

A UNIVERSAL BOUND ON THE STRONG COUPLING SCALE OF A GRAVITATIONALLY COUPLED MASSIVE SPIN-2 PARTICLE

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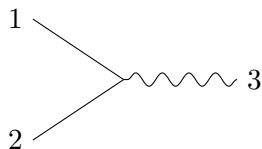
UNIVERSAL GRAVITATIONAL INTERACTIONS

S-MATRIX EQUIVALENCE PRINCIPLE

- ▶ Every particle that interacts with Einstein gravity must have a minimal coupling vertex with a universal coupling constant

Weinberg:

$$\mathcal{V}_{\text{cubic}} = \frac{2i}{M_p} (\epsilon_3 \cdot p_1)^2 (\epsilon_1 \cdot \epsilon_2)^s .$$

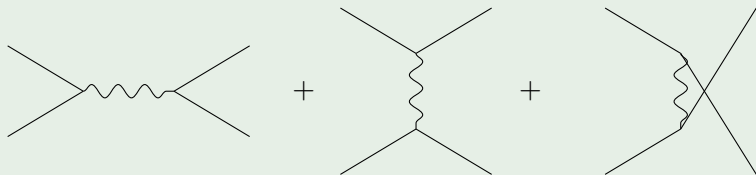


LOW SPIN PARTICLES

SIMPLE SCALAR EXAMPLE

- ▶ Consider a scalar minimally coupled to gravity,

$$S = \frac{1}{2} \int d^4x \sqrt{-g} (M_p^2 R - \partial_\mu \phi \partial^\mu \phi - m^2 \phi^2).$$



- ▶ For $E \gg m$, the four-point amplitude is

$$\mathcal{A} = \frac{1}{4M_p^2} \frac{(\mathbf{s}^2 + \mathbf{t}^2 + \mathbf{u}^2)^2}{\mathbf{stu}}.$$

MASSLESS HIGHER-SPIN PARTICLES

- ▶ For massless particles with $s > 2$, the S -matrix equivalence principle is incompatible with gauge invariance:

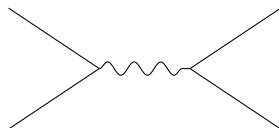
$$p_1 \cdot \frac{\partial}{\partial \epsilon_1} \left(\frac{2}{M_p} (\epsilon_3 \cdot p_1)^2 (\epsilon_1 \cdot \epsilon_2)^s + \dots \right) \neq 0.$$

NO-GO RESULT

Massless higher-spin particles cannot couple directly or indirectly to Einstein gravity in flat spacetime.

MASSIVE HIGHER-SPIN PARTICLES

- ▶ Massive higher-spin particles can couple to gravity, e.g. QCD and string theory.
- ▶ However, isolated massive particles with $m \ll M_p$ and $s > 1$ cannot remain fundamental point-like particles up to M_p .



A Feynman diagram consisting of two incoming lines on the left and two outgoing lines on the right, connected by a wavy propagator in the middle. To the right of the diagram is a tilde symbol followed by the expression $\frac{E^{2k}}{M_p^2 m^{2k-2}}$.

$$\sim \frac{E^{2k}}{M_p^2 m^{2k-2}}$$

- ▶ The local effective field theory violates perturbative unitarity at some scale $\Lambda_k \equiv (m^{k-1} M_p)^{1/k} \ll M_p$.
- ▶ Contact terms can partially cancel the bad high-energy behaviour and raise the strong coupling scale.

BOUNDING THE STRONG COUPLING SCALE

- ▶ How large can Λ_k be for a given spectrum of particles?

STRATEGY:

1. Classify all cubic and quartic vertices
2. Construct the general four-point amplitude consistent with locality, unitarity, Lorentz invariance, gauge invariance, and crossing symmetry.
3. Find the amplitude with the highest strong coupling scale.

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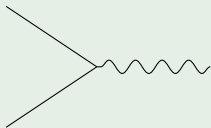
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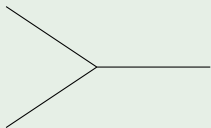
- ▶ Here we look at massive spin 2 coupled to gravity.

EXAMPLE

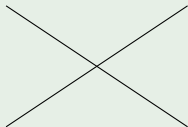
CLASSIFYING SPIN-2 VERTICES



5 structures,



4 structures,



95 structures.

RESULTS

- ▶ The highest strong coupling scale for a unitary gravitationally coupled massive spin-2 particle is $\Lambda_3 = (m^2 M_p)^{1/3}$.

IMPLICATIONS

- ▶ Lower bound on the mass of an isolated light massive spin-2 particle: if $\Lambda_3 \gtrsim 10^{-3}$ eV then $m \gtrsim 10^{-18}$ eV.
- ▶ Large- N QCD: if the lightest glueball has spin 2, then the next lightest state cannot be heavier than Λ_3 .

EXAMPLES

Λ_3 THEORIES: SATURATING THE BOUND

- ▶ Ghost-free bigravity [Hassan & Rosen](#), a generalization of ghost-free massive gravity [de Rham, Gabadadze, & Tolley](#).
- ▶ A gravitationally coupled pseudotensor—no known theory. Uses two-derivative parity-odd vertex and exists only in $4d$.
- ▶ Pseudo-linear theory with massive and massless spin-2 particles (no gravity) [JB, Hinterbichler, & Johnson](#).

EXAMPLES

M_p THEORY

- ▶ If we allow imaginary cubic couplings, i.e. ghosts, then the maximum strong coupling scale is M_p .
- ▶ The unique amplitude is generated by quadratic curvature gravity,

$$S = M_p^2 \int d^4x \sqrt{-g} \left(\frac{1}{2}R + \frac{1}{4m^2}C_{\mu\nu\rho\sigma}C^{\mu\nu\rho\sigma} \right).$$

- ▶ This amplitude is also contained in the bigravity amplitude [Paulos & Tolley](#).

HIGHER-SPIN GENERALISATION

- ▶ **Porrati & Rahman**: for a charged massive spin- s particle the strong coupling scale satisfies

$$\Lambda \leq \frac{m}{q^{1/(2s-1)}}.$$

- ▶ Assume the lightest state satisfies the weak gravity conjecture:

$$q \geq \frac{m}{M_p} \implies \Lambda \leq (m^{2s-2} M_p)^{1/(2s-1)}.$$

CONJECTURE

The maximum strong coupling scale for a gravitationally coupled massive spin- s particle is Λ_{2s-1} **Rahman**.

- ▶ This is true for $s \in \{1, \frac{3}{2}, 2\}$.

CONCLUSIONS

- ▶ Effective field theories of gravitationally coupled massive higher-spin particles can exist, but they have low strong coupling scales.
- ▶ For spin- s , the maximum strong coupling scale is conjectured to be Λ_{2s-1} .
- ▶ We have proven this for $s = 2$ by studying the four-point scattering of massive particles with graviton exchange.

FUTURE DIRECTIONS

OPEN QUESTION

- ▶ Can we raise the cutoff to M_p by adding a finite number of additional particles?
- ▶ This works for $s = \frac{3}{2}$, e.g. addition of scalar and pseudoscalar gives broken $\mathcal{N} = 1$ supergravity.
- ▶ For $s = 2$, we can get to $\Lambda_{3/2} = (mM_p^2)^{1/3}$ with a Kaluza-Klein reduction of $5d$ gravity.