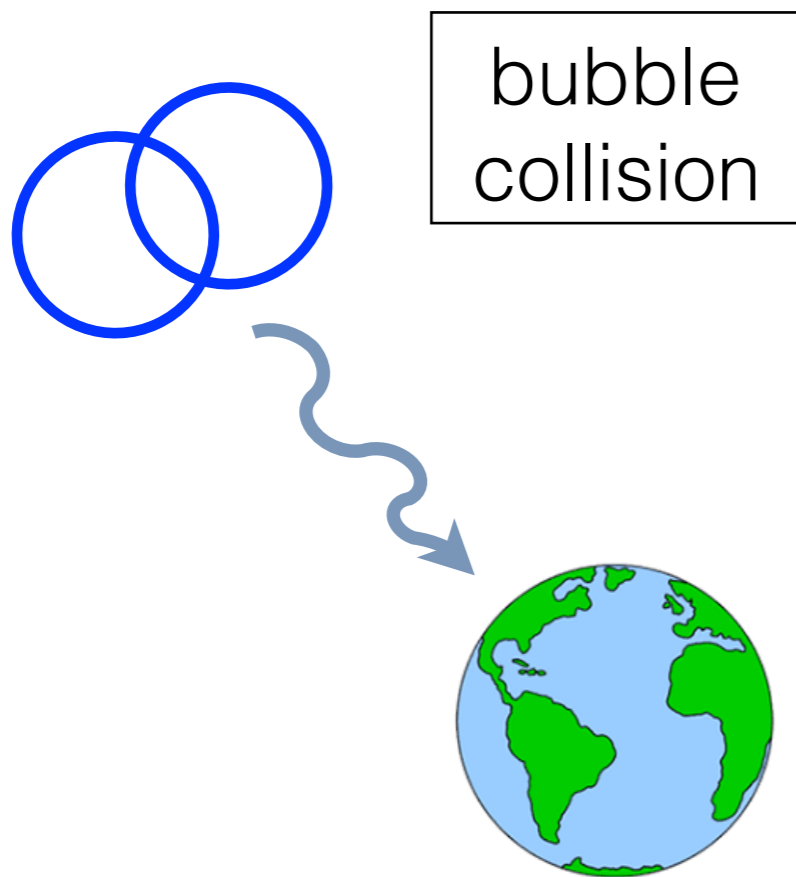


Study physics of  
inflation / reheating,  
universe evolution



# GW from first order phase transition

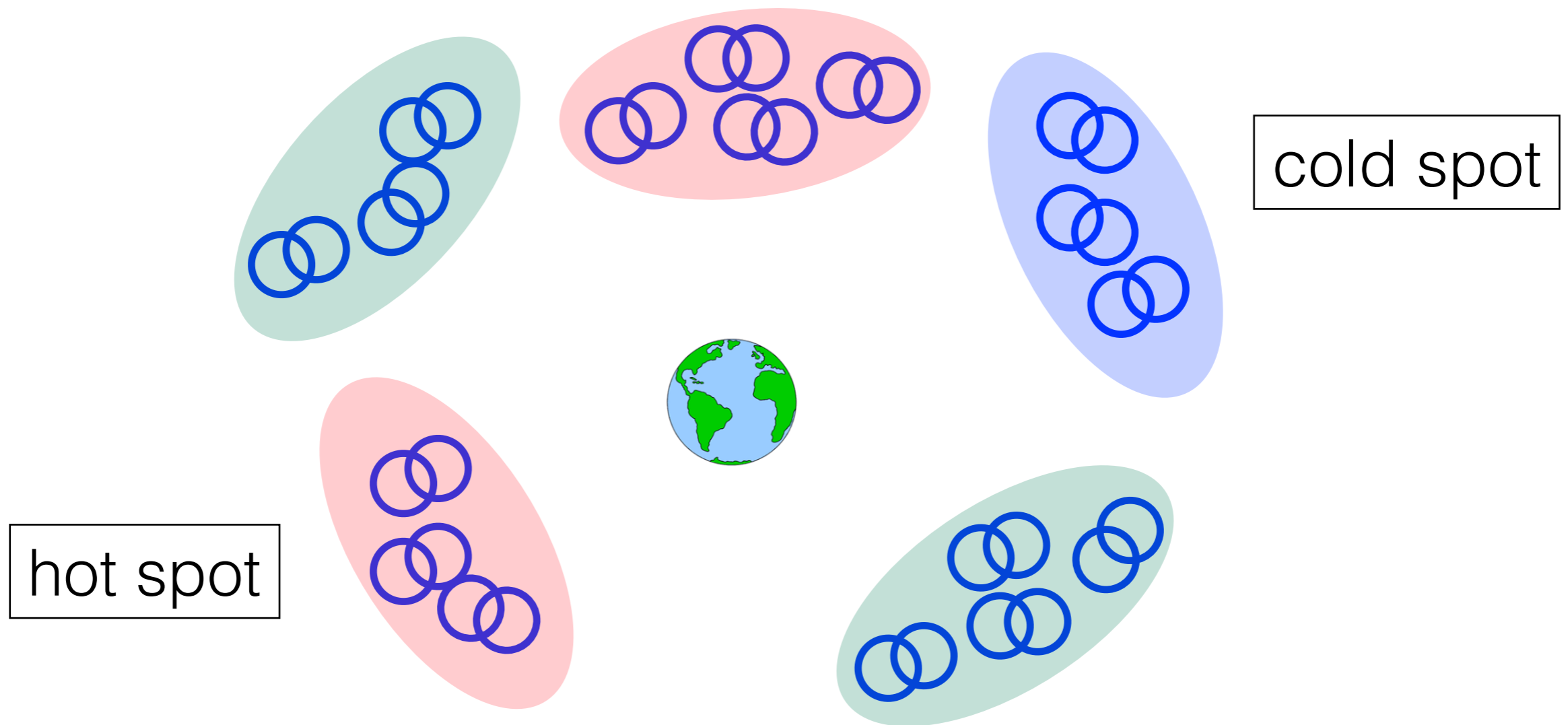
Most of the discussions so far have been focusing on GW's **energy / frequency spectrum** from PT



1512.06239

# GW from first order phase transition

However, the **anisotropic pattern** of GW provides valuable info of inflation/reheating mechanism



many earlier studies on stochastic GWB,  
e.g., see Romano & Cornish (2017) and the reference there

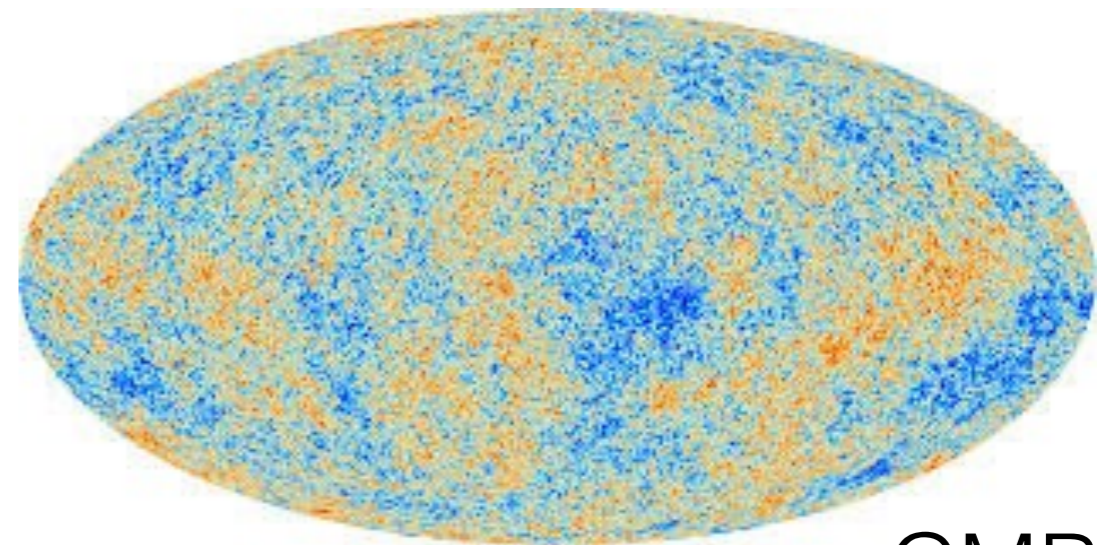
# Gravitational Wave Background (GWB)

Similar to the CMB spectrum, but with  
photon from last scattering  $\rightarrow$  GW from PT

hot spot

Higher energy photons

Higher energy GW

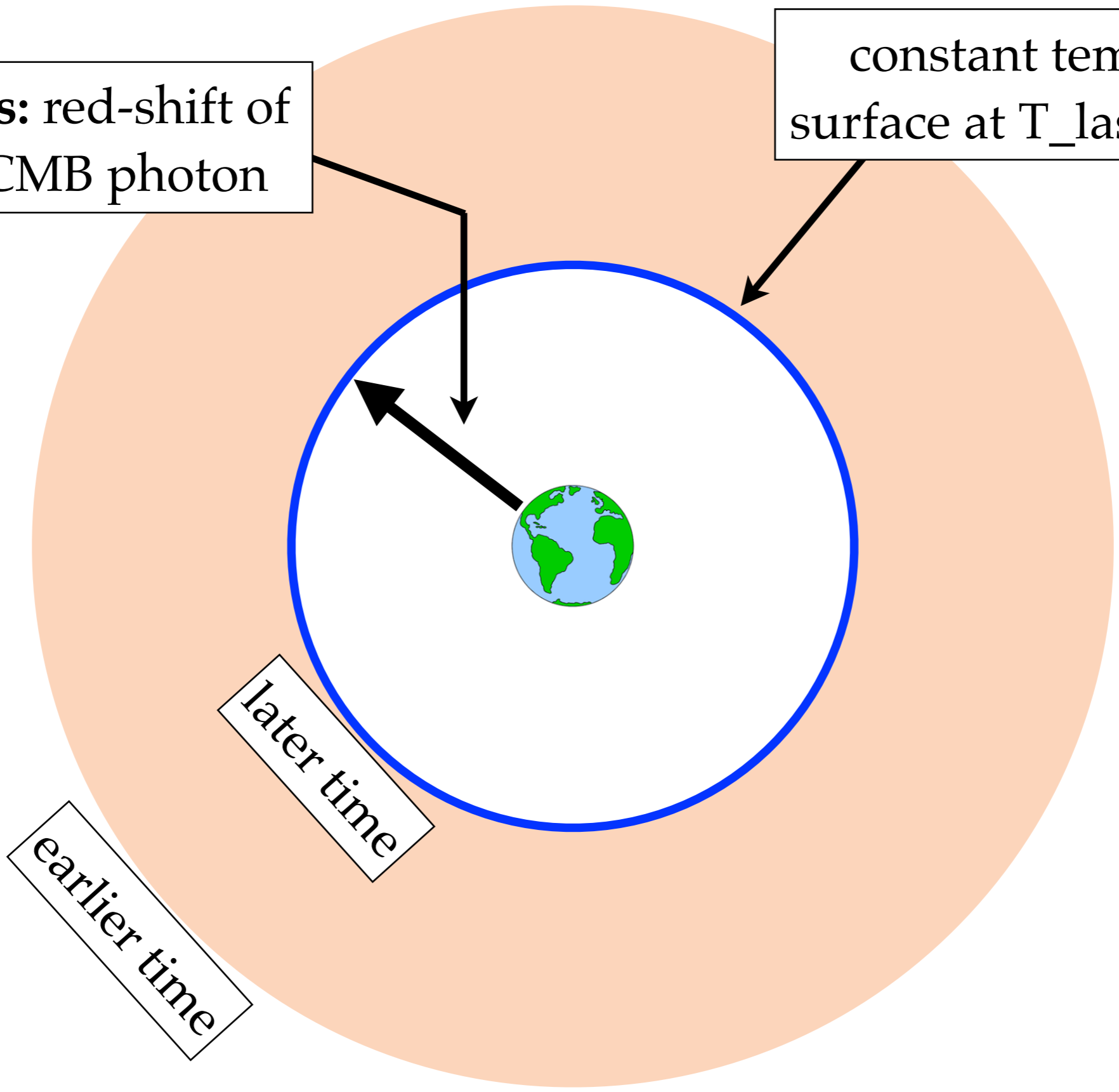


CMB

where does the hot / cold spot come from?

