

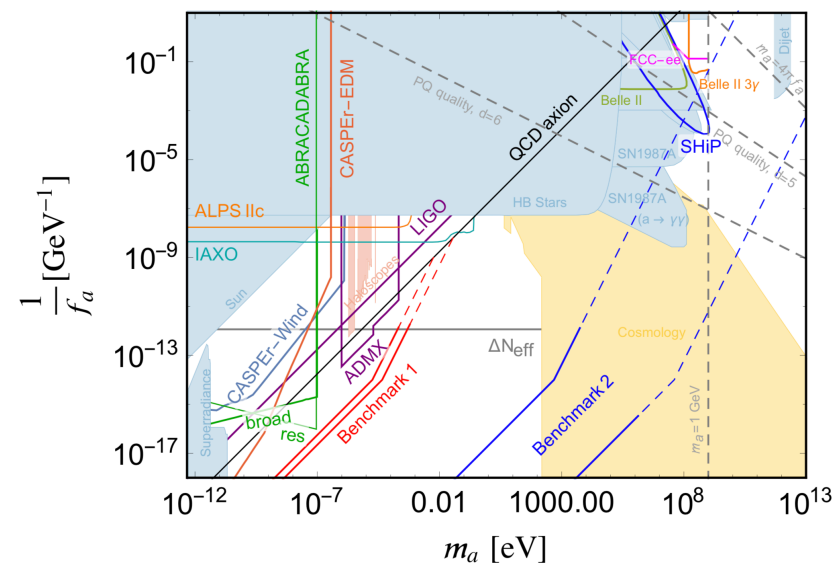
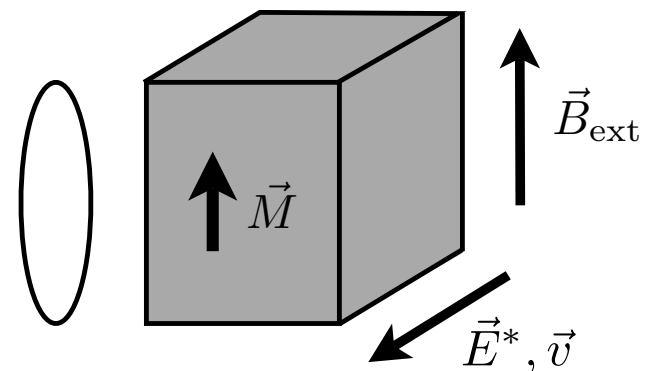
Perspectives on Axions

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SQUID pickup loop



Axion vitals

Mass: sub-eV

Spin: 0

Parity: odd

Charge: 0

Field value: angular



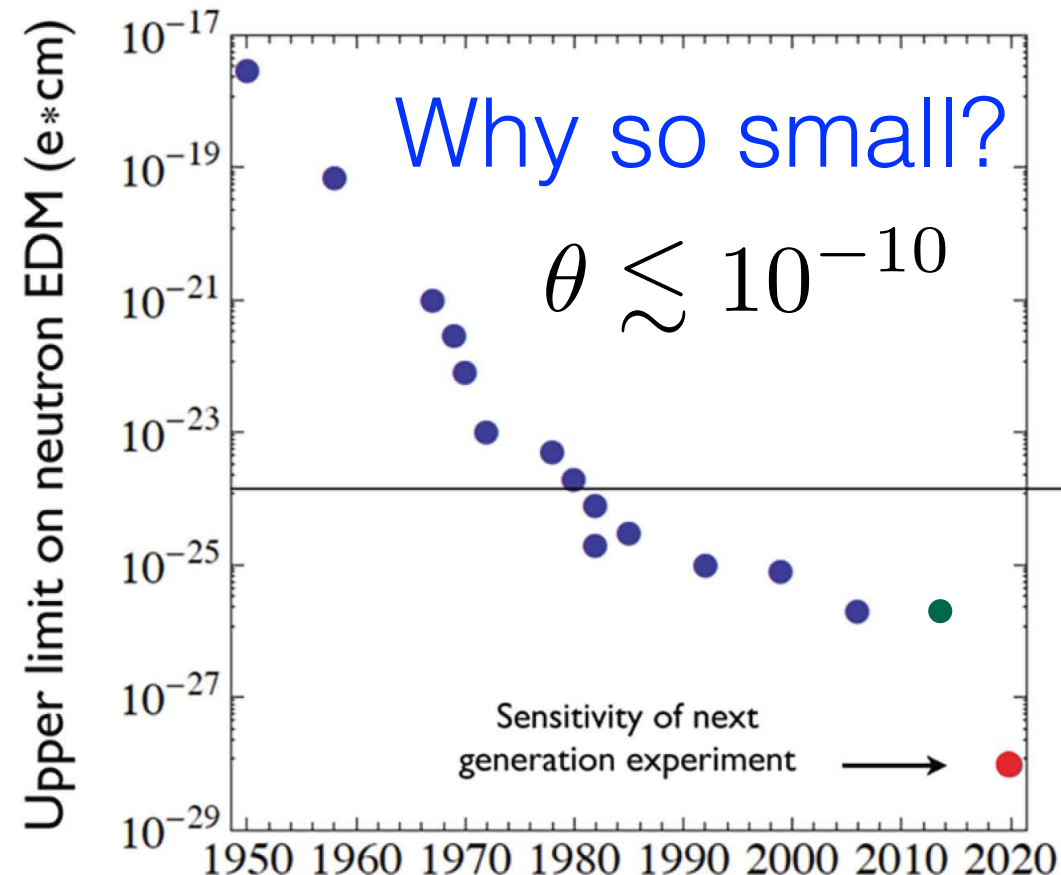
$$a(x^\mu) = f_a \theta(x^\mu)$$

“axion decay constant”
or
“Peccei-Quinn (PQ) scale”

$$\theta \in [-\pi, \pi] \text{ (dimensionless)}$$

Who ordered that?

$$\mathcal{L}_{\text{QCD}} \supset \frac{\theta}{32\pi^2} \text{Tr} G_{\mu\nu} \tilde{G}^{\mu\nu} \quad \longrightarrow \quad d_n \approx 3.6 \times 10^{-16} \theta \text{ e cm}$$



Strong
CP problem
of QCD

Solution: axion dynamically cancels θ

$$\mathcal{L}_{\text{QCD}} \supset \left(\theta - \frac{a}{f_a} \right) \frac{1}{32\pi^2} \text{Tr} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

Axion DM: here and now

$$a(\mathbf{x}, t) = \frac{\sqrt{2\rho_{\text{DM}}}}{m_a} \cos(m_a t + \mathcal{O}(v_{\text{DM}})\mathbf{x})$$

amplitude set by local DM density

oscillates at frequency set by DM mass

e.g. $m_a = 10^{-9}$ eV
 $\lambda_{\text{Comp}} \sim \text{km}$
 $\tau_{\text{Comp}} \sim \mu\text{s}$

Local DM velocity \rightarrow Spatial coherence \rightarrow Temporal coherence

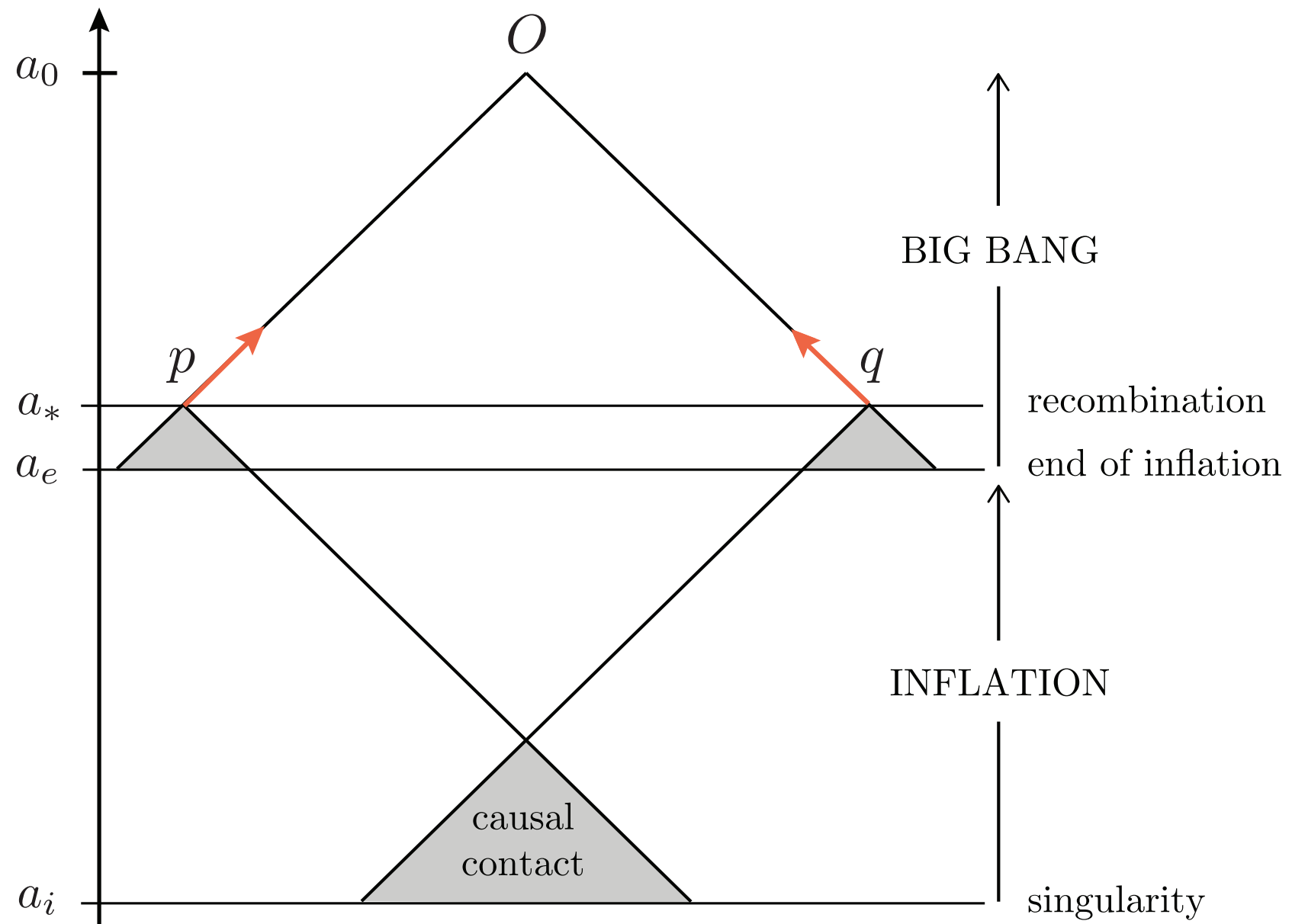
$$\Delta v_{\text{DM}} \sim v_{\text{DM}} \sim 10^{-3} \quad \lambda_{\text{dB}} = \frac{\lambda_{\text{Comp}}}{v_{\text{DM}}} \quad \tau_{\text{coh}} = \frac{\tau_{\text{Comp}}}{v_{\text{DM}}^2}$$

Experiments can exploit enhanced coherence time

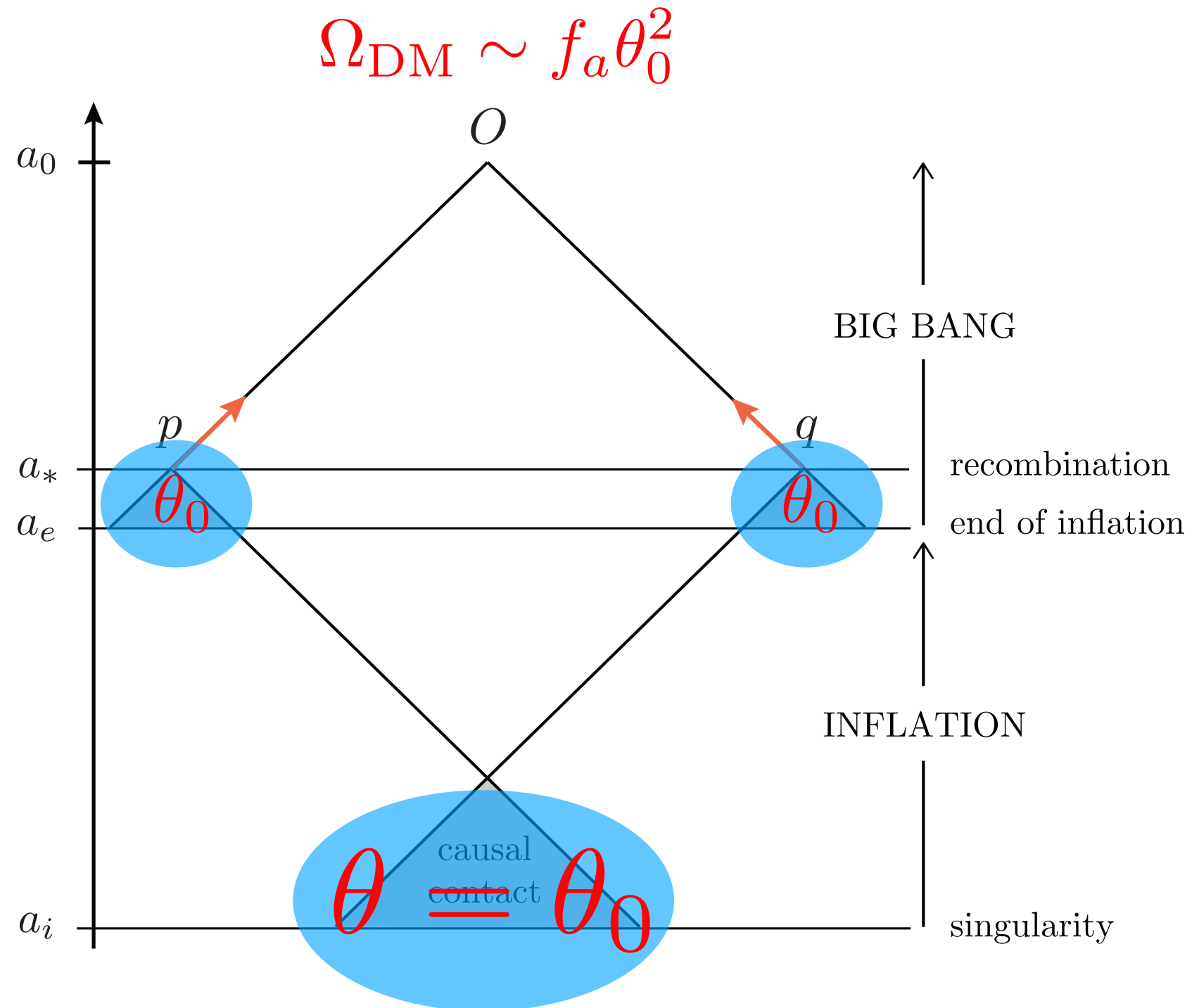
Perspective #0:
Everything I'm going to
say has caveats.
(c.f. WIMP does not mean
mSUGRA neutralino)

Perspective #1:
Axions can teach us a lot
about cosmology
and astrophysics

Two scenarios for PQ breaking

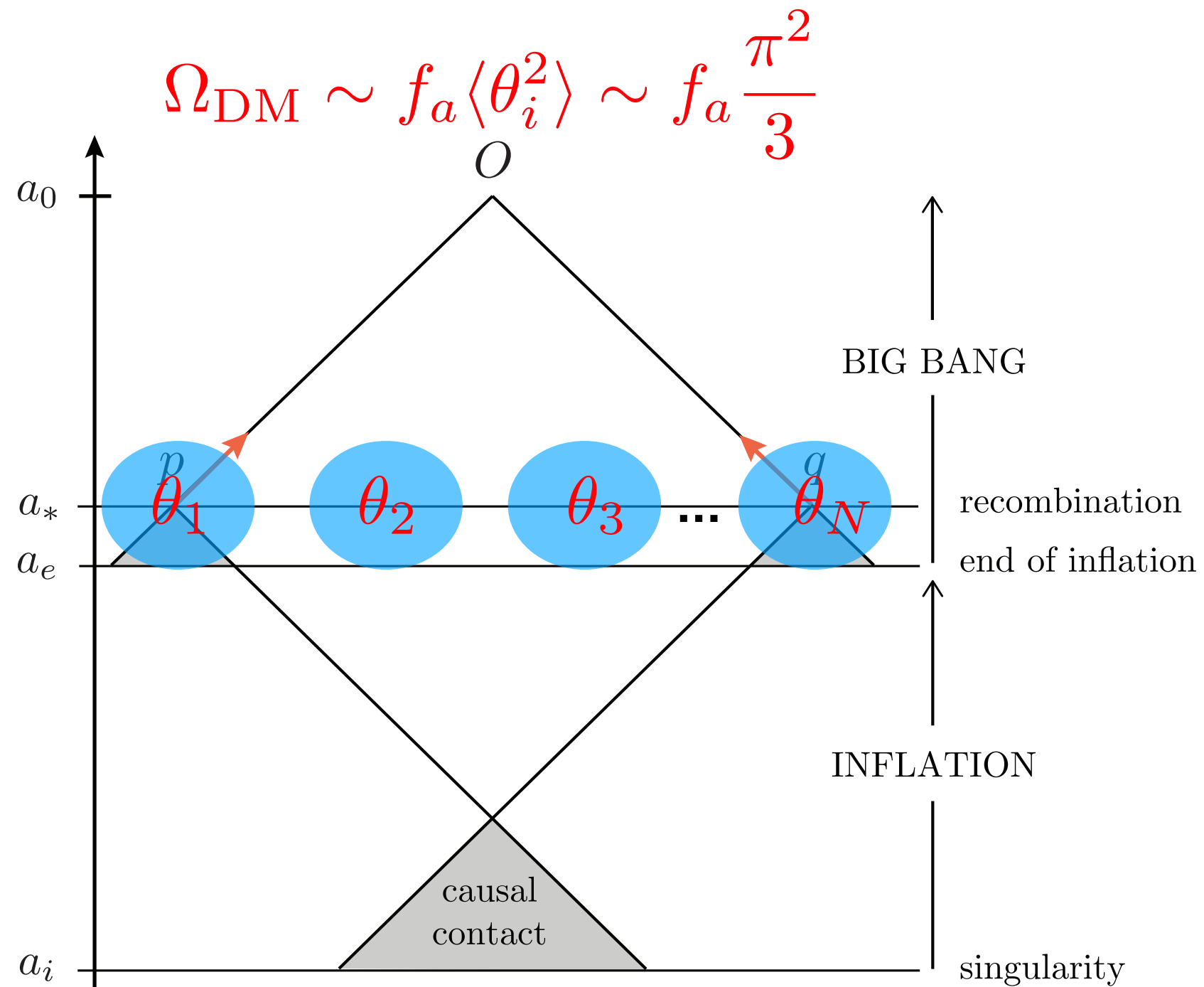


Two scenarios for PQ breaking



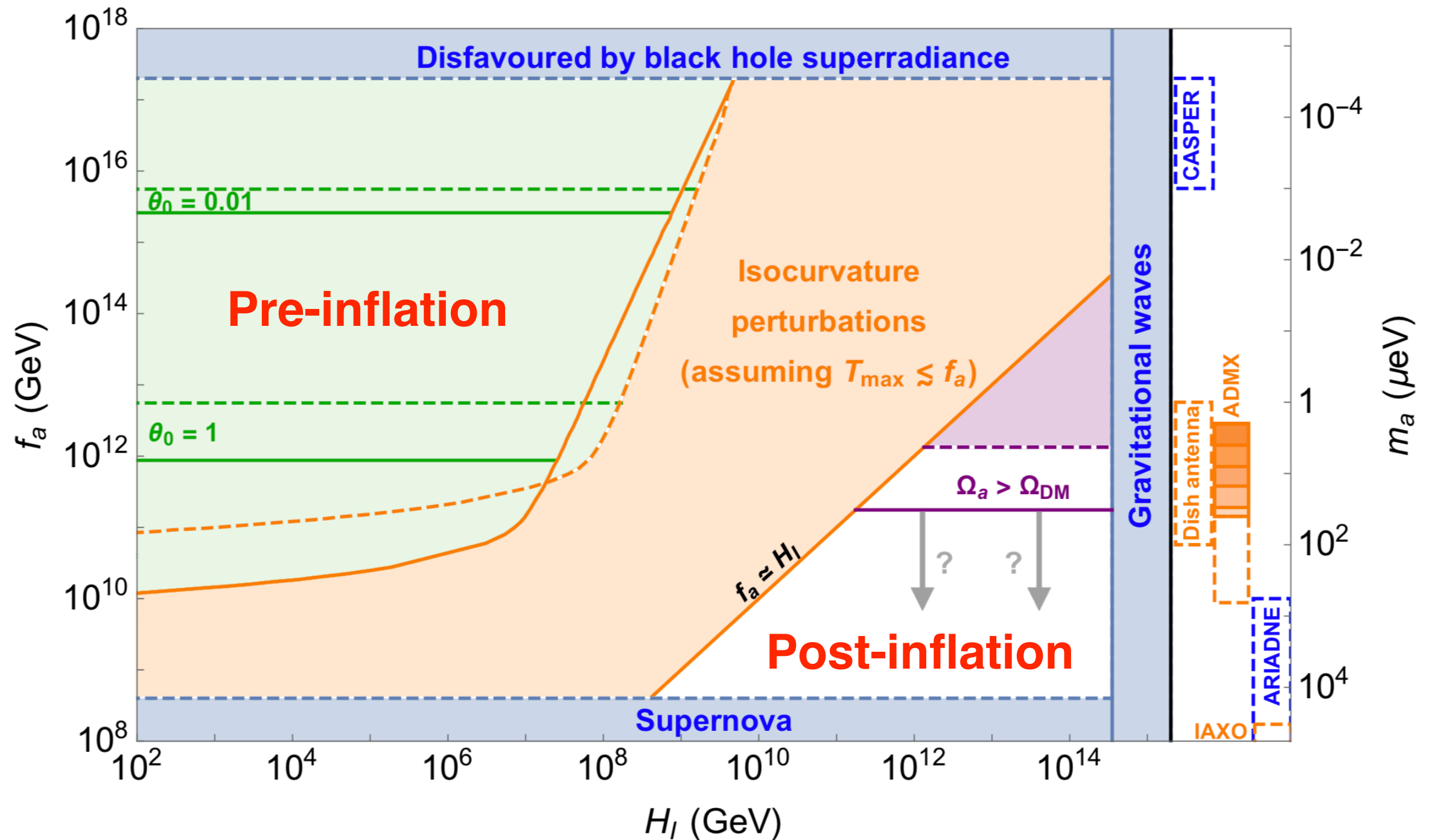
$f_a > H_I, T_R$: pre-inflation, **two** free params for relic density