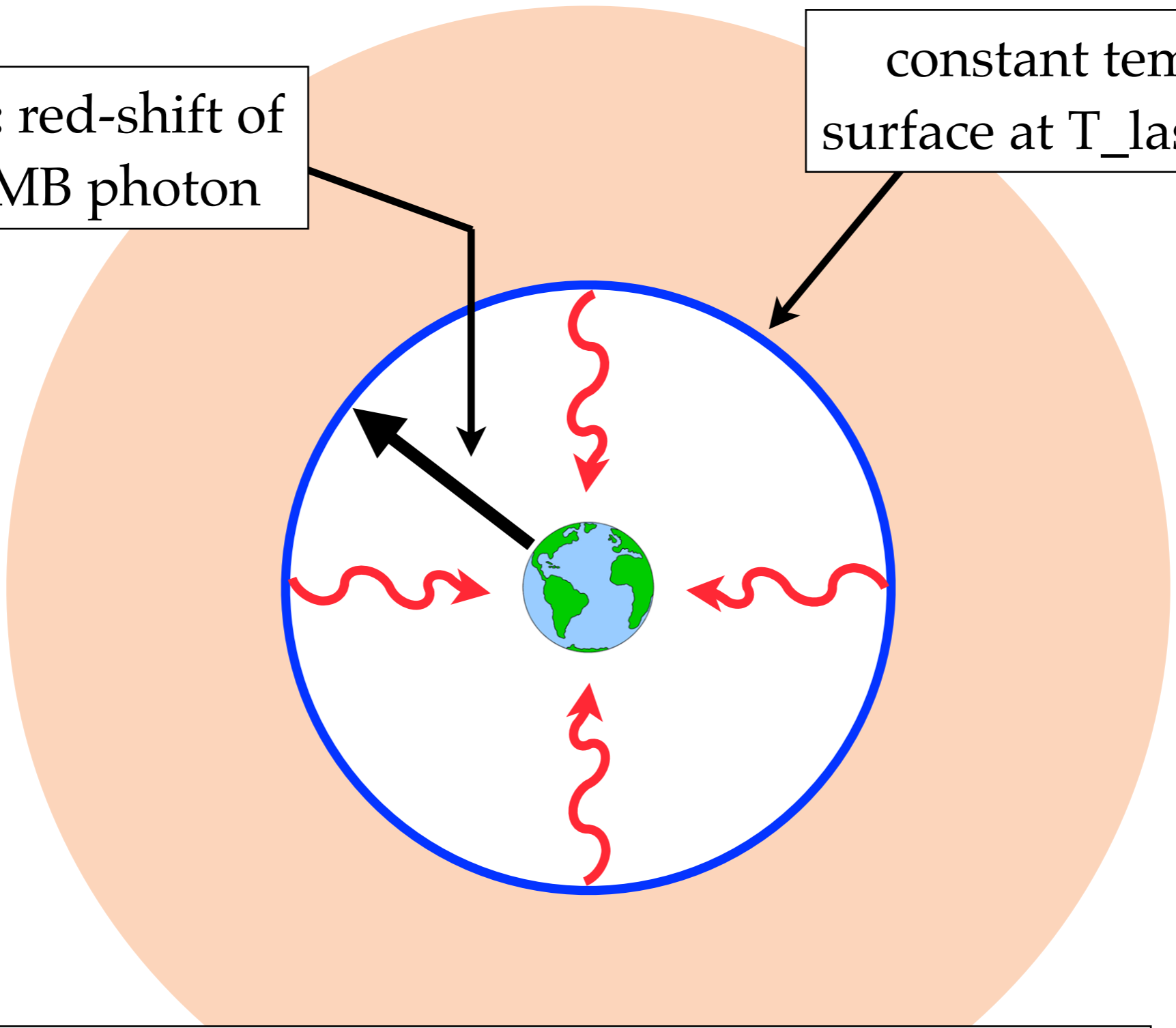
**radius:** red-shift of the CMB photon

constant temperature surface at  $T_{\text{last scattering}}$



radius: red-shift of the CMB photon

constant temperature surface at  $T_{\text{last scattering}}$

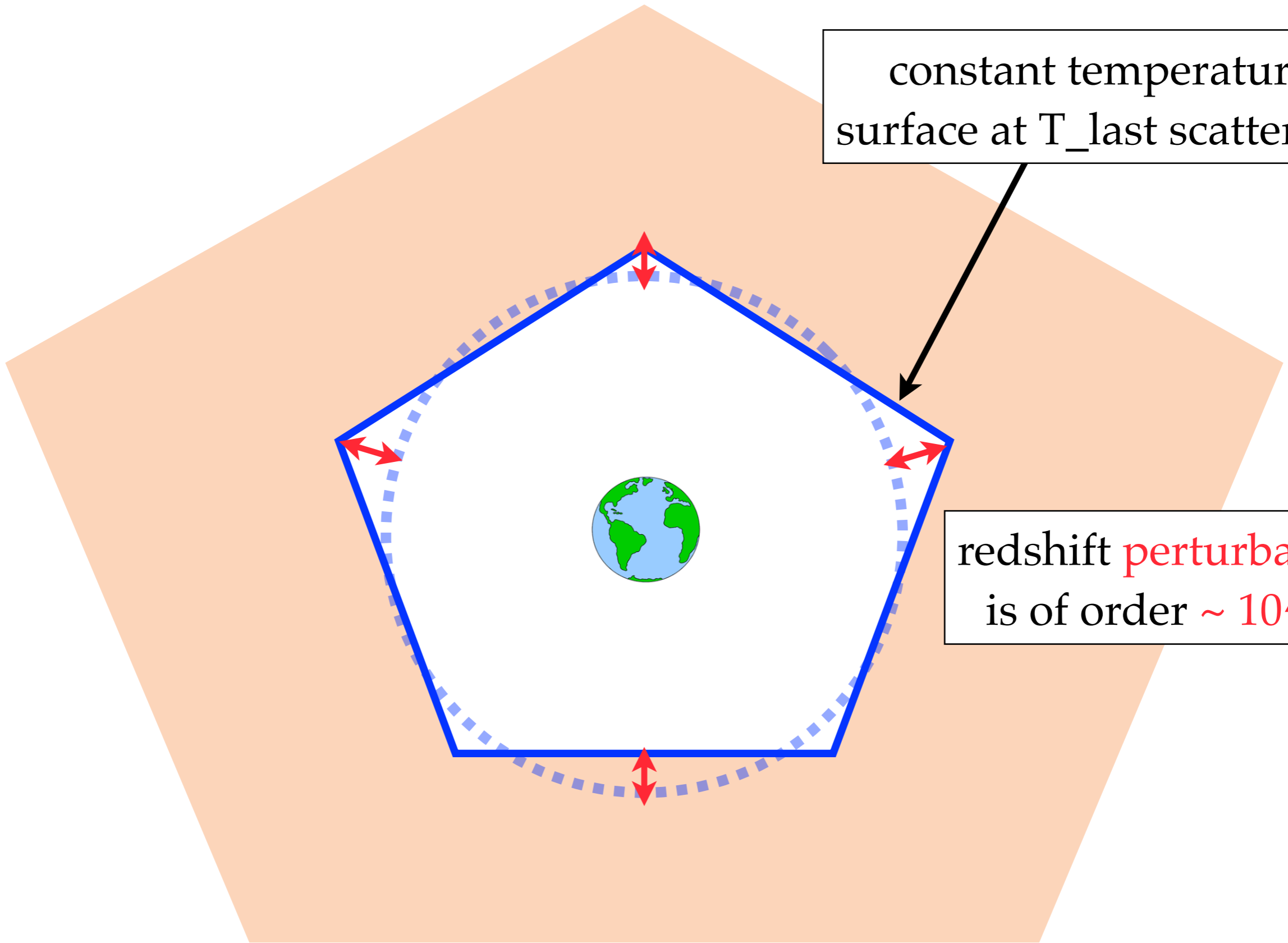


In a homogeneous universe  
=> uniform photon redshift from last scattering

CMB



constant temperature  
surface at  $T_{\text{last scattering}}$

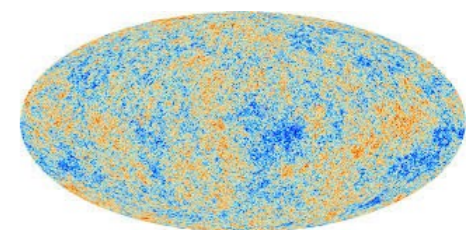


redshift **perturbation**  
is of order  $\sim 10^{-5}$

constant temperature surface at  $T_{\text{last scattering}}$

redshift **perturbation** is of order  $\sim 10^{-5}$

CMB



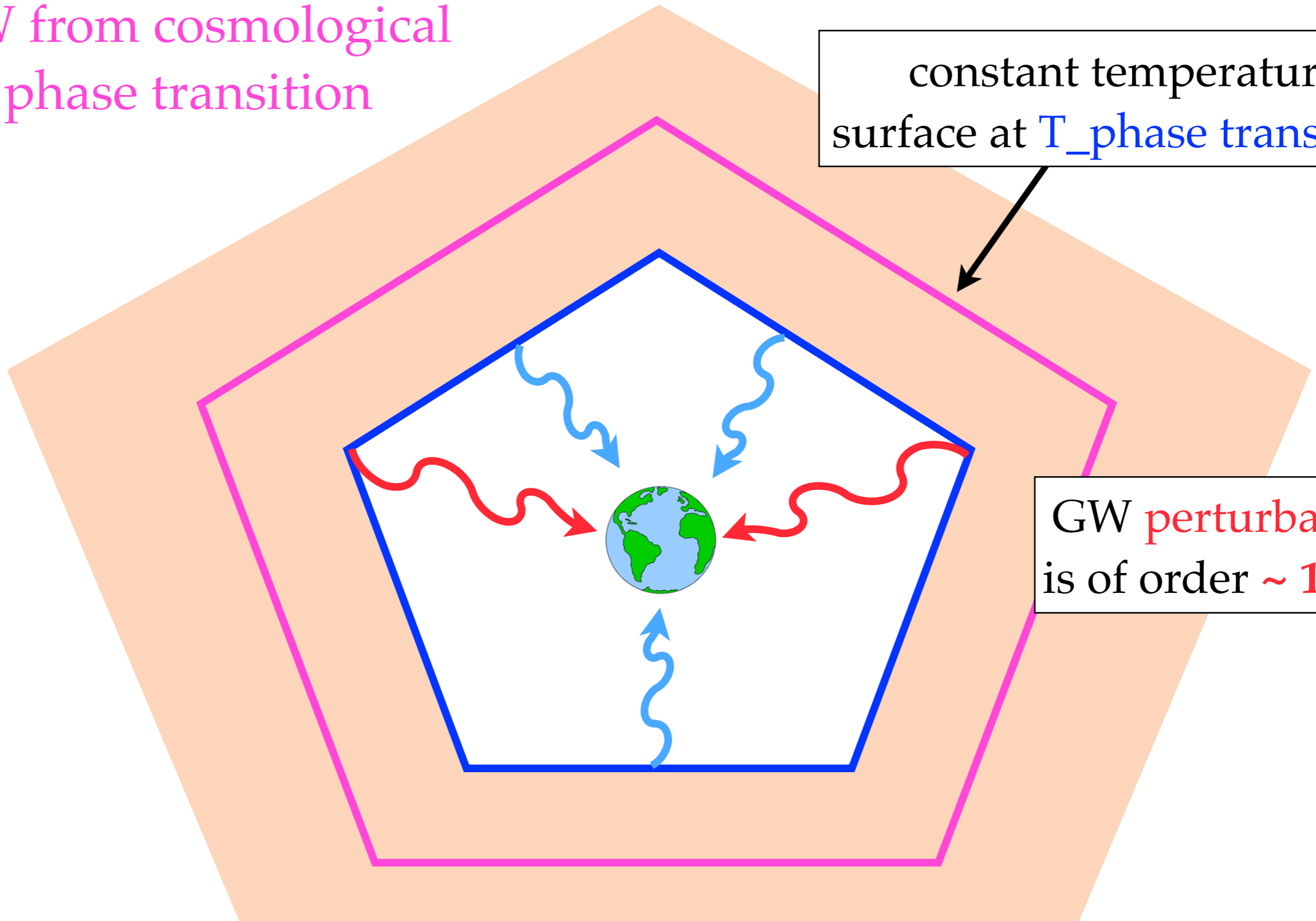
With primordial temperature perturbation  
 $\Rightarrow$  anisotropic redshift for last scattering photon

GW from cosmological  
phase transition

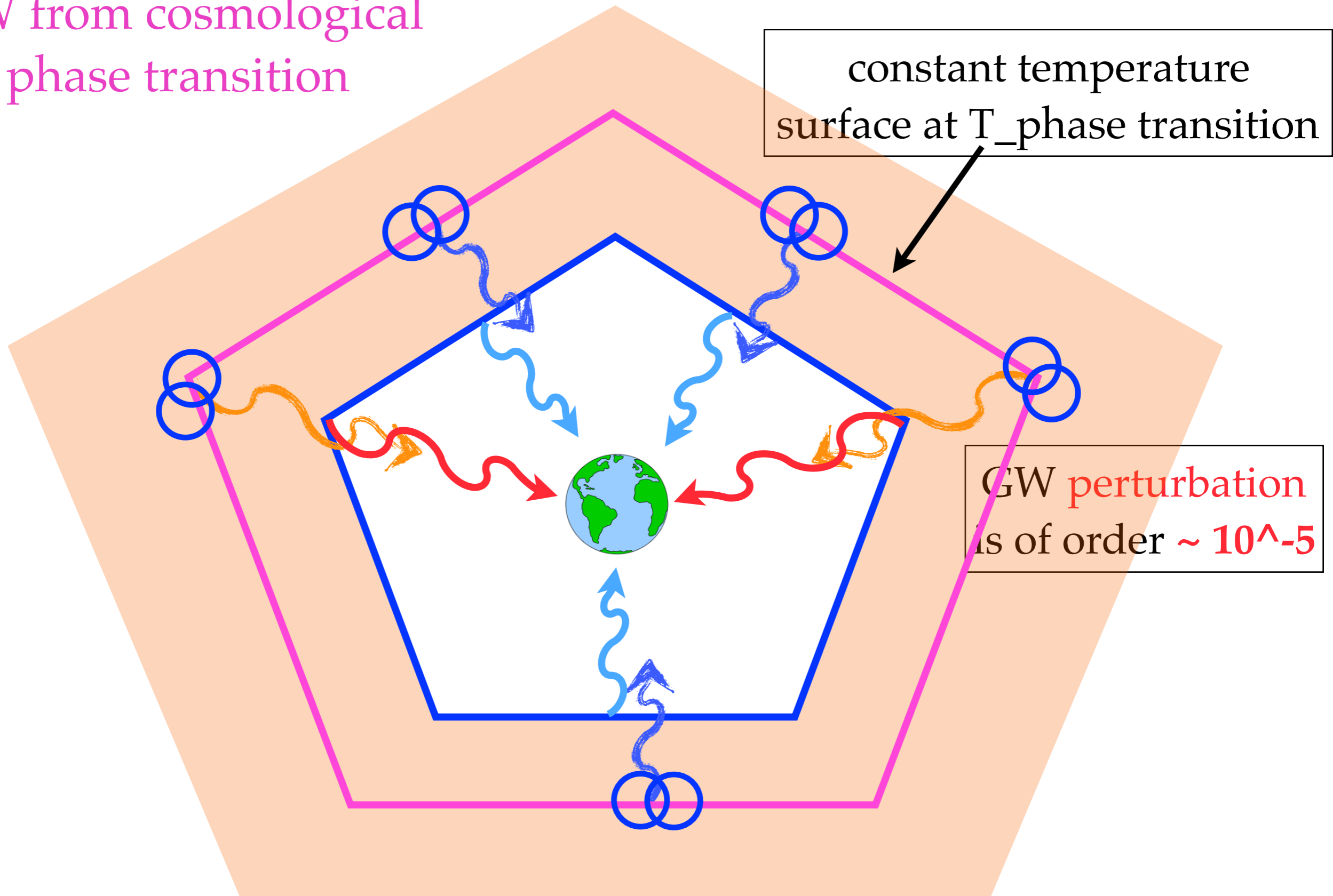
constant temperature  
surface at  $T_{\text{phase transition}}$

GW perturbation  
is of order  $\sim 10^{-5}$

With a single reheating process  
 $\Rightarrow$  GW perturbation is totally correlated to CMB



# GW from cosmological phase transition

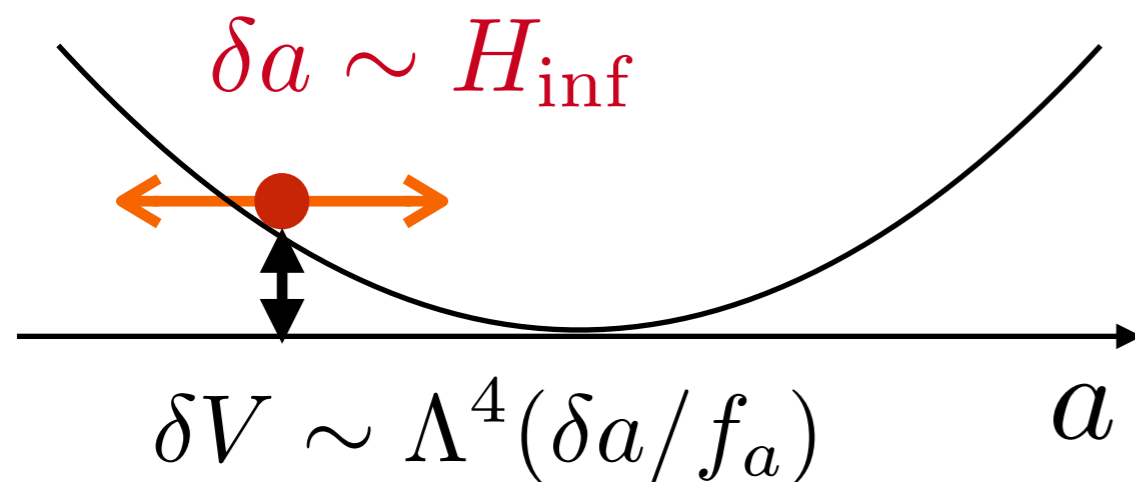


# Iso-curvature perturbation

If in addition to the inflaton, there's an **axion-like particle** fluctuating during inflation

$$V = \Lambda^4 \left( 1 - \sin \frac{a}{f_a} \right)$$

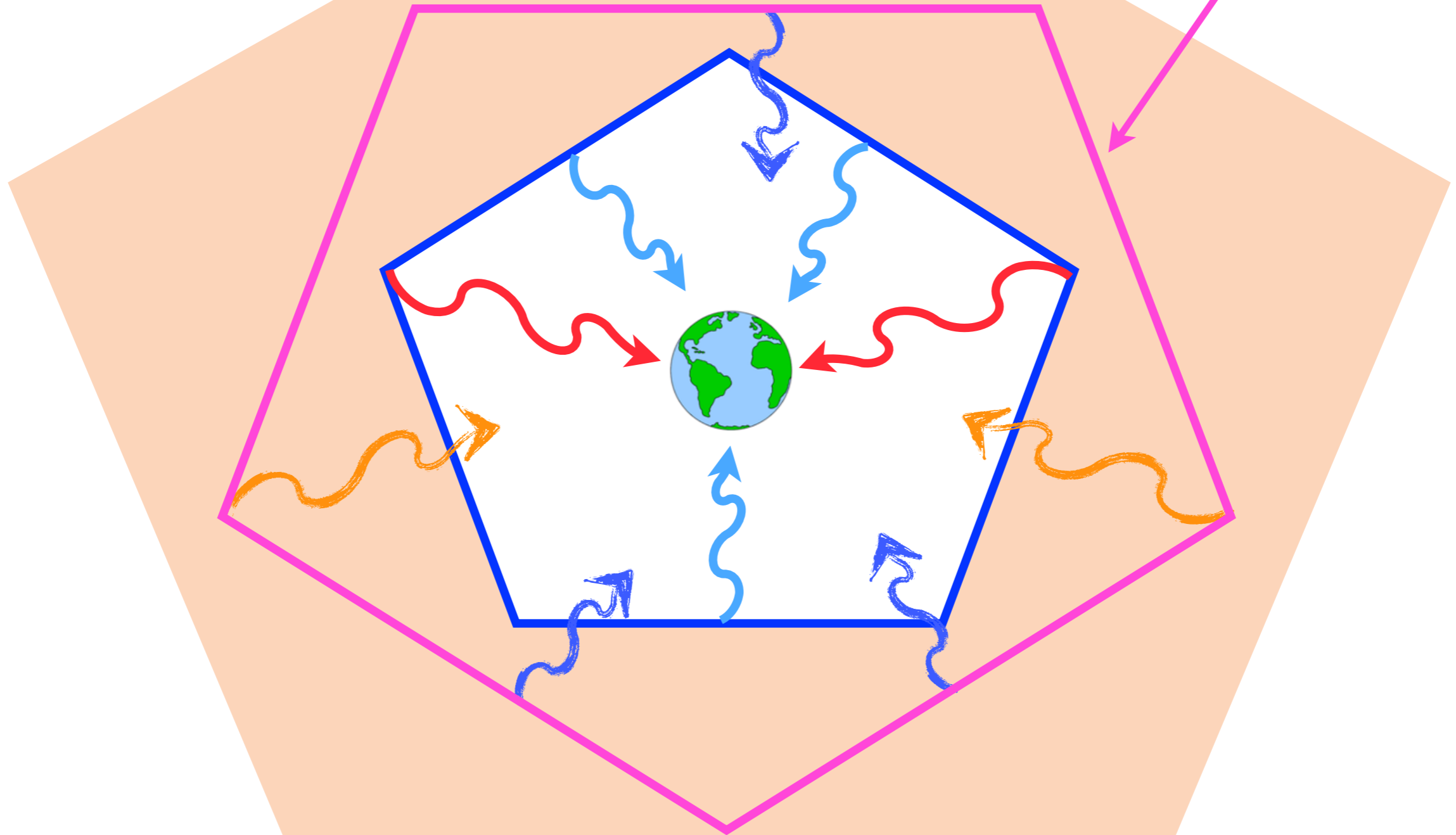
$$\frac{\delta \rho_a}{\rho_a} \sim \frac{\delta V}{V} \sim \frac{H_{\text{inf}}}{f_a}$$