Two scenarios for PQ breaking



$f_a < H_I$: post-inflation, **one** free param. for relic density

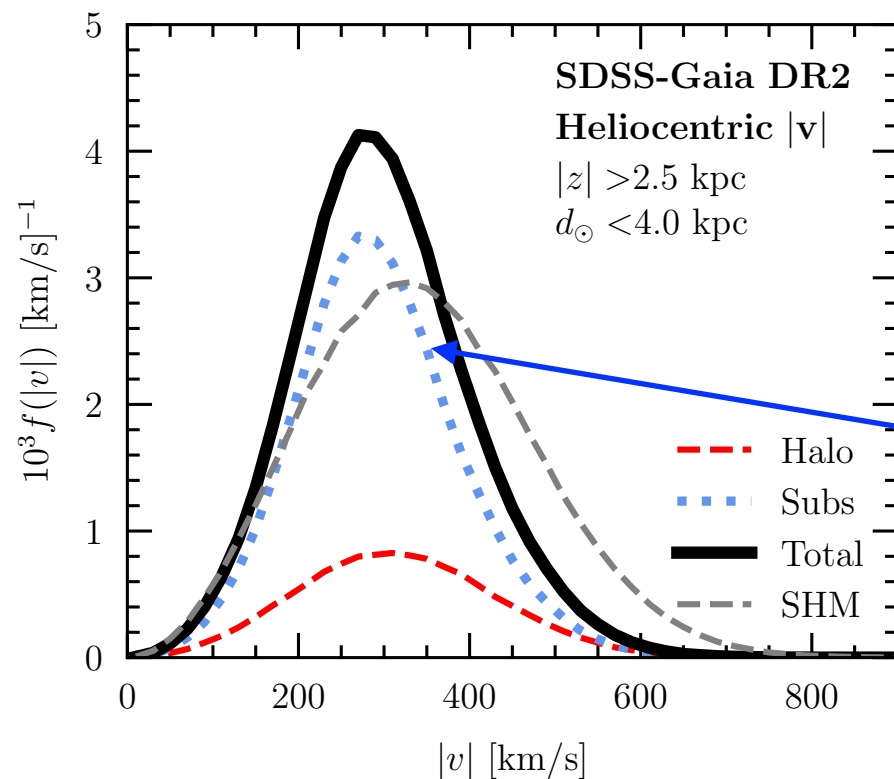
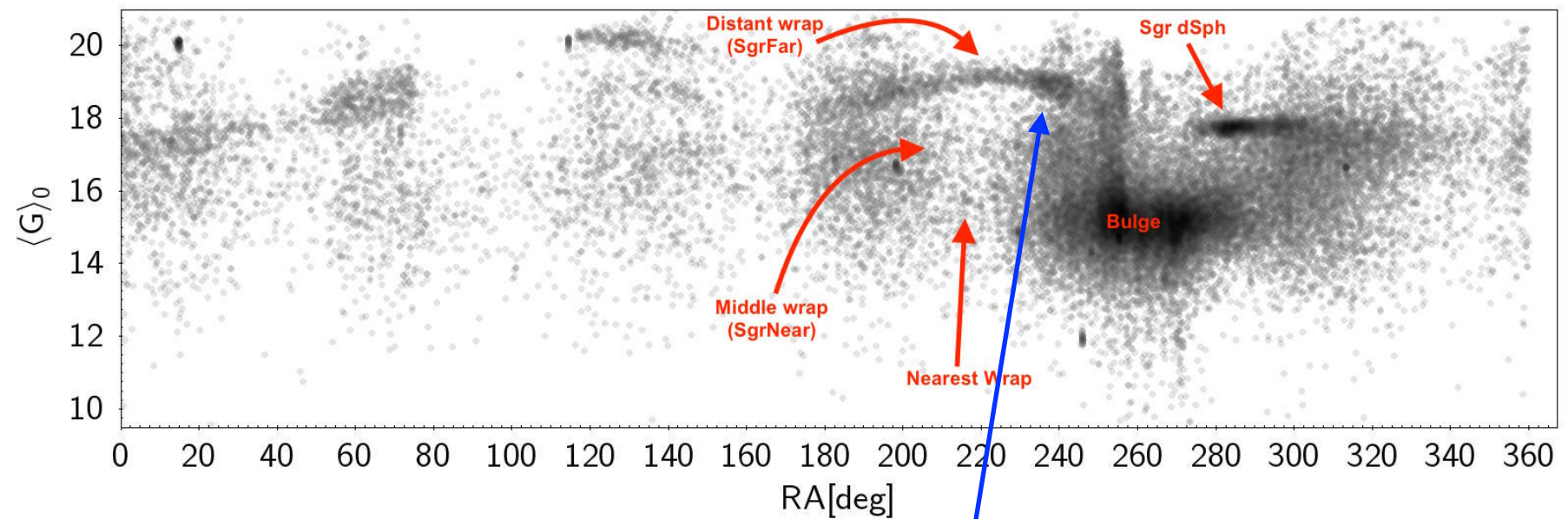
Axions and inflation



Axion DM discovery implies low/high inflation scale!

Dark matter substructure

Milky Way halo is not smooth!



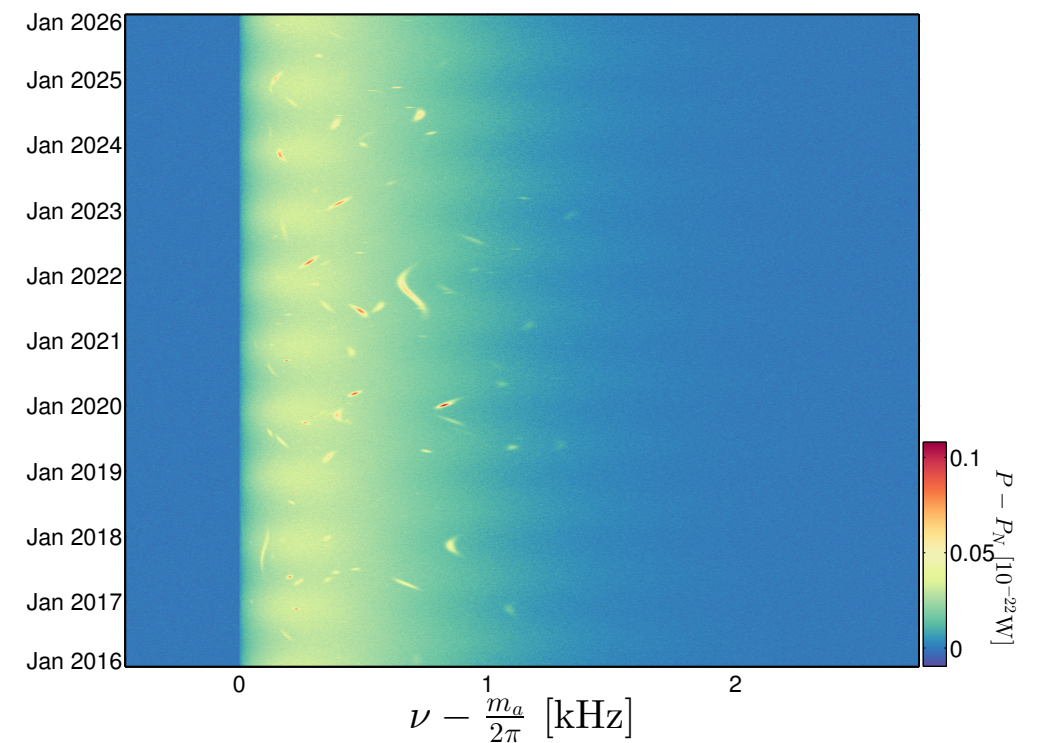
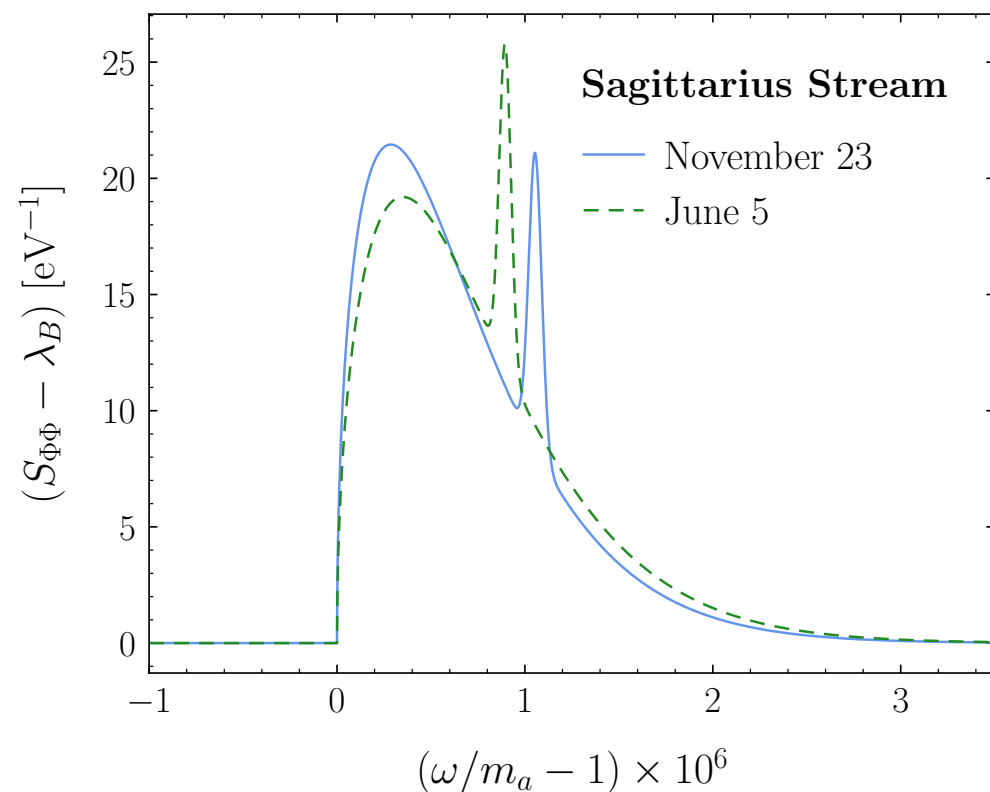
If DM follows stream stars, could have **very** narrow dispersion

substructure has smaller dispersion

Axion “halometry”

$$a(t) = \frac{\sqrt{2\rho_{\text{DM}}}}{m_a} \int d^3\mathbf{v} g(\mathbf{v}) \cos(\omega_{\mathbf{v}}(t - \mathbf{v} \cdot \mathbf{x}))$$

$$\omega_{\mathbf{v}} = m_a \left(1 + \frac{1}{2} v^2 + \mathcal{O}(v^4) \right)$$



Broadband-type (e.g. ABRACADABRA)

Resonant-type (e.g. ADMX)