can generate larger & uncorrelated perturbations to the inflaton fluctuation

$$C^{cross} \equiv \frac{\langle \rho_{GW}(1) \rho_{CMB}(2) \rangle}{\bar{\rho}_{GW} \bar{\rho}_{CMB}} = 0$$

uniform temperature  
surface at  $T_{\text{phase transition}}$



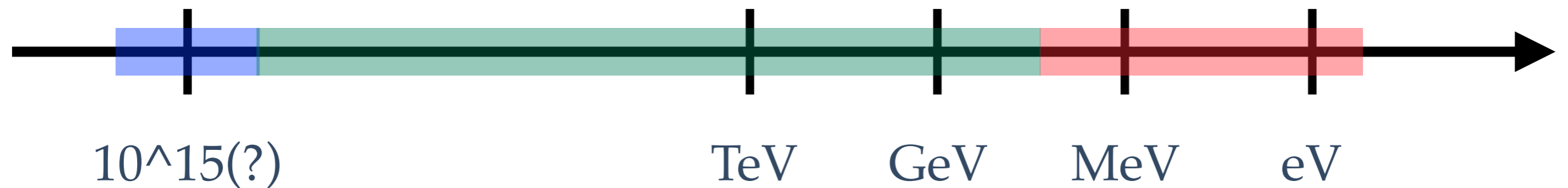
GW perturbation comes from different reheating process  
 $\Rightarrow$  GWB can be “uncorrelated” with CMB

# GW provides a probe of the unknown thermal history

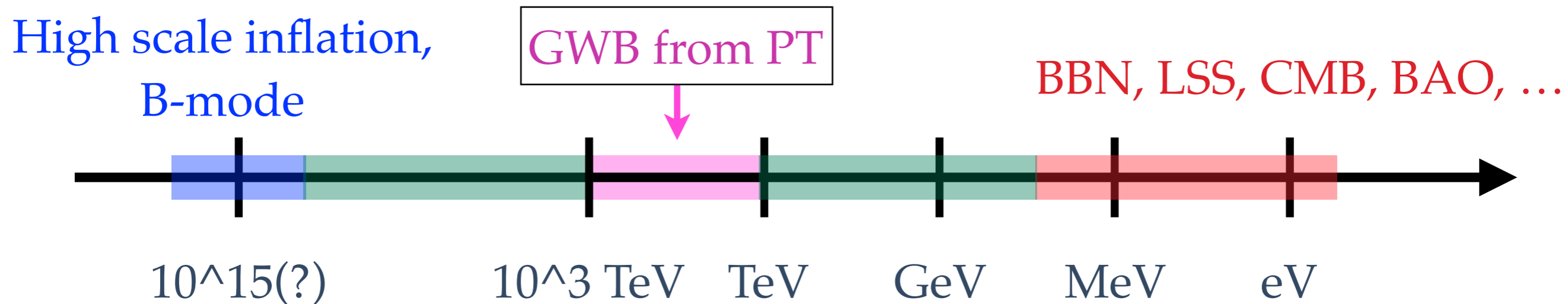
High scale inflation,  
B-mode

?

BBN, LSS, CMB, BAO, ...



# GW provides a probe of the unknown thermal history



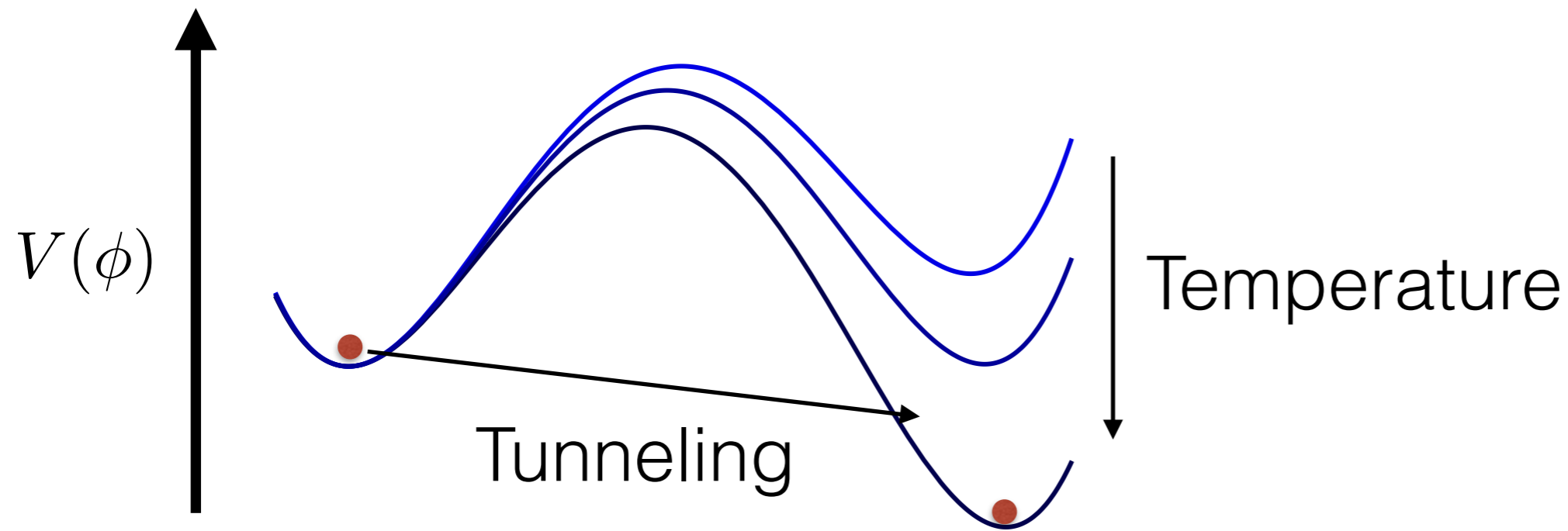
Existence of cosmological PT?

Is there only one source of the density perturbation?

Is there only one reheating process?



# First order phase transition

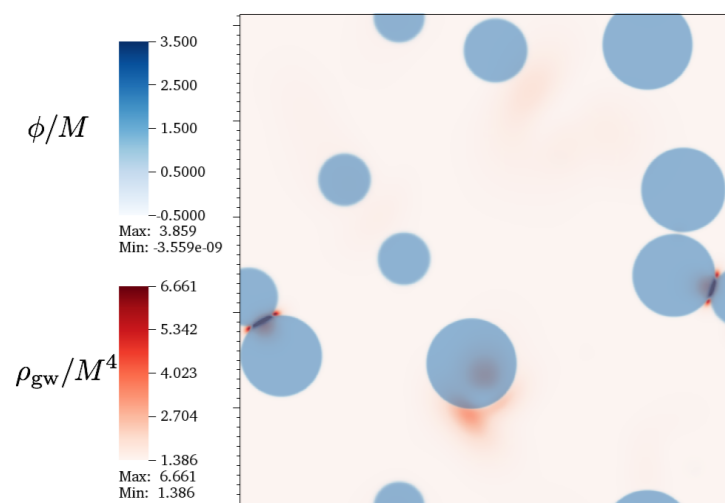


$$\Gamma(T) = A(T) e^{-S(T)}$$

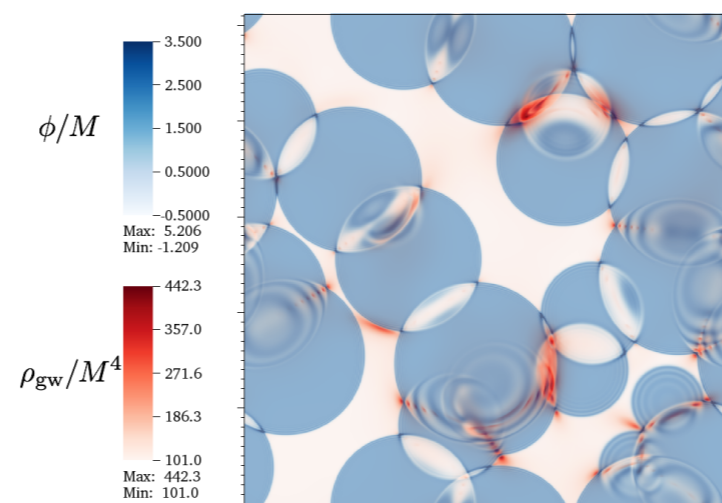
PT rate as a function of temperature

# GW from first order PT

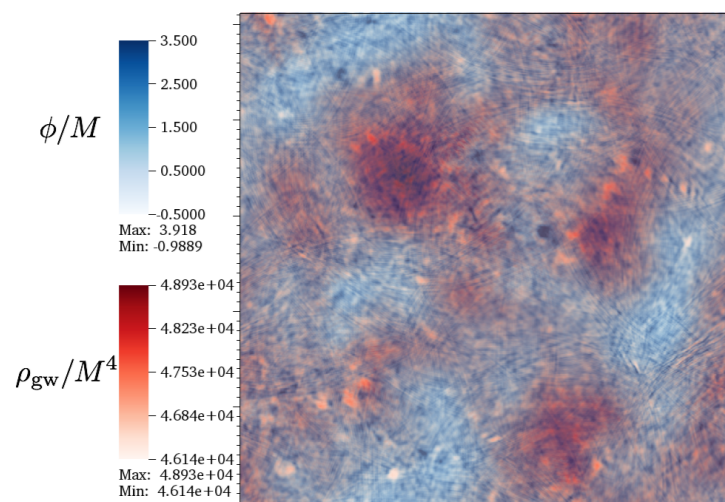
- The collisions of the bubbles generate gravity waves (need quadruple mass for GW)



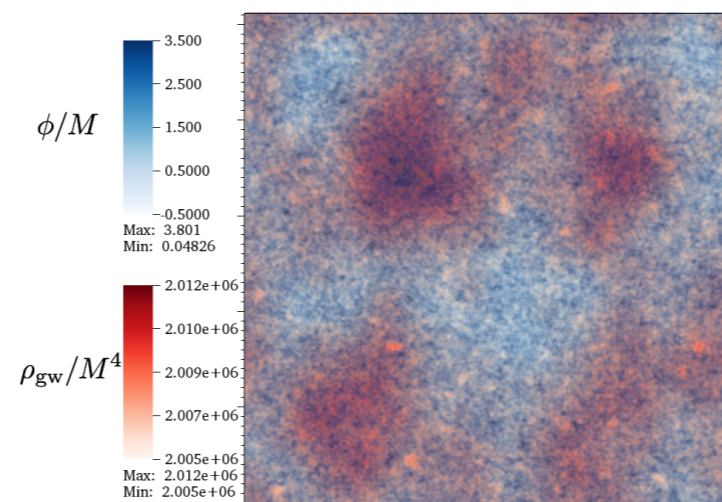
(a)  $t/R_* = 0.35$



(b)  $t/R_* = 0.66$



(c)  $t/R_* = 2.50$



(d)  $t/R_* = 7.8$

In the sky today:  
 $> 10^{30}$  bubbles  
from TeV scale PT

# Energy density of GW from PT

$$\rho_{\text{GW}} \sim \frac{\rho_{PT}^2}{\rho_{\text{total}}} (H_{PT} \Delta t_{PT})^2$$

$$\rho_{\text{GW}}^{\text{today}} \approx 0.1 (H_{PT} \Delta t_{PT})^2 \rho_{\gamma} \approx 10^{-5} - 10^{-2} \rho_{\gamma}$$

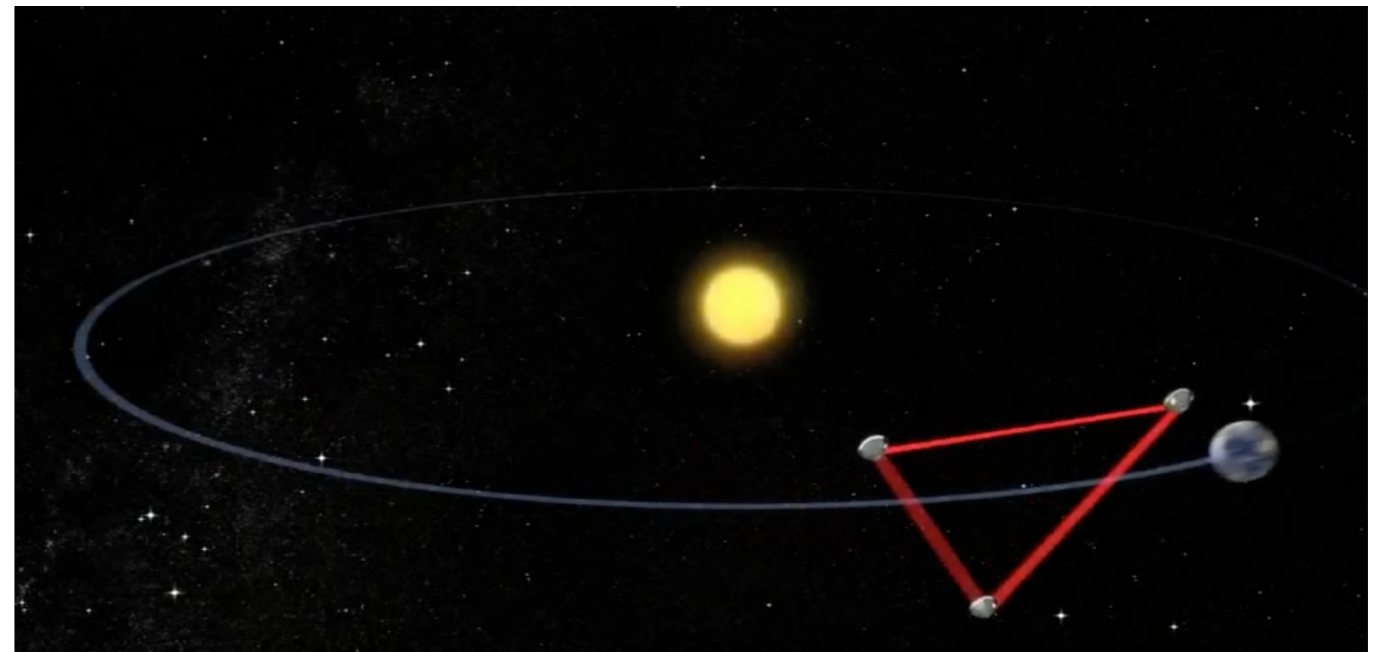
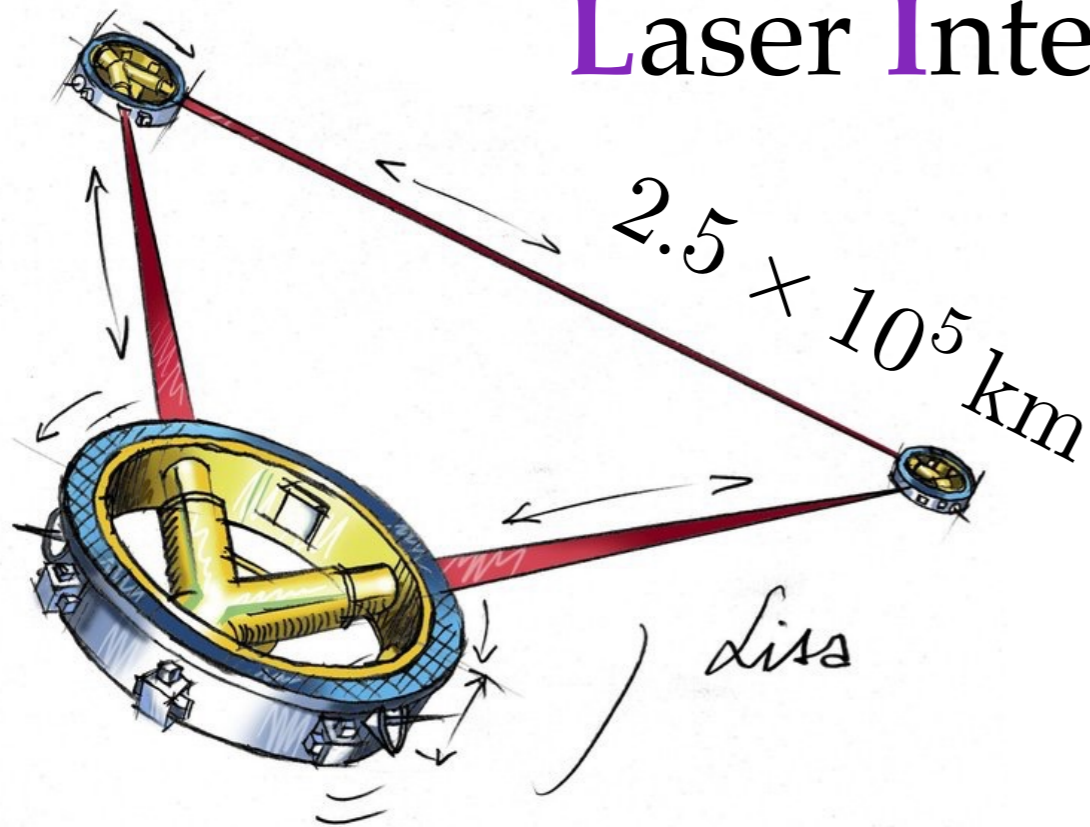
$$\omega_{\text{GW}}^{\text{today}} \sim H_{PT} \left( \frac{T_{\text{CMB}}^{\text{today}}}{T_{PT}} \right) \sim \text{mHz} - \text{Hz}$$