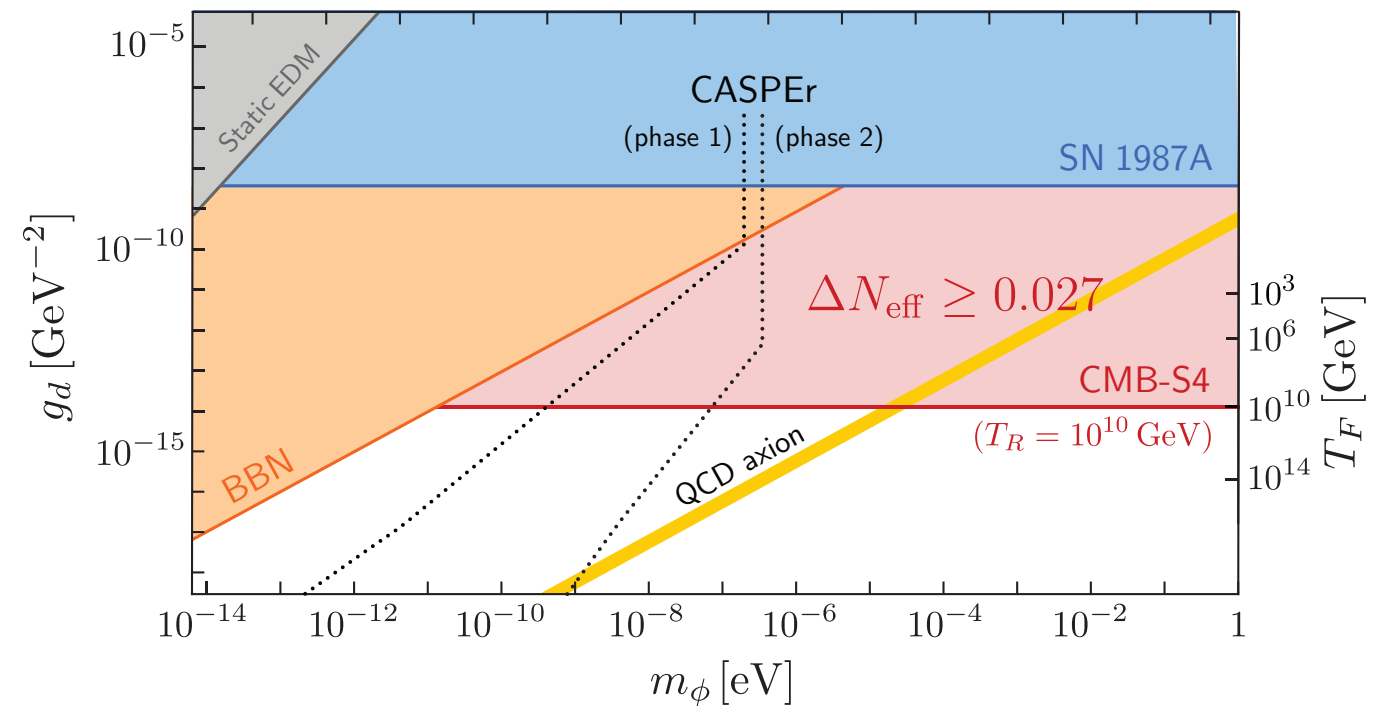
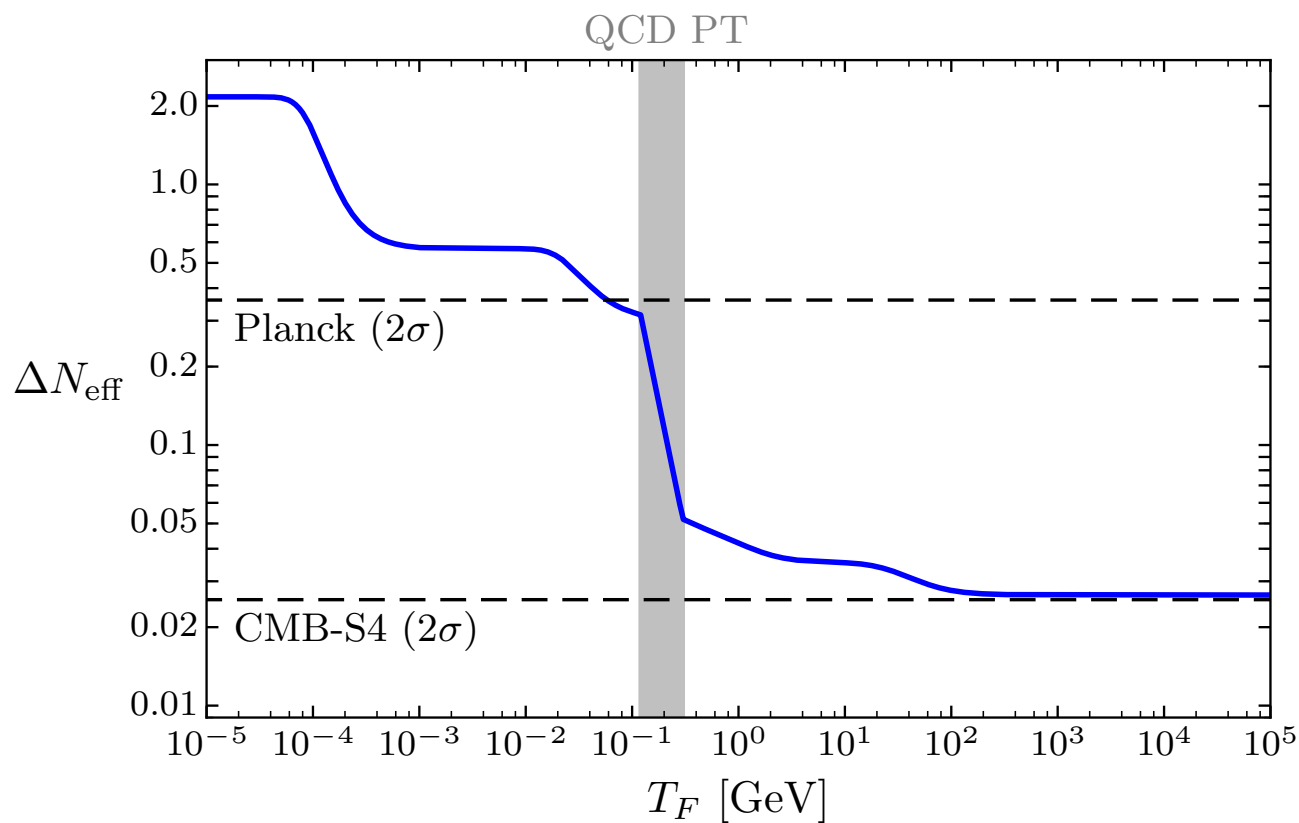
Much easier to identify structure in $g(\mathbf{v})$ for axions than WIMPS

Axions and reheating

If reheat temperature is too high, axions thermalize and contribute to N_{eff} :

decays to gluons

$$\frac{T_F^3}{f_a^2} \sim \frac{\pi}{\sqrt{90}} \sqrt{g_{*,R}} \frac{T_F^2}{M_{\text{pl}}}$$



Axion discovery + null CMB-S4 implies upper bound on T_R !

Perspective #2:
We will reach the QCD
target for the axion-photon
coupling in 20-30 years

Axion DM modifies Maxwell

Generic coupling to E+M:

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

In presence of **static** background EM fields,
induces **oscillating** response fields:

$$\nabla \times \mathbf{B}_r = \frac{\partial \mathbf{E}_r}{\partial t} - g_{a\gamma\gamma} \left(\mathbf{E}_0 \times \cancel{\nabla} a - \mathbf{B}_0 \frac{\partial a}{\partial t} \right)$$

$$\nabla \cdot \mathbf{E}_r = -g_{a\gamma\gamma} \mathbf{B}_0 \cdot \cancel{\nabla} a$$

gradients suppressed by $v_{DM} \sim 10^{-3}$

Axion-photon searches

$$\underbrace{\nabla \times \mathbf{B}_r}_{\text{Cavity regime}} = \frac{\partial \mathbf{E}_r}{\partial t} + g_{a\gamma\gamma} \mathbf{B}_0 \frac{\partial a}{\partial t}$$

Cavity regime: $\lambda_{\text{Comp}} \sim R_{\text{exp}}$
ADMX

$$\nabla \times \mathbf{B}_r = \cancel{\frac{\partial \mathbf{E}_r}{\partial t}} + g_{a\gamma\gamma} \underbrace{\mathbf{B}_0 \frac{\partial a}{\partial t}}_{\mathbf{J}_{\text{eff}}}$$

Quasistatic regime: $\lambda_{\text{Comp}} \gg R_{\text{exp}}$
ABRACADBRA

$$\cancel{\nabla \times \mathbf{B}_r} = \frac{\partial \mathbf{E}_r}{\partial t} + g_{a\gamma\gamma} \mathbf{B}_0 \frac{\partial a}{\partial t}$$

Radiation regime: $\lambda_{\text{Comp}} \ll R_{\text{exp}}$
MADMAX

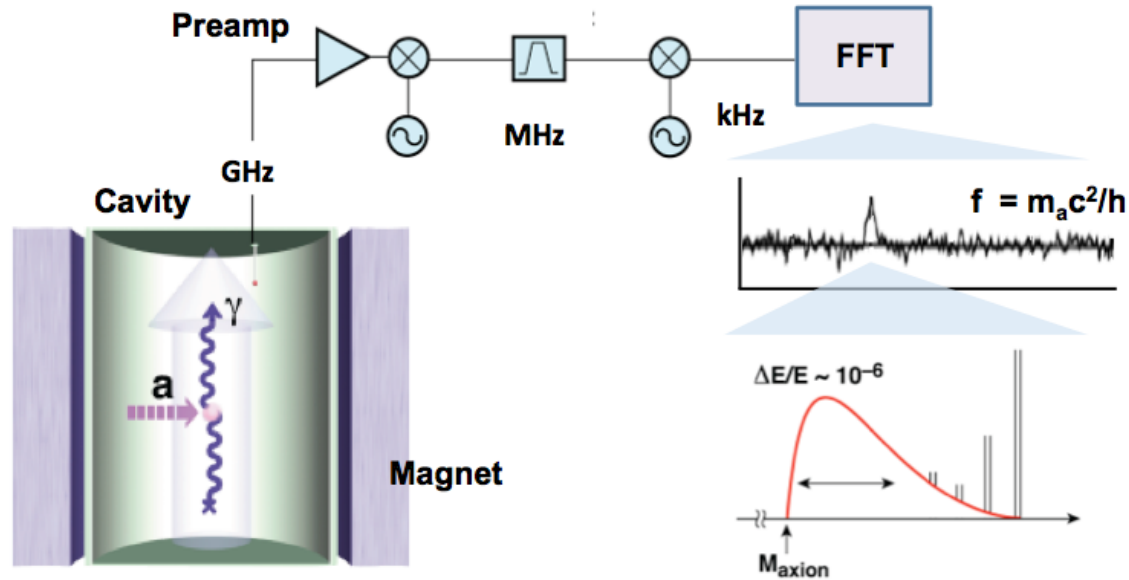
ADMX: resonant cavity detection

$$\nabla \times \mathbf{B}_r = \frac{\partial \mathbf{E}_r}{\partial t} + g_{a\gamma\gamma} \mathbf{B}_0 \frac{\partial a}{\partial t}$$