$$T_{PT} \sim \text{TeV} - 10^3 \text{TeV}$$

See also 1512.06239

# GW detectors

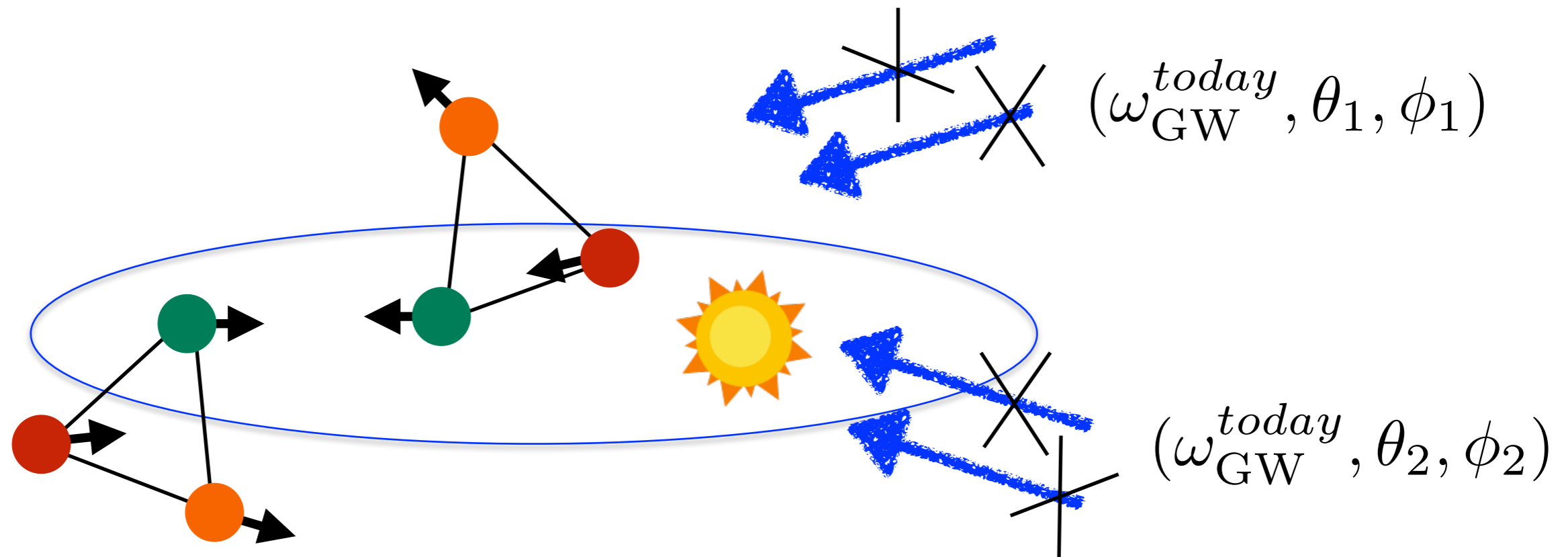
## Laser Interferometer Space Antenna



Similar ideas, more futuristic

BBO, DECIGO, ALIA

# Angular measurement



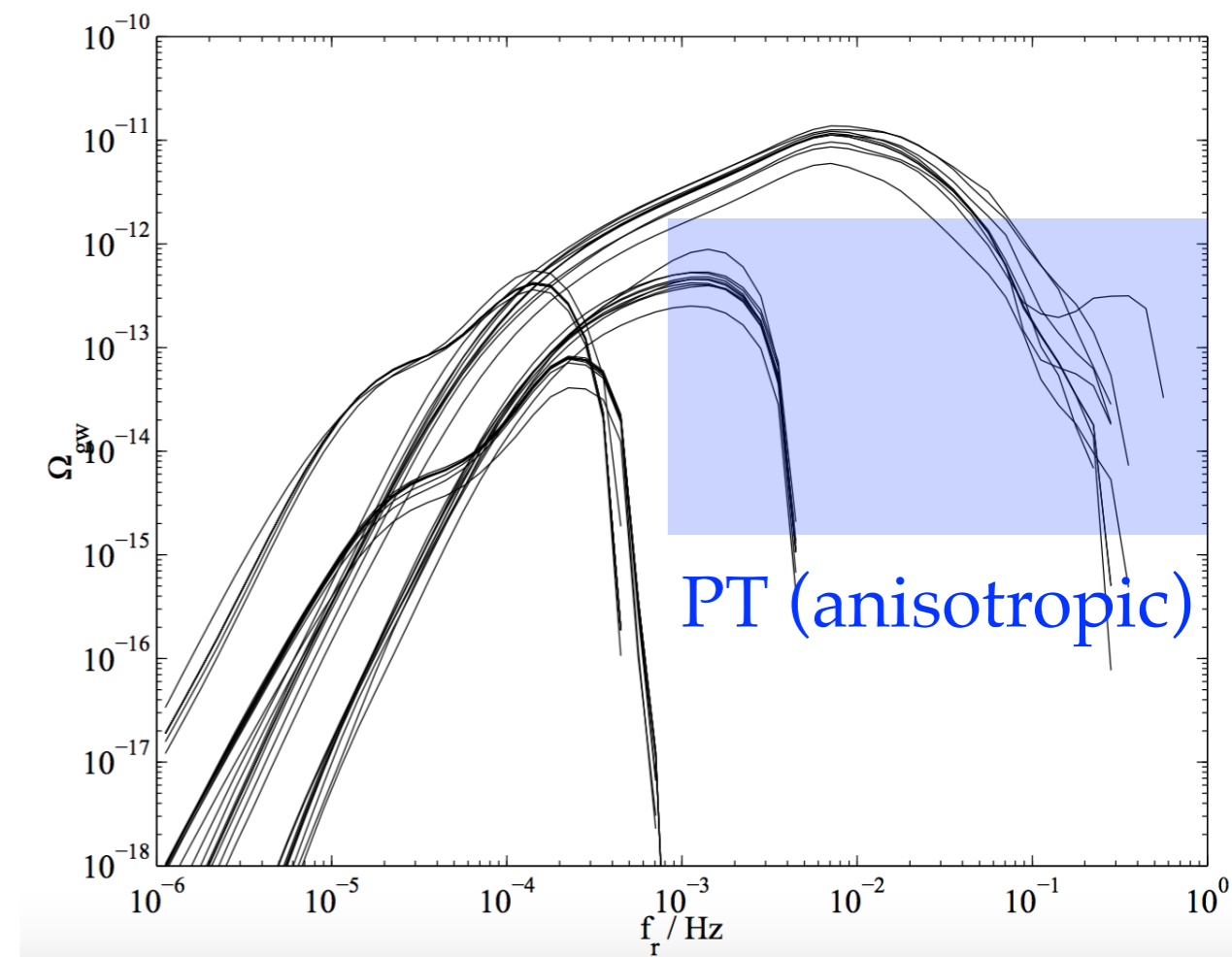
- **Method:** variation of **strains** in time for each **polarization** mode with different **detector location/Doppler shift**
- LISA may get to  $\sim 0.01$  steradians ( $\ell_{\text{max}} = \mathcal{O}(10)$ ), more detectors (BBO/DECIGO) can do better [Cutler(1997), Giampieri et al (1997)]

# Astrophysical foreground

**Unresolvable white dwarf merger**  
generates the dominant  
background to our signal

However, most of these background  
**follow galaxy distribution** and can  
be subtracted with enough data

Adams & Cornish (2013)

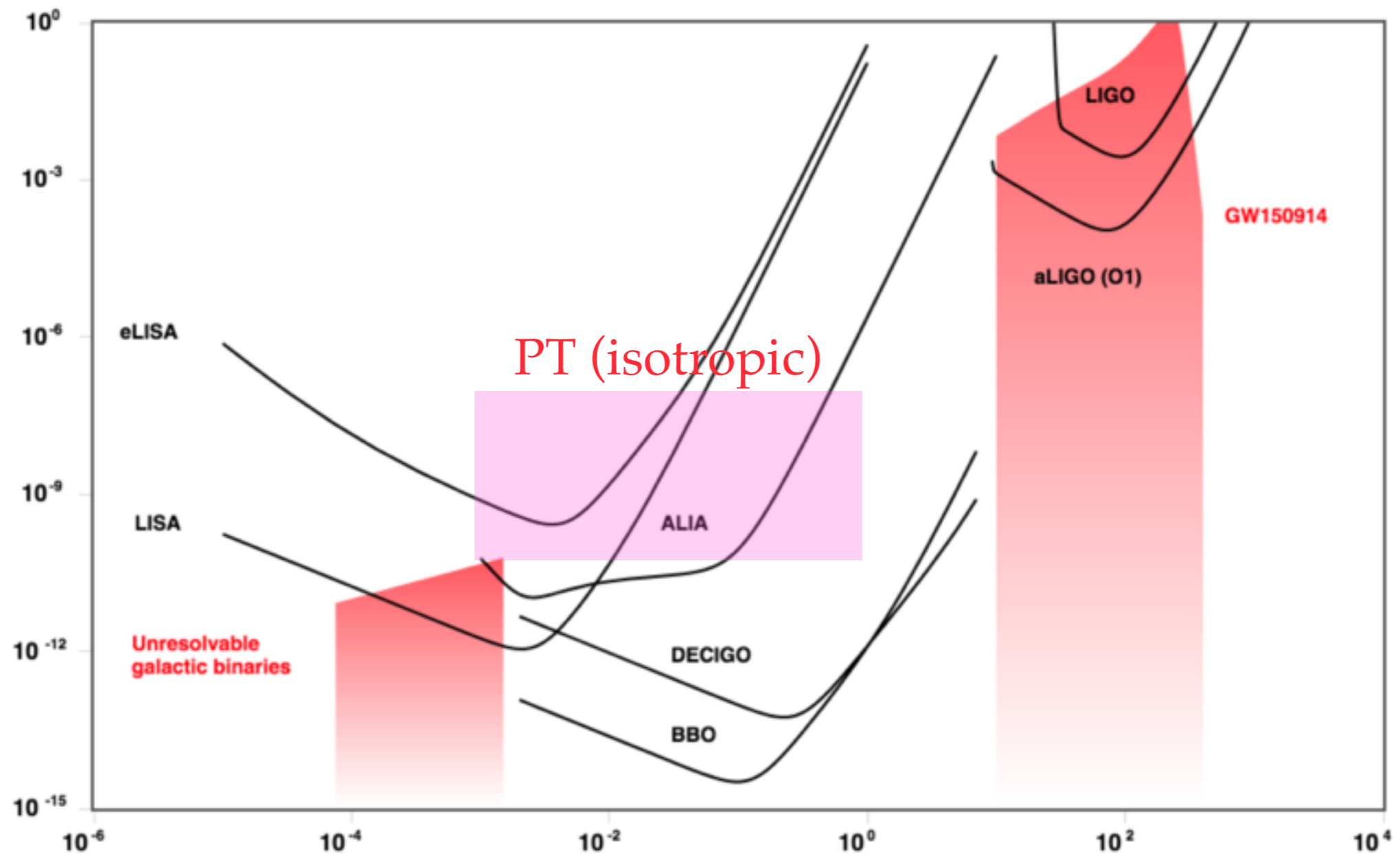


Farmer & Phinney (2003)

# Energy density of GW from PT

$$\rho_{\text{GW}}^{\text{today}} \approx 10^{-5} - 10^{-2} \rho_{\gamma}$$

$\Omega_{\text{GW}} h^2$



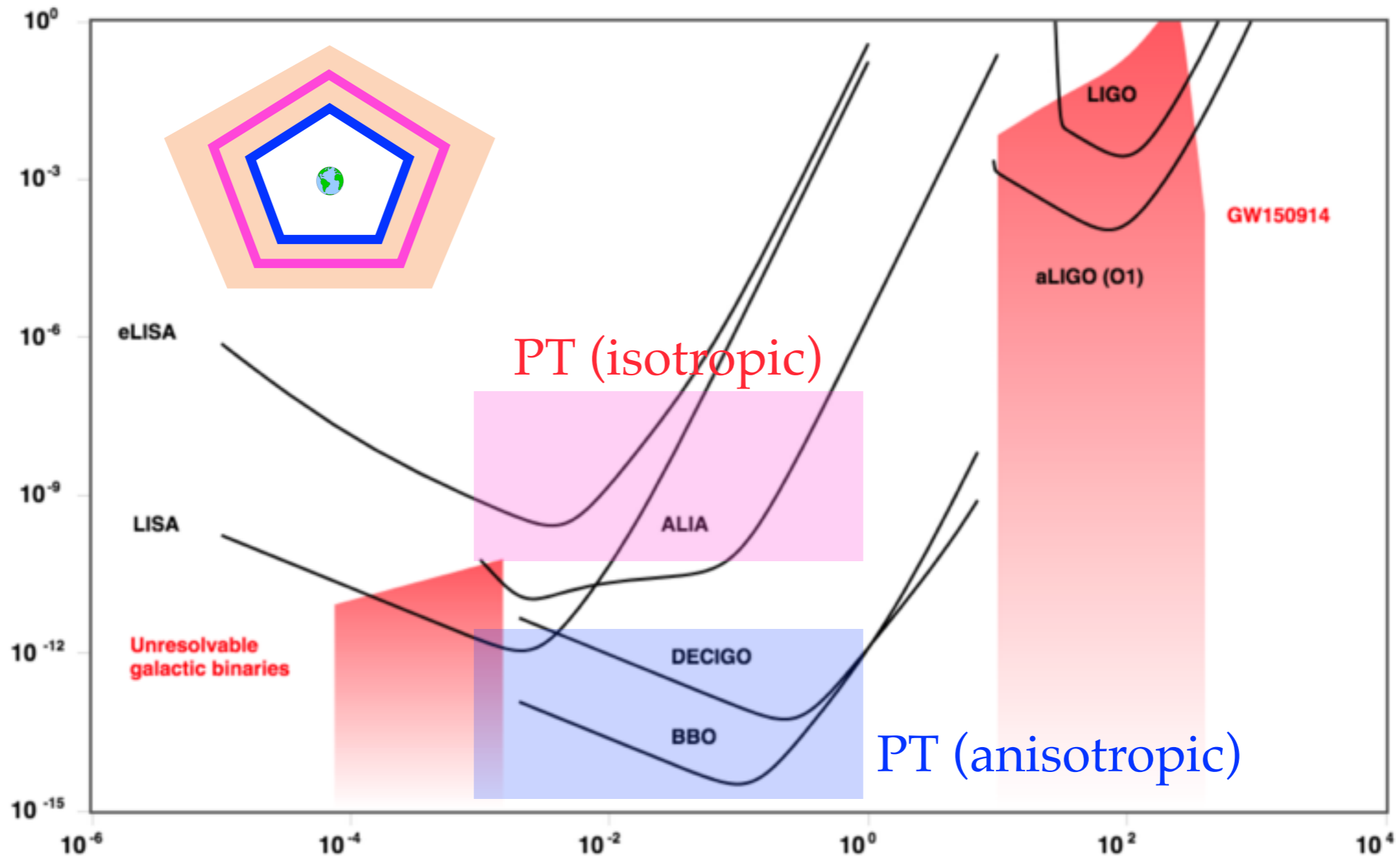
Frequency (Hz)