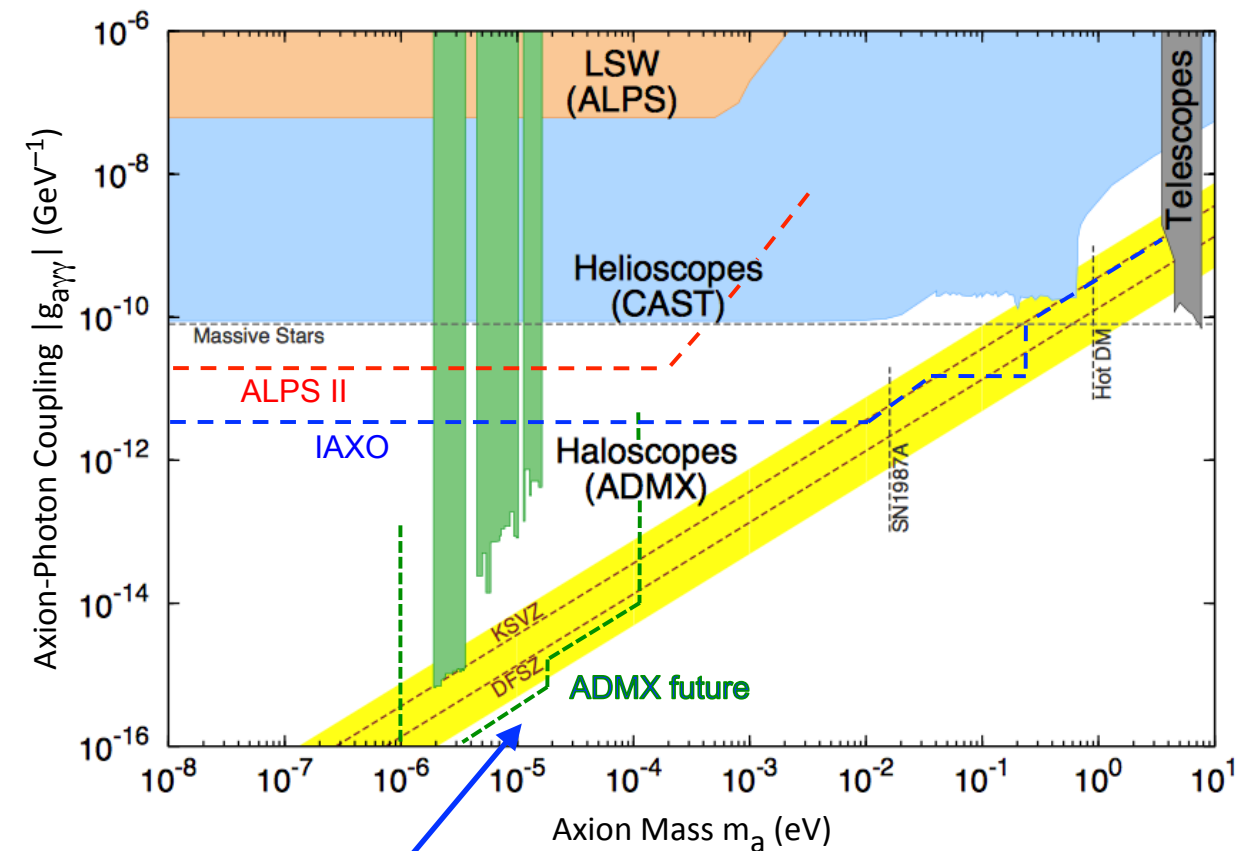
cavity response

axion source

$$P \sim g_{a\gamma\gamma}^2 \frac{\rho_{\text{DM}}}{m_a} B_0^2 V Q$$



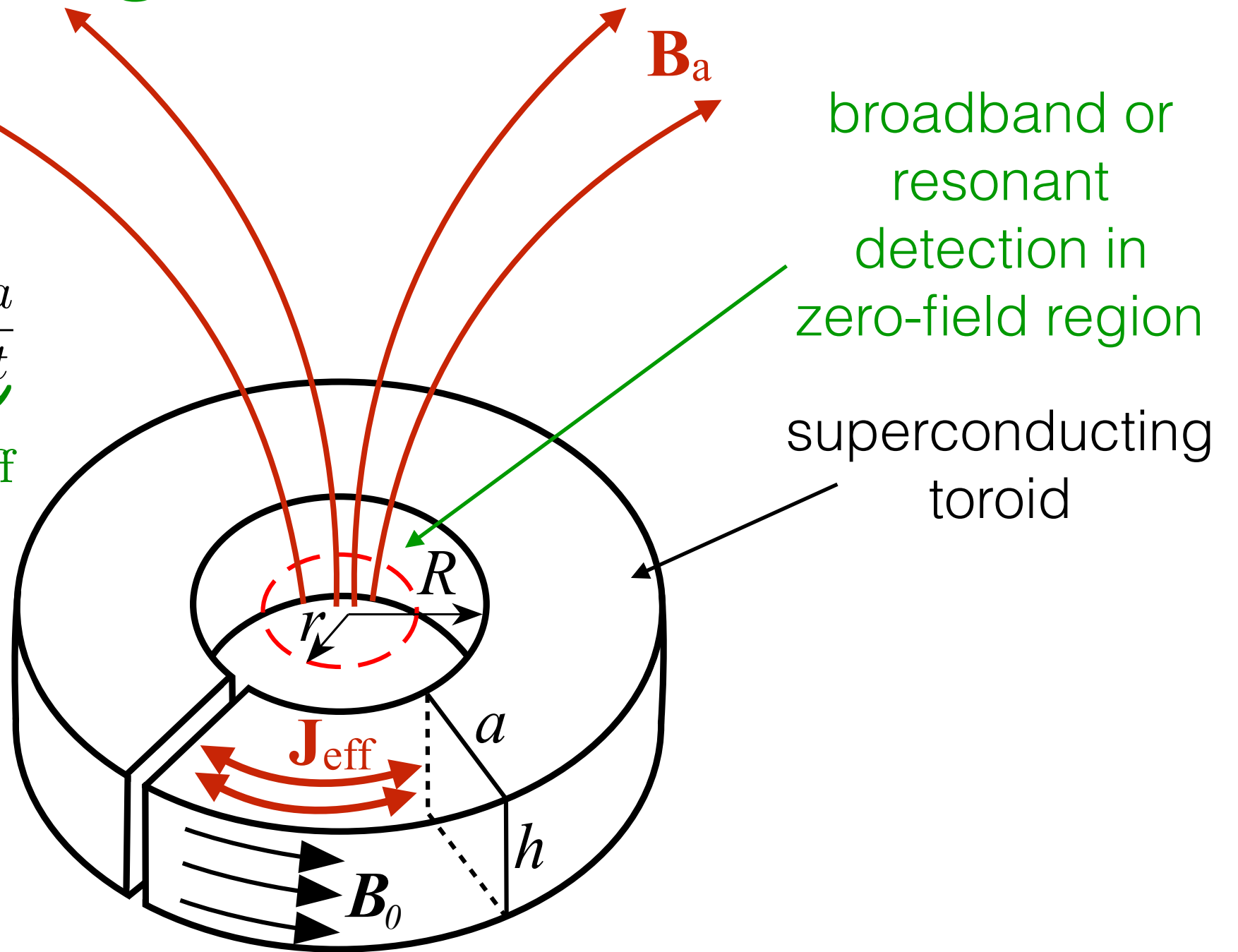
Tune cavity modes to scan axion masses



Cavity b.c. fix mass range to cavity size; larger masses -> smaller V

Quasistatic regime: ABRACADABRA

$$\nabla \times \mathbf{B}_r = \cancel{\frac{\partial \mathbf{E}_r}{\partial t}} + \underbrace{g_{a\gamma\gamma} \mathbf{B}_0 \frac{\partial a}{\partial t}}_{\mathbf{J}_{\text{eff}}}$$



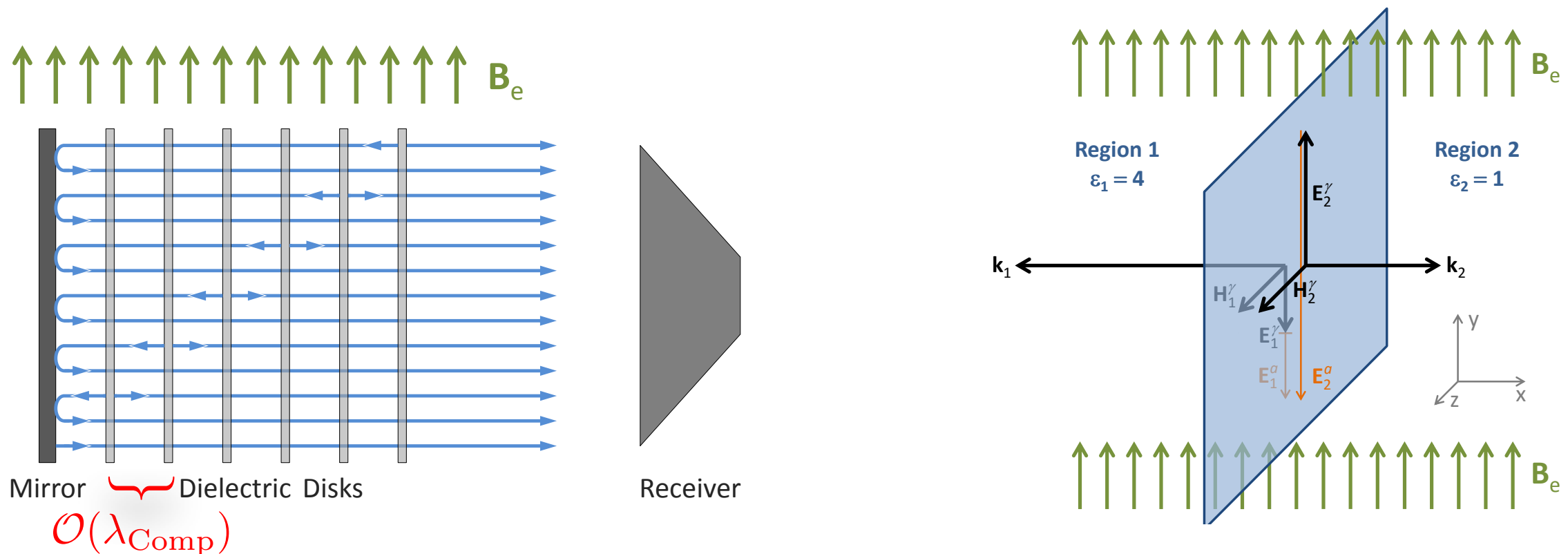
$$\Phi_a(t) = g_{a\gamma\gamma} \sqrt{2\rho_{\text{DM}}} \cos(m_a t) \times (B_{\text{max}} V G_{\text{toroid}})$$

Volume enhancement: B-field energy scales as $B_0^2 V^2$

Radiation regime: MADMAX

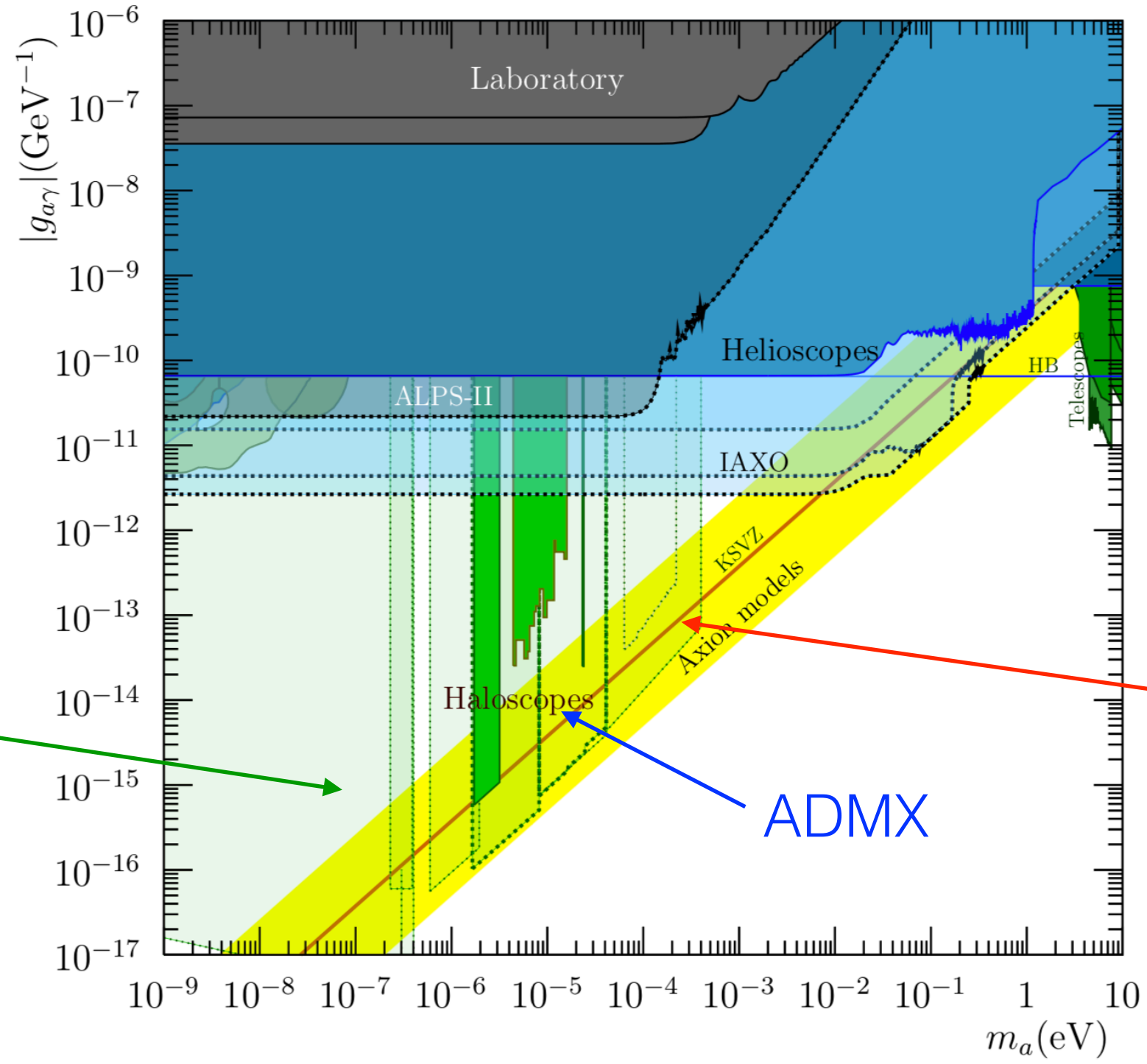
$$\nabla \times \mathbf{B}_r = \epsilon \frac{\partial \mathbf{E}_r}{\partial t} + g_{a\gamma\gamma} \mathbf{B}_0 \frac{\partial a}{\partial t} \implies \mathbf{D}_r(t) = \epsilon \mathbf{E}_r(t) = -g_{a\gamma\gamma} \mathbf{B}_0 a(t)$$

E+M boundary condition at interfaces forces
radiation to cancel axion-induced **D**

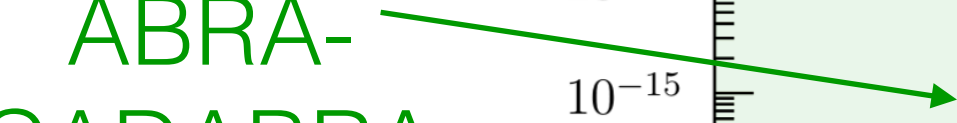


Best of both worlds: **large volume** and **high Q**

Axion-photon coupling: the future



ABRA-CADABRA



ADMX

MADMAX

Perspective #3:
The QCD target is
not the end of the game!