[rhcole.com/apps/GWplotter/](http://rhcole.com/apps/GWplotter/)

# Detection possibility

$$\delta\rho_{\text{GW}}^{\text{today}} \approx 10^{-10} - 10^{-7} \rho_{\gamma}$$

$\Omega_{\text{GW}} h^2$



Frequency (Hz)

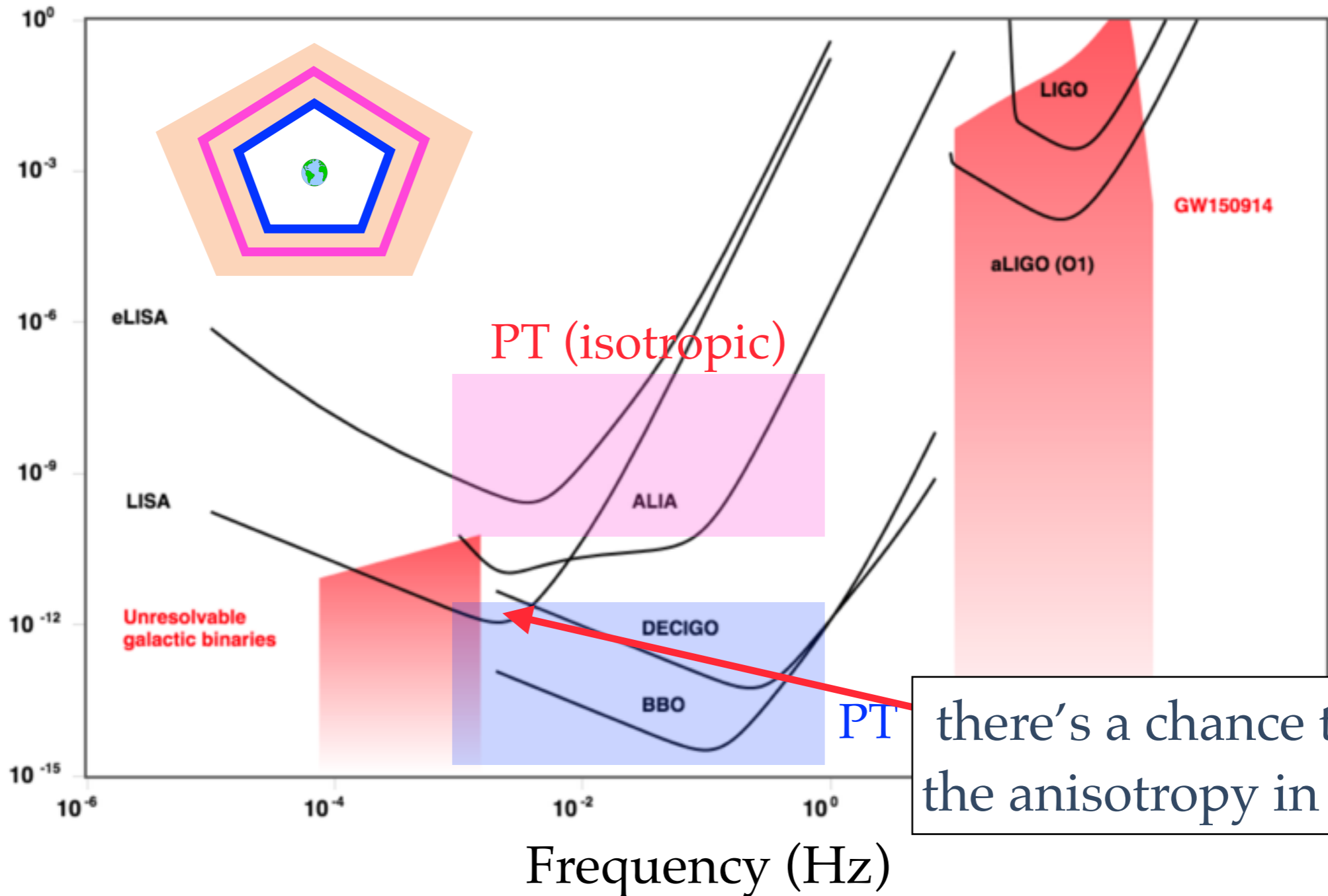
[rhcole.com/apps/GWplotter/](http://rhcole.com/apps/GWplotter/)



# Detection possibility

$$\delta\rho_{\text{GW}}^{\text{today}} \approx 10^{-10} - 10^{-7} \rho_{\gamma}$$

$\Omega_{\text{GW}} h^2$

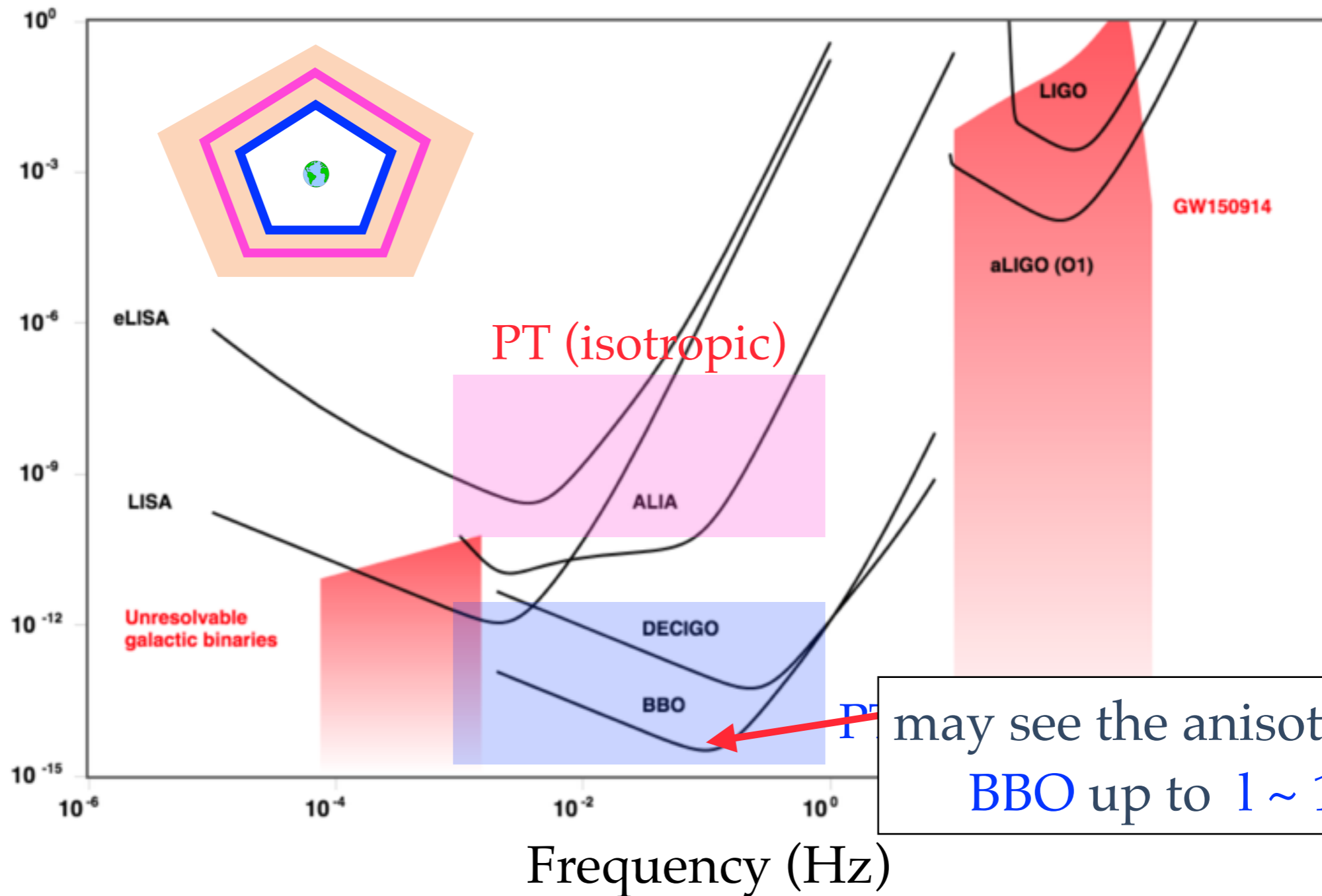


there's a chance to see the anisotropy in **LISA**!