Line vs. band

For the “canonical” QCD axion:

$$\mathcal{L} \supset \frac{a}{f_a} G_{\mu\nu} \tilde{G}^{\mu\nu} \implies d_n^{\text{QCD}} \approx 2.4 \times 10^{-16} \frac{a}{f_a} e \cdot \text{cm} \quad \text{no wiggle room!}$$

But photon coupling depends on UV completion

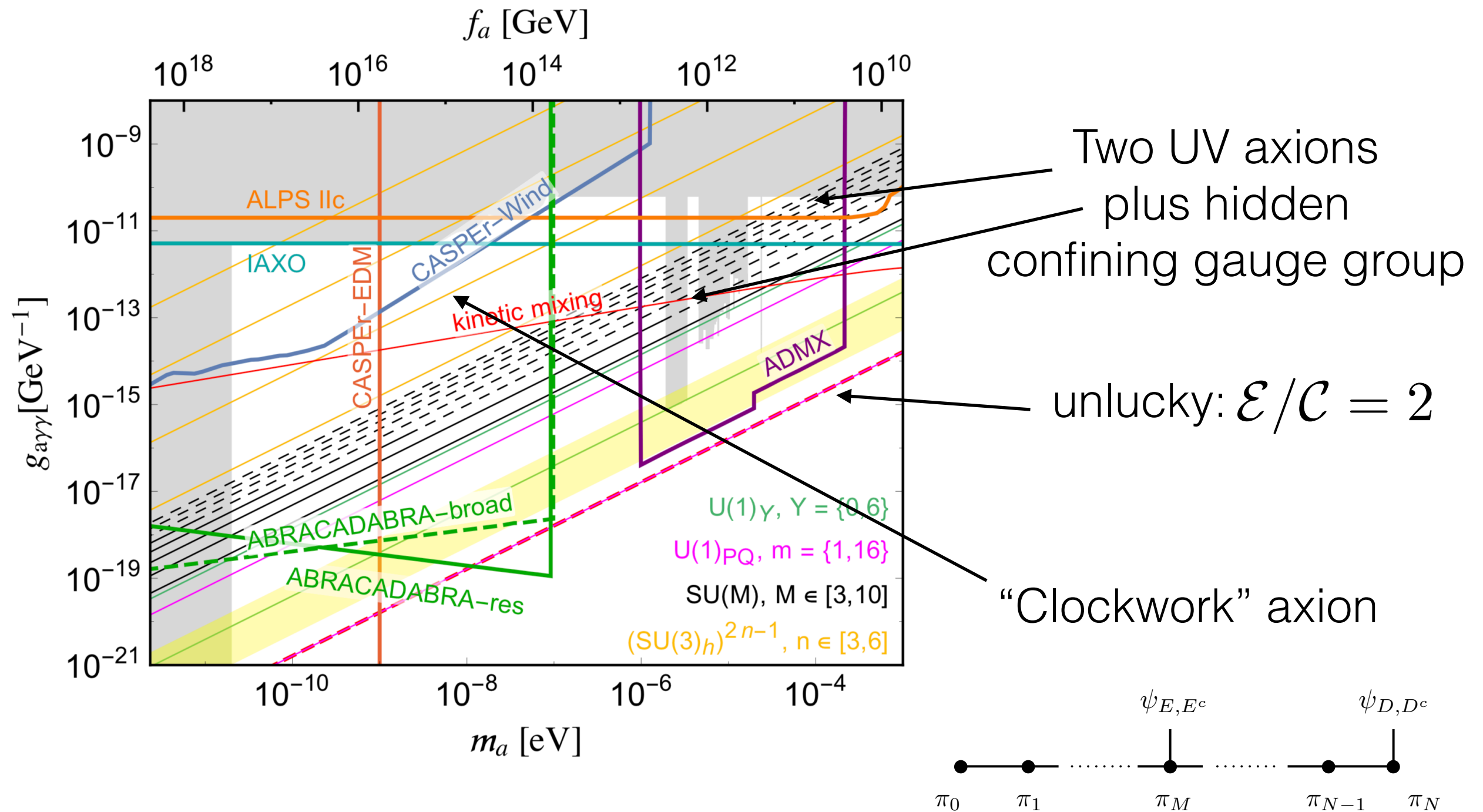
$$\varphi = \sigma e^{ia/f_a} \quad \mathcal{L}_{\text{KSVZ}} \supset \varphi \bar{Q}_L Q_R \quad \mathcal{L}_{\text{DFSZ}} \supset \varphi^2 H_u H_d$$

$$g_{a\gamma\gamma} = \frac{\alpha_{\text{EM}}}{2\pi f_a} \times \left(\frac{\mathcal{E}}{\mathcal{C}} - 1.92(4) \right)$$

EM anomaly, color anomaly: integers

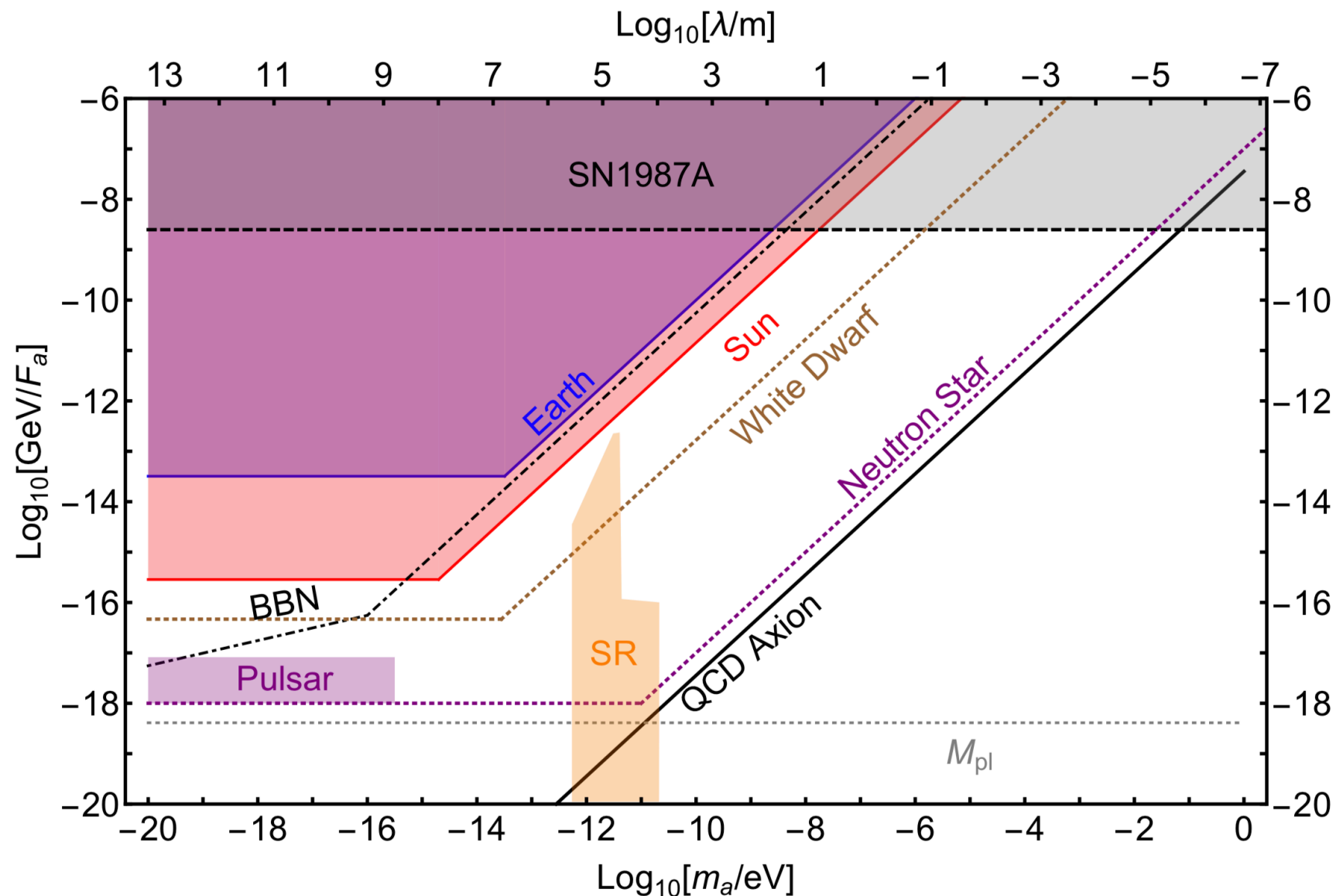
Range of possible values depending on PQ charges

Living off the band (photons)

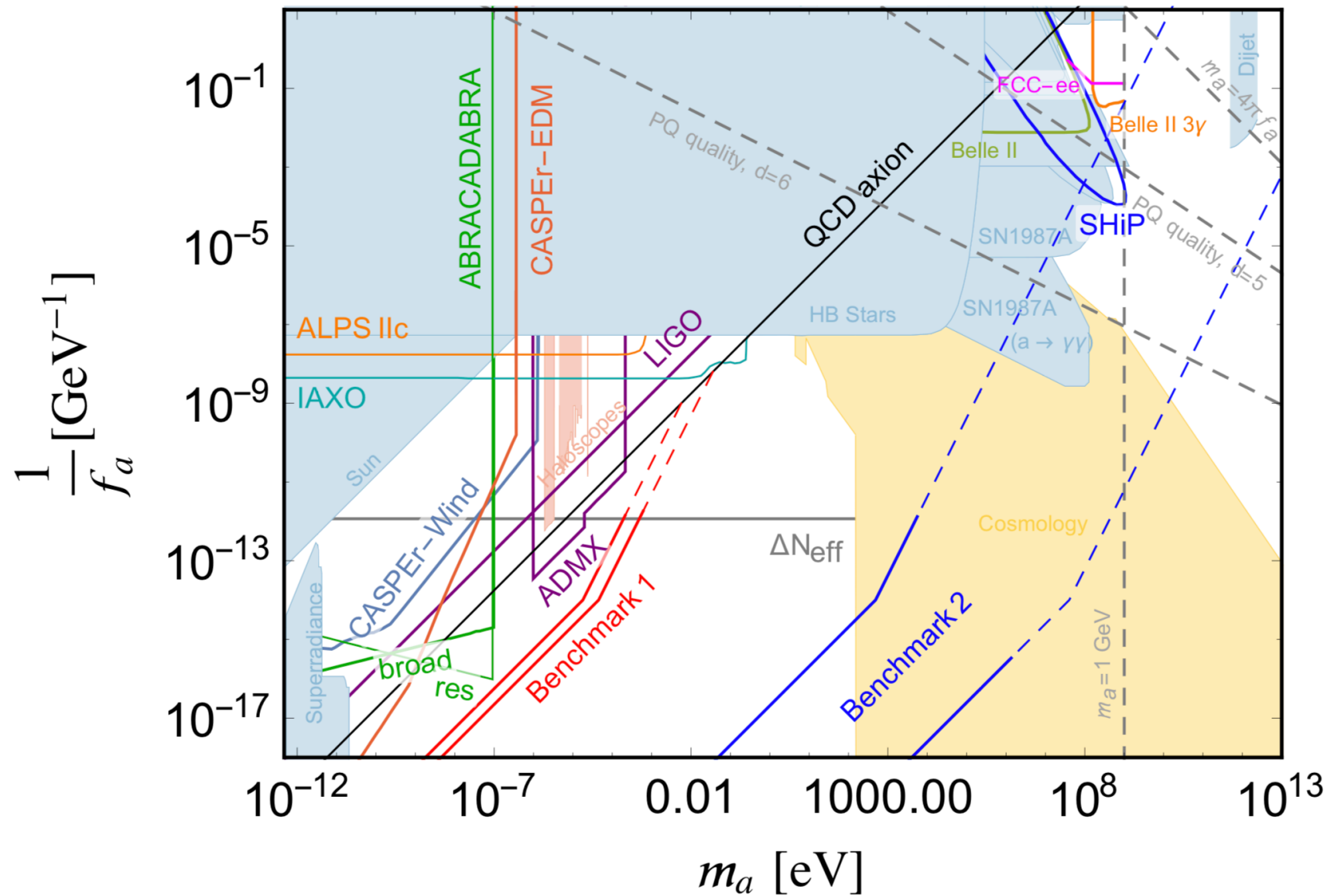


Living above the line (nEDM)...

N copies of QCD: $\mathcal{L} = \sum_k \left(\frac{a}{f_a} + \frac{2\pi k}{N} + \theta \right) G_k \tilde{G}_k \implies \frac{m_a(N)}{m_a(N=1)} \sim \frac{4}{2^{N/2}}$



...or below the line (nEDM)



$$SU(3)_1 \times SU(3)_2 \rightarrow SU(3)_c$$

$$\Rightarrow \mathcal{L} \supset \Lambda_1^4 \cos(a_1/f_1 - \bar{\theta}_1) + \Lambda_2^4 \cos(a_2/f_2 - \bar{\theta}_2)$$

Instanton effects can make
 $\Lambda_1, \Lambda_2 \gg \Lambda_{\text{QCD}}$

\Rightarrow **heavy axion**

Perspective #4:
Looking for the nEDM
coupling for axion dark matter
is **really** hard

Comparing EM response

$$\frac{a}{f_a} G_{\mu\nu} \tilde{G}^{\mu\nu} \implies \frac{i}{2} g_d a \underbrace{\bar{N} \sigma_{\mu\nu} \gamma_5 N}_{\text{magnetization/polarization tensor}} F^{\mu\nu} - \frac{1}{4} g_{a\gamma\gamma} F_{\mu\nu} F^{\mu\nu}$$

NR limit in medium: $\mathbf{P} = n_n \kappa_p \epsilon_S d(t)$

$\mathbf{J}_{\text{eff}} = g_{a\gamma\gamma} \mathbf{B}_0 \partial a / \partial t$

$\mathbf{D} \equiv \mathbf{E} + \mathbf{P}$

$\nabla \cdot \mathbf{D} \implies \mathbf{E}_{\text{EDM}}$

$\partial \mathbf{D} / \partial t \implies \mathbf{B}_{\text{EDM}}$

bounded by
atomic physics

unrealistically
large

$$\frac{\mathbf{B}_{\text{EDM}}}{\mathbf{B}_{a\gamma\gamma}} = 10^{-4} \times \left(\frac{n_n}{10^{22} \text{ cm}^{-3}} \right) \left(\frac{B_0}{10 \text{ T}} \right) \left(\frac{\epsilon_S \kappa_p}{1} \right)$$

The NMR loophole

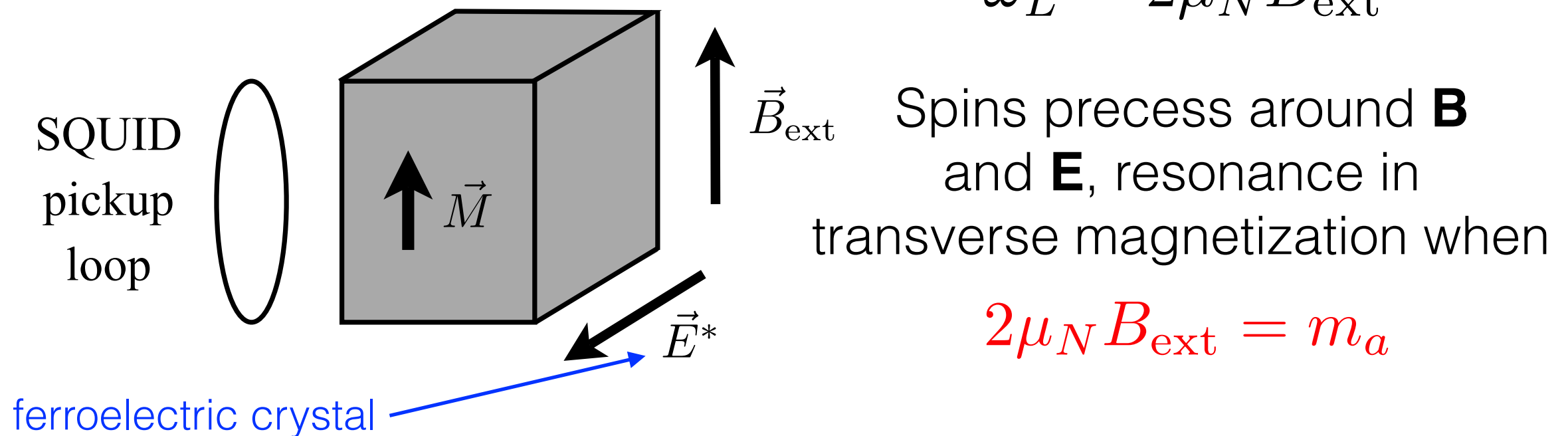
Previous argument based on Maxwell only...
but Dirac told us how spins couple to EM fields

$$H = \epsilon_S \mathbf{d}_n(t) \cdot \mathbf{E}^* \leftrightarrow \mu_N \cdot \mathbf{B}_\perp(t)$$

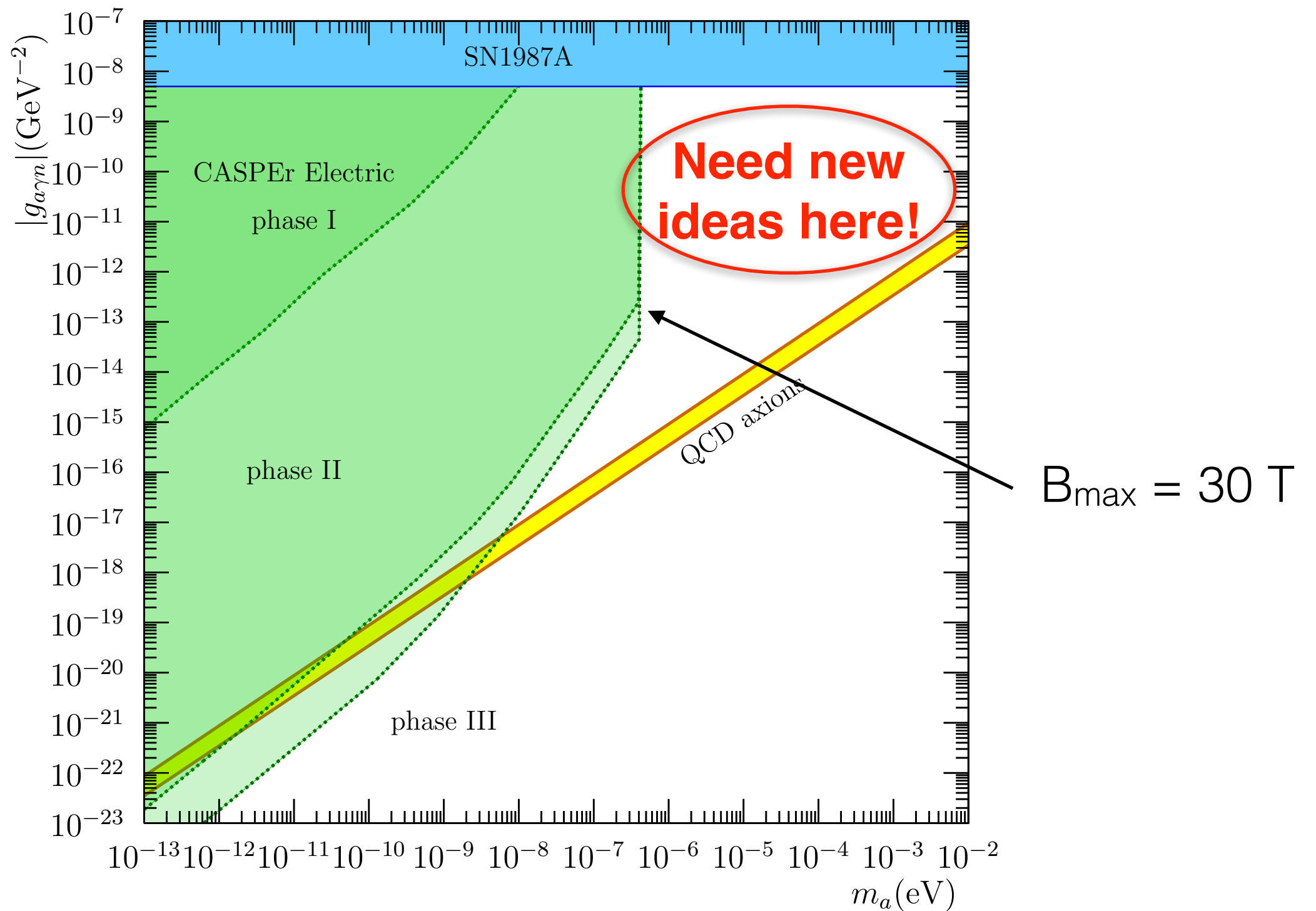
oscillates at $\omega = m_a$

Larmor oscillations:

$$\omega_L = 2\mu_N B_{\text{ext}}$$



nEDM parameter space



Closing thoughts

- There is a clear parameter space target for the QCD axion, at least as well-motivated (in a Bayesian sense) as the canonical SUSY WIMP
- An **exclusion** of all or part of this parameter space would be great - but it wouldn't rule out axions!
- If we are lucky enough to **discover** axion DM, the prospects for learning more about inflation, DM halo, and the thermal history of our universe are even better than for the WIMP
- **Many more experiments in the coming years!**