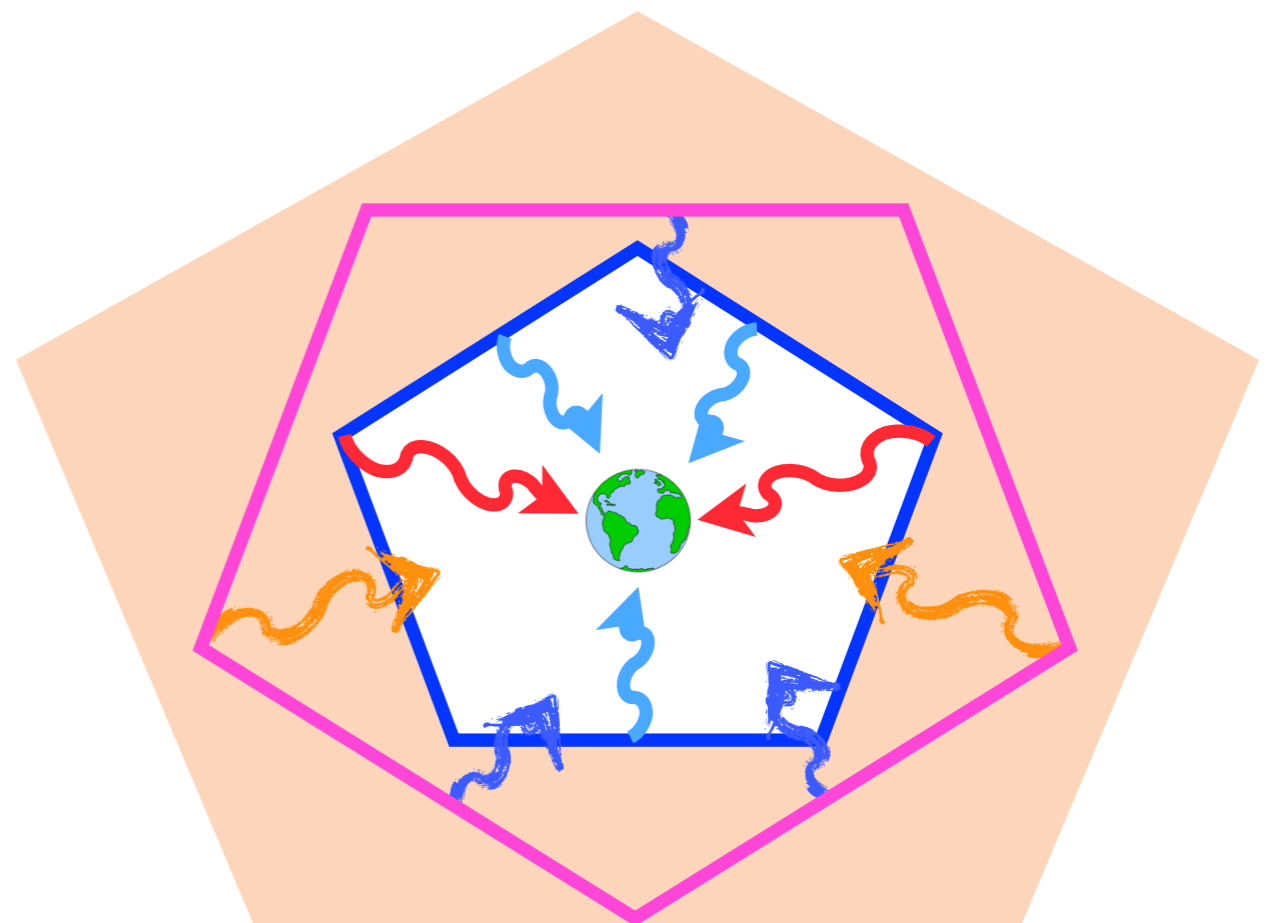
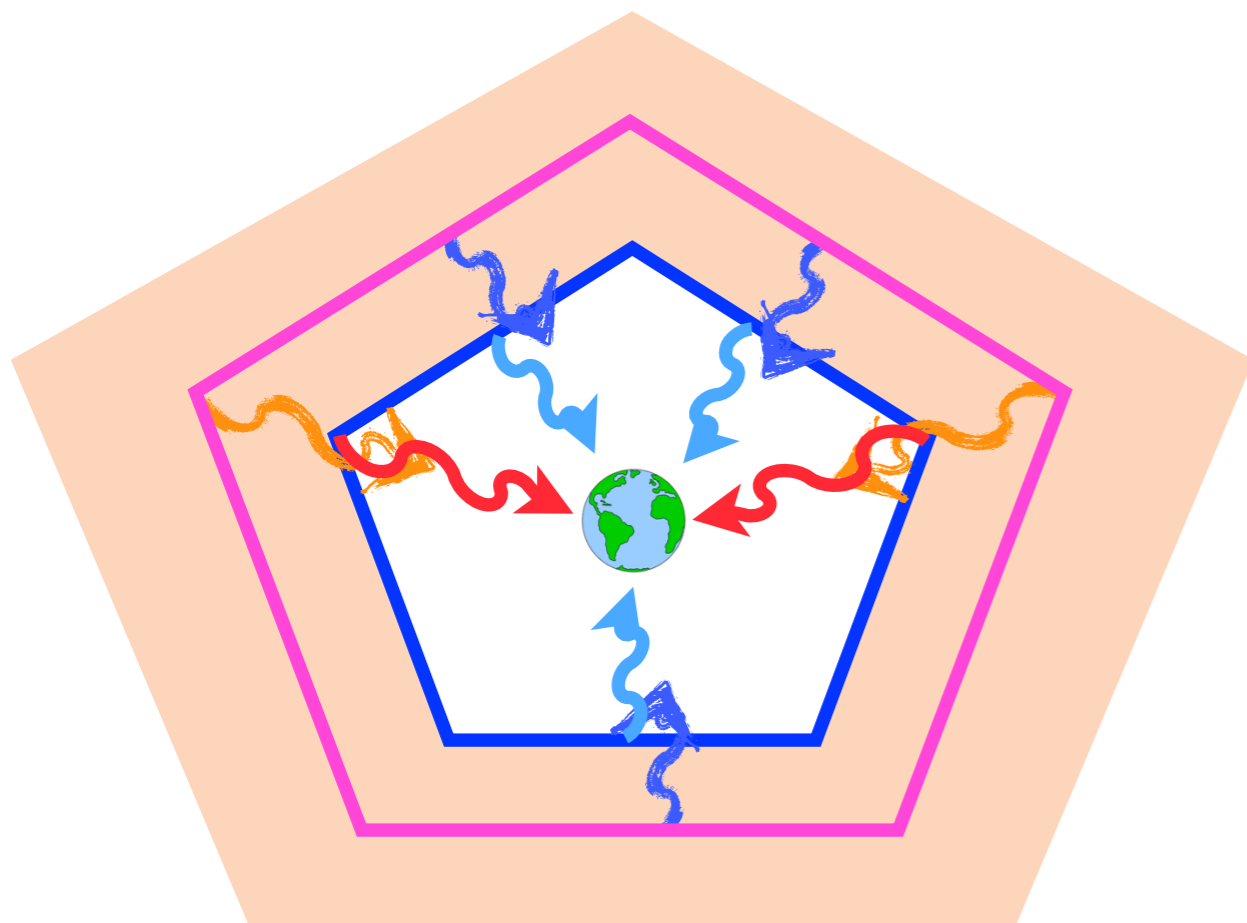
# Detection possibility

$$\delta\rho_{\text{GW}}^{\text{today}} \approx 10^{-10} - 10^{-7} \rho_{\gamma}$$

$\Omega_{\text{GW}} h^2$

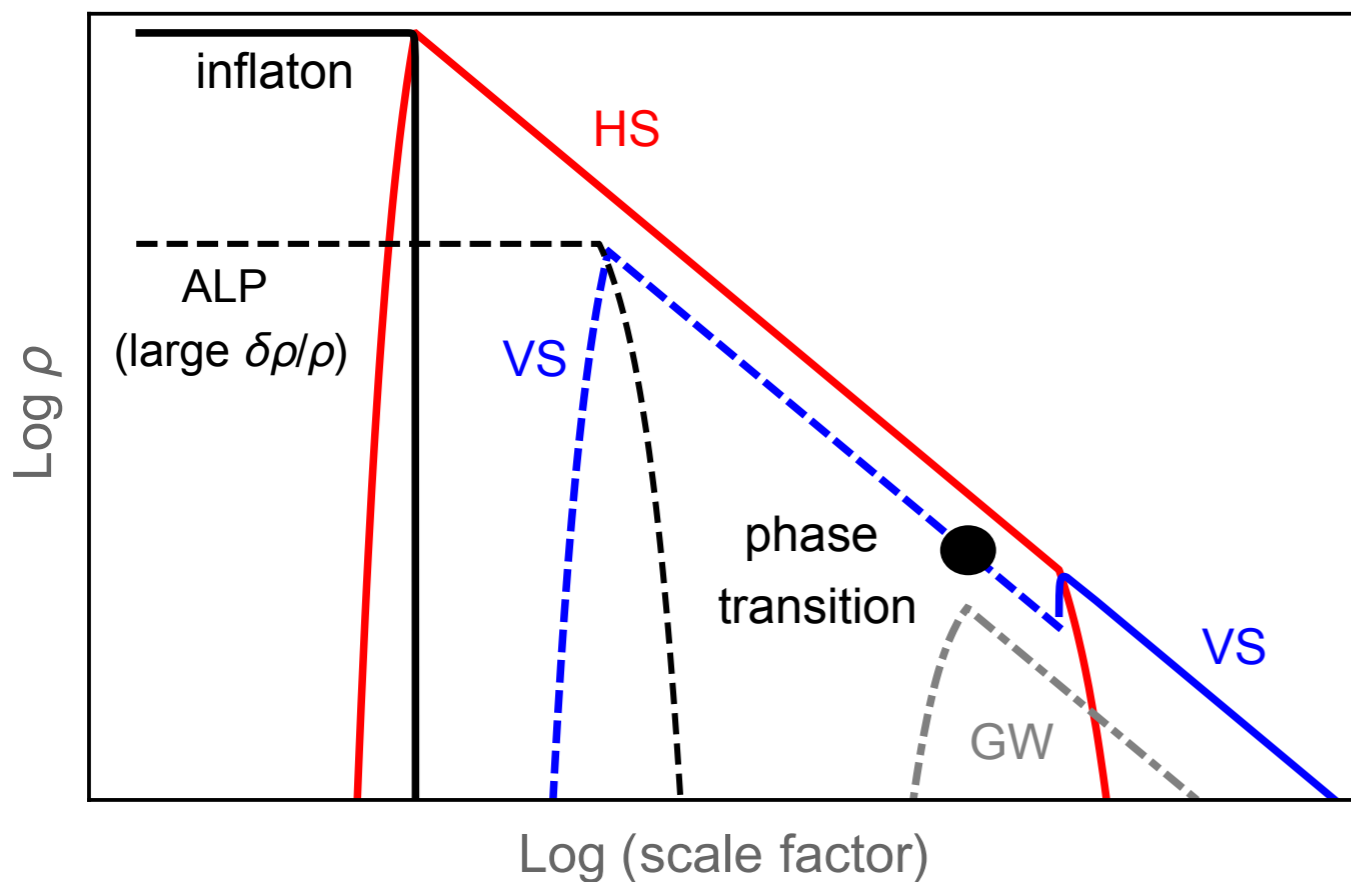


# Non-minimal Story



# e.g., a curvaton model

$$\delta\rho_{\text{GW}} \sim 0.1 \left( \frac{\rho_{\text{VS}}}{\rho_{\text{HS}}} \right)^2 (H_{\text{PT}} \Delta t_{\text{PT}})^2 \left( \frac{\delta\rho}{\rho} \right)_{\text{GW}} \rho_\gamma$$



$$H_{\text{PT}} \Delta t_{\text{PT}} = 0.1$$

$$\left( \frac{\delta\rho}{\rho} \right)_{\text{GW}} = 10^{-4} \quad \frac{\rho_{\text{VS}}}{\rho_{\text{HS}}} = 0.1$$

Larger energy contrast

~ CMB isocurvature constraint

Visible at BBO up to  $\ell_{\text{max}} \approx 100$

# Conclusion and outlook

First Order  
Phase Transition

Gravitational  
Wave

Inflaton / Curvaton  
Perturbation

Anisotropic  
GW Background

LISA / BBO



# Conclusion and outlook

? cosmo source

pre-heating: Bethke et al (2014)  
cosmic string: Jenkins et al (2018)

Gravitational  
Wave

? perturbation

Anisotropic  
GW Background

? GW detector