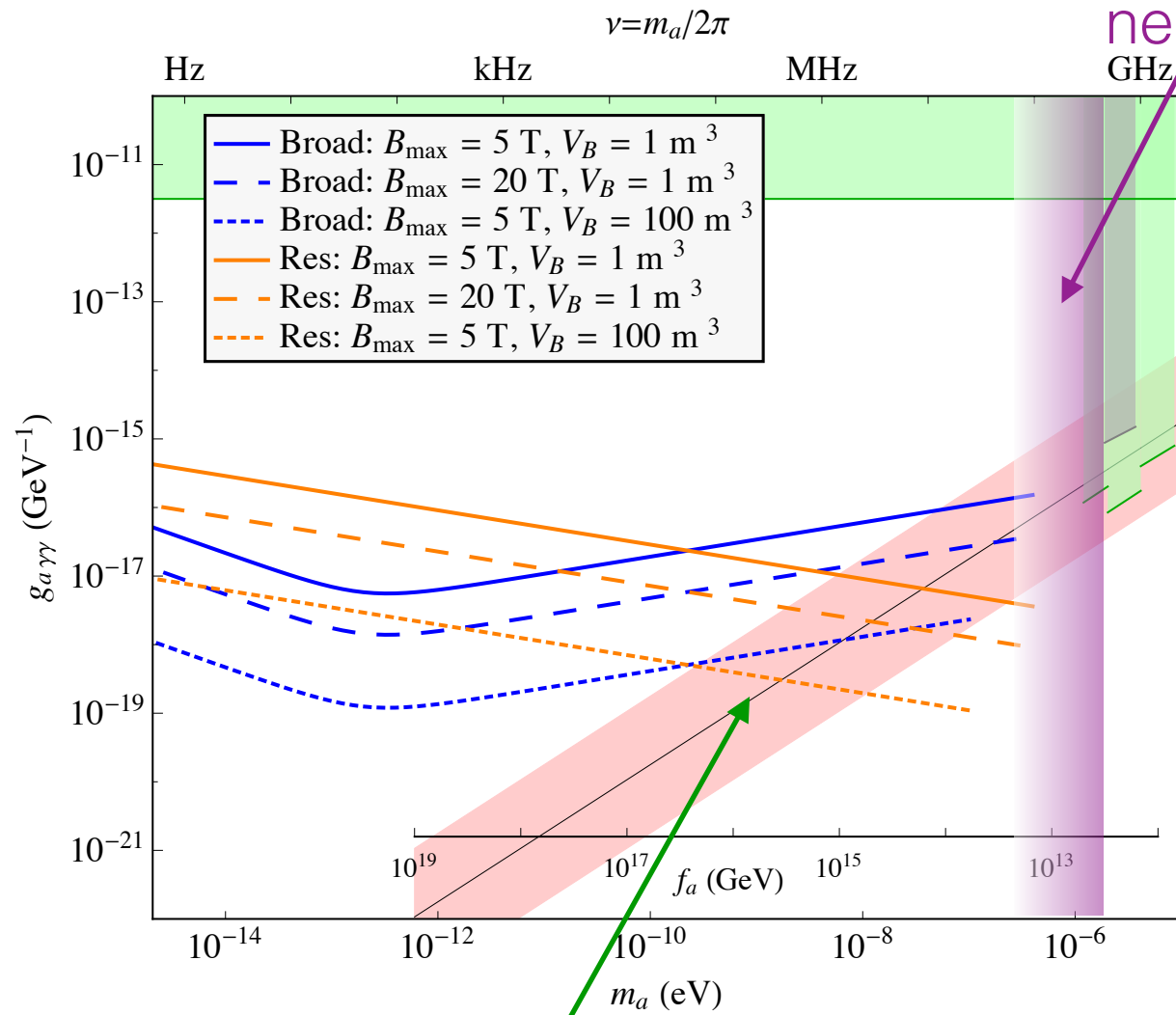
Backup Slides

ABRACADABRA reach

ABRA-10cm prototype:

Full-scale reach:

QS breaks down
(detailed sim. needed)



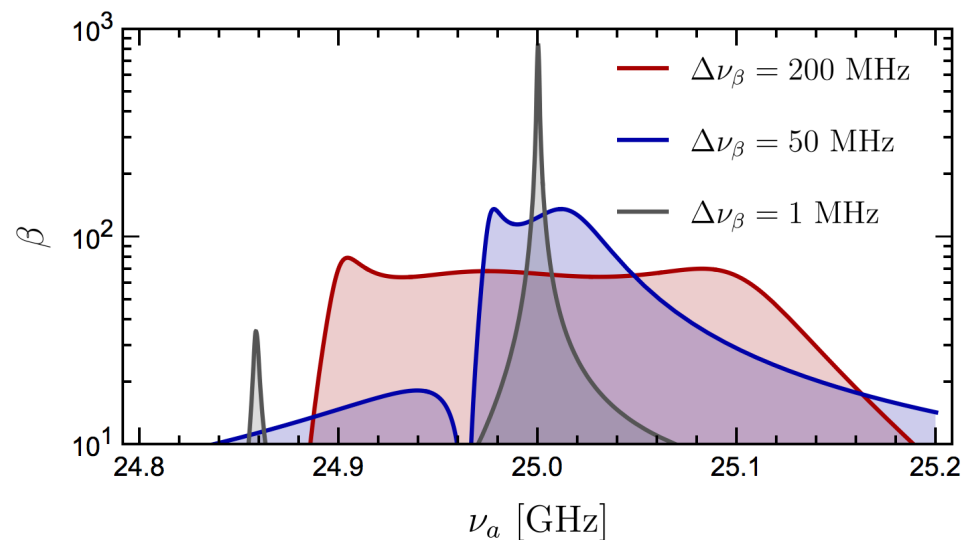
QCD axion



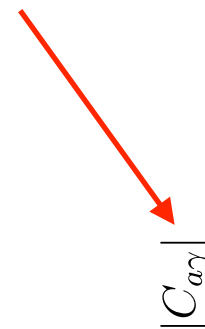
Data being analyzed now - stay tuned!

MADMAX reach

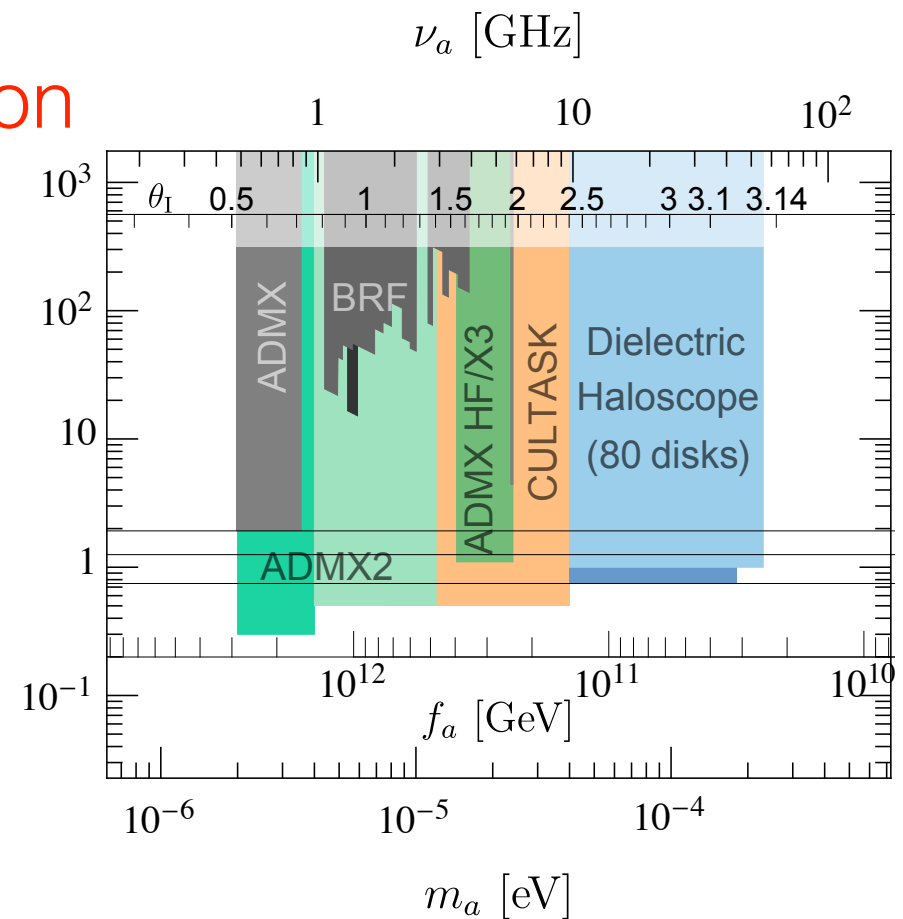
Broadband and resonant modes possible:



=1 if
QCD axion



3-year runtime:

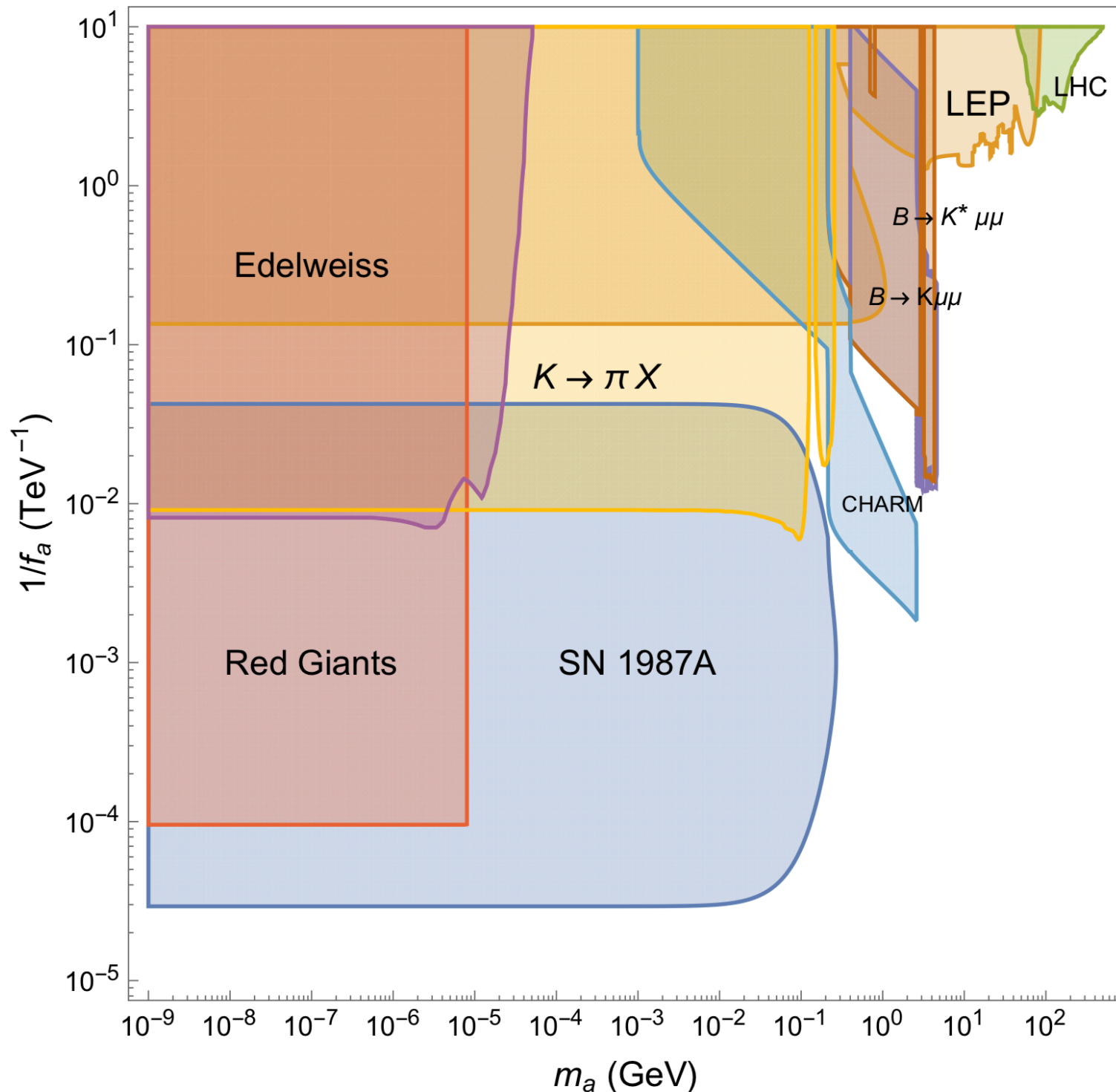


$$P \propto g_{a\gamma\gamma}^2 \rho_{\text{DM}} B_0^2 A \beta^2$$

$$\int \beta(\nu_a)^2 d\nu_a = N_{\text{disks}} \times \text{const.}$$

Excellent prospects
in high-frequency regime

Photophobic ALP



Left-right symmetry:

$$\mathcal{L} \supset \frac{a}{f_a} (W_R \widetilde{W}_R - W_L \widetilde{W}_L)$$

IR coupling to photons
only at **two loops** and/or
suppressed by axion mass

Note: NOT
the QCD axion!
No coupling to gluons